
LithoSim: A Large, Holistic Lithography Simulation Benchmark for AI-Driven Semiconductor Manufacturing

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Abstract

Lithography orchestrates a symphony of light, mask and photochemicals to transfer the integrated circuit patterns onto the wafer. Lithography simulation serves as the critical nexus between circuit design and manufacturing, where its speed and accuracy fundamentally govern the optimization quality of downstream resolution enhancement techniques (RETs). While machine learning promises to circumvent computational limitations of lithography process through data-driven or physics-informed approximations of computational lithography, existing simulators suffer from inadequate lithographic awareness due to insufficient training data capturing essential process variations and mask correction rules. We present LithoSim, the most comprehensive lithography simulation benchmark to date, featuring over 4 million high-resolution input-output pairs with rigorous physical correspondence. The dataset systematically incorporates alterable optical source distributions, metal and via mask topologies with optical proximity correction (OPC) variants, and process windows reflecting fab-realistic variations. By integrating domain-specific metrics spanning AI performance and lithographic fidelity, LithoSim establishes a unified evaluation framework for data-driven and physics-informed computational lithography. The data (<https://huggingface.co/datasets/grandiflorum/LithoSim>), code (<https://dw-hongquan.github.io/LithoSim>), and pre-trained models (<https://huggingface.co/grandiflorum/LithoSim>) are released openly to support the development of hybrid ML-based and high-fidelity lithography simulation for the benefit of semiconductor manufacturing.

1 Introduction

Simulation stands as a cornerstone of modern artificial intelligence (AI), enabling data-driven emulation of complex physical system, from protein folding dynamics [1] to climate modeling [2, 3, 4]. These AI-powered simulation not only accelerate computational cost [5, 6] but also unlock closed-loop optimization paradigms by bridging synthetic data simulation with differentiable physical models [7, 8]. A critical application of this paradigm is in semiconductor manufacturing, specifically lithography simulation [9, 10]. Lithography is a optical and chemical system of transferring intricate circuit patterns M onto silicon wafers using light J with a fixed projector H depicted in Figure 1(b). However, at nanometer scales, fundamental physics of optical diffraction and unavoidable manufacturing variations (*a.k.a.* process variations) distort the intended patterns. Techniques called resolution enhancement technologies (RETs) [11, 12, 13], such as optical proximity correction (OPC) and source mask optimization (SMO) shown in Figure 2, are used to pre-distort the design masks to

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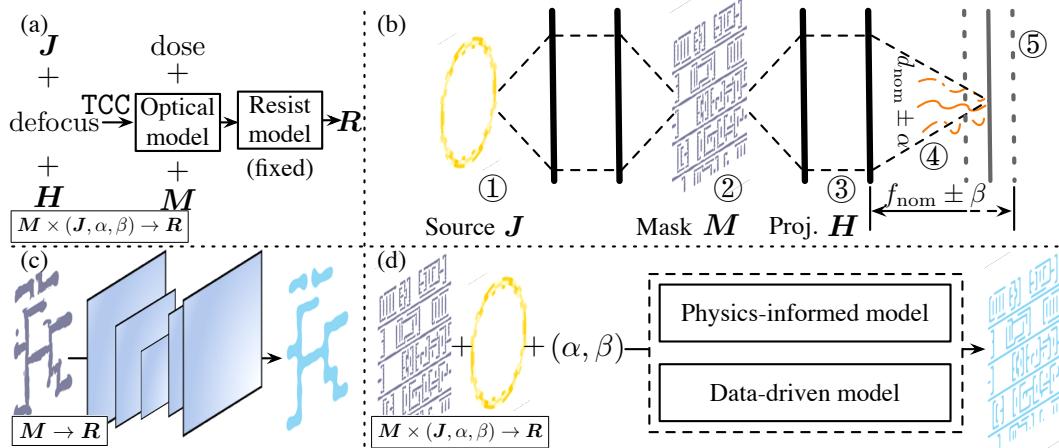


Figure 1: (a). Lithography simulation tools by combining source and defocus on a fixed projector to create an optical model (TCC in Appendix A.1), then using mask and dose inputs to generate resist. (b). Physical lithography setup comprises 5 primary elements: ① An adjustable illumination system J . ② The mask setup M with a basic binary design made of see-through and non-see-through sections. ③ An aligned and fixed projection module H . ④ An exposure mechanism with 2 critical process variation (α, β) . ⑤ A resist station to yield the end produced resist R . (c). Previous benchmark [14] at 45nm node considering source and process variations as constants, using DNNs for limited surrogate models $M \rightarrow R$. (d). Our benchmark at sub-28nm node considers simulation across larger mask ranges with source and process variations, using data-driven or physics-informed generative models for holistic simulation $M \times (J, \alpha, \beta) \rightarrow R$ with all the elements ① to ⑤.

Table 1: Comparison of Lithography Simulation Benchmarks.

Items	CAD13 [15]	ISPD19 [16]	N14 [17]	LithoBench [14]	LithoSim
# of Var.	source	×	×	×	620
	dose	3	×	×	13
	defocus	2	×	×	5
Mask Config.	Type	M	V	V	M/V
	Num.	5k	21k	1.6k	16k/115k
	Size	4	4	4	4/1
Tech. Node	Metal	32	–	–	32
	Via	–	40	14	45
# of Output	resist	30k	21k	1.6k	> 4M

Mask size and Tech. node measurements in μm^2 and nm, respectively. $k = 1,000$, $M = 1,000,000$. In mask type, M: Metal, V: Via, OPC: mask optimization for compensating optical diffraction.

compensate for these effects, aiming to print the desired pattern accurately. RET workflows heavily rely on simulating the lithography process.

Traditional lithography simulators use complex physical models like Figure 1(a) that are computationally extremely expensive with $> 10^3$ CPU-hours per square millimeter. This bottleneck makes simulation and RET optimization slow and impractical. Machine Learning (ML) offers a promising path by learning differentiable image-to-image translation between the input mask design M and the final printed resist pattern R in Figure 1(c), bypassing the costly physics solvers to create fast surrogate models [18].

However, current public datasets for ML-based lithography such as CAD13 [15], ISPD19 [16], N14 [17], and LithoBench [14] listed in Table 1 are inadequate for developing models that meet RET requirements, suffering from 3 key limitations. First, datasets are outdated scaling, primarily covering older $32 \sim 45\text{nm}$ technology nodes, not the cutting-edge sub-28nm nodes used in advanced lithography. Second, mask scales, typically $\leq 4\mu\text{m}^2$, are too small to capture crucial optical proximity effects. Third, They lack 4 essential variations that RET must handle: different types of mask M with

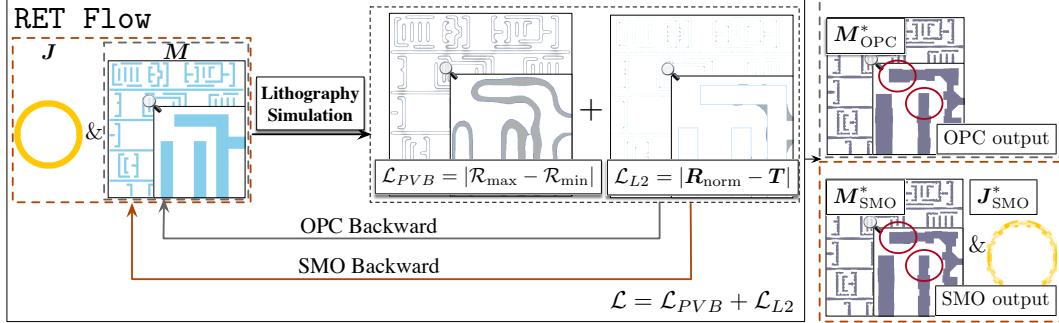


Figure 2: Overview of RETs (OPC and SMO).

or without OPC [19], variations in the light source shape and intensity \mathbf{J} , fluctuations in exposure dose α , deviations in defocus β of fixed projector \mathbf{H} shown in Figure 1(b). This lack of realism severely limits the practical lithography of models trained on current datasets for differentiable optimization applications [11, 12, 13, 19, 20, 21, 22, 23, 24, 25, 26, 27] in Figure 2, where accurately simulating the interaction of all these physical variables is essential.

For real semiconductor manufacturing, Lithography simulation forms the computational backbone of modern RETs. As illustrated in Figure 2, RET relies on iterative, physics-aware feedback from the simulator to optimize mask \mathbf{M} and illumination source \mathbf{J} listed in Appendix A.2. The goal is to minimize a composite loss function that includes the contour fidelity under nominal conditions and robustness across process variations. This necessitates a simulator that is not only fast but also accurately models the interaction of all physical variables, a capability absent in existing benchmarks.

To address those critical gaps, we introduce LithoSim illustrated in Figure 1(d), a comprehensive benchmark designed to enable the development and evaluation of ML models for practical lithography simulation and differentiable RET optimization. LithoSim provides:

- Masks at sub-28nm nodes, both with and without OPC, covering larger scales with $16\mu\text{m}^2$ to capture proximity effects.
- Extensive parametric combinations listed in Table 1 covering over 600 distinct source configurations with **annular**, **quadrupole**, and **dipole** illuminations, 13 dose variation levels spanning from -12% to $+12\%$ of the nominal value, and 5 defocus offsets over a range of $\pm 80\text{nm}$, mirroring the key variables in RET flow.
- The first unified benchmark and evaluation framework to assess modern deep learning architectures (CNNs [28], Vision Transformers [29], physics-informed models like FNO-based flows [21, 17], and SOCS [30, 10]) on their ability to simulate lithography patterns with metrics both in ML and lithography domain.
- A unique out-of-distribution (OOD) evaluation for model generalization under varying mask conditions, a core requirement for RET. Specifically, it allows testing models trained on OPC’ed masks on completely non-OPC’ed masks, as well as the reverse. This directly mimics the flow where mask \mathbf{M} is iteratively modified during differentiable optimization like OPC and SMO, while a robust simulator must remain accurate even as the input mask changes significantly between iterations.

2 Related Work

The advancement of ML-based lithography simulators is hampered by the limited scope of existing metal [15] and via [16, 17] datasets. Current metal layer data, such as CAD13 [15], relies predominantly on only 10 base patterns at the 32nm node, artificially augmented via rotation and reflection to generate 4,875 synthetic variants under identical design rules [11]. Similarly, via layer datasets comprise fragmented sub-regions of full-chip layouts [16, 17], simulated under idealized and fixed process conditions. While these resources have facilitated initial research into data-driven architectures [28, 31, 32] and physics-informed models [17, 30], they fundamentally lack critical manufacturing parameters, especially notably, realistic source illuminator profiles and process varia-

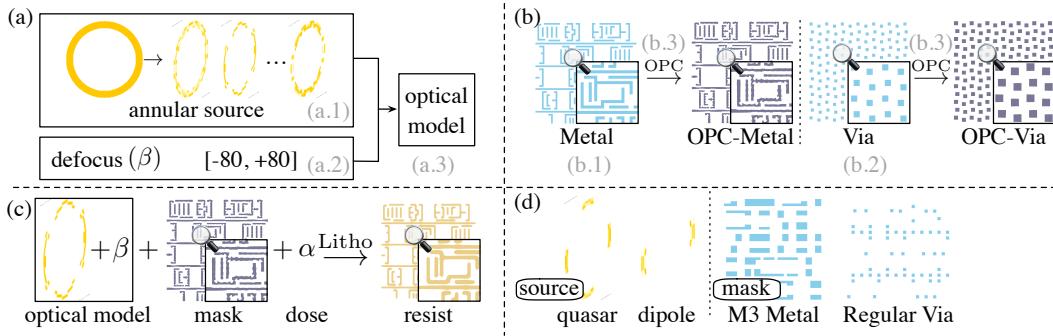


Figure 3: LithoSim Dataset Collection Pipeline. (a). Source & Optical Model Generation: (a.1) generates sources \mathbf{J} with normalized intensity distributions, (a.2) applies defocus levels per source, (a.3) output $>1,800$ optical models via simulation tool. (b). Mask Preparation: (b.1) extracts layout clips from full-chip M1 design. (b.2) synthesizes via layouts with foundry design rules. (b.3) processes original designs with OPC to generate OPC'ed masks. (c). Resist Synthesis: simulates resists \mathbf{R} via simulation tool. (d).Out-of-Distribution (OOD) Benchmark: generates for testing model generalization to unseen conditions.

tions used in rigorous simulation [9, 10, 33]. This omission ultimately renders the resulting models unsuitable for RET-oriented optimization.

Recent advances in fabrication-aware neural lithography, such as bilevel optimization [26, 13] and end-to-end differentiable neural pipeline [24, 34], highlight the critical role of manufacturing-digital twins in closing design-to-fabrication gaps. While these approaches [26, 24] excel at modeling post-lithography 3D topography, LithoSim addresses a complementary challenge: it focus on predicting resist contours under optical and process variations directly supports emerging differentiable ILT like [20, 23, 22]. By providing standardized evaluation of PV-band generalization critical for mask optimization in [25, 35, 27], LithoSim bridges the gap between high-fidelity physical emulation and optimizers requiring differentiable surrogates.

3 LithoSim Dataset Construction

3.1 Experiment Outline

The experimental framework formulates lithography simulation as a high-dimensional regression problem with four complementary input modalities: source, mask, dose, and defocus. Mask inputs $\mathbf{M} \in \{0, 1\}^{W \times H}$ represent binary patterns at sub-28nm resolutions, with dimensions scaling as $16\mu\text{m}^2$ ($W = H = 4096$) to capture proximity effects. Source configurations $\mathbf{J} \in \mathbb{R}^{N \times 3}$ describe particular light source distribution through N discrete source points j_i ($i \in [0, N]$), each defined by normalized intensity $v_i \in [0, 1]$ and Cartesian coordinates $(x_i, y_i) \in [-1, 1]^2$. Dose and defocus parameters (α, β) introduce controlled process variations, where dose modulates exposure energy $\alpha \in [-0.12, 0.12]$ while defocus emulates lens aberrations $\beta \in [-80, 80]$, conforming commonly used variations in real simulations.

All the experiments is trained and tested with 4 H100 Graphics cards with Intel Core Xeon Platinum 8462Y+ processors with Adam optimizer and a 10^{-4} learning rate of 10^{-5} weight decay. Either a linear combination of BCE and Dice loss, or only MSE is used as loss fuction.

3.2 Dataset Collection

The dataset is generated through a scalable lithography simulation pipeline executed on 100 parallelized CPUs, following the simulation flow illustrated in Figure 1 (a). To ensure diversity and physical fidelity, the source and mask integrates manufacturing-specific design rules and rigorous computational lithography principles. Following advanced lithography, we set NA is 1.35 and wavelength is 193nm, incorporating Zernike lens aberrations up to 37 terms. Optical model needs to be built before the simulation and each requires approximately 40 minutes to complete the process.

Table 2: Details of LithoSim Benchmark.

Dataset	Train	Val	Test	Total
OPC-Metal	693, 330	99, 000	198, 000	990, 330
Metal	903, 672	129, 096	258, 423	1, 291, 191
OPC-Via	655, 842	93, 654	187, 341	936, 837
Via	607, 365	86, 757	173, 514	867, 636
OOD	–	–	1, 580	1, 580

Subsequent resist simulations consume 15 seconds per pattern, generating final 4096×4096 images with 1nm/pixel resolution.

Source and Optical Model Generation. A total of more than 600 annular illumination sources with $0 \sim 1$ normalized intensity distributions are first synthesized based on the central symmetry of off-axis illumination as well as the classical values of the inner and outer radium. For each source, three defocus values (-40nm , 0nm , $+40\text{nm}$) are applied to simulate process variations, yielding more than 1,800 unique optical models using the rigorous lithography simulator following Figure 3 (a).

Mask Preparation. As illustrated in Figure 3 (b), two types of mask are constructed: (1) **Metal Layer:** 1,200 layout clips (16nm^2 each) are extracted from a full-chip M1 layer design. These clips are processed through optical proximity correction (OPC) using the optical models, generating paired Metal (original) and OPC-Metal (corrected) mask sets; (2) **Via Layer:** 1,200 via layouts adhering to foundry design rules are synthesized and similarly corrected via OPC, producing Via and OPC-Via mask sets.

Resist Synthesis. 4 types of mask datasets (Metal, OPC-Metal, Via, OPC-Via) are combined with $\pm 10\%$ normalized dose variations and calculated through corresponding optical model to simulate resist profiles. This cross-condition sampling strategy produces a comprehensive in-distribution dataset capturing multi-physics interactions across source distributions, mask types, and process variations shown in Figure 3 (c).

Out-of Distribution (OOD) Dataset. To evaluate model generalization, 20 additional illumination sources (10 dipole, 10 quasar) are designed. These sources with ± 80 defocus and $\pm 12\%$ dose are paired with 20 layout clips from M3 and via layers of a distinct CPU design illustrated in Figure 3. The OOD dataset is generated using identical simulation pipelines but exhibits structural and process condition disparities compared to the primary dataset.

Following the above data collection guidelines, LithoSim benchmark in Table 2 combines high-throughput computational lithography with AI-oriented data diversity, producing widely distributed multi-parameters (source, mask, dose, defocus) to resists mappings. Figure 4 visualizes all the datasets with different lithography conditions in LithoSim. OPC’ed masks (OPC-Metal and OPC-Via) yield resists with smaller edge placement error compared with non-OPC’ed masks. Compared to nominal dose, a positive deviation expands resist area while a negative deviation induces the undercut of resist. Defocus perturbations introduce subtler but critical effects, inducing $< 1\text{nm}$ resist contour shifts that ML-based models must capture to enable robust RET. A slight bias also occupies in the correction of the same mask by different light sources. The systematic variation of optical models, mask corrections, and essential process parameters establishes a robust foundation for data-driven and physics-informed lithography modeling.

3.3 Dataset Split

LithoSim benchmark in Table 2 is partitioned to evaluate simulation performance across in-distribution and out-of-distribution (OOD) scenarios. For each mask category (Metal, OPC-Metal, Via, OPC-Via), the corresponding data samples are stratified into training (70%), validation (10%), and testing (20%) subsets. The validation set serves for hyperparameter tuning and early stopping, while the test set quantifies in-distribution predictive accuracy. Crucially, splits are performed independently per mask type to prevent cross-contamination between original (Metal, Via) and OPC-corrected (OPC-Metal, OPC-Via) layouts, mitigating biases in learning mask-correction synergies.

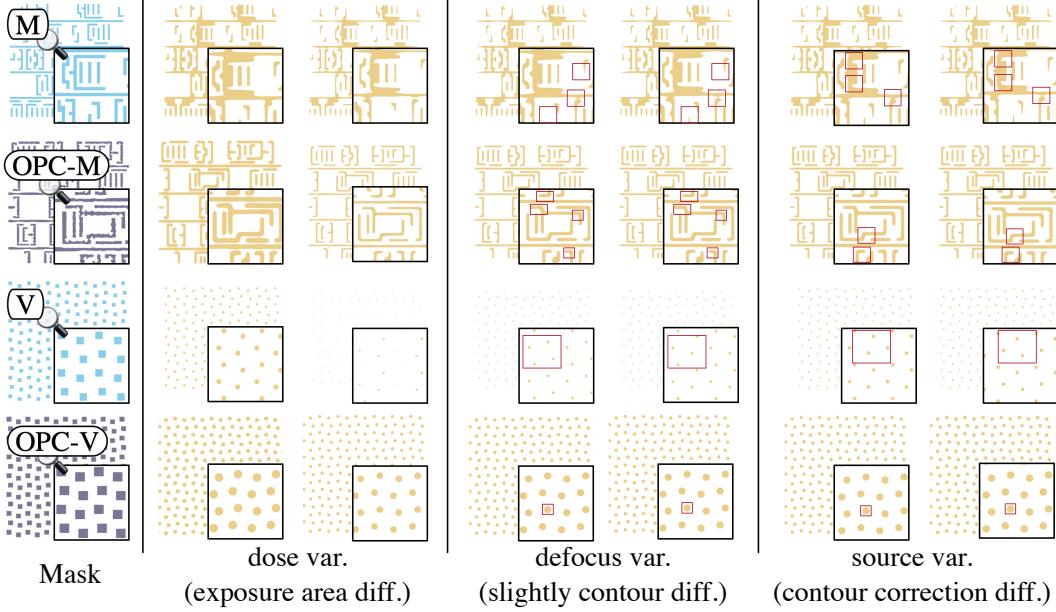


Figure 4: The splits of LithoSim benchmark and comparison of different lithography conditions.

To assess generalization beyond training distributions, the OOD dataset, comprising M3/via layer clips and unconventional illumination (dipole, quasar), is reserved exclusively for testing. This separation ensures that OOD evaluation reflects real-world scenarios where models encounter unseen design rules, optical conditions, or process variation drifts.

4 Experiments

4.1 Baseline Architectures

We establish six baseline architectures for lithography simulation, comprising 2 data-driven models (ED-CNN, ED-Trans) and 4 physics-informed variants (RFNO, CFNO, MFNO, SOCS). We also add an **electromagnetic (EM) approximation method** as an upper bound. ML models should asymptotically approach this white-box results. Crucially, a viable ML model must demonstrate robust performance not only on in-distribution data but also on out-of-distribution cases. This requirement stems from the industry’s stringent criterion that edge placement error (EPE) should remain below 1nm in lithography simulation regardless of mask variations to qualify for small-scale industrial testing. Implementation details appear in Appendix A.4.

All baselines share unified conditional encoding schemes: 2D continuous positional encoding and chunk-based compression with dynamic query generation as well as hierarchical attention (intra-chunk local attention followed by cross-chunk global aggregation) for source coordinates ($[B, N, 3] \rightarrow [B, N, D] \rightarrow [B, K, D]$, $K \ll N$) while 1D encoding for dose and defocus variations ($[B, 1] \rightarrow [B, D]$). All condition is embedded into backbones using chunked litho-aware attention, which enables memory-efficient cross-attention between masks and lithography parameters (source, dose, defocus) through compressed conditions and chunk-wise computation. Implementation details appear in Appendix A.3.

Encoder-Decoder CNN (ED-CNN). It implements hierarchical encoder-decoder processing following CNN-based [28, 31, 36] flow. The encoder employs cascaded ResNet blocks with channel-wise multipliers and non-local attention at specified resolutions. Chunked cross-attention fuses physical parameters (source, dose, and defocus) at the bottleneck. The decoder uses transposed convolutions and residual attention blocks for detail-preserving upsampling.

Encoder-Decoder Transformer (ED-Trans). It introduces spatial-domain transformers [37] through patch embedding and sequence processing. Input masks are projected and reshaped to enable standard

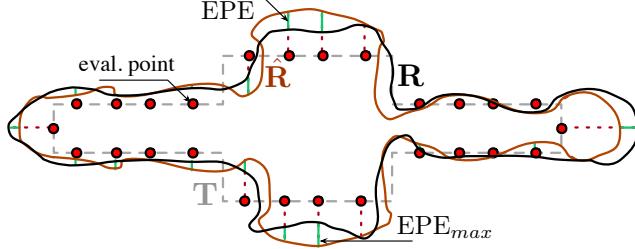


Figure 5: Illustration of EPE calculation.

transformer operations in sequence. Then, sequence-based masks are processed by four transformer layers with learnable positional encoding. Following cross-attention fusion of source, dose, and defocus, depth-wise transformers enable hierarchical abstraction before spatial reconstruction via inverse projection.

Reduced FNO (RFNO). It employs a reduced Fourier neural operator [17, 38] in Figure 6 that operates masks in the frequency domain through parameterized low-rank kernel convolutions in Fourier space, utilizing truncated mode interactions to capture global low frequency. The architecture explicitly bridges spectral (RFNO) and spatial (CNN) representations, then fuses physical parameters to reconstruct final resists.

Convolutional FNO (CFNO). It introduces a convolutional Fourier neural operator [21] in Figure 7 that synergizes spectral transformations with spatial convolutions for efficient operator learning. CFNO first decomposes high-dimensional masks into localized patches, projects them into the Fourier domain via FFT, and applies a parameterized linear transformation to capture global interactions. These spectral features are then mapped back to the spatial domain through inverse FFT and restructured into geometric masks. The architecture also cat spectral CFNO and spatial CNN, then fuses physical parameters and generate resists via a decoder.

Mixed FNO (MFNO). It leverages both global frequency-domain correlations [39] through CFNO and spatial locality via RFNO [17]. MFNO in Figure 8 processes masks through spectral decomposition in localized chunks, employing separate parameterized weights for low-frequency and high-frequency components to enable multiscale frequency modulation. Masks are partitioned into spatial chunks where Fourier transforms extract frequency features, with truncated modes reducing computational complexity while preserving dominant spectral patterns. A CNN enhances local feature interactions after inverse Fourier reconstruction.

Sum of Coherent Sources (SOCS). It introduces a physics-inspired framework, drawing parallels to the optical lithography process [30, 10] (see Appendix A.1). SOCS first transforms masks into frequency domain through FFT, followed by a dedicated complex-valued encoder comprising cascaded complex-ResNet blocks and complex-attention mechanisms to preserve phase-aware representations. Lithography parameters are adaptively integrated through chunked complex litho-aware attention, enabling parameter-conditioned feature fusion. Spatial details are subsequently recovered via a complex decoder architecture that synergistically combines complex transposed convolution operators with complex-ResNet. The final resist profile prediction is achieved through inverse FFT (IFFT) followed by sum of mask decomposition to reconstruct the spatial-domain results.

4.2 Evaluation Metrics

We provide popular deterministic metrics in the machine learning and lithography simulation on semiconductor manufacture, including MSE, PA, mIOU, EPE_{max} and EPE_{avg} . Details of metrics are list in Appendix A.5.

- **Mean Squared Error (MSE)** is sensitive to penalize outliers, which is critical for evaluating generalization ability of lithography simulation (Eq. 19).
- **Pixel Accuracy (PA)** is used to evaluate overall accuracy of resists (Eq. 20).
- **Intersection Over Union (IOU)** is used to evaluate detailed pixel differences of resists (Eq. 21).

Table 3: Comparison of multi-scale ML-based lithography simulation.

Data	Method	MSE	PA	IOU	EPE _{max}	EPE _{avg}	TAT
		$\times 10^{-3}(\downarrow)$	%(\uparrow)	%(\uparrow)	nm(\downarrow)	nm(\downarrow)	ms(\downarrow)
OPC-Metal	ED-CNN	11.51 \pm 8.39	98.85 \pm 0.84	91.06 \pm 6.30	1.75 \pm 0.49	1.47 \pm 0.28	8.94 \pm 0.24
	ED-Trans	19.67 \pm 9.32	98.03 \pm 1.33	85.12 \pm 9.15	2.03 \pm 0.69	1.81 \pm 0.72	11.64 \pm 0.25
	RFNO	9.72 \pm 6.49	99.03 \pm 0.65	92.42 \pm 5.00	1.70 \pm 0.56	1.12 \pm 0.38	9.91 \pm 0.31
	CFNO	20.15 \pm 9.24	97.98 \pm 1.42	84.84 \pm 1.42	2.96 \pm 0.72	2.36 \pm 0.59	10.00 \pm 0.42
	MFNO	6.28 \pm 3.84	99.37 \pm 0.38	95.29 \pm 2.44	1.29 \pm 0.28	1.02 \pm 0.27	9.98 \pm 0.31
	SOCS	7.94 \pm 4.30	99.18 \pm 0.51	93.17 \pm 5.67	1.55 \pm 0.32	1.07 \pm 0.58	8.51 \pm 0.20
Metal	EM	5.83	99.51	97.32	1.02	0.74	289.62×10^3
	ED-CNN	8.06 \pm 5.17	99.09 \pm 0.52	92.32 \pm 4.62	1.64 \pm 0.24	1.30 \pm 0.40	9.12 \pm 0.27
	ED-Trans	9.89 \pm 5.14	99.01 \pm 0.51	91.69 \pm 5.14	1.71 \pm 0.30	1.37 \pm 0.25	11.30 \pm 0.24
	RFNO	13.59 \pm 8.94	98.64 \pm 0.89	88.58 \pm 7.29	1.84 \pm 0.36	1.53 \pm 0.39	9.49 \pm 0.29
	CFNO	13.08 \pm 7.13	98.69 \pm 0.71	89.11 \pm 5.81	1.71 \pm 0.48	1.50 \pm 0.48	10.00 \pm 0.25
	MFNO	8.39 \pm 5.38	99.03 \pm 0.54	92.18 \pm 3.62	1.65 \pm 0.33	1.33 \pm 0.29	10.55 \pm 0.34
OPC-Via	SOCS	9.35 \pm 7.39	99.01 \pm 0.70	91.95 \pm 6.31	1.82 \pm 0.38	1.35 \pm 0.38	8.20 \pm 0.22
	EM	7.05	99.33	96.05	1.31	0.99	281.07×10^3
	ED-CNN	5.36 \pm 3.96	99.46 \pm 0.40	90.68 \pm 5.65	1.96 \pm 0.37	1.59 \pm 0.42	9.03 \pm 0.24
	ED-Trans	5.56 \pm 3.63	99.44 \pm 0.36	89.99 \pm 5.72	1.94 \pm 0.30	1.67 \pm 0.33	11.14 \pm 0.22
	RFNO	3.91 \pm 2.28	99.61 \pm 0.23	92.68 \pm 4.32	1.85 \pm 0.27	1.42 \pm 0.28	9.70 \pm 0.31
	CFNO	6.87 \pm 5.14	99.31 \pm 0.51	87.67 \pm 8.09	2.10 \pm 0.41	1.84 \pm 0.35	10.19 \pm 0.27
Via	MFNO	6.04 \pm 3.97	99.40 \pm 0.39	90.99 \pm 4.54	1.99 \pm 0.25	1.50 \pm 0.23	10.72 \pm 0.34
	SOCS	5.28 \pm 3.61	99.49 \pm 0.52	91.12 \pm 7.02	1.98 \pm 0.63	1.79 \pm 0.58	8.02 \pm 0.27
	EM	3.52	99.71	95.65	1.15	0.92	276.19×10^3
	ED-CNN	4.65 \pm 2.95	99.54 \pm 0.30	81.39 \pm 8.95	1.07 \pm 0.29	0.93 \pm 0.34	8.92 \pm 0.24
	ED-Trans	5.69 \pm 4.20	99.43 \pm 0.42	77.93 \pm 9.54	1.36 \pm 0.53	0.97 \pm 0.49	11.30 \pm 0.23
	RFNO	4.77 \pm 4.02	99.54 \pm 0.40	83.10 \pm 3.30	1.03 \pm 0.11	0.89 \pm 0.10	9.23 \pm 0.28
Via	CFNO	5.94 \pm 4.42	99.41 \pm 0.44	76.19 \pm 9.70	1.37 \pm 0.38	1.01 \pm 0.40	9.58 \pm 0.24
	MFNO	6.39 \pm 1.24	99.36 \pm 4.84	73.52 \pm 4.73	1.47 \pm 0.13	1.02 \pm 0.12	9.97 \pm 0.24
	SOCS	5.09 \pm 4.20	99.58 \pm 0.33	80.47 \pm 4.46	1.24 \pm 0.41	0.99 \pm 0.40	7.82 \pm 0.22
	EM	3.41	99.79	89.20	0.75	0.64	274.40×10^3

- **Edge Placement Error (EPE_{max}/EPE_{avg})** is a critical indicator for assessing alignment discrepancies in semiconductor manufacturing. As illustrated in Figure 5, it evaluates the reliability of the lithography simulation by calculating the distance between the predicted resist contour and the ground truth after selecting evaluation points on the layout.
- **Turn Around Time (TAT)** is the total amount of time spent by simulation process from coming in the ready state for the first time to its completion.

4.3 Baseline Model Results

Table 3 summarizes the lithography simulation efficiency of all 6 baseline models across 4 mask categories of LithoSim. Each metric in Table 3 is followed by the standard deviation of the corresponding dataset. More experimental settings is list in Appendix A.6.

Overall simulation accuracy and speed. While Transformer-based baseline (ED-Trans) incur the highest turnaround time (TAT) due to hybrid global attention operations, resulting in substantial computational and memory requirements. SOCS achieves minimal latency by strictly adhering to the Hopkins-based frequency-domain encoding-decoding paradigm. Physics-informed models generally exhibit comparable TATs, with data-driven approaches (ED-CNN, ED-Trans) demonstrating overall competitive lithographic awareness when trained on the large scale of LithoSim, a testament to the dataset’s capacity to compensate for inductive biases of lithography through sheer data volume.

Data-driven baseline comparison. ED-CNN, leveraging its CNN backbone enhanced with spatial-channel attention mechanisms, marginally outperforms ED-Trans across all metrics, particularly excelling on Metal datasets (*i.e.* OPC-Metal: 91.06% IOU, Metal: 92.32% IOU). This superiority stems from hierarchical capacity of ED-CNN to resolve local mask critical features while modeling long-range optical interactions via attention-based context aggregation. In contrast, the global

Table 4: Generalization ability comparison of baseline models.

Train	Test	Method	MSE($\times 10^{-3}$)	PA(%)	IOU(%)	EPE _{max} (nm)	EPE _{avg} (nm)
OPC-Metal	Metal	ED-CNN	33.99($\uparrow 25, 93$)	96.60($\downarrow 2.49$)	74.58($\downarrow 17.74$)	3.52($\uparrow 1.88$)	2.79($\uparrow 1.49$)
		ED-Trans	40.89($\uparrow 31.00$)	95.91($\downarrow 3.1$)	69.89($\downarrow 21.80$)	3.76($\uparrow 2.05$)	2.95($\uparrow 1.58$)
		RFNO	30.45($\uparrow 16.86$)	96.95($\downarrow 1.69$)	76.98($\downarrow 11.60$)	3.20($\uparrow 1.36$)	2.52($\uparrow 0.99$)
		CFNO	39.30($\uparrow 26.22$)	96.07($\downarrow 2.57$)	70.63($\downarrow 18.48$)	3.72($\uparrow 2.01$)	2.94($\uparrow 1.44$)
		MFNO	39.28($\uparrow 30.89$)	96.07($\downarrow 2.96$)	70.64($\downarrow 21.54$)	3.66($\uparrow 32.01$)	2.89($\uparrow 1.56$)
		SOCS	20.31 ($\uparrow 10.95$)	97.03 ($\downarrow 1.98$)	85.57 ($\downarrow 6.38$)	2.82 ($\uparrow 1.00$)	2.22 ($\uparrow 0.87$)
OPC-Via	Via	ED-CNN	11.62($\uparrow 6.97$)	98.84($\downarrow 0.70$)	62.58($\downarrow 18.81$)	1.46($\uparrow 0.39$)	1.05($\uparrow 0.12$)
		ED-Trans	12.04($\uparrow 6.35$)	98.80($\downarrow 0.63$)	62.18($\downarrow 15.75$)	1.47($\uparrow 0.11$)	1.10($\uparrow 0.13$)
		RFNO	11.15($\uparrow 6.38$)	98.88($\downarrow 0.66$)	63.39($\downarrow 19.71$)	1.44($\uparrow 0.41$)	1.07($\uparrow 0.18$)
		CFNO	14.23($\uparrow 0.11$)	98.58($\downarrow 0.11$)	59.45($\downarrow 0.11$)	1.52($\uparrow 0.15$)	1.21($\uparrow 0.20$)
		MFNO	12.75($\uparrow 6.36$)	98.73($\downarrow 0.63$)	60.75($\downarrow 12.77$)	1.50($\uparrow 0.03$)	1.16($\uparrow 0.14$)
		SOCS	7.71 ($\downarrow 2.62$)	99.43 ($\downarrow 0.15$)	66.39 ($\downarrow 14.08$)	1.29 ($\uparrow 0.05$)	1.02 ($\uparrow 0.03$)
All	OOD	ED-CNN	5.97	99.40	74.13	1.39	0.90
		ED-Trans	6.81	99.32	73.04	1.51	1.04
		RFNO	5.34	99.47	74.71	1.35	0.87
		CFNO	13.89	98.61	63.12	2.03	1.55
		MFNO	6.27	99.37	73.43	1.43	0.94
		SOCS	4.13	99.79	80.24	0.91	0.60

self-attention of ED-Trans prioritizes mask-wide pattern correlations, achieving suboptimal edge placement error (EPE) compared with ED-CNN in dense layout regions.

Physics-informed baseline comparison. MFNO dominates OPC-Metal simulations (95.29% IOU, 0.69nm EPE) by synergistically capturing global low-frequency optical kernels and local mask topology modulations, a critical requirement for modeling OPC-induced mask feature. The performance of MFNO degrades on OPC-Via and Via layers with 90.99% and 73.52% IOU respectively, where localized low-frequency scattering dominates, favoring RFNO’s reduced Fourier domain focus with 92.68% and 83.10% IOU on OPC-Via and Via. The exclusive global spectral processing of CFNO proves least effective for lithography, particularly on OPC-Metal with 20.15×10^{-3} MSE and > 2 nm EPE, as well as only 97.98% PA and 84.84% IOU, as it disregards detailed mask-level edge variations. SOCS delivers stable performance across all mask categories by rigorously encoding Hopkins’ partial coherent imaging principles in Appendix A.1, matching top baselines performances.

The baseline results of LithoSim highlight dataset-specific architectural preferences: Metal/OPC-Metal simulations demand concurrent global-local frequency feature learning, while Via layers benefit from localized frequency-space constraints. Also, the parity between data-driven and physics-informed models on LithoSim underscores the dataset’s role as an equalizer, providing sufficient physical constraints through data diversity to compensate for missing litho-aware information.

4.4 Baseline Model Generalization Capabilities

The out-of-distribution (OOD) evaluation in Table 4 rigorously assesses baseline models’ ability to generalize across various mask distribution. Models trained exclusively on OPC’ed datasets (OPC-Metal and OPC-Via) are tested on uncorrected counterparts (Metal and Via), simulating real-world scenarios where optimized masks must predict uncorrected lithographic outcomes firstly. Additionally, models trained on the full LithoSim dataset are evaluated on the OOD benchmark, which introduces different illumination (dipole/quasar), mask (M3 metal and regular via layer), and process variation distributions.

Data-driven model generalization capabilities. They exhibit significant sensitivity to OPC-induced topology changes on Metal. ED-Trans suffers a 31.00% MSE increase and 17.74% IOU decrease. In contrast, ED-CNN’s hybrid architecture, combining convolutional locality with channel-spatial attention, achieves marginally better robustness (MSE +25.93%, IOU -17.74%), outperforming all physics-informed models except RFNO and SOCS. This suggests chunked mask feature extraction, when augmented with attention-based optical context modeling, can partially compensate for missing physics constraints in data-driven approaches.

physics-informed model generalization capabilities. SOCS achieves superior stability with minimal performance degradation: MSE increases by only 10.95×10^{-3} (vs. ED-CNN’s 25.93×10^{-3}) and IOU drops by 6.38% when trained on OPC-Metal and tested on Metal. Its physics-grounded Hopkins formulation inherently compensates for mask distribution shifts, maintaining $< 3\text{nm}$ maximum edge placement error (EPE) even under OOD conditions. RFNO achieves the second best performance on both Metal and Via datasets with more low frequency aware in a local range of masks. The full-dataset training paradigm further highlights the OOD supremacy of SOCS, achieving 4.13×10^{-3} MSE, 80.24% IOU, and 0.6nm average EPE on novel M3/via layouts with a 0.44nm margin under ED-Trans.

These results collectively affirm that while data-driven models benefit from LithoSim’s diversity, physics-constrained architectures such as RFNO and SOCS remain indispensable for reliable OOD generalization, which is a critical requirement for production-grade RET integration.

5 Limitations

Idealizations. LithoSim leverages rigorous lithography simulator to achieve comprehensive lithographic variation coverage, with two approximations: fixed chemical kinetics assuming ideal resist chemistry modeling during PEB/development illustrated as fixed resist model in Figure 1 (a), and homogeneous resist-substrate optical constants (neglecting wavelength-dependent refractive indices n and interfacial reflectivity k). Despite these simplifications, LithoSim preserves dominant physics governing optical imaging—notably the coupled impacts of source polarization, defocus-dependent aberration, and OPC-induced mask modifications on resist exposure. Future extensions could integrate resist chemistry models while maintaining compatibility with foundational optical-mask-process variability of LithoSim. Currently, we are collaborating with fab partners to conduct LithoSim verification utilizing actual production line data.

Downstream testing. A critical challenge is to integrate learned lithography simulators as modular components into downstream RET flows, such as optical proximity correction (OPC) [11, 27], source mask optimization (SMO) [12, 13], and sub-resolution assist feature (SRAF) insertion [22]. While LithoSim provides foundational losses (e.g. L_2 , process variation bands in Appendix A.2) and co-optimizable source-mask pairs essential for differentiable optimization, its current formulation remains a standalone tool, lacking the systems-level engineering required for seamless integration into tool chains. Future work could merge its variation-resilient predictions with topography-aware models [26, 23] to co-optimize manufacturability across the lithography stack. Our ultimate goal is to embed LithoSim within these RET flows, wherein it bridges the first critical gap: enabling ML models to supply all differentiable losses outlined in Figure 2 through CUDA-accelerated computations.

6 Conclusions

LithoSim establishes a comprehensive and physically-grounded benchmark for advancing AI-driven lithography simulation in semiconductor manufacturing. By integrating diverse optical sources, mask rules, and realistic process variations, it enables robust training and evaluation of both data-driven and physics-informed models. The benchmark not only bridges critical gaps in existing datasets but also provides a unified framework for assessing model accuracy, generalization, and readiness for downstream resolution enhancement techniques. Through open access to data and code, LithoSim lays a foundational step toward scalable, high-fidelity, and differentiable computational lithography, essential for next-generation design for manufacturing flows.

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Justification: LithoSim introduces lithography simulation benchmark with more than 4 million rigorously curated input-output pairs, integrating optical variations, mask corrections, and process variations to establish a unified evaluation flow for ML-based simulation.

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Justification: LithoSim discusses limitations in Section 5, covering idealized assumptions and downstream integration challenges. For idealizations, LithoSim employs two approximations: fixed chemical kinetics and homogeneous resist-substrate optical constants, though it retains core physics governing optical imaging. Future work could incorporate dynamic resist chemistry models. Regarding downstream testing, while LithoSim provides multi-scale representations and source-mask pairs critical for RET workflows (e.g., OPC/SMO/SRAF), it currently lacks systems-level engineering for seamless integration into EDA toolchains. The authors emphasize the need of LithoSim to bridge this gap through CUDA-accelerated RET operationalization.

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Justification: LithoSim describes theoretical formulations for optical lithography in Section A.1 and FNO-based architectures Section A.4. For the SOCS approximation in lithography modeling, assumptions include decomposing source/projector/mask interactions via TCC with SVD truncation (retaining dominant eigenvalues) and approximating the imaging integral via Eq. 5. The FNO framework assumes learnable spectral weights (\mathcal{W}_θ) can approximate lithography kernels by truncating high-frequency modes (e.g., $|k| \leq m$ in RFNO). The validity of these approximations is implicitly supported by alignment with lithography physics (e.g., frequency-domain interactions) and benchmarking results.

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Justification: LithoSim introduce experiment settings briefly in Appendix A.6. The [Hugging Face dataset](#) has been divided into `opc_mtal`, `opc_via`, `metal`, and `via` with a `train_val_test` split. In [Github repo](#), LithoSim also gives a detailed guideline.

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5. Open access to data and code

Question: Does the paper provide open access to the data and code, with sufficient instructions to faithfully reproduce the main experimental results, as described in supplemental material?

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Justification: LithoSim provides open access to the dataset, code, and pre-trained models via Hugging Face (<https://huggingface.co/datasets/grandiflorum/LithoSim>; <https://huggingface.co/grandiflorum/LithoSim>) and a project website (<https://dw-hongquan.github.io/LithoSim>), including pre-trained models for reproducibility.

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Justification: In [A.6](#), LithoSim introduces computer resources on 4 H100 Graphics cards with Intel Core Xeon Platinum 8462Y+ processors.

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A Technical Appendices and Supplementary Material

A.1 Optical Lithography Approach

Typical optical lithography model comprises 3 essential components: source, mask, and projector, as illustrated in Figure 1 (b). The light rays propagate through the projector and the mask and produce diffracted light with layout pattern information. The intensity of optical imaging can be formulated as,

$$\mathbf{I}(x, y) = \int \int \int \int \int \int_{-\infty}^{\infty} \mathbf{J}(f, g) \mathcal{F}(\mathbf{M})(f', g') \mathcal{F}(\mathbf{M})^*(f'', g'') \mathbf{H}(f + f', g + g') \mathbf{H}^*(f + f'', g + g'') \exp(-j2\pi((f' - f'')x + (g' - g'')y)) df dg df' dg' df'' dg'', \quad (1)$$

where \mathbf{I} is the imaging intensity, \mathbf{J} is the source, \mathbf{H} is the optical transfer function (OTF) of projector, and $\mathcal{F}(\mathbf{M})$ is the frequency of the mask \mathbf{M} ; (f, g) , (f', g') , and (f'', g'') represent the normalized frequency-domain coordinates of \mathbf{H} , $\mathcal{F}(\mathbf{M})$, and $\mathcal{F}(\mathbf{M})^*$. This formulation does not have an analytical solution but only an approximate solution.

A fast approach method, SOCS approach separating source \mathbf{J} and projector \mathbf{H} from mask \mathbf{M} as,

$$\mathbf{I}(x, y) = \int \int \int \int_{-\infty}^{\infty} \mathcal{T}(f', g'; f'', g'') \mathcal{F}(\mathbf{M})(f', g') \mathcal{F}(\mathbf{M})^*(f'', g'') \exp(-j2\pi((f' - f'')x + (g' - g'')y)) df' dg' df'' dg'', \quad (2)$$

where \mathcal{T} is the transmission cross-coefficients (TCC) given by,

$$\text{TCC}(f', g'; f'', g'') = \iint_{-\infty}^{\infty} J(f, g) H(f + f', g + g') H^*(f + f'', g + g'') df dg. \quad (3)$$

Applying SVD decomposition, Eq. 3 can be approximated by Sum of coherent source (SOCS),

$$\text{TCC}(f', g'; f'', g'') \approx \sum_{q=1}^{\infty} \kappa_q \Phi_q(f', g') \Phi_q^*(f'', g''), \quad (4)$$

where, κ_q and Φ_q are q-th eigenvalue and eigenvector of TCC. For fast calculation, we can keep the Q largest eigenvalues and obtain final SOCS approach as,

$$\mathbf{I}(x, y) = \sum_{q=1}^Q \kappa_q \|\Phi_q(x, y) \otimes M(x, y)\|^2, \quad (5)$$

where $\phi_q(x, y)$ and $M(x, y)$ are the spatial distribution of Φ_q and $\mathcal{F}(\mathbf{M})$ respectively.

A.2 Relationship between lithography simulation and RET

As illustrated in Figure 2, lithography simulation forms the computational backbone of modern resolution enhancement techniques (RET) [19], enabling the optimization of sources \mathbf{J} and masks \mathbf{M} through iterative physics-aware feedback.

The simulator maps (\mathbf{J}, \mathbf{M}) to resists \mathbf{R} , which are evaluated via two critical metrics: L2 contour fidelity (geometric deviation from target layout \mathbf{T} under normalized condition) and process variation band (PVB) robustness across dose (α) and focus β conditions as,

$$\begin{aligned} \mathcal{L}_2 &= \|\mathbf{R}_{\text{norm}} - \mathbf{T}\|_2^2 \\ \mathcal{L}_{\text{PVB}} &= \|\mathbf{R}_{\text{max}} - \mathbf{R}_{\text{min}}\|_2^2 \end{aligned} \quad (6)$$

where \mathbf{R}_{norm} is the resist under $(\alpha, \beta) = (0, 0)$, \mathbf{R}_{max} and \mathbf{R}_{min} are resists under $(\alpha, \beta) = (-0.1, -40)$ and $(\alpha, \beta) = (0.1, 40)$ respectively.

Consequently, the comprehensive RET loss is formulated as,

$$\mathcal{L}_{\text{RET}} \equiv \mathcal{L}_{\text{OPC}} \equiv \mathcal{L}_{\text{SMO}} = \gamma \mathcal{L}_2 + \eta \mathcal{L}_{\text{PVB}}, \quad (7)$$

where γ and η are weighting factors for the respective loss components.

In optical proximity correction (OPC) mode, the illumination source \mathbf{J} is fixed, and the simulator guides mask optimization through gradient-based updates:

$$\mathbf{M}^* = \underset{\mathbf{M}}{\operatorname{argmin}} \mathcal{L}_{OPC}(\mathbf{J}, \mathbf{M}). \quad (8)$$

Source mask optimization (SMO) extends this framework by co-optimizing \mathbf{J} and \mathbf{M} in a coupled parameter space as,

$$(\mathbf{J}^*, \mathbf{M}^*) = \underset{(\mathbf{J}, \mathbf{M})}{\operatorname{argmin}} \mathcal{L}_{SMO}(\mathbf{J}, \mathbf{M}). \quad (9)$$

LithoSim contains all the input parameters required by Eq. 7, not only the source and mask as the optimization subjects, but also dose and defocus involved in the loss calculation. This makes it possible to train lithography simulation using LithoSim and thereby achieve CUDA-accelerated RET.

A.3 Litho-condition Embedding

Process Variations Embedding: LithoSim incorporates critical process variations (PV) through a physics-informed positional encoding scheme. For dose and defocus inputs (normalized to $[-1, 1]$), we employ a continuous positional encoding that transforms scalar PV into a spectral representation through logarithmic frequency bands. For a given PV $v \in [-1, 1]$, the encoding generates $d_{pv}/2$ frequency components with wavelengths logarithmically spaced following,

$$\begin{aligned} PE(v)_{2k} &= \sin(v \cdot e^{-k \cdot \ln(10^4 / d_{pv})}) \\ PE(v)_{2k+1} &= \cos(v \cdot e^{-k \cdot \ln(10^4 / d_{pv})}) \end{aligned} \quad (10)$$

Source Positional Embedding: The source spatial characteristics are encoded through a multi-frequency 2D positional encoding that preserves optical reciprocity and illumination coherence properties. For source coordinates $(x, y) \in [-1, 1]^2$ and backbone model dimension d_s ,

$$\begin{aligned} PE(x, y)_{4k} &= \sin(x \cdot e^{-k \cdot \ln(10^4 / d_s)}) \\ PE(x, y)_{4k+1} &= \cos(x \cdot e^{-k \cdot \ln(10^4 / d_s)}) \\ PE(x, y)_{4k+2} &= \cos(y \cdot e^{-k \cdot \ln(10^4 / d_s)}) \\ PE(x, y)_{4k+3} &= \cos(y \cdot e^{-k \cdot \ln(10^4 / d_s)}) \end{aligned} \quad (11)$$

Source Compression: LithoSim implements a multi-scale attention mechanism that preserves critical optical characteristics while enabling efficient processing of high-dimensional source patterns. The compression occurs through 3 physics-aware stages.

(1). *Coherent Chunk Processing* splits source \mathbf{J} into $C = 64$ chunks matching optical cross-effect size,

$$\mathcal{B}_k = \{\mathbf{J}_i\}_{i=d_s C}^{(d_s+1)C} \in \mathbb{C}^{C \times D}, \quad (12)$$

where positional encoding in Eq. 11 maintains inter-pixel phase relationships critical for diffraction modeling of every chunks.

(2). *Intra-chunk Self-attention* models local interference within coherence area as,

$$\mathcal{C}_{\mathcal{B}_i} = \operatorname{softmax} \left(\frac{Q_{local} K_{\mathcal{B}_i}^T}{\sqrt{d}} \otimes M_{valid} \right) \cdot V_{\mathcal{B}_i} \quad (13)$$

where M_{valid} represents the valid position of source (e.g. radium $\sigma \in [0.68, 0.83]$ for annular source), $K_{\mathcal{B}_i}$ and $V_{\mathcal{B}_i}$ is the key and value of i -th chunked source, Q_{local} is local learnable query.

(3). *Inter-chunk Self-attention* captures global source contribution blending as,

$$\mathcal{C} = \sum_{i=1}^K w_i \mathcal{C}_i, \quad w_i \propto e^{\langle Q_{global}, \mathcal{C}_i \rangle}, \quad (14)$$

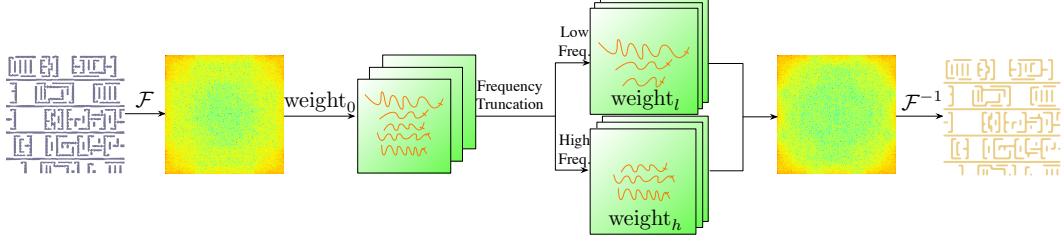


Figure 6: Reduced Fourier Neural Operator (RFNO).

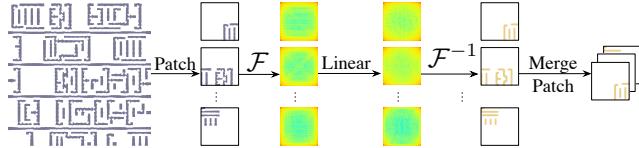


Figure 7: Convolutional Fourier Neural Operator (CFNO).

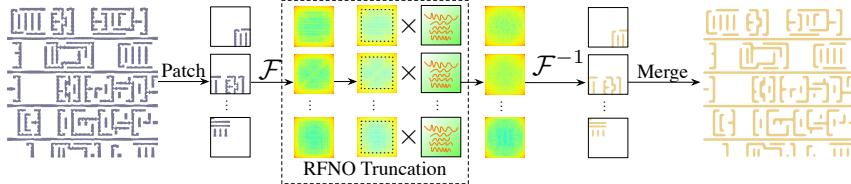


Figure 8: Mixed Fourier Neural Operator (MFNO).

where \mathcal{C} is final compressed source feature, Q_{global} is global query of total chunked source, w_i is the weight of i -th chunked source.

Chunked Litho-aware Cross-attention: LithoSim implements condition embedding into mask feature $\mathbf{M} \in \{0, 1\}^{H \times W}$ for source and process variations (PV) respectively based on chunked cross-attention. \mathbf{M} is partitioned into $N = \frac{H \times W}{d_m^2}$ local chunks of size $d_m \times d_m$.

(1). *PV cross-attention:* For i -th chunked mask region $\mathcal{M}_i \in \{0, 1\}^{d_m \times d_m}$ and embedded process variations $\mathcal{V} = PE(v)$ after positional embedding, the PV cross-attention is given by,

$$\mathcal{M}' = \sum_{i=1}^N \text{softmax} \left(\frac{Q_i K^T}{\sqrt{d}} \right) V, \quad (15)$$

where $Q_i = W_Q \mathcal{M}_i$, $K = W_K \mathcal{V}$, and $V = W_V \mathcal{V}$. W_Q , W_K , and W_V is learnable projection parameters for each chunked mask and process variation. By decomposing the mask into $d_m \times d_m$ optical proximity correction (OPC) regions and computing multi-head attention between chunked mask features (queries) and process-encoded variations (keys/values), it models dose-dependent resist thresholding and defocus-induced blur as spatially varying modulation operators.

(2). *Source cross-attention:* For j -th chunked mask region $\mathcal{M}_j \in \{0, 1\}^{d_m \times d_m}$ and compressed source \mathcal{C} in Eq. 14, the source cross-attention is given by,

$$\mathcal{M}'' = \sum_{j=1}^N \text{softmax} \left(\frac{Q_j K^T}{\sqrt{d}} \otimes M_{valid} \right) V, \quad (16)$$

where $Q_j = W_Q \mathcal{M}_j$, $K = W_K \mathcal{C}$, and $V = W_V \mathcal{C}$. W_Q , W_K , and W_V is learnable projection parameters for each chunked mask and compressed source, M_{valid} is the valid region of source.

A.4 Baseline Architecture

The fusion between FNOs, including RFNO, CFNO, and MFNO, and lithography simulation from their shared reliance on spectral representations for efficient physical process approximation. In

optical lithography, Eq. 5 can be simplified to formulate as,

$$\mathbf{I} = |\mathcal{F}^{-1}[\mathcal{F}(\mathbf{M}) \otimes \mathcal{F}(\mathbf{K})]|^2 \quad (17)$$

where \mathbf{K} is the lithography kernel which is dependent on source and defocus (Figure 1 (a)). FNOs natively operate in the spectral domain through learnable truncated mode interactions $\mathcal{W}_\theta \in \mathbb{C}^{m \times m}$ approximating optical kernel by,

$$\text{FNO}(k) = \mathcal{F}^{-1}[\mathcal{W}_\theta(\mathbf{k}) \cdot \mathcal{F}(M)(\mathbf{k})], \quad (18)$$

where \mathcal{W}_θ is local learnable complex-valued spectral weights truncated at modes $|k| \leq m$ in **RFNO** (Figure 6), is a patched global complex-valued linear layer in **CFNO** (Figure 7), is patched learnable complex-valued spectral weights in **MFNO** (Figure 8), which aligns with lithography's inherent frequency-space physics in Eq. 17.

FNO-based models typically requires the combination of FNO with an CNN encoder-decoder structure [38, 21, 17] to achieve the purpose of extracting low-frequency mask features at different scales. Unlike FNO, **SOCS** rigorously adheres to the methodology of Eq. 5. The mask is first transformed into the frequency domain via FFT, with all encoding, decoding, and condition interactions executed exclusively in the spectral domain, before directly outputting the resist profile through IFFT.

A.5 Evaluation Metrics Details

AI performance metrics: Given the predicted resist $\hat{\mathbf{R}}$ and the ground truth resist \mathbf{R} , the pixel number is N , MSE, PA, IOU is defined respectively as,

$$\text{MSE} = \frac{1}{N} \|\mathbf{R} - \hat{\mathbf{R}}\|^2 \quad (19)$$

$$\text{PA} = \frac{\mathbf{R} \cap \hat{\mathbf{R}}}{\mathbf{R}} \quad (20)$$

$$\text{IOU} = \frac{\mathbf{R} \cap \hat{\mathbf{R}}}{\mathbf{R} \cup \hat{\mathbf{R}}} \quad (21)$$

Lithographic fidelity metrics: As illustrated in Figure 5, given the predicted resist contour $\mathbf{C}_{\hat{\mathbf{R}}}$, the ground truth resist $\mathbf{C}_{\mathbf{R}}$, and original layout contour $\mathbf{C}_{\mathbf{T}}$. First, sample evaluation points \mathbf{P} at regular intervals (typically 20nm) along $\mathbf{C}_{\mathbf{T}}$. For each point $P_i \in \mathbf{P}$, construct a perpendicular line that intersects both $\mathbf{C}_{\mathbf{R}}$ and $\mathbf{C}_{\hat{\mathbf{R}}}$ at points $P_{i,\mathbf{R}}$ and $P_{i,\hat{\mathbf{R}}}$ respectively. The edge placement error (EPE) at P_i is then defined as the length of the vertical segment $\overline{P_{i,\mathbf{R}}P_{i,\hat{\mathbf{R}}}}$. The maximum EPE across all evaluation points \mathbf{P} is denoted as EPE_{max} , while the average EPE is calculated as EPE_{avg} .

A.6 Experiment Settings

LithoSim is trained and tested with 4 H100 Graphics cards with Intel Core Xeon Platinum 8462Y+ processors. All the baselines is trained with Adam optimizer and a 10^{-4} learning rate of 10^{-5} weight decay.

LithoSim uses a linear combination of BCE and Dice loss in Eq. 22 for ED-CNN, ED-Trans, RFNO, CFNO, and MFNO, as well as MSE loss for SOCS.

$$\mathcal{L} = \alpha \mathcal{L}_{dice} + \beta \mathcal{L}_{BCE}, \quad (22)$$

where LithoSim sets $\alpha = \beta = 1$.

In condition embeddings (A.3), LithoSim uniformly sets output dimension of source positional embedding $d_s = 8$, compressed factor $K = 16$, and chunk size 256 for each source. In process variation embedding, the output dimension of value positional embedding is also set as $d_v = 8$. Mask chunk size is set as 64 to capture proximity optical effects.