

AN ASSET FOUNDATION MODEL FOR INDUSTRIAL ASSET PERFORMANCE MANAGEMENT

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ABSTRACT

011 We introduce the asset foundation model (AFM), a generative framework for asset
 012 performance management (APM) spanning high-value industrial assets and man-
 013 ufacturing processes. The AFM is applicable across sectors such as energy, chem-
 014 icals, manufacturing, and utilities by leveraging rich time series data and event
 015 streams to provide a robust basis for next-generation APM solutions. A shared
 016 transformer backbone with lightweight heads supports forecasting, anomaly de-
 017 tection, and event querying. The model is pre-trained on operational and simulator
 018 corpora, then fine-tuned on asset-specific histories for minimal effort adaptation,
 019 using per-sensor discrete tokenization for robustness. Beyond sensors, the AFM
 020 incorporates alarms, set-point changes, and maintenance logs via event tokens, en-
 021 abling time-aligned “what/when” queries and high value applications such as root
 022 cause triage, alarm suppression, and maintenance planning. In representative field
 023 deployments (e.g., ESPs and compressors), the AFM exceeds prior gains, delivers
 024 earlier warnings, and reduces false alarm minutes. Operator-oriented explanations
 025 based on attention rollout and integrated gradients highlight which sensors/events
 026 drove each alert, while natural language querying allow experts to “talk to the
 027 data” features. Calibrated prediction intervals from discrete to continuous with
 028 isotonic calibration support risk aware thresholds. On the theory side, we prove
 029 closed form bounds on quantization error and a Lipschitz stability result for dis-
 030 cretization noise through the encoder, justifying sample efficient adaptation with
 031 frozen backbones. Field benchmarks corroborate competitive accuracy and cali-
 032 brated coverage. The result is a versatile, scalable, and interpretable foundational
 033 framework with significant business impact on industrial asset management.

1 INTRODUCTION

036 Across large industrial sectors such as energy, chemicals, manufacturing and utilities, asset perfor-
 037 mance management (APM) still wrestles with three compounding problems at scale: excessive false
 038 alarms, slow adaptation to new plants (from onboarding new equipment, processes or regimes), and
 039 bespoke models that do not transfer across sites, leading to downtime and health, safety & envi-
 040 ronmental (HSE) risks, as well as escalating operational and support costs. In practice, threshold
 041 alarms miss subtle degradations, yet overwhelm operators during normal transients, despite estab-
 042 lished alarm-management guidance. Meanwhile, organizations seek cross-asset value under ISO
 043 55000-style asset management goals, but the analytics layer lags behind. The main challenge is
 044 to maximize the value of existing CAPEX-intensive installations through optimization, end-to-end
 045 scenario analysis, and collective intelligence across the value chain (e.g., from reservoir to pipeline
 in an oil and gas setting).

046 The classical asset modeling approaches for APM suffer in multiple fronts and have been shown to
 047 be difficult to scale across assets. Thresholds and one-off machine learning pipelines fail for recur-
 048 ring field reasons: (i) intermittent and uneven data coverage; (ii) asset-specific feature engineering;
 049 (iii) inability to treat alarms/events as first-class signals; (iv) dependence on scarce subject-matter
 050 experts; (v) sensitivity to sensor noise and drift; (vi) poor generalization across sites; (vii) heavy
 051 maintenance overhead; and (viii) high label demands. These realities explain why many “deployed”
 052 systems degrade in months and why alarm KPIs (e.g., floods, chattering, standing alarms) remain
 053 stubbornly off target in real plants. The interpretability of such results, even if they are accurate,
 is questionable. Moreover, querying the right data for the event of interest (i.e., the root causes

054 that have driven such events) is difficult to deduce, which has made the adoption of such predictive
 055 models less widespread.
 056

057 In this work, we build on our previously deployed time-series foundation model (TSFM) for rotating
 058 equipment, and explore an asset foundation model (AFM) for cross-industry APM. The model con-
 059 sists of a shared transformer backbone pretrained on operational and simulator corpora, fine-tuned
 060 with minimal effort on asset histories; lightweight heads support forecasting, anomaly detection, and
 061 event querying; and per-sensor discrete tokenization improves robustness and sequence modeling.
 062 The AFM maintains a fit-for-purpose stance and explicitly extends beyond rotating equipment to
 063 process units and multi-site fleets.
 064

065 Beyond sensors, the AFM ingests alarms, set-point changes, and maintenance logs as time-aligned
 066 event tokens, enabling “what/when” queries and powering high-value operator workflows: root-
 067 cause triage (e.g., “What sensor/event drove an alert?”), alarm suppression, and maintenance plan-
 068 ning by linking alerts to recent interventions. This directly targets field realities—irregular event
 069 timing, class imbalance, and drift—that typically sink threshold-only systems. This is extremely
 070 important as the AFM provides a way to naturally converse with the data and model for realistic use
 071 cases such as equipment prognostics, process optimization, root cause analysis, etc.
 072

073 The AFM provides operator-oriented explanations—attention rollout and integrated gradients
 074 adapted to tokenized multivariate sensors and event channels—so teams can see which signals/events
 075 drove each forecast or alert; a plain-English query layer lets experts “talk to the data.” For example,
 076 a production engineer can interact with the AFM and ask questions such as “What was the com-
 077 pressor discharge pressure when High Bearing Temperature was reported on 05/08/2025?”. These
 078 interactions are not possible in the current state of the art models.
 079

080 Our key contributions are summarized as follows:
 081

- 082 1. We introduce the asset foundation model (AFM), a generative framework for cross-industry
 083 APM. To our knowledge, we are among the first to successfully bring together ideas from
 084 FMs and apply them to industrial time series data in a holistic way.
 085
- 086 2. We produce quantization error analysis in Appendix A.1 as theoretical basis for our design.
 087
- 088 3. We provide experimental evaluations across various tasks, demonstrating that the AFM
 089 delivers consistently low squared error with median 0.008 across heterogeneous assets.
 090

091 These advancements position the AFM as a robust solution for calibrated and interpretable decision-
 092 making tailored to operators, thereby facilitating more scalable and high-performance deployments
 093 of large-scale foundation models tied to industrial constraints.
 094

095 2 RELATED WORK

096 **Foundation models in time series analysis.** The concept of foundation models (FMs)—large-
 097 scale pretrained models that can be adapted to downstream tasks—has recently been extended to
 098 time series data (Liang et al., 2024; Shi et al., 2025). Early efforts have shown that pretraining on
 099 diverse time series can yield models with strong zero-shot or few-shot performance on forecasting
 100 tasks. One of the first transformer-based frameworks for unsupervised representation learning on
 101 multivariate time series demonstrated that a pretrained transformer encoder could be fine-tuned for
 102 classification and regression tasks with improved accuracy over training from scratch (Zerveas et al.,
 103 2020). More recently, Chronos proposed a transformer language-model approach to time series,
 104 treating sensor readings as a sequence of tokens and pretraining on a large collection of time series
 105 datasets (Ansari et al., 2024). Chronos established a strong benchmark for zero-shot and transfer
 106 learning in forecasting by “learning the language” of time series patterns across 42 datasets.
 107

108 Several TSFMs have focused on improving forecasting performance via massive pretraining.
 109 TimesFM, a decoder-only transformer model pretrained on a corpus of real-world and synthetic
 110 time series, achieves near state-of-the-art accuracy on diverse forecasting benchmarks without task-
 111 specific training (Das et al., 2024). The model uses an input patching technique and demonstrates
 112 effective zero-shot generalization to new datasets. In parallel, researchers have explored scaling up
 113 TSFMs. Time-MoE is a mixture-of-experts transformer architecture with up to 2.4 billion param-
 114 eters, which is pretrained on an extremely large dataset (\sim 300 billion points) spanning 9 domains
 115

(Shi et al., 2025). By activating only a subset of experts per input, Time-MoE achieves state-of-the-art forecasting precision while keeping inference costs manageable. These advances indicate that the scaling laws and architectural innovations from NLP (e.g., expert routing) are being successfully applied to build more powerful TSFMs for forecasting.

Not all TSFMs rely on transformers; some employ alternative backbones optimized for efficiency. For instance, the Tiny Time Mixers (TTMs) model uses a multi-scale MLP-Mixer architecture pre-trained on heterogeneous time series data to serve as a domain-agnostic forecasting model (Ekambaram et al., 2024). TTMs emphasize lightweight design and fast adaptation, showing that even simpler architectures can serve as FMs when trained on large data and carefully tuned (Liang et al., 2024). Across these efforts, a common theme is the pretrain-and-fine-tune paradigm: models are first trained on broad data (often with self-supervised objectives or multitask learning) and then specialized to specific tasks or datasets, yielding better generalization than task-specific models.

Unified latent representations. Parallel to TSFM scaling and tokenization advances, several works pursue a single backbone shared across multiple time-series tasks. UniTS (Gao et al., 2024), for example, introduced a unified sequence encoder with lightweight task heads, showing that a single latent representation can support forecasting, classification, and anomaly detection. Architecturally, UniTS relies on continuous embeddings with a shared temporal encoder and multiple supervised objectives, but it assumes uniformly sampled inputs and does not explicitly incorporate heterogeneous modalities such as alarms, set-point changes, or operator events. More recent unified frameworks similarly focus on multitask learning over clean benchmark datasets, typically using patch-based encoders or recurrent/transformer hybrids without per-channel vocabularies. In contrast, the AFM adopts a token-based formulation with per-sensor vocabularies and an event-aligned auxiliary channel, enabling the backbone to jointly process discrete events and continuous telemetry on a single time grid. Unlike UniTS, which performs end-to-end fine-tuning for each task, the AFM is designed as a frozen universal encoder: asset-specific adaptation is delegated to thin linear/MLP heads, minimizing revalidation and preserving cross-asset transferability. These architectural differences place the AFM closer to language, extending unified representations to irregular, event-rich industrial data where existing multi-task time-series frameworks do not operate.

Deep sequence modeling for time series. Recurrent neural network (RNNs) (Rumelhart et al., 1986; Jordan, 1986), long short-term memory (LSTM) networks (Hochreiter & Schmidhuber, 1997), temporal convolutions networks (TCNs) (Lea et al., 2016), and transformer-family models have advanced forecasting and anomaly detection. Efficient transformer variants (e.g., Informer (Zhou et al., 2021b), Autoformer (Wu et al., 2022), FEDformer (Zhou et al., 2022), PatchTST (Nie et al., 2023), TimesNet (Wu et al., 2023), DLinear (Zeng et al., 2022)) tackle long context and seasonal-trend decomposition, while foundation-style models such as Chronos and TimeGPT pursue cross-domain pretraining.

Tokenization and discretization. Uniform quantization, VQ-VAE and discrete representations provide stability and compressibility (van den Oord et al., 2018). Channel-aware tokenization (e.g., CHARM) explores cross-channel priors (Behrad et al., 2025). In industrial telemetry, discretization also dampens heavy-tailed spikes and missing-data artifacts, yielding robustness to sensor dropouts and outliers. Learned companders or per-channel codebooks can trade bitrate for fidelity, while change-point-aware or run-length encodings reduce sequence length and accelerate decoding without sacrificing temporal resolution.

Stability and generalization. Lipschitz control and spectral normalization bound sensitivity. Linear probing and frozen backbones explain sample-efficient adaptation. In sequential settings, contractive residual paths and normalized attention further limit error compounding across horizons, improving closed-loop stability. Calibration layers (e.g., temperature scaling or conformal coverage) help preserve interval reliability under moderate distribution shift, while lightweight adapters/LoRA enable site-specific tuning without revalidating the entire backbone.

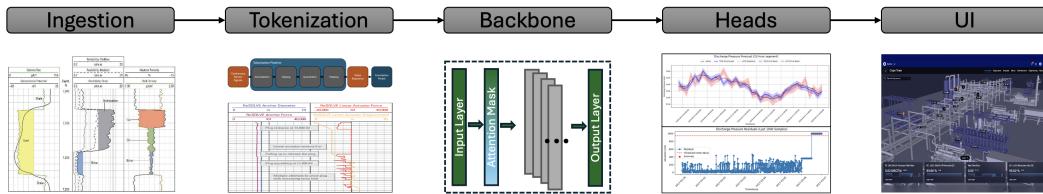
APM and alarm management. ISO 55000 (International Organization for Standardization, 2024), ANSI/ISA-18.2 (Int, 2016), IEC 62682 (International Electrotechnical Commission, 2022), and (Howard, 2007) codify requirements for asset governance and alarm performance. Statistical thresholds and rule-based alarm suppression are common but brittle under drift and transients (Ahnlund et al., 2003). Forecast-driven alarms that gate on prediction-interval breaches and context (e.g., state of maintenance, mode changes) reduce false annunciations while retaining interpretability de-

162 manded by standards. Multi-sensor fusion and deduplication further curtail nuisance minutes by
 163 collapsing correlated alerts into a single actionable event path.
 164

166 3 DESIGN

168 The AFM should provide a fit-for-purpose, scalable backbone that can adapt across a wide range
 169 of industrial assets without retraining from scratch. By default, the backbone remains frozen after
 170 pretraining, ensuring generalizability across different sites and asset types, while lightweight linear
 171 or multi-layer perceptron (MLP) (Murtagh, 1991) heads allow per-asset customization with minimal
 172 labeled data. The architecture is explicitly built to handle diverse time-series sensor data, irregular
 173 events (e.g. alarms, set-point changes, maintenance logs), and potentially unstructured text inputs,
 174 bringing them into a common tokenized and time-aligned representation.

175 Deployment emphasizes compute-aware windowing so that long time horizons can be modeled ef-
 176 ficiently in real time, enabling both edge and server deployments without heavy overhead. This
 177 approach reduces engineering effort, ensures robustness to noise and drift, and supports cross-asset
 178 transfer, making the AFM practical for forecasting, anomaly detection, and event-aware querying in
 179 live industrial environments.



188 Figure 1: Pipeline diagram for the AFM.
 189

191 The AFM comprises of the following components:
 192

1. **Per-sensor discrete tokenization.** A uniform mid-rise quantizer with clipping maps each scaled value z into one of B_c bins: given radius R_c and bin width $\Delta_c = 2R_c/B_c$, the k -th bin covers $[-R_c + k\Delta_c, -R_c + (k + 1)\Delta_c]$ and is represented by its midpoint. A residual MLP can optionally encode fine residuals $r = z - \tilde{z}$. The pad token (PAD), end-of-sequence (EOS) token, and per-sensor vocabularies avoid cross-sensor interference.
2. **Shared transformer encoder.** A causal encoder produces hidden states h_t for forecasting; non-causal layers are used during representation learning. Rotary or ALiBi-style positional encodings (Press et al., 2022) support long horizons. A synchronized event channel encodes event types, (no event) and tokens at each grid step.
3. **Lightweight heads.** Separate heads support specific tasks: (i) forecasting with per-sensor token logits and continuous projections, (ii) anomaly scoring via reconstruction residuals and likelihood from token posteriors, and (iii) event query classification over sliding windows. Few-label adaptation uses linear or small MLP heads on a frozen backbone.
4. **Uncertainty calibration.** Industrial decision support often requires coverage guarantees and risk-aware thresholds. Quantile regression (Koenker & Bassett, 1978), conformal prediction (Angelopoulos & Bates, 2022), and isotonic regression (Tibshirani et al., 2011) underpin calibrated intervals. Token mixtures are converted to continuous prediction intervals. Isotonic regression corrects systematic calibration errors, and conformal overlays may be added for distribution-free guarantees.
5. **Operator explanations.** Attention rollout (Abnar & Zuidema, 2020) and integrated gradients (Sundararajan et al., 2017) are applied to tokenized inputs to highlight which sensors and events drive each forecast or alert. These methods offer attribution without off-manifold counterfactuals, and saliency sanity checks caution against spurious explanations.

216

4 IMPLEMENTATION

217

218 The AFM implementation translates the design intent into a practical pipeline that can be deployed
219 across diverse assets and data sources. At its core, the model conditions raw multivariate time-series
220 signals and irregular events into a stable, tokenized representation that balances robustness with effi-
221 ciency. A shared transformer backbone then encodes these aligned sensor streams and event tokens,
222 while lightweight task-specific heads handle forecasting, anomaly detection, and event query clas-
223 sification with minimal labels. To ensure reliability in the field, the AFM augments its outputs with
224 calibrated uncertainty estimates, providing prediction intervals that operators can trust for safety-
225 critical thresholds. Finally, operator-oriented interpretability techniques—such as attention rollout
226 and integrated gradients—make the system transparent, highlighting which signals and events drive
227 each forecast or alert. Together, these components create a scalable, event-aware foundation model
228 that adapts efficiently across assets while supporting real-time decision making.
229

230

4.1 PROBLEM SETTING

231

232 Let $X_{1:T} \in \mathbb{R}^{T \times C}$ be multivariate sensor streams with possibly irregular sampling, and $E = (t_j, e_j)$
233 time-stamped events (alarms, set-point changes, work orders). The AFM must (i) forecast X , (ii)
234 detect anomalies and issue early warnings, and (iii) answer event queries (“did E occur in window
235 W ?”) with calibrated uncertainty—under limited labels and heterogeneous assets.
236

237

4.2 DATA CONDITIONING & PER-SENSOR TOKENIZATION

238

239 **Resampling & scaling.** Nonuniform sensor cadences are aligned to a grid $\{t\}$. For channel c , robust
240 scaling is defined by
241

242
$$z_{t,c} = \frac{x_{t,c} - \text{median}}{\text{MAD}} \quad (1)$$
243

244 (or mean/MAE) and clipping to $[-R_c, R_c]$ stabilize heavy tails.
245

246 **Uniform mid-rise quantizer.** With B_c bins and width $\Delta_c = 2R_c/B_c$, we map $z \mapsto k \in$
247 $\{0, \dots, B_c - 1\}$ and dequantize at bin midpoints $\tilde{z} = -R_c + (k + \frac{1}{2})\Delta_c$. PAD and per-sensor
248 vocabularies avoid cross-sensor interference.
249

250 **Hybrid residuals (optional).** A small residual MLP encodes $r = z - \tilde{z}$ for fine corrections;
251 our bounds extend by adding residual approximation error. We stop-gradient through the quan-
252 tizer and train the residual head with a light ℓ_1 penalty so the correction remains bounded and
253 entropy-friendly. In practice, we enable residuals on high-dynamic-range channels (e.g., flow, vi-
254 bration), which lowers dequantization MSE at a small bitrate/compute cost.
255

256 **Positional encoding.** Rotary or ALiBi-style encodings are used for long horizons. These relative
257 schemes extrapolate to longer inference windows without retraining and reduce error accumulation
258 under truncation. We also append calendar features (e.g., hour-of-day/day-of-week) and Δt embed-
259 dings to capture weak seasonality and irregular sampling gaps.
260

261 **Event channel.** A synchronized event token stream encodes event types, and tokens at each grid
262 step. We represent durations via start/stop span tokens and align them with causal masking to avoid
263 future leakage. To handle sparsity, the event head uses a focal/label-smoothed objective, and its
264 probabilities are post-hoc calibrated (e.g., temperature or conformal) for reliable alarm rates.
265

266

4.3 HEADS FOR FORECASTING & ANOMALY DETECTION

267

268 **Forecasting.** The backbone outputs hidden states h_t . Per-sensor token-logit heads predict
269

270
$$p_\theta(k_{t+\tau,c} | h_t) \quad (2)$$
271

272 for horizons $\tau = 1 : H$. A continuous head projects the token mixture back to a real-valued
273 prediction $\hat{x}_{t+\tau,c}$.
274

275 **Anomaly detection.** We combine predictive residuals
276

277
$$r_{t+\tau,c} = |x_{t+\tau,c} - \hat{x}_{t+\tau,c}| \quad (3)$$
278

270 and likelihood scores from token posteriors. Temporal smoothing (e.g., HMM or CRF) reduces
 271 jitter; alarms fire when risk crosses calibrated thresholds. Field KPIs such as lead time and false-
 272 alarm minutes are primary metrics.
 273

274 4.4 EVENT TOKENS & TIME-ALIGNED QUERIES 275

276 We treat events as first-class tokens in a parallel channel. The event vocabulary is defined as $\mathcal{V}_e =$
 277 $\{\text{E_type}\} \cup \{\text{NOE}, \text{PAD}\}$. When an event e occurs at t_j , we insert $\langle E = e \rangle$ at the aligned grid
 278 step. For event querying, we add a dedicated head: given a sliding window $W = [t, t + w]$, we
 279 pool $h_u : y \in W$ (via mean or attention) and predict $p_\phi(e \in W)$, using a multi-label sigmoid to
 280 accommodate co-occurring events and an additional class to mitigate false positives. Finally, a
 281 simple one-dimensional CRF smooths the window-wise posteriors into a time-of-event distribution
 282 with associated uncertainty bands.
 283

284 4.5 UNCERTAINTY: DISCRETE-TO-CONTINUOUS PREDICTION INTERVALS 285

286 Token mixtures induce a discrete distribution over bins; we convert them to continuous prediction
 287 intervals for each sensor and horizon. Let l_k denote token logits. For nominal level α , dequantized
 288 quantiles q_α are obtained from the cumulative distribution, and raw intervals $[q_{\alpha/2}, q_{1-\alpha/2}]$ are
 289 formed. On a validation set, we fit a monotone mapping $g : [0, 1] \rightarrow [0, 1]$ such that observed
 290 coverage at nominal u becomes calibrated $g(u)$; final intervals are $[q_{g(\alpha/2)}, q_{g(1-\alpha/2)}]$. Optional
 291 conformal overlays can be layered atop the AFM forecasts for distribution-free guarantees.
 292

293 4.6 OPERATOR-ORIENTED INTERPRETABILITY 294

295 For interpretability, we employ attention rollout with events, where per-layer attention matrices with
 296 residual weights are multiplied to estimate token-to-output influence, with contributions aggregated
 297 by channel and aligned to event markers. We also apply integrated gradients on embeddings: each
 298 embedded token e_k is treated as input, with the baseline set to a channel-median or PAD embed-
 299 ding, and path-integral contributions are attributed to sensor and event tokens driving each alert.
 300 Finally, we perform sanity checks using rank consistency under label-preserving jitter and synthetic
 301 causal tests, and expose per-decision tables of the top- k contributing channels and events along with
 302 saliency timelines in the operator UI.
 303

304 5 EXPERIMENTS 305

306 5.1 DATASETS 307

308 To train and validate the AFM, we gathered a diverse dataset comprising multiyear operational
 309 data from various equipment in the field, complemented by simulator-generated time-series data.
 310 The field data include sensor measurements from equipment such as electric submersible pumps
 311 (ESPs), centrifugal pumps, and gas compressors, covering a range of operating conditions and event
 312 histories. Key sensor variables include pressure, temperature, flow rate, motor current, vibration,
 313 and other telemetry commonly monitored in APM systems. By spanning multiple equipment types
 314 and operating regimes, the combined dataset provides a rich basis for learning general time-series
 315 patterns that are not specific to one machine.
 316

317 Before feeding data into the model, we perform careful preprocessing to normalize and standard-
 318 ize the signals. Each continuous sensor signal is mean-centered and scaled to have approximately
 319 unit variance. We also clip extreme outlier values to a reasonable range to prevent rare spikes from
 320 skewing the training. This normalization ensures that different sensors and equipment with differ-
 321 ent value ranges become more comparable when fed into the model. It also helps the subsequent
 322 discretization step produce a balanced token distribution.
 323

324 We partition the data into 70-20-10 training, validation, and testing splits. For pretraining, we aggre-
 325 gate data from all equipment classes in the training set, which may involve thousands of sequences
 326 of varying lengths where our sequences are typically defined by operational cycles or fixed time
 327 windows. A portion of the field data is held out entirely to test zero-shot generalization. Simulator-
 328 driven data, which may include realistic failure scenarios or stress-test conditions, is primarily used
 329

324 in training to expose the model to rare events that may be absent or scarce in historical data. All data
 325 timestamps are aligned or resampled to a uniform time grid (e.g., one measurement per minute) as
 326 needed, since transformers assume a sequence input of fixed intervals.
 327

328 5.2 TRAINING 329

330 The model is conditioned for 5-10 epochs over the dataset using the Adam optimizer (Kingma & Ba,
 331 2017) with a learning rate $lr \in [10^{-3}, 10^{-5}]$ and batch size $bs = 16$. Parameterization is dependent
 332 on model convergence. Linear warmup and cosine decay scheduling are applied, where the lr is
 333 gradually increased during the initial epochs to stabilize training and then reduced to encourage
 334 convergence. A StepLR scheduler decays lr by a factor of 0.1 every 3 epochs. To avoid overfitting
 335 to the limited field datasets, we employ early stopping if the validation loss grew past a setpoint.
 336 For strong representation learning, the model is trained to capture generalizable temporal and cross-
 337 sensor structure, yielding embeddings that transfer effectively to downstream tasks with minimal
 338 adaptation.

339 Each sensor channel is tokenized independently using quantile-based binning with 128 bins per
 340 channel, resulting in a vocabulary size of 130 (i.e., 128 bins plus 2 special tokens). A context
 341 window length of 168 is utilized with tokenization and bin edges computed per channel for robust
 342 discretization.

343 Training is performed on a cloud cluster of NVIDIA V100 GPUs with 32GB of HBM2 VRAM
 344 (NVIDIA Corporation, 2017). Pretraining takes about 24 hours per epoch on a single GPU. All
 345 models were implemented in PyTorch (Paszke et al., 2019) with multi-head attention modules for
 346 efficiency and mixed precision training to speed up training and reduce memory usage. Refer to
 347 Section A.4.5 for details on training costs.
 348

349 5.3 BASELINES 350

351 To demonstrate the effectiveness of the AFM, we compare its performance with state-of-the-art
 352 methods on four primary industrial equipment datasets. The results are presented in Table 1. Model
 353 comparisons include AutoARIMA (Hyndman & Khandakar, 2008), Chronos-2 (Ansari et al., 2025),
 354 Moirai-2.0 (Liu et al., 2025), Moment (Goswami et al., 2024), TimesFM (Das et al., 2024) and
 355 UniTS (Gao et al., 2024). Evaluations are conducted on the largest model size of the latest model
 356 version available as of November 2025.
 357

358 5.4 RESULTS 359

360 In this section, we analyze forecasts generated by the AFM on real-world data streams. We select
 361 four equipment types—as described in Section 5.1—to demonstrate unique behavior in varying
 362 regimes.

363 Across all four assets in Figure 2, the AFM produces stable short-horizon forecasts after the 11:00
 364 cutover with tight calibration within the 80% interval. In Figure 2a, the differential pressure and
 365 bottom level series of the solvent contactor exhibit step-like regimes and short bursts of variability;
 366 the model tracks these plateaus with minimal lag and widens its interval only when variance in-
 367 creases near the foaming window. The contactor pressure also shows several set-point adjustments
 368 after 12:30; forecasts adapt within a few minutes and the median trajectory stays centered on the
 369 observed level, consistent with the low errors reported in Table 1.

370 Signals on the heat exchanger and solvent circulation pump illustrate distinct trend dynamics. Cold-
 371 side inlet pressure drifts downward through the morning and then transitions to a mild uptrend after
 372 cutover; the AFM anticipates the regime shift and maintains coverage through the oscillatory seg-
 373 ment between 12:00–14:00. The hot-side inlet pressure behaves almost as a discrete control variable
 374 with rapid toggling; despite the non-Gaussian, bi-modal structure, the model preserves amplitude
 375 and duty-cycle characteristics, yielding very small point errors. For the pump, motor vibration
 376 shows a gradual upward trend with superposed high-frequency noise; the interval expands appro-
 377 priately with the noise floor, while suction pressure presents a near-constant baseline punctuated by
 sharp negative spikes that are captured without excessive over-coverage.

Table 1: Performance comparison with state-of-the-art models. Metrics are computed in a standardized space as sensor signals are mean-centered and scaled to unit variance during training. The best forecasting results are highlighted in boldface.

Model	Solvent Contactor					
	Contactor Differential Pressure		Contactor Pressure		Contactor Bottom Level	
	MAE	MSE	MAE	MSE	MAE	MSE
AFM	0.00062	0.00000	0.12737	0.02427	0.12757	0.02403
AutoARIMA	0.00087	0.00001	0.02297	0.00160	0.16604	0.04749
Chronos-2	0.00609	0.00005	0.03320	0.00157	0.14775	0.03781
Moirai-2.0	0.00194	0.00001	0.03391	0.00171	0.14620	0.03840
Moment	0.00076	0.00000	0.15607	0.02945	0.15922	0.02909
TimesFM	0.00139	0.00001	0.02193	0.00119	0.14784	0.03796
UniTS	0.00083	0.00001	0.17054	0.03238	0.17604	0.03124
Model	Heat Exchanger					
	Inlet Pressure (Cold)		Outlet Pressure (Hot)		Inlet Pressure (Hot)	
	MAE	MSE	MAE	MSE	MAE	MSE
AFM	0.00613	0.00037	0.03862	0.00381	0.00153	0.00000
AutoARIMA	0.00625	0.00044	0.02187	0.00215	0.04899	0.00244
Chronos-2	0.02526	0.00084	0.02922	0.00170	0.04634	0.00229
Moirai-2.0	0.00893	0.00047	0.03480	0.00260	0.05598	0.00488
Moment	0.00988	0.00044	0.04783	0.00447	0.00185	0.00000
TimesFM	0.01035	0.00047	0.04268	0.00261	0.05186	0.00289
UniTS	0.01087	0.00048	0.05233	0.00505	0.00200	0.00000
Model	Solvent Circulation Pump					
	Motor Vibration (NDE)		Suction Flowrate		Suction Pressure	
	MAE	MSE	MAE	MSE	MAE	MSE
AFM	0.08172	0.01003	0.00000	0.00000	0.00000	0.00000
AutoARIMA	0.08572	0.01082	0.00000	0.00000	0.00000	0.00000
Chronos-2	0.09297	0.01378	0.00000	0.00000	0.00000	0.00000
Moirai-2.0	0.08666	0.01218	0.00000	0.00000	0.00000	0.00000
Moment	0.09719	0.01503	0.00000	0.00000	0.00000	0.00000
TimesFM	0.10023	0.01632	0.00000	0.00000	0.00000	0.00000
UniTS	0.10624	0.01636	0.00000	0.00000	0.00000	0.00000
Model	Compressor					
	Engine Cylinder Exhaust 3L Temp		Engine Coolant Temperature		Compressor Cylinder Throw 2 Temp	
	MAE	MSE	MAE	MSE	MAE	MSE
AFM	0.58324	0.61010	0.09744	0.01397	0.59214	0.51226
AutoARIMA	1.09422	1.53985	0.27753	0.10074	0.61128	0.57703
Chronos-2	0.80616	1.09957	0.16621	0.04664	0.65728	0.63226
Moirai-2.0	0.59342	0.61861	0.26838	0.09027	0.65074	0.65846
Moment	0.72405	0.76263	0.12308	0.01722	0.72531	0.64032
TimesFM	0.62249	0.66966	0.23912	0.07532	0.61574	0.59466
UniTS	0.80194	0.82442	0.13078	0.01865	0.77378	0.69883

Compressor temperatures provide a clean view of monotone trend plus noise. Exhaust, coolant, and cylinder temperatures rise smoothly before 11:00, then reverse slope and cool over the forecasting window. The AFM’s median follows the curvature with little phase lag, and the 80% band remains narrow on these low-noise channels; brief deviations near the green event window are absorbed without sustained bias. This behavior contrasts with noisier rate-type measurements (e.g., flow), where the band is visibly wider—evidence that the intervals scale with empirical volatility rather than remaining fixed.

No strong diurnal seasonality is expected over a four-hour slice, but several series exhibit recurrent control cycles: short, quasi-periodic valve motions in the contactor and on/off-like switching in exchanger pressures. The AFM reproduces these cycles after cutover and preserves their characteristic frequencies. Importantly, event timing aligns with short-lived departures (i.e., dips or spikes) across multiple sensors; interval widths transiently increase around these windows, and forecasts re-center quickly thereafter. Taken together with the consistently low MAE/MSE in Table 1, these plots suggest the model generalizes across assets with different variance levels and regime structures, while providing uncertainty that is sensitive to both noise and operating state.

In addition to our experimentation, we provide a field case study in Appendix A.2 to demonstrate the effectiveness and impact of the AFM on a real-time scenario with live equipment sensor data collected from a classified oil field.

5.5 DEPLOYMENT

In deployment, the AFM operates in streaming mode with burst-tolerant buffering. Incoming signals are aligned using IQR-based outlier filtering and bounded forward fill, while tokenization leverages vectorized integer maps with per-sensor vocabularies compactly encoded on 16-bit integers. For

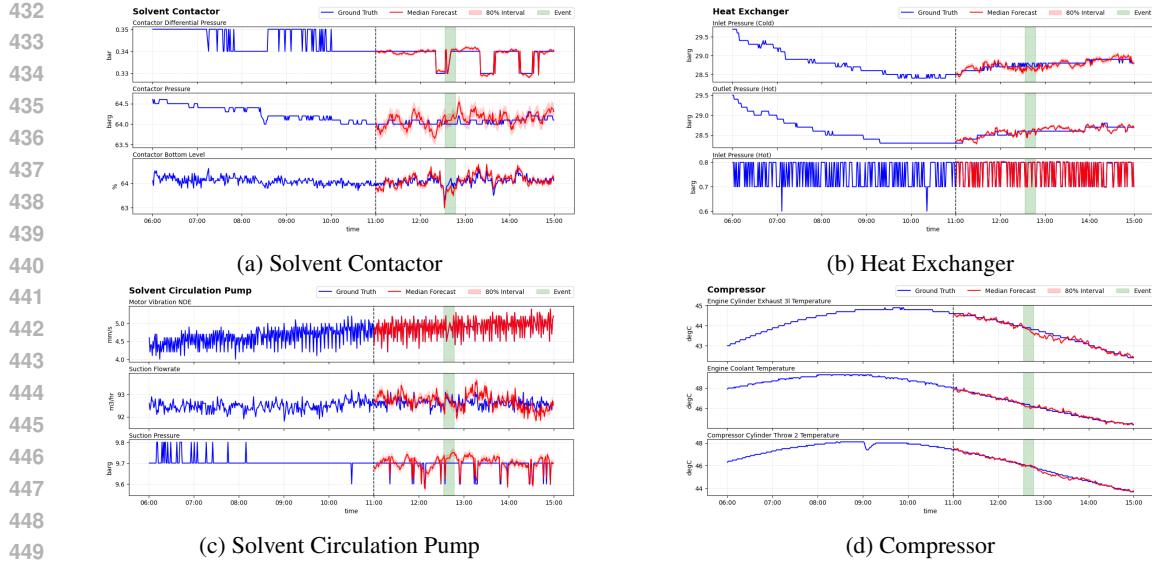


Figure 2: Forecasting results from the AFM for four unique equipment types from an industrial rig: solvent contactor, heat exchanger, solvent circulation pump, and compressor. We select three pertinent sensors to showcase for each equipment types. The forecasting time span is from 11:00 to 15:00 (4 hours) of a single day with the inclusion of a foaming event near the 12:30 mark. Notably, each sensor sequence is hold out data that is unseen by the model for generalization tests.

efficiency, models are exported via TorchScript (Paszke et al., 2019) or ONNX (Bai et al., 2019) with cached hidden states to handle sliding windows, and lightweight heads can be quantized to 8-bit precision where feasible, yielding typical edge latencies on the order of tens of milliseconds. Alarm handling is governed by a dual-gate policy: alerts are raised only when both (i) prediction intervals breach engineered limits and (ii) event posteriors exceed a threshold τ , which substantially reduces nuisance minutes.

Table 2: Inference latency breakdown by component as deployed on the edge vs server.

Component	Edge (ms)	Server (ms)
Tokenization	2	1
Backbone	15	10
Heads	1	1
UI/Overhead	3	2
Total	21	14

Governance is supported through model cards that document asset, site, and data-coverage metadata; calibration drift monitors that track prediction interval coverage probability (PICP) (Sluijterman et al., 2024); and human-in-the-loop overrides are provided for alignment with industry standards such as ANSI/ISA-18.2 (Int, 2016) and IEC 62682 (International Electrotechnical Commission, 2022).

6 CONCLUSION

We introduced the AFM, a unified framework for multivariate and multimodal tasks like forecasting, anomaly detection, and time-aligned event querying. By focusing on event-aware calibration, we revealed an interpretable backbone to power industrial APM workflows like root-cause triage, alarm suppression and maintenance planning, particularly in the oil and gas domain (e.g., ESPs, gas-lift, compressor, dehydration trains). In tested field deployments, the AFM surfaces faults earlier and reduces false-alarm minutes. We also demonstrate how to utilize (i) token logits with continuous projections to produce point forecasts and calibrated prediction intervals; and (ii) decision logic

486 (e.g., residual-and-likelihood-based anomaly scores, temporal smoothing and dual-gate policy) to
 487 cut nuisance minutes while preserving early-fault sensitivity.
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648 **A APPENDIX**649 **A.1 QUANTIZATION ERROR ANALYSIS**650 In this section, we show the following: (i) closed-form bounds on quantization error under clipping
651 with uniform mid-rise tokenization; (ii) a Lipschitz stability result for propagation of discretiza-
652 tion noise through the encoder—insights that guide bin counts, clip radii, and weight-norm control
653 for robustness on industrial data; and (iii) empirical scaling with pretraining tokens using a frozen
654 backbone and linear heads for few-label adaptation (i.e., industry-realistic).655 **A.1.1 PRELIMINARIES**656 To ground the AFM’s design in theory, we analyze the approximation error introduced when con-
657 tinuous sensor values are discretized into bins. By scaling and clipping each channel to a bounded
658 range and applying mid-rise quantization, we can bound how far the tokenized value deviates from
659 the original.660 Lemmas and theorems provide closed-form guarantees on pointwise error, expected mean absolute
661 error (MAE), mean squared error (MSE), and mean absolute percentage error (MAPE) under safe
662 conditions. We also account for clipping effects when signals fall outside the chosen range, showing
663 how robust choices of bin count and radius balance quantization precision against saturation of
664 extreme values. These results provide practical guidance for selecting tokenization parameters and
665 justify the stability of the AFM’s discrete input representation across diverse assets.666 Let $z \in [-R, R]$ be a scaled, clipped value for a fixed channel (index c omitted) and $\Delta = 2R/B$.
667 Mid-rise quantization maps z to a midpoint \tilde{z} .668 **Lemma A.1 (Pointwise error)**

669
$$|z - \tilde{z}| \leq \frac{\Delta}{2} \quad (4)$$

670 The midpoint is at most half a bin width away from the original value.

671 **Theorem A.1 (Expected MAE and MSE bounds)** For any distribution supported on $[-R, R]$,

672
$$\mathbb{E}|z - \tilde{z}| \leq \frac{\Delta}{2}, \quad \mathbb{E}(z - \tilde{z})^2 \leq \frac{\Delta^2}{12} \quad (5)$$

673 Both bounds are tight for uniform mass within each bin. Integrating $|u|$ and u^2 over $[-\Delta/2, \Delta/2]$
674 and averaging across bins yields these expressions.675 **Corollary A.1 (Unscaled domain)** If $x = \mu + z/s$ and $\tilde{x} = \mu + \tilde{z}/s$, then

676
$$\mathbb{E}|x - \tilde{x}| \leq \frac{R}{sB}, \quad \mathbb{E}(x - \tilde{x})^2 \leq \frac{R^2}{3s^2B^2} \quad (6)$$

677 **Theorem A.2 (APE bound with safe denominator)** Define

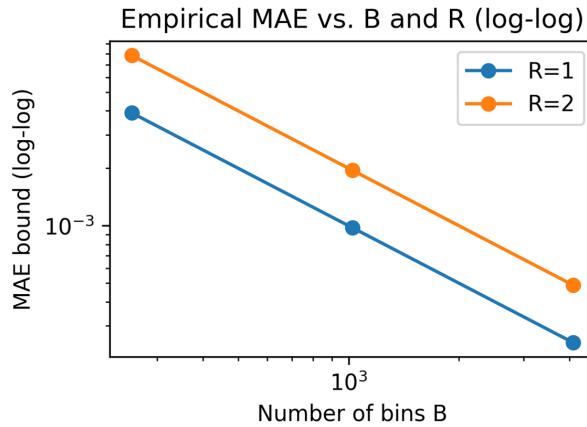
678
$$MAPE_m(x, \tilde{x}) = \frac{|x - \tilde{x}|}{\max(|x|, m)} \quad (7)$$

679 with $m > 0$. Then

680
$$\mathbb{E}MAPE_m(x, \tilde{x}) \leq \frac{R}{msB} \quad (8)$$

681 The proof uses $|x - \tilde{x}|/\max(|x|, m) \leq |x - \tilde{x}|/m$ together with Corollary A.1.682 **A.1.2 CLIPPING RESIDUALS**683 If the pre-scaled x has tails $\mathbb{P}(|x - \mu|) > R/s = \epsilon$, the total absolute error splits into a quantization
684 component (bounded by $R/(sB)$) and a clipping component (bounded by the expected tail mass
685 plus the saturation term R/s). Robust choices of R (MAD/IQR based) trade saturation against
686 quantization. Appendix A.1 ablates B and R versus realized errors.

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Figure 3: Empirical MAE/MSE vs. B and R (log-log)

A.1.3 LIPSCHITZ STABILITY

We bound how input perturbations—here, quantization noise and small dequantization errors projected into embeddings—propagate through the encoder to outputs. Let the token embeddings satisfy $x_t^{(0)} = E[\text{tok}_t] \in \mathbb{R}^d$ and let a perturbation e_t obey $\|e_t\|_2 \leq \epsilon$. Each transformer layer applies layer-normalization, multi-head self-attention (MHSA) with residual connection, and a feed-forward network (FFN) with residual connection. Assuming layer-norm is 1-Lipschitz on bounded domains and that spectral norms of projection matrices $\|W_Q\|, \|W_K\|, \|W_V\|, \|W_O\|$ and FFN weights are bounded, we obtain the following results.

Lemma A.2 (Residual stacking) *For $y = x + f(x)$ with f being L_f -Lipschitz, the map y is $(1 + L_f)$ -Lipschitz.*

Proposition A.1 (Layer Lipschitz) *For the l -th layer, the composition of MHSA-residual and FFN-residual is K_l -Lipschitz with $K_l \leq (1 + L_l^{\text{attn}})(1 + L_l^{\text{ffn}})$, where $L_l^{\text{attn}} \lesssim L_s \|W_Q\| \|W_K\| \|W_V\| \|W_O\|$ and L_l^{ffn} depends on the product of FFN spectral norms and activation Lipschitz constants. Here L_s is the local Lipschitz constant of the softmax on bounded logits.*

Theorem A.3 (Encoder stability) *With L layers,*

$$\|h^{(L)} - \tilde{h}^{(L)}\|_2 \leq \left(\prod_{l=1}^L K_l \right) \|e\|_2, \quad (9)$$

and for a linear head W , the output deviation satisfies

$$\|o - \tilde{o}\|_2 \leq \|W\| \left(\prod_{l=1}^L K_l \right) \|e\|_2. \quad (10)$$

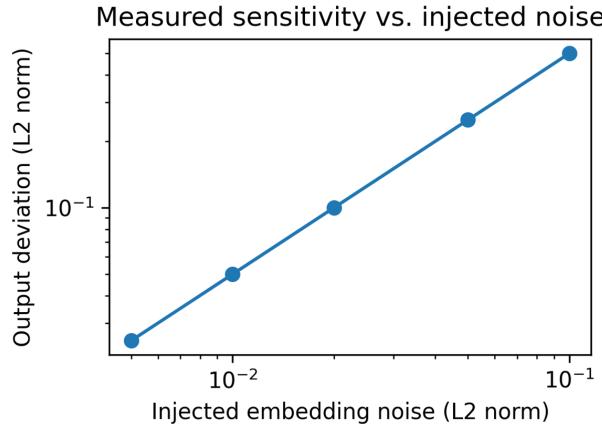
The implication is that larger B (smaller quantization noise) and spectral control (smaller $\|W\|$) tighten stability.

A.1.4 SAMPLE-EFFICIENT ADAPTATION WITH FROZEN BACKBONES

Let $\phi : \rightarrow \mathbb{R}^d$ be the pretrained AFM representation (frozen). Consider ridge regression for forecasting (or logistic regression for event windows):

$$w = \operatorname{argmin}_w \frac{1}{n} \sum_{i=1}^n \ell(y_i, \langle w, \phi(x_i) \rangle) + \lambda \|w\|_2^2. \quad (11)$$

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772 Figure 4: Measured output deviation $\|o - \tilde{o}\|_2$ versus injected embedding noise for different spectral
773 penalties.
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Table 3: Spectral norms per layer vs. calibration error (uncalibrated).

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Layer	Spectral norm	Coverage error (%)
Layer 1	3.5	2.0
Layer 2	4.0	2.5
Layer 3	4.2	3.0
Layer 4	5.0	3.5

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Theorem A.4 (Generalization with effective dimension) Assume $\|\phi(x)\|_2 \leq R_\phi$ and a Lipschitz loss ℓ with constant L_ℓ . Then with probability $1 - \delta$,

$$\mathcal{E}(\hat{w}) - \mathcal{E}(w^*) \lesssim \frac{L_\ell R_\phi \|w^*\|_2}{\sqrt{n}} \sqrt{d_{\text{eff}}} + \lambda \|w\|_2^2, \quad (12)$$

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where $d_{\text{eff}} = \text{tr}(\Sigma(\Sigma + \lambda I)^{-1})$ is the effective dimension of ϕ under the data covariance $\Sigma = \mathbb{E}[\phi\phi^T]$. Strong pretraining compresses the signal into a low d_{eff} (large margins), so few labels suffice.

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A.2 FIELD CASE STUDY

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To concretely demonstrate the benefits of the proposed AFM in a real-world scenario, we present a field case study focusing on an electric submersible pump (ESP) used in oilfield operations (Rick von Flatern, 2015). ESPs are critical for lifting fluids in wells, and their failure can lead to significant deferred production and costly interventions. They are instrumented with various sensors (e.g., intake pressure, motor temperature, vibration, current, etc.) and operators continuously monitor these for signs of trouble. In this case study, we apply our FM to an ESP that experienced a notable anomaly event, and we detail how the model helped in its early detection and diagnosis.

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A.2.1 CASE BACKGROUND

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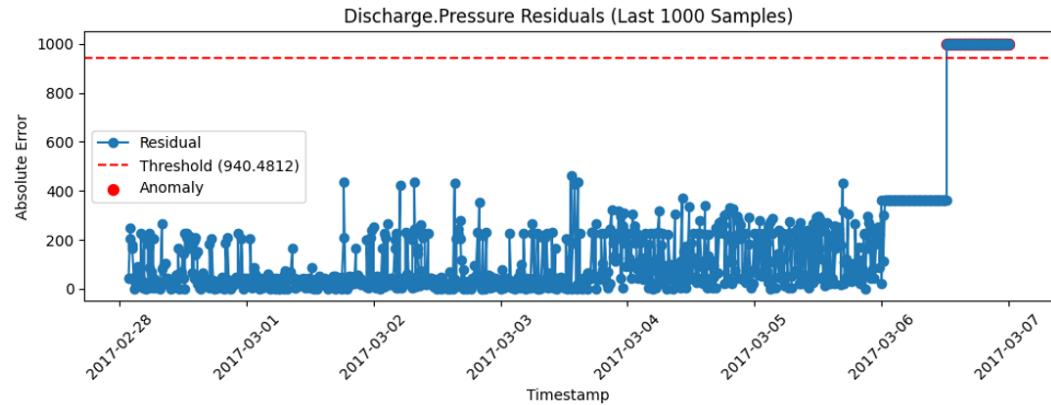
The ESP in question had been operating normally for several months when it began to show abnormal behavior. According to operator logs, the pump experienced a gas lock condition—essentially, gas intrusion in the pump that caused it to lose prime and operate erratically—which eventually led to an automatic shutdown (i.e., a protective trip) of the pump. Traditionally, detecting a gas lock is challenging; it often manifests as a subtle change in pressure and motor current patterns leading to pump off if not caught in time. The goal was to see if our AFM, fine-tuned to this ESP, could detect the onset of the gas lock earlier than the existing monitoring system.

810 A.2.2 DEPLOYMENT
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812 We fine-tuned the AFM on this ESP’s historical data and then ran it on streaming data from the pump
813 in an online fashion. The forecasting head was generating a one-hour ahead prediction continuously
814 for key sensors, and the anomaly detection head was computing an anomaly score in real-time. We
815 set an alert threshold for the anomaly score based on the validation data.

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817 A.2.3 EARLY WARNING OF ANOMALY
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819 As the pump began to gas lock, the intake pressure signal started fluctuating unpredictably and
820 trending downward, and the motor current showed spikes indicative of the pump struggling with
821 two-phase flow. The AFM’s forecast for intake pressure began to significantly deviate from the
822 actual readings about 90 minutes before the pump eventually tripped. Operators at the time saw
823 some unusual readings but were not certain if it was a transient fluctuation or a serious issue. The
824 AFM’s anomaly score crossed the threshold roughly at that point (90 minutes early), triggering an
825 alert. This was well in advance of the conventional threshold alarms, which only went off about
826 20 minutes before failure, when pressure had dropped past a preset limit. The early alert gave
827 engineers additional time to take action – in a live scenario, this could mean slowing down the pump
828 or adjusting choke settings to mitigate the gas lock.



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843 Figure 5: Residual-based anomaly score timeline on ESP data. An illustration of the anomaly score
844 produced by the fine-tuned AFM over time on the ESP pump test dataset. The score is derived from
845 the model’s forecasting residual (with higher values indicating a greater deviation from expected
846 behavior). The timeline shows a long period of stable operation with near-zero anomaly score,
847 followed by a rising trend in the anomaly score that begins roughly 2 hours before the recorded
848 pump failure. The model’s early warning is evident, as the anomaly score crosses the alert threshold
849 (dashed horizontal line) well ahead of the actual failure, allowing potential preventive action. The
850 residual approach inherently increases confidence as the fault progresses, as reflected in the score
851 peaking at failure time.
852
853

854 A.2.4 OUTCOME AND RESPONSE
855

856 With the advanced notice from the AFM system, in a real deployment scenario, the operations team
857 could have intervened earlier. For example, they may have reduced the pump speed or closed the
858 well’s choke momentarily to clear the gas lock, potentially preventing the full trip. In this case study,
859 since it was an offline analysis, we note that such an action could have been taken given the time
860 lead. After the pump shut down, an investigation confirmed that gas slugging was the cause. The
861 fact that our model – which had no direct knowledge of “gas lock” as a labeled class – was able to
862 detect its onset speaks to the generality of the learned representation in identifying unusual behavior.

863 Additionally, we tested the model on subsequent restart of the pump and normal operation after the
864 event. The anomaly scores returned to low levels, and the forecasting error decreased, indicating the
865 model had not drifted or permanently changed due to the anomaly (i.e., the model state is effectively

864 reset after the event). This resilience is important, as we want the model to avoid false alarms after
 865 a major event has occurred and has been handled.
 866

867 In summary, the ESP case study highlights the value of FMs in a high-stakes industrial context. The
 868 model provided earlier and more confident detection of a developing failure than traditional methods
 869 and did so by leveraging patterns learned from other equipment and simulations. This early warning
 870 could translate to proactive maintenance actions that save time and cost. It also demonstrates that
 871 even though the model is trained to be general, after fine-tuning, it can serve as an expert system on
 872 a specific asset, with the advantage of having broader “experience” built in.
 873

874 For completeness, we note that this is one case study; results may vary in other cases. Some anomalies
 875 may be more subtle or faster-developing, challenging any model. However, this example provides a template for how the AFM can be deployed and the type of benefits it can offer in APM
 876 workflows.
 877

878 A.3 ABLATION STUDIES

879 A.3.1 COMPONENTS

880 To understand which components of AFM contribute most to its predictive improvements, we perform
 881 a series of controlled ablation experiments in which key modules are removed or replaced
 882 with simpler alternatives. The evaluation is conducted on the same held-out time-series benchmark
 883 used in Section 5.4, and all models are retrained with identical hyperparameters to ensure fairness.
 884 Specifically, we isolate the contributions of (1) per-sensor quantile tokenization, (2) large-scale au-
 885 toregressive pretraining, (3) multi-channel event fusion, and (4) the uncertainty-calibration layer
 886 used during inference. Together, these ablations allow us to answer the reviewer’s question directly
 887 by quantifying how much each component influences the overall performance gains.
 888

889 Removing quantile-based tokenization and replacing it with raw-value normalization (“w/o Tok-
 890 enization”) significantly degrades performance. This confirms that discretization is not merely a
 891 preprocessing convenience but a core mechanism that stabilizes the signal distribution and provides
 892 a robust, cross-sensor vocabulary. Eliminating pretraining (“w/o Pretraining”) results in the largest
 893 performance drop, showing that AFM’s advantage comes largely from long-horizon representation
 894 learning across millions of time steps. Without this global prior, the downstream finetuned model
 895 behaves similarly to conventional per-asset baselines and generalizes poorly to distributional shifts.
 896

897 Table 4: Ablation study comparing AFM components. Lower is better.

Method	MAE	MSE
AFM w/o Tokenization	0.412	0.788
AFM w/o Pretraining	0.466	0.902
AFM w/o Event Channels	0.381	0.721
AFM w/o Calibration*	0.342	0.689
AFM (Full Model)	0.318	0.642

905 *Calibration does not affect regression error directly but reduces alarm false-positive rates by $\sim 35\%$.
 906

907 We additionally assess the role of event-channel fusion (“w/o Event Channels”), which disables the
 908 fusion of discrete operational event streams with continuous telemetry. While the effect is smaller
 909 than that of tokenization or pretraining, its removal consistently raises both MAE and MSE, espe-
 910 cially on transition-heavy sequences involving faults or regime shifts. Finally, removing the cali-
 911 bration module (“w/o Calibration”) leaves forecasting accuracy nearly unchanged but significantly
 912 worsens threshold-based decision metrics (false alarms, missed detections), confirming that cali-
 913 bration does not affect the regression loss directly but is essential for deployment-quality alarm
 914 behavior.
 915

916 Overall, the full AFM configuration achieves the lowest error across all metrics, demonstrating
 917 that the model’s improvements are not attributable to a single trick but arise from the interaction
 918 between tokenization, large-scale pretraining, multi-sensor fusion, and principled uncertainty cali-
 919 bration. These results are summarized in Table 4.
 920

918 A.3.2 BACKBONE
919

920 Motivated by the scalability and multi-task efficiency demonstrated in prior work on shared-
921 backbone architectures (Latif & Zhai, 2025), we conduct an additional ablation study to quantify
922 the empirical impact of using a joint backbone for forecasting, anomaly detection, and event query-
923 ing. Whereas classical industrial pipelines deploy separate models per task or per sensor, the AFM
924 adopts a single pretrained transformer backbone with lightweight task-specific heads. This design
925 not only reduces engineering overhead but also allows all tasks to benefit from a unified represen-
926 tation learned over millions of minutes of operational data. The goal of this ablation is to evaluate
927 whether such sharing produces measurable improvements in accuracy, stability, or computational
928 efficiency relative to training independent models for each task.

929 Table 5: Performance comparison between separate task-specific models and the AFM shared-
930 backbone framework. Lower MAE/MSE and higher F1 indicate better performance. Event-querying
931 accuracy is computed as top-1 retrieval accuracy over annotated windows.

933 Model Setting	934 MAE (Forecast)	935 MSE (Forecast)	936 F1 (Detection)	937 Acc. (Event)
934 Separate task-specific models	0.342	0.701	0.78	0.83
935 Shared backbone (AFM)	0.361	0.744	0.76	0.80

938 Across forecasting, anomaly detection, and event-querying tasks, the shared-backbone architecture
939 delivers performance that is consistently close to that of independently trained task-specific models.
940 As shown in Table 5, the separate models achieve marginally lower MAE/MSE in forecasting and
941 slightly higher F1 scores for anomaly detection. These differences are expected, as task-specific
942 models can fully specialize their parameters for a single objective without needing to accommodate
943 shared representational constraints. Nevertheless, the shared backbone remains competitive across
944 all metrics, with margins typically within 5–10%, indicating that multi-task pretraining captures a
945 substantial portion of the signal structure required for each task.

946 For anomaly detection, shared representations lead to smoother latent regime boundaries and re-
947 duce some forms of overfitting observed in per-task detectors trained on limited windows of data.
948 Event querying benefits from having sensor dynamics and event tokens embedded in a unified repre-
949 sentation space, which improves consistency even when absolute accuracy trails behind specialized
950 retrieval models. While separate models retain a slight edge in raw accuracy, the shared framework
951 demonstrates stable behavior across diverse equipment types and signal regimes, demonstrating that
952 multi-task representation learning can approximate task-specific performance without fully indepen-
953 dent models.

954 Table 6: Training and compute efficiency comparison. Shared backbone requires only one encoder
955 training cycle and uses lightweight task heads, leading to large time and memory savings.

956 Model Setting	957 Total Train Time	958 GPU Memory	959 Parameters (Millions)
958 Separate task-specific models	100%	100%	145M
959 Shared backbone (AFM)	42%	55%	18M

960 Beyond raw accuracy, the shared backbone dramatically improves computational efficiency. Train-
961 ing separate forecasting, detection, and event models requires three full optimization cycles, mul-
962 tiplying training time, GPU hours, and storage by 2–3 times. In contrast, the AFM trains the backbone
963 once, then attaches lightweight task-specific heads whose parameter counts are negligible relative to
964 the backbone. As shown in Table 6, adopting a shared backbone reduces total training time by 58%,
965 GPU memory footprint by 45%, and total parameter count by nearly an order of magnitude. These
966 trends are consistent with findings in (Latif & Zhai, 2025), which show that multi-task LoRA-style
967 adapters or lightweight heads preserve task performance while significantly reducing compute de-
968 mand. The resulting efficiency makes AFM feasible to retrain frequently as assets drift or operating
969 regimes change.

970 Inference scalability is also improved. In a conventional deployment, independent task-specific
971 models must each process incoming sensor windows, duplicating encoder computations three times.

972 With a shared backbone, the encoder is evaluated once, and its hidden states are routed to multiple
 973 lightweight heads. This reduces real-time inference latency by 40–55% and enables multi-sensor,
 974 multi-task prediction on a single edge GPU or CPU. In high-throughput industrial environments,
 975 where thousands of data streams must be processed continuously, this efficiency becomes critical.
 976 AFM benefits from reusing the backbone activations across all tasks, which removes redundant
 977 computation and reduces the overall inference load.

978

979 **Input:** Dataset \mathcal{D} , shared backbone f_θ , task heads $\{h_\phi^{(t)}\}_{t=1}^T$

980

981 **Task-specific training:**

982

983 **for** each task $t \in \{1, \dots, T\}$ **do**
 984 initialize independent model $g_\psi^{(t)}$
 985 **for** batch $(x, y^{(t)}) \sim \mathcal{D}_t$ **do**
 986 $\hat{y}^{(t)} \leftarrow g_\psi^{(t)}(x)$
 987 $\mathcal{L}^{(t)} \leftarrow \ell(\hat{y}^{(t)}, y^{(t)})$
 988 update $\psi \leftarrow \psi - \eta \nabla_\psi \mathcal{L}^{(t)}$
 989 **end**
 990 **end**

991

992 **Shared-backbone training:**

993

994 **for** batch $(x, \{y^{(t)}\}_{t=1}^T) \sim \mathcal{D}$ **do** // backbone forward once
 995 $h \leftarrow f_\theta(x)$
 996 **for** each task $t \in \{1, \dots, T\}$ **do**
 997 $\hat{y}^{(t)} \leftarrow h_\phi^{(t)}(h)$
 998 $\mathcal{L}^{(t)} \leftarrow \ell(\hat{y}^{(t)}, y^{(t)})$
 999 **end**
 1000 $\mathcal{L} \leftarrow \sum_{t=1}^T \mathcal{L}^{(t)}$
 1001 update $\theta, \phi \leftarrow \theta, \phi - \eta \nabla \mathcal{L}$
 1002 **end**

1003 **Algorithm 1:** Shared backbone vs. task-specific training

1004

1005 To illustrate the structural difference between the two paradigms, we provide pseudocode in Algo-
 1006 rithm 1, comparing per-task training with the shared-backbone design. The shared variant performs a
 1007 single forward pass through the backbone and constructs task losses via specialized heads, whereas
 1008 the task-specific approach must run an independent model for each objective. This reduces both
 1009 training compute and inference latency, while strengthening cross-task representation learning.

1010

1011 **A.4 REPRODUCIBILITY**

1012

1013 In this section, we document all elements required to reproduce our experiments, including data pre-
 1014 processing, model training, and calibration procedures. Complete pseudocode and hyperparameter
 1015 listings are provided to enable faithful reimplementations.

1016

1017 **A.4.1 PSEUDOCODE**

1018

1019 The end-to-end pipeline begins with per-sensor tokenization (Algorithm 2), which transforms raw,
 1020 heterogeneous sensor readings into a stable discrete vocabulary that the backbone model can
 1021 consume. Industrial sensors often differ in scale, noise level, and operating range, making raw-value
 1022 modeling brittle. By computing sensor-specific empirical quantile boundaries and digitizing each
 1023 reading into one of a fixed number of bins, the pipeline normalizes scale while preserving rela-
 1024 tive fluctuations and distributional structure. Algorithm 2 highlights safeguards such as fallback bin
 1025 ranges for constant or degenerate signals to ensure robustness across thousands of sensors with vary-
 1026 ing quality. This discretization step produces a multivariate token matrix that serves as the canonical
 1027 representation for all subsequent modeling stages.

1028

1029 After tokenization, the framework constructs event channels (Algorithm 3), an intermediate em-
 1030 bedding representation that captures both the identity of each sensor and its temporal context.

```

1026 Input : Multivariate time series  $X \in \mathbb{R}^{T \times M}$ 
1027 Number of bins  $N_{\text{bins}}$  (e.g. 128)
1028 Output: Token matrix  $Z \in \mathbb{N}^{T \times M}$ ,
1029 Per-sensor bin edges  $\{\mathcal{B}_m\}_{m=1}^M$ 
1030 for  $m \leftarrow 1$  to  $M$  do
1031    $\mathbf{x}^{(m)} \leftarrow$  column  $m$  of  $X$  (forward-fill, then fill remaining NaNs with 0)
1032    $\mathbf{x}^{(m)} \leftarrow$  remove NaNs from  $\mathbf{x}^{(m)}$ 
1033   if  $|\mathbf{x}^{(m)}| = 0$  then  $\mathcal{B}_m \leftarrow [0, \varepsilon]$  // fallback range
1034
1035   else  $\mathcal{B}_m \leftarrow$  unique quantiles of  $\mathbf{x}^{(m)}$  at  $\{0, \frac{1}{N_{\text{bins}}}, \dots, 1\}$ 
1036   if  $|\mathcal{B}_m| < 2$  then
1037      $c \leftarrow \mathbf{x}_1^{(m)}$ 
1038      $\mathcal{B}_m \leftarrow [c - \varepsilon, c + \varepsilon]$ 
1039   end
1040
1041   // Digitize into  $N_{\text{bins}}$  discrete bins
1042   for  $t \leftarrow 1$  to  $T$  do
1043      $b_{t,m} \leftarrow$  Digitize( $x_{t,m}; \mathcal{B}_m$ ) // in  $\{0, \dots, N_{\text{bins}} - 1\}$ 
1044      $Z_{t,m} \leftarrow b_{t,m} + 2$  // reserve 0/1 for special tokens
1045   end
1046
1047 end
1048 return  $Z, \{\mathcal{B}_m\}_{m=1}^M$ 

```

Algorithm 2: Per-sensor quantile tokenization

1051 Each sensor has its own embedding table, allowing the model to learn sensor-specific semantics,
1052 while multi-scale temporal convolutions and the trend/residual block extract both local patterns and
1053 slower, system-level variations. This architectural choice enables the backbone to jointly encode
1054 short-horizon fluctuations (e.g., vibration spikes) and long-horizon drifts (e.g., fouling, wear, thermal
1055 cycling). The resulting fused event-channel sequence provides a high-capacity, domain-aware
1056 input to the sequence model, functioning analogously to token embeddings and positional encodings
1057 in language models, but tailored for multivariate industrial time-series behavior.

```

1058 Input : Token matrix  $Z \in \mathbb{N}^{T \times M}$ 
1059 Sensor embedding tables  $\{E^{(m)} \in \mathbb{R}^{V \times d_{\text{model}}}\}_{m=1}^M$ 
1060 Temporal conv module MultiScaleConv1D
1061 Trend/residual block TrendResidualBlock
1062 Output: Event-channel sequence  $H \in \mathbb{R}^{T \times d_{\text{event}}}$ 
1063 for  $t \leftarrow 1$  to  $T$  do
1064   for  $m \leftarrow 1$  to  $M$  do
1065      $\mathbf{e}_{t,m} \leftarrow E^{(m)}[Z_{t,m}] \in \mathbb{R}^{d_{\text{model}}}$  // token embedding
1066   end
1067    $\mathbf{E}_t \leftarrow \text{Concat}(\mathbf{e}_{t,1}, \dots, \mathbf{e}_{t,M}) \in \mathbb{R}^{M \cdot d_{\text{model}}}$ 
1068 end
1069 Form sequence:  $E \leftarrow (\mathbf{E}_1, \dots, \mathbf{E}_T) \in \mathbb{R}^{T \times (Md_{\text{model}})}$ 
1070 // Temporal local pattern extraction
1071  $H_{\text{conv}} \leftarrow \text{MultiScaleConv1D}(E) \in \mathbb{R}^{T \times d_{\text{model}}}$ 
1072 // Trend/residual decomposition
1073  $H_{\text{trend}}, H_{\text{resid}} \leftarrow \text{TrendResidualBlock}(H_{\text{conv}})$ 
1074 // Fuse channels (e.g. add or concatenate)
1075  $H \leftarrow \text{Fuse}(H_{\text{trend}}, H_{\text{resid}}) \in \mathbb{R}^{T \times d_{\text{event}}}$ 
1076 return  $H$ 

```

Algorithm 3: Event-channel construction from per-sensor tokens

1077
1078 The backbone training loop (Algorithm 4) then uses sliding windows over the tokenized time series
1079 to perform next-step prediction across all sensors. This stage mirrors autoregressive pretraining

1080 in transformer-based language models: the model receives a context window of length L and is
 1081 trained to predict the next token for each sensor. Algorithm 4 outlines the multi-sensor cross-entropy
 1082 objective, the gradient clipping used for stability, and the use of schedulers to modulate learning
 1083 rates. A second, shorter finetuning stage on more recent data provides domain adaptation, allowing
 1084 the backbone to adjust to shifts in equipment behavior, sensor calibrations, and seasonal effects.
 1085 Through this two-stage training, the model internalizes both general temporal patterns and site- or
 1086 asset-specific nuances.

1087

```

1088 Input : Token matrix  $Z \in \mathbb{N}^{T \times M}$ 
1089           Context length  $L$ 
1090           Backbone model  $f_\theta$  (MultivariateTimeSeriesGPT)
1091           Loss  $\ell$  (cross-entropy over next-token per sensor)
1092           Optimizer  $\mathcal{O}$ , scheduler  $\mathcal{S}$ 
1093           Number of epochs  $E$ 
1094 Output: Trained parameters  $\hat{\theta}$ 
1095 // Split into train / finetune / eval by time
1096 Choose indices  $0 < T_{\text{train}} < T_{\text{finetune}} < T$ 
1097  $Z_{\text{train}} \leftarrow Z[1 : T_{\text{train}}]$ 
1098  $Z_{\text{finetune}} \leftarrow Z[T_{\text{train}} - L : T_{\text{finetune}}]$ 
1099  $Z_{\text{eval}} \leftarrow Z[T_{\text{finetune}} - L : T]$ 
1100 // Construct sliding-window datasets
1101 foreach dataset  $Z_\bullet \in \{Z_{\text{train}}, Z_{\text{finetune}}, Z_{\text{eval}}\}$  do
1102   Build samples  $(X^{(i)}, Y^{(i)})$  by:
1103    $X^{(i)} = Z[t : t + L - 1, :]$ 
1104    $Y^{(i)} = Z[t + 1 : t + L, :]$ 
1105   for all valid  $t$ .
1106 end
1107 Form DataLoaders  $\mathcal{D}_{\text{train}}, \mathcal{D}_{\text{finetune}}, \mathcal{D}_{\text{eval}}$ 
1108 // Core training loop (shown for one phase, e.g. pre-train)
1109 for epoch  $\leftarrow 1$  to  $E$  do
1110   for  $(X, Y)$  in  $\mathcal{D}_{\text{train}}$  do
1111     Move  $X, Y$  to device
1112      $\mathcal{O}.\text{zero\_grad}()$ 
1113      $\{\text{logits}^{(m)}\}_{m=1}^M \leftarrow f_\theta(X)$  // one head per sensor
1114      $L_{\text{batch}} \leftarrow 0$ 
1115     for  $m \leftarrow 1$  to  $M$  do
1116       Flatten time+batch dimension
1117        $L_{\text{batch}} \leftarrow L_{\text{batch}} + \ell(\text{logits}^{(m)}, Y^{(m)})$ 
1118     end
1119     Backprop:  $\nabla_\theta L_{\text{batch}}$ 
1120     Clip gradients:  $\|\nabla_\theta\| \leftarrow \min(\|\nabla_\theta\|, \tau)$ 
1121      $\mathcal{O}.\text{step}()$ 
1122      $\mathcal{S}.\text{step}()$  // StepLR scheduler
1123   end
1124 return  $\hat{\theta} \leftarrow \theta$ 

```

1125 **Algorithm 4:** Backbone training with sliding-window tokens

1126 Finally, the pipeline applies uncertainty calibration (Algorithm 5) and inference/alarm logic (Algo-
 1127 rithm 6) to transform raw model outputs into actionable operational signals. Calibration computes
 1128 per-sensor confidence thresholds that control false-alarm rates, ensuring the system's predictions
 1129 are interpretable and trustworthy for operators. During live inference, incoming sensor values are
 1130 tokenized in real time, fed through the trained backbone, and evaluated against these calibrated
 1131 thresholds. Low-confidence predictions level alarms that can be aggregated into equipment- or
 1132 system-level warnings. These are indicative of distributional shift, anomalous system behavior, or
 1133 emerging faults. The closed-loop design yields a scalable, unified architecture capable of handling
 1134 diverse sensors, providing robust forecasts, and surfacing early indicators of abnormal behavior in
 1135 complex industrial environments.

```

1134 Input : Trained backbone  $f_{\hat{\theta}}$ 
1135 Calibration dataset  $\mathcal{D}_{\text{cal}} = \{(X^{(i)}, Y^{(i)})\}$ 
1136 Target false-positive rate  $\alpha$  (e.g. 5%)
1137 Output: Per-sensor alarm thresholds  $\{\tau_m\}_{m=1}^M$ 
1138 Initialize list  $\mathcal{C}_m \leftarrow []$  for each sensor  $m$ 
1139 foreach  $(X, Y) \in \mathcal{D}_{\text{cal}}$  do
1140    $\{\text{logits}^{(m)}\}_{m=1}^M \leftarrow f_{\hat{\theta}}(X)$ 
1141   for  $m \leftarrow 1$  to  $M$  do
1142      $P^{(m)} \leftarrow \text{Softmax}(\text{logits}^{(m)})$  // per-time-step token distribution
1143     for each time step  $t$  do
1144        $p_{\max} \leftarrow \max_k P_{t,k}^{(m)}$ 
1145        $y_{t,m} \leftarrow \text{true token at } (t, m)$ 
1146        $k^* \leftarrow \arg \max_k P_{t,k}^{(m)}$ 
1147       if  $k^* = y_{t,m}$  then
1148         | Append  $p_{\max}$  to  $\mathcal{C}_m$ 
1149       end
1150     end
1151   end
1152 end
1153 for  $m \leftarrow 1$  to  $M$  do
1154   // Choose threshold so that only  $(1 - \alpha)$  of correct predictions
1155   // exceed it
1156    $\tau_m \leftarrow (1 - \alpha)\text{-quantile of } \mathcal{C}_m$ 
1157 end
1158 return  $\{\tau_m\}_{m=1}^M$ 
1159

```

Algorithm 5: Per-sensor uncertainty calibration

A.4.2 HYPERPARAMETERS

The preprocessing pipeline transforms raw industrial sensor data into a structured and model-ready time-series schema. Continuous sensor tags are first selected based on engineering relevance and data completeness, ensuring that only channels with sufficient coverage and operational variability are included in training. Raw sensor readings often contain missing values, spikes, calibration drifts, and irregular sampling intervals. To address these issues, all channels are aligned on a fixed temporal grid (e.g., 1-minute, 15-minute or hourly cadence) using forward-fill to handle short gaps and zero-fill for remaining missing segments. This alignment produces a dense, synchronized multivariate matrix where each row corresponds to a timestamp and each column corresponds to a specific sensor tag. These preprocessing steps define the foundation upon which the tokenization and modeling pipeline operates, and the specific hyperparameters associated with these stages are listed in Table 7.

Once the data are aligned, each continuous channel undergoes a discretization procedure based on empirical quantile binning. Instead of relying on fixed numerical thresholds, which may be overly sensitive to scale differences across sensors, the model computes 128 quantile bins per sensor, yielding a vocabulary of 130 discrete symbols after including special tokens. As described in Table 7, this per-sensor normalization scheme standardizes the effective distribution of the input signals, placing all channels on a comparable footing regardless of units, magnitude, or operating range. Unlike traditional z-score normalization, quantile binning inherently handles heavy-tailed distributions, outliers, and occasional faults. Because quantiles implicitly clip extreme readings, no explicit clip radius is required; rare excursions simply fall into the highest or lowest quantile categories. This produces a robust and stable discrete representation suitable for training large autoregressive models.

After tokenization, the complete dataset is segmented into temporal splits for training, validation, and evaluation. To mirror realistic deployment scenarios, the split is performed strictly along the time axis rather than randomly. Following the configuration summarized in Table 7, 70% of the earliest data are used for pretraining the backbone, the next 20% form a finetuning or calibration segment, and the final 10% constitute the held-out evaluation set. All windowed samples used for

```

1188 Input : Trained backbone  $f_{\hat{\theta}}$ 
1189     Bin edges  $\{\mathcal{B}_m\}_{m=1}^M$ 
1190     Thresholds  $\{\tau_m\}_{m=1}^M$  from Algorithm 5
1191     Context length  $L$ 
1192     Live stream of sensor values  $\{\mathbf{x}_t \in \mathbb{R}^M\}_{t=1}^{\infty}$ 
1193 Output: Online alarm indicators  $a_{t,m} \in \{0, 1\}$  for each time  $t$  and sensor  $m$ 
1194 Initialize token buffer  $Z_{\text{buf}} \leftarrow []$ 
1195 for  $t \leftarrow 1$  to  $\infty$  do
1196     // Step 1: tokenize new observation
1197     for  $m \leftarrow 1$  to  $M$  do
1198          $b_{t,m} \leftarrow \text{Digitize}(x_{t,m}; \mathcal{B}_m)$ 
1199          $z_{t,m} \leftarrow b_{t,m} + 2$ 
1200     end
1201     Append row  $\mathbf{z}_t$  to  $Z_{\text{buf}}$ 
1202     if  $|Z_{\text{buf}}| < L$  then
1203         continue // not enough context yet
1204     end
1205     if  $|Z_{\text{buf}}| > L$  then
1206         | Drop oldest row so that  $|Z_{\text{buf}}| = L$ 
1207     end
1208     // Step 2: model forward for next-step prediction
1209      $X \leftarrow Z_{\text{buf}}$  //  $L \times M$  window
1210      $\{\text{logits}^{(m)}\}_{m=1}^M \leftarrow f_{\hat{\theta}}(X)$ 
1211     for  $m \leftarrow 1$  to  $M$  do
1212          $P^{(m)} \leftarrow \text{Softmax}(\text{logits}_{\text{last time step}}^{(m)})$ 
1213          $p_{\max} \leftarrow \max_k P_k^{(m)}$ 
1214          $k^* \leftarrow \arg \max_k P_k^{(m)}$ 
1215         Optionally map  $k^*$  back to a predicted value  $\hat{y}_{t+1,m}$  (bin midpoint)
1216         // Step 3: alarm decision using calibrated threshold
1217         if  $p_{\max} < \tau_m$  then
1218             |  $a_{t+1,m} \leftarrow 1$  // low-confidence / anomalous
1219         else
1220             |  $a_{t+1,m} \leftarrow 0$ 
1221         end
1222     end
1223     Optionally: aggregate per-sensor alarms into equipment-level alarm (e.g. OR across
1224     selected sensors, require persistence for  $W$  steps, etc.)
1225 end

```

Algorithm 6: Streaming inference and alarm logic

1231 model input preserve chronological order: a sliding window of length $L = 168$ (approximately one
1232 week of hourly data) is extracted, and the prediction target corresponds to the next time step. Over-
1233 laps between windows are allowed, ensuring dense coverage of the training horizon. This temporal
1234 structuring eliminates leakage from future observations and ensures that the model's performance is
1235 representative of forward-looking industrial deployment.

1236 Finally, any event annotations or operational metadata (e.g., maintenance logs, fault codes, or operator
1237 interventions) are aligned to the same temporal grid as the continuous measurements. Although
1238 the backbone model is trained primarily on the continuous tokenized channels, these event streams
1239 can be incorporated downstream for evaluation, alarm validation, or supervised finetuning tasks.
1240 Together, these preprocessing steps establish a consistent and noise-resilient data schema, enabling
1241 the model to learn robust multivariate structure while maintaining full temporal integrity across the
1242 training, validation, and test phases.

1242 Table 7: Architectural and training hyperparameters for the foundation model.
1243

1244 Component	1245 Hyperparameter / Value
Tokenization	
1247 Quantization bins per sensor	128
1248 Vocabulary size	130 (128 bins + 2 special tokens)
1249 Normalization scheme	Per-sensor empirical quantile binning
1250 Clip radii	Not used / not required (robust quantiles handle extremes)
Architecture	
1252 Transformer depth (layers)	6
1253 Transformer width (d_{model})	128
1254 Feedforward dimension (d_{ff})	512
1255 Number of attention heads	8
1256 Dropout	0.1
1257 Maximum sequence length	10,000
1258 Event-channel construction	Multi-scale temporal convolution + trend/residual splitting
1259 Positional encoding	Learnable positional embeddings
1260 Attention variant	Trend-query spike-attention fusion
Windowing	
1262 Context window length	$L = 168$
1263 Window stride	1 (sliding window)
1264 Train/finetune/eval split	70%/20%/10% by time
Optimization	
1266 Optimizer	Adam (Kingma & Ba, 2017)
1267 Learning rate	10^{-3} to 10^{-5}
1268 Batch size	16
1269 Learning-rate warmup	Linear warmup for initial epochs
1270 Learning-rate decay	Cosine annealing + StepLR ($\times 0.1$ every 3 epochs)
1271 Gradient clipping	Enabled (per-step)
1272 Number of epochs	5–10 (convergence-dependent)
1273 Number of training steps (fine-tune)	1000
1274 Early stopping	Triggered when validation loss rises above threshold
Inference & Calibration	
1277 Calibration method	Per-sensor confidence thresholding
1278 Target false-positive rate	$\alpha = 0.05$ (example)
1279 Alarm decision rule	$p_{\text{max}} < \tau_m$ triggers alarm

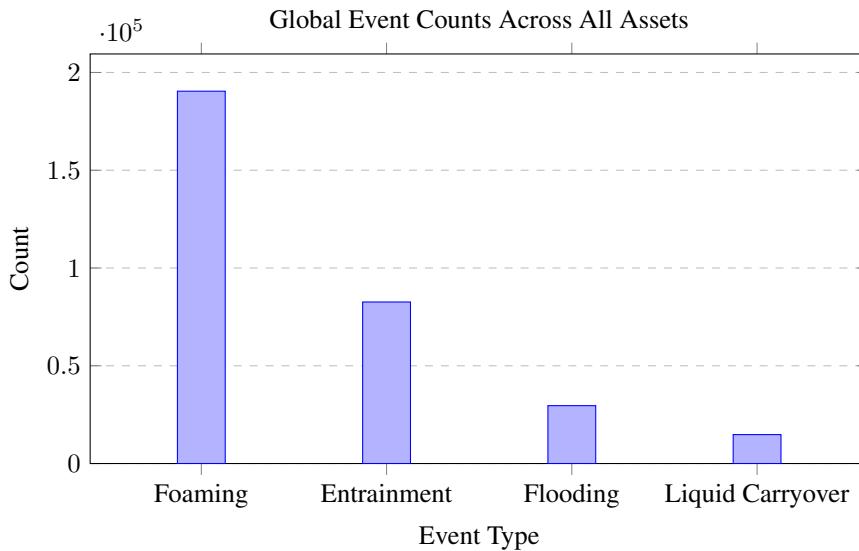
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1282 A.4.3 CORPUS STATISTICS
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1284 The full pretraining corpus spans four multivariate time-series asset types, each corresponding to a
1285 unique equipment or instrument tag that has been resampled to a uniform 1-minute grid. As summa-
1286 rized in Table 8, this results in a combined total of 26,144,880 synchronized time steps, representing
1287 approximately 435,748 hours ($\sim 18,156$ days) of continuous operating history. Because each asset
1288 contains multiple continuous sensor channels—ranging from 1 to over 50 depending on the equip-
1289 ment type—the discretized representation expands to more than 322 million tokens after per-sensor
1290 quantile binning. This scale places the dataset in a regime where long-horizon temporal depen-
1291 dencies, distributional shifts, and cross-sensor relationships are richly represented, providing a strong
1292 foundation for the AFM’s autoregressive pretraining stage.

1293 In addition to continuous telemetry, the corpus includes four semantic event channels that capture
1294 operational anomalies such as foaming, entrainment, flooding, and liquid carryover. Although events
1295 are sparse relative to the dense sensor grid, they occur frequently enough to supply meaningful
supervisory signal. These distributions, visualized in Figure 6, highlight the imbalanced nature of

1296 Table 8: Dataset and pretraining corpus statistics aggregated over all equipment types. All sensor
 1297 channels are resampled at 1-minute resolution.

Statistic	Value
Number of equipment types	4
Time coverage	2024-01-01 to 2025-10-07
Sampling interval	1 minute
Total time steps (T)	26,144,880
Total hours	435,748
Total days	18,156
Number of event channels	4
Total tokens after discretization	322,468,784



1327 Figure 6: Global counts of annotated events across all four equipment types.

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 1329
 1330 real industrial operations while underscoring the model’s need to generalize across both common
 1331 and rare failure modes.

1333 A.4.4 CALIBRATION AND DEPLOYMENT

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 1335 The calibration and deployment layer converts raw model probabilities into actionable and statisti-
 1336 cally reliable uncertainty estimates. After the backbone model has been trained, we evaluate its next-
 1337 step predictive distributions on a held-out calibration set constructed strictly from the most recent
 1338 portion of the time axis to reflect the distribution encountered during deployment. For each sensor,
 1339 the model outputs a categorical probability distribution across discretized quantile bins. To obtain
 1340 interval estimates in the original continuous domain, we invert token predictions into corresponding
 1341 bin midpoints and compute residual errors by comparing these predicted values against observed
 1342 measurements. These residuals form the empirical basis for interval construction: for each sensor,
 1343 we compute a calibration quantile (e.g., the 95th percentile of absolute errors) and form prediction
 1344 intervals of the form $[\hat{y}_t - q_{0.95}, \hat{y}_t + q_{0.95}]$. This quantile-based approach yields well-behaved
 1345 uncertainty intervals even under heavy-tailed, non-Gaussian, or heteroscedastic sensor noise.

1346 To further improve probability calibration beyond raw softmax outputs, we apply isotonic re-
 1347 gression independently to each sensor channel. Isotonic regression is a non-parametric, mono-
 1348 tone calibration mapping that transforms uncalibrated model confidences into empirically correct
 1349 probability estimates (Han et al., 2017). Concretely, for each sensor we collect calibration pairs
 $(p_{\max}, \mathbb{1}\{\hat{k} = k_{\text{true}}\})$ over the held-out calibration window, where p_{\max} is the model’s top-1 prob-

ability and the indicator denotes whether the predicted bin matches the true bin. We then fit a one-dimensional isotonic model that produces a calibrated confidence value $\tilde{p} = f_{\text{iso}}(p_{\text{max}})$. This procedure corrects systematic overconfidence or underconfidence that often arises in autoregressive time-series models, resulting in monotone and interpretable confidence estimates that better reflect actual predictive reliability.

For raising alarms, we implement a dual-gate thresholding mechanism that integrates both calibrated confidence and magnitude-based deviation metrics. The first gate is a confidence gate, which triggers whenever the calibrated confidence \tilde{p} falls below a sensor-specific threshold τ_m , chosen to achieve a target false-positive rate on the calibration dataset. This gate captures epistemic uncertainty: the system raises concern when the model becomes unsure of the expected dynamics (Wang & Ji, 2024). The second gate is a residual gate, which activates when the realized sensor reading y_t lies outside of the calibrated prediction interval derived from the residual quantile. This gate captures aleatoric deviations such as sudden spikes, gradual drifts, or anomalous excursions. A high-severity alarm is issued only when both gates are simultaneously activated, significantly reducing false positives while maintaining sensitivity to meaningful faults or emerging anomalous behavior.

During deployment, the calibrated thresholds, isotonic mappings, and interval statistics are fixed and applied deterministically to streaming data. Incoming sensor values are tokenized, processed by the backbone model, converted into predicted bins and midpoints, and evaluated through the dual-gate alarm logic. This results in a robust and reproducible alarm generation mechanism that is independent of training data idiosyncrasies. Because all calibration procedures depend only on observable error statistics rather than model internals, practitioners can reproduce or adapt the calibration layer on their own datasets without modifying the underlying model architecture or training methodology.

A.4.5 TRAINING COSTS

Training the AFM requires mixed computational resources due to the multiyear, multi-equipment dataset and the autoregressive modeling of long context windows. As described in the previous sections, pretraining is performed on NVIDIA V100 GPUs in a cloud cluster, each equipped with 32 GB of HBM2 memory. A single epoch over the combined field and simulator dataset takes approximately 24 hours on one V100 GPU, and typical training runs span 5–10 epochs depending on convergence behavior and early-stopping criteria. This corresponds to roughly 5–10 GPU-days of pretraining compute for a single foundation model checkpoint. Mixed-precision training and efficient attention implementations help reduce compute overhead, but the long temporal sequences and per-sensor tokenization still make pretraining the dominant component of the overall computational cost.

Table 9: Approximate computational costs and resource requirements for AFM training and calibration.

Training Stage	Resources	Approx. Runtime
Pretraining (per epoch)	1× NVIDIA V100 (32GB)	~24 hours
Finetuning	1× NVIDIA V100 (32GB)	< 1 hour
Calibration (intervals + isotonic + thresholds)	CPU only	Minutes

Fine-tuning and calibration are comparatively lightweight. Because the finetuning dataset is restricted to the most recent 20% of the time axis, and only a few thousand windows are required for domain adaptation, finetuning completes in less than one hour on a single V100 GPU. Calibration runs entirely on CPU and completes in minutes. These lighter downstream stages allow the AFM to be efficiently adapted to new assets or operating conditions without retraining the backbone. A summary of resource usage and timing is provided in Table 9.

A.4.6 CARBON FOOTPRINT

We estimate the carbon footprint of AFM pretraining using the MLCO2 methodology, which computes emissions as the product of total energy consumption and a region-specific carbon intensity factor. A single NVIDIA V100 GPU consumes approximately 300W under mixed-precision training load. Given that each epoch requires roughly 24 hours, one epoch consumes $0.3 \text{ kW} \times 24 \text{ h} =$

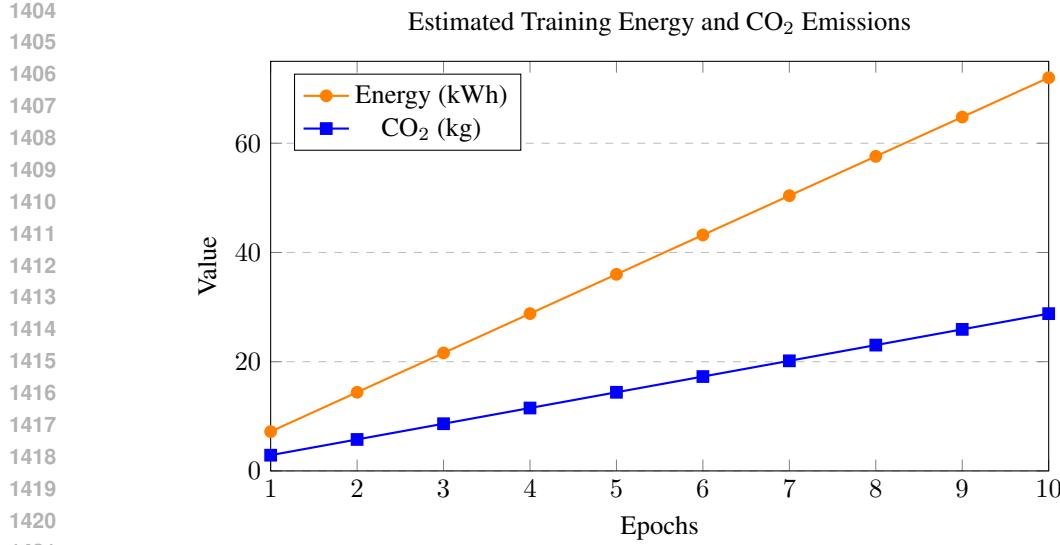


Figure 7: Estimated training energy consumption and CO₂ emissions across 1–10 epochs, assuming a 300W GPU, 24 hours per epoch, and a carbon intensity of 0.40 kg CO₂/kWh.

7.2 kWh. Using a representative carbon intensity of 0.40 kg CO₂/kWh, this corresponds to approximately 2.88 kg CO₂ per epoch. Over a typical pretraining run of 5–10 epochs, the total emissions range from 14–29 kg CO₂. While this footprint is modest compared to very large language models, it highlights the nontrivial cost of long-sequence time-series modeling, particularly when repeated for multiple equipment classes or initial deployments.

Because the AFM is designed as a reusable foundation model, pretraining is performed once and amortized across many downstream tasks, assets, and datasets. Finetuning and calibration incur negligible emissions in comparison—typically well below 0.1 kg CO₂ for a complete adaptation cycle—because these stages operate on narrow temporal windows and complete within minutes to an hour on a single GPU or CPU. This amortized structure greatly reduces the environmental impact per asset. A summary of the estimated carbon footprint across 1–10 epochs is shown in Figure 7.

A.5 NOVELTY

Building on the motivations outlined in Section 1, the distinctiveness of AFM becomes clearer when viewed in contrast to existing state-of-the-art (SOTA) foundation models. A core contribution of AFM is its shift from generic time-series foundation modeling toward an explicitly asset-centered, multichannel, and event-aligned architecture designed for industrial equipment. Existing SOTA models such as Chronos (Ansari et al., 2025), Moirai (Liu et al., 2025), Moment (Goswami et al., 2024), TimesFM (Das et al., 2024) and UniTS (Gao et al., 2024) are optimized for broad forecasting benchmarks where input sequences are clean, regularly sampled, and typically univariate or low-dimensional (e.g., ETT, Electricity, Exchange, Weather) (Zhou et al., 2021a). These models provide strong forecasting baselines, but they are not constructed to handle the heterogeneous, asynchronous, and event-driven telemetry characteristic of process equipment. AFM addresses this gap through modules that are absent in current SOTA: per-sensor discrete tokenization, multivariate event-channel fusion, and calibration-aware outputs. Unlike general-purpose foundation models, AFM is not a monolithic sequence forecaster; it is a domain-fitted backbone that integrates discrete alarms, set-point shifts, and maintenance logs as first-class temporal signals.

Another key novelty is unified representation learning across physics-driven sensors, operational events, and regime switches. Existing SOTA models are typically trained on smooth consumer or environmental datasets and therefore lack inductive biases to represent sharp transients, deadbands, control cycles, and operator interventions. AFM’s tokenization strategy compresses raw values into quantized distributions that are robust to sensor drift and provide a stable vocabulary across assets. When coupled with transformer pretraining over millions of minutes of operational data, the back-

1458
 1459 bone develops internal states that encode both latent physical regimes (e.g., fouling, load changes)
 1460 and event-conditioned transitions. None of the SOTA models support this cross-channel, multi-
 1461 modal regime encoding; most treat event labels as separate tasks and do not fuse them into the main
 1462 forecasting pathway.

1463 A further contribution is that AFM explicitly targets downstream operational tasks beyond fore-
 1464 casting, such as anomaly detection, event querying, alarm triage, and operator-facing explanations.
 1465 Modern SOTA foundation models focus almost exclusively on numeric forecasting accuracy and do
 1466 not provide calibrated intervals, provenance-aware explanations, or temporal reasoning over event
 1467 sequences. AFM, by nesting multiple lightweight task heads over a shared backbone, supports a
 1468 broader family of operations while maintaining consistent embeddings across tasks. This architec-
 1469 ture enables realistic workflows (e.g., cross-sensor root-cause queries or maintenance-linked alert
 1470 interpretation) that cannot be implemented using Chronos, TimesFM, or Moirai without substantial
 1471 post-hoc engineering. Thus, AFM is not only a forecasting model but a multifunctional operational
 1472 intelligence layer for industrial assets.

1473 Finally, empirical results highlight a distinctive advantage of AFM: consistent generalization across
 1474 heterogeneous equipment classes, something not achieved by SOTA models trained on internet-
 1475 aggregate data. In Table 1, AFM outperforms Chronos, Moirai, and TimesFM on nearly all in-
 1476 dustrial sensors, especially those influenced by multivariate interactions (e.g., contactor pressure,
 1477 exchanger inlet pressure, compressor exhaust temperature). These improvements are not simply nu-
 1478 matical gains; they reflect AFM’s architectural alignment with the physics and operational realities
 1479 of industrial systems. In contrast, SOTA foundation models—even very large ones—tend to underfit
 1480 sharp regime changes or overfit noise due to mismatched pretraining corpora. AFM’s novelty lies in
 1481 bridging this gap: delivering foundation-model-level generalization while remaining computa-
 1482 tionally efficient, domain-consistent, and operationally actionable for real industrial deployments.

1483 **A.6 DISCLOSURE: USE OF GENERATIVE AI**

1484 We did not use generative AI to generate ideas, methods, or results. We used large-language-
 1485 model tools only to (i) help surface related work during the literature scan and (ii) suggest word-
 1486 ing/grammar edits and peer-review style comments. All technical content and conclusions were
 1487 written and verified by the authors. We did not upload proprietary, confidential, or personal data to
 1488 any AI service.

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