LPC: A Logits and Parameter Calibration Framework on Continual Learning

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Abstract

Deep learning based pre-trained natural language processing (NLP) models typically pretrain on large unlabeled corpora first, then finetune on new tasks. When we execute such a paradigm on continuously sequential tasks, the model will suffer from the catastrophic forgetting problem (i.e., they forget the parameters learned in previous tasks when we train the model on newly emerged tasks). Inspired by the idea of how humans learn things, we aim to maintain the old knowledge when we transfer 011 to novel contents and calibrate the old and new knowledge. We propose a Logits and Parame-014 ter Calibration (LPC) framework to reduce the catastrophic forgetting in the continual learning process. The proposed framework includes 017 two important components, the Logits Calibra-018 tion (LC) and Parameter Calibration (PC). The core idea is to reduce the difference between 019 old knowledge and new knowledge by doing calibration on logits and parameters so that the 021 model can maintain old knowledge while learning new tasks without preserving data in pre-024 vious tasks. First, we preserve the parameters learned from the base tasks. Second, we train the existing model on novel tasks and estimate the difference between base logits and parameters and novel logits and parameters. Third, we drift from the base tasks to novel tasks gradually. Furthermore, we integrate the logtis and parameter calibration into a brand-new optimization algorithm. Finally, we do experiments on 7 scenarios of the GLUE (the General Lan-033 guage Understanding Evaluation) benchmark. The experimental results show that our model achieves state-of-the-art performance on all 7 037 scenarios.

1 Introduction

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Predicting labels for a large number of instances occurring continuously is a crucial problem in many real-world applications like online tweets/news summary, online product classification in e-commerce systems, and online dialogue learning systems. In these scenarios, we not only require the model to learn from its own experiences, but also expect the model to be capable of continuously acquiring, fine-tuning, and transferring knowledge over time (Parisi et al., 2019), which is also known as continual learning. One of the most essential existing challenges we aim to solve in the continual learning is the catastrophic forgetting problem (McCloskey and Cohen, 1989; Kirkpatrick et al., 2017a). The forgetting typically happens when we apply the pre-trained model (e.g., BERT (Devlin et al., 2018)) on newly emerged tasks, the model usually forgets the parameters it learned from previous tasks when we train it on new incoming tasks. 043

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Existing works trying to solve the catastrophic forgetting problem are varied, which can be divided into two categories: (1) storing exemplars from previous classes (Rebuffi et al., 2017; Rolnick et al., 2019); (2) regularizing the parameters when we fine-tune the model on new tasks (Kirkpatrick et al., 2017b; Li and Hoiem, 2017; Aljundi et al., 2018). Such methods aim to transfer or store the knowledge of previous tasks to the newly emerged tasks and preserve the knowledge learned previously. Memory Aware Synapses (MAS) (Aljundi et al., 2018) is an advanced approach by computing the importance of the neural network parameters in an unsupervised and online manner. MAS assigns more weights on the parameters that are most important to the model and allows the model to selectively forgets those weights that are not so essential. Also, Lee et al. (Lee et al., 2020) successfully reduce the catastrophic forgetting during the fine-tuning step by randomly mixing pre-trained parameters into a downstream model in a dropoutstyle.

The methods mentioned above address the catastrophic forgetting through multi-task learning. They typically require storing the data from old or pre-trained tasks, and replay them during the

fine-tuning. However, this learning pattern does not consider the constraint of memory resource or privacy issues, e.g., the data of old tasks is often 086 inaccessible or too large for the continual adaptation setting. Unlike the multi-task learning strategy, here we focus on the calibration of knowledge gap between different tasks, which can reduce the catas-090 trophic forgetting without any old data/task replay. The proposed calibration framework is used for both encoder parameters and output classifiers, we first train the novel model and evaluate the base model on novel tasks. Specifically, we add the logits calibration that can amplify the softmax output of the base model, and overcome the bias towards the novel category (Zhao et al., 2020), which can simultaneously enforce the model to preserve previous knowledge via explicit weight constraints. 100 Also, for the calibration on encoder parameters, we 101 encourage the model to maintain previously learned 102 knowledge by simulating the training objective us-103 ing the parameters of the base model. Then, during 104 105 the training on novel tasks, the model will calibrate parameters with target drift form the base tasks to 106 the novel tasks to balance new task learning and 107 old knowledge maintenance. It allows the model 108 to focus on novel tasks by making the learning objective drifting from the base tasks to novel tasks 110 gradually. 111

Accordingly, we propose a Logits and Parameter Calibration framework LPC (shown in Figure 1) on continual learning scenario, which is used to reduce catastrophic forgetting without further data storage. The proposed calibration mechanism includes two components for both model encoder parameters and output logits, we finally integrate these two calibrations into a brand-new optimization algorithm by decoupling them from the gradient updates in Adam optimizer. We do experiments on the GLUE benchmark with pre-trained models BERT-base and ALBERT-xxlarge and achieve state-of-the-art performance.

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The contributions of our work are three folds. 125 First, we propose LPC, a novel continual learning 126 framework, which can reduce catastrophic forget-127 ting effectively without storing previous instances. 128 Second, we develop a new mechanism by calibrat-129 ing the logits and parameters with target drift from 130 base tasks to novel tasks, thereby alleviating the 131 catastrophic forgetting during the model updating. 132 Third, combining with a parameter regularization 133 based approach, our model achieves state-of-the-134

art performance while addressing the old knowledge forgetting without data storage. Therefore, the newly proposed LPC is feasible for researchers to use for further explorations in this field. 135

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2 Related Works

2.1 Continual Learning

Continual learning is also named as life-long learning, sequential learning, or incremental learning. As the name suggests, continual learning aims to learn tasks in a sequential way. In the field of biology, biological neural networks exhibit continual learning in which they acquire new knowledge over a lifetime (Zenke et al., 2017). However, continual learning in deep neural networks suffers from a phenomenon called catastrophic forgetting (Shin et al., 2017). Thus, one of the most essential goals of continual learning systems is to achieve satisfying performance on all tasks in an incremental way. Reducing catastrophic forgetting plays a vital role to achieve it. Current continual learning approaches can be classified into the following three families (De Lange et al., 2019): (1) Replay methods, (2) Regularization-based methods, and (3) Parameter isolation methods. Replay methods store samples in a raw format or generate pseudo-samples. Regularization-based methods eschews storing raw inputs, prioritizing privacy, and alleviating memory requirements. Parameter isolation methods dedicate different model parameters to each task to prevent any possible forgetting. Our method is an advanced regularization-based method alleviating the catastrophic forgetting without data storage.

2.2 Fine-tuning

Fine-tuning is a successful method in transfer learning by the following four steps: (1) pretrain a source neural network model on the source datasets; (2) create a new neural network model which copies all model designs and their parameters on the source model except the output layer; (3) add an output layer to the target model; (4) train the target model on the target datasets. Girshick et al. (Girshick et al., 2014) propose a R-CNN to fine-tune all network parameters. Long et al. (Long et al., 2015) propose DAN only fine-tuning the parameters of the last few layers. Li et al. (Li et al., 2018) investigate several regularization schemes that explicitly promote the similarity of the finetuned model with the original pre-trained model.



Figure 1: The Overview of LPC Framework. (1) Given the large-scale input texts from base tasks, we first pre-train a base model on these texts and initialize our model (for novel tasks) same as the base one. (2) We do base parameter preservation to preserve the parameters of the pre-trained model, and estimate the difference between base parameters and novel parameters during training, then compute the loss for the base model L_B . (3) During the novel task training, we compute logtis q_b and q_n for the base model and the novel model, respectively. (4) We do logits calibration (e.g., cross entropy with logits calibration for classification tasks) given q_b and q_n using L_{CELC} or L_{MSELC} for regression tasks as the loss for the novel model L_N . (5) In the parameter calibration with target drift, the objective function drifts from L_B to L_N gradually with the annealing coefficient $\lambda(t)$. (6) Finally, we perform back propagation to update the parameters of the novel model with parameter calibration.

Guo et al. (Guo et al., 2019) propose an adaptive fine-tuning approach SpotTune which automatically decides the optimal set of layers to fine-tune in a pre-trained model on a new task. Our method is a trade-off between multi-task learning and finetuning.

3 **Proposed Approach**

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In this section, we introduce our proposed Logits and Parameter Calibration framework, LPC. The 192 LPC framework includes two essential parts: (1) Logits Calibration (LC) that execute calibration on the logits to reduce the logits forgetting and 195 increase the accuracy and (2) Parameter Calibra-196 tion (PC) to do calibration on the parameters to 197 reduce the parameter forgetting. For the Logits Calibration, we apply the Cross Entropy with Logits Calibration (CELC) for classification tasks (or the Means Squared Error with Logits Calibration (MSELC) for regression tasks). The Parameter Calibration consists of three components: (1) Base

Parameter Preservation (BPP) that tries to preserve the parameters we learned from base tasks, (2) Novel Task Training (NTT) that trains the previous model on novel tasks, and (3) Parameter Calibration with Target Drift (PCTD) that focuses on drifting from the base tasks to novel tasks gradually. What is more, we introduce LPC algorithm by integrating the Logits Calibration (CELC or MSELC) and all three parts of Parameter Calibration (BPP, NTT, and PCTD) into a brand-new optimization algorithm based on the well-known Adam (Kingma and Ba, 2014) optimization algorithm.

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Logits Calibration 3.1

In this section, we introduce our proposed logtis calibration, the Cross Entropy with Logits Calibration (CELC) for classification tasks. Some other loss function (e.g., the Mean Squared Error for regression) can also be combined with the Logits Calibration, in the following paragraph.

Algorithm 1 LPC

- 1: given initial learning rate $\alpha \in \mathbb{R}$, momentum factors $\beta_1 = 0.9$, $\beta_2 = 0.999$, $\epsilon = 10^{-8}$, pre-trained parameter vector $\theta^* \in \mathbb{R}^n$, hyperparameter for the regularizer $\delta \in \mathbb{R}$, coefficient of the quadratic penalty $\gamma \in \mathbb{R}$, hyperparameter controlling the annealing rate $r \in \mathbb{R}$, hyperparameter controlling the timesteps $t_0 \in \mathbb{N}$.
- 2: initialize timestep $t \leftarrow 0$, parameter vector $\theta_{t=0} \in \mathbb{R}^n$, importance weights $\Omega \leftarrow 1$, first moment vector $m_{t=0} \leftarrow 0$, second moment vector $v_{t=0} \leftarrow 0$, schedule multiplier $\eta_{t=0} \in \mathbb{R}$.

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4:	$t \leftarrow t + 1$		▷ update timestep
5:	$x \leftarrow \text{SelectBatch}(\mathbf{x})$		⊳ select batch data
6:	$q_{n,t} \leftarrow Q_{n,t}(x,\theta_{t-1})$	▷ compute output logits	s for the novel model
7:	$q_{b,t} \leftarrow Q_{b,t}(x,\theta^*)$	⊳ compute output logi	ts for the base model
8:	$\nabla(f_t(x;\theta_{t-1})) \leftarrow \nabla(L_{CELC}(q_{n,t},q_b))$	$_{t}) \parallel L_{MSELC}(q_{n,t},q_{b,t}))$	▷ compute gradients
9:	$\Omega_t \leftarrow \Omega_{t-1}$		
10:	for $k \leftarrow 0$ to N do		
11:	$g_t(x_k) \leftarrow \nabla l_2^2(f_t(x_k; \theta_{t-1}))$		
12:	$\Omega_t \leftarrow \Omega_t + \ g_t(x_k)\ $		
13:	end for		
14:	$\Omega_t \leftarrow \Omega_t / N$	▷ compute importance weights after	r each update epochs
15:	$\lambda(t) \leftarrow 1/(1 + \exp(-r \cdot (t - t_0)))$	⊳ compute	annealing coefficient
16:	$g_t \leftarrow \lambda(t) \nabla f_t(x; \theta_{t-1}) + 2(1 - \lambda(t))$	$\delta \gamma \Omega_t(\theta_{t-1} - \theta^*)$ \triangleright co	mpute new gradients
17:	$m_t \leftarrow \beta_1 m_{t-1} + (1 - \beta_1) g_t$	⊳ update biased f	irst moment estimate
18:	$v_t \leftarrow \beta_2 v_{t-1} + (1 - \beta_2) g_t^2$	b update biased second r	aw moment estimate
19:	$\hat{m}_t \leftarrow m_t / (1 - \beta_1^t)$	▷ compute bias-corrected f	irst moment estimate
20:	$\hat{v}_t \leftarrow v_t / (1 - \beta_2^t)$	▷ compute bias-corrected second r	aw moment estimate
21:	$\eta_t \leftarrow \text{SetScheduleMultiplier}(t)$	\triangleright can be fixed, decay, or also be us	sed for warm restarts
22:	$\theta_t \leftarrow \theta_{t-1} - \eta_t (\frac{\lambda(t)}{\lambda(t)} \alpha \hat{m}_t / (\sqrt{\hat{v}_t} + \epsilon))$	+ $2(1-\lambda(t))\delta\gamma\Omega_t(\theta_{t-1}-\theta^*)$)	▷ update parameters
23: U	ntil stopping criterion is met		
24: re	eturn optimized parameters θ_t		

3.1.1 Cross Entropy with Logits Calibration

The Cross Entropy (CE) Loss (Zhang and Sabuncu, 2018) is a widely-used loss for classification tasks in deep learning. It first applies a log softmax function on the output logits of the neural network. Then, it computes the negative log likelihood (nll) loss on the output of the log softmax function. Typically, the cross entropy loss can be defined as follows:

$$L_{CE}(q) = -\sum_{i=1}^{N_C} p_i \log(\frac{\exp(q_{n,i})}{\sum_{j=1}^{N_C} \exp(q_{n,j})})$$
(1)

where N_C is the total number of classes in the novel tasks. $q_{n,i}$ represents the output logits for class i of the novel model on the novel tasks. p_i

can be considered as the binary label of class i. If the data input x belongs to class i, the value of p_i will be 1, otherwise, the value will be 0.

Nevertheless, the original cross entropy loss only concerns the performance of the novel model. Thus, the model will suffer the catastrophic forgetting problem with the step increasing. In order to reduce the catastrophic forgetting problem, we consider to simultaneously evaluate the base model on the novel tasks and compute the output logits of the base model q_b .

Inspired by the idea from (Kukleva et al., 2021) which revises the original cross entropy loss by adding the summation of the exponential logtis of the base classes classifier to the denominator to change the normalization scale, we add the logits information of the base model into the cross entropy loss.

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However, different from Kukleva's method, we do logtis calibration by adding the difference between each logits of the novel model and the base model $(q_{n,i} - q_{b,i})$ to the corresponding output logits $q_{n,i}$ of the novel model for class *i*. In this way, the model can preserve important output logits information of each class for the base model in an element-wise way. Our proposed Cross Entropy with Logits Calibration (CELC) Loss is shown in Equation 2:

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$$L = -\sum_{i=1}^{N_C} p_i \log(\frac{\exp(q_{n,i} + \mu(q_{n,i} - q_{b,i}))}{\sum_{j=1}^{N_C} \exp(q_{n,j} + \mu(q_{n,j} - q_{b,j}))})$$
(2)

where we multiply the difference between the logits for the novel model and the base model $(q_n - q_b)$ by a weight item $\mu \in [0, 1]$ to control the calibration degree. By employing this new loss function, we can also increase the accuracy of the model through training process by giving a reward to the logits for the correct class if $q_{n,i}$ is larger than $q_{b,i}$, otherwise, giving a penalty to the logits for the correct class if $q_{n,i}$ is smaller than $q_{b,i}$.

3.1.2 Mean Squared Error with Logits Calibration

Mean Squared Error (MSE) Loss (Fisher, 1922) is the most commonly-used loss function for regression tasks. It computes the squared L2 norm between output logits and the true values and takes the mean of the full batch. Follow the idea of the logits calibration on cross entropy loss, we evaluate the base model on novel tasks and take out the output logits q_b . We measure the difference between the output logits of the novel model and the base model by adding a squared L2 norm on the difference between logits of the novel model and the base model $(q_n - q_b)^2$ to the original function. The proposed Mean Squared Error with Logits Calibration Loss L_{MSELC} is shown in Equation 3:

$$L_{MSELC}(q) = (q_n - p)^2 + \mu (q_n - q_b)^2 \quad (3)$$

3.2 Parameter Calibration

In this section, we introduce the second module of our model, Parameter Calibration (PC). Our proposed Parameter Calibration method can effectively reduce the catastrophic forgetting by giving a penalty to the prediction if the parameters of the novel model are different from the base model297by adding the squared difference between the pa-
rameters of the novel model and the base model298to the training loss. It includes three parts: (1)300Base Parameter Preservation (BPP), (2) Novel Task301Training (NTT), and (3) Parameter Calibration with302Target Drift (PCTD).303

3.2.1 Base Parameter Preservation

As shown in Figure 1, in Base Parameter Preser-305 vation, we try to maintain the parameters of the 306 base model like BERT (Devlin et al., 2018). Here, 307 we add a regularization to the posterior of parame-308 ters given data. The Base Parameter Preservation 309 method can be regarded as an improved method 310 derived from EWC (Kirkpatrick et al., 2017b) and 311 MAS (Aljundi et al., 2018). Different from EWC, 312 BPP measures the importance of each parameter 313 by introducing the importance weights Ω . During 314 training, the novel model preserves the information 315 of the most important parameters to a great extent 316 by penalizing the changes to those important pa-317 rameters more severely. The detailed derivation of 318 our proposed loss function is shown in Equation 4: 319

$$\begin{split} L_B &= -\log p(\theta|D_B) \\ \approx -\log p(\theta^*|D_B) + \delta(\theta - \theta^*)^T H(\theta^*) \Omega(\theta)(\theta - \theta^*) \\ \approx \delta(\theta - \theta^*)^T H(\theta^*) \Omega(\theta)(\theta - \theta^*) \\ \approx \delta(\theta - \theta^*)^T (NF(\theta^*) + H_{prior}(\theta^*)) \Omega(\theta)(\theta - \theta^*) \\ \approx \delta N \sum_{ij} F_{ij} \Omega_{ij}(\theta_{ij} - \theta^*_{ij})^2 \\ \approx \delta NF \sum_{ij} \Omega_{ij}(\theta_{ij} - \theta^*_{ij})^2 \\ = \delta \gamma \sum_{ij} \Omega_{ij}(\theta_{ij} - \theta^*_{ij})^2 \end{split}$$

(4)

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where δ is a hyperparameter for the regularizer. $H(\theta^*)$ is the Hessian matrix of the optimization objective with respect to θ^* . We can approximate $H(\theta^*)$ with the empirical Fisher information matrix $F(\theta^*)$ (Martens, 2014). N is the total number of data inputs in D_B . $H_{prior}(\theta^*)$ is the Hessian matrix of the negative log prior probability $-\log p(\theta)$. EWC ignores $H_{prior}(\theta^*)$ and approximates $H(\theta^*)$ by assigning the diagonal values of $F(\theta^*)$ to $H(\theta^*)$. Thus, we replace NF with a constant value γ at the end of the derivation. We can consider γ as a coefficient of the quadratic penalty. During the derivation, we can simply ignore $-\log p(\theta^*|D_B)$ as it is a constant term with

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respect to θ^* . $\Omega(\theta)$ is estimated by the sensitivity of the squared L2 norm of the function output to their changes. We can obtain Ω_{ij} by accumulating the gradients over the given data points by Equation 5:

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$$\Omega_{ij} = \frac{1}{N} \sum_{k=1}^{N} ||g_{ij}(x_k)||$$
(5)

where $g_{ij}(x_k) = \frac{\partial [l_2^2(f(x_k;\theta))]}{\partial \theta_{ij}}$ is the gradients of the squared L2 norm of the learned neural network with respect to the parameter θ_{ij} . The output of $f(x_k;\theta)$ is the loss of the network.

In Equation 4, θ_{ij} is the parameter of the novel model of the connections between pairs of neurons n_i and n_j in two consecutive layers. θ^* represents the pre-trained parameters, which can be assumed as a local minimum of the parameter space as shown in Equation 6:

$$\theta^* = \arg\min_{\theta} \{-\log p(\theta|D_B)\}$$
 (6)

3.2.2 Novel Task Training

In the novel task training process, we train the novel model and evaluate the base model on novel tasks simultaneously. The function of the neural network whose output is the loss of the model can be represented as follows:

$$L_N = f_t(x; \theta_{t-1}) \tag{7}$$

where t is the timestep. We compute the loss by the proposed Cross Entropy with Logits Calibration (CELC) for classification tasks and Mean Squared Error with Logits Calibration (MSELC) for regression tasks as follows:

$$f_t = L_{CELC}(Q(x; \theta_{t-1})) \parallel L_{MSELC}(Q(x; \theta_{t-1}))$$
(8)

where $Q(x; \theta_{t-1})$ represents the function of the novel model and the base model whose output are logits with data inputs x and parameters θ_{t-1} of the model in timestep t - 1.

3.2.3 Parameter Calibration with Target Drift

Multi-task learning tries to achieve satisfying performance on both of the base tasks and novel tasks.
However, one of the most essential problems of
multi-task learning is that it is inconsistent with
adaptation (Chen et al., 2020). To deal with this
problem, we introduce Parameter Calibration with

Target Drift, a method allowing the objective function to gradually drift from L_B to L_N with the annealing coefficient $\lambda(t)$:

$$L_T = \lambda(t)L_N + (1 - \lambda(t))L_B \tag{9}$$

where t refers to the timestep during the training process. We compute $\lambda(t) = \frac{1}{1 + \exp(-r \cdot (t - t_0))}$ as the sigmoid annealing function (Kiperwasser and Ballesteros, 2018), where r is the hyperparameter controlling the annealing rate and t_0 is the hyperparameter controlling the timesteps.

When $t < t_0, -r \cdot (t - t_0)$ will be positive. In this case, if $r \to \infty$, then $\exp(-r \cdot (t - t_0)) \to \infty$, $\lambda(t) \rightarrow 0, L_T = L_B$. When $t > t_0, -r \cdot (t - t_0)$ will be negative. In this case, if $r \to \infty$, then $\exp(-r \cdot (t-t_0)) \rightarrow 0, \lambda(t) \rightarrow 1, L_T = L_N.$ At this moment, our method can be regarded as fine-tuning. Otherwise, if $r \to 0$, then $-r \cdot (t - t)$ $t_0) \to 0, \exp(-r \cdot (t - t_0)) \to 1, \lambda(t) \to 0.5,$ $L_T = 0.5L_N + 0.5L_B$. In this case, our method can be regarded as multi-task learning. Finally, if $0 < r < \infty$, then $0 < \lambda < 1$. In this case, our method can be regarded as a trade off between finetuning and multi-task learning. With time goes by, the objective of the model drifts from base tasks to novel tasks gradually. Finally, by doing back propagation, we update parameters of the novel model with parameter calibration.

3.3 LPC Algorithm

In this section, we combine the Logits Calibration (CELC) with all three parts of Parameter Calibration (BPP, NTT, and PCTD) into a brand-new optimization algorithm as shown in Algorithm 1. The Logits Calibration (LC) part is shown from line 6 to line 8. The Parameter Calibration (PC) part is shown from line 9 to line 18 and line 24. Here, we introduce LPC Algorithm which integrates the quadratic penalty with importance weights and the annealing coefficient into a complete optimization algorithm by decoupling them from the gradient update in Adam optimization algorithm (Kingma and Ba, 2014). The orange part in Algorithm 1 depicts how LPC is different from Adam.

From line 9 to line 16, we show how we calculate Ω by initializing Ω as a tensor filled with the scalar value one. The size of Ω are the same as that of parameter size of the base model and the novel model. From line 11 to line 14, we accumulate the gradients of the squared L2 norm of the learned neural network over the given data inputs to obtain

Table 1: Experimental Results. All of results are the medians over 5 runs. The metric for CoLA is mcc (Matthew Correlation Coefficient). The metric for STS-B is corr (Average of Pearson and Spearman Correlation Coefficient). All other metrics are acc (Accuracy).

Model	CoLA mcc 8.5k	MRPC acc 3.7k	QNLI acc 105k	RTE acc 2.5k	SST-2 acc 67k	STS-B corr 7k	WNLI acc 634	Avg acc	Avg mcc	Avg corr
BERT-base + PALs (Stickland and Murray, 2019)	51.2	84.6	90.0	76.0	92.6	85.8	N/A	N/A	51.2	85.8
BERT-large + Adapters (Houlsby et al., 2019)	59.5	89.5	90.7	71.5	94.0	86.9	N/A	N/A	59.5	86.9
BERT-large + Diff pruning (Guo et al., 2020)	60.5	87.0	92.9	68.1	93.8	83.5	N/A	N/A	60.5	83.5
BERT-base + Adam (rerun) _{Median}	57.1	81.3	91.0	63.9	93.1	89.2	56.3	77.1	57.1	89.2
BERT-base + RecAdam (rerun) _{Median}	59.9	85.7	91.4	70.8	93.1	90.0	56.3	79.5	59.9	90.0
BERT-base + LPC _{Median}	61.8	86.1	91.5	74.7	93.2	90.3	62.0	81.5	61.8	90.3
ALBERT-xxlarge + Adam (rerun) $Median$ ALBERT-xxlarge + RecAdam (rerun) $Median$ ALBERT-xxlarge + LPC $Median$	70.5	88.8	93.7	72.9	91.1	92.2	69.0	83.1	70.5	92.2
	70.5	87.5	93.9	89.5	93.9	92.8	78.9	88.7	70.5	92.8
	74.1	89.4	94.3	89.5	95.8	93.3	81.7	90.1	74.1	93.3

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bidirectional Transformer encoder. In BERT, the

method.

Evaluations

RecAdam (Chen et al., 2020).

Experimental Setup

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4.1

Transformer uses bidirectional self-attention. AL-BERT is an advanced deep pre-trained language model with lower memory consumption and faster training speed than BERT. ALBERT improves BERT using parameter reduction techniques and employing self-supervised loss for sentence-order

importance weights Ω_{ij} for parameter θ_{ij} . In line

15, we compute the mean value of Ω_{ij} by dividing it

by N. Here, N is the total number of data inputs at

a given phase. In line 18, we compute the gradients

of the loss function as a weighted combination of

the gradients of L_N and L_B . In line 24, we update

the network parameters θ by the gradient descent

In this section, we evaluate LPC on the Gen-

eral Language Understanding Evaluation (GLUE)

(Wang et al., 2018) benchmark. We compare our

model with PALs (Stickland and Murray, 2019),

Adapters (Houlsby et al., 2019), Diff Pruning (Guo

et al., 2020), Adam (Kingma and Ba, 2014), and

We perform the experiments based on deep pre-

trained language models BERT-base¹ (Devlin et al.,

2018) and ALBERT-xxlarge (Lan et al., 2019), re-

spectively. BERT aims to learn a Transformer en-

coder for representing texts. BERT is a multi-layer

prediction (SOP). We evaluate our approach LPC on the GLUE benchmark. GLUE benchmark is a collection of resources for training, evaluating, and analyzing natural language understanding (NLU) systems (Wang et al., 2018). It contains the following 9 different scenarios: (1) Single-Sentence Scenarios: CoLA The Corpus of Linguistic Acceptability (Warstadt et al., 2019), and SST-2 The Stanford Sentiment Treebank (Socher et al., 2013); (2) Similarity and Paraphrase Senarios: MRPC The Microsoft Research Paraphrase Corpus (Dolan and Brockett, 2005), **OOP** The Quora Question Pairs dataset², and STS-B The Semantic Textual Similarity Benchmark (Cer et al., 2017); (3) Inference Scenarios: MNLI The Multi-Genre Natural Language Inference Corpus (Williams et al., 2017), QNLI The Stanford Question Answering Dataset (Rajpurkar et al., 2016), RTE The Recognizing Textual Entailment datasets (Dagan et al., 2005) (Haim et al., 2006) (Giampiccolo et al., 2007) (Bentivogli et al., 2009), and WNLI The Winograd Schema Challenge (Levesque et al., 2012).

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4.2 Results

We perform experiments on 7 scenarios of the GLUE benchmark as shown in Table 1. From the experimental results with BERT-base model, we outperform BERT-base with Adam and BERT-base with RecAdam (Chen et al., 2020) models on 7 out of 7 scenarios of the GLUE benchmark and achieve 2.5% improvements on average measured by acc on MRPC, QNLI, RTE, SST-2, and WNLI, 3.2% improvements measured by mcc on CoLA, and 0.3% improvements measured by corr on STS-B compared with RecAdam. Especially, we achieve significant improvements on WNLI corpus (+10.1%) and CoLA corpus (+5.5%). From the experimen-

¹https://huggingface.co/transformers/model_doc/bert.html

²https://www.quora.com/q/quoradata/First-Quora-Dataset-Release-Question-Pairs

Table 2: The Results of Ablation Study on Adam, Logtis Calibration (LC), Parameter Calibration (PC), and Logits and Parameter Calibration (LPC). All of results are the medians over 5 runs. The metric for CoLA is mcc (Matthew Correlation Coefficient). The metric for STS-B is corr (Average of Pearson and Spearman Correlation Coefficient). All other metrics are acc (Accuracy).

Model	CoLA mcc 8.5k	MRPC acc 3.7k	QNLI acc 105k	RTE acc 2.5k	SST-2 acc 67k	STS-B corr 7k	WNLI acc 634	Avg acc	Avg mcc	Avg corr
BERT-base + Adam (rerun) Median	57.1	81.3	91.0	63.9	93.1	89.2	56.3	77.1	57.1	89.2
BERT-base + LC Median	61.2	82.8	91.5	66.8	92.3	89.3	56.3	77.9	61.2	89.3
BERT-base + PC Median	61.4	85.3	91.5	72.2	92.8	90.2	57.7	79.9	61.4	90.2
BERT-base + LPC Median	61.8	86.1	91.5	74.7	93.2	90.3	62.0	81.5	61.8	90.3

tal results on ALBERT-xxlarge model, we outperform ALBERT-xxlarge with Adam and ALBERTxxlarge with RecAdam models on 7 out of 7 scenarios of the GLUE benchmark and achieve 1.6% improvements on average measured by acc on MRPC, QNLI, RTE, SST-2, and WNLI, 5.1% improvements measured by mcc on CoLA, and 0.5% improvements measured by corr on STS-B compared with RecAdam. Specifically, we achieve great improvements on CoLA corpus (+5.1%) and WNLI corpus (+3.5%). What is more, there is no obvious relationship between the size of the datasets and the results. Namely, our model performs well on both large datasets and small datasets.

4.3 Ablation Study

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As we have mentioned, our model (LPC) has two important components, Logits Calibration (LC) and Parameter Calibration (PC). Thus, we do ablation 508 study on these two components separately with BERT-base pre-trained model on the 7 scenarios 510 of the GLUE benchmark. The results of albation study is shown in Table 2. We can see both of 512 LC and PC achieve better results than the baseline 513 Adam. LPC achieves the best results among all 514 three models. Compared with Adam, LC achieves 516 1.0% improvements on average measured by acc on MRPC, QNLI, RTE, SST-2, and WNLI, 7.2% improvements measured by mcc on CoLA, and 0.1% 518 improvements measured by corr on STS-B. Com-519 pared with Adam, PC achieves 3.6% improvements 520 on average measured by acc on MRPC, QNLI, RTE, SST-2, and WNLI, 7.5% improvements measured 522 by mcc on CoLA, and 1.1% improvements measured by corr on STS-B. Compared with Adam, 524 LPC achieves 5.7% improvements on average mea-525 sured by acc on MRPC, ONLI, RTE, SST-2, and 526 WNLI, 8.2% improvements measured by mcc on CoLA, and 1.2% improvements measured by corr

on STS-B.

5 Conclusion

In this paper, we propose Logits and Parameter Calibration (LPC) framework on continual learning to deal with the catastrophic forgetting problem. The proposed framework includes two important components, Logits Calibration (LC) and Parameter Calibration (PC). We propose the Cross Entropy Loss with Logits Calibration (CELC) for classification tasks and the Mean Squared Error with Logits Calibration (MSELC) for regression tasks. The Parameter Calibration consists of three components: (1) Base Parameter Preservation (BPP), (2) Novel Task Training (NTT), and (3) Parameter Calibration with Target Drift (PCTD). What is more, we introduce LPC algorithm by integrating the Logits Calibration and all three parts of Parameter Calibration (BPP, NTT, and PCTD) into a brand-new optimization algorithm based on the well-known Adam optimization algorithm. We do experiments on 7 scenarios of GLUE benchmark and achieve state-of-the-art performance on all the 7 scenarios. The limitation of our work is that our work cannot handle the online learning settings. This means that when data comes in an online manner (sometimes without labels), we have no technique to handle it. Thus, our future direction is to make our model fit the online learning settings. We also release the open-source LPC Algorithm to further benefit the continual learning research community.

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A LPC Appendix

A.1 Hyperparameter Analysis

In this section, we analyze the most essential hyperparameters we set in the LPC model. δ is a hyperparameter controlling the level of regularization. Setting δ between 1 and 2 balances the level of regularization. Ω is a parameter measuring the importance of different parameters in the model. Initializing Ω as ones makes the importance of each parameter more balanced. The hyperparameter u_e controls the updating epochs of Ω . Typically, u eis between 1 and 16. $w \, s$ is a hyperparameter controlling the number of steps of updating with low learning rate before/at the beginning of the training process. We set $w \ s$ as 0, 320 or 640. After these warmup steps, we will use the regular learning rate to train our model until convergence. In other words, we have a few steps adjustment before we actually train the model. From our experiments, we find that the hyperparameters δ , u_e , and w_s have great influences on the experimental results.

Figure 2 shows the comparison of different hyperparameter (δ , u e, and w s) initializations on CoLA, MRPC, and STS-B corpora with BERTbase pre-trained model.

In Figure 2 chart (1), we set $u_e = 2$ and $w_s = 2$ 320. We can see when δ increases from 1 to 1.2, the performance of the model decreases a lot. After that, the performance of the model increases with δ increasing. The model achieves the best results when $\delta = 2$ on all the three corpora.

In Figure 2 chart (2), we set $\delta = 2$ and w s =320. We can see the performance of the model varies with different values of u_e . Specifically, when u_e increases from 1 to 2, the performance of the model improves a lot. While when u_e increases from 2 to 4, the performance decreases in a large extent. However, when u_e increases from 4



Figure 2: Comparison of Different Hyperparameter Initializations on CoLA, MRPC, and STS-B Corpora with BERT-base Pre-trained Model. The metric for CoLA, MRPC, and STS-B are mcc (Matthew Correlation Coefficient), acc (Accuracy), and corr (Average of Pearson and Spearman Correlation Coefficient), respectively.

Table 3: The Results of Ablation Study on Adam, Logtis Calibration (LC), Parameter Calibration (PC), and Logits and Parameter Calibration (LPC) with ALBERT-xxlarge Pre-trained Model. All of results are the medians over 5 runs. The metric for CoLA is mcc (Matthew Correlation Coefficient). The metric for STS-B is corr (Average of Pearson and Spearman Correlation Coefficient). All other metrics are acc (Accuracy).

Model	CoLA mcc 8.5k	MRPC acc 3.7k	QNLI acc 105k	RTE acc 2.5k	SST-2 acc 67k	STS-B corr 7k	WNLI acc 634	Avg acc	Avg mcc	Avg corr
ALBERT-xxlarge + Adam (rerun) Median	70.5	88.0	93.7	72.9	91.1	92.2	69.0	82.9	70.5	92.2
ALBERT-xxlarge + LC Median	71.0	88.5	93.8	88.4	95.5	92.3	70.4	87.3	71.0	92.3
ALBERT-xxlarge + PC Median	74.1	88.6	94.0	88.4	95.7	92.9	74.6	88.3	74.1	92.9
ALBERT-xxlarge + LPC Median	74.1	89.4	94.3	89.5	95.8	93.3	81.7	90.1	74.1	93.3

to 8, the model performance increases again. When u_e increases from 8 to 16, there is a slight increase on the performance.

In Figure 2 chart (3), we set $\delta = 1$ and $u_e = 1$. We can see when w_s increases from 0 to 320, there is a big increase on all three corpora. However, when w_s increases from 320 to 640, the performance decreases slightly, instead.

A.2 Forgetting Analysis

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In addition to computing accuracy, we also measure the forgetting by computing the euclidean distance between the parameters of the novel model and the base model on CoLA corpus. Figure 3 shows the comparison of parameter forgetting from the first epoch to the last epoch and the corresponding accuracy after convergence with epoch increasing among LPC, RecAdam and Adam. In Figure 3 chart (1), with epoch increasing, the euclidean distance of Adam increases a lot, which means the forgetting of Adam is huge with the epoch increasing. However, our model (LPC) reduces the forgetting in a large extent compared with Adam and achieves similar forgetting with RecAdam, another baseline trying to reduce carastrophic forgetting. Here, the forgettnig of our model is a little bit worse than RecAdam is because our model tries to remember the most important parameters while forget unimportant parameters. Furthermore, in Figure 3 chart (2), we can see our model (LPC) achieves the best accuracy compared with RecAdam and Adam all the time after convergence (Epoch 4). 804

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A.3 Ablation Study with ALBERT-xxlarge Model

As we have mentioned, our model (LPC) has two important components, Logits Calibration (LC) and Parameter Calibration (PC). In addition to doing ablation study with BERT-base pre-trained model, we also do ablation study on these two components separately with ALBERT-xxlarge pre-trained model on the 7 scenarios of the GLUE benchmark. The results of albation study with ALBERT-xxlarge pre-trained model is shown in Table 3. We can see with ALBERT-xxlarge pre-trained model, both of LC and PC achieve better results than the baseline Adam. LPC achieves the best results among all three models. Compared with Adam, LC achieves 5.3% improvements on average measured by acc on MRPC, QNLI, RTE, SST-2, and WNLI, 0.7% im-



Figure 3: Comparison of Parameter Forgetting and Model Performance with the Epoch Increasing on CoLA Corpus with BERT-base Pre-trained Model.

provements measured by mcc on CoLA, and 0.1% improvements measured by corr on STS-B. Com-829 pared with Adam, PC achieves 6.5% improvements 830 on average measured by acc on MRPC, QNLI, RTE, 831 SST-2, and WNLI, 5.1% improvements measured 832 by mcc on CoLA, and 0.8% improvements mea-833 sured by corr on STS-B. Compared with Adam, 834 LPC achieves 8.7% improvements on average mea-835 sured by acc on MRPC, QNLI, RTE, SST-2, and 836 WNLI, 5.1% improvements measured by mcc on 837 CoLA, and 1.2% improvements measured by corr 838 on STS-B. Thus, we can conclude that our model 839 can achieve state-of-the-art results with different 840 pre-trained model. These results prove the scalabil-841 ity of our model. 842