CONTINUAL LEARNING VIA CONTINUAL WEIGHTED SPARSITY AND META-PLASTICITY SCHEDULING

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Abstract

Continual Learning (CL) is fundamentally challenged by the stability-plasticity dilemma: the trade-off between acquiring new information and maintaining past knowledge. To address the stability, many methods keep a replay buffer containing a small set of samples from prior tasks and employ parameter isolation strategies that allocate separate parameter subspaces for each task, reducing interference between tasks. To get more refined, task-specific groups, we adapt a dynamic sparse training technique and introduce a continual weight score function to guide the iterative pruning process over multiple rounds of training. We refer to this method as the continual weighted sparsity scheduler. Furthermore, with more incremental tasks introduced, the network inevitably becomes saturated, leading to a loss of plasticity, where the model's adaptability decreases due to dormant or saturated neurons. To mitigate this, we draw inspiration from biological meta-plasticity mechanisms, and develop a meta-plasticity scheduler to dynamically adjust these task-specific groups' learning rates based on the sensitive score function we designed, ensuring a balance between retaining old knowledge and acquiring new skills. The results of comparison on popular datasets demonstrate that our approach consistently outperforms existing state-of-the-art methods, confirming its effectiveness in managing the stability-plasticity trade-off.

1 INTRODUCTION

To navigate the complexities of real-world environments, an intelligent system must continuously learn, adapt, and apply knowledge over time (Parisi et al., 2019; Kudithipudi et al., 2022). This need has driven the study of continual learning (CL), where a typical setting is to learn a sequence of tasks incrementally while retaining performance on previous tasks, despite not having access to all tasks simultaneously. These tasks may involve acquiring new skills, revisiting previously learned ones, or adapting to different environments and contexts, each posing its own set of challenges (Hadsell et al., 2020; Wang et al., 2024a).

038 Unlike traditional machine learning models, which assume a static data distribution, CL involves learning from dynamic data distributions across a sequence of tasks. A key challenge in CL is the 040 stability-plasticity dilemma (Grossberg, 1987), which arises when balancing the need to acquire new 041 knowledge while preserving past knowledge. Stability is threatened when learning new tasks causes 042 the model to overwrite or degrade the representations learned from previous tasks, particularly at 043 task boundaries where shifts in data distribution are most pronounced (Robins, 1995; Buzzega et al., 044 2020). This can result in a sharp performance decline on older tasks, or in extreme cases, complete forgetting of previously acquired knowledge (Parisi et al., 2019). On the other hand, maintaining plasticity is crucial for adapting to new tasks and incorporating fresh information, but excessive 046 plasticity can erode previously learned skills. Achieving the right trade-off between stability and 047 plasticity is essential, yet remains a fundamental challenge for CL algorithms. 048

Existing CL algorithms typically retain a small buffer of samples from previous tasks during the training of new tasks, which helps mitigate the distribution shift and preserve stability by maintaining past knowledge (Verwimp et al., 2021; Bhat et al., 2022). Building on this common strategy, two
 primary approaches have been proposed to address the stability challenge: replay-based methods and parameter isolation methods. Replay-based methods optimize the use or selection of memory buffers, while parameter isolation methods allocate separate parameter subspaces for each task,



076 Figure 1: Our continual learning process is divided into two main steps: (1) using the continual 077 weighted sparsity scheduler to identify task-specific neuron groups, involving iteratively pruning neurons and connections, and (2) using the meta-plasticity scheduler to adjust learning rate for each 079 connection based on the sensitive score for each group. In the continual weighted sparsity scheduler, the depth of the purple color of neurons represents the activation value, with darker shades indicating 081 stronger activation. Neurons with lower activation values are pruned. Additionally, the width of 082 the orange connections represents the continual weighted score (CWS). Connections with lower 083 scores are pruned. In the meta-plasticity scheduler, each group has a different learning rate update 084 strategy based on its sensitive score. Ultimately, the entire model updates the learning rates for all 085 connections, stored in a learning rate matrix. Lighter colors indicate higher learning rates.

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088 reducing interference between tasks (Wang et al., 2024a). In this work, we mainly focus on the parameter isolation approaches. Previous work typically relies on a fixed pruning strategy for each 089 task, applying a one-time pruning with a predefined sparsity based on a score function (Mallya & 090 Lazebnik, 2018; Vijayan et al., 2023). To improve upon this, we propose the continual weighted 091 sparsity scheduler, inspired by recent dynamic sparse training techniques. Specifically, instead of 092 applying a single round of pruning, our method iteratively prunes the network with a gradually increasing sparsity over multiple rounds of training. This ensures that the most active neurons and 094 their corresponding connections, which are most relevant to the current task, are retained. The 095 iterative pruning process thus results in a more refined, task-specific neuron and connection group, 096 preserving knowledge more effectively.

Since the network capacity is limited, as more incremental tasks are introduced, the network will 098 eventually become saturated. Recent studies have demonstrated that neural networks may gradually 099 lose their capacity to learn from new experiences, a phenomenon referred to as the loss of plastic-100 ity, which is potentially caused by dormant or saturated neurons, further complicating the learning 101 process (Lyle et al., 2023; Sokar et al., 2023). To address this issue, we adopt a mechanism in-102 spired by biological systems known as *meta-plasticity* (Kudithipudi et al., 2022), which refers to 103 the phenomenon where the strength of individual synapses can be modulated by neural activity, 104 with the ease of synaptic strengthening or weakening varying over time. This is also described as 105 the "plasticity of plasticity", meaning that a synapse's capacity for change depends on its internal biochemical state. These states are influenced by the synapse's history of modifications and recent 106 neural activity, enabling fast learning and slow forgetting (Abraham & Bear, 1996; Abraham, 2008). 107 Building on this concept, we propose the *meta-plasticity scheduler*. After identifying task-specific

108 neuron and connection groups during training, we calculate a sensitivity score for each group by 109 measuring the average normalized magnitude difference across all connections between the two 110 most recent tasks. During subsequent model updates, the learning rate of each connection is dynam-111 ically adjusted based on the sensitive scores within these groups. Unlike previous approaches that 112 reset connections of dormant neurons through weight reinitialization, our method provides a more fine-grained, connection-level, and task-aware adjustment, allowing for a flexible and dynamic tun-113 ing of connections. By considering the influence of previously learned knowledge on the current 114 task, our approach ensures that the network maintains better plasticity in the CL setting, facilitating 115 both knowledge retention and adaptation to new tasks. 116

In summary, to address the stability-plasticity dilemma in CL, we propose a framework that integrates the continual weighted sparsity scheduler and the meta-plasticity scheduler. To validate our approach, we comprehensively compare it against state-of-the-art CL methods on popular datasets.
We also evaluate the stability and plasticity of our models over a long sequence of tasks, providing deeper insights into the effectiveness of our method. Comprehensive validation tests and analyses consistently demonstrate that our framework outperforms existing approaches, effectively addressing the stability-plasticity trade-off in CL.

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2 RELATED WORK

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127 **Approaches to address stability in CL.** To address stability in CL, various approaches aim to pre-128 vent or minimize this degradation, ensuring that the network retains knowledge from previous tasks 129 even as it learns new ones. One prevalent strategy involves storing a limited number of past training 130 samples in a small memory buffer (Ratcliff, 1990; Robins, 1995), similar to the experience replay 131 mechanism observed in the brain (Rasch & Born, 2007). Based on this consensus, researchers have developed two primary approaches to further tackle the stability issue: replay-based approaches and 132 parameter-isolation approaches. Replay-based approaches focus on optimizing both buffer construc-133 tion and buffer exploitation to make better use of the limited memory buffer, enhancing the retention 134 of past knowledge. GCR (Tiwari et al., 2022) introduces a selection mechanism that approximates 135 the gradients of previously seen data to update the buffer. DER++ (Buzzega et al., 2020) and CLS-136 ER (Arani et al., 2022) enhance consistency in predictions by using both soft targets and ground-137 truth labels. MRFA (Zheng et al., 2024) refines decision boundaries by augmenting the block-level 138 features of rehearsal samples across multiple layers. On the other hand, parameter-isolation ap-139 proaches have explored task-specific parameter isolation methods to further minimize interference 140 between tasks. For example, PackNet (Mallya & Lazebnik, 2018) and CLNP (Golkar et al., 2019) 141 leverage the over-parameterization of deep neural networks (DNNs) to accommodate multiple tasks 142 within a fixed model capacity. Similar to the brain, these models learn both connection strengths 143 and a sparse architecture for each task, effectively isolating task-specific parameters. More recently, TriRE (Vijayan et al., 2023) introduces a method for retaining the most prominent neurons while 144 promoting the activation of less active ones, and TPL (Lin et al., 2024) proposes a more principled 145 approach for task-ID prediction to enhance task isolation. Though effective, these methods typi-146 cally use a fixed pruning strategy with a predefined sparsity, leading to less accurate task-specific 147 sub-networks and reduced downstream performance. In contrast, our continual weighted sparsity 148 scheduler employs iterative pruning, progressively increasing the sparsity across multiple training 149 rounds. This gradually refines the network, preserving key neurons and connections. Experiments 150 show our method, as a novel parameter isolation technique, outperforms existing replay-based and 151 parameter isolation approaches in retaining task-specific knowledge, thus better addressing the sta-152 bility challenge in CL.

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154 Approaches to maintain plasticity in CL. To address the challenge of plasticity in CL, several 155 strategies have been proposed, most of which are based on reinitializing some or all of the net-156 work's weights during training. For instance, Zhou et al. (2021) suggest that selective forgetting 157 can enhance generalization, while Zhang et al. (2022) demonstrate that resetting different layers has 158 varying impacts on network performance. Additionally, Zhao et al. (2023) introduced a method 159 to fine-tune task-specific parameters on buffered data to improve plasticity. Refresh (Wang et al., 2024b) dynamically eliminates outdated or less relevant information by refreshing some of the old 160 task-specific weights from the CL model, thereby enhancing the retention of older knowledge while 161 efficiently acquiring information for new tasks. Unlike these previous approaches, we leverage the fundamental mechanism of meta-plasticity found in biological systems (Langille & Brown, 2018).
 Instead of directly reinitializing weights of the model, our meta-plasticity scheduler dynamically adjusts the ease with which neurons adapt, depending on their activity levels on recent tasks. This mechanism enables a more nuanced and adaptive regulation of neural plasticity, allowing for greater flexibility and precision in controlling how learning unfolds in the network.

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3 Methods

We begin by outlining the definitions and preliminaries of CL in Section 3.1, followed by an overview of our system in Section 3.2. We then introduce our proposed continual weighted sparsity scheduler in Section 3.3, and the meta-plasticity scheduler in Section 3.4.

3.1 PRELIMINARIES

177 CL is characterized by learning from dynamic data distributions. In practice, training samples of 178 different distributions arrive sequentially. A working model f_{θ} parameterized by θ needs to learn 179 corresponding task(s) with limited or no access to previous training samples and perform well on 180 their test sets. Formally, CL problems typically comprise $t \in \{1, 2, ..., T\}$ sequential tasks, with c classes per task, and data that appear incrementally over time. Each task has an associated task-181 specific data distribution: $(x_t, y_t) \in D_t$, where x_t is the input data, y_t is the data label, and t is 182 the task identity. The overall objective of CL is to maintain performance on previous datasets D_i 183 where $i \in \{1, 2, \dots, t-1\}$, while ensuring sufficiently good performance on the current dataset 184 D_t . In this work, we consider two well-known CL scenarios, class-incremental learning (Class-IL) 185 and task-incremental learning (Task-IL), both of which have disjoint label spaces across tasks. In 186 the former, task identities are provided only during training, whereas in the latter, task identities are 187 available during both training and testing.

Similar to common approaches, we maintain a memory buffer D_m to retain information from previous tasks. Considering the constraints of CL, the model does not have infinite storage for previous experience, and thus $|D_m| \ll |D_t|$. Given the current task data D_t and the memory buffer D_m , a combination of the task-wise loss \mathcal{L}_t and the experience replay-based loss \mathcal{L}_{rep} is commonly used during the training of the working model f_{θ} :

$$\begin{cases} \mathcal{L}_t = \mathbb{E}_{(x_i, y_i) \sim D_t} [\mathcal{L}_{ce}(f_\theta(x_i), y_i)] \\ \mathcal{L}_{rep} = \mathbb{E}_{(x_i, y_j) \sim D_m} [\mathcal{L}_{ce}(f_\theta(x_j), y_j)] \end{cases}$$
(1)

where \mathcal{L}_{ce} is the cross-entropy loss. \mathcal{L}_t focuses on the current task data D_t , primarily enhancing the model's plasticity, while \mathcal{L}_{rep} , derived from the memory buffer D_m , primarily enhances the model's stability.

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3.2 OVERVIEW OF OUR SYSTEM

As shown in Figure 1, our system contains two main steps that alternate continuously during the task training process: (1) filter out task-specific neuron groups that are highly active to the current task, and then integrate them into the existing neuron group pool; (2) update the meta-plasticity of all groups based on their sensitive scores.

Specifically, for a new task t, we perform multiple rounds of network pruning by gradually increasing target sparsity and iteratively pruning neurons and connections in the working model. This iterative pruning process refines a more task-specific group, preserving knowledge more effectively. The refined group is subsequently integrated into the existing pool of neuron groups.

Once the task-specific neuron groups are identified, we calculate the sensitive score for each group and adjust the learning rates of connections within those groups based on their scores. This adjustment either releases or suppresses the neuron update capacity, achieving an optimal balance between stability and plasticity. Finally, we employ reservoir sampling to update the replay buffer D_m and reinitialize the most dormant neurons for future tasks. The entire process is detailed in Algorithm 1.

216	Algorithm 1 Continual Learning via Continual Weighted Sparsit	y and Meta-Plasticity Scheduling.
217	Initialize: working model f_{θ} , data stream D, number of tasks '	T. target sparsity for each task ΔS .
218	total training steps for each task N .	, 8 1 3
219	$\mathcal{G} \leftarrow \{\}, D_m \leftarrow \{\}.$	
220	for all tasks $t \in \{1, 2, \dots, T\}$ do	
221	Retrieve task data D_t from D .	
222	for epochs $n \in \{1, 2, \dots, N\}$ do	
223	Update the target sparsity S_t^n using Equation 4.	▷ Sparsity scheduling
224	for a batch of data $\mathcal{B}_t \subset D_t$ and $\mathcal{B}_m \subset D_m$ do	
225	Update f_{θ} using Equation 1.	
226	end for	
227	Prune neurons in f_{θ} using Equation 5.	▷ Neuron selection
228	Drop and grow connections using Equation 6.	\triangleright Connection selection
229	end for	
230	Extract $g_t, \mathcal{G} \leftarrow \mathcal{G} \cup g_t$.	
231	Update groups' meta-plasticity using Equation 10.	▷ Meta-plasticity scheduling
201	Update D_m .	, i.e. E
232	Reinitialize input weights of dormant neurons based on Eq	uation 5.
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3.3 **CONTINUAL WEIGHTED SPARSITY SCHEDULER**

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237 To preserve task-specific information and address the stability challenge, we propose the continual 238 weighted sparsity scheduler, inspired by recent dynamic sparse training techniques, to enhance the 239 selection of parameters when performing parameter isolation in CL. Specifically, for the current 240 task t, we iteratively perform multiple rounds of network pruning. At the beginning of each pruning 241 round, we calculate the target sparsity which is raised from the previous round (Step 1). Next, we 242 utilize the activation score of neurons to perform neuron selection based on the target sparsity (Step 2a). Then, for the selected neurons, we apply our proposed *continual weighted score* (CWS) function 243 to further refine the selection of connections (Step 2b). The continual weighted sparsity scheduler 244 allows us to progressively obtain a network with increasing sparsity, ultimately reaching the pre-245 defined target sparsity. Throughout the rounds, information from task t is maximally preserved. 246

Step 1. Sparsity scheduling. For a new task t, we first calculate the available network sparsity that has not been allocated to previous tasks, denoted as S_{t-1} . Then, we assign a fixed sparsity ΔS to task t, resulting in the target sparsity $S_{t,N}$ after training the task for N epochs. 250

Denote the working model f_{θ} as a graph $g = (\mathcal{N}, \mathcal{E})$, where \mathcal{N} is the set of neurons in the model 251 and $\mathcal{E} \subseteq \mathcal{N} \times \mathcal{N}$ is the set of connections between the neurons. We aim to decompose q into T 252 task-specific sub-networks. For task t, the corresponding sub-network is denoted as $g_t = (\mathcal{N}_t, \mathcal{E}_t)$, 253 where $\mathcal{N}_t \subseteq \mathcal{N}$ and $\mathcal{E}_t \subseteq \mathcal{N}_t \times \mathcal{N}_t$. Then we have: 254

$$S_t = 1 - \frac{\left|\bigcup_{i=1}^t \mathcal{N}_i\right|}{\left|\mathcal{N}\right|},\tag{2}$$

with $S_0 = 100\%$. As mentioned above, each task is allocated a pre-defined sparsity ΔS , meaning 258 that $\frac{|\mathcal{N}_t|}{|\mathcal{N}|} = \Delta S$. It is important to note that S_t may not be equal to $1 - t \times \Delta S$ because there may be overlapping neurons and connections between these sub-networks. Here, we adopt an automated 260 gradual pruning algorithm (Zhu & Gupta, 2017) to achieve task-wise sparsity scheduling. We first set the target sparsity of the model after training total N epochs as: 262

$$S_{t,N} = \max(0, S_{t-1} - \Delta S).$$
 (3)

In our experiments, we set ΔS to 15%, as this level of sparsity has shown comparable performance 264 to that of a fully dense network (Han et al., 2015; Graesser et al., 2022). Then, during the multi-265 round training process of the task t, we use the following sparsity scheduling: 266

 $S_{t,n} = S_{t,N} - S_{t,N} (1 - \frac{n}{N})^3, \qquad n = 1, 2, \dots, N,$ (4)

where $S_{t,n}$ is the sparsity of f_{θ} after training *n* epochs. Next, we distribute the overall sparsity $S_{t,n}$ to the target sparsity $S_{t,n}^{(l)}$ for each layer l based on the number of neurons $d^{(l)}$ in each layer, guiding the selection of the most active neurons. We adopt the *Erdős-Rényi* method (Mocanu et al., 2018)
 here, and the sparsity distribution across layers is provided in more detail in Appendix B.1.

Step 2a. Neuron selection. Once we obtain $S_{t,n}^{(l)}$, we need to prune the layer by selecting essential neurons first. Let $a_i^{(l)}(x)$ denote the activation of neuron *i* in layer *l* under input *x* from a batch of training data $\mathcal{B}_t \subset D_t$. Then we define the activation score of a neuron *i* in layer *l* via the normalized average of its activation as follows:

$$\mathbf{A}_{i}^{(l)} = \frac{\mathbb{E}_{x \in \mathcal{B}_{t}} |a_{i}^{(l)}(x)|}{\sum_{k=0}^{d^{(l)}} \mathbb{E}_{x \in \mathcal{B}_{t}} |a_{k}^{(l)}(x)|}.$$
(5)

Neurons with high activation scores within the top $S_{t,n}^{(l)}$ will be selected. The neurons with the lowest activation score, which is referred to as the *most dormant neurons*, will be reinitialized after the current task has been trained (Line 16 in Algorithm 1).

Step 2b. Connection selection. After selecting the most active neurons, we select the most important connections between these neurons based on our continual weighted score (CWS) function, which extends the continual weight importance proposed by Wang et al. (2022b):

$$CWS(\omega) = \|\omega\|_1 + \alpha_1(\|\frac{\delta\hat{\mathcal{L}}_{ce}(D_t;\theta)}{\delta\omega}\|_1 + \|\frac{\delta\hat{\mathcal{L}}_{new}(D_t;\theta)}{\delta\omega}\|_1) + \alpha_2\|\frac{\delta\hat{\mathcal{L}}_{ce}(D_m;\theta)}{\delta\omega}\|_1, \quad (6)$$

where $\omega \in \theta$ is the weight, $\hat{\mathcal{L}}_{ce}(D_t; \theta)$ denotes the single-head form of the cross-entropy loss on 291 the current task data D_t , which only takes into account the classes relevant to the current task by 292 masking out the logits of other classes, $\mathcal{L}_{ce}(D_m;\theta)$ denotes the loss on the memory buffer data 293 D_m . Compared to Wang et al. (2022b), we introduce the task-aware term $\hat{\mathcal{L}}_{new}(D_t;\theta)$ to improve 294 the model's ability to recognize task boundaries, which is the cross-entropy loss for new/old task 295 distinction. The CWS ensures that we maintain: (1) weights of greater magnitude for output stability, 296 (2) weights significant for the current task for learning capacity, (3) weights significant for task 297 distinction and (4) weights significant for previous tasks to prevent catastrophic forgetting, with two 298 hyper-parameter α_1 and α_2 are used to regulate the weight of current and buffered data, respectively. 299 In this paper, we follow Wang et al. (2022b) and set $\alpha_1 = 0.5$ and $\alpha_2 = 1$. Apart from dropping 300 the most useless connections, we also grow the connections with the highest gradients on current 301 task $\|\frac{\delta \mathcal{L}_t}{\delta \omega}\|_1$ from the dropped connections. Newly grown connections are initialized to zero and, 302 therefore, do not affect the output of the network.

After iterative pruning of the neurons and connections, we obtain a group of neurons and connections g_t for task t. As T tasks are sequentially introduced, finally, we will get a set of groups of neurons and connections, denoted as $\mathcal{G} = \{g_1, g_2, \dots, g_T\}$.

307 308 3.4 META-PLASTICITY SCHEDULER

A common approach to achieving task isolation in CL is to freeze task-specific parameters once the task is completed (Mallya & Lazebnik, 2018; Vijayan et al., 2023). While this strategy helps preserve acquired knowledge, it limits the network's ability to adapt to new tasks and challenges. In contrast, biological systems utilize meta-plasticity, a mechanism where synapses dynamically adjust their capacity to change based on their modification history. This concept is crucial for enhancing a network's long-term learning potential and adaptability (Kudithipudi et al., 2022).

Inspired by that, we propose a neuro-level dynamic learning rate schedule strategy. Each neuron has an independent learning rate schedule strategy based on its sensitivity to recent activities. This approach suppresses overly active parts to reduce the forgetting of old knowledge while simultaneously identifying and revitalizing gradually rigid sections, thereby maintaining the ability to learn new information quickly.

Specifically, we first calculate the normalized magnitude difference of the weight for connection ebetween layer l and layer l + 1 after training two consecutive tasks, as follows:

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$$C_e = \frac{\|\omega_t^e - \omega_{t-1}^e\|_1}{\|W_t^{(l)} - W_{t-1}^{(l)}\|_1},\tag{7}$$

where $\omega_t^e \in \theta$ denotes the weight of the connection e learned after training on task t, and $W^{(l)} \in \theta$ is the weight matrix between layer l and layer l + 1.

Then we measure the sensitivity of all groups based on the average normalized magnitude difference across all connections within each group. Given a set of groups of neurons and connections \mathcal{G} from Section 3.3, we define a sensitive score SS_{g_t} for each group g_t :

$$SS_{g_t} = \frac{(1/|\mathcal{E}_t|) \sum_{e \in \mathcal{E}_t} C_e}{\sum_{k=1}^{|\mathcal{G}|} ((1/|\mathcal{E}_k|) \sum_{e \in \mathcal{E}_k} C_e)} \times |\mathcal{G}|,$$
(8)

where \mathcal{E}_t is the connections in the group g_t . The learning rates of connections within the group g_t are then updated as:

$$\ln_{g_t} \leftarrow \ln_{g_t} \times \lambda^{(1 - SS_{g_t})},\tag{9}$$

where $\lambda > 1$ is used to control the change magnitude of the learning rate. Based on the group update strategy, we have the update strategy for each connection to achieve meta-plasticity scheduling:

$$\ln_{e} \leftarrow \ln_{e} \times \prod_{\substack{g_{t} \in \mathcal{G}\\ e \in \mathcal{E}_{*}}} \lambda^{(1-\mathrm{SS}_{g_{t}})}.$$
(10)

Here, we consider groups with an SS < 1 to be relatively inactive, as their parameter variation is smaller than the average across all groups. For these groups, we increase their meta-plasticity, while for those with an SS > 1, we do the opposite. We also note that when $\lambda = 0$, it is equal to the strategy of freezing task-specific parameters.

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4 EXPERIMENTS

4.1 EXPERIMENTAL SETTINGS

Datasets. To evaluate the performance of our method in Class-IL and Task-IL scenarios, we follow standard image classification benchmarks in CL (Rebuffi et al., 2017; Wu et al., 2019) and employ three different datasets: CIFAR-10, CIFAR-100, and Tiny-ImageNet. Specifically, CIFAR-10 is divided into 5 disjoint tasks with 2 classes per task. CIFAR-100 is divided into 10 tasks with each containing 10 disjoint classes. Tiny-ImageNet consists of 200 classes, divided into 10 tasks with 20 classes per task. The statistics of the different datasets are provided in Appendix A.1.

Baselines. We extensively compare our method with representative and recent baselines, including replay-based approaches: ER (Chaudhry et al., 2019), DER++ (Buzzega et al., 2020), CLS-ER (Arani et al., 2022), ER-ACE (Caccia et al., 2021), Co²L (Cha et al., 2021), GCR (Tiwari et al., 2022), DRI (Wang et al., 2022a), Refresh (Wang et al., 2024b), MRFA (Zheng et al., 2024) and task-isolation approaches: TriRE (Vijayan et al., 2023), TPL (Lin et al., 2024). Additionally, as in previous CL works, we offer a lower bound baseline SGD, without any support, and an upper bound baseline Joint, where the CL model is trained using the full dataset.

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Metrics. Overall performance is primarily evaluated by average accuracy (AA). Let $a_{k,j} \in [0, 1]$ denote the classification accuracy evaluated on the test set of the *j*-th task after incremental learning of the *k*-th task ($j \le k$). AA is computed as $\frac{1}{T} \sum_{j=1}^{T} a_{T,j}$ after learning a total of *T* tasks. Additionally, following Sarfraz et al. (2022), we evaluate the model's stability, plasticity, and the trade-off between the two; the details of how these three metrics are calculated can be found in Appendix C.1. For each experiment, we fix the order of the classes and report the average AA and one standard deviation across all tasks over 5 runs with different initializations.

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4.2 EXPERIMENTAL RESULTS

Overall performance. As shown in Table 1, our method consistently outperforms the baselines
 across most datasets in both Class-IL and Task-IL settings. Notably, as the dataset complexity and
 the number of tasks increase from CIFAR-10 to Tiny-ImageNet, the performance gap between our
 method and the baselines grows considerably.

Mathada	CIFAR-10		CIFAR-100		Tiny-ImageNet	
Methous	Class-IL	Task-IL	Class-IL	Task-IL	Class-IL	Task-IL
SGD	19.62±0.05	61.02±3.33	17.49 ± 0.28	40.46 ± 0.99	7.92 ± 0.26	18.31 ± 0.68
Joint	92.20±0.15	$98.31{\scriptstyle\pm0.12}$	70.56 ± 0.28	86.19 ± 0.43	59.99±0.19	82.04 ± 0.10
ER	44.79±1.86	$91.19{\pm}0.94$	21.40 ± 0.22	61.36 ± 0.35	8.57 ± 0.04	38.17 ± 2.00
DER++	64.88±1.17	$91.92{\scriptstyle\pm0.60}$	29.60 ± 1.14	$62.49{\scriptstyle\pm1.02}$	10.96±1.17	40.87 ± 1.16
CLS-ER	61.88±2.43	$93.59{\scriptstyle \pm 0.87}$	43.38 ± 1.06	72.01 ± 0.97	17.68 ± 1.65	52.60 ± 1.56
ER-ACE	62.08±1.44	$92.20{\scriptstyle \pm 0.57}$	35.17±1.17	63.09 ± 1.23	11.25 ± 0.54	44.17 ± 1.02
Co^2L	65.57±1.37	$93.43{\scriptstyle \pm 0.78}$	31.90 ± 0.38	$55.02{\scriptstyle\pm0.36}$	13.88 ± 0.40	42.37 ± 0.74
GCR	64.84±1.63	$90.80{\scriptstyle \pm 1.05}$	33.69 ± 1.40	$64.24{\scriptstyle\pm0.83}$	13.05 ± 0.91	42.11 ± 1.01
DRI	65.16±1.13	$92.87{\scriptstyle\pm0.71}$	-	-	17.58 ± 1.24	44.28 ± 1.37
TriRE	68.17±0.33	$92.45{\scriptstyle\pm0.18}$	43.91 ± 0.18	71.66 ± 0.44	20.14 ± 0.19	$55.95{\scriptstyle \pm 0.78}$
TPL	70.06±0.47	$92.33{\scriptstyle \pm 0.32}$	36.90 ± 0.42	$76.53{\scriptstyle \pm 0.27}$	20.06±0.77	54.20 ± 0.51
Refresh	74.42 ± 0.82	$94.64{\scriptstyle \pm 0.38}$	38.49 ± 0.76	$77.71 {\pm} 0.85$	20.81±1.28	54.06 ± 0.79
MRFA	73.38 ± 0.54	$93.44{\scriptstyle \pm 0.16}$	37.23 ± 0.65	$75.83{\scriptstyle \pm 0.48}$	21.68 ± 0.55	$54.59{\scriptstyle\pm0.42}$
Ours	75.31±0.71	95.79 ±0.65	40.61±0.58	79.91±0.63	23.25 ±0.59	58.32±0.73
A B B B B B B B B B B B B B B B B B B B						Refresh MRFA Ours
				о .	Task ID	5 6 10

Table 1: Comparison of the overall performance of prior methods across various CL scenarios.

Figure 2: a. Stability-Plasticity trade-off for CL models trained on CIFAR-100 with 10 tasks. b.
Comparison of our method against other representative baselines in terms of Task-IL accuracy on the CIFAR-100 dataset divided into 10 tasks. We report the average accuracy of individual tasks in 5 runs with different seeds. The shaded area represents the error range determined by the maximum and minimum values.

Stability-Plasticity trade-off. We further analyze the trade-off between stability and plasticity achieved by our method, as well as the performance across all tasks after training, as shown in Figure 2. From Figure 2a, it is evident that our method demonstrates the best stability while maintaining near-optimal plasticity, which leads to the most favorable stability-plasticity trade-off. This explains why our approach achieves the best overall performance. Figure 2b provides additional insight, showing that our method significantly outperforms others on the earlier tasks. We believe this is due to the task isolation mechanism, which contributes to the superior stability of our method compared to others. However, when looking at the last four tasks, we observe a slight performance decline, especially on the final task, where the performance is not the best. This may explain why our plas-ticity is not the highest. We suspect this is due to the network gradually becoming saturated, leaving insufficient neurons available for learning new tasks. More results are provided in Appendix C.3.

Task isolation. To validate the effectiveness of task isolation in our method, we analyze the ex-tracted neuron groups, with the results from the last shortcut layer shown on the left of Figure 3. Each row represents the neuron group extracted for a specific task. From the first few rows, we can see that the neurons allocated to each task typically have no overlap, confirming the effectiveness of our approach in minimizing interference between tasks through parameter isolation. However, as the number of tasks increases and the network reaches saturation, neurons used by older tasks are gradually released. This results in some overlap between the neurons used for later tasks and those for earlier tasks, as seen in the lower rows. Despite this, the overlap between adjacent tasks remains well-controlled. While we aim for complete task separation, the overlap between neuron groups in



Figure 3: Left: Visualization of the neuron groups extracted for each task for the last shortcut layer when training on CIFAR-100 with 10 tasks. Each row from top to bottom represents a task, from task 1 to task 10. Right: Visualization of the feature vectors from the last convolutional layer using t-SNE, with different colors representing different tasks, and the colors match those in the left one.

rows suggests the similarity between tasks. We also visualize the features of task samples using t-SNE, as shown on the right side of Figure 3. The visualization reveals good separability between different tasks, though there is some overlap at the boundaries of certain tasks. For example, tasks 7 and 8, represented by the red and brown clusters, exhibit more overlap, which can also be observed in the left-side neuron visualization where these tasks share more neurons compared to others. We believe this overlap is due to inherent similarities between the tasks themselves.

Table 2: Comparison of the overall performance of prior methods with 20 tasks.

Methods	CIFAR-100	0 (20 Tasks)	Tiny-ImageNet (20 Tasks)		
Wiethous	Class-IL	Task-IL	Class-IL	Task-IL	
SGD	18.91 ± 0.34	45.31 ± 0.76	10.47 ± 0.47	23.22 ± 0.52	
Joint	74.12 ± 0.42	$89.81{\scriptstyle\pm0.58}$	66.37 ± 0.21	$86.94{\scriptstyle\pm0.23}$	
TriRE	38.29 ± 0.66	76.62 ± 0.37	27.41 ± 0.79	55.87 ± 0.44	
TPL	37.38 ± 0.94	77.64 ± 0.55	26.85 ± 0.86	$54.99{\scriptstyle \pm 0.75}$	
Refresh	39.53 ± 0.85	$79.81{\scriptstyle \pm 0.32}$	27.59 ± 0.64	55.52 ± 0.51	
MRFA	38.52 ± 0.63	$78.93{\scriptstyle \pm 0.72}$	27.72 ± 0.65	$56.82{\scriptstyle \pm 0.52}$	
Ours	41.69+0.57	82.46+0.61	30.53+0.66	59.82 +0.81	



Figure 4: Comparison of our method against other baselines on the CIFAR-100 dataset with 20 tasks. We report the average accuracy of individual tasks in 5 runs with different seeds. The shaded area represents the error range determined by the maximum and minimum values.

Performance on long sequences of tasks. As mentioned earlier, when the number of tasks increases, network saturation may occur, potentially affecting performance. To evaluate this, we conduct experiments on a longer task sequence, with the results shown in Table 2. Our method consistently outperforms all baselines in both Class-IL and Task-IL scenarios. We report the performance of all 20 tasks after training, as illustrated in Figure 4. Similar to the case with 10 tasks, our method demonstrates superior performance in preserving the accuracy of the earlier tasks. Fur-

thermore, it maintains relatively high accuracy and exhibits less fluctuation for newly added tasks compared to other methods. More results on Tiny-ImageNet can be found in Appendix C.3.

4.3 ABLATION STUDY

Continual weighted sparsity scheduler. To demonstrate the advantages of our approach, we compare our continual weighted sparsity scheduler with two baselines: (1) Static—a network trained with fixed sparsity from scratch, and (2) RigL (Evci et al., 2020)-the foundation of our method, which uses a dynamic sparse training approach that prunes connections based solely on the mag-nitude of weights, meaning that only the first term in Equation 6 is used to compute the continual weighted score. As shown in Table 3, the dynamic sparsity approach outperforms static sparse training, and our continual weighted sparsity scheduler yields even more promising results.

Table 3: Comparison of different sparse training methods across various CL scenarios with 10 tasks. We provide the average accuracy of all tasks after training.

Methods	CIFA	R-100	Tiny-Imag	
Wiethous	Class-IL	Task-IL	Class-IL	Task-IL
Static	37.45 ± 0.56	$76.39{\scriptstyle \pm 0.25}$	21.36 ± 0.41	54.28 ± 0.57
RigL	39.49 ± 0.81	$77.78{\scriptstyle \pm 0.42}$	22.54 ± 0.64	$56.75{\scriptstyle\pm0.55}$
Ours	40.61±0.58	79.91±0.63	$23.25{\scriptstyle\pm0.59}$	$58.32{\scriptstyle\pm0.73}$

Meta-plasticity scheduler. To validate the effectiveness of the meta-plasticity scheduler we introduce, we experiment with several different values for λ in Equation 10 to observe its impact on overall performance. When λ is set to 0, the corresponding parameters remain frozen, which is equivalent to a task-specific parameter freezing scheme. On the other hand, setting λ to 1 effectively disables the meta-plasticity scheduler, meaning it has no effect. As shown in Table 4, freezing taskspecific parameters proves to be effective, and the scheduler we introduce ($\lambda > 1$) further improves performance. The value of λ , as long as above 1, does not affect results much, while larger λ leads to slightly better performance on more challenging tasks. This may be because as λ increases, the meta-plasticity exhibits greater variability, making neurons more responsive to external inputs.

Table 4: The average accuracy for different λ in Equation 10 across various CL scenarios.

λ	CIFA	R-100	Tiny-ImageNet		
	Class-IL	Task-IL	Class-IL	Task-IL	
0	38.14±0.77	75.26 ± 0.45	21.81 ± 0.59	$54.84{\scriptstyle\pm0.84}$	
1	34.70 ± 0.35	$70.96{\scriptstyle \pm 0.65}$	17.20 ± 0.72	$49.68{\scriptstyle\pm0.30}$	
10	40.61±0.58	79.91±0.63	$23.25{\scriptstyle\pm0.59}$	$58.32{\scriptstyle\pm0.73}$	
20	40.42 ± 0.61	79.52 ± 0.49	$23.35{\scriptstyle\pm0.57}$	58.52 ± 0.44	
50	40.25 ± 0.42	$79.18{\scriptstyle \pm 0.36}$	23.44 ± 0.47	$58.71{\scriptstyle\pm0.32}$	
100	40.19 ± 0.35	$79.06{\scriptstyle \pm 0.42}$	$23.48{\scriptstyle\pm0.48}$	$58.77{\scriptstyle\pm0.71}$	

CONCLUSION

In this paper, we propose a framework that combines the continual weighted sparsity scheduler and the meta-plasticity scheduler to address the stability-plasticity trade-off in CL. The continual weighted sparsity scheduler iteratively prunes the network with progressively increasing sparsity over multiple rounds, leading to a more refined, task-specific group of neurons and connections, thereby preserving knowledge more effectively. Meanwhile, the meta-plasticity scheduler, inspired by biological meta-plasticity mechanisms, introduces connection-level and task-aware adjustments. This enables flexible, dynamic tuning of connections, supporting both knowledge retention and adaptation to new tasks. Experimental results demonstrate that our approach effectively balances stability and plasticity and outperforms other baselines. In the future, we aim to integrate dynamic network expansion into our framework to address challenges in real-world applications, which often involve a larger number of tasks, and potentially lack clear task boundaries.

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A DATASETS AND SETTINGS

We evaluate the effectiveness of our approach in two different types of CL scenarios: Class Incremental Learning (Class-IL) and Task Incremental Learning (Task-IL). In both settings, each task
introduces a set number of new classes for the model to learn. A CL model learns these tasks sequentially while maintaining the ability to distinguish between all previously encountered classes.
The key difference is that, in Task-IL, task labels are available during inference, making it a simpler
scenario compared to Class-IL, where no such labels are provided.

675 A.1 DATASET DETAILS

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677To evaluate the performance of our method in Task-IL and Class-IL scenarios, we employ three
different datasets: CIFAR-10, CIFAR-100, and Tiny-ImageNet. The CIFAR-10 dataset consists of
 $60,000\ 32\times32$ colored images in 10 classes, with 6000 images per class. There are 50,000 training
images and 10,000 test images. CIFAR-100 is just like the CIFAR-10, except it has 100 classes
containing 600 images each. There are 500 training images and 100 testing images per class. Tiny-
ImageNet contains 100,000 images of 200 classes (500 for each class) downsized to 64×64 colored
images. Each class has 500 training images, 50 validation images, and 50 test images.

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B ADDITIONAL DETAILS ABOUT OUR METHOD

B.1 LAYER-WISE SPARSITY DISTRIBUTION

Given a target sparsity $S_{t,n}$ for the model, a uniform sparsity distribution is commonly used by 688 setting the sparsity $S_{t,n}^{(l)}$ of each individual layer l equal to the total sparsity $S_{t,n}$. However, applying 689 690 the same level of sparsity to narrower layers may result in insufficient feature retention. To address 691 this, we adopt the Erdős-Rényi (ER) method (Mocanu et al., 2018), which distributes the sparsity $S_t^{n,l}$ of each layer proportional to the term $\frac{d^{(l-1)}+d^{(l)}}{d^{(l-1)}\times d^{(l)}}$, where $d^{(l)}$ and $d^{(l-1)}$ are the numbers of neurons in layers l and l-1, respectively. This method makes larger layers relatively more sparse 692 693 694 than smaller ones. In the ER method, the input and output layers are relatively denser because they usually have fewer incoming or outgoing connections. This allows the network to better utilize the observations and learned representations at the highest layers in the network. 696

8 B.2 Loss Function

The loss function we used to update the working model f_{θ} here is introduced by Liang & Li (2024), they decouple the \mathcal{L}_t in Equation 1 to two components:

$$\mathcal{L}_t = \mathbb{E}_{(x_i, y_i) \sim D_t} [\mathcal{L}_{ce}(f_\theta(x_i), y_i; t) + \mathcal{L}_n(f_\theta(x_i)))], \tag{11}$$

702 where $\mathcal{L}_{ce}(t)$ represents the loss on classes of the current task, and \mathcal{L}_n represents the loss of classifi-703 cation of new/old class. Then two hyper-parameters are introduced to control the weight of the two 704 different learning objectives: 705

$$\mathcal{L}'_t = \mathbb{E}_{(x_i, y_i) \sim D_t} [\beta_1 \mathcal{L}_{ce}(f_\theta(x_i), y_i; t) + \beta_2 \mathcal{L}_n(f_\theta(x_i))].$$
(12)

Here, we adopt the optimal parameter combination used in the experiments from Liang & Li (2024), with $\beta_1 = 1$ and $\beta_2 = 0.1$.

С ADDITIONAL EXPERIMENTS

713 C.1 STABILITY-PLASTICITY TRADE-OFF 714

715 A CL model is said to be stable if it can retain previously learned information, and plastic if it can 716 effectively acquire new information. Following Sarfraz et al. (2022), let $a_{k,j} \in [0,1]$ denote the 717 classification accuracy evaluated on the test set of the j-th task after incremental learning of the k-th task $(j \leq k)$. The stability is evaluated by calculating the average performance across all preceding 718 T-1 tasks as: 719

stability
$$= \frac{1}{T-1} \sum_{j=1}^{T-1} a_{T,j}.$$
 (13)

The models' plasticity can be accessed by computing the average performance of each task after its initial learning as:

$$plasticity = \frac{1}{T} \sum_{j=1}^{T} a_{j,j}.$$
(14)

Finally, the trade-off measure determines the optimal balance between the stability and the plasticity of the model. This measure is calculated as the harmonic mean of stability and plasticity:

$$\text{Trade-off} = \frac{2 \times \text{stability} \times \text{plasticity}}{\text{stability} + \text{plasticity}}.$$
(15)

C.2 IMPLEMENTATION DETAILS 735

We run all the experiments on an NVIDIA GeForce RTX-3090Ti GPU. Our implementations are based on Ubuntu Linux 20.04 with Python 3.8. Additionally, we use ResNet-50 as the feature extractor for all of our investigations. We use the Adam optimizer with a learning rate of 0.001 at the beginning to train the model, and we use a batch size of 32 and train the model for 50 epochs for 740 each task.

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C.3 ADDITIONAL EXPERIMENTAL RESULTS

744 **Stability-Plasticity trade-off.** We provide the trade-off between stability and plasticity achieved 745 by our method, as well as the performance across all tasks after training on the Tiny-ImageNet 746 with 10 tasks, with the results shown in Figure 5. Our method demonstrates the best stability while 747 maintaining plasticity, which leads to the most favorable stability-plasticity trade-off. This explains 748 why our approach achieves the best overall performance. Figure 5b provides additional insight, similar to the results in CIFAR-100 with 10 tasks. Our method significantly outperforms others on 749 the earlier tasks. 750

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752 **Performance on long sequences of tasks.** We provide the performance of all 20 tasks after train-753 ing on the Tiny-ImageNet, as illustrated in Figure 6 and the stability-plasticity trade-off evaluation in Figure 7. Our method demonstrates superior stability by preserving the accuracy of the earlier 754 tasks. Furthermore, it maintains relatively high accuracy and exhibits less fluctuation for newly 755 added tasks compared to other methods, highlighting its plasticity.



Figure 5: a. Stability-Plasticity trade-off for CL models trained on Tiny-ImageNet with 10 tasks. b.
Comparison of our method against other representative baselines in terms of Task-IL accuracy on
the Tiny-ImageNet divided into 10 tasks. The graph reports the average accuracy of individual tasks
at the end of CL training in 5 runs with different seeds. The shaded area represents the error range
determined by the maximum and minimum values.



Figure 6: Comparison of our method against other representative baselines in terms of Task-IL accuracy on the Tiny-ImageNet dataset divided into 20 tasks. The graph reports the average accuracy of individual tasks at the end of CL training in 5 runs with different seeds. The shaded area represents the error range determined by the maximum and minimum values.

Comparison on different task-wise sparsity. In the previous experiments, we allocated 15% of the neurons exclusively to each task, as this ratio was shown to be optimal according to the results from Graesser et al. (2022). To explore how this parameter affects performance, we conducted additional experiments comparing different task-specific sparsity ratios, as shown in Table 5. From the results, we observe that the performance for the 20% ratio is not as good as those for 15%. We believe that increasing the sparsity allocation may lead to more interference between tasks. On the other hand, when the ratio is set too small, there is a sharp decline in performance, which we attribute to the insufficient information retained by the selected neurons and connections.

Table 5: The average accuracy for different ΔS used in Equation 3

ΛS	CIFAR-100		Tiny-ImageNet	
ΔS	Class-IL	Task-IL	Class-IL	Task-IL
20%	40.18 ± 0.43	78.62 ± 0.44	22.59 ± 0.54	57.89 ± 0.57
15%	40.61±0.81	79.91±0.42	$23.25{\scriptstyle\pm0.64}$	$58.32{\scriptstyle \pm 0.55}$
10%	38.49 ± 0.53	76.22 ± 0.45	21.68 ± 0.77	$55.59{\scriptstyle\pm0.73}$
5%	37.22 ± 0.89	$72.94{\scriptstyle\pm1.01}$	21.66 ± 0.75	$52.91{\scriptstyle\pm0.91}$



Figure 7: Stability-Plasticity trade-off for CL models trained on Tiny-ImageNet with 20 tasks.

Comparison of different connection pruning methods. There are two commonly used strategies to select the most important connections: (1) magnitude-based and (2) fisher information-based. The idea behind magnitude pruning is that small valued weights impact the network's output less and can be safely pruned without significantly affecting performance. Fisher information-based pruning evaluates the importance of connections based on their contributions to the Fisher information matrix. Connections with low contributions, indicating less relevance or importance, are pruned or set to zero. Wang et al. (2022b) proposed continual weighted importance (CWI), which considers not only the importance of weights within the current task but also the possibility of it being crucial for other tasks. Here, we extend the CWI by introducing an additional item $\|\frac{\delta \mathcal{L}_{new}(D_t;\theta)}{\delta_{t+1}}\|_1$, which consider the capacity of distinguishing the task boundary for the $\hat{\mathcal{L}}_{new}$ represents the cross entropy loss for new/old class distinction. To validate the effectiveness of the CWS we proposed, we com-pare it against the other three methods, with the result reported in Table 6. It can be observed that our proposed CWS can help improve the overall performance. Additionally, the improvement in Task-IL is relatively smaller compared to Class-IL, as the extension of CWI primarily enhances the model's ability to recognize task boundaries, a feature that is more crucial in the Class-IL setting.

Table 6: Comparison of the effect of various connection pruning methods used in Section 3.3 ondifferent datasets.

Method	CIFA	R-100	Tiny-ImageNet	
Wiethou	Class-IL	Task-IL	Class-IL	Task-IL
Magnitude	38.89 ± 0.71	77.29 ± 0.73	22.48 ± 0.79	$56.69{\scriptstyle\pm0.50}$
Fisher-information	37.26 ± 0.45	$74.05{\scriptstyle\pm0.51}$	21.54 ± 0.81	$54.31{\scriptstyle\pm0.78}$
CWI	$39.88{\scriptstyle\pm0.82}$	$79.45{\scriptstyle \pm 0.83}$	22.86 ± 0.68	58.13 ± 0.56
Ours	$40.61{\scriptstyle \pm 0.58}$	$79.91{\scriptstyle\pm0.63}$	$23.25{\scriptstyle\pm0.59}$	$58.32{\scriptstyle\pm0.73}$

Task-wise and step-wise sparsity scheduling. We provide the visualization of the target and real sparsity of the working model f_{θ} during training on CIFAR-100 with 10 tasks in Figure 8. As tasks are sequentially introduced, the total sparsity of the network gradually decreases while the sparsity gradually increases during the training process for each task. Furthermore, the real sparsity of the network at the end of each task does not match the target sparsity, due to some overlap between task-specific neuron groups.

Sparsity scheduling frequency. During the training process for each task, we now do the sparsity scheduling for each training epoch, which may be time-consuming and computing-consuming. A typical solution is to update the sparsity periodically. We extend the sparsity scheduling to a periodical version with the period denoted as ΔT , then we have:

$$S_{t,n} = S_{t,N} - S_{t,N} (1 - \frac{n}{N})^3, \qquad n = \Delta T, 2\Delta T, \dots, N.$$
 (16)

We compare the impact of different ΔT values on the average accuracy of the CIFAR-100 with 10 tasks in Figure 9. When ΔT is set to the total number of training epochs, the method effectively



Figure 8: Visualization of sparsity scheduling results for CIFAR-100 with 10 tasks. Each task trains 50 epochs here. The target sparsity is calculated by Equation 4, while the real sparsity is calculated after training of each task by Equation 3.

reduces to static sparse training. As illustrated in Figure 9, changing the update interval from 1 to 5 has minimal impact on performance. However, when updates become too infrequent-such as only occurring once per task-there is a noticeable drop in performance. Therefore, to balance time and computational costs, it is recommended to use a shorter update interval such as 5 epochs.



Figure 9: The average accuracy for different ΔT used in Equation 16. We set $\Delta T = 1, 5, 10, 25, 50$ here, with each task training for a total of 50 epochs.

