Amalga: Designable Protein Backbone Generation with Folding and Inverse Folding Guidance

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Abstract

Recent advances in deep learning enable new approaches to protein design through 1 2 inverse folding and backbone generation. However, backbone generators may produce structures that inverse folding struggles to identify sequences for, indi-3 cating designability issues. We propose Amalga, an inference-time technique that 4 5 enhances designability of backbone generators. Amalga leverages folding and inverse folding models to guide backbone generation towards more designable 6 conformations by incorporating "folded-from-inverse-folded" (FIF) structures. 7 To generate FIF structures, possible sequences are predicted from step-wise pre-8 dictions in the reverse diffusion and further folded into new backbones. Being 9 intrinsically designable, the FIF structures guide the generated backbones to a more 10 designable distribution. Experiments on both de novo design and motif-scaffolding 11 demonstrate improved designability and diversity with Amalga on RFdiffusion. 12

13 **1 Introduction**

Rational protein design aims to create novel proteins or modify existing ones to obtain desired structures and functions. Accurate protein design methods enable direct applications such as enzyme engineering [10] and antibody-based drug design [15]. However, the vast combinatorial spaces of protein sequence and structure, along with their intricate interdependence, render this problem a longstanding challenge in biotechnology.

Fortunately, recent advances in deep learning illuminate new approaches to design proteins *de novo*. 19 Capitalizing on abundant sequence and structure data, inverse protein folding models [7, 4] have 20 succeeded in designing protein sequences that fold into specified target structures. Meanwhile, 21 inspired by the formidable successes of diffusion models in image generation [6, 11], diffusion-based 22 backbone generators [2, 13, 16, 17, 14] explore the prospects of generating novel protein backbone 23 structures. The integration of these two methods outlines a pipeline to design proteins: 1) sample 24 protein structures using backbone generators; 2) determine corresponding sequences with inverse 25 folding models; 3) screen the generated proteins based on *designability* - how well the generated 26 sequence folds into the accompanying structure; and 4) further screen the *designable* structures for 27 desired applications, based on both sequences and structures. 28

While existing backbone generation models, as exemplified by RFdiffusion [14], produce backbones with sensible local structures and appropriate proportions of stable secondary structures (helices and sheets), inverse folding models struggle to identify sequences for a sizable proportion of the generated backbones, even when human evaluation deeming them reasonable. Quantitatively, RFdiffusion benchmarking indicates approximately 30% of samples did not satisfy the designability criterion. We reckon this issue arises due to two possible factors: 1) current protein folding and inverse folding

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³⁵ models lack sufficient accuracy; 2) most existing backbone generation models are explicitly trained

to reproduce structures alone, without capturing the intricate sequence-structure relationship which
 essentially depicts designability. We aim to address the second factor in this paper.

Here we propose Amalga, a simple yet effective inference-time technique to enhance the designability 38 of diffusion-based backbone generators. By harnessing off-the-shelf folding and inverse folding 39 models, Amalga guides backbone generation towards more designable conformations. Specifically, 40 Amalga generates a set of "folded-from-inverse-folded" (FIF) structures by folding the sequences 41 which are inverse folded from step-wise predicted backbones. These FIF structures, being inherently 42 designable, are aligned to the predicted backbone and input into RFdiffusion's self-conditioning 43 channel. Intuitively, this encourages RFdiffusion to match the distribution of designable structures. 44 While retraining or finetuning RFdiffusion with FIF inputs may further improve performance, we 45 demonstrate that Amalga significantly boosts designability when applied solely during inference. 46

47 **2** Preliminaries

Diffusion-based Protein Backbone Generation. Recent works [1, 13, 17] have explored generating protein backbones using diffusion models such as denoising diffusion probabilistic model (DDPM) [6] and generative stochastic differential equations [12]. These generative models leverage forward and reverse diffusion processes to gradually transform samples from a simple prior distribution (often Gaussian) into complex backbone structures. The forward process perturbs the coordinates and orientations of each residue by adding noise with different scales on the timestep t. The reverse process then recovers high-quality backbones by iteratively predicting less noisy versions from the prior. Taking DDPM as an example, the forward and backward diffusion processes are formulated as:

$$q(x_t|x_{t-1}) = \mathcal{N}(x_t; \sqrt{1 - \beta_t x_{t-1}, \beta_t I}) \tag{1}$$

$$p_{\theta}(x_{t-1}|x_t) = \mathcal{N}(x_{t-1}; \mu_{\theta}(x_t, t), \Sigma_{\theta}(x_t, t)) \tag{2}$$

where $q(x_t|x_{t-1})$ perturbs x_{t-1} with Gaussian noise to obtain x_t , and p_{θ} predicts the reverse step result with neural networks based on the diffused sample x_t .

RFdiffusion. RFdiffusion [14] is a recent example of diffusion-based backbone generators. It finetunes RosseTTAFold [3], a multiple sequence alignment (MSA) based protein structure prediction model, with noised samples generated from the forward diffusion. Specifically, the structures of proteins to be designed are perturbed, and their corresponding sequences are masked. RFdiffusion also utilizes the original template channel in RosseTTAFold to input previously generated backbones through this channel to encourage the model to match the distribution of designable structures. **Designability Formulation**. Given a folding model *f* and an inverse folding model f^{-1} , the general

Designability Formulation. Given a folding model f and an inverse folding model f^{-1} , the general designability metric $\mathcal{D}(\mathbf{x})$ is defined as:

$$\mathcal{D}(\mathbf{x}) := \min_{\mathbf{s} \in \mathcal{S}} \|\mathbf{x} - f(\mathbf{s})\| \approx \|\mathbf{x} - f(f^{-1}(\mathbf{x}))\|$$
(3)

where *s* and x denote protein sequences and structures respectively, $\|\cdot\|$ quantifies the structural differences between two conformations (e.g. RMSD), and *S* represents the set of all feasible protein sequences. Conceptually, designability measures how accurately a structure x can be reproduced by its predicted sequence $f^{-1}(\mathbf{x})$ after folding, with lower values indicating higher designability. Notably, this metric depends on the accuracy of the folding and inverse folding models.

62 **3 Method**

Figure 1 illustrates the workflow of Amalga at each timestep t of the reverse diffusion process. We demonstrate Amalga on RFdiffusion, while the idea is broadly applicable to other baselines [17, 13]. The model takes as input the noised backbone \mathbf{x}_{t+1} from the forward process, the predicted backbone $\hat{\mathbf{x}}_{t+1}$, and the FIF samples $\{\tilde{\mathbf{x}}_{t+1}^i\}_{i=1}^{N_{\text{FIF}}}$ generated in the previous step to make new backbone $\hat{\mathbf{x}}_t$. This predicted backbone, together with \mathbf{x}_{t+1} , is used to compute the noised input for the next timestep via the reverse diffusion formula. Amalga then inverse folds the prediction $\hat{\mathbf{x}}_t$ using ESM-IF [7] to generate possible sequences $\{\mathbf{s}_t^i\}_{i=1}^{N_{\text{FIF}}}$. These sequences are then folded using ESMFold [9] to obtain new FIF backbones $\{\tilde{\mathbf{x}}_t^i\}_{i=1}^{N_{\text{FIF}}}$ to guide the next step. Note that $\hat{\mathbf{x}}_t$ is directly produced by the backbone



Figure 1: Amalga pipeline in each step. Amalga generates FIF samples from step-wise predicted backbones and inputs them to the model via the self-conditioning channel.

⁷¹ generator, thus assumed to have more reasonable structures and sensible inverse folding results, while

 \mathbf{x}_t is the intermediate result in the diffusion process, thus with discontinuities.

⁷³ In an attempt to further guide the model towards predicting foldable protein structures, we also ⁷⁴ explored providing the predicted sequences ($\{s_t^i\}$) as inputs to the sequence channel of RFdiffusion. ⁷⁵ As the sequence channel in the original RosseTTAFold architecture leveraged multiple sequence ⁷⁶ alignments (MSAs) to inform structural predictions, we hypothesized that explicitly providing these ⁷⁷ inverse-folded sequences could similarly enhance folding precision. However, as is shown in the next ⁷⁸ section, experiments inserting $\{s_t^i\}$ did not always result in improved performance. We believe the ⁷⁹ model likely requires a finetuning stage in order to integrate the sequences more properly.

In fact, the FIF samples directly inherit zero designability error, since their sequences are known to fold into the generated structures (up to the error of the folding model). As such, they are already successful design outcomes for unconstrained, *de novo* generation. However, these FIF structures may not conform to the motif constraints specified by the user. In contrast, the final output structure from the reverse diffusion process will explicitly satisfy the desired motifs, since they are fixed during this process. Therefore, Amalga balances global designability, provided by guiding the diffusion model with the FIF samples, and precise motif reconstruction in the final output.

87 4 Experiments

88 Settings. We conducted comparative experiments between the original RFdiffusion model and the 89 RFdiffusion model augmented with Amalga. We utilized ProteinMPNN [4] following RFdiffusion 90 for inverse folding, however, we replaced AlphaFold [8] with ESMFold to fold the final structures, 91 as ESMFold achieves superior performance when multiple sequence alignments are unavailable. 92 This replacement did not significantly altered the results, as we have analyzed in the appendix. For 93 Amalga, we tested settings with $N_{\text{FIF}} = 1, 5$. We reported results for two Amalga variants: one where 94 we input predicted sequences via the MSA channel (denoted "+seq"), and one where we did not. 95 We evaluated two backbone generation task schemes: 1) de novo design, in which backbones are

We evaluated two backbone generation task schemes: 1) de novo design, in which backbones are generated without external constraints, and 2) motif-scaffolding, in which backbones should contain a predefined motif with known sequence and structure. In the former task, we generated 20 structures of lengths 100, 150, 200, 250 and 300, respectively. In the latter task, we generated 100 structures for each of the 25 benchmark tasks in RFdiffusion. We use the root-mean-square deviation of self-consistency (scRMSD) and the in silico success rate to depict designability. The scRMSD measures the error between a generated structure and its closest foldable structure:

$$\operatorname{cRMSD}(\hat{\mathbf{x}}) = \min_{\boldsymbol{s} \in \mathcal{F}^{-1}(\hat{\mathbf{x}})} \operatorname{RMSD}(\hat{\mathbf{x}}, f(\boldsymbol{s}))$$
(4)

where $\mathcal{F}^{-1}(\hat{\mathbf{x}})$ denotes the set of 8 inverse-folded sequences of $\hat{\mathbf{x}}$. The in silico success criteria were adopted from RFdiffusion: for de novo design, an scRMSD below 2Å was required to be considered successful; for motif-scaffolding, an additional requirement was that the RMSD between the motif in the best design and the target motif be less than 1Å. We also report a metric of design diversity: all success backbones were clustered using MaxCluster [5] with a TM-score threshold of 0.5. The diversity was quantified as the number of the unique clusters in the generated success samples.

		% success	DE NOVO scRMSD	Diversity	Moti % success	F-SCAFFOLI scRMSD	DING Diversity
RFdiffusi	on	86.00	1.29	15.60	69.28	1.24	14.24
Amalga	$(N_{\rm FIF} = 1)$ $(N_{\rm FIF} = 1 + cog)$	86.00 87.00	1.58	16.00	73.20	1.05	14.88
	$(N_{\text{FIF}} \equiv 1, +\text{seq})$ $(N_{\text{FIF}} = 5)$	83.00	1.65	15.40	74.24 75.64	0.98	14.24 16.56
	$(N_{\rm FIF} = 5, + \text{seq})$	83.00	1.43	15.80	70.84	1.03	16.44

Table 1: Results of Amalga and the original RFdiffusion, averaged over all cases.



Figure 2: Success rate of 25 benchmark tasks in RFdiffusion. RFdiffusion (ref) in light blue displays statistics directly taken from [14], while RFdiffusion in dark blue shows reproduced statistics under our settings, comparable to Amalga. The columns are ranked by RFdiffusion performance.

Results. Table 1 shows metrics averaged on all 100 de novo generation samples and 2500 motif-101 scaffolding samples. Notably, results for motif-scaffolding are more informative, as in de novo 102 task the FIF samples are already samples with zero scRMSD. Overall, Amalga obtained superior 103 designability and diversity over RFdiffusion. Adding the sequence into the MSA channel (+seq) with 104 $N_{\rm FIF} = 1$ improves the performance, while the contradictory result holds with $N_{\rm FIF} = 5$. We posit 105 that the model needs further training to adapt to more inverse-folded sequences. We examine the 106 specific success rate of 25 motif-scaffolding tasks in Figure 2. Amalga consistently outperforms 107 RFdiffusion on the 25 benchmark cases with few exceptions. Notably, we observed significant 108 improvements in the RFdiffusion performance over the originally reported. We posit the current 109 release of RFdiffusion parameters have been refined since its publication. Results with regard to 110 motif RMSDs, etc. are available in the appendix. 111

Efficiency. We analyzed the running time of Amalga to quantify the introduced complexity of FIF computation. To generate one 100 amino acid protein, the running time on a 32GB NVIDIA V100 GPU increased from 1'00'' to 3'04'' with $N_{\text{FIF}} = 1$ and 5'12'' with $N_{\text{FIF}} = 5$. Overall, the introduced complexity is comparable to the original model's complexity.

116 5 Conclusion & Future Work

In this work, we have proposed Amalga as a broadly applicable inference-time technique to enhance 117 the designability of diffusion-based backbone generators exemplified by RFdiffusion. Our experi-118 ments demonstrate that Amalga successfully improves the designability and diversity of generated 119 structures from RFdiffusion, at the cost of additional inverse folding and folding computations. As 120 a direct path for improvement, an obvious next step is to fine-tune RFdiffusion to better adapt it 121 to Amalga inputs. Furthermore, inference speed could be enhanced by optimizing Amalga imple-122 mentation, such as enabling batched ESMFold inference. Since predicted backbones may not vary 123 drastically step-by-step, utilizing longer intervals between FIF evaluations leads to another gain of 124 efficiency. For more rigorous validation, pending experimental conditions, we hope to perform wet 125 lab experiments to further prove the effectiveness of Amalga designs. As ongoing work, we are also 126 actively exploring adaptations of this approach to other existing protein design baselines. 127

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187 A Implementation Details

Our work implements the open-source code of RFdiffusion ³. We use the default sampling settings from RFdiffusion, except where noted. The number of sampling steps is set to 50, and the C_{α} translation noise scalar is 1. For generating FIF samples, we leverage ESM-IF and ESMFold models ⁴ due to their state-of-the-art performance and efficiency. To evaluate generated sequences orthogonally, we follow the original RFdiffusion and use ProteinMPNN ⁵, replacing the protein folding model from AlphaFold with ESMFold for its superior single-sequence structure prediction.

194 B Effect of Folding Models

To examine whether the folding model used for evaluation impacts the final results, we generate 10
samples for each case and fold the same ProteinMPNN sequences with both ESMFold and Alphafold2.
Using the same designability criteria as described in Section 4, Fig. 3 shows that the choice of folding
model does not substantially influence the evaluation of designability.



Figure 3: Designability metrics between AlphaFold and ESMFold.

199 C RMSD Variation in Sampling

We plot the step-wise RMSD and motif RMSD between the backbone generator output $\hat{\mathbf{x}}_t$ and the FIF samples $\{\tilde{\mathbf{x}}_t^i\}$ during the denoising process on two motif-scaffolding cases. Notably, as $\hat{\mathbf{x}}_t$ maintains the target motif almost identically, the reported motif RMSD reflects the deviation between FIF samples and the target motif. As shown in Figure 4, both RMSDs decrease consistently following the reverse process.



Figure 4: Step-wise RMSDs between FIF samples and generated backbones.

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³https://github.com/RosettaCommons/RFdiffusion

⁴https://github.com/facebookresearch/esm

⁵https://github.com/dauparas/ProteinMPNN

2 Tate.	Diversity			45	10			5	5		5	33	20	S	5	16	72	49	23	37	17	ω		52	15	3
R succes	SR, %	100	100	5	75	100	90	61	83	91	98	66	91	49	5	16	91	85	63	66	98	95	96	<u>79</u>	69	53
	MRMSD	0.34 ± 0.06	0.34 ± 0.05	0.81 ± 1.04	0.84 ± 0.84	0.41 ± 0.03	0.64 ± 0.35	1.11 ± 0.65	0.77 ± 0.37	0.78 ± 0.32	0.55 ± 0.19	0.50 ± 0.19	0.70 ± 0.52	1.69 ± 1.44	3.75 ± 2.01	1.50 ± 1.08	0.65 ± 0.35	0.90 ± 1.19	1.58 ± 1.93	0.45 ± 0.18	0.45 ± 0.16	0.51 ± 0.23	0.50 ± 0.22	0.85 ± 0.52	0.90 ± 0.48	1.49 ± 1.38
	RMSD	0.41 ± 0.05	0.46 ± 0.12	0.79 ± 1.10	1.61 ± 1.92	0.40 ± 0.03	0.64 ± 0.47	1.17 ± 0.80	0.85 ± 0.39	0.82 ± 0.39	0.62 ± 0.22	0.60 ± 0.22	0.75 ± 0.86	1.91 ± 1.73	4.16 ± 1.89	1.61 ± 1.39	0.59 ± 0.18	0.84 ± 1.10	1.56 ± 1.90	0.47 ± 0.11	0.51 ± 0.18	0.58 ± 0.39	0.56 ± 0.23	0.67 ± 0.40	0.74 ± 0.35	1.28 ± 1.40
	Diversity	1	1	48	11	1	3	1	3	1	2	23	15	4	1	16	68	38	15	34	21	4	1	42	15	3
1	SR, %	100	100	5	99	100	85	51	99	90	87	96	92	47	3	29	91	78	56	98	67	95	94	<u> </u>	78	47
$\frac{N_{mn}}{N_{mn}}$	MRMSD	0.34 ± 0.07	0.34 ± 0.05	0.77±0.70	0.93 ± 0.84	0.41 ± 0.03	0.70 ± 0.39	1.13 ± 0.54	0.91 ± 0.43	0.78 ± 0.23	0.62±0.24	0.60 ± 0.31	0.83 ± 1.16	1.69 ± 1.49	4.20 ± 2.12	1.70 ± 1.41	0.72±0.78	0.96 ± 1.22	1.43 ± 1.42	0.44±0.17	0.47 ± 0.22	0.62 ± 1.31	0.53±0.32	1.03 ± 1.26	0.96 ± 0.91	1.43 ± 1.21
nhae miranini	RMSD	0.42 ± 0.06	0.46 ± 0.10	0.82 ± 0.87	1.83 ± 2.01	0.40 ± 0.04	0.75 ± 0.46	1.24 ± 0.86	1.02 ± 0.48	0.83 ± 0.32	0.69 ± 0.27	0.65 ± 0.26	0.87 ± 1.00	2.03 ± 1.91	4.33 ± 1.80	1.81 ± 1.55	0.64 ± 0.55	0.76 ± 0.63	1.52 ± 1.61	0.51 ± 0.20	0.52 ± 0.19	0.71 ± 1.42	0.60 ± 0.32	0.77 ± 0.75	0.82 ± 1.01	1.25 ± 1.17
	Diversity	-	-	47	14	-	5	1	4	-	7	20	17	4	-	12	64	34	16	33	20	4	-	42	12	2
	SR, %	100	100	5	63	100	<i>LL</i>	39	65	83	80	90	62	42		20	88	71	49	98	94	97	93	76	72	50
DEdiffue	MRMSD	0.36 ± 0.07	0.36 ± 0.05	1.03 ± 1.66	1.10 ± 0.87	0.48 ± 0.05	0.99 ± 1.44	1.33 ± 0.80	0.97 ± 0.45	0.86 ± 0.29	0.78 ± 0.32	0.72 ± 0.65	1.02 ± 1.49	1.92 ± 1.77	5.29±2.12	1.88 ± 1.02	0.84 ± 0.95	0.96±0.96	1.87 ± 1.87	0.45 ± 0.24	0.49 ± 0.24	0.49 ± 0.22	0.59 ± 0.29	0.95 ± 0.61	1.19 ± 1.50	1.58 ± 1.50
	RMSD	0.44 ± 0.07	0.48 ± 0.10	1.08 ± 1.53	2.07 ± 2.30	0.45 ± 0.05	1.16 ± 1.50	1.49 ± 1.23	1.22 ± 0.62	0.87 ± 0.29	0.85 ± 0.36	0.90 ± 1.31	1.09 ± 1.35	2.31 ± 2.12	5.37±1.94	1.99 ± 1.30	0.75 ± 0.75	0.99 ± 1.11	1.92 ± 2.00	0.54 ± 0.19	0.56 ± 0.22	0.56 ± 0.22	0.67 ± 0.30	0.76 ± 0.52	0.96 ± 1.27	1.44 ± 1.34
1 1000		1BCF	1 PRW	1QJG	1 YCR	2KL8	3IXT	4JHW	4ZYP	5IUS	5TPN	5TRV_long	5TRV_mid	5TRV_short	5WN9	5YUI	6E6R_long	6E6R_mid	6E6R_short	6EXZ_long	6EXZ_mid	6EXZ_short	6VW1	7MRX_long	7MRX_mid	7MRX_short

Table 2: Detailed results of 25 benchmark tasks without additional sequences. MRMSD refers to the motif RMSD and SR refers to the success rate.

refers to the success rate.		Diversity	1	1	45	11	1	1	9	5	1	4	36	19	4	3	15	71	42	13	37	19	2	1	50	22	4
	F seq	SR, %	100	100	2	61	100	100	056	86	95	94	80	88	48	5	0	85	86	53	98	<i>L</i> 6	19	98	99	62	32
	$N_{\rm FIF} = 5$ -	MRMSD	0.35 ± 0.07	0.35 ± 0.05	0.98 ± 1.40	1.04 ± 0.99	0.38±0.04	0.47 ± 0.12	0.89 ± 0.41	0.75 ± 0.41	0.65 ± 0.25	0.54 ± 0.32	0.56±0.42	0.63 ± 0.77	2.08 ± 2.07	3.17±1.64	1.18 ± 1.29	0.75±0.69	0.69 ± 0.56	1.83 ± 2.13	0.45 ± 0.25	0.49 ± 0.49	0.78 ± 0.60	0.47 ± 0.20	1.05 ± 0.77	1.07 ± 0.76	1.54±0.84
WSD and SF		RMSD	0.42 ± 0.07	0.45 ± 0.09	1.06 ± 1.64	2.06 ± 2.29	0.40 ± 0.05	0.50 ± 0.13	0.89 ± 0.46	0.80 ± 0.52	0.70 ± 0.34	0.62 ± 0.36	0.66 ± 0.61	0.64 ± 0.53	2.11 ± 2.10	3.80 ± 2.12	1.33 ± 1.57	0.76±0.79	0.68 ± 0.48	1.96 ± 2.81	0.51 ± 0.27	0.56 ± 0.47	1.03 ± 1.15	0.54 ± 0.22	0.97 ± 1.29	0.94 ± 1.04	1.45±0.98
o the motif I		Diversity	1	1	44	11	1	1	3	7	1	2	24	17	4	7	6	99	37	13	38	17	5	1	42	11	3
D refers to	+ seq	SR, %	100	100	4	99	100	66	64	73	92	88	97	90	51	4	4	89	89	54	66	95	92	96	80	78	52
nces. MRMSI	$N_{\rm FIF} = 1$ -	MRMSD	0.35 ± 0.08	0.33 ± 0.04	0.84 ± 0.84	0.97 ± 0.82	0.37 ± 0.04	0.53 ± 0.19	1.04 ± 0.60	0.83 ± 0.39	0.70 ± 0.26	0.64 ± 0.35	0.51 ± 0.22	0.75 ± 0.94	1.46 ± 1.26	3.92 ± 1.84	1.44 ± 0.86	0.79 ± 1.28	0.67 ± 0.46	1.83 ± 2.05	0.44 ± 0.16	0.49 ± 0.21	0.58 ± 0.33	0.48 ± 0.22	0.81 ± 0.40	0.87 ± 0.48	1.31±0.98
itional sequer		RMSD	0.43±0.07	0.43 ± 0.10	0.83±0.78	1.97 ± 2.17	0.38±0.04	0.56±0.22	1.16 ± 0.88	0.91±0.45	0.73±0.30	0.73 ± 0.34	0.61±0.27	0.80 ± 1.01	1.69 ± 1.44	4.21±1.83	1.49 ± 0.99	0.83 ± 1.95	0.62 ± 0.43	1.82 ± 2.03	0.52 ± 0.13	0.54 ± 0.19	0.70±0.59	0.55 ± 0.23	0.62 ± 0.18	0.69 ± 0.26	1.15±0.84
sks with add		Diversity		1	47	14		5		4		2	20	17	4		12	64	34	16	33	20	4	1	42	12	2
chmark ta	ion	SR, %	100	100	5	63	100	LL	39	65	83	80	90	62	42		20	88	71	49	98	94	97	93	76	72	50
ilts of 25 benc	RFdiffus	MRMSD	0.36 ± 0.07	0.36 ± 0.05	1.03 ± 1.66	1.10 ± 0.87	0.48 ± 0.05	0.99 ± 1.44	1.33 ± 0.80	0.97 ± 0.45	0.86 ± 0.29	0.78 ± 0.32	0.72 ± 0.65	1.02 ± 1.49	1.92 ± 1.77	5.29 ± 2.12	1.88 ± 1.02	0.84 ± 0.95	0.96±0.96	1.87 ± 1.87	0.45 ± 0.24	0.49 ± 0.24	0.49 ± 0.22	0.59 ± 0.29	0.95 ± 0.61	1.19 ± 1.50	1.58±1.50
Detailed resul		RMSD	0.44 ± 0.07	0.48 ± 0.10	1.08 ± 1.53	2.07 ± 2.30	0.45 ± 0.05	1.16 ± 1.50	1.49 ± 1.23	1.22 ± 0.62	0.87 ± 0.29	0.85 ± 0.36	0.90 ± 1.31	1.09 ± 1.35	2.31 ± 2.12	5.37±1.94	1.99 ± 1.30	0.75±0.75	0.99 ± 1.11	1.92 ± 2.00	0.54 ± 0.19	0.56 ± 0.22	0.56 ± 0.22	0.67 ± 0.30	0.76 ± 0.52	0.96 ± 1.27	1.44±1.34
Table 3:			1BCF	1 PRW	1QJG	1 YCR	2KL8	3IXT	4JHW	4ZYP	SIUS	5TPN	5TRV_long	5TRV_mid	5TRV_short	5WN9	5YUI	6E6R_long	6E6R_mid	6E6R_short	6EXZ_long	6EXZ_mid	6EXZ_short	6VW1	7MRX_long	7MRX_mid	7MRX_short

RMSD and SR refers to the succ	
) refers to the motif	
1 sequences. MRMSI	
with additiona	
enchmark tasks	
iled results of 25 b	
3: Deta	