

000 001 002 003 004 005 PROTOCODE: PROTOTYPE-DRIVEN INTERPRETABILITY FOR CODE GENERATION IN LLMS 006 007 008 009

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ABSTRACT

031 Since the introduction of Large Language Models (LLMs), they have been widely
032 adopted for various tasks such as text summarization, question answering, speech-
033 to-text translation, and more. In recent times, the use of LLMs for code generation
034 has gained significant attention, with tools such as Cursor and Windsurf demon-
035 strating the ability to analyze massive code repositories and recommend relevant
036 changes. Big tech companies have also acknowledged the growing reliance on
037 LLMs for code generation within their codebases. Although these advances sig-
038 nificantly improve developer productivity, increasing reliance on automated code
039 generation can proportionally increase the risk of suboptimal solutions and in-
040 secure code. Our work focuses on automatically sampling In-Context Learning
041 (ICL) demonstrations which can improve model performance and enhance the in-
042 terpretability of the generated code. Using AST-based analysis on outputs from
043 the MBPP test set, we identify regions of code most influenced by the chosen
044 demonstrations. In our experiments, we show that high-quality ICL demon-
045 strations not only make outputs easier to interpret but also yield a positive per-
046 formance improvement on the pass@10 metric. Conversely, poorly chosen ICL
047 demonstrations affected the LLM performance on the pass@10 metric negatively
048 compared to the base model. Overall, our approach highlights the importance
049 of efficient sampling strategies for ICL, which can affect the performance of the
050 model on any given task.
051

1 INTRODUCTION

052 In recent years, Large Language Models (LLMs) have gained significant traction in the fields of
053 code completion and code filling. This growth has been fueled by the availability of large-scale
054 open-source datasets such as The vault Manh et al. (2023), CodeSearchNet Husain et al. (2020),
055 CodeXGlue Lu et al. (2021) and many others. Alongside these datasets, we have also witnessed
056 the emergence of open-source models designed specifically for code-related tasks, including the
057 CodeLlama series Rozière et al. (2024), Qwen Coder Hui et al. (2024) series, and StarCoder se-
058 ries Li et al. (2023a). In parallel, closed-source models such as GPT-4o OpenAI et al. (2024) and
059 Claude Code Anthropic (2025) have been widely adopted by various big tech companies for
060 generating production-ready code. Despite these advancements, most of these models remain difficult
061 to interpret in the context of code generation. While a variety of interpretability methods have been
062 developed to interpret the outputs generated by LLMs and foster trust in their usage across domains,
063 many of these approaches are generic and not specifically tailored for code generation tasks. Some
064 methods, however, are focused on interpretability in code generation. For instance, Code-Q Palacio
065 et al. (2025) identifies influential tokens that guide the model’s output, but it requires repeated
066 sampling and generation, which introduces significant computational overhead during inference.

067 Another method, ATrust Palacio et al. (2024), leverages Abstract Syntax Trees (ASTs) by us-
068 ing model-generated token probabilities. Tokens are mapped to code level subsets, which are then
069 grouped into terminal and non-terminal nodes within the AST. Each non-terminal node is repre-
070 sented by the aggregated confidence of its associated terminal nodes. However, this approach re-
071 quires storing the probability distribution over the entire vocabulary at every step of generation,
072 which scales poorly as the output length increases. To address these challenges, we propose a
073 manifold-based sampling strategy that automatically samples a set of ICL demonstrations from a
074 given dataset. These demonstrations enable interpretability by combining attribution and AST-based

054 analysis. Our method segments the generated code into interpretable regions, such as Iterations,
 055 Data structures, etc., allowing users to understand which regions of the generated code are most
 056 affected by the sampled demonstrations. To the best of our knowledge, we are the first to unify
 057 prototype-driven ICL sampling with AST-grounded attribution for code interpretability.
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- **Prototype Sampling via Joint Manifold and Metric Learning:** Our method introduces
 060 a principled approach to sample In-Context Learning (ICL) demonstrations by combining
 061 *piecewise-linear manifold learning* and *proxy anchor-based metric learning*. This
 062 joint formulation ensures that the sampled prototypes are not only *geometrically faithful*—capturing the local data structure—but also *semantically discriminative*.
 063
- **Prototype-Gradient Attribution for AST-Grounded Interpretability:** We propose a
 064 novel attribution mechanism using the gradient of similarity between prototype and token
 065 embeddings to estimate token-level influence. These scores are then propagated through
 066 the *Abstract Syntax Tree (AST)* to produce *faithful, syntax-aware confidence maps*, en-
 067 abling both *local (node-level)* and *global (category-level)* interpretability of generated
 068 code—while avoiding the memory overhead of storing token probabilities.
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070

071 2 RELATED WORK

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073 According to Bilal et al. (2025), explainability techniques in AI systems can be broadly divided into
 074 three categories: (1) post hoc explanations, (2) intrinsic interpretability, and (3) human-centered ex-
 075 planations. Post hoc explanation methods aim to interpret a model’s decisions after predictions have
 076 been made. Common approaches include Local Interpretable Model-Agnostic Explanations (LIME)
 077 Ribeiro et al. (2016), Shapley Additive Explanations (SHAP) Lundberg & Lee (2017). LIME pro-
 078 vides local explanations by identifying the most important features for a single prediction. Similarly,
 079 SHAP evaluates the contribution of each feature by measuring changes in the prediction when fea-
 080 tures are systematically removed. In addition, gradient-based methods such as SmoothGrad Smilkov
 081 et al. (2017) and Integrated Gradients Sundararajan et al. (2017) calculate model gradients with re-
 082 spect to input features to determine the sensitivity of the model’s output to each feature.
 083

084 Intrinsic interpretability, in contrast, focuses on designing model architectures so that their behavior
 085 is inherently explainable. One example is concept bottleneck models Koh et al. (2020), which were
 086 extended to large language models (LLMs) by Sun et al. (2025) for sentence classification task. Their
 087 approach generates concepts for each class, making the classification process directly interpretable.
 088 However, this approach faces limitations in generating suitable concepts for diverse tasks and does
 089 not scale well to text generation. Another related method, Proto-Im Xie et al. (2023) , extends
 090 prototype networks to text classification. Instead of generating concepts like concept bottlenecks, it
 091 learns trainable prototypes and maps them to the nearest training samples for interpretability.
 092

093 A particularly influential method within intrinsic interpretability is Chain-of-Thought (CoT) Wei
 094 et al. (2023), which generates intermediate reasoning steps. CoT has been shown to improve both
 095 plausibility and task performance compared to demonstrations that provide only the final answers
 096 Wei et al. (2023) Cobbe et al. (2021). Building upon this, Self-Consistency Wang et al. (2023)
 097 was proposed as an extension of CoT. This method prompts the model to produce multiple reason-
 098 ing chains and answers, and then selects the final output using a majority vote across the answers.
 099 Although effective, Self-Consistency only ensures correctness of the final prediction, without ver-
 100 ifying whether the reasoning chains themselves are valid or faithful. To address this, SEA-CoT
 101 Wei Jie et al. (2024) was introduced. SEA-CoT evaluates generated reasoning chains based on the
 102 implication with the task context and the overlap of the token level, ensuring that both the reasoning
 103 process and the final answer align more closely with the task requirements. However, as stated by
 104 Jacovi & Goldberg (2020), the reasoning chains from LLM often appear plausible to humans but are
 105 not necessarily faithful to the true decision-making process of the LLM. Plausibility refers to how
 106 convincing the interpretation is to humans, while faithfulness measures the degree to which it truly
 107 represents the internal reasoning of the LLM.
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109 Most of the above methods are designed for generic tasks, with a limited focus on code-specific ap-
 110 plications. The method ASTrust was developed specifically for interpretability in code generation. It
 111 builds Abstract Syntax Trees (ASTs) to align with program structure and assigns confidence scores
 112 to non-terminal nodes by aggregating probabilities from their terminal nodes. These scores are de-

rived from token-level probabilities output by the model. Ma et al. (2024) demonstrates that LLMs already possess strong syntactic awareness, rivaling AST-based static code analysis. However, the method ATrust has key limitations: its token sampling method is not well justified. Greedy sampling ignores the advantages of stochastic approaches, while stochastic sampling requires storing probabilities for all vocabulary tokens at every step an impractical, memory-intensive process. In contrast, our method avoids this heavy storage by relying on attribution-based prototype influence, which captures the effect of sampled demonstrations without requiring full vocabulary distributions. As a result, our approach preserves the benefits of stochastic sampling Shi et al. (2024) while remaining significantly more scalable and practical for code generation interpretability.

3 METHODOLOGY

Prototype-based approaches provide an interpretable mechanism to associate each class with representative examples, commonly referred to as prototypes. A simple baseline is to define prototypes using statistics such as class means or medoids in the embedding space. However, these statistical summaries fail to capture the intrinsic geometry of the representation space: they are vulnerable to outliers, insensitive to intra-class multimodality, and often yield prototypes that are statistically central yet semantically uninformative.

To overcome these shortcomings, we turn to the manifold perspective. The manifold hypothesis Cayton (2005) posits that high-dimensional representations lie on low-dimensional manifolds. Leveraging this structure allows prototypes to be sampled from regions that faithfully capture the local geometry of the data, rather than from globally averaged or distorted positions in embedding space. While classical manifold learning techniques such as t-SNE van der Maaten & Hinton (2008), UMAP McInnes et al. (2020), and LLE Roweis & Saul (2000) emphasize neighborhood preservation, they often distort local dependencies or fail to maintain global structure. We therefore adopt a piecewise-linear manifold learning strategy, which decomposes nonlinear manifolds into locally linear regions.

While geometry preserves structural fidelity, it does not guarantee that prototypes are discriminative across classes. To enforce both intra-class compactness and inter-class separation, we integrate metric learning objectives. Traditional formulations such as triplet or contrastive loss require pre-specified prototypes and extensive mining, making them inefficient and unstable. Instead, we employ Proxy-Anchor loss, which introduces learnable class-level proxy vectors to directly optimize intra-class cohesion and inter-class margins. After training, each learned proxy vector is mapped to its nearest training instance using euclidean distance.

As highlighted in Rodriguez-Cardenas et al. (2023), in the context of ICL, the selection of demonstrations plays a crucial role in model performance. In our approach, we dedicate considerable effort to identifying the most suitable prototypes (ICL examples) for each LLM. Our method can be divided into two main components. In the first stage, we initialize a simple neural network h_θ and train it on Dataset D to jointly optimize manifold learning and metric learning objectives. Once the training is complete, the learned proxy vectors are employed to sample prototypes.

3.1 DATASET

We have used the Magicoder-OSS-Instruct-75K Wei et al. (2024) for sampling the prototypes. This dataset consists of 75,000 synthetic instruction-following examples generated using OSS-Instruct; it contains 9 programming languages. For every query, it has a programming language id, the query, and the code solution. For every sample in the dataset, we have used the following prompt structure to format all the samples in the dataset.

Prompt Structure: *"This is the query being assigned: "+" "+ [/Q]+ "+"The following is the code solution to the query"+ "+"+[/S]"*. Where the placeholders $[/Q]$ and $[/S]$ are for query and code solution respectively. After formatting the prompts, we use the respective Large Language model(M) to encode the final prompts into the latent representations (z). We simultaneously label encode the programming language ID for using them as class labels; this method gives us 9 different classes, and for each sample in the dataset, we will be storing the encoded label (l) and the latent representation (z) as pairs in dataset D .

162 **3.2 TRAINING OVERVIEW**
163164 As mentioned in 3, our method consists of two stages. In the first stage of our method, we initialize
165 a simple neural network h_θ Tab 3 and train it on Dataset D to jointly optimize manifold learning
166 and metric learning objectives 1. The neural network h_θ learns to map the high-dimensional
167 encoded representations into lower dimensions. Before the training process, we initialize the proxies
168 θ_q and θ_m . Here both the proxies are unique for each class and initialized randomly with $\theta_q = \theta_m$.
169 The proxy vector θ_q is updated via back-propagation, and the proxy vector θ_m is updated via the
170 Momentum update He et al. (2020) where γ is the momentum constant, $[\theta_k \leftarrow \gamma\theta_k + (1 - \gamma)\theta_q]$ 171 During training, for every mini-batch B we build linear piecewise manifolds as outlined in 3.3. For
172 every point in B , we then compute the manifold-based similarity following the procedure in 3.4.
173 This similarity measure is used to compute the manifold point-to-point loss $\mathcal{L}_{\text{manifold}}$. At the same
174 time, we compute the Proxy Anchor loss \mathcal{L}_{PA} using randomly initialized class proxies θ_q and latent
175 representations z in batch B . The final loss is computed as, $\mathcal{L}_{\text{total}} = \mathcal{L}_{\text{PA}} + \mathcal{L}_{\text{manifold}}$.176 While the manifold loss preserves local geometric structure, the Proxy-Anchor loss promotes intra-
177 class compactness and inter-class separation, thereby facilitating the discriminative learning of pro-
178 tootypes. Across epochs, the network parameters are updated via backpropagation. After training,
179 the momentum-updated proxies θ_m are used to select the nearest training instance as the prototype
180 for each class, yielding a single prototype per class for the subsequent stage.181 After the completion of the training process, we proceed to the second stage, where we generate the
182 code completions using the prototypes. After that, we utilize the encoded latent representations of
183 the prototypes to calculate the confidence score per token for AST analysis. For each code com-
184 pletion, we compute a prototype attribution-based score to quantify the influence of the prototypes
185 on the generated code. Specifically, influence is measured by the attribution between the sampled
186 demonstrations and the code completions. Finally, we perform an AST analysis to analyze how the
187 prototypes impact the syntactic structure of the generated code.188
189 **3.3 MANIFOLD CONSTRUCTION**
190191 Based on the Manifold hypothesis, we can assume that the encoded latent representations z , which
192 are inherently complex and non-linear, can be locally approximated into smaller chunks of linear
193 regions. Our approach leverages this structural assumption to automatically identify representative
194 prototypes that capture the essential characteristics of each action class.195 To efficiently approximate the structure of the linear data manifolds, we adopt a piecewise linear
196 manifold learning method which constructs localized m -dimensional linear submanifolds around
197 selected anchor points. Given a mini batch B containing N data points, we randomly select n
198 of them to serve as anchors. For each anchor point $h_\theta(z_i)$, we initially collect its $m-1$ nearest
199 neighbors in the encoded representation space based on Euclidean distance to form the neighborhood
200 set X_i .201 The manifold expansion process proceeds iteratively by attempting to add the m -th nearest neighbor
202 to X_i . After each addition, we recompute the best-fit m -dimensional submanifold using PCA and
203 assess whether all points in X_i can be reconstructed with a quality above a threshold $T\%$. If the
204 reconstruction quality remains acceptable, the new point is retained in X_i ; otherwise, it is excluded.
205 This evaluation is repeated for subsequent neighbors $N(h_\theta(x_i))_j$ for $j \in \{m+1, \dots, k\}$, gradually
206 constructing a local linear approximation of the manifold.207 The final set X_i comprises all points in the anchor's neighborhood that lie well within an m -
208 dimensional linear submanifold. A basis for this submanifold is computed by applying PCA to X_i
209 and extracting the top m eigenvectors. We choose PCA for this task as it can effectively construct
210 the lower-dimensional manifolds for the locally linear regions.211
212 **3.4 TRAINING OBJECTIVES**
213214 **Proxy Anchor Loss:** We use a modified version of proxy anchor loss with Euclidean distance
215 instead of cosine similarity:

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$$\mathcal{L}_{\text{PA}} = \frac{1}{|\Theta_+|} \sum_{\theta_q \in \Theta_+} \log \left(1 + \sum_{z \in \mathcal{Z}_{\theta_q}^+} \exp(-\alpha \cdot (\|h_\theta(z) - \theta_q\|_2 - \epsilon)) \right) \quad (1)$$

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$$+ \frac{1}{|\Theta|} \sum_{\theta_q \in \Theta} \log \left(1 + \sum_{z \in \mathcal{Z}_{\theta_q}^-} \exp(\alpha \cdot (\|h_\theta(z) - \theta_q\|_2 - \epsilon)) \right) \quad (2)$$

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Here, Θ denotes the set of all proxies, where each proxy $\theta_q \in \Theta$ serves as a representative vector for a class. The subset $\Theta_+ \subseteq \Theta$ includes only those proxies that have at least one positive embedding in the current batch B . For a given proxy θ_q , the latent representations \mathcal{Z} in B (where $z \in \mathcal{Z}$) are partitioned into two sets: $\mathcal{Z}_{\theta_q}^+$, the positive embeddings belonging to the same class as θ_q , and $\mathcal{Z}_{\theta_q}^- = \mathcal{Z} \setminus \mathcal{Z}_{\theta_q}^+$, the negative embeddings. The scaling factor α controls the sharpness of optimization by amplifying hard examples when large (focusing gradients on difficult pairs) or smoothing training when small (spreading weight across all pairs). The margin ϵ enforces a buffer zone between positives and negatives by requiring positives to be closer to their proxies and negatives to be sufficiently farther away.

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Manifold Point-to-Point Loss: This loss helps in estimating the point to point similarities preserving the geometric structure:

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$$\mathcal{L}_{\text{manifold}} = \sum_{i,j} (\delta \cdot (1 - s(z_i, z_j)) - \|h_\theta(z_i) - h_\theta(z_j)\|_2)^2 \quad (3)$$

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where $s(z_i, z_j)$ is the manifold similarity computed as:

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$$s(z_i, z_j) = \frac{s'(z_i, z_j) + s'(z_j, z_i)}{2}$$

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with $s'(z_i, z_j) = \alpha(z_i, z_j) \cdot \beta(z_i, z_j)$, where:

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$$\alpha(z_i, z_j) = \frac{1}{(1 + o(z_i, z_j))^N}$$

$$\beta(z_i, z_j) = \frac{1}{(1 + p(z_i, z_j))^N}$$

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In equation 3, h_θ is a simple neural network with a structure specified in Table 3 and δ is a scaling factor that determines the maximum separation between dissimilar points. The loss encourages Euclidean distances in the embedding space to match manifold-based dissimilarities $1 - s(z_i, z_j)$, ensuring that the learned metric space respects the underlying manifold structure. $o(z_i, z_j)$ is the orthogonal distance from point z_i to the manifold of point z_j , and $p(z_i, z_j)$ is the projected distance between point z_j and the projection of z_i on the manifold. The parameters N_α and N_β control how rapidly similarity decays with distance, with $N_\alpha > N_\beta$ ensuring that similarity decreases more rapidly for points lying off the manifold than for points on the same manifold.

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Distance Calculation. For each point pair (z_i, z_j) , the distances $o(z_i, z_j)$ and $p(z_i, z_j)$ are calculated using the manifold basis vectors P_j associated with point z_j . The projection of z_i onto P_j is computed as $\text{proj}_{P_j}(z_i) = z_j + \sum_k (z_i - z_j, v_k) v_k$, where v_k are the basis vectors of P_j . The orthogonal distance is then $o(z_i, z_j) = \|z_i - \text{proj}_{P_j}(z_i)\|_2$, and the projected distance is $p(z_i, z_j) = \|\text{proj}_{P_j}(z_i) - z_j\|_2$. This process is repeated for all point pairs, capturing the full geometric structure of the data manifold.

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4 RESULTS

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We evaluated the effectiveness of different sampling methods by applying them as in-context learning (ICL) examples on the MBPP test set Austin et al. (2021). To demonstrate the effectiveness of

270 Table 1: Performance comparison across different models and methods on the MBPP dataset
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Model → Method ↓	Qwen3-0.6B		Llama3.2-1B		Falcon3-1B		Starcoder-1B-base		Qwen2.5coder-0.5B		Codellama-7B	
	pass@1	pass@10	pass@1	pass@10	pass@1	pass@10	pass@1	pass@10	pass@1	pass@10	pass@1	pass@10
base	0.011	0.048	0.007	0.042	0.010	0.063	0.008	0.040	0.041	0.116	0.021	0.116
diversity	0.0076	0.037	0.012	0.061	0.010	0.042	0.002	0.011	0.021	0.063	0.007	0.035
similarity	0.009	0.050	0.013	0.050	0.011	0.050	0.007	0.032	0.023	0.069	0.018	0.079
mbpp	0.006	0.024	0.007	0.042	0.002	0.018	0.005	0.004	0.021	0.095	0.009	0.039
prototypes(ours)	0.019	0.059	0.010	0.058	0.020	0.068	0.012	0.050	0.048	0.122	0.030	0.122

279 Table 2: Performance comparison across different models and methods on the MBPP+ Dataset
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Model → Method ↓	Qwen3-0.6B		Llama3.2-1B		Falcon3-1B		Starcoder-1B-base		Qwen2.5coder-0.5B		Codellama-7B	
	pass@1	pass@10	pass@1	pass@10	pass@1	pass@10	pass@1	pass@10	pass@1	pass@10	pass@1	pass@10
base	0.0078	0.0396	0.005	0.037	0.009	0.058	0.008	0.037	0.031	0.100	0.015	0.090
diversity	0.0067	0.031	0.007	0.045	0.007	0.034	0.002	0.011	0.017	0.048	0.006	0.026
similarity	0.0061	0.037	0.008	0.054	0.007	0.042	0.006	0.029	0.017	0.055	0.013	0.067
mbpp	0.002	0.016	0.005	0.042	0.001	0.013	0.004	0.032	0.016	0.077	0.006	0.040
prototypes(ours)	0.016	0.050	0.007	0.050	0.015	0.050	0.010	0.046	0.039	0.108	0.024	0.103

288
289 our method we have used 2 sets of models for experimentation, the first set consisting of generic
290 models of Qwen3 Yang et al. (2025), Llama-3.2 AI (2024), Falcon-3 Team (2024) and for the second
291 set we have used code heavy pre-trained models Starcoder-base Li et al. (2023b), Qwen2.5-Coder
292 Hui et al. (2024), Codellama Rozière et al. (2024).

293 The results are reported on a scale from [0, 1], where 0 is the lowest and 1 is the highest (For instance,
294 0.1 can be interpreted as 10%). While the numerical margins may appear small at first glance, even
295 modest gains in code completion represent substantial improvements. For context, GPT-4-1106
296 ope (2023), which is estimated to be at least 1000× larger than the models used for our experiments,
297 achieves a score of 0.786 on the MBPP test set. This comparison highlights an important distinction:
298 in many benchmarks, partial overlap between a generated solution and the reference solution may
299 yield a nonzero score even if the final answer is incorrect. In contrast, code benchmarks are more
300 stringent, as each generated program is independently evaluated against unit test cases. Therefore,
301 even incremental improvements in $Pass@k$ metrics are highly significant for code generation tasks.

302 The Qwen2.5-coder model, despite having fewer parameters than Codellama, achieves comparable
303 performance on both the $Pass@1$ and $Pass@10$ metrics across the MBPP and MBPP+ test sets.
304 Among all comparisons, the similarity-based sampling method surpasses our approach only for the
305 Llama3.2 model; in every other case, our method consistently outperforms alternative strategies
306 across all models. As noted by Rodriguez-Cardenas et al. (2023), within the ICL setting, the quality
307 of selected demonstrations can also negatively affect model performance.

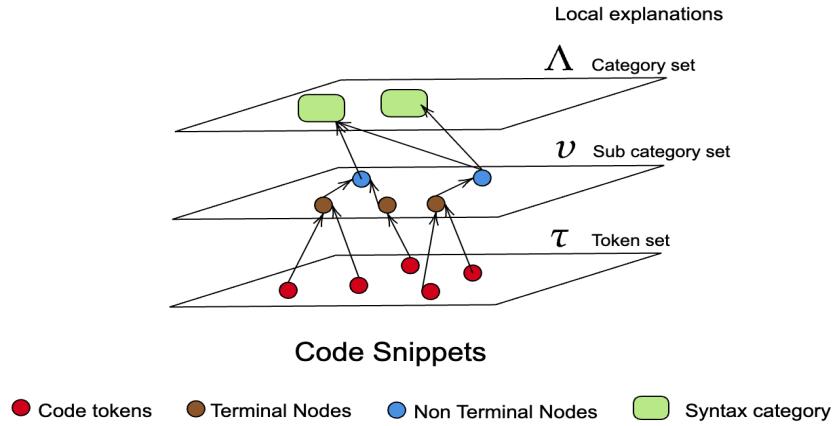
308 For the Qwen3 and Qwen2.5-coder models, using demonstrations sampled from methods other than
309 the prototype-based approach leads to a decline in performance on both MBPP and MBPP+. A
310 similar trend is observed for the Starcoder and Codellama models. These results suggest that the
311 Qwen family of models, as well as code-pretrained models in general, are particularly sensitive to
312 the choice of ICL demonstrations. An unsuitable set of demonstrations can reduce performance
313 compared to the base model, underscoring the importance of effective sampling strategies for ICL.

314 5 AST ANALYSIS

317 We perform an Abstract Syntax Tree (AST) analysis to identify which syntactic regions of the generated
318 code are most influenced by the sampled prototypes. In the AST framework, the authors
319 employ token-level probabilities produced by the model M as the confidence scores in the token
320 set. For a sequence of tokens w_1, w_2, \dots, w_i , the probability of generating the next token w_{i+1} is
321 defined as equation 4 where M denotes the Large Language Model and $M(w_{1:i})$ represents the
322 non-normalized log probabilities output by the model for the given context.

$$323 P(w_{i+1} | w_{1:i}) = \text{Softmax}(M(w_{1:i})), \quad (4)$$

Figure 1: Conceptual working of AST analysis



As discussed in Section 2.2, this method suffers from high memory overhead when combined with stochastic sampling strategies. To mitigate this limitation, we instead leverage attribution-based scores between the sampled prototypes and the generated code samples, and use these scores as token-level confidence in AST analysis. Concretely, for a model-generated code snippet C , we extract the tokens w_i along with their latent representations z_{w_i} . Let the latent representation of a sampled prototype p be z_p . We compute the mean prototype vector z_a as $z_a = \sum_{i \in P} z_i$. Next, we compute the dot product between z_a and each z_{w_i} , and compute its gradient with respect to z_{w_i} . The normalized gradients $\nabla_{z_{w_i}}$ (equation 5) are then used as confidence scores per token in the AST analysis.

$$\nabla_{z_{w_i}} = \frac{d(z_a \cdot z_{w_i})}{dz_{w_i}} \quad (5)$$

5.1 SYNTAX GROUNDED EXPLANATIONS

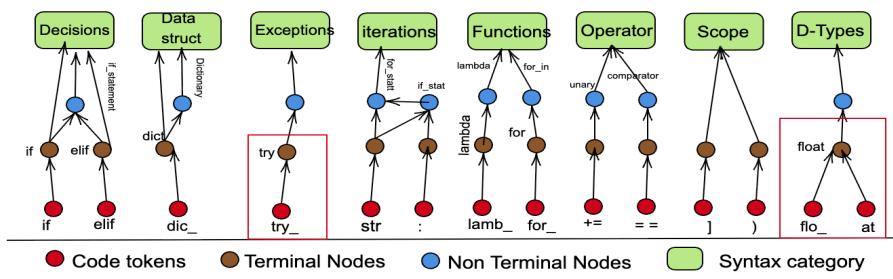


Figure 2: Alignment & Clustering Interactions. The δ function aligns tokens w_i to terminal nodes λ . Terminal and Non-terminal nodes $\lambda, \alpha \in v$ are clustered by Syntax Categories Λ

AST analysis involves using the prototype-based attribution scores as token confidence scores explained in 5. We then compute the average confidence over tokens corresponding to each AST node, and report these averages as performance values grouped by manually defined syntax categories. The process follows three steps, illustrated in Fig.1 1. In Step1, for every generated code snippet, the tokenizer splits the code into tokens w_i (forming the token set τ D.1), and the model assigns a confidence score to each token as described in 5. In Step2, the token-level predictions are aligned with the respective Abstract Syntax Tree (AST) terminal nodes. Terminal nodes retain the raw confidences, whereas non-terminal nodes hierarchically store aggregated values. Together, terminal and non-terminal nodes form the subcategory set v D.1. For instance, the token 'if' from the

378 token set aligns with a terminal AST node but is grouped under the non-terminal node 'if_statement'.
 379 Finally, in Step 3, the analysis introduces eight syntax categories to summarize model predictions.
 380 These categories aggregate subcategories into broader, human-interpretable groups. The Syntax
 381 Categories form a fixed Category Set Λ D.1, providing more intuitive elements for interpretation.

382 For example, the sub-categories 'if_statement' and 'if' are grouped under the syntax category 'De-
 383 cisions' 2. Ultimately, ASTrust outputs an averaged score for each category to provide global
 384 explanations, along with an AST tree visualization that embeds confidence scores at every node
 385 for local explanations. In essence, we argue that syntax elements encode semantic information that
 386 contextualizes token-level confidence scores, though this semantic value differs depending on the
 387 granularity of the elements. For instance, tokens alone convey less interpretable meaning compared
 388 to higher-level categories. AST analysis thus serves as a post-hoc explanation framework at both
 389 local and global levels. Local explanations focus on breaking down a single code snippet into AST
 390 elements to interpret its generation, while global explanations rely on multiple generated snippets to
 391 provide a holistic view of the model through Syntax Categories (SCs) D.1.

392 393 394 395 396 397 398 399 400 401 402 403 404 405 406 407 408 409 410 411 412 413 414 415 416 417 418 419 420 421 422 423 424 425 426 427 428 429 430 431 5.2 CODE SYNTACTIC ANALYSIS

395 To assess the attribution-based confidence score of each Syntax Category (SC) for the 6 LLMs, we
 396 present an AST analysis. 3 illustrates the AST interpretability performance segregated by Sy-
 397 ntax Categories (SCs) for each model type. The Qwen2.5 Coder and Qwen3 3 (a) models exhibit
 398 highly consistent confidence across all syntax categories, with nearly identical values. Both mod-
 399 els demonstrate their strongest performance in Scope, Data Structures, and Functions, indicating
 400 reliability in handling structured data, variable and function scoping, and modular code organiza-
 401 tion. Moderate confidence is observed for Iteration, Decisions, Operators, and Data Types, while the
 402 lowest confidence is consistently assigned to Exception handling, suggesting potential limitations in
 403 generating or reasoning about robust error-handling constructs. Overall, these results suggest that
 404 both Qwen2.5 Coder and Qwen3 are best suited for structured programming tasks, while being less
 405 dependable for control-flow-intensive or exception-heavy code generation.

406 The Llama models 3 (b) exhibit broadly similar confidence trends across syntax categories, with
 407 CodeLlama consistently showing a slight advantage over Llama-3.2. Both models demonstrate their
 408 highest reliability in Data Structures, Functions, and Iteration, suggesting strong capabilities in tasks
 409 that require structured data handling, modular code organization, and loop-based constructs. Mod-
 410 erate confidence is observed in Scope, Decisions, Operators, and Data Types, indicating stable but less
 411 pronounced strengths. In contrast, Exception handling remains the weakest category for both mod-
 412 els, highlighting a shared limitation in generating or reasoning about robust error-handling logic.
 413 Collectively, these results suggest that while the Llama models are well-suited for structured pro-
 414 gramming tasks, they are less dependable for exception-heavy scenarios.

415 The Falcon and StarCoder models 3 (c) display distinct differences in their syntax-grounded confi-
 416 dence. StarCoder consistently achieves higher confidence across nearly all categories compared to
 417 Falcon, indicating stronger overall reliability. Both models perform best in Scope, Data Structures,
 418 and Functions, suggesting robustness in structured programming tasks and modular code organiza-
 419 tion. StarCoder further extends this strength to Iteration and Decisions, where it shows clear im-
 420 provements over Falcon, highlighting its ability to handle control flow more effectively. In contrast,
 421 Exception handling remains the weakest category for both models, underscoring a shared limitation
 422 in generating robust error-handling constructs. Taken together, these results indicate that while Fal-
 423 con is moderately capable across most categories, StarCoder offers broader syntactic reliability and
 424 is better suited for tasks requiring control flow and structured data handling.

425 426 427 428 429 430 431 6 FUTURE WORKS

427 In our experiments, prototypes were sampled exclusively from the Magicoder dataset. While this
 428 choice provided a consistent basis for evaluation, extending the analysis to additional datasets could
 429 offer a broader understanding of prototype quality. In fact, our method can naturally be applied as a
 430 global metric for ranking datasets with respect to their ability to yield effective prototypes. Another
 431 limitation arises from differences in model stability. For example, Llama3.2 5 exhibited high sen-
 432 sitivity to changes in nearly all hyperparameters, which led to inconsistent results on the *Pass@k*

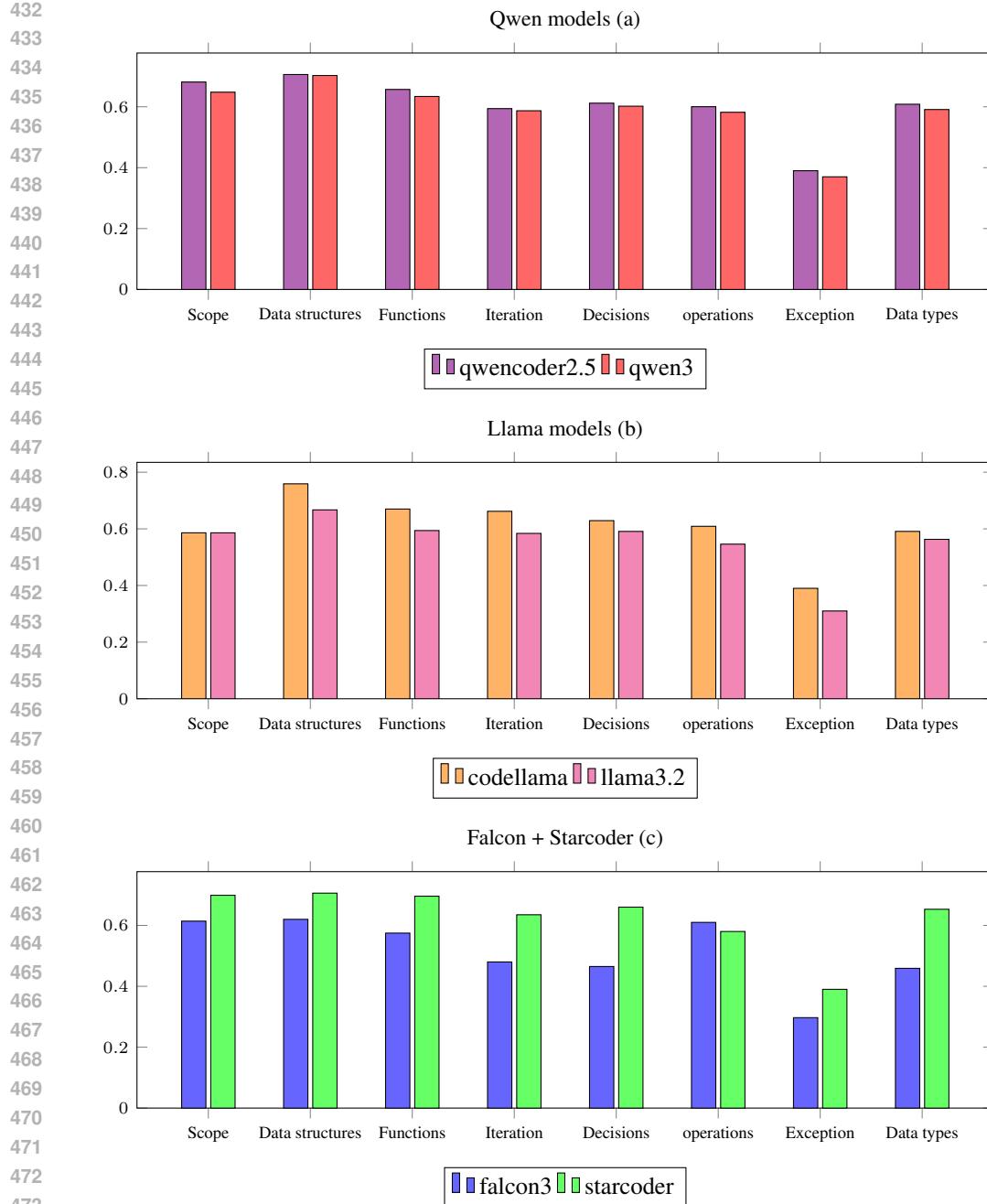


Figure 3: AST analysis on 6 LLMs

metric. In contrast, the Qwen2.5 Coder model 5 displayed only marginal sensitivity, with the exception of the α parameter, resulting in more stable and reliable performance. Finally, while our current approach uses sampled prototypes as in-context learning demonstrations, the framework can be extended toward pre-hoc interpretability by design. In particular, prototype steering could be explored as a mechanism for influencing model behavior, offering new avenues for both interpretability and controllability in LLMs.

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810 A RELATED WORKS
811812 A.1 MANIFOLD LEARNING
813814 The manifold hypothesis is a well-established principle in Machine Learning, which suggests that
815 Cayton (2005):816 *Although data points often appear to have very high dimensionality, with thou-
817 sands of observed features, they can typically be represented by a much smaller
818 set of underlying parameters. In essence, the data resides on a low-dimensional
819 manifold embedded within a high-dimensional space.*
820821 Based on the Manifold hypothesis Manifold learning focuses on uncovering low-dimensional struc-
822 tures in high dimensional data. Manifold learning techniques like TSNE van der Maaten & Hinton
823 (2008), UMAP McInnes et al. (2020), LLE Roweis & Saul (2000) and Isomap Tenenbaum et al.
824 (2000) utilize information derived from the linearized neighborhoods of points to construct low
825 dimensional projections of non-linear manifolds in high dimensional data.826 The method Piecewise-Linear Manifolds for Deep Metric Learning Bhatnagar & Ahuja (2024) aims
827 to train a neural network to learn a semantic feature space where similar items are close together and
828 dissimilar items are far apart, in an unsupervised manner. This method is based on using linearized
829 neighborhoods of points to construct a piecewise linear manifold, which helps estimate a continuous-
830 valued similarity between data points.
831832 A.2 METRIC LEARNING
833834 Metric learning aims to learn an embedding space where semantically similar samples are close
835 and dissimilar ones are far apart. Common loss functions include **Contrastive loss** Hadsell et al.
836 (2006), aims at making representations of positive pairs closer to each other, while pushing negative
837 pairs further away than a positive margin. It is commonly used in tasks such as face verification or
838 representation learning with Siamese networks. Here (z_i, z'_i) are embeddings of a pair, $y_i \in \{0, 1\}$
839 indicates similarity, and m is the margin.
840

841
$$\mathcal{L} = \frac{1}{N} \sum_{i=1}^N \left[y_i \|z_i - z'_i\|_2^2 + (1 - y_i) \max(0, m - \|z_i - z'_i\|_2)^2 \right]$$

842

843 **Triplet loss** Schroff et al. (2015) is another metric learning objective that enforces relative similarity
844 by ensuring that an anchor x_a is closer to a positive sample x_p (same class) than to a negative
845 sample x_n (different class) by at least a margin. Unlike contrastive loss, which only considers
846 pairwise distances, triplet loss leverages relative comparisons, making it more effective in learning
847 discriminative embeddings for tasks such as face recognition and image retrieval, here $f(\cdot)$ is the
848 embedding function, m is the margin, x_a is the anchor, x_p is a positive sample, and x_n is a negative
849 sample.
850

851
$$\mathcal{L} = \frac{1}{N} \sum_{i=1}^N \max \left(0, \|f(x_a^i) - f(x_p^i)\|_2^2 - \|f(x_a^i) - f(x_n^i)\|_2^2 + m \right)$$

852

853 **Multi-class N-pair loss** Sohn (2016) generalizes triplet loss by comparing one positive sample
854 against multiple negative samples simultaneously. This encourages more efficient optimization than
855 triplet loss, which only considers a single negative at a time, leading to better embedding separation
856 for tasks such as image classification, retrieval, and verification. Here $f(\cdot)$ is the embedding func-
857 tion, x_a^i is the anchor, x_p^i is the positive sample of the same class, and $\{x_n^j\}$ are negatives from other
858 classes.
859

860
$$\mathcal{L} = \frac{1}{N} \sum_{i=1}^N \log \left(1 + \sum_{j \neq i} \exp \left(f(x_a^i)^\top f(x_n^j) - f(x_a^i)^\top f(x_p^i) \right) \right)$$

861

864 **Supervised contrastive loss** Khosla et al. (2021) extends contrastive loss by leveraging label information to pull together embeddings from all samples of the same class, rather than relying only
 865 on pairwise similarity. Unlike contrastive loss, which is limited to positive and negative pairs, supervised
 866 contrastive loss uses class supervision to exploit multiple positives per anchor, leading to
 867 richer and more discriminative representations. Here $P(i)$ is the set of indices of positives sharing
 868 the same class as anchor x_i , τ is a temperature scaling parameter, and $f(\cdot)$ is the embedding
 869 function.

871

$$872 \quad 873 \quad 874 \quad \mathcal{L} = \sum_{i=1}^N \frac{-1}{|P(i)|} \sum_{p \in P(i)} \log \frac{\exp(f(x_i)^\top f(x_p)/\tau)}{\sum_{a=1}^N \mathbf{1}_{[a \neq i]} \exp(f(x_i)^\top f(x_a)/\tau)}$$

875

876 **Proxy-Anchor Loss:** Proxy-Anchor Loss Kim et al. (2020) replaces anchors with learnable class
 877 representatives (proxies), removing the need for anchor sampling as in contrastive, triplet, or N-pair
 878 losses. Instead of comparing individual samples, embeddings are optimized against proxies, which
 879 serve as stable anchors for each class.

880

$$881 \quad 882 \quad 883 \quad \mathcal{L}_{PA} = \frac{1}{|\Theta_+|} \sum_{\theta_q \in \Theta_+} \log \left(1 + \sum_{z \in \mathcal{Z}_{\theta_q}^+} \exp(-\alpha \cdot (s(z, \theta_q) - \epsilon)) \right) \\ 884 \quad 885 \quad 886 \quad + \frac{1}{|\Theta|} \sum_{\theta_q \in \Theta} \log \left(1 + \sum_{z \in \mathcal{Z}_{\theta_q}^-} \exp(\alpha \cdot (s(z, \theta_q) - \epsilon)) \right)$$

887

888 A.3 IN CONTEXT LEARNING

889

890 In-context learning (ICL) Brown et al. (2020), is a paradigm that enables language models to perform
 891 tasks using only a few demonstrations without explicit parameter updates. Since demonstrations are
 892 expressed in natural language, ICL provides an interpretable interface for interacting with large
 893 language models (LLMs). Furthermore, ICL resembles the human decision-making process of learning
 894 through analogy Winston (1980). Unlike supervised training, ICL is a training-free framework that
 895 allows models to generalize to new tasks without additional computational costs for fine-tuning.

896

897 Based on Dong et al. (2024), several unsupervised strategies have been proposed to sample effective
 898 demonstrations for ICL. A simple yet effective method is to select the nearest neighbors of the input
 899 instance based on similarity measures (Liu et al. (2022), Tanwar et al. (2023), Qin et al. (2024)).
 900 Common distance metrics include L2 distance and cosine similarity derived from sentence embeddings.
 901 Beyond distance-based approaches, mutual information Sorensen et al. (2022) and perplexity
 902 Gonen et al. (2023) have also been shown to be useful for selecting prompts without labeled data or
 903 model-specific assumptions.

904

905 Although off-the-shelf retrievers provide convenient solutions for a wide range of NLP tasks, they
 906 are often heuristic and sub-optimal due to the absence of task-specific supervision. To overcome this
 907 limitation, supervised retriever-based methods have been introduced (Rubin et al. (2022) Ye et al.
 908 (2023) Wang et al. (2024) Zhang et al. (2022)). For instance, Rubin et al. (2022) proposed EPR, a
 909 two-stage framework for training dense retrievers to identify suitable demonstrations. Building on
 910 this, Li et al. (2023c) developed a unified retriever capable of selecting demonstrations across diverse
 911 tasks, while Mavromatis et al. (2023) introduced AdaICL, a model-adaptive method that leverages
 912 LLMs to predict outcomes for unlabeled data and assign uncertainty scores to guide demonstration
 913 selection.

914

915 Rodriguez-Cardenas et al. (2023) emphasized the sensitivity of demonstration selection by comparing
 916 two different prompt groups in a controlled experiment. One group exhibited a positive causal
 917 effect, improving the Average Treatment Effect (ATE) by 5.1% on Chatgpt, while the other group
 918 showed a negative causal effect, decreasing ATE by 3.3% relative to the control group. Here, ATE
 919 quantifies the average causal influence of a treatment (i.e., the chosen prompt group) on model
 920 performance. These findings highlight the critical role of demonstration quality: poorly chosen ex-
 921 amples may reduce performance, sometimes performing worse than LLMS that do not use ICL at

918 all. Throughout the paper, we use the terms demonstrations and examples interchangeably in the
 919 context of ICL.
 920

921 **B METHODOLOGY**
 922

923 **B.1 EVALUATION DATASET AND METRIC**
 924

926 MBPP dataset consists of 973 python programming questions. Each question contains a textual
 927 description of the function to be generated for evaluation. For each question, there are 3 pre-defined
 928 unit tests which the model-generated code has to pass. The samples also contain a reference code.
 929 The MBPP testset is a sampled set of 378 questions for evaluation. The MBPP+ dataset is also
 930 similar in terms to MBPP dataset except it was created by Liu et al. (2023) and here each question
 931 has more than 3 unit tests per question for evaluation.
 932

933 We employed the sampled prototypes as ICL demonstrations to generate code completions on the
 934 MBPP test set Austin et al. (2021), and evaluated the code completions using *pass@1* Chen et al.
 935 (2021) and *pass@10* Chen et al. (2021) metrics. We used the evalplus Liu et al. (2023) library
 936 for code post-processing and calculating the *pass@1* and *pass@10* metrics. The *pass@k* metric
 937 assesses the functional correctness of generated code by checking performance against predefined
 938 unit tests. Unlike CodeBLEU Ren et al. (2020), which only reflects surface-level similarity, *pass@k*
 939 is more reliable for evaluating functional correctness since it directly verifies whether at least one
 940 generated program passes the test cases.
 941

942 In *pass@k* metric, n is the total no.of problems, k ($n \geq k$) is the no.of code samples generated
 943 per problem, c ($c \leq n$) represents the count of correct samples which pass unit tests. A problem
 944 is considered solved if any sample passes the unit tests, and the total fraction of problems solved is
 945 reported.
 946

$$\text{pass}@k = \mathbb{E}_{\text{problems}} \left[1 - \frac{\binom{n-c}{k}}{\binom{n}{k}} \right]$$

947 The below is the architecture of h_θ neural network we used. It is a Single-layer network 3 with
 948 intermediate normalizations. For most of the LLMs the prototype size is set to 50. All of the layers
 949 of h_θ are used during training and updated via backpropagation.
 950

951 **Table 3: Model Architecture**
 952

953 Layer	954 Layer Parameters
954 Linear	(latent size z , Prototype size)
955 InstanceNorm1d	Prototype size z
956 ReLU	-

957 **B.2 TRAINING PARAMETERS**
 958

959 In the first stage of our framework, dedicated to prototype sampling, the network h_θ is trained for
 960 200 epochs on the training dataset D . Training utilizes two independent Adam optimizers: one
 961 for the network parameters and another for the proxy parameters. Both optimizers are initialized
 962 with a learning rate of $1e-3$, combined with a scheduler that decays the learning rate by a factor
 963 of $\eta_t = 0.97$. The dimensionality of the encoded vector z is determined by the underlying Large
 964 Language Model (M). A mini-batch size of 128 samples is maintained throughout training.
 965

966 For the initial set of experiments, the hyperparameters for manifold construction and manifold point-
 967 to-point loss estimation are configured as follows: $T = 90\%$, $\delta = 2$, $m = 3$, $N_\alpha = 4$, and
 968 $N_\beta = 0.5$. The momentum constant for updating θ_m is set to $\gamma = 0.99$. For Proxy Anchor loss, we
 969 employ $\alpha = 32$ and $\epsilon = 0.1$. These settings serve as the baseline configuration; subsequently, an
 970 ablation study is conducted on the above parameters for LLMs that exhibited comparatively lower
 971 performance than competing methods.
 972

972 All experiments were conducted on an NVIDIA RTX A6000 GPU. In the first stage of our method,
 973 we train a lightweight neural network h_θ to sample prototypes, which requires approximately 640
 974 MB of GPU memory and about 7 hours of training time without parallelization. With parallelized
 975 estimation of manifold-based similarities, the training time is reduced to roughly 2 hours, with a
 976 peak GPU memory usage of about 4700 MB across all LLMs.

977 Our proposed method demonstrates resource efficiency by requiring fewer demonstrations while
 978 achieving performance on par with fine-tuning approaches. This efficiency makes it particularly ad-
 979 vantageous in low-resource environments, where fine-tuning large language models demands sub-
 980 stantial GPU memory and training time. Furthermore, our method yields competitive improvements
 981 in code completion tasks compared to fine-tuning.

983 B.3 SAMPLING STRATEGIES

- 985 • **Similarity-based sampling:** The test query was encoded following the same procedure as in the
 986 Magicoder dataset. Demonstrations were then selected from each programming language class
 987 based on the closest Euclidean distance to the test query. This method would be sampling 9
 988 distinct prototypes from each class.
- 989 • **Diversity-based sampling:** We computed the mean vector for each class using the latent repre-
 990 sentations z and selected the sample closest to each class mean using Euclidean distance. This
 991 method would be sampling 9 distinct prototypes from each class.
- 992 • **Base model:** For the LLMs being tested no ICL demonstrations were provided, only the test query
 993 was provided.
- 994 • **MBPP Few shots:** The authors of the MBPP test set used and experimented with the samples
 995 at indexes 2, 3, 4 as ICL examples. In our experiments, we also use the same set of samples for
 996 comparison.
- 997 • **Prototype:** This term represents our method, where after finishing training we project the learned
 998 proxy vectors onto nearest training samples and use them as ICL demonstrations for code com-
 999 pletion. This method would be sampling 9 distinct prototypes from each class.

1001 B.4 CODE COMPLETION PROMPTS

1003 For every LLM, the following prompts were used to generate the code completions.

```
1004 ICL_examples = [(q1, s1), (q2, s2), ...]
1005 # where  $q_i$  is the code query and  $s_i$  is the code solution
1006
1007 icl_prompt = ''
1008 if ICL_examples is not None:
1009     for query, sol in ICL_examples:
1010         icl_prompt += f"You are an expert programmer, and here is your
1011         task: {prob}\n[BEGIN]\n{sol}\n[DONE]\n\n"
1012
1013 icl_prompt += f"You are an expert Python programmer, and here is your
1014         task: {test_problem}\n[BEGIN]\n"
```

1015 B.5 MODEL ANALYSIS

1017 The table presents the token lengths of sampled prototypes along with the 99th percentile, 95th
 1018 percentile, and average token lengths across the MBPP dataset for combined query and solution
 1019 inputs. Since each input consists of the sampled prototypes used as demonstrations together with
 1020 the MBPP test queries, we estimate the overall input token lengths to assess whether all prototypes
 1021 can be accommodated. These token length statistics are reported separately for each LLM.

1022 From the table, it can be observed that the sampled prototype token lengths exceed the context
 1023 window of the Falcon3-1B model. Therefore, for code completion on Falcon, we restricted the ICL
 1024 demonstrations to only the prototype representing the Python class, as it closely aligns with the
 1025 problems in the MBPP test set. The same procedure was applied across all sampling strategies for
 the Falcon3 model.

Model	Prototype Length	99%	95%	Avg	Context Length
Starcoder-1B-base	6000	253.8	186	80.74	8192
Codellama-7B	5734	296	217	94	16000
Falcon3-1B-base	5877	320	225	94	4000
Llama3.2-1B	4288	228	163	74	128000
Qwen2.5coder-0.5B	3054	228	166	73	32000
Qwen3-0.6B	5069	229	166	73	32000

Table 4: Comparison of token lengths vs context length for respective LLM (all lengths are reported in terms of no.of tokens)

The table also shows that the Codellama model, being code-specific, produces a higher number of tokens compared to the Llama3.2 model. This highlights the optimized tokenization techniques of the Llama3.2 series, as Codellama is derived from the Llama2 family of models. In contrast, the Qwen series follows an opposite trend, where the code-specific model generates fewer tokens relative to its general-purpose counterpart.

All reported scores in this paper have been independently recomputed across every model and sampling method. The results for the base model (without ICL) may differ from those documented in the official technical reports, which can be attributed to several factors. Based on our experimental findings, we outline the potential reasons that may have influenced performance aside from the ICL demonstrations.

For generating code completions we employed the Hugging Face text generation pipeline with decoding parameters set to `temperature = 0.6` and `top-p = 0.9`. Our experiments revealed that even minor adjustments to these parameters, with only two variations, led to improved performance across all models and sampling methods. Notably, most technical reports for benchmark evaluations do not specify the decoding strategies employed, which contributes to variability in reported results. This observation underscores the importance of performing hyperparameter optimization during the decoding stage of generation.

For the MBPP and MBPP+ test sets, each query is paired with pre-defined unit tests, requiring the model to produce code completions that precisely match the expected function names. While one way to ensure success would be to include the reference solution as a demonstration for each query, such an approach risks data leakage, as the model would be exposed to the ground-truth answers rather than generating them independently. To mitigate this issue, we deliberately excluded reference code solutions from the input queries.

It can be inferred that code sanitization procedures also play a crucial role in determining benchmark performance. In our experiments, we employed the evalplus library to sanitize the generated code completions. However, despite this sanitization, certain residual tokens were not removed, which in turn impacted the execution outcomes and consequently affected the reported performance. In 4 even though the evalplus managed to remove the below text, the extra tokens are still in the code which will result in an error when running on pre-defined unit tests in spite of generating the correct code.

C ABLATION STUDY

As outlined in Section B.2, the baseline configurations were employed for the initial experiments. To further investigate performance limitations, we conducted an ablation study focusing on LLMs that demonstrated comparatively weaker results. Specifically, under the baseline settings, the Llama3.2 and Qwen3 models underperformed relative to other methods. Consequently, we performed an extensive hyperparameter ablation on these models to better understand their sensitivities and performance dynamics.

C.1 EFFECT OF m

The parameter m denotes the dimension of the linear submanifold X_i , which locally approximates the data manifold around a point $h_\theta(z)$. To examine its effect, we vary m in the range [2, 8] with

```

1080
1081         def square_of_list(
1082             my_list):
1083             """Return the square of each
1084             element in my_list."""
1085             return [lambda x: x**2 for x in
1086                 my_list]
1087         END
1088     [END]
1089     The function should return a list
1090     of squares of each element in
1091     my_list. You should use lambda
1092     function to calculate squares.
1093     Hint: Use the built-in function sum
1094     () to calculate the square of
1095     each element in my_list.
1096
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1109
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1111
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1116
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1119
1120
1121
1122
1123
1124
1125
1126
1127
1128
1129
1130
1131
1132
1133

```

```

def square_of_list(
    my_list):
    """Return the square of each
    element in my_list."""
    return [lambda x: x**2 for x in
        my_list]
END
[END]

```

Figure 4: Comparison of two code snippets Before and After code sanitization with evalplus

a step size of 1. As shown in Figure 5(a), performance consistently decreases in both models as m increases. This trend arises because X_i is intended to approximate the immediate neighborhood of a point, which is inherently low-dimensional. Larger values of m may lead to overfitting, since only a limited number of nearby samples are available within a batch to reliably estimate X_i , thereby degrading performance. Furthermore, we observe that the computational overhead for prototype sampling increases with larger m , underscoring the trade-off between accuracy and efficiency.

C.2 EFFECT OF γ

The parameter γ denotes the momentum constant used to update the proxy vector θ_m during prototype sampling. Following He et al. (2020), higher values of γ are expected to yield improved performance, as the proxy updates become smoother and more stable. Consistent with this observation, Figure 5(b) shows that in both models, performance improves as γ increases, highlighting the importance of stable momentum updates for effective representation learning.

C.3 EFFECT OF N_α & N_β

The parameters N_α and N_β control the decay of similarity based on the orthogonal and projected distances, respectively, of a point from the linear submanifold in the neighborhood of another point. We vary N_α in the range [1, 6] with a step size of 1, and N_β in the range [0.5, 3] with a step size of 0.5. As shown in Figure 5(c), increasing N_β leads to a slight performance gain in the Qwen2.5-Coder model, while the Llama3.2 model exhibits larger fluctuations but follows an overall upward trend. Similarly, Figure 5(d) shows that performance improves marginally with larger N_α in the Qwen2.5-Coder model, whereas the Llama3.2 model demonstrates a clearer and more consistent increase. This effect can be explained by the relationship between N_α and N_β : as N_α approaches N_β , a point A at distance ε within the linear neighborhood of a point B (and thus sharing many features with B and its neighbors) may be treated as equally dissimilar to B as another point C located at an orthogonal distance ε from the neighborhood of B .

C.4 EFFECT OF T

The reconstruction threshold T determines the quality of points admitted into the linear submanifold X_i . We vary T in the range [0.7, 0.95] with a step size of 0.05. As shown in Figure 5(e), both models exhibit a clear upward trend in performance as T increases, underscoring the importance of ensuring that only high-quality points are incorporated into X_i . While the Llama3.2 model follows this overall increasing trend, it displays noticeable fluctuations compared to the more stable improvement observed in the Qwen2.5-Coder model.

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C.5 EFFECT OF δ

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The scaling factor δ regulates the maximum separation between dissimilar points. We vary δ in the range [0.8, 3.2] with a step size of 0.4. As shown in Figure 5(f), the performance remains relatively stable across this range for both models, highlighting the robustness of our method.

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C.6 EFFECT OF α

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The scaling factor α controls the sharpness of the exponential term in the Proxy Anchor loss. We vary its value over 5, 10, 15, 20, 25, 30, 32. As shown in Figure 5(g), both models exhibit an overall increasing trend in performance with larger α . However, the Qwen2.5-coder model displays higher fluctuations compared to the more stable Llama3.2 model.

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C.7 EFFECT OF ϵ

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The margin parameter ϵ enforces that positive embeddings are pulled within this distance from their corresponding class proxies. We vary its value across 0.001, 0.005, 0.05, 0.1, 0.2. As shown in Figure 5(h), the Qwen2.5-coder model demonstrates stable performance across the range of ϵ , whereas the Llama3.2 model exhibits a decreasing trend with noticeable fluctuations. This indicates that larger values of ϵ impose overly strict constraints on the separation between positive and negative proxies, thereby hindering the embeddings from effectively satisfying the margin requirement.

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C.8 OVERALL EFFECT

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From Figure 5, we observe that the Llama3.2 model exhibits high sensitivity to parameter variations, displaying substantial fluctuations in performance. This trend aligns with the results reported in Tables 1 and 2, where the similarity-based sampling method achieves the highest score for Llama3.2, further highlighting its instability under different configurations. In contrast, the Qwen2.5-coder model demonstrates relatively stable behavior, showing consistently increasing trends across most parameters, with the notable exception of the scaling factor α .

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D AST ANALYSIS

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D.1 INTERPRETABLE SYNTAX SETS AND INTERACTIONS

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Token Set τ , this set contains the code tokens w_i derived from the generated code snippets C , where each token's confidence is computed as outlined in 5. **Subcategory Set** v , this set consists of elements from Context-Free Grammars (CFGs), which are rules that capture the syntactic and structural aspects of a programming language. Formally, a CFG is defined as $G = (\alpha, \lambda, \omega, \beta)$, where α is the finite set of non-terminal nodes, λ the finite set of terminal nodes, ω the finite set of production rules, and β the start symbol. CFGs utilize terminal and non-terminal nodes (i.e., subcategories) to specify production rules ω for statements such as conditionals, assignments, or operators. Importantly, terminal and non-terminal nodes serve distinct purposes. These nodes correspond to the elements of the subcategory set v , with $\lambda, \alpha \in v$.

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The interaction between the token set τ and the subcategory set v is governed by the **Alignment Function** δ . This function establishes a many-to-one or one-to-one mapping from each token w_i in the token set τ to a terminal node λ in the subcategory set v . For example, Fig.2 2 shows the alignment of the token 'try_' with the terminal node 'try', where the character '_' is disregarded. It is important to note that tokenization may produce sequences in which tokens do not align one-to-one with terminal nodes. For instance, Fig.2 2 illustrates how the tokens 'flo_' and 'at' are both aligned with the terminal node 'float'. Formally, this can be expressed as $\delta('flo_','at') \rightarrow ['float']$, representing a many-to-one mapping. Thus, the alignment between code tokens and terminal nodes is strictly many-to-one (which includes the special case of one-to-one), but never one-to-many or many-to-many.

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Category Set Λ . Step 3 in Fig.1 1 illustrates how λ and α are combined into a category $c \in \Lambda$. The elements of the Category Set Λ are referred to as Syntax Categories (SCs). Based on tree-sitter bindings for Python, we define eight distinct SCs. These categories represent semantic units

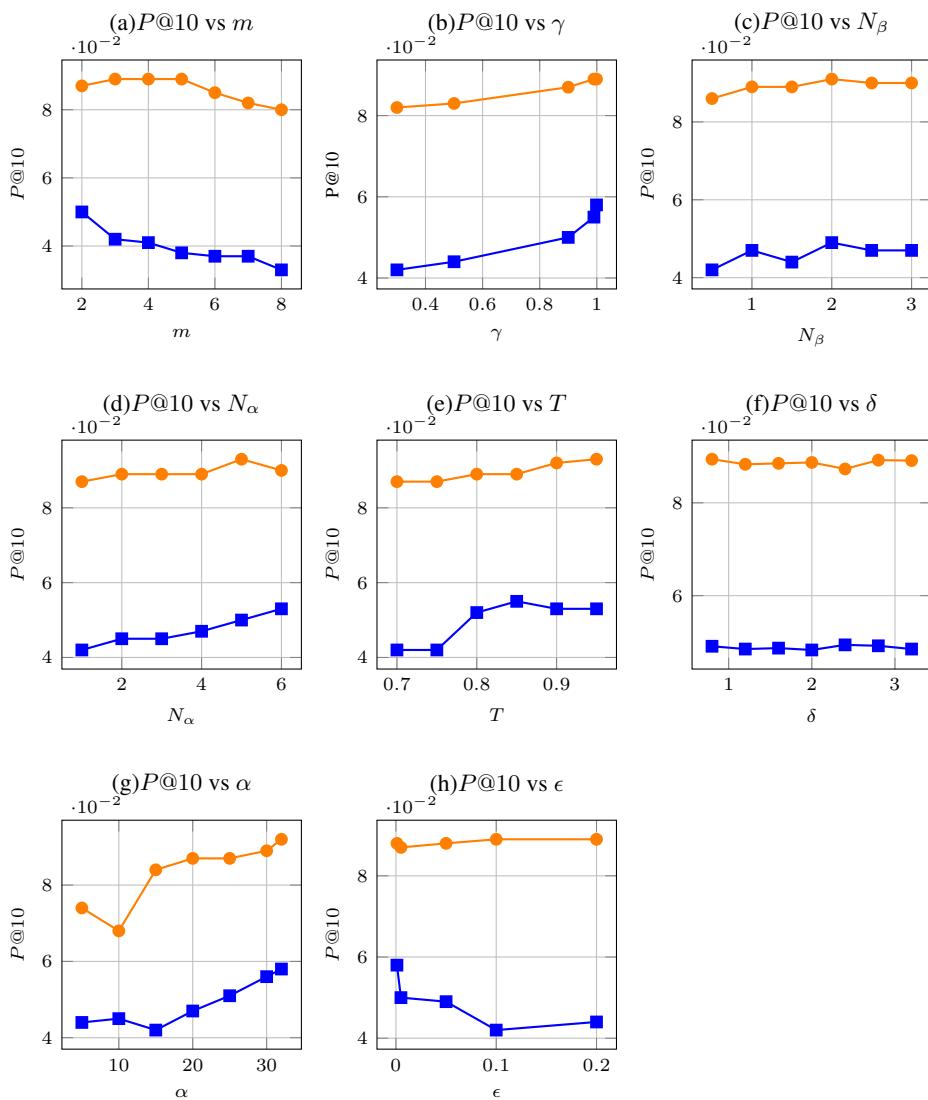


Figure 5: Ablation study of Qwen2.5-Coder-0.5B and Llama3.2-1B models. █ Qwen2.5-Coder-0.5B
█ Llama3.2-1B

that facilitate the syntax-level interpretability of LLMs. Consequently, AST analysis provides a developer-oriented explanation of Token-Level confidence. In summary, each token in a sequence s can be mapped to a category $c \in \Lambda$. Through AST analysis, developers can directly relate LLM code predictions to meaningful structural attributes.

A **clustering function** ζ computes the confidence performance of λ and α nodes (subcategories) within an AST by hierarchically aggregating Token-Level Confidences into a category $c \in \Lambda$. After tokens are aligned to their respective nodes using δ , AST analysis groups them into either their corresponding category or non-terminal α node, following the AST structure. In some cases, terminal λ nodes may be directly aggregated into a category without involving intermediate non-terminal α nodes. The function ζ can be configured to use different aggregation strategies, such as average, median, or maximum. In our experiments, we define the clustering function as $\zeta : v \rightarrow \text{avg}(w_{1:i})$ for a subset of tokens $w_{\leq i}$. The 8 defined syntax categories are:

1242 • Decisions
1243 • Data Structures
1244 • Exceptions
1245 • Iterations
1246 • Functional Programming
1247 • Operators
1248 • Scope
1249 • Data Types

1247 E LLM USAGE

1248 LLM was used to improve the quality of writing, and to assist in the LaTeX code review; it was not
1249 used during the ideation or experimentation phase.

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