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# Beyond accuracy: understanding the performance of LLMs on exams designed for humans

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## Abstract

1 Many recent studies of LLM performance have focused on the ability of LLMs  
2 to achieve outcomes comparable to humans on academic and professional exams.  
3 However, it is not clear whether such studies shed light on the extent to which  
4 models show reasoning ability, and there is controversy about the significance and  
5 implications of such results. We seek to look more deeply into the question of  
6 how and whether the performance of LLMs on exams designed for humans re-  
7 flects true aptitude inherent in LLMs. We do so by making use of the tools of  
8 psychometrics which are designed to perform meaningful measurement in test  
9 taking. We leverage a unique dataset that captures the detailed performance of  
10 over 5M students across 8 college-entrance exams given over a span of two years  
11 in Brazil. With respect to the evaluation of LLM abilities, we show that the tools  
12 of Item Response Theory (IRT) provide a more informative evaluation of model  
13 performance than the usual accuracy metrics employed in previous studies. Dig-  
14 ging deeper, we show that the modeling framework of IRT, by explicitly modeling  
15 the difficulty levels of questions, allows us to quantitatively distinguish between  
16 LLMs that answer questions in “human-like” patterns versus LLMs that do not.  
17 We also show how to quantitatively identify cases in which exam results are not  
18 reliable measurements of an LLM’s ability. Using the tools of IRT we can also  
19 identify specific questions that appear to be either much easier, or much harder,  
20 for machines than for humans, and we give some reasons for those differences.  
21 Overall, our study shows that the conventional focus on accuracy as the primary  
22 performance metric for LLM studies does not allow us to deeply understand the  
23 true capabilities of LLMs and compare them to that of humans. Thus, we claim  
24 that psychometric modeling should play a larger role in the evaluation of LLM  
25 capabilities on exams designed for humans.

## 26 1 Introduction

27 Large Language Models (LLMs) have demonstrated an impressive ability in performing well on ex-  
28 aminations designed for humans [25, 30], such as the US bar exam [27], the US Medical Licensing  
29 Exam [21], and many others [45, 53]. This yields controversy in how researchers should interpret  
30 such results, raising two kinds of criticisms of those apparent successes. The first is the potential for  
31 publicly-given exams (and answers) to leak into models’ training data. The second, and more fun-  
32 damental, issue is the notion of *construct validity* [44]. Most exams given to humans are intended to  
33 measure a construct, e.g., legal analysis ability, medical analysis ability, etc. However, the reliability  
34 of these exams in measuring the relevant construct for non-humans is usually ignored, and exams  
35 that are valid in one context may not generalize across different groups, settings or tasks [24].

36 Formalizing the notion of construct validity in general is challenging. Since the 1950s, the field  
37 of psychometrics has been grappling with how to design examinations that validly measure human  
38 abilities along specific dimensions. The primary tool developed has been Item Response Theory  
39 (IRT) [10], which has been employed in psychology, medicine, and especially in educational test-

40 ing. IRT formalizes the unobserved construct as a continuous latent variable, and models stochastic  
41 responses of humans to questions as a logistic regression conditional on that latent variable.

42 In this paper, we demonstrate how IRT can help shed light on whether LLMs are in fact show-  
43 ing human-like performance on exams intended for humans. As a case study, we use one of the  
44 largest university-entrance exams in the world, a dataset comprising the performance of over 5 mil-  
45 lion Brazilian students on eight multiple-choice exams administered over two years. Each exam  
46 was prepared and fitted to an IRT model by educational testing experts, giving us an unparalleled  
47 opportunity to examine the performance of LLMs in detail.

48 Our results show that the LLMs we study reveal performance patterns that are consistent with ex-  
49 pected human behavior in many cases. Nonetheless, we also frequently observe significant deviation  
50 from human-like behavior. We demonstrate how to use the tools of IRT to quantitatively distinguish  
51 between human-like and non-human-like behavior. We then explore the differences between mod-  
52 els and exam types that correlate with differences in response patterns. Lastly, we use the tools of  
53 IRT and psychometrics to identify cases where exams are not producing reliable estimates of LLM  
54 ability and understand why this happens. This occurs because exams are in some cases too difficult  
55 for the models, and in other cases too easy for them and as such they cannot properly measure the  
56 ability of certain LLMs.

57 Moving beyond conclusions about current models, the broader contribution of our study is to demon-  
58 strate the power of IRT as a framework for evaluating LLMs. For example, in Classical Test Theory  
59 (CTT), no attempt is made to assess the difficulty of individual questions, in-line with majority of in  
60 standard LLM benchmarks that pursues accuracy [8, 43, 16, 4]. In contrast, as we will show below,  
61 IRT simultaneously measures both test takers and exam questions (on the same scale). In doing so,  
62 IRT allows one to distinguish between test takers with similar CTT (accuracy) scores, but differing  
63 levels of true ability, by inspecting the *pattern* of correct or incorrect answers given. Moreover, we  
64 deploy a broader set of tools (e.g., goodness-of-fit, Fisher information, discrimination index) which  
65 enable us to evaluate which are the cases in which fitting the IRT model to the LLMs response  
66 patterns gives us reliable estimates of the models’ ability. Thus, we believe that the methods of our  
67 study represent a valuable step beyond the use of simple accuracy for assessing whether both current  
68 and future LLMs show human-like response patterns.

## 69 2 Related Work

70 Our study connects a number of research areas, spanning benchmarking LLMs, the applications of  
71 item response theory, and the evaluation of LLMs using exams designed for humans.

72 **Benchmarking LLMs.** The most common strategy to evaluate LLMs is through traditional large-  
73 scale NLP benchmarks [46, 40, 11, 18, 16, 19, 4]. Conventionally, benchmark evaluation relies on  
74 some notion of accuracy – the number of correct answers – as a proxy for ability [8, 43]. A key  
75 distinction of our study is to draw attention to the limitations of the use of accuracy alone [34] for  
76 evaluating the performance of LLMs on benchmarks in understanding the similarity between the  
77 performance of models versus humans.

78 **LLMs and Exams Designed for Humans.** Many attempts to evaluate LLMs use exams designed  
79 for humans, e.g., at college-entrance [1, 26] or college-level [14, 37, 47, 13, 41, 53]. These exams  
80 also generally use accuracy as a metric of ability; one focus of our work is on how to use IRT  
81 analysis to determine when such exams in fact perform meaningful measurement.

82 The Brazilian nationwide college-entrance exams we use in this work (ENEM), detailed in Sec-  
83 tion 4.1, were used in previous efforts to evaluate NLP models [38, 39, 26]. However, those studies  
84 only used accuracy and did not make use of the IRT models associated with the exam, which is a  
85 central aspect our work.

86 **IRT in Machine Learning.** Work in psychometrics (i.e., the measurement of human cognitive  
87 abilities), detailed in Section 3, has shown that using accuracy as a exam score may not reflect the  
88 true underlying abilities of individuals [15]. As a result, IRT has been advocated for use in machine  
89 learning (ML) as an improved tool for benchmarking. The authors in [33] show that it is possible to  
90 produce rankings of NLP models which are more reliable and stable using IRT than accuracy. Item  
91 response theory has also been shown to help in spotting noisy questions, identifying overfitting,

92 selecting features, and designing better benchmarks for ML [29, 35, 20, 54, 22]. However, there is  
 93 a critical difference between the previous uses of IRT in ML and our work. Previous work uses IRT  
 94 by training an IRT model on the results of ML models solving question-answering or classification  
 95 questions. Our method is different: we leverage the fact that we have access to an IRT model trained  
 96 on *human responses*, and we do not retrain on *model responses*. We take this approach because  
 97 a central goal of our study is to explore whether LLMs are in fact following response patterns *as*  
 98 *exhibited by human test takers*.

99 Finally, we note that [42] shares some goals with our work. The investigation seeks to understand  
 100 whether LLMs show human-like response biases in surveys. We also look at the question of whether  
 101 LLMs show human-like response patterns, but we study the question along different dimensions:  
 102 (a) patterns of correct and incorrect answers in exams; and (b) the ways in which LLMs choose  
 103 incorrect answers. Additionally, Xia *et al.* [51] recognize that accuracy as a single metric does not  
 104 capture errors LLMs can make in intermediate steps when solving mathematical tasks, and they  
 105 systematically study those errors.

### 106 3 Background

107 In this section, we give some background of the tools we use from psychometrics.

108 **Classical Test Theory (CTT):** CTT [2] evaluates test takers based on the fraction of questions  
 109 they answer correctly. We call this score *accuracy* or *CTT* score of the test taker and we use these  
 110 two terms interchangeably. Inadequately, CTT does not differentiate between difficult and easy  
 111 questions, nor does it take into consideration the *patterns of correct answers*. For example, the CTT  
 112 score does not penalize a test taker who answers correctly difficult questions, but answers wrongly  
 113 easy ones – despite the fact that such a pattern might be indicative of randomness or cheating.

114 **Item Response Theory (IRT):** IRT [12, 5] is a model used extensively in psychometrics to measure  
 115 the ability level of the test takers and evaluate the difficulty of the test questions (which are referred  
 116 to as *items* in psychometrics). IRT takes into consideration the difficulty of the questions when evalu-  
 117 ating test-taker’s performance and also makes use of the pattern of correct and incorrect responses  
 118 on the exam. The model associates with every test taker  $j$  a parameter  $\theta_j$ , which corresponds to the  
 119 *ability* of  $j$ . The two-parameter IRT model (2PL) associates every question  $i$  with two parameters  
 120  $\phi_i = (\alpha_i, \beta_i)$ . The model assumes that a test taker with ability  $\theta_j$  answers question  $i$  associated with  
 121  $\phi_i$  correctly with probability given by the logistic function:

$$p_{ij} = \frac{e^{\alpha_i(\theta_j - \beta_i)}}{1 + e^{\alpha_i(\theta_j - \beta_i)}}. \quad (1)$$

122 Parameter  $\alpha_i$  is the *discrimination parameter* and  $\beta_i$  is the *difficulty* of question  $i$ . Note that the  
 123 ability  $\theta_j$  and the difficulty level  $\beta_i$  are in the same scale; after all, the difference  $(\theta_j - \beta_i)$  directly  
 124 affects  $p_{ij}$ . For fixed  $\alpha_i$ , the difficulty parameter  $\beta_i$  is the value (on the ability scale) for which  
 125  $p_{ij} = 0.5$ . Parameter  $\alpha_i$  characterizes how well question  $i$  can differentiate among test takers  
 126 located at different points of the ability continuum;  $\alpha_i$  is proportional to the slope of  $p_{ij} = p_i(\theta_j)$   
 127 at the point where  $p_{ij} = 0.5$  – the steeper the slope, the higher the discriminatory power of  $i$ . All  
 128 the parameters of this model take values in  $(-\infty, +\infty)$ . Note that any set of questions comprising  
 129 an exam spans a certain range of  $\beta_i$  values; such a set is not appropriate to assess test takers with  
 130 abilities outside this range.

131 The 3-Parameter IRT model (3PL for short) is an extension of the above model that also incorporates  
 132 a *pseudo-guessing parameter*  $\gamma_i$ . Thus, in 3PL every question  $i$  is associated with three parameters  
 133  $\Phi_i = (\alpha_i, \beta_i, \gamma_i)$ ;  $\alpha_i$  and  $\beta_i$  are the same as before. Intuitively,  $\gamma_i$  is the probability of answering  
 134 correctly based on random guess with  $\gamma_i \in [0, 1]$ . Thus, the probability of a test taker with ability  $\theta_j$   
 135 to answer question  $i$  correctly is:  $P_{ij} = \gamma_i + (1 - \gamma_i)p_{ij}$ .

136 Given test-taker responses, the parameters of the model can be estimated using Bayesian meth-  
 137 ods [5]. In our case, the ENEM dataset came with a set of questions for which the parameters  
 138  $(\alpha_i, \beta_i, \gamma_i)$  had already been fitted by education experts [17]. Therefore, for each one of the LLMs  
 139 we considered, we only need to compute their ability parameters – given their response patterns.  
 140 Intuitively, large values of  $\theta$  correspond to test takers with high ability levels and vice versa. High  
 141 ability value  $\theta$  of an LLM implies better performance.

142 Although the ability levels of test takers can be used as a measure of their performance, one should  
 143 also know if the test takers are *consistent* with the model, e.g., they should answer easy questions  
 144 correctly if they answer difficult questions correctly. One index that enables us to evaluate the  
 145 consistency of the test takers with the model is the  $l_z$  index [12]. Intuitively, the  $l_z$  index is based  
 146 on the standardization of a test-taker’s log-likelihood function given their theta values. Assume a  
 147 set of  $I$  questions and test taker  $j$  with ability  $\theta_j$  and response vector  $\mathbf{r}_j$  such that  $\mathbf{r}_j(i) = 1$  (resp.  
 148  $\mathbf{r}_j(i) = 0$ ) if  $j$  answered question  $i$  correctly (resp. wrongly). Then, the log-likelihood of  $j$  is  
 149 simply:  $L_j = \sum_{i \in I} [\mathbf{r}_j(i) \ln P_{ij} + (1 - \mathbf{r}_j(i)) \ln(1 - P_{ij})]$ . To standardize  $L_j$  we need both its  
 150 mean ( $\mathbb{E}[L_j]$ ) and variance ( $\text{Var}(L_j)$ ). Then, the  $l_z$  score is computed as:

$$l_z(j) = \frac{L_j - \mathbb{E}[L_j]}{\sqrt{\text{Var}(L_j)}}. \quad (2)$$

151 In a well-designed test, the  $l_z$  scores are expected to have a unit normal distribution – this is the  
 152 case for humans taking the ENEM test (see for example Figure 3). In general,  $l_z$  values close to 0  
 153 are considered good: it means the test takers’ response patterns are consistent with what is expected  
 154 from them by the model. Negative  $l_z(j)$  scores reflect an unlikely response vector. A positive  $l_z(j)$   
 155 score indicates that  $j$  has a more likely response vector than indicated by their ability.

156 We can access the amount of information that an item  $i$  provides to estimate  $\theta$  under the 3PL model  
 157 by the Fisher information, which is given by:

$$\mathcal{I}_i(\theta) = \alpha_i^2 \left[ \frac{(p_i - \gamma_i)^2}{(1 - \gamma_i)^2} \right] \left[ \frac{1 - p_i}{p_i} \right]. \quad (3)$$

158 The total information of a test is simply the sum of item information, i.e.,  $\mathcal{I}(\theta) = \sum_{i \in I} \mathcal{I}_i(\theta)$ .  
 159 The Fisher information is connected with the standard error of the estimation, given by  $SE(\theta) =$   
 160  $1/\sqrt{\mathcal{I}(\theta)}$ . When a test has high Fisher information in a certain  $\theta$  range, the test has more discrimi-  
 161 native power in that range, producing scores with less measurement errors.

## 162 4 Methods

### 163 4.1 The ENEM Exam

164 The *Exame Nacional do Ensino Médio* (ENEM), world’s second largest university entrance exam  
 165 behind Chinese’s Gaokao exam, is taken by millions of Brazilian students each year [39]. ENEM  
 166 comprises questions requiring different levels of domain-specific knowledge and reasoning [3].

167 The exam is in Brazilian Portuguese and consists of four sections, each of which has 45 multiple-  
 168 choice questions with five options [17]. Each section is treated as a separate exam for the purposes  
 169 of modeling via IRT. The four sections consist of the **Humanities**, the **Languages and Codes**, the  
 170 **Natural Sciences**, and the **Math** exams. The description of these exams is given in Appendix A.11.

171 Since 2009, the grades assigned to ENEM test-takers have been determined using IRT. Using IRT  
 172 helps to penalize guessing, differentiate among students that otherwise would get the same (CTT)  
 173 grade, and compare among students that took exams in different years. The ENEM organizers  
 174 release not only the exam content and questions, but also the student (anonymized) responses and  
 175 their CTT and IRT scores, which enables downstream studies.

176 From our standpoint, there are a number of relevant aspects of the process used by the ENEM de-  
 177 velopers [17]. First, questions are given to a sample of students, whose answers are used to find  
 178 inconsistencies and errors. Next, an important test of construct validity is to verify the unidimen-  
 179 sionality of the latent trait, for which the ENEM team uses Full Information Factor Analysis [7].  
 180 Finally, the IRT model itself is fit using the Marginal Maximum Likelihood Estimator [6]. Using the  
 181 results, the developers may exclude questions having poor model fit.

182 The exams, their solutions, and all the fitted parameters of the 3PL IRT model ( $\theta_j, \alpha_i, \beta_i, \gamma_i$ ) are  
 183 publicly available at the Brazilian government website [17]. To the best of our knowledge, these data  
 184 are the largest and most comprehensive public dataset based on item-response theory available. The  
 185 datasets contain questions and complete response patterns of all students taking the exams in 2022

186 and 2023. Questions for the 2023 exam were released in November 2023, minimizing the chance  
187 they are in training data for most of the LLMs we considered. However, we expect fragments of the  
188 exam being in the training data (e.g. poems, and any other widely available material used as part of  
189 a question)<sup>1</sup>. The number of test takers per year ranged from 2.2M to 3.7M.

190 The ENEM exams are initially made available as PDF files; we used the Python library *PyPDF2*,  
191 followed by regular expressions and some manual adjustments to extract each question from its  
192 exam file. In order to account for possible effects of Language, as diagnosed in previous work [31],  
193 we translated all questions to English and run all experiments in Portuguese and English. For those  
194 exam questions that incorporated images, we used the version of the exam designed for blind people  
195 containing textual descriptions of the images. We manually audited all questions in 2022 and 2023  
196 exams to ensure their quality (Appendix A.1).

## 197 4.2 Models

198 We evaluate the following family of models: the open source models Mistral-7B, Gemma-7B,  
199 Llama2-7B, Llama2-13B, Llama3-8B, and GPT 3.5. For the open source models, we evaluate  
200 on both instructed and non-instructed tuned versions. Our choice of models enables the study of  
201 models of similar size (the majority of our models are of size 7B), but also introduces diversity of  
202 architectures (GPT, Gemma, Mistral, Llama), size (7B vs. 13B), training data (Llama2 vs. Llama3),  
203 and training strategies (with and without instruction tuning).

204 We prompt models with {0, 1, 4}-shots, following conventional question-answer benchmark  
205 prompting strategies [32] (example prompts in Appendix A.4). We measure model’s next token  
206 probability across five option letters, and average predictions across 30 *shuffles* of the order of the  
207 answer choices to correct for the well-known effect of position bias [28] (Details in Appendix A.4).

## 208 5 Results

209 In this section, we present our main findings. All the results we show here are for the 2023 ENEM  
210 exams, with four-shot prompting. Results for the 2022 ENEM exam and for zero-shot and one-shot  
211 prompting and for open source instructed tuned models are shown in Appendices A.6 – A.9. The  
212 results we show in this section are strongly consistent with the results we get for the 2022 ENEM  
213 exam and for one-shot prompting.

### 214 5.1 Accuracy vs. Ability Level

215 We first investigate how humans compare to LLMs when IRT parameter  $\theta$  is used instead of accuracy  
216 (the metric that is employed in most LLM benchmarking, e.g., [8, 43]). In Figure 1 we plot the CTT  
217 score (accuracy) vs IRT score ( $\theta$ ) for 30 shuffles of answer options for each model. The light blue  
218 background points correspond to the humans who took the exam. Each of the closed curves in the  
219 figure corresponds to one LLM, and shows the central 90% of the LLM’s distribution.

220 First, we observe that there are many cases where identical accuracy scores result in different  $\theta$   
221 scores. This reflects the fact that IRT takes into account not just the number, but also the pattern  
222 of correct answers. Second, for many LLMs, particularly in the Humanities and Languages exams,  
223 there is overall greater variability in the accuracy score than in the IRT score. This suggests that IRT  
224 is less sensitive to the variations in LLM output that are due to the LLM’s inherent randomness.

225 To compare the performance between LLMs and humans, we compare their IRT scores ( $\theta$ ). Recall  
226 that IRT score of 0 corresponds to the average ability of a human test taker. Across all four subjects,  
227 the majority of models have CTT and IRT scores overlapping with humans. LLMs in general achieve  
228  $\theta$  scores above that of the human average in Humanities, Languages, and Natural Sciences, but below  
229 human average in Mathematics. Looking at specific models, we find the Llama2 models at the lower  
230 end of  $\theta$  scores, Mistral and Llama3 in the middle range, and GPT-3.5 and Gemma-7B at the higher  
231 end of  $\theta$  scores.

232 The language of the exam affects some models’ performance. In Languages and Natural Sciences,  
233 GPT-3.5 tends to perform better in Portuguese compared to English, while in Humanities and Natural

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<sup>1</sup>Gemma models are released in 2024 and we suspect contamination issues from analysis in Appendix A.3.

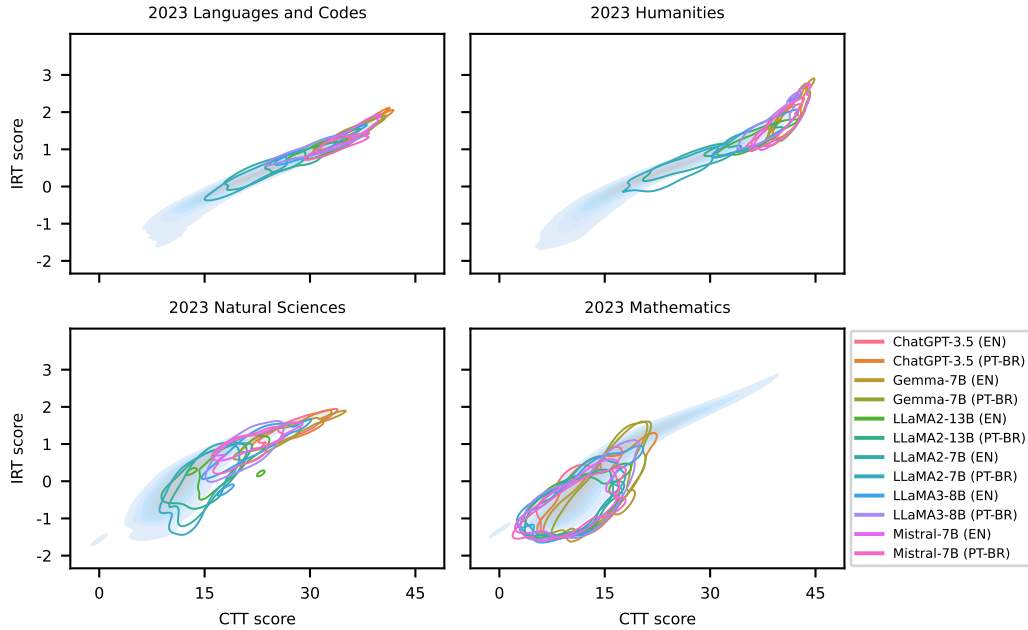


Figure 1: Distribution of CTT (accuracy) and IRT scores for humans and LLMs for the ENEM 2023 exam. LLMs are non-instructed tuned open source models and GPT3.5 with four-shot. LLM datapoints are computed from different shuffles of the order of answer choices.

234 Sciences, the Llama models tend to perform worse in Portuguese than in English. This suggests that  
 235 there are differences regarding the reasoning ability and the amount of knowledge accessible to the  
 236 models in each language.

237 Importantly, outlier models all tend to have higher accuracy and/or lower IRT scores than humans.  
 238 These models answer more questions correctly than humans do, but show error patterns that are not  
 239 entirely human-like. We dig into this phenomenon next.

## 240 5.2 Response Patterns

241 One of our goals is to assess whether the LLMs we examine show good fit to the ENEM IRT model,  
 242 as crafted by the educational expert team described in Section 4.1. Intuitively, a test taker showing  
 243 good fit to an IRT model is an individual  $j$  that tends to make less frequent mistakes on “easy”  
 244 questions (question  $i$  with  $\beta_i < \theta_j$ ) while making more frequent mistakes on “hard” questions  
 245 (question  $i$  with  $\beta_i > \theta_j$ ). Thus, to assess fit we need to inspect the response patterns of the LLMs.

246 Figure 2 shows the response patterns of LLMs for the 2023 exam. Every cell  $(i, j)$  corresponds to  
 247 the probability that LLM  $i$  answered question  $j$  correctly, where probabilities are computed over the  
 248 30 shuffles. We use gray scale with a black (resp. white) cell representing 1 (resp. 0). Questions  
 249 are ordered in increasing order of their  $\beta$  values. Generally, rows with darker overall patterns (higher  
 250 correctness) are indicative of higher  $\theta$  scores.

251 The figure demonstrates a number of points. For example, on the Math exam, the figure exhibits a  
 252 response pattern that appears to show low  $\theta$  values for all models, which confirms results in Figure 1.  
 253 In addition, the figure shows that for some questions, the 30 shuffles of answer choices of a given  
 254 model are often either all correct or all incorrect. However, there are some grey areas in the figure for  
 255 all the exams, indicating that shuffling the options can affect the LLM’s answers on certain items.  
 256 Furthermore, the patterns show that many questions appear to be either “easy” (black) or “hard”  
 257 (white) for all models at the same time. Likewise, in many cases models show similar performance  
 258 on the English and Portuguese versions of a given question.

259 Overall, the response patterns we observe suggest that the Math exam is “too difficult,” with mod-  
 260 els often resorting to guessing. On the other hand, most LLMs consistently answer correctly the

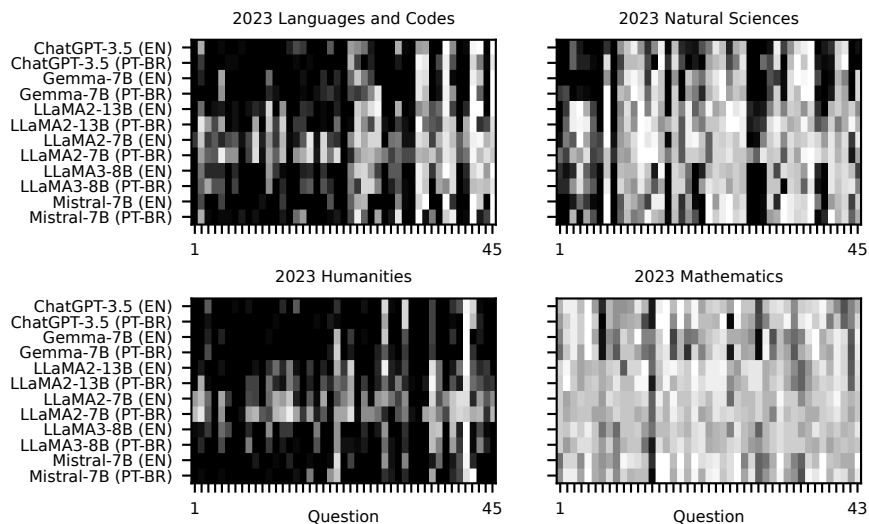


Figure 2: Response patterns for each LLM, where darker indicates more often correct (across random option shuffles). Questions are sorted in increasing difficulty ( $\beta$  value). LLMs are non-instructed tuned open source models and GPT3.5 with four-shot.

261 questions in the Humanities exam, implying that this is an easy exam for them. The performance of  
 262 LLMs in the Natural Science exam is the most interesting as there are blocks of questions that most  
 263 LLMs answer consistently correctly, interleaved with blocks of questions that most LLMs answer  
 264 incorrectly. This suggests that there are questions that are easy for humans but difficult for LLMs  
 265 and vice versa. In the next subsection we analyze this phenomenon more closely.

### 266 5.3 Reliability of IRT scores for LLMs

267 In this section, we investigate whether the ENEM exam is a valid test for LLMs’ ability, in the same  
 268 way it is for humans. Intuitively, we want to define measures that allow us to quantify to what extent  
 269 we trust the IRT scores we obtained for LLMs. We propose three different ways of doing this. The  
 270 first is *goodness-of-fit* that quantifies whether the response of LLMs fit the IRT model. The second  
 271 is based on *Fisher information*, measuring how much information the exam provides for estimating  
 272 the  $\theta$ s in a certain range. Finally, we use the *discrimination index* which evaluates the capacity of  
 273 questions to accurately distinguish between high and low performing test takers.

274 **Goodness-of-fit:** We use the  $l_z$  score (see Section 3) assess whether the test taker is behaving in  
 275 a manner consistent with the model. Alternatively, we ask what is the *appropriateness* of a test-  
 276 taker’s estimated  $\hat{\theta}$  as a measure of the test taker’s true  $\theta$ ? For example, imagine that an LLM has  
 277 a response pattern of missing easy questions and correctly answering more difficult ones. Such a  
 278 pattern may arise because the LLM was lucky on the hard questions, or it may arise because the  
 279 LLM had access to memorized patterns that assisted in answering the hard questions. Generally,  
 280 low  $l_z$  scores suggest that the  $\theta$  estimate of the model is less reliable [12].

281 In Figure 3 we show  $l_z$  scores plotted against  $\theta$  scores of LLMs across the four exams in 2023 (2022  
 282 is shown in Appendix A.9). As in previous plots, the light blue points in the background show the  
 283 distribution of the same two scores for the human test takers. Starting again with the Math exam, we  
 284 note that  $l_z$  values are low, but now we can see that the response patterns of the LLMs are indeed  
 285 quite human-like; LLMs behave like humans with similarly low  $l_z$  values. One possible reason for  
 286 this behavior is that the Mathematics exam tends to be the harder exam of ENEM, leading to more  
 287 guessing, which may make the human  $l_z$  values for Mathematics smaller.

288 For the Languages exam, models perform better in general (higher  $\theta$  values) and the most  $l_z$  scores  
 289 being close to 0 (and with a similar spread as the human distribution of  $l_z$ ’s) suggest that these  $\theta$   
 290 estimates are reliable – the models are showing human-like response patterns.

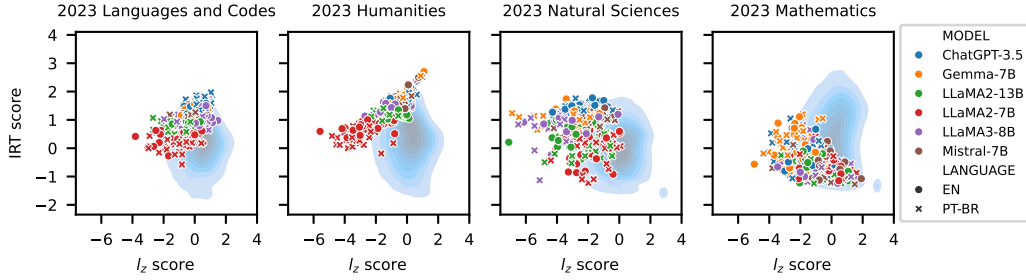


Figure 3: Distribution of  $l_z$  and IRT scores for humans and LLMs. LLMs are non-instructed tuned open source models and GPT3.5 with 4-shot. LLM datapoints are computed from different shuffles.

291 The results become more nuanced as we look at the Natural Sciences exam. For this exam, most  
 292 models, including the high performing ones (i.e., GPT-3.5 and Gemma-7B), show values well out-  
 293 side the human distribution, with a long tail in the negative values of  $l_z$ . Comparing the GPT-3.5 and  
 294 Gemma-7B results in Figures 1 and 4, we can infer that the high accuracy (CTT scores) achieved by  
 295 these models on the Natural Sciences exam are quite misleading; although GPT-3.5 and Gemma-7B  
 296 answer many questions correctly, their response pattern is very unlikely, with very low  $l_z$  values.  
 297 This corroborates with Figure 2, which shows an interchange of blocks of correct and incorrect  
 298 answers from the models, creating an unlikely response pattern.

299 In Humanities, almost all LLMs perform reasonably well, achieving  $\theta$  scores above zero (the average  
 300 human level). However, Llama2-7B, while obtaining above average accuracy scores (Figure 1) and  
 301 good  $\theta$  scores, has low average  $l_z$  scores. This suggests that the IRT scores Llama2-7B may be not  
 302 reliable. Examination of the corresponding rows in Figure 2 shows that this is the only model that  
 303 does not have a consistent response pattern across shuffles, leading to the observed low  $l_z$  score.

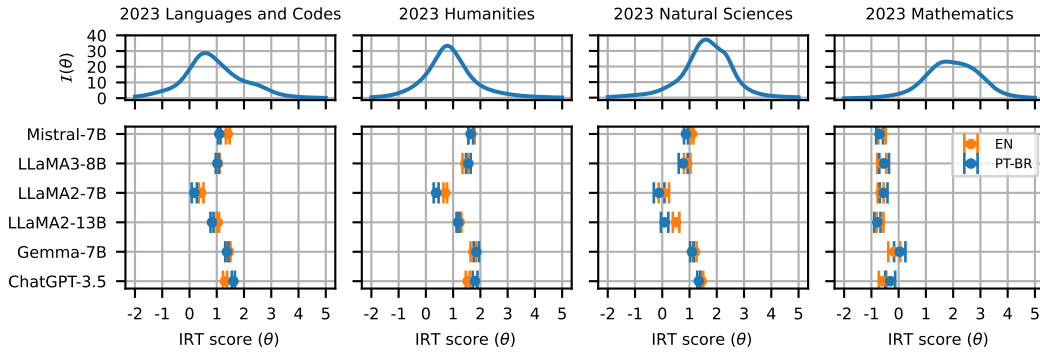


Figure 4: Total Fisher information of the exams and the IRT scores (95% Confidence Interval (CI)) for LLMs. LLM datapoints are computed from different shuffles.

304 **Fisher Information:** We investigate further whether the ENEM exams are giving us accurate esti-  
 305 mates of the LLMs ability levels from another standpoint – that of Fisher Information (see Section 3,  
 306 Equation (3)). Intuitively, Fisher Information quantifies whether there was enough information in  
 307 the test to infer the ability level of a test taker at a certain ability level. Figure 4 shows, for every  
 308 ENEM exam, the total Fisher Information  $\mathcal{I}(\theta)$  on the top plot, and the  $\theta$  scores for the models (95%  
 309 Confidence Interval (CI) computed using the shuffles) on the bottom plot. This plot reinforces the  
 310 observation that for some models in Natural Sciences and for all models in Mathematics, the mod-  
 311 els’  $\theta$  are not in the range of the exam with highest information – the models ability levels fall in the  
 312 tail of the Fisher Information histogram. Hence, *the Math exam is not useful for making meaningful*  
 313 *measurements of these LLMs*, casting doubt on the informativeness of the models’  $\theta$  scores on this  
 314 exam. The lack of discrimination ability of this exam is reflected by the responses for many models  
 315 showing apparently random response patterns in the corresponding heatmap (see Figure 2).



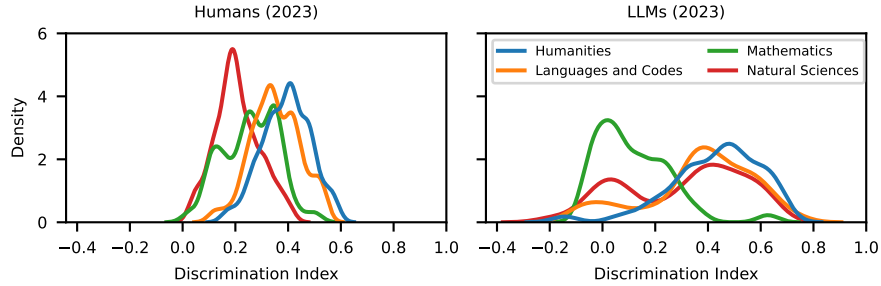


Figure 5: Discrimination Indices for questions in the 2023 exam for both Humans and LLMs.

316 **Discrimination Index:** To further assess the reliability of the IRT scores, we also turn into psychometrics and use the notion of the item *discrimination index* ( $DI$ ), which measures how well an item  
 317 on a test distinguishes between high and low scorers on the entire test [9]. Let  $P_h$  (resp.  $P_l$ ) be the  
 318 proportion of the top 25% (resp. low 25%) LLMs (in terms of  $\theta$ , including the shuffles) that correctly  
 319 answer the item; then  $DI = P_h - P_l$ , the difference of the two proportions.  $DI$  ranges from -1 to 1,  
 320 and questions with  $DI$  higher than 0.2 are considered good, while lower  $DI$  indicates flaws [50].  
 321

322 Figure 5 shows the distribution of the discrimination indices computed for humans and LLMs for the  
 323 2023 exam. Overall, we notice that discrimination indices computed for LLMs are more negative  
 324 compared to those of humans. We also observe that a significant fraction of Math questions have low  
 325 discriminative power, reinforcing the hypothesis that this exam is not well designed to measure Math  
 326 abilities for LLMs. Nonetheless, the Humanities and Languages have several questions with very  
 327 good discriminative power. Interestingly, the Natural Sciences exam appears to follow a bimodal  
 328 distribution, containing both informative and poorly-designed questions. This may be a reflection of  
 329 the fact that the Natural Sciences exam is a hybrid test, containing a mix of knowledge-based items  
 330 and items that demand more complex reasoning over numbers and images, which can be less useful  
 331 for evaluating the current state-of-the-art LLMs.

332 **Attributes affecting reliability of IRT scores:** In a further investigation, shown in Appendix A.2,  
 333 we explore potential causes of low discrimination. We investigate item attributes such as the ex-  
 334 istence of images or numbers in the questions as we believe that these attributes impede LLMs  
 335 from understanding the question properly. Our preliminary results suggest that LLMs’ ability to  
 336 understand math questions and parse images is sub-par compared to their capacity in answering  
 337 pure text-based questions. In Appendix A.10 we show examples of non-discriminating and highly  
 338 discriminating items for the 2023 Natural Sciences exam. In Appendix A.3, we reach a similar  
 339 conclusion by looking at model accuracy against model perplexity, a model intrinsic metric.

## 340 6 Conclusions

341 The ongoing debate in LLM evaluation centers around whether exams designed for humans are  
 342 appropriate tools for measuring the performance of LLMs. In this paper, we provide a case study  
 343 that illustrates methods that can be used to address this question, as well as specific results for a  
 344 range of current LLMs. We leverage the largest known human exam for which a public IRT model  
 345 is available, and show that IRT can be leveraged to distinguish between human-like and non-human-  
 346 like responses under the model. We show cases where LLMs respond in non-human-like ways and  
 347 show how to identify those cases using a model-fit metric. Further, we show that using IRT we  
 348 can determine when an exam is capable of making meaningful measurement of an LLM’s ability  
 349 in a given subject area. Using our evaluation framework, we find that the ENEM Math exam is not  
 350 appropriate to make meaningful measurements of the models’ ability, for the LLMs we study. At  
 351 the same time, Humanities and Language exams are better suited for evaluating the LLMs’ abilities  
 352 on those subjects. We conclude that IRT modeling, drawing on a long history of psychometric  
 353 theory, provides a set of crucial tools for assessing whether exams designed for humans are actually  
 354 meaningful measures of LLM ability. Our results suggest that they should be used in future studies  
 355 when questions are raised regarding the performance of LLMs on human exams.

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language	subject	Accuracy (CTT)	$\theta$	$l_z$
en	humanities	$29.5 \pm 10.7$	$-0.57 \pm 0.56$	$-1.25 \pm 1.18$
en	languages	$24.7 \pm 8.6$	$-0.99 \pm 0.49$	$-0.39 \pm 1.03$
en	science	$25.5 \pm 8.2$	$-0.34 \pm 0.53$	$-0.74 \pm 1.25$
en	math	$22 \pm 6.3$	$-0.6 \pm 0.34$	$-0.66 \pm 0.97$
pt-br	humanities	$24 \pm 7$	$-0.83 \pm 0.38$	$-0.83 \pm 1.08$
pt-br	languages	$23.1 \pm 7.1$	$-1.06 \pm 0.42$	$-0.32 \pm 1.01$
pt-br	science	$23.5 \pm 7.3$	$-0.48 \pm 0.41$	$-0.5 \pm 1.18$
pt-br	math	$23.2 \pm 6.4$	$-0.55 \pm 0.4$	$-0.86 \pm 1.05$

Table 1: Random choice selection performance on English and Portuguese versions of 2022 test 4 subjects.

## 501 A Supplemental Material

### 502 A.1 Manual auditing of exam questions

503 Assuming the original questions written by the ENEM authorities are good test instruments for  
504 testing student capability, we focus on ensuring the quality of adapted dataset for LLM evaluation.  
505 We manually correct the artifacts for each question in 2022 and 2023. In the next sections, we  
506 describe the artifacts from those easier to address (sec A.1.2 A.1.3), to deeper-rooted problems (i.e.,  
507 harder to correct, sec A.1.4), as well as how we addressed them manually (sec A.1.5).

#### 508 A.1.1 Label accuracy

509 We assume answers are correct as translation and parsing of single characters can be quite reliable,  
510 and that the original ENEM test is tested across millions of human test takers and will be discarded  
511 if it had a wrong answer. When we look at the label distribution for 2022, options “ABCDE” each  
512 occur 39/39/37/36/33 times, making it fairly balanced. We also ran random baselines on the same  
513 option shuffles as the model (Table 1).

#### 514 A.1.2 Translation artifacts

515 We found several issues pertaining to initial round of translation in this dataset. Mainly, independent  
516 translation of question context and answer option leads to incoherence. Details are sometimes mis-  
517 translated (“p.d.d” translated to “d.d.p”). There are many non-standardized translations pertaining  
518 to chemical formulas, proper nouns, and mathematical formulas. In general, there are significant  
519 amount of awkward phrasing, incomplete translation, and linguistic idiosyncrasies lost in transla-  
520 tion.

521 **Independent translation of context and question** In a few cases, the answer options are expected  
522 to complete the last sentence of the question. After translation, options do not all fit as completions of  
523 the sentence (Q11). Translation without context also leads to improper translation of polysemantic  
524 terms. “Coagulation” maybe translated correctly in the question, but becomes “coagulating” as  
525 a stand-alone word (Q96). “Good” and “fair” (when used as survey options) gets translated to  
526 “regular” and “I will” as stand-alone options (Q171)

527 **Inconsistent translation details** Within the same questions, there are cases where the same con-  
528 cept is translated differently. In one question, the context introduces the concept “potential difference  
529 (p.d.d)”, and later referred to it as “d.d.p” and “d.p.d”. Within different options, the same unit can  
530 sometimes be plural and sometimes be singular (when it should be consistently plural)

531 **Non-standard translation** 1) Chemical formula translation is non-standard. “N2O3” becomes “N  
532 2O3”, and “NH4+” becomes “NH4 positively charged”. 2) (Proper) nouns are sometimes capital-  
533 ized when they shouldn’t. For instance, one question begins with the sentence “*On the Gravitational*  
534 *Field of a Mass Point According to Einstein’s Theory A ‘Black Hole is a...*” 3) Mathematical equa-  
535 tions are overly verbatim. This we suspect is partially due to an issue with using audio version of the

536 test. For example, if an option is the formula  $9\left(\frac{8!}{(8-2)!2!} - 1\right)$ , its Portuguese representation would  
537 be “9 vezes ( 8 fatorial dividido por ( 8 menos 2) fatorial vezes 2 fatorial) menos 1)” and the En-  
538 glish translation exacerbates the situation by translating parenthesis literally as well: “9 times open  
539 parenthesis, open parenthesis, 8 factorial divided by, open parenthesis, open parenthesis, 8 minus  
540 2, close parenthesis, factorial times 2 factorial, close parenthesis, close parenthesis, minus 1, close  
541 parenthesis.”. Sometimes, delimiters are omitted after translation: “9,300” becomes “9 300”.

542 **Awkward phrasings** There exist awkward phrasings throughout translation. They range from  
543 causing minor difficulty in understanding (i.e., “*Life: the science of biology Bears, because they*  
544 *are not truly hibernating, wake up due to the presence of thermogenin, a mitochondrial protein that*  
545 *prevents protons from reaching ATP synthase, generating heat.*”) to sometime completely non-sense  
546 (i.e., “*articulation of several narrative nuclei*”)

547 **Incomplete translation** There is no fine line between proper code switching (where proper nouns  
548 should remain in Portuguese script) to in-complete translation. The amount of Portuguese left over  
549 range from single words, to phrases in options (not consistently across options), to entire sentences  
550 within the question.

551 **Linguistic idiosyncrasies lost in translation** In one question, the problem arises when English  
552 translation does not match with literal tokens of expressions in Portuguese (“*Next to the man is*  
553 *the message: “Men don’t cry”, with a large X drawn over the word “no”*). The word “no” does  
554 not appear in the English phrase “Men don’t cry” but the statement as a whole makes sense in the  
555 Portuguese version of the instruction. In a separate question, the topic is on testing for a Portuguese  
556 specific pronoun inflection. However, when it was translated into one single word in English, the  
557 question no longer makes sense (“*They told me... - They told me. - Huh? - The correct word is “they*  
558 *told me”. Not “they told me”. - I speak the way I want to. And I’ll tell you more... Or is it “tell*  
559 *you”? - What’s that? - I’m telling you that you... - “You” and “you” don’t go together... ”*)

### 560 **A.1.3 Document parsing artifacts**

561 Each section consistently contains an error of this kind, where the last part of the question got wrong-  
562 fully parsed into part of the first option (option (A)). In a separate instance, a figure was wrongfully  
563 parsed into one of the options of the previous question. In the Portuguese version of the exam, struc-  
564 tural components of the question (e.g., title, subtitle, caption) are consistently concatenated together  
565 without proper separation. This often leads to incoherent English translations.

### 566 **A.1.4 Audio-version artifacts**

567 Audio description of images, tables, and figures are not always sufficient, or the most intuitive. For  
568 instance, a question asks test taker to note why a particular painting stands out, and the answer is  
569 due to the painting’s “distortion when representing human figure”, which is difficult to qualitatively  
570 describe, no matter how complete the description of an image is. Similarly, textual description  
571 of geometric figures can be impossibly complicated (“*...Figure of a grid with 7 horizontal and 7*  
572 *vertical lines, on which a polygonal path is drawn by means of a continuous line on the grid lines,*  
573 *joining the starting point P , located on the second vertical line, from left to right, and between the*  
574 *sixth and seventh horizontal lines, from top to bottom, to the end point Q , which is located between*  
575 *the sixth and seventh vertical lines, from left to right, and on the second horizontal line, from top to*  
576 *bottom...*”)

### 577 **A.1.5 Manual Correction**

578 The majority of the artifacts begin with incorrect parsing of the PDF documents related to struc-  
579 tural components. To address this, we manually audited each question, and added correct spacing  
580 and newlines to each question. These improvements result in better translations from DeepL API  
581 qualitatively. After translation, we make minimal edits to improve syntactic and semantic issues  
582 through Grammarly to obtain a score of at least 95<sup>2 3</sup>. For each answer option, we ensure consistent

---

<sup>2</sup>grammarly.com/

<sup>3</sup>We chose not to use a large model such as GPT3.5 to rephrase the translations because it may artificially lower the perplexity and change the meaning of the questions.

583 part-of-speech, especially if they are sentence completions of the questions. For math and science  
584 sections, we follow consistent markdown-like format the same way as other mathematical reasoning  
585 datasets [16, 11, 52]. Here we list the full set of modification rules for 2022 (question numbers are  
586 referenced in parenthesis):

- 587 • Separate description of the image by '\n' before and after.
- 588 • “Por cento” becomes %.
- 589 • Number in the form 7 000 becomes 7000.
- 590 • From “abre aspas” “fecha aspas” to “”.
- 591 • Remove “Descrição da estrutura química”, “Descrição do esquema”, “Descrição da  
592 associação de baterias”, “Descrição da imagem” from the options”.
- 593 • “De carga positiva” to +, “De carga negativa” to -, “de carga dois menos” to (2-).
- 594 • For a subset of the questions, we follow the non-blind version of the question (157, 158,  
595 163, 166, 168, 171, 174, 177, 178, 179)
- 596 • Remove period at the end options or questions of math questions (to avoid confusion).

597 Here are the list of rules we use for English version of the exam (2022):

- 598 • Change number decimal from “3,1415” to “3.1415”.
- 599 • Manual translation fix (49, 162).

#### 600 **A.1.6 Limitations of the dataset**

601 There are a few limitations of the dataset:

- 602 1. Even though the English version of the exam is modified manually, there are still issues  
603 with the presentation of the questions. We rely mostly on Grammarly feedback, but it is  
604 not perfect. Our judgement of how fluently a question is written is also subjective. The  
605 ideal method would be to recruit professional human translators, which is costly and time  
606 consuming.
- 607 2. The content of many of the questions are focused on knowledge common to Brazilian  
608 culture, or problems in Brazilian society. The English translations may not cover the full  
609 extent of cultural, language specific phenomenons or connotations.
- 610 3. We assume the transcription of images and tables to be sufficient for the models to under-  
611 stand and solve the question.

#### 612 **A.2 Attributes that affect goodness-of-fit**

613 Given that questions have wide range of discrimination indices for LLMs, we investigate a potential  
614 cause described in the psychometrics literature for aberrant response patterns: lack of *subabili-*  
615 *ties* [23], i.e., specific skills required to answer a question correctly. We hypothesize that some item  
616 attributes, such as whether the question contains images or numbers in its statement or among the  
617 options, may be disproportionately harder for LLMs and hence represent subabilities that explain  
618 the aberrant response patterns quantified in Figure 3.

619 We built a contingency table relating non-discriminative/discriminative items (i.e., items with dis-  
620 criminative index lower/higher than 0.2) and the aforementioned attributes, and run a  $\chi^2$  indepen-  
621 dence test. The results for the Natural Sciences exam are shown in Table 2. For this exam, we  
622 observe high  $\chi^2$  values which indicate that the abilities of the LLM models with respect to math  
623 reasoning and interpreting images are sub-par compared to their capacity in solving pure text ques-  
624 tions. While Language and Humans exams are most purely text and the Math exam mostly demands  
625 reasoning with images and numbers, the nature of the Natural Sciences exam is hybrid, containing  
626 both types of questions. This may well explain the bimodal distribution of discrimination indices  
627 in Figure 5 and the aberrant response patterns identified by the very low  $l_z$  scores in Figure 3, and  
628 highlights how psychometrics can aid the design of better and more valid benchmarks for LLMs.

Table 2:  $\chi^2$  test for the correlation between poorly-discriminating items and item attributes in the Natural Sciences exam in 2022 and 2023. Significant values are in bold. High values of  $\chi^2$  indicate that images or numbers make the item less useful to evaluate the LLMs we experiment with.

Item Attribute	2022	2023
Contains images	0.401 (0.052)	<b>3.906</b> (0.048)
Contains numbers in the answers	<b>7.331</b> (0.007)	<b>6.264</b> (0.012)
Contains numbers in the statement	<b>3.961</b> (0.046)	3.212 (0.073)

### 629 A.3 Model accuracy relation to model perplexity

630 One reason that models may error differently than humans is due to their training corpus. If models  
 631 have encountered similar question or topics, if not identical, to those in our dataset during training,  
 632 they may perform unexpectedly well, even if the questions are difficult. Recent work in data con-  
 633 tamination proposed a few model intrinsic metrics that can be used to detect contamination [36].  
 634 Mainly, the Min-k% Prob score takes the average probability of the top-k percentile tokens with  
 635 minimum probabilities <sup>4</sup>:

$$\text{MIN-K\% Prob}(x) = -\frac{1}{E} \sum_{x_i \in \text{Min-K\%}(x)} \log p(x_i | x_1, \dots, x_{i-1}) \quad (4)$$

636 where  $x = x_1, x_2, \dots, x_N$  denotes the input sequence of N tokens, Min-K% Prob(x) represents the  
 637 set containing tokens with minimum k percentile probabilities, and E represents the size of such set.  
 638 Note here that Min-k% Prob is intrinsic to each model, and if a model has been exposed to more  
 639 similar training data as the questions, its Min-k% Prob would be low for that question.

640 We do not expect any model to have unexpectedly low Min-K% Prob(x) on any of our questions,  
 641 considering it is highly unlikely that the ENEM questions were parsed and translated to English, and  
 642 somehow ended up in the training corpus. What we are more interested here, is whether such score  
 643 is correlated to model’s accuracy on the answer predictions. If they are negatively correlated (i.e.  
 644 high Min-K% Prob corresponds to low accuracy), this is evidence for the hypothesis that training on  
 645 related data leads to higher accuracy.

646 To investigate this hypothesis, we plot 4-shot model accuracy (averaged across 31 option shuffles)  
 647 against Min-20% Prob for four subjects in exam 2022 in English along with the Pearson correlations  
 648 <sup>5</sup> in Figure 6. In all except 1 model-subject pair (Llama2 chat in humanities, we investigate this  
 649 further) do we see a significant negative correlation ( $p < 0.05$ ) between accuracy and Min-k 20%  
 650 Prob, indicate that model doesn’t necessarily do better if they have encountered similar data during  
 651 training. Another way to interpret this, is that it is not likely that these models have seen our data  
 652 during training.

653 **The few negative correlation cases** As seen before, we observe a significant negative correlation  
 654 for Llama-2 7B Chat in humanities. To get a full understanding of whether this is a stand-alone  
 655 phenomenon, we examine Portuguese version of the exam, as well as exam in 2023, and show our  
 656 findings below in Table 3. We do not see the same correlation in the Portuguese version of the  
 657 exam. However, we additionally see Gemma-it negatively correlated with humanities section in  
 658 both English and Portuguese version of the exam in 2023, as well as Gemma with languages section  
 659 in 2023. The later two correlations are robust across a few other metrics we investigated from [36]  
 660 as well, we think this may suggest data contamination, but we cannot test such hypothesis because  
 661 Gemma training data is not public.

662 **Positive correlations in 2022 science** In 2022 Science, both English and Portuguese, we see sig-  
 663 nificant *positive* correlation across all models (Table 3).

664 Through qualitative analysis, we find that the questions with highest perplexities were formatted  
 665 more in a sentence completion-like structure similar to Question 1. Whereas less perplexity ques-

<sup>4</sup>We follow the equation in <https://github.com/swj0419/detect-pretrain-code/blob/main/src/run.py>

<sup>5</sup><https://docs.scipy.org/doc/scipy/reference/generated/scipy.stats.pearsonr.html>



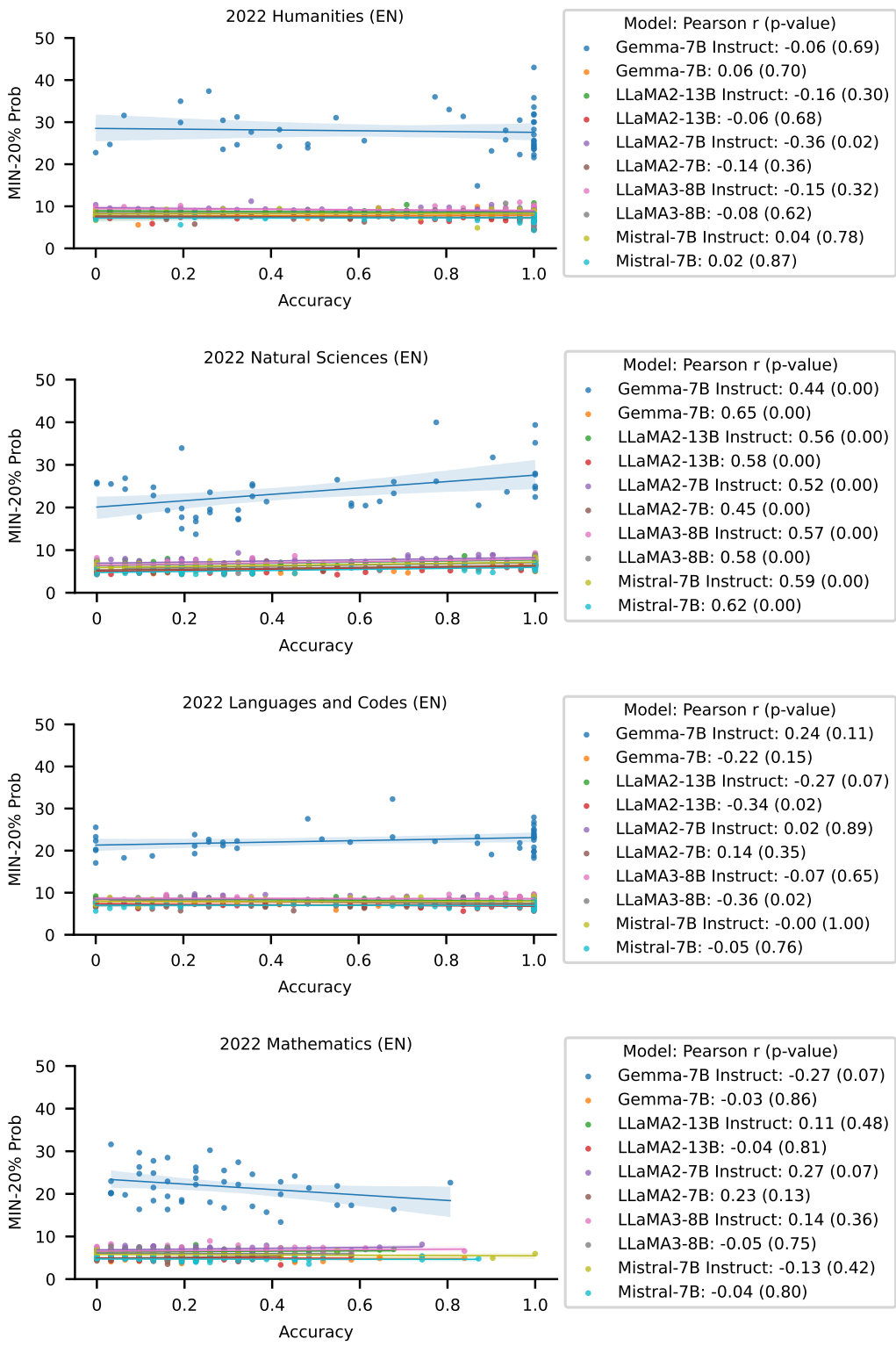


Figure 6: Model Min-20% Prob vs. 4-shot accuracy across four subjects in 2022 in English

666 tions involve more image/table description with reasoning needed to obtain the answer (question 2).  
667 This is similar to what we discover with discriminative index in Section ?? in the main text.

```
668 1 Question: Technique modifies rattlesnake venom protein to create a
669     drug that modulates blood clotting
670 2
671 3 Rattlesnake venom can cause life-threatening hemorrhaging to those
672     bitten by the snake. However, researchers from Brazil and Belgium
673     have developed a molecule of pharmaceutical interest, PEG-
674     collinein-1, from a protein found in the snake's venom. The
675     molecule is capable of modulating blood clotting. Although the
676     technique is not new, it was applied for the first time from an
677     animal toxin in its recombinant form, i.e. produced in the
678     laboratory by a genetically modified fungus.
679 4
680 5 This new drug has potential applications for
681 6 Options:
682 7 (A) prevent the formation of thrombi, typical in some cases of stroke.
683 8 (B) treat the consequences of profound anemia, due to the loss of a
684     large volume of blood.
685 9 (C) prevent the manifestation of urticaria, commonly related to
686     allergic processes.
687 10 (D) reduce swelling of the lymph nodes, part of the immune response to
688     different infections.
689 11 (E) regulate the fluctuations in blood pressure characteristic of
690     hypertension.
```

Listing 1: high perplexity question with high model accuracy.

```
691 1 Question: On a hot day, two colleagues are playing with the water from
692     the hose. One of them wants to know how high the water jet
693     reaches from the outlet when the hose is positioned vertically.
694     The other colleague then proposes the following experiment: they
695     position the water outlet of the hose in a horizontal direction, 1
696     meter above the ground, and then measure the horizontal distance
697     between the hose and the place where the water hits the ground.
698     The measurement of this distance was 3 meters, and from this, they
699     calculated the vertical reach of the water jet. Consider the
700     acceleration of gravity to be 10 meters per second squared.
701 2
702 3 The result they obtained was
703 4 Options:
704 5 (A) 1.50 meter.
705 6 (B) 2.25 meters.
706 7 (C) 4.00 meters.
707 8 (D) 4.50 meters.
708 9 (E) 5.00 meters.
```

Listing 2: low perplexity question with low model accuracy.

709 We also tried filtering for top N percent most difficult questions per subject and recalculate all the  
710 correlations. We did not find any significant difference to results above.

#### 711 A.4 Prompting Details

712 To administering the test to LLMs, we measure the next token logits across the 5 letter options  
713 directly (i.e. letter “A”, “B”, “C”, “D”, “E”), and take the argmax as the model’s choice (invariant  
714 to sampling temperature). We shuffle the option orders (30 runs) and take the average to calibrate  
715 model’s prior on generating each letter options. For API-based model (GPT3.5), we query for 1  
716 token generation, and obtain top-20 logits, and use that for our prediction. In the sections below we  
717 include 0-shot (Listing 3), 1-shot (Listing 4, 5, 6, 7), and 4-shot prompts (Listing 8) we use in main  
718 experiments. For 1-shot, we choose the 1-shot example for each of the four subjects by selecting  
719 the easiest question (i.e., with lowest  $\beta$ ) from the same subject in the 2021 exam. For 4-shot, we  
720 concatenate the 1-shots from four subjects and shuffle the options to evenly distribute the answer  
721 among five option letters.

year	lang	subj	L2-7b	L2-7b-it	L2-13b	L2-13b-it	L3-8b-it	L3-8b	M-7b	M-7b-it	G-7b-it	G-7b	
2022	en	CH	-0.14/0.36	<b>-0.36/0.02</b>	-0.06/0.68	-0.16/0.30	-0.15/0.32	-0.08/0.62	0.02/0.87	0.04/0.78	-0.06/0.69	0.06/0.70	
		LC	0.14/0.35	0.02/0.89	<b>-0.34/0.02</b>	-0.27/0.07	-0.07/0.65	<b>-0.36/0.02</b>	-0.05/0.76	-0.00/1.00	0.24/0.11	-0.22/0.15	
		CN	<b>0.45/0.00</b>	<b>0.52/0.00</b>	<b>0.58/0.00</b>	<b>0.56/0.00</b>	<b>0.57/0.00</b>	<b>0.58/0.00</b>	<b>0.62/0.00</b>	<b>0.59/0.00</b>	<b>0.44/0.00</b>	<b>0.65/0.00</b>	
		MT	0.23/0.13	0.27/0.07	-0.04/0.81	0.11/0.48	0.14/0.36	-0.05/0.75	-0.04/0.80	-0.13/0.42	-0.27/0.07	-0.03/0.86	
		CH	-0.09/0.56	-0.12/0.43	-0.06/0.70	-0.05/0.73	-0.07/0.65	-0.05/0.74	-0.09/0.56	-0.06/0.69	-0.20/0.18	0.18/0.24	
	pt	LC	0.10/0.53	-0.02/0.88	-0.06/0.67	-0.05/0.73	0.08/0.61	-0.20/0.20	0.14/0.35	-0.09/0.56	0.14/0.37	-0.21/0.16	
		CN	<b>0.41/0.01</b>	<b>0.42/0.00</b>	<b>0.49/0.00</b>	<b>0.48/0.00</b>	<b>0.57/0.00</b>	<b>0.52/0.00</b>	<b>0.53/0.00</b>	<b>0.52/0.00</b>	<b>0.46/0.00</b>	<b>0.58/0.00</b>	
		MT	-0.17/0.26	-0.15/0.34	0.12/0.44	-0.02/0.91	0.07/0.66	-0.08/0.59	-0.18/0.23	-0.14/0.35	-0.05/0.76	0.12/0.42	
		CH	-0.06/0.72	-0.07/0.66	-0.09/0.56	0.06/0.69	-0.20/0.20	-0.18/0.23	-0.20/0.18	-0.07/0.65	<b>-0.32/0.03</b>	-0.16/0.30	
		LC	-0.06/0.67	-0.22/0.15	<b>-0.31/0.04</b>	-0.24/0.12	-0.21/0.17	<b>-0.30/0.04</b>	-0.18/0.23	-0.08/0.61	-0.05/0.76	<b>-0.32/0.03</b>	
2023	en	CN	0.21/0.17	0.21/0.17	<b>0.31/0.04</b>	0.16/0.31	<b>0.30/0.05</b>	0.28/0.06	0.14/0.35	0.15/0.34	0.20/0.19	0.24/0.11	
		MT	0.17/0.28	-0.07/0.66	-0.04/0.82	-0.02/0.87	-0.05/0.75	0.15/0.35	0.03/0.85	0.19/0.21	0.06/0.68	0.16/0.32	
		CH	-0.00/1.00	-0.02/0.92	0.09/0.58	0.18/0.25	-0.02/0.90	-0.11/0.46	-0.04/0.77	0.01/0.96	<b>-0.30/0.05</b>	-0.09/0.55	
		LC	-0.21/0.16	-0.23/0.13	-0.27/0.07	-0.17/0.26	-0.20/0.18	-0.24/0.11	-0.18/0.23	-0.10/0.53	-0.13/0.40	<b>-0.36/0.02</b>	
		CN	0.11/0.49	0.17/0.26	0.25/0.10	0.04/0.82	0.14/0.37	<b>0.36/0.01</b>	0.15/0.32	0.14/0.35	0.08/0.61	0.13/0.41	
	pt	CH	-0.01/0.96	0.02/0.87	-0.02/0.90	-0.04/0.79	-0.07/0.67	0.06/0.71	-0.08/0.60	0.09/0.56	0.18/0.24	0.28/0.06	

Table 3: Correlation between model accuracy and Min-k% Prob across exam, languages, and subjects for all models (**L2**=llama2, **L3**=Llama3, **M**=Mistral, **G**=gemma, **it**=instruction-tuned/chat). The first number indicates the coefficient of the correlation, and the second, the p-value. Entries with p-value < 0.05 are in **bold**. **CN**=Humanities, **LC**=Languages, **CN**=Sciences, **MT**=Math

722 **Potential limitations** We ran exploratory experiments with Chain-of-Thought (CoT) like prompting  
723 [49], but did not see significant changes. We did not include the results because CoT prompting  
724 requires generating reasoning strings and parsing answers, making 30-shuffles extremely slow  
725 to run for all models. Future directions could explore how much effect more complex prompting  
726 techniques have in assimilating model behaviors. Regarding the best prompting strategy, we do  
727 acknowledge recent criticisms on first letter evaluation[48]. At the time of our writing, it is still  
728 the best evaluation strategy for multiple choice question-answering data. We also acknowledge that  
729 there are more capable models than GPT3.5 that is available through API services but as our work is  
730 not trying to identify the SOTA model we did not feel the need to evaluate latest and largest models.  
731 Lastly, we assume Portuguese and Brazilian culture is present in the training data for the language  
732 models we test. Future work could evaluate the amount of multilingual training’s affect on some of  
733 these IRT metric we propose.

```

734 Here are some questions from a college entrance exam. Choose the
735 correct answer to the best of your ability, and output in the
736 following format:
737 Answer: (Option)
738
739 Question: {QUESTION}
740 Options:
741 (A) {OPTION_A}
742 (B) {OPTION_B}
743 (C) {OPTION_C}
744 (D) {OPTION_D}
745 (E) {OPTION_E}
746 Answer: (

```

Listing 3: 0-shot prompt used across all four subjects.

```

747 Here are some questions from a college entrance exam. Choose the
748 correct answer to the best of your ability, and output in the
749 following format:
750 Answer: (Option)
751
752 Question:
753 Buffalos are animals considered rustic by breeders and are therefore
754 left in the field without reproductive control. Because of this
755 type of breeding, inbreeding is common, leading to the appearance
756 of diseases such as albinism and heart defects, among others.
757 Separating the animals properly by sex would minimize the
758 occurrence of these problems.
759
760 What prior biotechnological procedure is recommended in this situation
761 ?

```

762 8  
763 9 Options:  
764 0 (A) Transgenics.  
765 1 (B) Gene therapy.  
766 2 (C) DNA vaccine.  
767 3 (D) Genetic mapping.  
768 4 (E) Therapeutic cloning.  
769 5  
770 6 Answer: (D) Genetic mapping.  
771 7  
772 8 Question: {QUESTION}  
773 9 Options:  
774 0 (A) {OPTION\_A}  
775 1 (B) {OPTION\_B}  
776 2 (C) {OPTION\_C}  
777 3 (D) {OPTION\_D}  
778 4 (E) {OPTION\_E}  
779 5 Answer: (

Listing 4: 1-shot prompt used for Natural Science.

780 1 Here are some questions from a college entrance exam. Choose the  
781 correct answer to the best of your ability, and output in the  
782 following format:  
783 2 Answer: (Option)  
784 3  
785 4 Question:  
786 5 A hamburger chain has three franchises in different cities. To include  
787 a new type of snack on the menu, the chain's marketing manager  
788 suggested putting five new types of snacks on sale in special  
789 editions. The snacks were offered for the same period of time to  
790 all the franchisees. The type with the highest average sold per  
791 franchise would be permanently included on the menu. At the end of  
792 the trial period, management received a report describing the  
793 quantities sold, in units, of each of the five types of snacks in  
794 the three franchises.  
795 6  
796 7 Image description: The table shows the quantity sold of each type of  
797 snack in franchises 1, 2, and 3.  
798 8 Franchise 1 sold 415 type-1 snacks, 395 type-2 snacks, 425 type-3  
799 snacks, 430 type-4 snacks, and 435 type-5 snacks.  
800 9 Franchise 2 sold 415 type-1 snacks; 445 type-2 snacks; 370 type-3  
801 snacks; 370 type-4 snacks and 425 type-5 snacks.  
802 0 Franchise 3 sold 415 type-1 snacks; 390 type-2 snacks; 425 type-3  
803 snacks; 433 type-4 snacks and 420 type-5 snacks.  
804 1  
805 2 Based on this information, the management has decided to include the  
806 following type of snack on the menu  
807 3  
808 4 Options:  
809 5 (A) 1  
810 6 (B) 2  
811 7 (C) 3  
812 8 (D) 4  
813 9 (E) 5  
814 0  
815 1 Answer: (E) 5  
816 2  
817 3 Question: {QUESTION}  
818 4 Options:  
819 5 (A) {OPTION\_A}  
820 6 (B) {OPTION\_B}  
821 7 (C) {OPTION\_C}  
822 8 (D) {OPTION\_D}  
823 9 (E) {OPTION\_E}

8240 Answer: (

Listing 5: 1-shot prompt used for Math.

```
825 1 Here are some questions from a college entrance exam. Choose the
826     correct answer to the best of your ability, and output in the
827     following format:
828 2 Answer: (Option)
829 3
830 4 Question:
831 5 The situation of the working class in England
832 6 Friedrich Engels
833 7
834 8 At the same time, thanks to the ample opportunities I have had to
835     observe the middle classes, your adversaries, I have quickly
836     concluded that you are right, absolutely right, not to expect any
837     help from them. Its interests are diametrically opposed to yours,
838     even if it constantly tries to claim the opposite and wants to
839     persuade you that it feels the greatest sympathy for your lot. But
840     her actions belie her words.
841 9
842 10 In the text, the author presents ethical outlines that correspond to
843 11
844 12 Options:
845 13 (A) the foundation of the idea of surplus value.
846 14 (B) concept of class struggle.
847 15 (C) fundamentals of the scientific method.
848 16 (D) paradigms of the inquiry process.
849 17 (E) domains of commodity fetishism.
850 18
851 19 Answer: (B) concept of class struggle.
852 20
853 21 Question: {QUESTION}
854 22 Options:
855 23 (A) {OPTION_A}
856 24 (B) {OPTION_B}
857 25 (C) {OPTION_C}
858 26 (D) {OPTION_D}
859 27 (E) {OPTION_E}
860 28 Answer: (
```

Listing 6: 1-shot prompt used for Humanities.

```
861 1 Here are some questions from a college entrance exam. Choose the
862     correct answer to the best of your ability, and output in the
863     following format:
864 2 Answer: (Option)
865 3
866 4 Question:
867 5 Sinh\`a
868 6 Chico Buarque and Jo\~ao Bosco
869 7
870 8 If the owner bathed
871 9 I wasn't there
872 10 By God our Lord
873 11 I didn't look Sinh\`a
874 12 I was in the fields
875 13 I'm not one to look at anyone
876 14 I'm not greedy anymore
877 15 I can't see straight
878 16
879 17 Why put me in the trunk
880 18 Why hurt me
881 19 I swear to you
882 20 I've never seen Sinh\`a
```

88321 [...]
88422 Why carve up my body
88523 I didn't look at Sinh'a
88624 Why would you
88725 You'll pierce my eyes
88826 I cry in Yoruba
88927 But I pray for Jesus
89028 So that you can
89129 Take away my light
89230
89331 In this fragment of the song's lyrics, the vocabulary used and the
894 situation portrayed are relevant to the country's linguistic
895 heritage and identity, in that
89632
89733 Options:
89834 (A) physical and symbolic violence against enslaved people.
89935 (B) value the influences of African culture on national music.
90036 (C) relativize the syncretism that makes up Brazilian religious
901 practices.
90237 (D) narrate the misfortunes of the love relationship between members
903 of different social classes.
90438 (E) problematize the different worldviews in society during the
905 colonial period.
90639
90740 Answer: (A) physical and symbolic violence against enslaved people
90841
90942 Question: {QUESTION}
91043 Options:
91144 (A) {OPTION\_A}
91245 (B) {OPTION\_B}
91346 (C) {OPTION\_C}
91447 (D) {OPTION\_D}
91548 (E) {OPTION\_E}
91649 Answer: (

Listing 7: 1-shot prompt used for Languages.

917 1 Here are some questions from a college entrance exam. Choose the
918 correct answer to the best of your ability, and output in the
919 following format:
920 2 Answer: (Option)
921 3
922 4 Question:
923 5 Buffalos are animals considered rustic by breeders and are therefore
924 left in the field without reproductive control. Because of this
925 type of breeding, inbreeding is common, leading to the appearance
926 of diseases such as albinism and heart defects, among others.
927 Separating the animals properly by sex would minimize the
928 occurrence of these problems.
929 6
930 7 What prior biotechnological procedure is recommended in this situation
931 ?
932 8
933 9 Options:
9340 (A) Transgenics.
9351 (B) Gene therapy.
9362 (C) DNA vaccine.
9373 (D) Genetic mapping.
9384 (E) Therapeutic cloning.
9395
9406 Answer: (D) Genetic mapping.
9417
9428 Question:
9439 Sinh'a
9440 Chico Buarque and Jo~ao Bosco

94521  
94622 If the owner bathed  
94723 I wasn't there  
94824 By God our Lord  
94925 I didn't look Sinh\`a  
95026 I was in the fields  
95127 I'm not one to look at anyone  
95228 I'm not greedy anymore  
95329 I can't see straight  
95430  
95531 Why put me in the trunk  
95632 Why hurt me  
95733 I swear to you  
95834 I've never seen Sinh\`a  
95935 [...]  
96036 Why carve up my body  
96137 I didn't look at Sinh\`a  
96238 Why would you  
96339 You'll pierce my eyes  
96440 I cry in Yoruba  
96541 But I pray for Jesus  
96642 So that you can  
96743 Take away my light  
96844  
96945 In this fragment of the song's lyrics, the vocabulary used and the  
970 situation portrayed are relevant to the country's linguistic  
971 heritage and identity, in that  
97246  
97347 Options:  
97448 (A) physical and symbolic violence against enslaved people.  
97549 (B) value the influences of African culture on national music.  
97650 (C) relativize the syncretism that makes up Brazilian religious  
977 practices.  
97851 (D) narrate the misfortunes of the love relationship between members  
979 of different social classes.  
98052 (E) problematize the different worldviews in society during the  
981 colonial period.  
98253  
98354 Answer: (A) physical and symbolic violence against enslaved people  
98455  
98556 Question:  
98657 The situation of the working class in England  
98758 Friedrich Engels  
98859  
98960 At the same time, thanks to the ample opportunities I have had to  
990 observe the middle classes, your adversaries, I have quickly  
991 concluded that you are right, absolutely right, not to expect any  
992 help from them. Its interests are diametrically opposed to yours,  
993 even if it constantly tries to claim the opposite and wants to  
994 persuade you that it feels the greatest sympathy for your lot. But  
995 her actions belie her words.  
99661  
99762 In the text, the author presents ethical outlines that correspond to  
99863  
99964 Options:  
100065 (A) the foundation of the idea of surplus value.  
100166 (B) concept of class struggle.  
100267 (C) fundamentals of the scientific method.  
100368 (D) paradigms of the inquiry process.  
100469 (E) domains of commodity fetishism.  
100570  
100671 Answer: (B) concept of class struggle.  
100772  
100873 Question:

1009<sup>7</sup>4 A hamburger chain has three franchises in different cities. To include  
1010 a new type of snack on the menu, the chain's marketing manager  
1011 suggested putting five new types of snacks on sale in special  
1012 editions. The snacks were offered for the same period of time to  
1013 all the franchisees. The type with the highest average sold per  
1014 franchise would be permanently included on the menu. At the end of  
1015 the trial period, management received a report describing the  
1016 quantities sold, in units, of each of the five types of snacks in  
1017 the three franchises.  
1018<sup>7</sup>5  
1019<sup>6</sup> Image description: The table shows the quantity sold of each type of  
1020 snack in franchises 1, 2, and 3.  
1021<sup>7</sup>7 Franchise 1 sold 415 type-1 snacks, 395 type-2 snacks, 425 type-3  
1022 snacks, 430 type-4 snacks, and 435 type-5 snacks.  
1023<sup>7</sup>8 Franchise 2 sold 415 type-1 snacks; 445 type-2 snacks; 370 type-3  
1024 snacks; 370 type-4 snacks and 425 type-5 snacks.  
1025<sup>7</sup>9 Franchise 3 sold 415 type-1 snacks; 390 type-2 snacks; 425 type-3  
1026 snacks; 433 type-4 snacks and 420 type-5 snacks.  
1027<sup>8</sup>0  
1028<sup>1</sup> Based on this information, the management has decided to include the  
1029 following type of snack on the menu  
1030<sup>2</sup>  
1031<sup>3</sup> Options:  
1032<sup>4</sup> (A) 1  
1033<sup>5</sup> (B) 2  
1034<sup>6</sup> (C) 3  
1035<sup>7</sup> (D) 4  
1036<sup>8</sup> (E) 5  
1037<sup>9</sup>  
1038<sup>0</sup> Answer: (E) 5  
1039<sup>1</sup>  
1040<sup>2</sup> Question: {QUESTION}  
1041<sup>3</sup> Options:  
1042<sup>4</sup> (A) {OPTION\_A}  
1043<sup>5</sup> (B) {OPTION\_B}  
1044<sup>6</sup> (C) {OPTION\_C}  
1045<sup>7</sup> (D) {OPTION\_D}  
1046<sup>8</sup> (E) {OPTION\_E}  
1047<sup>9</sup> Answer: (

Listing 8: 4-shot prompt used across all four subjects.



1048 **A.5 Compute Resources**

1049 We used GPUs (V100 or A100) provided by a university cluster<sup>6</sup>. For the main experiments, we  
1050 used around 200 hours of GPU time (roughly 20 hours per model). Moreover, we used the OpenAI  
1051 API to run the experiments with GPT3.5.

1052 **A.6 Zero and One Shot prompting Results for 2023**

1053 **A.6.1 CTT and IRT  $\theta$**

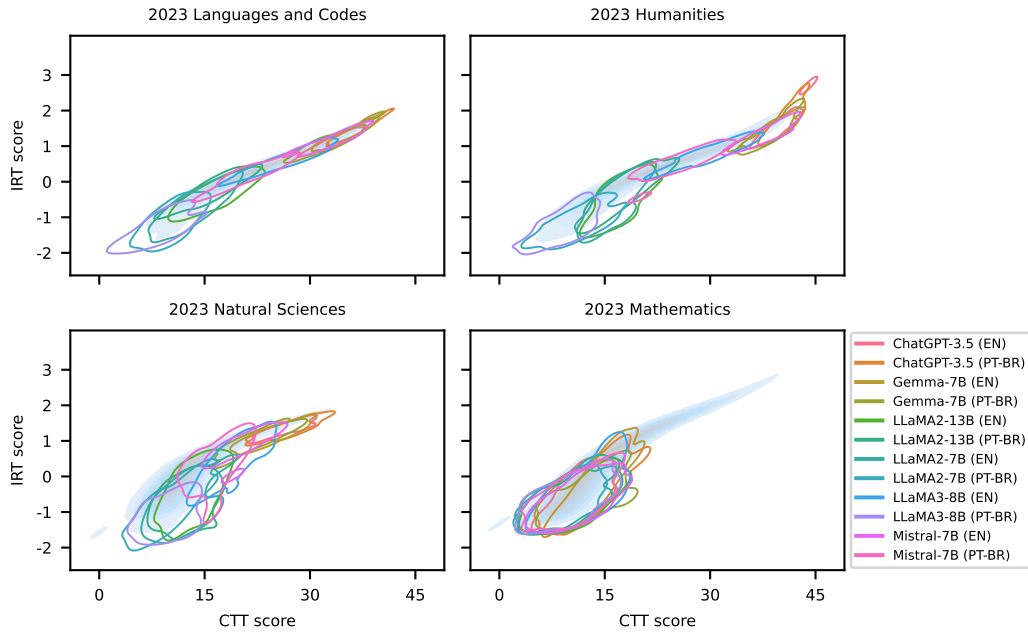


Figure 7: Distribution of CTT (accuracy) and IRT scores for humans and LLMs for the ENEM 2023 exam. LLMs are non-instructed tuned open source models and GPT3.5 with zero-shot. LLM datapoints are computed from different shuffles.

<sup>6</sup>We will disclose it after the reviewing phase due to the double-blind process.

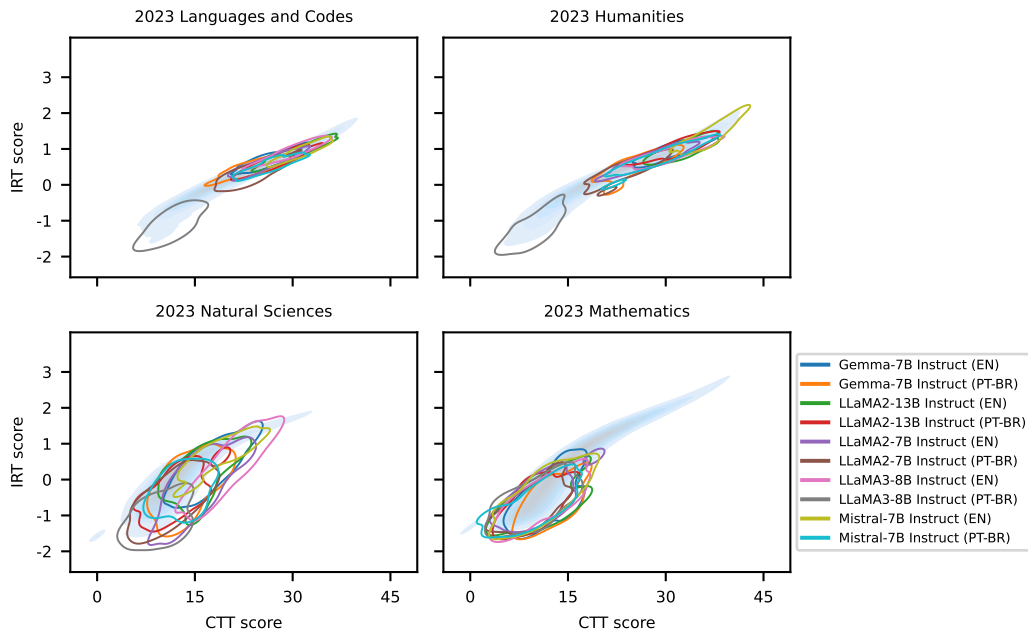


Figure 8: Distribution of CTT (accuracy) and IRT scores for humans and LLMs for the ENEM 2023 exam. LLMs are instructed tuned open source models with zero-shot. LLM datapoints are computed from different shuffles.

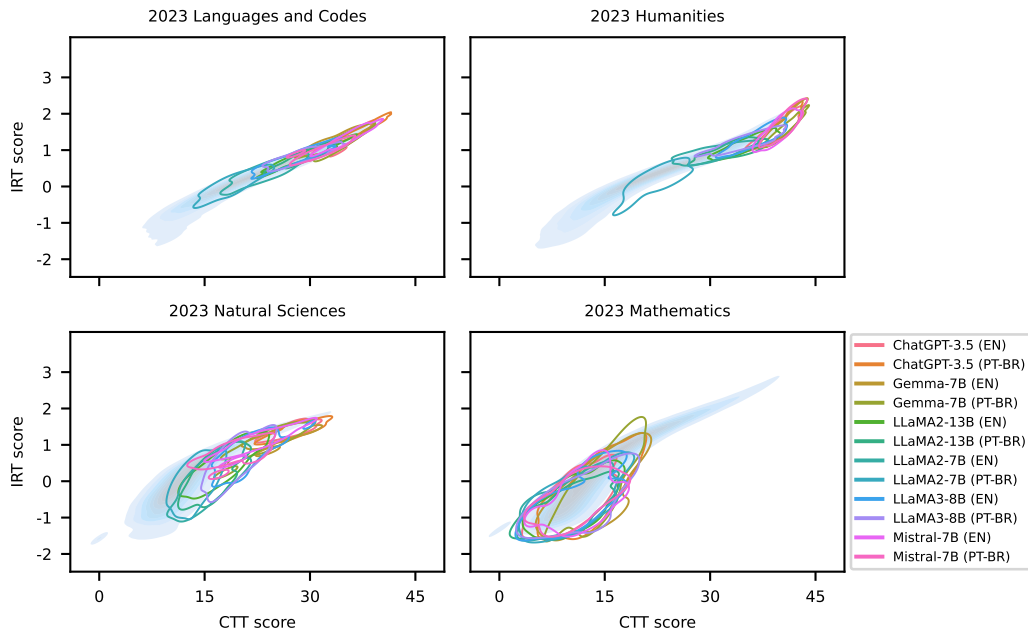


Figure 9: Distribution of CTT (accuracy) and IRT scores for humans and LLMs for the ENEM 2023 exam. LLMs are non-instructed tuned open source models and GPT3.5 with one-shot. LLM datapoints are computed from different shuffles.

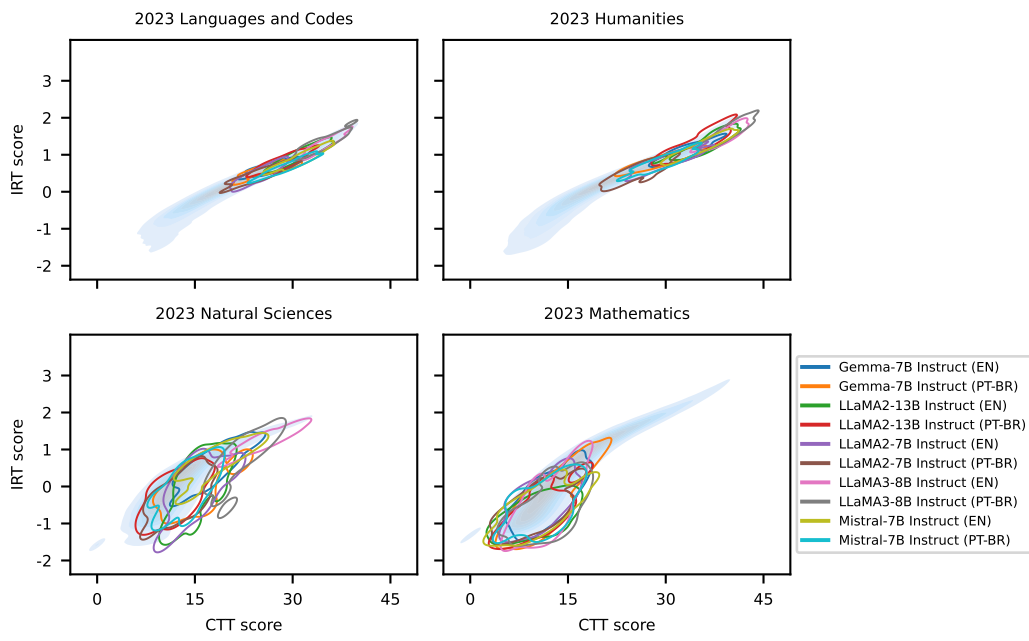


Figure 10: Distribution of CTT (accuracy) and IRT scores for humans and LLMs for the ENEM 2023 exam. LLMs are instructed tuned open source models with one-shot. LLM datapoints are computed from different shuffles.

1054 **A.6.2 Response Patterns**

1055 We show 43 items for the 2023 Math exam, instead of 45, because 2 items failed to converge and  
 1056 produce item parameters when the ENEM organizers fitted the human model.

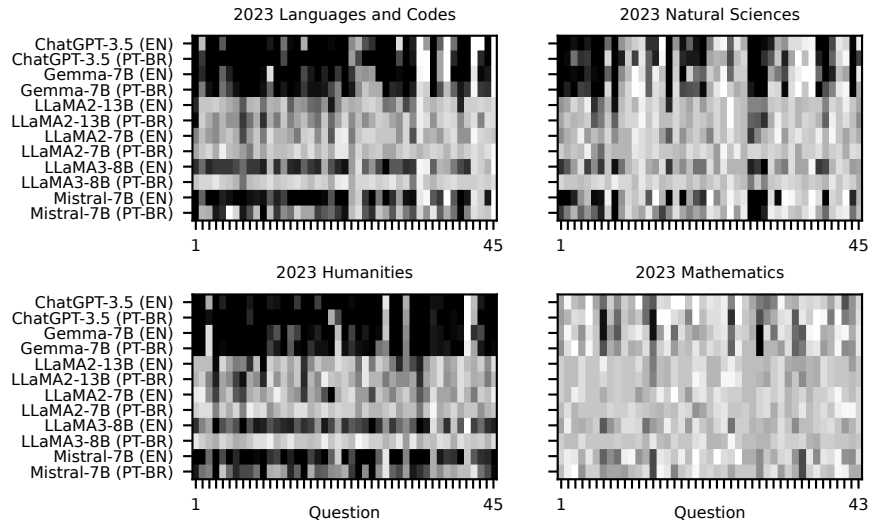


Figure 11: Response patterns for each LLM, where darker indicates more often correct. Questions are sorted by difficulty ( $\beta$  value). LLMs are non-instructed tuned open source models and GPT3.5 with zero-shot.

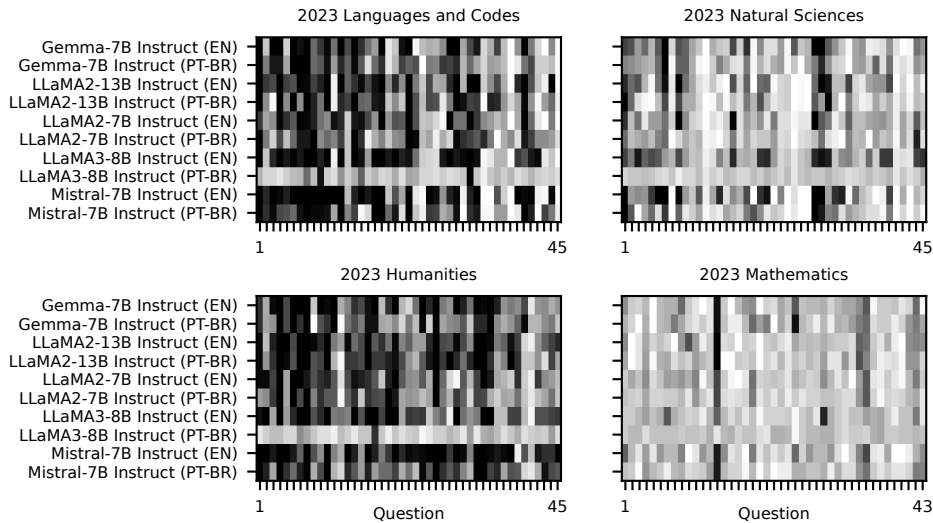


Figure 12: Response patterns for each LLM, where darker indicates more often correct. Questions are sorted by difficulty ( $\beta$  value). LLMs are instructed tuned open source models with zero-shot.

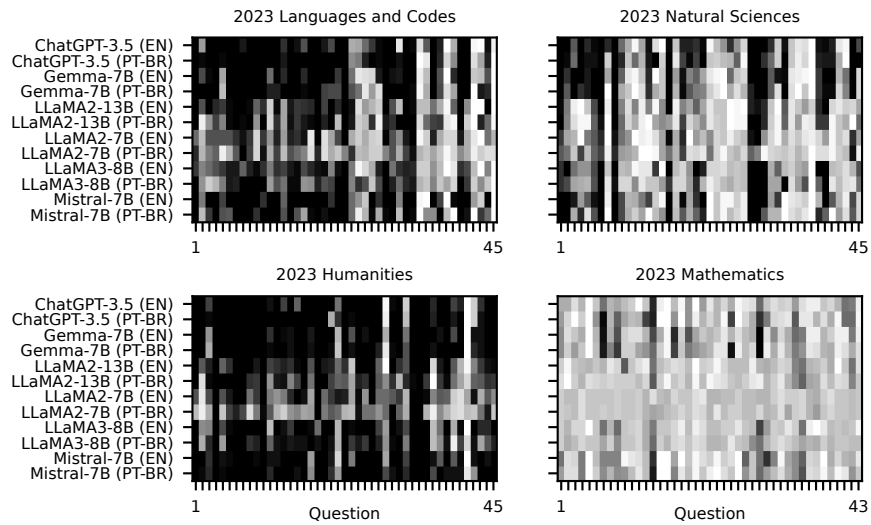


Figure 13: Response patterns for each LLM, where darker indicates more often correct. Questions are sorted by difficulty ( $\beta$  value). LLMs are non-instructed tuned open source models and GPT3.5 with one-shot.

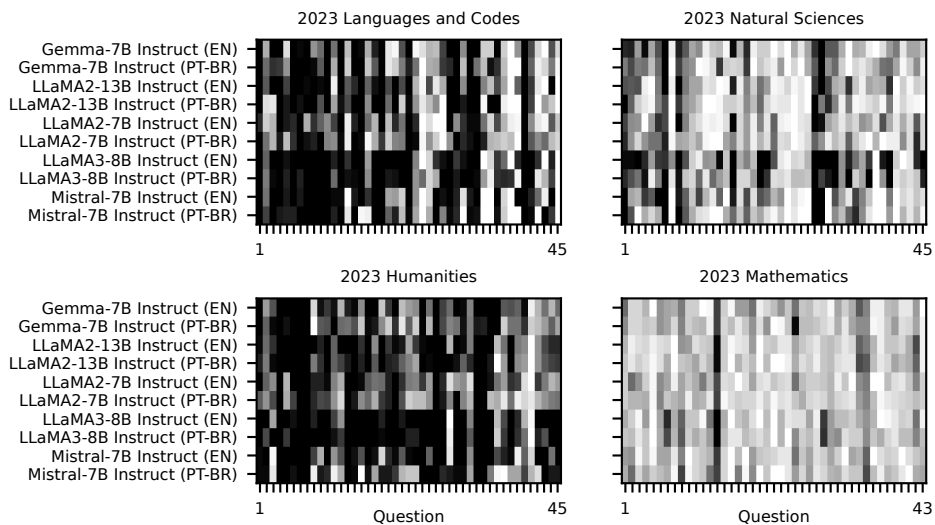


Figure 14: Response patterns for each LLM, where darker indicates more often correct. Questions are sorted by difficulty ( $\beta$  value). LLMs are instructed tuned open source models with one-shot.

1057 **A.6.3 Comparing IRT  $\theta$  and  $l_z$**

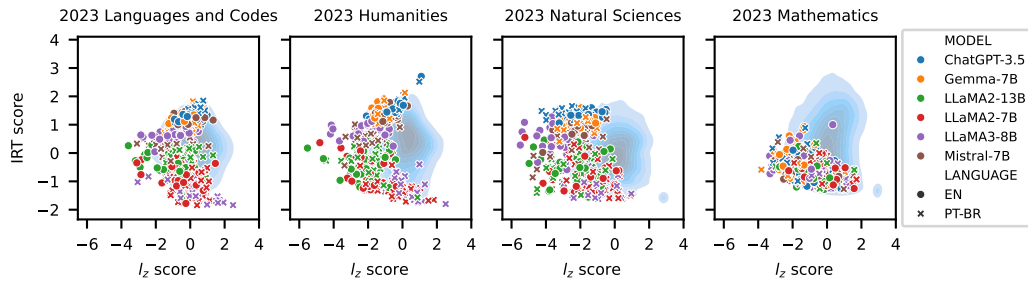


Figure 15: Distribution of  $l_z$  and IRT scores for humans and LLMs in the ENEM 2023 exam. LLMs are non-instructed tuned open source models and GPT3.5 with zero-shot. LLM datapoints are computed from different shuffles.

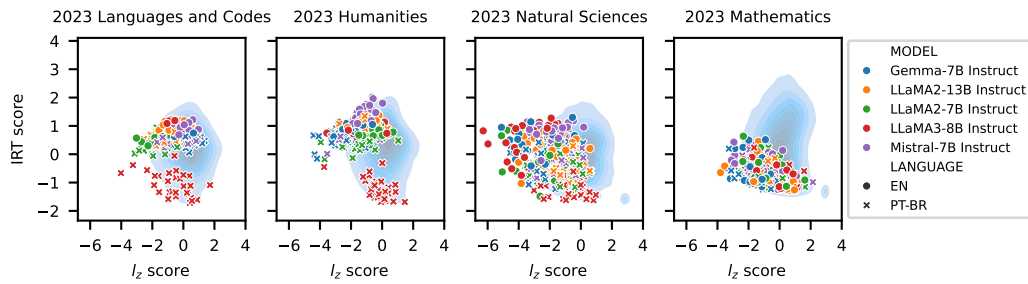


Figure 16: Distribution of  $l_z$  and IRT scores for humans and LLMs in the ENEM 2023 exam. LLMs are instructed tuned open source models with zero-shot. LLM datapoints are computed from different shuffles.

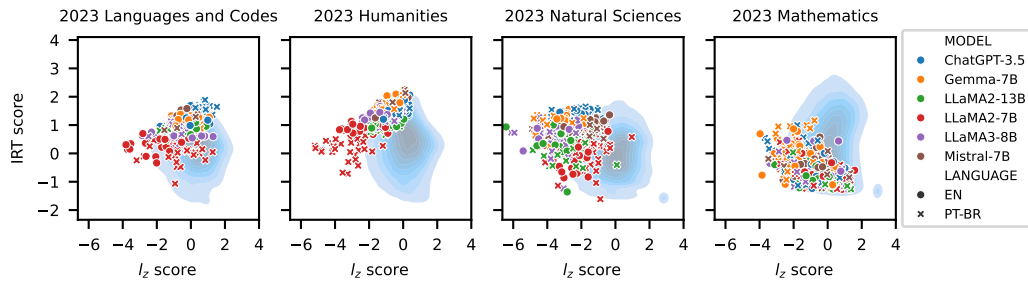


Figure 17: Distribution of  $l_z$  and IRT scores for humans and LLMs in the ENEM 2023 exam. LLMs are non-instructed tuned open source models and GPT3.5 with one-shot. LLM datapoints are computed from different shuffles.

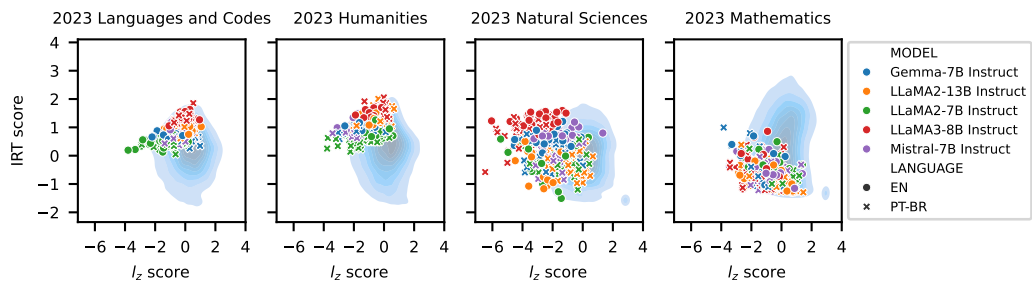


Figure 18: Distribution of  $l_z$  and IRT scores for humans and LLMs in the ENEM 2023 exam. LLMs are instructed tuned open source models with one-shot. LLM datapoints are computed from different shuffles.

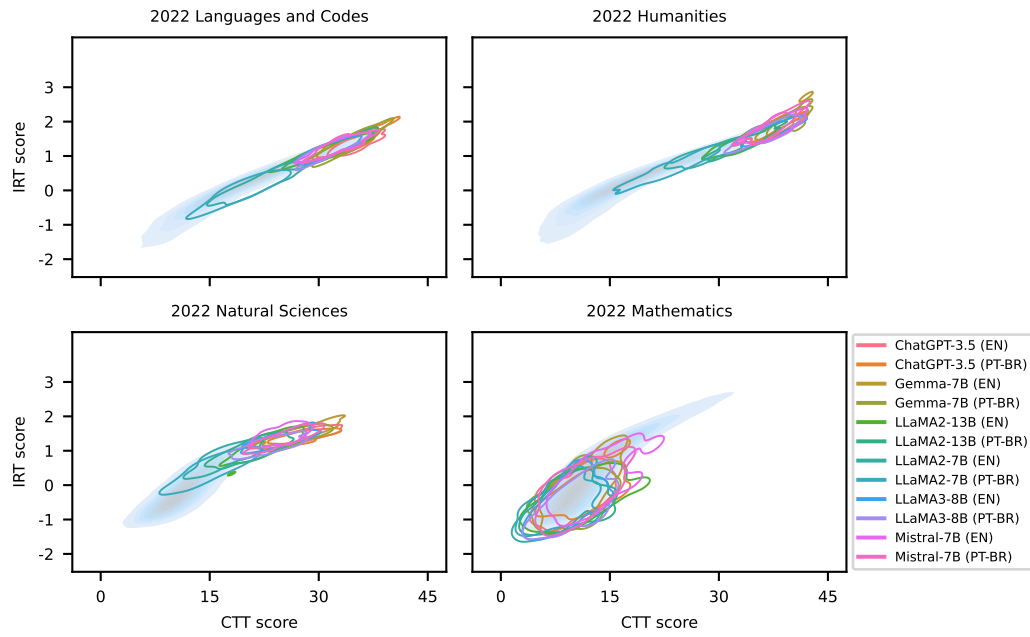


Figure 19: Distribution of CTT (accuracy) and IRT scores for humans and LLMs for the ENEM 2022 exam. LLMs are non-instructed tuned open source models and GPT3.5 with four-shot. LLM datapoints are computed from different shuffles.



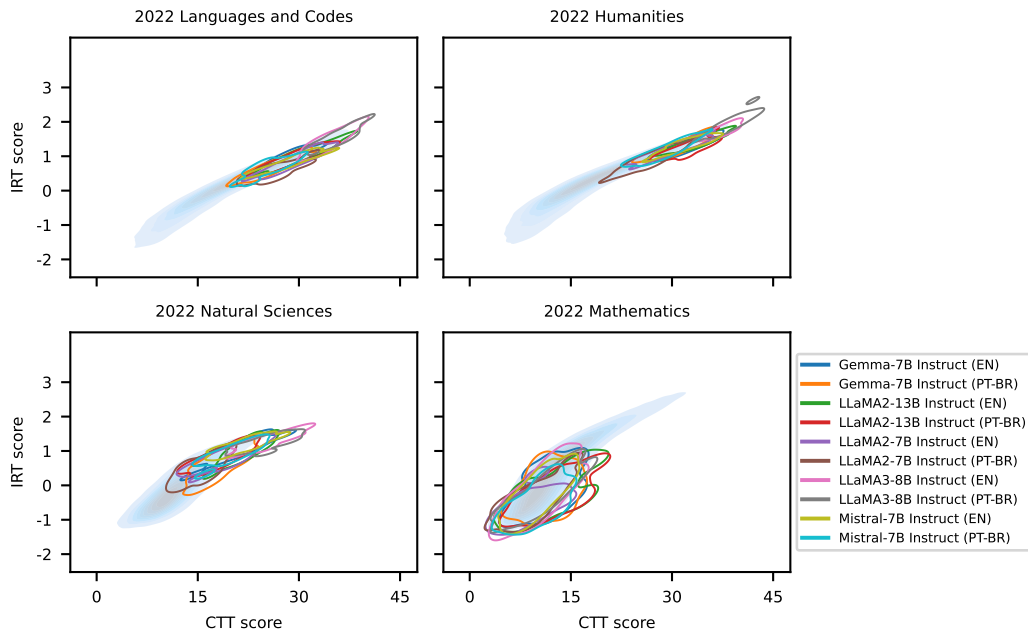


Figure 20: Distribution of CTT (accuracy) and IRT scores for humans and LLMs for the ENEM 2022 exam. LLMs are instructed tuned open source models with four-shot. LLM datapoints are computed from different shuffles.

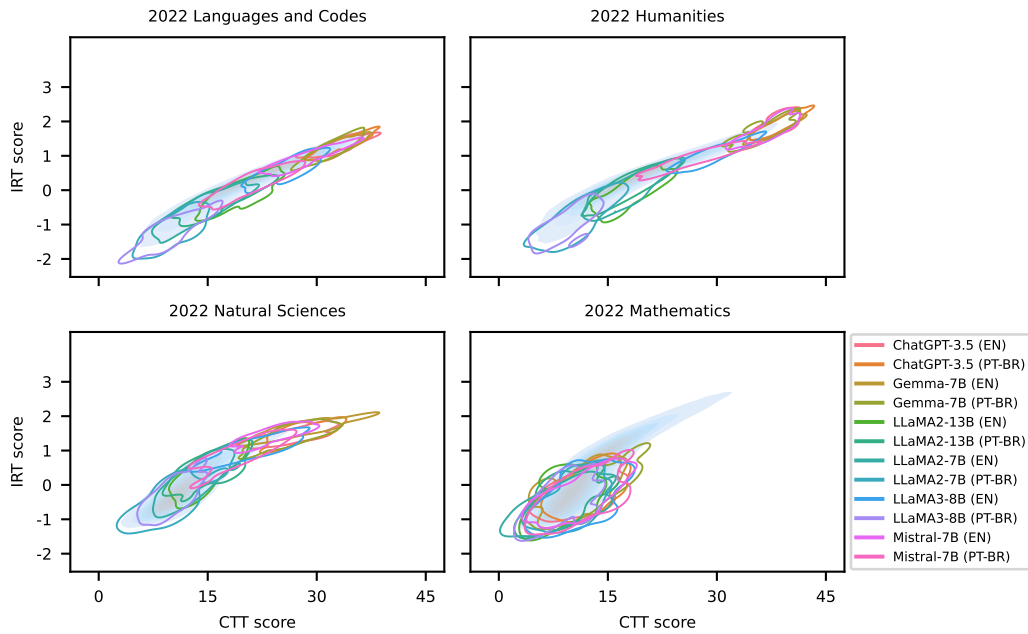


Figure 21: Distribution of CTT (accuracy) and IRT scores for humans and LLMs for the ENEM 2022 exam. LLMs are non-instructed tuned open source models and GPT3.5 with zero-shot. LLM datapoints are computed from different shuffles.

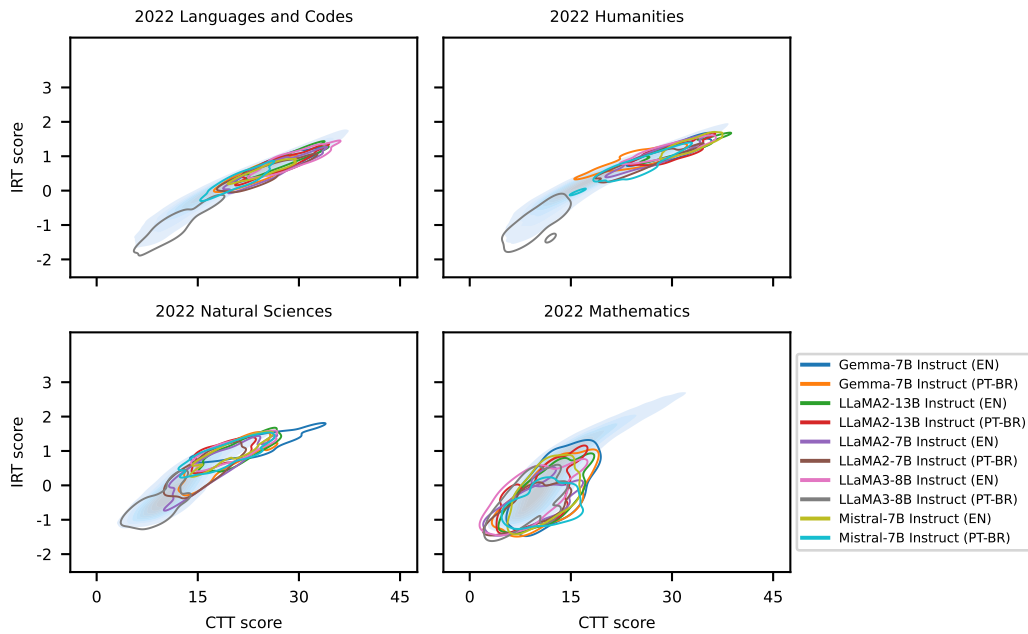


Figure 22: Distribution of CTT (accuracy) and IRT scores for humans and LLMs for the ENEM 2022 exam. LLMs are instructed tuned open source models with zero-shot. LLM datapoints are computed from different shuffles.

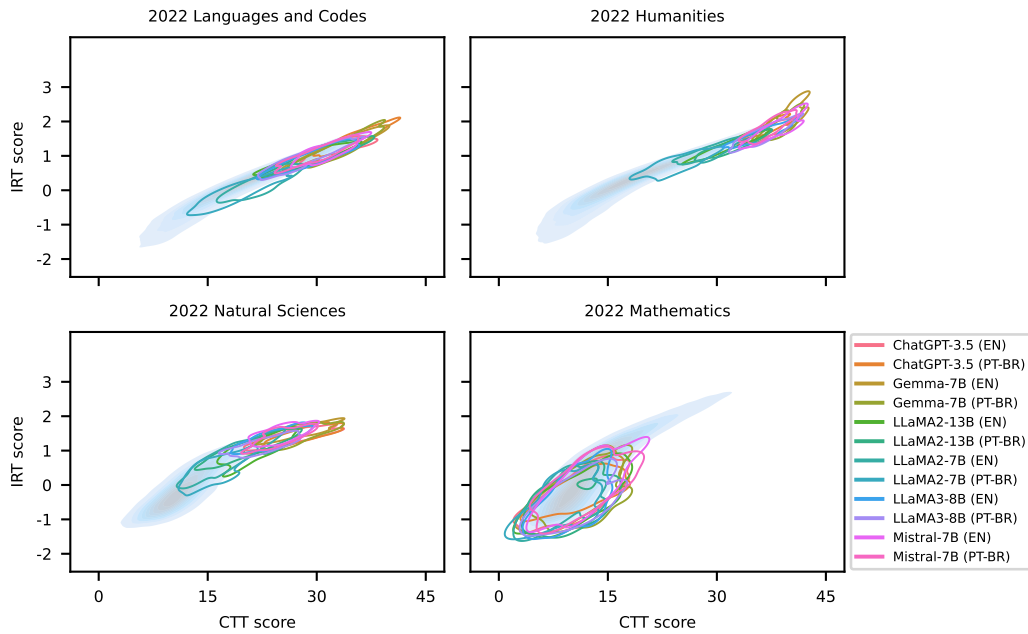


Figure 23: Distribution of CTT (accuracy) and IRT scores for humans and LLMs for the ENEM 2022 exam. LLMs are non-instructed tuned open source models and GPT3.5 with one-shot. LLM datapoints are computed from different shuffles.

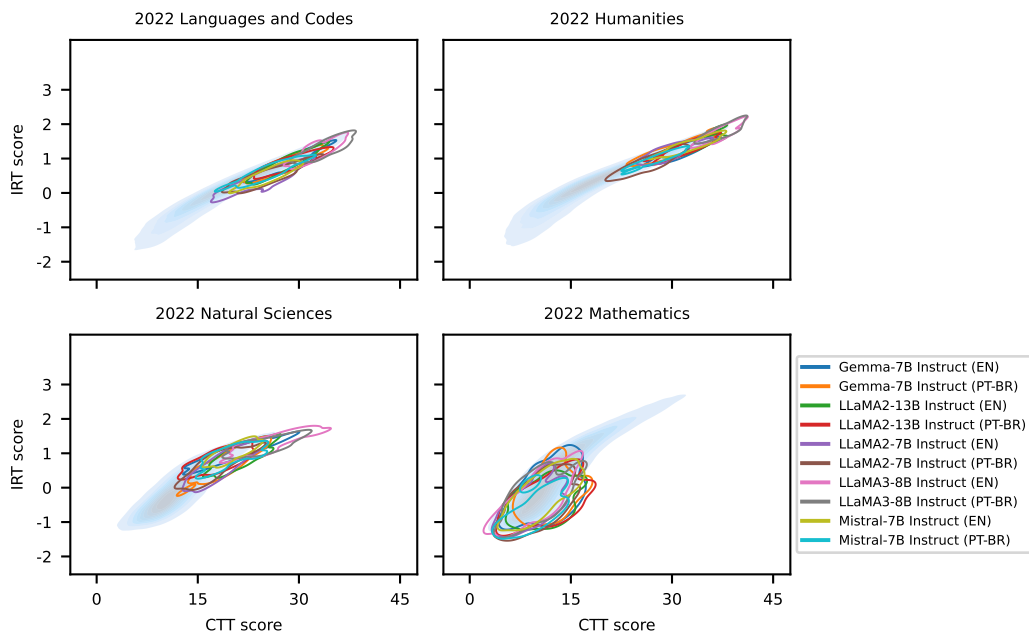


Figure 24: Distribution of CTT (accuracy) and IRT scores for humans and LLMs for the ENEM 2022 exam. LLMs are instructed tuned open source models with one-shot. LLM datapoints are computed from different shuffles.

1059 **A.8 Response Patterns for 2022**

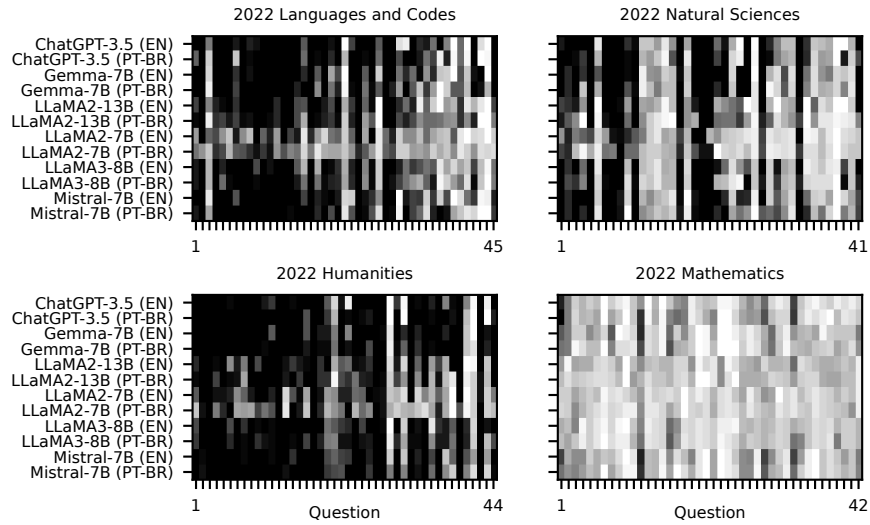


Figure 25: Response patterns for each LLM, where darker indicates more often correct. Questions are sorted by difficulty ( $\beta$  value). LLMs are non-instructed tuned open source models and GPT3.5 with four-shot.

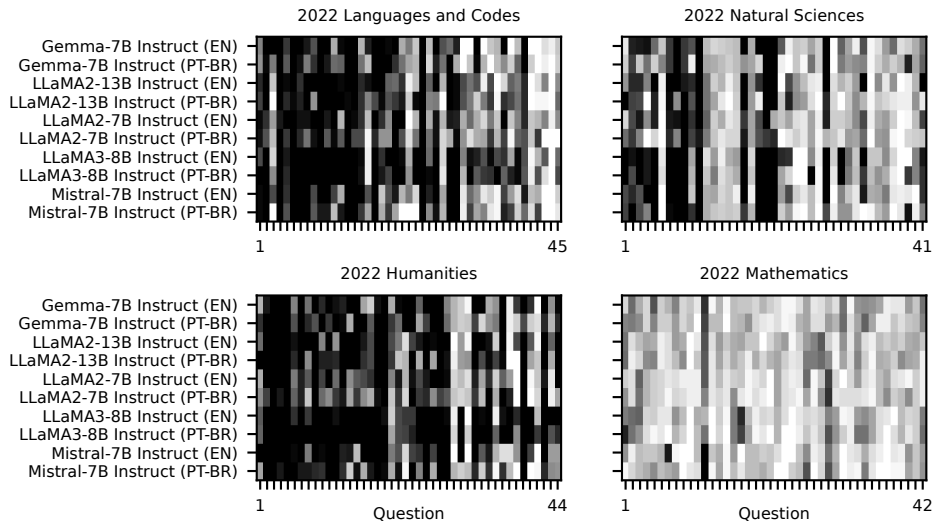


Figure 26: Response patterns for each LLM, where darker indicates more often correct. Questions are sorted by difficulty ( $\beta$  value). LLMs are instructed tuned open source models with four-shot.

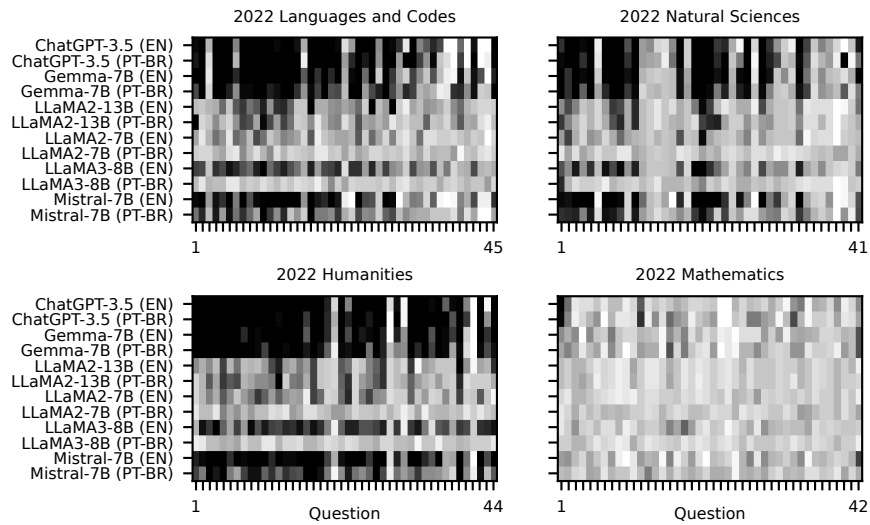


Figure 27: Response patterns for each LLM, where darker indicates more often correct. Questions are sorted by difficulty ( $\beta$  value). LLMs are non-instructed tuned open source models and GPT3.5 with zero-shot.

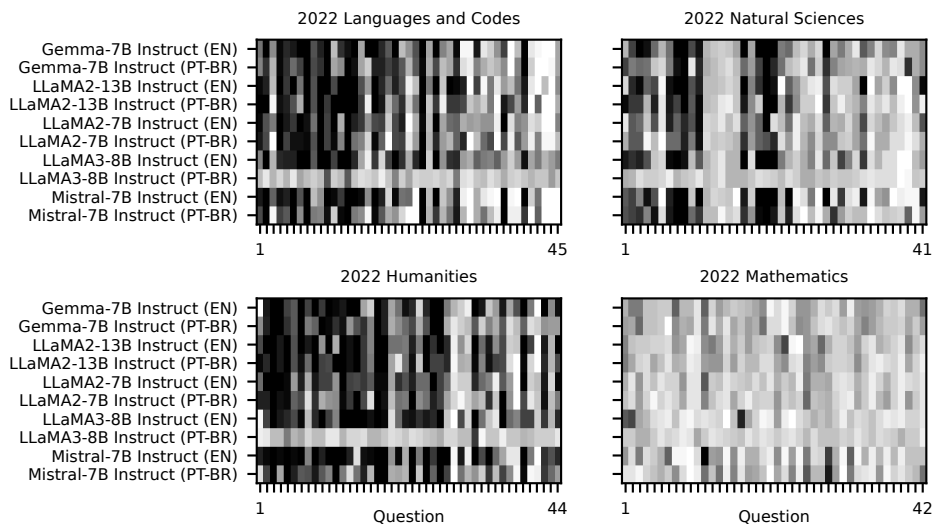


Figure 28: Response patterns for each LLM, where darker indicates more often correct. Questions are sorted by difficulty ( $\beta$  value). LLMs are instructed tuned open source models with zero-shot.

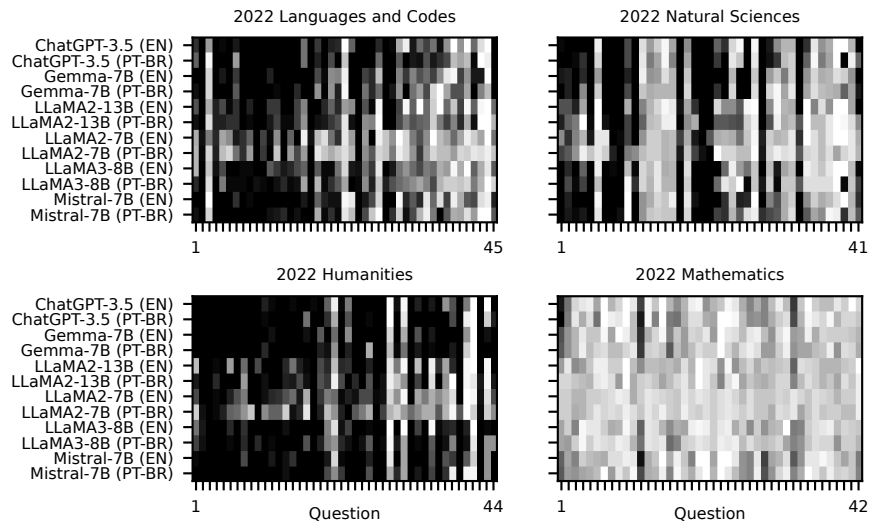


Figure 29: Response patterns for each LLM, where darker indicates more often correct. Questions are sorted by difficulty ( $\beta$  value). LLMs are non-instructed tuned open source models and GPT3.5 with one-shot.

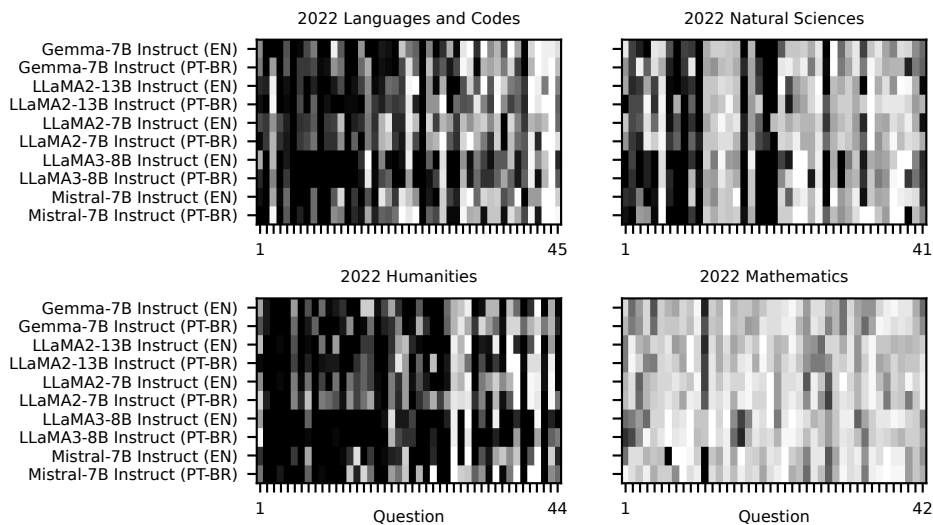


Figure 30: Response patterns for each LLM, where darker indicates more often correct. Questions are sorted by difficulty ( $\beta$  value). LLMs are instructed tuned open source models with one-shot.

1060 **A.9 Comparing IRT  $\theta$  and  $l_z$  for 2022**

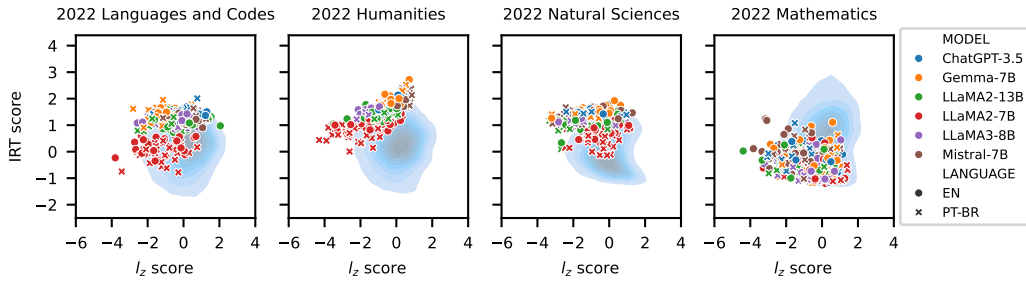


Figure 31: Distribution of  $l_z$  and IRT scores for humans and LLMs in the ENEM 2022 exam. LLMs are non-instructed tuned open source models and GPT3.5 with four-shot. LLM datapoints are computed from different shuffles.

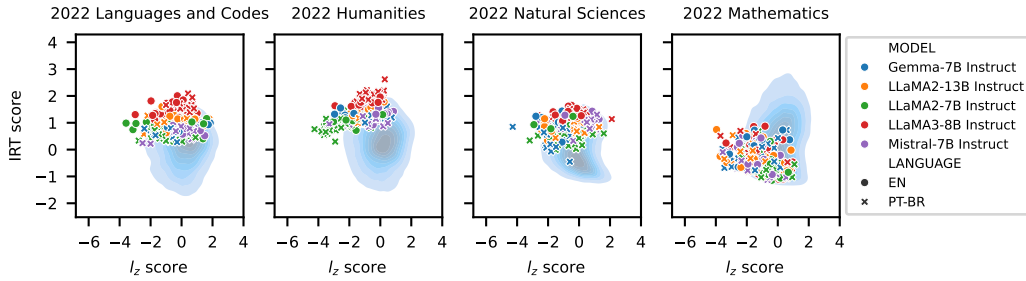


Figure 32: Distribution of  $l_z$  and IRT scores for humans and LLMs in the ENEM 2022 exam. LLMs are instructed tuned open source models with four-shot. LLM datapoints are computed from different shuffles.

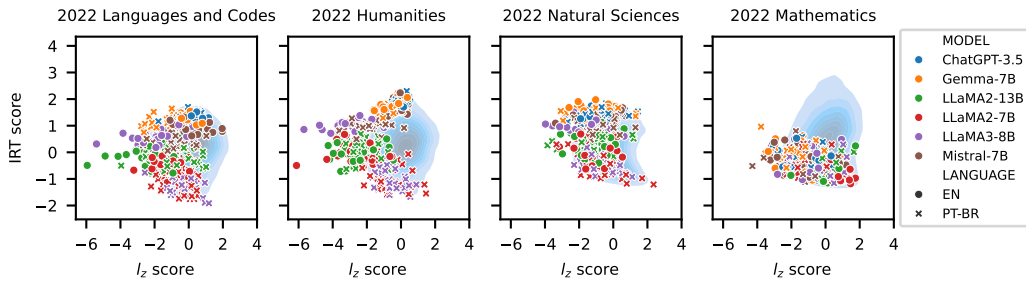


Figure 33: Distribution of  $l_z$  and IRT scores for humans and LLMs in the ENEM 2022 exam. LLMs are non-instructed tuned open source models and GPT3.5 with zero-shot. LLM datapoints are computed from different shuffles.

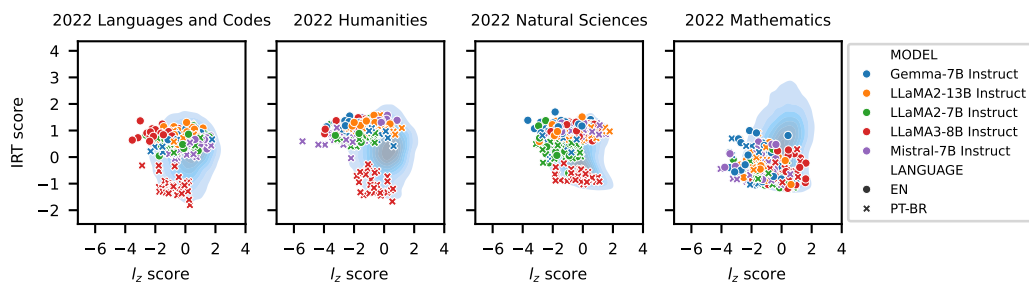


Figure 34: Distribution of  $l_z$  and IRT scores for humans and LLMs in the ENEM 2022 exam. LLMs are instructed tuned open source models with zero-shot. LLM datapoints are computed from different shuffles.

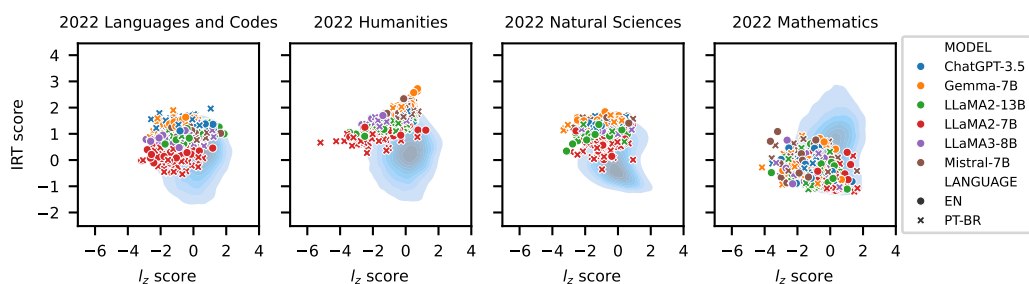


Figure 35: Distribution of  $l_z$  and IRT scores for humans and LLMs in the ENEM 2022 exam. LLMs are non-instructed tuned open source models and GPT3.5 with one-shot. LLM datapoints are computed from different shuffles.

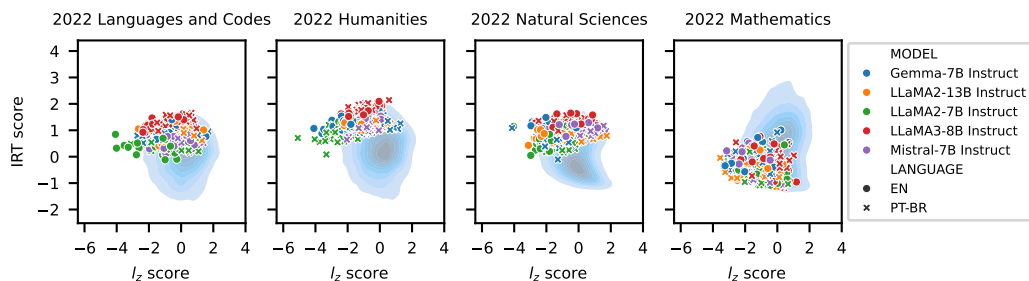


Figure 36: Distribution of  $l_z$  and IRT scores for humans and LLMs in the ENEM 2022 exam. LLMs are instructed tuned open source models with one-shot. LLM datapoints are computed from different shuffles.



1061 **A.10 Examples of non-discriminating and highly discriminating items for the 2023 Natural**  
1062 **Sciences exam.**

1063 **A.10.1 Poorly discriminative questions**

1064 **Question 107 (discrimination index -0.013)**

1065 Municipalities are responsible for managing their urban waste (garbage) cleaning and collection  
1066 according to the Federal Constitution. However, there are reports that part of this waste winds up in-  
1067 cinerated, releasing toxic substances into the environment and causing explosions-related accidents  
1068 when incinerating aerosol bottles (e.g., deodorants, insecticides, and repellents). The high tempera-  
1069 ture causes all the contents inside these bottles to vaporize, increasing the internal pressure until it  
1070 explodes.

1071 Suppose there is a metal aerosol bottle with a capacity of 100 milliliters containing 0.1 mol of  
1072 gaseous products at a temperature of 650 degrees Celsius at the moment of explosion.

1073 Consider:  $R = \frac{0.082 \times \text{liter} \times \text{atmosphere}}{\text{mol} \times \text{Kelvin}}$

1074 The pressure, in atmospheres, inside the flask at the moment of the explosion is closest to

- 1075 A. 756
- 1076 B. 533
- 1077 C. 76
- 1078 D. 53
- 1079 E. 13

1080 **Question 108 (discrimination index -0.076)**

1081 The circuit with three identical incandescent light bulbs, shown in the figure, consists of a mixed  
1082 association of resistors. Each bulb (L1, L2, and L3) is associated in parallel with a resistor of  
1083 resistance R, forming a set. These sets are connected in series, with all the bulbs having the same  
1084 brightness when connected to the power supply. After several days in use, only lamp L2 burns out,  
1085 while the others remain lit.

1086 Figure description: a power supply connected to three sets, arranged in series clockwise, in the  
1087 following sequence: the parallel set of L1 and R, the parallel set of L2 and R, and the parallel set of  
1088 L3 and R.

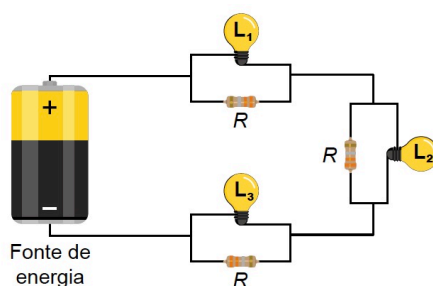


Figure 37: Question 108 Natural Sciences

1089 In the case where all the bulbs work, after L2 burns out, the brightness of the bulbs will be

- 1090 A. the same.
- 1091 B. more intense.
- 1092 C. less intense.
- 1093 D. less intense for L1 and the same for L3.
- 1094 E. more intense for L1 and less intense for L3.

1095 **Question 109 (discrimination index 0.013)**

1096 A company's transport safety team is evaluating the behavior of the tensions that appear in two  
1097 horizontal ropes, 1 and 2, used to secure a load of mass  $M$  equal to 200 kilograms to the truck,  
1098 as shown in the illustration. When the truck starts from rest, its acceleration is constant and equal  
1099 to 3 meters per second squared, while when it arbitrarily brakes, its braking is constant and equal  
1100 to 5 meters per second squared. In both situations, the load is about to move, and the direction of  
1101 the truck's movement is shown in the figure. The coefficient of static friction between the box and  
1102 the bottom surface of the body is 0.2. Consider the acceleration due to gravity to be 10 meters per  
1103 second squared, the initial tension in the ropes is zero, and the two ropes are ideal.

1104 Figure description: a truck traveling horizontally to the right (represented by the vector  $V$ ). A box  $M$   
1105 is resting on the central surface of its body. The box is attached to the rear of the body by horizontal  
1106 rope 1 and to the front by horizontal rope 2.

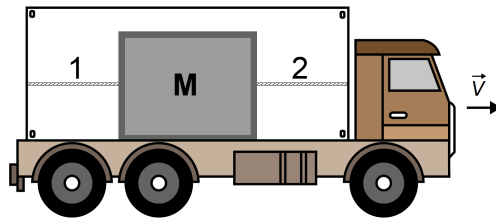


Figure 38: Question 109 Natural Sciences

1107 When the truck is accelerating and braking, the tensions in ropes 1 and 2 in Newton will be

- 1108 A. acceleration:  $T_1=0$  and  $T_2=200$ ; braking:  $T_1=600$  and  $T_2=0$ .  
1109 B. acceleration:  $T_1=0$  and  $T_2=200$ ; braking:  $T_1=1400$  and  $T_2=0$ .  
1110 C. acceleration:  $T_1=0$  and  $T_2=600$ ; braking:  $T_1=600$  and  $T_2=0$ .  
1111 D. acceleration:  $T_1=560$  and  $T_2=0$ ; braking:  $T_1=0$  and  $T_2=960$ .  
1112 E. acceleration:  $T_1=640$  and  $T_2=0$ ; braking:  $T_1=0$  and  $T_2=1040$ .

1113 **A.10.2 Highly discriminative questions**

1114 **Question 124 (discrimination index 0.650)**

1115 Update of the Portuguese Society of Neonatology's recommendation

1116 Glass containing aluminum is an excellent material for packaging medicines and supplements be-  
1117 cause heating can sterilize it. However, when the drug or supplement contains substances that bind  
1118 strongly to this metal's ion, the aluminum's dissolution is promoted by the displacement of the  
1119 chemical equilibrium established between the species immobilized in the glass and the species in  
1120 solution. For this reason, it is recommended that newborn nutrition supplements containing calcium  
1121 gluconate be packaged in plastic containers rather than in this type of glass.

1122 If this supplement is packaged in this type of glass, the risk of contamination by aluminum will be  
1123 greater if the

- 1124 A. glass of the bottle is translucent.
- 1125 B. concentration of calcium gluconate is high.
- 1126 C. glass bottle is thicker.
- 1127 D. glass is previously sterilized at high temperatures.
- 1128 E. reaction of aluminum with calcium gluconate is endothermic.

1129 **Question 91 (discrimination index 0.624)**

1130 It is a common requirement to turn off devices, such as cell phones, whose operation involves emit-  
1131 ting or receiving electromagnetic waves when traveling by plane. The justification for this procedure  
1132 is, among other things, the need to eliminate sources of electromagnetic signals that could interfere  
1133 with the pilots' radio communications with the control tower.

1134 This interference can only occur if the waves emitted by the cell phone and those received by the  
1135 plane's radio

- 1136 A. are both audible.
- 1137 B. have the same power.
- 1138 C. have the same frequency.
- 1139 D. have the same intensity.
- 1140 E. propagate at different speeds.

1141 **Question 130 (discrimination index 0.621)**

1142 The number of bees is in decline in various regions of the world, including Brazil, and multiple  
1143 factors are contributing to the collapse of their hives. In the United States, seed bombs of native  
1144 plant species have been used to combat the disappearance of these insects. They are small balls  
1145 filled with seeds, compost, and clay. When they are thrown and exposed to sun and rain, they  
1146 germinate even in poorly fertile soil.

1147 This method contributes to the preservation of bees because

- 1148 A. it reduces predation.
- 1149 B. it reduces the use of pesticides.
- 1150 C. it reduces competition for shelter.
- 1151 D. it increases the food supply.
- 1152 E. it increases breeding sites.

1153 **A.11 Description of Exams**

1154 The **Humanities** exam assesses understanding of geographical, cultural, and socioeconomic trans-  
1155 formations, as well as comprehension of social and political institutions, technological changes, and  
1156 the use of historical knowledge to promote conscious engagement in society. It requires recognizing  
1157 the interactions between society and nature in various historical and geographical contexts.

1158 The **Languages and Codes** exam assesses the use of communication in various contexts. This in-  
1159 cludes some knowledge and use of foreign languages, understanding of body language, analysis and  
1160 interpretation of expressive resources in different languages, comprehension of opinions in specific  
1161 languages, and understanding the impact of communication on personal and social life.

1162 The **Natural Sciences** exam assesses understanding of natural sciences and recognizing their roles  
1163 in production, economic and social development. It involves associating environmental degrada-  
1164 tion or conservation with productive and social processes, understanding the interactions between  
1165 organisms and the environment, and applying specific knowledge of physics, chemistry, and biology.

1166 The **Math** exam assesses the usage of geometric knowledge to represent reality, understanding no-  
1167 tions of magnitudes, measurements, and their variations for solving everyday problems, interpreting  
1168 information of scientific and social nature obtained from reading graphs and tables, and making  
1169 trend predictions, extrapolations, interpolations, and interpretations.

## 1170 **NeurIPS Paper Checklist**

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1172 Question: Do the main claims made in the abstract and introduction accurately reflect the  
1173 paper’s contributions and scope?

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1175 Justification: We show how IRT can be used to study LLM in comparison to humans  
1176 through multiple-metric propositions (Section 3) and their results and discussions (Sec-  
1177 tion 5).

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1192 of contamination correlation study in Appendix A.3, limitation of the dataset curation in  
1193 Appendix A.1

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1311 Evaluation scripts can be seen in our code.

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