FREETRAJ: TUNING-FREE TRAJECTORY CONTROL VIA NOISE GUIDED VIDEO DIFFUSION

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Paper under double-blind review

ABSTRACT

Diffusion model has demonstrated remarkable capability in video generation, which further sparks interest in introducing trajectory control into the generation process. While existing works mainly focus on training-based methods (*e.g.*, conditional adapter), we argue that diffusion model itself allows decent control over the generated content without requiring any training. In this study, we introduce a tuning-free framework to achieve trajectory-controllable video generation, by imposing guidance on both noise construction and attention computation. Specifically, 1) we first show several instructive phenomena and analyze how initial noises influence the motion trajectory of generated content. 2) Subsequently, we propose FreeTraj, a tuning-free approach that enables trajectory control by modifying noise sampling and attention mechanisms. 3) Furthermore, we extend FreeTraj to facilitate longer and larger video generation with controllable trajectories. Equipped with these designs, users have the flexibility to provide trajectories manually or opt for trajectories automatically generated by the LLM trajectory planner. Extensive experiments validate the efficacy of our approach in enhancing the trajectory controllability of video diffusion models. Generated video samples are available at the anonymous website: <https://FreeTraj.github.io>.

028 029 1 INTRODUCTION

030 031 032 033 034 035 036 037 038 039 040 041 042 Thanks to the powerful modeling capabilities of diffusion models, significant progress has been made in open-world visual content generation, as evidenced by numerous foundational text-to-video models [\(Wang et al., 2023b;](#page-13-0) [Chen et al., 2024b\)](#page-10-0). These models can generate vivid dynamic content based on arbitrary text prompts. However, while text prompts offer flexibility, they fall short of concretely expressing users' intentions, particularly regarding geometric control. Although existing trajectory control works primarily rely on training ControlNet-like structures [\(Wang et al., 2023c;](#page-13-1) [Chen et al., 2023d\)](#page-10-1), we contend that diffusion model itself contains the potential of substantial control over the generated content without necessitating additional training. In this paper, we aim to investigate the dynamics modeling mechanisms of video diffusion models and explore the possibility of explicitly controlling object trajectories by leveraging their internal properties. While most of the existing efforts are made by modifying text embeddings or adjusting attention mechanisms to enable control or editing [\(Ren et al., 2024;](#page-12-0) [Geyer et al., 2023\)](#page-11-0), the influence of initial noises on video motion remains under-explored.

043 044 045 046 047 048 049 050 051 052 053 For text-to-video diffusion models, there is considerable diversity in the generated content (*e.g.,* motion trajectories) from the same text prompt, depending on the choice of initial noises. This phenomenon motivates us to raise a question: Is it possible to regulate the motion trajectories with some designs over initial noises? FreeInit [\(Wu et al., 2023c\)](#page-13-2) has observed that low-frequency signals are more resistant to additive noises, which makes the diffusion model biased to inherit layout or shape information from the initial noises. Consequently, by arranging the low-frequency components of noises across frames, we can manipulate the inter-frame content correlation, *i.e.,* the temporal movements of the generated video. However, this constraint is not that reliable because the inter-frame region correlation is not directly aligned with object semantics. Prior works [\(Jain et al., 2023a;](#page-11-1) [Ma](#page-12-1) [et al., 2023a\)](#page-12-1) have demonstrated that trajectories can also be influenced by adjusting the attention weights assigned to different objects in some specific areas. Thus, to achieve object-level-based trajectory control, we propose to utilize text-based attention to locate the target objects in cooperation with noise space manipulation.

054 055 056 057 058 059 060 061 062 063 064 065 However, introducing alterations to the noise or attention mechanism carries the risk of causing artifacts in the generated videos. For example, applying a local mask to the self-attention operation can cause partially abnormal values because this diverges from the case encountered by the models during training. Furthermore, these minor anomalies can propagate through subsequent layers and become amplified in the following denoising steps, ultimately filling the target region with artifacts. We call such a phenomenon as *attention isolation*. Previous work [\(Jain et al., 2023a\)](#page-11-1) suffers from this problem and is easy to generate artifacts in the areas with masks. In our proposed FreeTraj system, we are fully aware of this issue and mitigate these risks by applying our operations to the noise and attention mechanisms with a tailor-made scheme. Instead of hard attention masks used in Peekaboo [\(Jain et al., 2023a\)](#page-11-1), our designed soft attention masks relieve the phenomenon of attention isolation. This approach strikes a balance between staying close to the training distribution and maintaining the ability to control trajectories.

066 067 068 069 070 071 072 073 074 075 076 077 In addition, FreeTraj can be seamlessly integrated into the long video generation framework, enriching the motion trajectories within the generated long videos. Current video generation models are typically trained on a restricted number of frames, leading to limitations in generating high-fidelity long videos during inference. FreeNoise [\(Qiu et al., 2023\)](#page-12-2) proposes a tuning-free and time-efficient paradigm for longer video generation based on pre-trained video diffusion models. Although FreeNoise brings satisfactory video quality and visual consistency, it has no guarantee for the various trajectories of generated objects, which are supposed to appear in long videos. With the help of some technical points proposed by FreeNoise, our FreeTraj successfully generates trajectory-controllable long videos. FreeTraj is also valuable in larger video generation. When we directly generate videos with resolutions larger than those in the model training process, we will easily get results with duplicated main objects [\(He et al., 2024\)](#page-11-2). However, FreeTraj will constrain the information of the main objects to the target areas. Signals of main objects are suppressed in other areas thus the duplication phenomenon will be reduced.

078 079 080 081 082 Our contributions are summarized as follows: 1) We investigate the mechanism of how initial noises influence the trajectory of generated objects through several instructive phenomenons. 2) We propose FreeTraj, an effective paradigm for tuning-free trajectory control with both noise guidance and attention guidance. 3) We extend the control mechanism to achieve longer and larger video generation with a controllable trajectory.

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2 RELATED WORK

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088 089 090 091 092 093 094 095 096 097 098 099 100 101 102 103 104 105 106 107 Diffusion Models for Visual Generation. Diffusion models have revolutionized image and video generation, showcasing their ability to produce high-quality samples. DDPM [\(Ho et al., 2020\)](#page-11-3) and Guided Diffusion [\(Dhariwal & Nichol, 2021\)](#page-10-2) are groundbreaking works that show diffusion models can generate high-quality samples. To improve efficiency, LDM [\(Rombach et al., 2022\)](#page-12-3) introduces latent space diffusion models that operate in a lower-dimensional space, reducing computational costs and training time, which serves as the foundation of Stable Diffusion. SDXL [\(Podell et al., 2023\)](#page-12-4) builds upon Stable Diffusion, achieving high-resolution image generation. Pixart-alpha [\(Chen et al.,](#page-10-3) [2023b\)](#page-10-3) replaces the backbone with a pure transformer, resulting in high-quality and cost-effective image generation. In terms of video generation, VDM [\(Ho et al., 2022b\)](#page-11-4) is the first video generation model that utilizes diffusion. LVDM [\(He et al., 2022\)](#page-11-5) takes it a step further by proposing a latent video diffusion model and hierarchical LVDM framework and achieves very long video generation. Align-Your-Latents [\(Blattmann et al., 2023b\)](#page-10-4) and AnimateDiff [\(Guo et al., 2023\)](#page-11-6) propose to insert temporal transformers into pre-trained text-to-image generation models to achieve text-to-video (T2V) generation. VideoComposer [\(Wang et al., 2023c\)](#page-13-1) presents a controllable text-to-video generation framework that is capable of controlling both spatial and temporal signals. VideoCrafter [\(Chen et al.,](#page-10-5) [2023a;](#page-10-5) [2024b\)](#page-10-0) and SVD [\(Blattmann et al., 2023a\)](#page-10-6) scale up the latent video diffusion model to large datasets. Lumiere [\(Bar-Tal et al., 2024\)](#page-10-7) introduces temporal downsampling to the space-time U-Net. Sora [\(OpenAI, 2024\)](#page-12-5) is a closed-source video generator that has impressive results announced most recently and has garnered much attention. In this work, we choose VideoCrafter 2.0 (referred to as VideoCrafter in the rest of the paper) as our pre-trained base model, as it is a current state-of-the-art open-sourcing model based on the comprehensive evaluations from Vbench [\(Huang et al., 2023b\)](#page-11-7) and EvalCrafter [\(Liu et al., 2023b\)](#page-12-6).

108 109 110 111 112 113 114 115 116 117 118 119 120 121 122 123 124 125 126 127 128 129 130 Trajectory Control in Video Generation. Given the critical role of motion in video generation, research on motion control in generated videos has garnered increasing attention. One intuitive method involves utilizing motion extracted from reference videos [\(Liu et al., 2023a;](#page-12-7) [Wei et al., 2023;](#page-13-3) [Zhao et al., 2023a;](#page-13-4) [Li et al., 2023;](#page-11-8) [Chen et al., 2024a;](#page-10-8) [Yatim et al., 2024\)](#page-13-5). For instance, approaches such as Tune-A-Video [\(Wu et al., 2023a\)](#page-13-6), MotionDirector [\(Zhao et al., 2023b\)](#page-13-7), and LAMP [\(Wu](#page-13-8) [et al., 2023b\)](#page-13-8) use specific videos as references to generalize their motions to various generated videos. Although these methods achieve significant motion control in video generation, they require training for each reference motion. To circumvent the need for specific motion training, ControlNet-like structures, such as VideoComposer [\(Wang et al., 2023c\)](#page-13-1) and Control-A-Video [\(Chen et al., 2023d\)](#page-10-1), employ depths, sketches, or moving vectors extracted from reference videos as conditions to control the motion of generated videos. However, these methods are limited to generating videos with pre-existing motions, constraining their creativity and customization. In contrast, controlling the motion of generated videos using trajectories or bounding boxes offers more flexibility and userfriendliness [\(Chen et al., 2023c;](#page-10-9) [Deng et al., 2023;](#page-10-10) [Wang et al., 2024;](#page-13-9) [Yang et al., 2024;](#page-13-10) [Huang](#page-11-9) [et al., 2023a\)](#page-11-9). While training-based methods [\(Chen et al., 2023c;](#page-10-9) [Yin et al., 2023a;](#page-13-11) [Deng et al.,](#page-10-10) [2023;](#page-10-10) [Wang et al., 2023d;](#page-13-12) [2024\)](#page-13-9) have demonstrated significant motion controllability, they demand substantial computing resources and are labor-intensive during data collection. Consequently, inspired by previous work applying attention mask for image editing [\(Hertz et al., 2022;](#page-11-10) [Cao et al., 2023\)](#page-10-11), several training-free trajectory control approaches [\(Yang et al., 2024;](#page-13-10) [Huang et al., 2023a\)](#page-11-9) have emerged. These methods, such as Peekaboo [\(Jain et al., 2023b\)](#page-11-11) and TrailBlazer [\(Ma et al., 2023b\)](#page-12-8), employ explicit attention control to direct the movement of generated objects according to specified trajectories. Our work also adopts a training-free approach. We enhance motion controllability in generated videos by imposing guidance on both noise construction and attention computation, resulting in improved performance in both motion control and video quality.

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3 METHODOLOGY

3.1 PRELIMINARIES: VIDEO DIFFUSION MODELS

135 136 137 138 139 140 Video Diffusion Models (VDM) [\(Ho et al., 2022a\)](#page-11-12) denotes diffusion models used for video generation, which formulates a fixed forward diffusion process to gradually add noise to the 4D video data $x_0 \sim p(x_0)$ and learn a denoising model to reverse this process. The forward process contains T timesteps, which gradually add noise to the data sample x_0 to yield x_t through a parameterization trick:

$$
q(\boldsymbol{x}_t|\boldsymbol{x}_{t-1})=\mathcal{N}(\boldsymbol{x}_t;\sqrt{1-\beta_t}\boldsymbol{x}_{t-1},\beta_t\boldsymbol{I}),\qquad q(\boldsymbol{x}_t|\boldsymbol{x}_0)=\mathcal{N}(\boldsymbol{x}_t;\sqrt{\bar{\alpha}_t}\boldsymbol{x}_0,(1-\bar{\alpha}_t)\boldsymbol{I}),\quad (1)
$$

142 143 where β_t is a predefined variance schedule, t is the timestep, $\bar{\alpha}_t = \prod_{i=1}^t \alpha_i$, and $\alpha_t = 1 - \beta_t$. The reverse denoising process obtains less noisy data x_{t-1} from the noisy input x_t at each timestep:

$$
p_{\theta}\left(\boldsymbol{x}_{t-1} \mid \boldsymbol{x}_{t}\right) = \mathcal{N}\left(\boldsymbol{x}_{t-1}; \boldsymbol{\mu}_{\theta}\left(\boldsymbol{x}_{t}, t\right), \boldsymbol{\Sigma}_{\theta}\left(\boldsymbol{x}_{t}, t\right)\right). \tag{2}
$$

Here μ_{θ} and Σ_{θ} are determined through a noise prediction network $\epsilon_{\theta}(x_t, t)$, which is supervised by the following objective function, where ϵ is sampled ground truth noise and θ is the learnable network parameters.

$$
\min_{\theta} \mathbb{E}_{t, \boldsymbol{x}_0, \boldsymbol{\epsilon}} \left\| \boldsymbol{\epsilon} - \boldsymbol{\epsilon}_{\theta} \left(\boldsymbol{x}_t, t \right) \right\|_2^2, \tag{3}
$$

151 152 153 154 155 156 157 158 Once the model is trained, we can synthesize a data point x_0 from random noise x_T by sampling x_t iteratively. Considering the high complexity and inter-frame redundancy of videos, Latent Diffusion Model (LDM) [\(Rombach et al., 2022\)](#page-12-3) is widely adopted to formulate the diffusion and denoising process in a more compact latent space. Latent Video Diffusion Models (LVDM) is realized through perceptual compression with a Variational Auto-Encoder (VAE) [Kingma & Welling](#page-11-13) [\(2014\)](#page-11-13), where an encoder \mathcal{E} maps $x_0 \in \mathbb{R}^{3 \times F \times H \times W}$ to its latent code $z_0 \in \mathbb{R}^{4 \times F \times H' \times W'}$ and a decoder \mathcal{D} reconstructs the video x_0 from the z_0 . Then, the diffusion model θ operates on the video latent variables to predict the noise $\hat{\epsilon}$.

$$
\boldsymbol{z}_0 = \mathcal{E}\left(\boldsymbol{x}_0\right), \quad \hat{\boldsymbol{x}}_0 = \mathcal{D}\left(\boldsymbol{z}_0\right) \approx \boldsymbol{x}_0, \quad \hat{\boldsymbol{\epsilon}} = \boldsymbol{\epsilon}_\theta(\boldsymbol{z}_t, \boldsymbol{y}, t), \tag{4}
$$

161 where y denotes conditions like text prompts. Most mainstream LVDMs [\(Blattmann et al., 2023b;](#page-10-4) [Wang et al., 2023b;](#page-13-0) [Chen et al., 2023a\)](#page-10-5) are implemented by a UNet equipped with convolutional

175 176 177 178 179 Figure 1: Noise resampling of initial high-frequency components. Gradually increasing the proportion of resampled high-frequency information in the frame-wise shared noises can significantly reduce the artifact in the generated video. However, this also leads to a gradual loss in trajectory control ability. A resampling percentage of 75% strikes a better balance between maintaining control and improving the quality of the generated video.

modules, spatial attentions, and temporal attentions. The basic computation block (whose feature input and output are h and h' respectively) could be denoted as:

 $\mathbf{h}' = TT(ST(Tconv(Conv(\mathbf{h}, t)), \mathbf{y}))$, TT = Proj_{in} \circ (Attn_{temp} \circ Attn_{temp} \circ MLP) \circ Proj_{out}. (5)

185 186 Here Conv and ST are residual convolutional block and spatial transformer, while Tconv denotes temporal convolutional block and TT denotes temporal transformers, serving as cross-frame operation modules.

3.2 NOISE INFLUENCE ON TRAJECTORY CONTROL

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190 191 192 193 194 195 196 During the training process of the video diffusion model, it cannot fully corrupt the semantics when adding noise, leaving substantial spatio-temporal correlations in the low-frequency components [\(Wu](#page-13-2) [et al., 2023c\)](#page-13-2). Those low-frequency correlations may still contain information about trajectory. Therefore, if we simulate the noises of the training process and manually add some spatio-temporal correlations in the low-frequency components, we have a chance to control the trajectory of the generated video.

197 198 199 200 Noise Flow. Our first attempt is to make the noise flow among frames. Instead of randomly sampling initial noises for all frames, we only sample the noise for the first frame. Then we move the noise from the top-left to the bottom-right with stride 2 and repeat this operation until we get initial noises z_T^{flow} for all frames. Specially, initial noise ϵ for each frame f in position $[i, j]$ is:

$$
\epsilon[i,j]^f = \epsilon[(i-2) \pmod{H}, (j-2) \pmod{W}]^{f-1}.
$$
 (6)

202 203 204 205 206 After denoising z_T^{flow} , although we will get a video with strong artifacts (Figure [1\)](#page-3-0), we can still find a valuable phenomenon: objects and textures in the video also flow in the same direction (top-left to bottom-right). This phenomenon verifies that the trajectory of the initial noises can guide the motion trajectory of generated results.

207 208 209 210 211 212 High-Frequency Noise Resampling. Artifacts in noise flow are mainly caused by deviation from the independent random distribution of the initial noises. Therefore, if we resample some new random independent noises to replace some dependent noises in z_T^{flow} , more realistic results are expected to be generated. According to the analysis of FreeInit [\(Wu et al., 2023c\)](#page-13-2), the trajectory information is mainly obtained in the low-frequency noise. Therefore, we use Fourier Transformation to resample high-frequency noise and get new latent $\tilde{z_T}$ to perform further denoising:

$$
\mathcal{F}_{z_T}^{low} = \mathcal{FFT}_{3D} (z_T) \odot \mathcal{H},
$$

\n
$$
\mathcal{F}_{\eta}^{high} = \mathcal{FFT}_{3D}(\eta) \odot (1 - \mathcal{H}),
$$

\n
$$
z_T = \mathcal{IFFT}_{3D} (\mathcal{F}_{z_T}^{low} + \mathcal{F}_{\eta}^{high}),
$$
\n(7)

Figure 2: Trajectory control via frame-wise shared low-frequency noise. The success cases on the left demonstrate that the moving objects in the generated videos can be roughly controlled by sharing low-frequent noise across the bounding boxes of the given trajectory. However, the precision of control and the success rate remain somewhat constrained, as evidenced by the failure instances on the right.

238 239 240 241 242 where \mathcal{FFT}_{3D} is the Fast Fourier Transformation operated on both spatial and temporal dimensions, and \mathcal{IFFT}_{3D} is the Inverse Fast Fourier Transformation that maps noise back from the blended frequency domain. H is the spatial-temporal Low Pass Filter (LPF), which is a tensor of the same shape as the latent. η is a newly sampled random noise to replace the high-frequency of the original noise. In this case, $z_T = z_T^{flow}$.

243 244 245 246 247 Figure [1](#page-3-0) shows that the visual quality is significantly improved as the proportion of high-frequency noise resampled increases. Correspondingly, the flow phenomenon is weakened. When 90% highfrequency noise is resampled, the flow is almost stopped with only some similar textures remaining (*e.g.,* branches from top-left to bottom right). Overall, 75% resampling strikes a good balance between sportiness and image quality.

248 249 250 251 252 Trajectory Injection. In noise flow, all objects in the foreground and background tend to move toward the direction of flow. If we only control the flow happening in the local area with some trajectories, can we guide the only main object to move following the corresponding trajectories? To answer it, we design some trajectories from simple to complex and make the flow area occupy a quarter of the area, as shown in the first row of Figure [2.](#page-4-0)

253 254 255 256 Instead of directly denoising random noises, we inject trajectory into the initial noises. We first initialize a random local noise ϵ_{local} according to the area of the input mask and F frames of random noises $[\epsilon_1, \epsilon_2, ..., \epsilon_F]$ independently. Then for each frame f, the initial noise ϵ_f will be replaced by the ϵ_{local} if in the area of the input mask:

257 258 259

260 261 $\tilde{\epsilon_f}[i,j] = \begin{cases} \epsilon_f[i,j] & \text{if } M_f[i,j] = 0 \\ \frac{\epsilon_f[i,j]}{[i,j]} & \text{if } M_f[i,j] = 1 \end{cases}$ $\epsilon_{local}[i^*, j^*]$ if $M_f[i, j] = 1$, (8)

262 263 264 where ϵ_f , $\epsilon_{local} \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$, M_f is the input mask of frame f, and $M_f[i, j] = 1$ if the position (i, j) is inside the bounding box of trajectory. $M_f[i, j] = 0$ otherwise. (i^*, j^*) is the corresponding local position in the box.

265 266 267 268 269 As shown in the left of Figure [2,](#page-4-0) some objects are well generated and follow the trajectory injected in initial noises although they may not be fully aligned with the given bounding boxes. While these objects move along the trajectory, they will also try to follow the prior knowledge of the physical world contained in the model (*e.g.* dolphins cannot go too far from the sea after jumping). And the right of Figure [2](#page-4-0) shows some failure cases. They are either poor in visual quality or in trajectory alignment.

Figure 3: An overview of FreeTraj. Our framework mainly contains two parts: guidance in noise and guidance in attention. For noise, we inject the target trajectory into the low-frequency part. For attention, we design different reweighing strategies according to the supposed behaviors in different attention layers. Here S, M_{CA} , M_{SA} , and M_{TA} are different attention masks.

Based on those observations, although we can utilize initial noises to guide the trajectory, we still need to involve additional control mechanisms to achieve accurate trajectory control, especially when the target trajectory deviates from a prior knowledge of the physical world contained in the model.

3.3 THE FRAMEWORK OF FREETRAJ

Given a target bounding box for a foreground object in the video, we suppose the pre-trained video model to generate results whose trajectory is aligned with the given box. To achieve that, we propose FreeTraj, which designs guidance in both noise and attention as shown in Figure [3.](#page-5-0)

3.3.1 GUIDANCE IN NOISE

296 297 298 299 As analyzed in Section [3.2,](#page-3-1) frame-wise shared low-frequency noise can guide the trajectory of generated objects. Therefore, we inject trajectory in the initial noises through Equation [8.](#page-4-1) To reduce the phenomena of attention isolation, we still need to remove some of the injected noises through High-Frequency Noise Resampling (Equation [7\)](#page-3-2).

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3.3.2 GUIDANCE IN ATTENTION

302 303 304 305 306 307 308 309 310 311 Object trajectories in generated videos with only noise guidance still tend to follow the prior information of the video model. In addition, the controlled object will be automatically selected by the model according to the training data distribution and cannot be manually specified. To make the control more precise and assignable, we also add trajectory guidance in attention. There are three kinds of attention layers in the UNet of VideoCrafter [\(Chen et al., 2024b\)](#page-10-0): spatial cross-attention, spatial self-attention, and temporal self-attention. Unlike previous work Peekaboo [\(Jain et al., 2023a\)](#page-11-1) directly masks the foreground and background respectively for all attention layers, we design different strategies according to the supposed behaviors in different attention layers. All attention editing is performed in the early steps $t \in \{T, \ldots, T - N\}$ of the denoising process, where T is the total number of denoising timesteps, and N is the number of timesteps for attention editing.

312 313 314 315 316 317 318 Attention Isolation. We find the previous designs in attention may cause attention isolation. It is a phenomenon that some regions become isolated either spatially or temporally and rarely pay attention to information outside their own region. This is often caused by the values in this area deviating too much from the training distribution. Unlucky, it is difficult for this region to restore itself to normal levels through valuable information from the other regions due to the isolation. Therefore, it is necessary to avoid attention isolation when we modify the attention mechanism without re-training. We will discuss more in the ablation study and appendix.

319 320 321 322 323 Cross Attention Guidance. Spatial cross-attention is the only place for prompts to inject the information from text embedding. Originally, the model would assign the object according to the prompts and initial noises. It is a random and unpredictable behavior. To force the model to only generate the target object in the given bounding box, we first add guidance to the cross-attention. Given query Q, key K, value V of cross-attention, and the re-scaled binary 2D attention masks M_a and M_a^j , which indicate the foreground and background areas of the generated video respectively.

Our guided cross-attention is:

$$
\text{GuidedCrossAttention}(Q, K, V, M_a, M'_a) = (\text{softmax}\left(\frac{QK^T}{\sqrt{d}} + \mathcal{M}\right) + \mathcal{S})V,
$$
\n
$$
\text{where } \mathcal{S}[i, j] = \begin{cases} 0 & \text{if } M_a[i, j] = 0 \\ \alpha g(i, j) & \text{if } M_a[i, j] = 1 \end{cases}, \text{and } \mathcal{M}[i, j] = \begin{cases} -\infty & \text{if } M'_a[i, j] = 0 \\ 0 & \text{if } M'_a[i, j] = 1 \end{cases} \tag{9}
$$

331 332 333 334 335 Here α is a coefficient to enhance the influence of target prompts in the foreground and $g(\cdot, \cdot)$ is a Gaussian weight [\(Ma et al., 2023a\)](#page-12-1). Note that the attention masks $M_a, M'_a \in \{0,1\}^{d_q \times d_k}$, where d_q and d_k are the lengths of queries and keys, respectively. They are attained with a given prompt P and the target mask $M_{\text{target}}^f[i]$ of frame $f(M_{\text{target}}^f[i]$ is a 1-D flatten form of M_f in Eq. [8\)](#page-4-1). In the cross-attention layer, M_a and M'_a are respectively denoted as M_{CA} and M'_{CA} , where

$$
M_{CA}^f[i,j] = \text{fg}\left(M_{\text{target}}^f[i]\right) * \text{fg}(P[j]),
$$

$$
M_{CA}^f[i,j] = \left(1 - \text{fg}\left(M_{\text{target}}^f[i]\right)\right) * (1 - \text{fg}(P[j])),
$$
\n(10)

340 341 where fg is a function that takes a pixel or a text token as input, returning 1 if it corresponds to the foreground of the video, and 0 otherwise.

342 343 344 345 Self Attention Guidance. Self-attention consists of the spatial part and temporal part. Without mandatory constraints, the information in the foreground and background will interact. In this case, the video model may still generate target objects at unexpected locations. Therefore, we design guided self-attention:

$$
\frac{346}{347}
$$

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$$
\text{GuidedSelfAttention}(Q, K, V, M_a) = \text{softmax}\left(\frac{QK^T}{\sqrt{d}} \odot \mathcal{W}\right) V,
$$
\n
$$
\text{where } \mathcal{W}[i, j] = \begin{cases} \beta & \text{if } M_a[i, j] = 0\\ 1 & \text{if } M_a[i, j] = 1 \end{cases} \tag{11}
$$

Here β is a coefficient to weaken the influence of the interaction of foreground and background. Compared to the hard mask using $-\infty$ to forbid the interaction of foreground and background, this soft mask design can avoid some artifacts caused by attention isolation.

The attention mask M_a designed in self-attention follows the Peekaboo [\(Jain et al., 2023a\)](#page-11-1). Specifically, in the spatial self-attention layer, M_a is denoted as M_{SA} , where

$$
M_{SA}^{f}[i,j] = \text{fg}\left(M_{\text{target}}^{f}[i]\right) * \text{fg}\left(M_{\text{target}}^{f}[j]\right) + \left(1 - \text{fg}\left(M_{\text{target}}^{f}[i]\right)\right) * \left(1 - \text{fg}\left(M_{\text{target}}^{f}[j]\right)\right),
$$
\n(12)

and in the temporal self-attention layer, M_a is denoted as M_{TA} , where

$$
M_{TA}^{i}[f,k] = \text{fg}\left(M_{\text{target}}^{f}[i]\right) * \text{fg}\left(M_{\text{target}}^{k}[i]\right) + \left(1 - \text{fg}\left(M_{\text{target}}^{f}[i]\right)\right) * \left(1 - \text{fg}\left(M_{\text{target}}^{k}[i]\right)\right).
$$
\n(13)

3.4 LONGER VIDEO GENERATION

368 369 370 371 FreeTraj can also be seamlessly integrated into the longer video generation framework FreeNoise [\(Qiu](#page-12-2) [et al., 2023\)](#page-12-2) to generate rich motion trajectories in long videos. FreeNoise mainly applies Local Window Fusion to the temporal attention to guarantee visual quality and utilize Noise Rescheduling in the noise initialization to reserve video consistency.

372 373 374 375 376 377 Local Window Fusion divides the temporal attention into several overlapped local windows along the temporal dimension and then fuses them together. In order to cooperate with Local Window Fusion, our guidance in temporal attention is only applied within each Local Window Fusion. Noise Rescheduling reuses and shuffles the sub-fragment of initial noises. To avoid our guidance in noise being destroyed, Equation [8](#page-4-1) and Equation [7](#page-3-2) are applied after Noise Rescheduling. Through the combined new framework, our method can achieve trajectory control over a long video sequence without any fine-tuning (Figure [7](#page-16-0) in the appendix).

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Table 1: Quantitative comparison of trajectory control. FreeTraj achieves competitive performance in metrics about video quality and gains the best scores in metrics that are related to trajectory control.

Method	FVD (L)	KVD (L)	CLIP-SIM $(†)$	mIoU $($ ^{$\dagger)$}	CD (
Direct	118.19	-2.28	0.980	0.161	0.225
MotionCtrl (Wang et al., 2023d)	825.80	68.07	0.939		0.248
MotionCtrl-256 (Wang et al., 2023d)	601.35	47.60	0.938	\equiv	0.245
Peekaboo (Jain et al., 2023a)	403.00	25.30	0.963	0.235	0.179
TrailBlazer (Ma et al., 2023a)	556.00	42.14	0.958	0.179	0.219
Ours	436.22	29.85	0.956	0.281	0.154
Ours-ShortMove	369.22	21.00	0.971	0.344	0.119

Figure 4: **Qualitative comparison of trajectory control.** We compare our proposed FreeTraj with direct inference (Direct), Peekaboo (Peek), and TrailBlazer (TraB). FreeTraj successfully generates high-fidelity results and is more accurate for trajectory control.

4 EXPERIMENTS

Based on performance and accessibility considerations, we choose the recently published open-source video diffusion model, VideoCrafter [\(Chen et al., 2024b\)](#page-10-0), as our pre-trained video model in this paper. All experiments are conducted based on this model. The inference resolution is fixed at 320×512 pixels and the video length is 16 frames unless stated otherwise.

417 418 419 420 421 422 423 424 425 426 Evaluation Metrics. To evaluate video quality, we report Fréchet Video Distance (FVD) [\(Unterthiner](#page-12-9) [et al., 2018\)](#page-12-9), Kernel Video Distance (KVD) [\(Unterthiner et al., 2019\)](#page-12-10). Since the tuning-free methods are supposed to keep the quality of the original pre-trained inference, we calculate the FVD and KVD between the original generated videos and videos generated by trajectory control methods. We use CLIP Similarity (CLIP-SIM) [\(Radford et al., 2021\)](#page-12-11) to measure the semantic similarity among frames. In addition, we utilize the off-the-shelf detection model, OWL-ViT-large [\(Minderer et al.,](#page-12-12) [2022\)](#page-12-12), to obtain the bounding box of the synthesized objects. Then Mean Intersection of Union (mIoU) and Centroid Distance (CD) are calculated to evaluate the trajectory alignment. CD is the distance between the centroid of the generated object and the input mask, normalized to 1. When OWL-ViT-large fails to detect the target object in the generated videos, the farthest point will be assigned as the penalty in CD.

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428 4.1 EVALUATION OF TRAJECTORY CONTROL

430 431 We first directly sample videos using the pre-trained model without trajectory control as a base reference. Then we compare our proposed FreeTraj to other trajectory-controllable video generation methods with diffusion models, MotionCtrl [\(Wang et al., 2023d\)](#page-13-12), Peekaboo [\(Jain et al., 2023a\)](#page-11-1) and **433 434** Table 2: User study. Users are requested to pick the best one among our proposed FreeTraj with the other baseline methods in terms of trajectory alignment, video-text alignment, and video quality.

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"A camel walking in a desert landscape."

"A bear running in the ruins, photorealistic, 4k, high definition."

Figure 5: Qualitative results with short movements. As shown in all generated 16 frames, the video quality and motion coherence are well preserved when we only require FreeTraj to generate some results with short movements (like from left to right or reverse).

458 459 460 461 462 463 464 TrailBlazer [\(Ma et al., 2023a\)](#page-12-1). MotionCtrl achieves trajectory control with the trainable object motion control module, requiring re-training for each base model. To support the input format of MotionCtrl, we convert the sequence of bounding boxes to the sequence of central points and omit the mIoU. In addition, MotionCtrl only releases one version for trajectory control which is trained on 256×256 resolution. However, the resolution of our baseline is 320×512 . For a fair comparison, we report the results of both resolutions. Peekaboo and TrailBlazer are two tuning-free methods that control trajectory through masked attention.

465 466 467 468 469 470 471 472 473 474 475 476 477 478 As shown in the first line of Figure [4,](#page-7-0) the original pre-trained VideoCrafter tends to generate objects that act around the center of the frame with limited movements. MotionCtrl can control the trajectory of objects but does not force the object center to align with the trajectory accurately, thus gaining a poor CD score. Notably, the object motion control module of MotionCtrl lacks transferability thus obtains worse performance in 320×512 . In addition, the frame quality of MotionCtrl is obviously inferior to that of other methods because it is trained based on VideoCrafter1 while can not be integrated into VideoCrafter2 directly. TrailBlazer is weak in control because it only applies the control in spatial cross-attention and temporal self-attention while information will leak through spatial self-attention. Videos generated by Peekaboo follow the given trajectory controls better because all kinds of attention are masked without information leakage. However, Peekaboo generates an additional black swan with weird artifacts, which is probably caused by the hard attention mask used in self-attention layers. Our FreeTraj controls trajectory via the combined effect of initial noise and attention layers, thus succeeding in driving the target object following the given trajectories with vivid motions. Our method also achieves competitive scores in FVD, KVD, and CLIP-SIM, which exhibits the reliable video quality generated by our method.

479 480 481 482 483 484 485 User Study. Furthermore, we conducted a user study to evaluate our results based on human subjective perception. Participants were asked to watch the generated videos from all methods, with each example displayed in a random order to avoid bias. They were then instructed to select the best video in three evaluation aspects: trajectory alignment, video-text alignment, and video quality. The results, as shown in Table [2,](#page-8-0) demonstrate that our approach outperforms the baseline methods by a significant margin, achieving the highest scores in all aspects. Notably, our method received nearly 70% votes in terms of trajectory alignment. This user study confirms the superiority of our approach in terms of trajectory alignment, video-text alignment, and video quality.

Figure 6: **Ablation results.** (a) No noise guidance, (b) no high-frequency noise resampling, (c) hard attention mask, and (d) our whole method.

Movement Scale. We evaluate control abilities on some complex trajectories (*e.g.*, top-left \rightarrow bottom-left \rightarrow bottom-right) within 16 frames. However, even for a real video, presenting such a long-range movement within 16 frames may lead to either motion incoherence or motion blur. Therefore, we also add some examples with shorter movements (*e.g.*, left \rightarrow right), whose range of movement is close to the setting of previous works. As shown in Figure [5,](#page-8-1) the video quality and motion coherence are well preserved. In addition, short movements also bring better FVD and KVD because this behavior is similar to reference videos directly generated by VideoCrafter.

4.2 ABLATION STUDIES

511 512 513 Ablation of Noise Guidance. To show the effectiveness of noise guidance, we run our designed attention guidance solely. Figure [6](#page-9-0) (a) shows that pure attention guidance can also control the trajectory but may lose some accuracy.

514 515 516 517 518 519 520 521 522 523 Ablation of Attention Isolation. We also study two settings that may cause attention isolation. The first one uses no high-frequency noise resampling when applying trajectory injection in initial noises (Equation [7\)](#page-3-2). The second one employs the hard attention mask in Equation [11.](#page-6-0) Usually, diffusion models have some robustness to deal with the input with small deviation and recover it to generate qualified results. However, both of these two strategies will easily cause the value of the attention layer to deviate far from the data distribution in the training stage. It will lead to attention isolation where isolated regions almost pay no attention to other regions, losing the chance to recover back to the normal distribution. As shown in Figure [6](#page-9-0) (b) and (c), blocky artifacts appear and follow the given trajectory in the generated videos. In addition, those artifacts happen to fall at the position of the attention mask or inject local noise.

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5 CONCLUSION

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527 528 529 530 531 532 533 534 535 536 537 538 539 In conclusion, our study has revealed several instructive phenomenons about how initial noises influence the generated results of video diffusion models. Leveraging the noise guidance and combining it with careful modifications to the attention mechanism, we introduce a tuning-free framework, FreeTraj, for trajectory-controllable video generation using diffusion models. We demonstrate that diffusion models inherently possess the capability to control generated content without additional training. By guiding noise construction and attention computation, we enable trajectory control and extend it to longer and larger video generation. Although not shown in this paper, our approach offers flexibility for users to provide trajectories manually or automatically generated by the LLM trajectory planner. Extensive experiments validate the effectiveness of our approach in enhancing the trajectory controllability of video diffusion models, providing a practical and efficient solution for generating videos with desired motion trajectories. However, this tuning-free paradigm is still limited by the underlying model, such as the consistency of object appearance that easily changes during large movements. We hope the study of initial noises can also inspire the training strategy of basic video models.

540 541 6 ETHICS STATEMENT

The primary objective of this project is to empower individuals without specialized expertise to create video art more effectively. Our paradigm, based on the pre-trained video diffusion model, assists the model in generating trajectory-controllable videos. It is important to note that the content generated by our tuning-free paradigm remains rooted in the original model. As a result, regulators only need to oversee the original video generation model to ensure adherence to ethical standards, and our algorithm does not introduce any additional ethical concerns.

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7 REPRODUCIBILITY STATEMENT

We have introduced the algorithm and implementation details in detail in the paper. A researcher familiar with the video diffusion model should be able to reproduce our method. In addition, we will release our code after acceptance for better promotion.

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Overview. In the supplementary material, we introduce implementation details in Section [A,](#page-14-0) show longer and larger results in Section [B,](#page-15-0) and finally, sharing more observations in Section [C.](#page-17-0)

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A APPENDIX: IMPLEMENTATION

761 762 A.1 HYPERPARAMETERS

763 764 765 766 767 768 During sampling, we perform DDIM sampling [\(Song et al., 2020\)](#page-12-13) with 50 denoising steps, setting DDIM eta to 0. The inference resolution is fixed at 320×512 pixels and the video length is 16 frames in the normal setting. The video length of longer inference is 64 frames and the inference resolution of larger inference is 640×512 pixels. The scale of the classifier-free guidance is set to 12.
 α in Equation 11 is 0.01. The kernel α in Equation [9](#page-6-1) is $\frac{0.25}{len_target_prompts \times proportion_target_box}$ and β in Equation [11](#page-6-0) is 0.01. The kernel division in Equation [9](#page-6-1) is 3.0 and the kernel shape is the same as the mask shape.

769 770 771 772 773 774 For quantitative comparison, we generate a total of 896 videos for each inference method, utilizing 56 prompts. We initialize 16 random initial noises for each prompt for direct inference. For trajectory control methods, each prompt is applied to 8 different trajectories with 2 random initial noises. The height and width of the trajectory bounding box are randomly chosen as 0.3, 0.35, or 0.4 of the canvas size.

775 776 777 In the user study, we mixed our generated videos with those generated by the other three baselines. A total of 27 users were asked to pick the best one according to the trajectory alignment, video-text alignment, and video quality, respectively.

A.2 PROMPTS

780 781 782 Our prompts are mostly extended from previous baselines[\(Jain et al., 2023a;](#page-11-1) [Ma et al., 2023a\)](#page-12-1) but replace some prompts that conflict with object movement, like standing or lying.

783 784 785 786 787 788 789 790 791 792 793 794 795 796 797 798 799 800 801 802 803 804 805 806 807 808 809 • A woodpecker climbing up a tree trunk. • A squirrel descending a tree after gathering nuts. • A bird diving towards the water to catch fish. • A frog leaping up to catch a fly. • A parrot flying upwards towards the treetops. • A squirrel jumping from one tree to another. • A rabbit burrowing downwards into its warren. • A satellite orbiting Earth in outer space. • A skateboarder performing tricks at a skate park. • A leaf falling gently from a tree. • A paper plane gliding in the air. • A bear climbing down a tree after spotting a threat. • A duck diving underwater in search of food. • A kangaroo hopping down a gentle slope. • An owl swooping down on its prey during the night. • A hot air balloon drifting across a clear sky. • A red double-decker bus moving through London streets. • A jet plane flying high in the sky. • A helicopter hovering above a cityscape. • A roller coaster looping in an amusement park. • A streetcar trundling down tracks in a historic district. • A rocket launching into space from a launchpad.

862 863 A-Story [\(He et al., 2023\)](#page-11-16) achieves multi-scene long video generation via character consistency. Streamingt2v [\(Henschel et al., 2024\)](#page-11-17) and FlexiFilm [\(Ouyang et al., 2024\)](#page-12-15) are training-based methods that train a conditional module on top of pre-trained video diffusion models conditioning on previous

 Þ "A corgi running on the grassland in the snow." "A dark knight riding a horse on the grassland." Figure 7: Longer video generation. Longer video generation allows us to plan some complex trajectories. FreeTraj succeeds in generating rich motion trajectories in long videos. Direct **Ours** "A fox running in a forest clearing." "A lion running on the grasslands." "A dark knight riding a horse on the grassland." Figure 8: **Larger video generation.** Directly generating larger videos will easily lead to the results with duplicated main objects anywhere. FreeTraj plans the trajectory for the main object and suppresses the duplication phenomenon. frames. Genlvideo [\(Wang et al., 2023a\)](#page-13-15) and FreeNoise [\(Qiu et al., 2023\)](#page-12-2) are recently proposed tuning- free methods for generating longer videos based on pre-trained video diffusion models to extend their generated length. In this work, we propose a tuning-free approach for long video generation based on long-term trajectory control. B.2 RESULTS OF LONGER GENERATION FreeTraj can be integrated into the longer video generation framework FreeNoise [\(Qiu et al., 2023\)](#page-12-2). With the help of some technical points proposed by FreeNoise, our FreeTraj successfully generated trajectory-controllable long videos. As shown in Figure [7,](#page-16-0) we plan two complex paths and FreeTraj succeeds in generating rich motion trajectories in long videos. B.3 RESULTS OF LARGER GENERATION When we directly use pre-trained video diffusion models to generate videos with higher resolutions compared to those in training, they will easily generate results with duplicated main objects any- where [He et al.](#page-11-2) [\(2024\)](#page-11-2). However, FreeTraj will plan the trajectory for the main object, and information

918 919 920 921 922 923 924 925 926 927 928 929 f_c^{low} Resample 50% Resample 75% Resample 90% Resample 100% Frame 1 Full z_{τ}^{flow} Frame 8 Frame 15

Figure 9: Noise resampling of initial high-frequency components. Gradually increasing the proportion of resampled high-frequency information in the frame-wise shared noises can significantly reduce the artifact in the generated video. However, this also leads to a gradual loss in trajectory control ability. A resampling percentage of 75% strikes a better balance between maintaining control and improving the quality of the generated video.

about the main object will be reduced out of the target areas. Therefore, the duplication phenomenon will be suppressed by FreeTraj (Figure [8\)](#page-16-1).

C APPENDIX: MORE OBSERVATIONS

C.1 MORE ABOUT NOISE FLOW

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Here we show another direction of noise flow. Instead of randomly sampling initial noises for all frames, we only sample the noise for the first frame. Then we move the noise from the bottom-left to the top-right with stride 2 and repeat this operation until we get initial noises z_T^{flow} for all frames. Specially, initial noise ϵ for each frame f in position $[i, j]$ is:

$$
\epsilon[i,j]^f = \epsilon[(i+2) \text{ (mod } H), (j-2) \text{ (mod } W)]^{f-1}.
$$
 (14)

949 950 951 952 953 After denoising z_T^{flow} , results in Figure [9](#page-17-1) show that objects and textures in the video also flow in the same direction (bottom-left to top-right). This phenomenon verifies that the trajectory of the initial noises can have an impact on the motion trajectory of the generated result. When the proportion of high-frequency noise resampled increases, the visual quality is significantly improved. Correspondingly, the flow phenomenon is weakened.

956 The initial noise guidance also works for some other similar base video models. As shown in Figure [10,](#page-18-0) the Noise Flow phenomenon still holds on AnimateDiff [\(Guo et al., 2023\)](#page-11-6).

957 958 C.2 ATTENTION ISOLATION IN TEMPORAL DIMENSION

959 960 Usually, we initialize 16 frames of random noises independently. Instead of normal sampling, we try partial repeated sampling by partially repeating some initial noises:

Normal Sampling:
$$
[\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4, \epsilon_5, \epsilon_6, \epsilon_7, \epsilon_8, \epsilon_9, \epsilon_{10}, \epsilon_{11}, \epsilon_{12}, \epsilon_{13}, \epsilon_{14}, \epsilon_{15}, \epsilon_{16}],
$$
 Partial Repeated Sampling: $[\epsilon_1, \epsilon_1, \epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4, \epsilon_5, \epsilon_6, \epsilon_7, \epsilon_8, \epsilon_9, \epsilon_{10}, \epsilon_{10}, \epsilon_{10}, \epsilon_{10}].$ (15)

964 965 966 967 968 969 970 971 Since spatio-temporal correlations in the low-frequency components of initial noises will guide the trajectory of generated objects, partial repeated sampling for initial noises will bring typical motion mode. As shown in Figure [11](#page-18-1) (b), the owl is stationary in the beginning and ending frames and only has significant action in the middle frames. However, due to the attention isolation, frames of generated results have obvious artifacts. We visualize one heat map of temporal attention and find that stationary frames mainly pay attention to frames with the same initial noises. When calculating the attention weights received by isolated frames, manually splitting a portion of attention weights from isolated frames to other frames will remove artifacts. As shown in Figure [11](#page-18-1) (c), an owl is well generated and its motion still fits the mode in (b).

Figure 10: Noise flow in AnimateDiff. In AnimateDiff, objects and textures in the video also flow in the same direction as the initial noises.

 Figure 11: Attention isolation in temporal dimension. Compared to normal sampling for initial noises (a), partial repeated sampling will lead to significant attention isolation in the temporal dimension and bring strong artifacts (b). When calculating the attention weights received by isolated frames, manually splitting a portion of attention weights from isolated frames to other frames will remove artifacts (c).

 Table 3: **Quantitative comparison of ablations.** Dynamics is the score of dynamic degree [\(Huang](#page-11-7) [et al., 2023b\)](#page-11-7). The best results are marked in bold, and the second best results are marked by underline.

Method	FVD (L)	KVD (L)	CLIP-SIM (\uparrow)	mIoU $($ \uparrow $)$	CD (L)	Dynamics (\uparrow)
No Noise Guidance	390.65	24.48	0.964	0.277	0.156	0.973
No Noise Resampling	513.79	39.88	0.960	0.279	0.167	0.973
Higher Intensity Control	697.72	62.06	0.951	0.322	0.149	1.000
Ours	436.22	29.85	0.956	0.281	0.154	0.982

"A horse galloping through a meadow."

Figure 12: Visualization of control intensity. When increasing the control intensity, the generated objects will follow the given bounding boxes more closely. However, meaningless patterns will be generated when the intensity is large.

C.3 QUANTITATIVE ABLATION

 We also conduct the ablation study quantitatively. For the setting of higher intensity control, we increase the α in Equation [9](#page-6-1) from 0.25 to 0.5. As shown in Table [3,](#page-19-0) our final setting achieves a competitive performance in both video quality and trajectory control.

 C.4 CONTROL INTENSITY

 We can easy adjust the control intensity by modifying the α in Equation [9.](#page-6-1) In this paper, $\alpha = 0.25$ is a default value to guarantee that most generated cases do not contain artifacts. However, as shown in Figure [12,](#page-19-1) $\alpha = 0.5$ is a better choice for higher control intensity. Users can get a better traject-controllable result by sampling more times with different random seeds. Meaningless patterns will be generated when the intensity is large.

C.5 METHOD COMPATIBILITY

 We test FreeTraj on another diffusion-based video generation method, AnimateDiff. As shown in Figure [13,](#page-20-0) FreeTraj effectively achieves trajectory control in AnimateDiff, potentially making it a versatile tool in video synthesis, especially for applications requiring rapid deployment without extensive training data.

 C.6 LLM-PLANED GENERATION

 We slightly modify the prompt from the previous work [\(Lian et al., 2023\)](#page-12-16) and the LLM will plan the bounding boxes for each frame. The results are shown in Figure [14.](#page-21-0)

