

SSPRONET: SECONDARY STRUCTURE AWARE GRAPH NEURAL NETWORK FOR PROTEIN REPRESENTATION LEARNING

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ABSTRACT

013 Graph structures are widely leveraged to represent proteins. However, to a large
 014 extent, proteins fold into complex three-dimensional conformations that cannot be
 015 entirely well-captured by graphs built only from sequence adjacency or distance
 016 cutoffs. In this paper, we discover that a more faithful characterization comes
 017 from secondary structure elements—such as α -helices and β -sheets—that reflect
 018 recurring local motifs and stabilizing hydrogen-bond patterns. To this end, we
 019 propose a new graph neural network framework that augments node repres-
 020 entations with the secondary structure assignment of each residue and introduces
 021 a novel edge-construction strategy based on hydrogen bonds weighted by their
 022 energetic strength. This formulation captures both local structural context and
 023 long-range couplings essential to protein stability. On commonly used bench-
 024 marks, our model achieves the leading accuracy compared with state-of-the-art
 025 methods while providing improved interpretability through biologically mean-
 026 ingful edges. These results highlight the promise of secondary-structure-aware,
 027 energy-weighted graphs as an effective inductive bias for protein representation
 028 learning.

1 INTRODUCTION

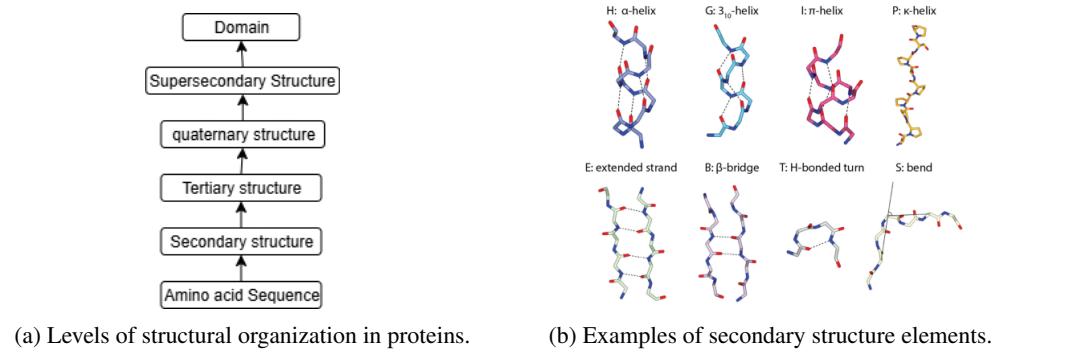
031 Graph Neural Networks (GNNs) have emerged as powerful learning paradigms for complex, re-
 032 lational data, with successes on social networks (Easley & Kleinberg, 2010), knowledge graphs
 033 (Easley & Kleinberg, 2010), molecular graphs (Wu et al., 2018), and biological networks (Barabasi
 034 & Oltvai, 2004), as well as for modeling 3D objects (Simonovsky & Komodakis, 2017), manifolds
 035 (Bronstein et al., 2017), and source code (Allamanis et al., 2017). Benchmarks such as the Open
 036 Graph Benchmark (OGB) have further catalyzed progress by standardizing tasks and evaluation (Hu
 037 et al., 2020).

038 **Proteins as graphs.** Proteins are composed of amino acids and realize diverse cellular functions
 039 by folding into three-dimensional (3D) conformations. Beyond the one-dimensional (1D) peptide
 040 sequence, each residue has 3D coordinates in space; effective modeling must therefore leverage
 041 both views. Notably, proteins with similar sequences can adopt very different folds (Alexander
 042 et al., 2009), whereas proteins with similar folds may have entirely different sequences (Agrawal
 043 & Kishan, 2001). These observations motivate representation learning methods that couple 1D
 044 sequence and 3D structure (Liu et al., 2022; Fout et al., 2017; Jumper et al., 2021; Gao et al., 2021;
 045 Gao & Ji, 2019; Yan et al., 2022; Wang et al., 2022b; Yu et al., 2022; Xie et al., 2022; Gui et al.,
 046 2022; Luo et al., 2022; Baldassarre et al., 2021; Jing et al., 2020; Zhang et al., 2022; Hermosilla &
 047 Ropinski, 2022; Fan et al., 2022; Hu et al., 2024).

048 **From proximity proxies to biophysical edges.** Radius cutoffs and sequence windows are con-
 049 venient, but do residues “interact” merely because they are close in space or adjacent in sequence,
 050 or because specific chemical and geometric conditions are satisfied (e.g., donor/acceptor compati-
 051 bility and orientation)? If proximity were the right criterion, why would model performance hinge
 052 so strongly on brittle hyperparameters (window size, cutoff radius) instead of stable, mechanistic
 053 rules? Prior work improves parts of this picture—CDConv separates discrete sequence from contin-
 054 uous geometry (Fan et al., 2022), ProNet enforces hierarchical completeness (Wang et al., 2022a),

054 CoupleNet couples dual graphs (Hu et al., 2024), and SCHull offers a sparse, connected scaffold
 055 (Wang et al., 2025)—yet the edge decision itself often remains a proximity proxy.
 056

057 Protein structure is organized into *secondary-structure* elements (e.g., α -helices, β -sheets) stabilized
 058 primarily by hydrogen bonds. As outlined in Schulz & Schirmer (2013), organization spans pri-
 059 mary, secondary, tertiary, and quaternary levels and extends to supersecondary motifs and domains
 060 (Fig. 1a). In practice, tools such as DSSP (Hekkelman et al., 2025) provide residue-level secondary-
 061 structure assignments and identify backbone hydrogen bonds (examples in Fig. 1b). These annota-
 062 tions suggest a more faithful inductive bias: *nodes* should encode secondary-structure context, and
 063 *edges* should reflect stabilizing interactions—with strengths that vary—rather than distance alone.
 This is precisely the gap we target next with SSProNet.



065 (a) Levels of structural organization in proteins. (b) Examples of secondary structure elements.
 066

067 Figure 1: (a) Protein structure levels, from primary to quaternary (plus supersecondary and do-
 068 mains). (b) Common secondary-structure elements such as α -helices, β -sheets, and turns, from
 069 DSSP (Hekkelman et al., 2025).
 070

081 1.1 CONTRIBUTION

082 We introduce *SSProNet*, a GNN that (i) enriches node features with each residue’s *secondary-
 083 structure assignment* and (ii) defines *edges* via *backbone hydrogen bonds* weighted by their *energetic
 084 strength*. Messages flow on this energy-weighted H-bond graph, fused with proximity edges that
 085 come from radial graph construction. To ensure geometric robustness, we adopt the $SE(3)$ -invariant
 086 descriptors from ProNet (Wang et al., 2022a), derived from local residue frames and inter-residue
 087 geometry, which guarantee a complete and rotation/translation-invariant structural representation.
 088 Architecturally, SSProNet is compatible with dual-stream coupling ideas (as in Hu et al. (2024))
 089 yet replaces “who-talks-to-whom” with a biophysically grounded criterion; it is complementary to
 090 CDCConv’s separation of discrete/continuous displacements (Fan et al., 2022), and can be paired with
 091 SCHull when a provably sparse/connected scaffold is desired (Wang et al., 2025).
 092

093 1.2 PAPER OUTLINE

094 Section 2 provides the necessary background for GNN-based protein representation learning and
 095 the motivation for our SSProNet. Section 3 formally introduces SSProNet, especially detailing its
 096 graph construction (secondary-structure nodes and energy-weighted H-bond edges) and invariant
 097 features. Section 4 presents experiments, including performance comparisons against the state-of-
 098 the-art SCHull framework (Wang et al., 2025). Section 5 concludes the paper.
 099

100 2 BACKGROUND AND MOTIVATION

101 2.1 PRELIMINARY

102 We model a protein as a 3D graph $G = (V, E, \mathbf{P})$, where V indexes residues (or atoms), E is an
 103 edge set, and $\mathbf{P} = \{\mathbf{P}_i \in \mathbb{R}^3\}_{i \in V}$ are coordinates (by default C_α for residue graphs). A repres-
 104 entation $\Phi(G)$ is $SE(3)$ -*invariant* if $\Phi(R\mathbf{P} + t) = \Phi(\mathbf{P})$ for any rotation $R \in SO(3)$ and translation
 105 $t \in \mathbb{R}^3$; it is *complete* (up to rigid motion) if $\Phi(G) = \Phi(G')$ implies the coordinates of G' are

108 congruent to G . Across biomolecular GNNs, four properties consistently drive performance and
 109 robustness: (i) $SE(3)$ symmetry handling (invariance/equivariance), (ii) *completeness*/expressivity
 110 of geometric encodings, (iii) a graph topology that is sparse, connected, and maximally informative,
 111 (iv) *biologically grounded* priors (e.g., secondary structure, hydrogen bonds).
 112

113 **2.2 HIERARCHICAL $SE(3)$ -AWARE ENCODERS**
 114

115 **Coarse-to-fine structure.** ProNet (Wang et al., 2022a) introduced hierarchical encoders that build
 116 $SE(3)$ -invariant, provably *complete* descriptors at three levels: (1) **amino-acid** (residue) with lo-
 117 cal frames and inter-residue geometry; (2) **backbone** augmenting with plane/dihedral relations to
 118 disambiguate chain orientation; (3) **all-atom** incorporating side-chain torsions for fine-grained dis-
 119 tinction. Interaction blocks (Hier-Geom-MP) integrate these descriptors into edge-gated message
 120 passing with residual updates and invariant graph readout. This architecture preserves $SE(3)$ sym-
 121 metry while maintaining discriminative power across scales, and serves as the backbone we inherit.
 122

123 **2.3 COUPLING SEQUENCE AND 3D GEOMETRY**
 124

125 **Continuous–discrete fusion.** Protein neighborhoods have two distinct regularities: 1D sequence
 126 (regular, discrete) and 3D space (irregular, continuous). CDConv (Fan et al., 2022) addresses this by
 127 convolving over a hybrid neighborhood (continuous displacements δ and discrete sequence offsets
 128 Δ) with offset-specific kernels, thereby reducing interference between the two modalities while
 129 letting them interact.

130 **Two-graph coupling.** CoupleNet (Hu et al., 2024) operationalizes the idea with two explicit edge
 131 families—*sequence* (small $|\Delta|$) and *radius* ($\|\mathbf{P}_i - \mathbf{P}_j\| \leq r$)—and performs coupled node–edge
 132 updates. After pooling, it expands spatial thresholds to grow the receptive field as features become
 133 coarser. The key takeaway is that architectural separation of sequence and spatial relations simplifies
 134 learning and stabilizes training.
 135

136 **2.4 GRAPH CONSTRUCTION PARADIGMS**
 137

138 **Radius/ ε -graphs and kNN.** Cutoff (ε) or kNN graphs are ubiquitous for coverage and simplicity,
 139 but can be either overly dense (hurting sample efficiency) or fragile (hurting connectivity), and may
 140 admit geometric ambiguities (distinct structures sharing similar local neighborhoods).

141 **Rigid, sparse, connected alternatives.** Recent *rigidity-aware* constructions (e.g., spherical-convex-
 142 hull or related projections) (Wang et al., 2025) aim for graphs with theoretical guarantees: low edge
 143 density, connectivity, and improved identifiability when paired with metric/dihedral edge attributes.
 144 These designs reduce spurious edges yet keep enough structure to reconstruct geometry up to isom-
 145 etry, improving downstream stability.
 146

147 **2.5 BIOLOGY-GROUNDED PRIORS**
 148

149 **Secondary structure and solvent accessibility.** DSSP (Hekkelman et al., 2025) remains the ref-
 150 erence for assigning per-residue secondary structure (H/E/C/... variants) and solvent accessibil-
 151 ity from PDB coordinates. These labels summarize recurring local conformations (helices, sheets,
 152 loops) and exposure, providing interpretable priors that complement purely geometric channels.

153 **Hydrogen bonds (H-bonds).** DSSP identifies backbone hydrogen bonds using an electrostatics-
 154 based energy criterion rooted in Kabsch–Sander. More negative energies indicate stronger bonds;
 155 common practice keeps only stabilizing bonds (e.g., threshold $h < 0$ kcal/mol, such as -0.5). Im-
 156 portantly, H-bonds are *nonlocal* along sequence and can bridge distant 3D regions (inter-strand β
 157 ladders, helix capping, long-range turns). As graph edges, they add sparse, physically interpretable
 158 couplings that typical radius graphs miss.
 159

160 **2.6 POSITIONING OUR APPROACH**
 161

The above motivates two design decisions we adopt in the below Section 3:

- **Keep the encoder, change the graph.** We retain ProNet’s hierarchical, SE(3)-invariant message passing (*capacity held constant*) and instead *redefine the topology* to include energy-filtered H-bond edges on top of a light proximity scaffold. This isolates the effect of biology-grounded connectivity.
- **Add lightweight residue priors.** We inject DSSP-derived secondary-structure and solvent-accessibility channels—interpretable cues that bias the model toward known structural regularities with minimal parameter overhead.

In contrast to prior two-graph schemes (sequence+radius) (Hu et al., 2024) or continuous–discrete kernels (Fan et al., 2022), our hybrid edge set introduces *chemistry-anchored* long-range constraints (H-bonds) while preserving the simplicity and coverage of a radius scaffold. Combined with complete hierarchical encoders (Wang et al., 2022a), this yields message passing over edges that are both *geometrically* informative and *biophysically* meaningful.

3 SSPRONET: SECONDARY STRUCTURE AWARE GRAPH NEURAL NETWORK FOR PROTEIN REPRESENTATION LEARNING

SSProNet builds on ProNet’s (Wang et al., 2022a) hierarchical, SE(3)-invariant encoders while introducing a biology-grounded graph and residue priors. Message passing operates on a hybrid edge set that combines generic proximity contacts with hydrogen-bond couplings anchored in protein chemistry.

3.1 GRAPH CONSTRUCTION

We represent each protein chain as a residue graph $G = (V, E)$ with one node per residue and C_α coordinates $\mathbf{P}_i \in \mathbb{R}^3$. The edge set is the union of a generic proximity graph and a biology-grounded hydrogen-bond graph: $E = (E_{\text{rad}} \cup E_{\text{HB}}) \setminus \{(i, i) \mid i \in V\}$.

Radius (proximity) edges. We connect residues that are spatially close:

$$E_{\text{rad}} = \{(i, j) : \|\mathbf{P}_i - \mathbf{P}_j\|_2 \leq r\},$$

with a cutoff r (default 10 Å) and an optional degree cap to bound neighborhood size. This provides a light, connected scaffold capturing generic short-range contacts.

Hydrogen-bond edges. From backbone hydrogen bonds identified by a standard secondary-structure tool (e.g., DSSP (Hekkelman et al., 2025)), we form directed edges between reported donor–acceptor residue pairs. Let E_{ij} denote the associated H-bond energy (more negative indicates stronger bonding). We retain only stabilizing bonds,

$$E_{\text{HB}} = \{(i, j) : \text{H-bond reported between } i \text{ and } j \text{ and } E_{ij} \leq h\},$$

with threshold $h < 0$ (default $h = -0.5$ kcal/mol). Unless stated otherwise, energies are used for *filtering* (to control precision/recall of E_{HB}) rather than as per-edge weights; undirected variants symmetrize by adding (j, i) whenever $(i, j) \in E_{\text{HB}}$.

Rationale. E_{rad} supplies coverage and local connectivity, while E_{HB} injects a sparse set of biophysically meaningful, often nonlocal couplings. As illustrated in Fig. 2, proximity-based edges are confined to local neighborhoods, whereas hydrogen-bond edges can span long sequence distances and link residues that are far apart in 3D but biochemically coupled. This highlights the key difference: SSPRONET does not rely solely on arbitrary cutoffs but grounds its connectivity in physically interpretable interactions. The combined edge set feeds ProNet-style encoders (Wang et al., 2022a), ensuring that message passing operates on both generic spatial contacts and stabilizing biochemical interactions.

3.2 NODE FEATURES AUGMENTED WITH BIOLOGICAL PRIORS

At each hierarchy level used by ProNet (Wang et al., 2022a) (residue, backbone, all-atom), SSPRONET augments the SE(3)-invariant geometric descriptors $\mathcal{F}(G)_{\text{base}}$, $\mathcal{F}(G)_{\text{bb}}$, and $\mathcal{F}(G)_{\text{all}}$ with two lightweight residue priors obtained from a standard annotator (e.g., DSSP (Hekkelman et al., 2025); see Appendix B): the secondary-structure label and solvent accessibility. These channels add interpretable biological context that complements ProNet’s primarily local geometric descriptors.

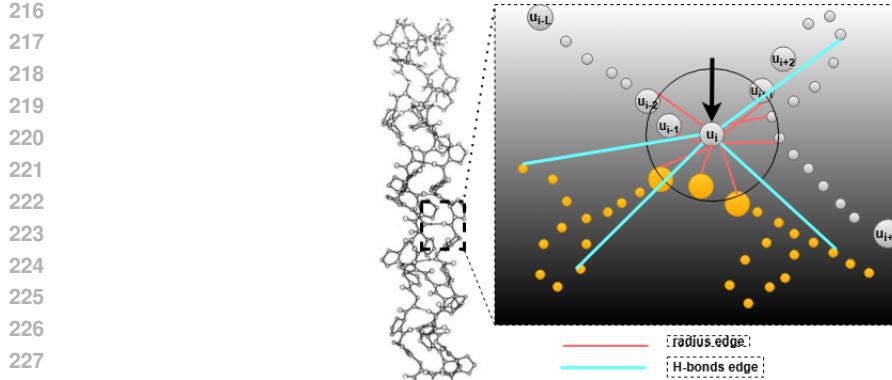


Figure 2: Comparison of graph construction strategies. Proximity-based graphs connect residues within a radius threshold, while SSProNet also adds hydrogen-bond edges that bridge distant sequence positions based on biophysical donor–acceptor rules. This expands the receptive field in a biologically meaningful way.

3.3 MODEL OVERVIEW

We retain ProNet’s hierarchical encoder (Wang et al., 2022a) and change (i) the topology $E = E_{\text{rad}} \cup E_{\text{HB}}$ (see Section 3.1) and (ii) the node channels (see Section 3.2). Below we specify one interaction block; stacking L blocks and adding a permutation-invariant readout completes SSProNet.

Notation. Let $\sigma(x) = x \text{ sigmoid}(x)$ (swish), \odot denote the Hadamard product, and $\|\cdot\|$ denote vector concatenation. For node i , $\mathcal{N}(i) = \{j : (i, j) \in E\}$ is its neighbor set. The hidden width is $d \in \mathbb{N}$. For each edge (i, j) we precompute three SE(3)-aware, ProNet-based descriptor families $\{\mathbf{f}_{ij}^{(k)}\}_{k=0}^2$ corresponding to: $k = 0$ (distance/angles), $k = 1$ (orientation or torsion; level-dependent), and $k = 2$ (positional).

Edge gates. We map descriptors to d -dimensional gates with small MLPs:

$$\mathbf{e}_{ij}^{(k)} = \phi_k(\mathbf{f}_{ij}^{(k)}) \in \mathbb{R}^d, \quad k \in \{0, 1, 2\}. \quad (1)$$

where ϕ_k is a two-layer perceptron for stream k , and $\mathbf{e}_{ij}^{(k)}$ is the edge-wise gate that scales the message transmitted along (i, j) in stream k .

Interaction block (Hier-Geom-MP). Given node states $\mathbf{x}^{(\ell)} = \{\mathbf{x}_i^{(\ell)}\}_{i \in V}$ at block ℓ , we form a message view and a residual view:

$$\tilde{\mathbf{x}}_i^{(\ell)} = \sigma(\mathbf{A}\mathbf{x}_i^{(\ell)} + \mathbf{a}), \quad \mathbf{r}_i^{(\ell)} = \sigma(\mathbf{B}\mathbf{x}_i^{(\ell)} + \mathbf{b}), \quad (2)$$

where $\mathbf{A}, \mathbf{B} \in \mathbb{R}^{d \times d}$ and $\mathbf{a}, \mathbf{b} \in \mathbb{R}^d$ are learnable; $\tilde{\mathbf{x}}_i^{(\ell)}$ is used to compute messages, while $\mathbf{r}_i^{(\ell)}$ provides the skip path.

Each stream k applies an edge-gated GraphConv-style update (Morris et al., 2019):

$$\mathbf{m}_{ij}^{(k)} = \mathbf{e}_{ij}^{(k)} \odot \tilde{\mathbf{x}}_j^{(\ell)}, \quad \text{message sent from } j \text{ to } i \text{ in stream } k, \quad (3)$$

$$\mathbf{u}_i^{(k)} = \sum_{j \in \mathcal{N}(i)} \mathbf{m}_{ij}^{(k)}, \quad \text{neighbor aggregation at node } i, \quad (4)$$

$$\mathbf{h}_i^{(k)} = \sigma(\mathbf{L}^{(k)} \mathbf{u}_i^{(k)}), \quad \text{stream-specific linear head}, \quad (5)$$

where $\mathbf{L}^{(k)} \in \mathbb{R}^{d \times d}$ is learnable and has the same shape across streams.

Fusion, mixing, and residual update. We concatenate the three stream outputs, mix them with a small MLP, and add the residual view:

$$\mathbf{h}_i = \|\mathbf{h}_i^{(k)}\|_{k=0}^2 \in \mathbb{R}^{3d}, \quad \mathbf{x}_i^{(\ell+1)} = \underbrace{\text{MLP}(\mathbf{C} \mathbf{h}_i)}_{\text{stream mixing}} + \mathbf{r}_i^{(\ell)}. \quad (6)$$

270 where $\mathbf{C} \in \mathbb{R}^{d \times 3d}$ projects the concatenated streams back to width d , and MLP (2–3 layers with
 271 swish and dropout) mixes the streams before the skip addition.
 272

273 **Readout and prediction.** After L blocks, we pool node embeddings and predict task outputs:
 274

$$\mathbf{h}_G = \sum_{i \in V} \mathbf{x}_i^{(L)}, \quad \hat{y} = \text{MLP}_{\text{out}}(\mathbf{h}_G), \quad (7)$$

275 where the sum is permutation-invariant pooling over residues, and MLP_{out} maps the graph embedding
 276 to logits (classification) or real values (regression).
 277

278 **Summary.** Eqs. 1—6 define a ProNet-style Hier-Geom-MP block with three geometric streams and
 279 edge-gated messages; Eq. 7 is the permutation-invariant graph readout. SSProNet preserves these
 280 mechanics but *grounds* E in biophysics (radius scaffold + energy-filtered H-bonds) and *augments*
 281 node inputs with DSSP secondary-structure and solvent-accessibility priors.
 282

283 4 EXPERIMENT

284 We evaluate our SSProNet on various protein tasks, including protein fold and reaction prediction,
 285 protein-ligand binding affinity prediction. Detailed descriptions of the datasets are provided in Sec-
 286 tion 4.1. Detailed experimental setup and optimal hyperparameters are provided in Appendix A.
 287

288 4.1 DATASETS

289 **Fold Dataset.** We use the same dataset as in (Wang et al., 2025; 2022a; Hou et al., 2018; Hermosilla
 290 et al., 2020). In total, this dataset contains 16,292 proteins from 1,195 folds. There are three test
 291 sets used to evaluate generalization ability:
 292

- 293 • Fold: proteins from the same *superfamily* are unseen during training,
 294
- Superfamily: proteins from the same *family* are unseen during training,
 295
- Family: proteins from the same family are present during training.
 296

297 Among the three test sets, **Fold** is the most challenging since it differs the most from the training
 298 distribution. In this task, 12,312 proteins are used for training, 736 for validation, 718 for Fold,
 299 1,254 for Superfamily, and 1,272 for Family.
 300

301 **Reaction Dataset.** For reaction classification, the 3D structures of 37,428 proteins representing 384
 302 EC numbers are collected from the PDB database (Berman et al., 2000), and EC annotations for each
 303 protein are obtained from the SIFTS database (Dana et al., 2019). The dataset is split into 29,215
 304 proteins for training, 2,562 for validation, and 5,651 for testing. Every EC number is represented in
 305 all three splits, and protein chains with more than 50% sequence similarity are grouped together.
 306

307 **LBA Dataset.** Following (Somnath et al., 2021) and (Townshend et al., 2021), we perform lig-
 308 and binding affinity (LBA) prediction on a subset of the commonly used PDBbind refined set (Wang
 309 et al., 2004; Liu et al., 2015). The curated dataset of 3,507 complexes is split into train/validation/test
 310 splits based on a 30% sequence identity threshold to evaluate model generalization on unseen pro-
 311 teins. For each protein–ligand complex, we predict the negative log-transformed binding affinity:
 312

$$313 \quad pK = -\log_{10}(K),$$

314 where K is the binding constant measured in molar units.
 315

316 4.2 BASELINES

317 Our main point of comparison is the recent state-of-the-art method **SCHull** (Wang et al., 2025),
 318 which currently leads performance on fold, reaction, and binding affinity tasks. To contextualize our
 319 contributions, we also benchmark SSProNet against a representative spectrum of methods in protein
 320 graph learning. Below we briefly describe each:
 321

- 322 • **GCN** (Kipf, 2016): a classic semi-supervised GNN that propagates features layer by layer using
 323 a first-order spectral approximation.

324 Table 1: Accuracy (%) on protein fold and enzyme reaction classification tasks. *Avg. Time* is the
 325 average time per epoch (s). A dash (–) means not reported.
 326

327 Method	React	Avg. Time	Fold				Avg. Time
			328 Fold	Super	Family	Avg.	
329 GCN (Kipf, 2016)	67.3	–	16.8	21.3	82.8	40.3	–
330 IEConv (Hermosilla et al., 2020)	87.2	–	45.0	69.7	98.9	71.2	–
331 DWNN (Li, 2022)	76.7	–	31.8	37.8	85.2	51.5	–
332 GearNet (Zhang et al., 2022)	79.4	–	28.4	42.6	95.3	55.4	–
333 HoloProt (Somnath et al., 2021)	78.9	–	–	–	–	–	–
334 MACE (Battatia et al., 2022)	–	–	23.7	21.4	60.2	35.1	114
335 MACE+SCHull (Wang et al., 2025)	–	–	27.0	23.1	65.0	38.4	105
336 SEGNN (Brandstetter et al., 2021)	–	–	28.8	30.4	77.1	45.4	121
337 SEGNN+SCHull (Wang et al., 2025)	–	–	32.0	33.6	86.7	50.3	115
338 GVP-GNN (Jing et al., 2020)	65.5	320	16.0	22.5	83.8	40.8	106.3
339 GVP-GNN + SCHull (Wang et al., 2025)	77.1	345	24.5	27.1	88.0	47.1	111
340 ProNet-Amino-Acid (Wang et al., 2022a)	86.0	210	51.5	69.9	99.0	73.5	70.5
341 ProNet-Amino-Acid+SCHull (Wang et al., 2025)	87.9	221	52.2	73.9	99.2	75.1	69.3
342 ProNet-Backbone (Wang et al., 2022a)	86.4	213	52.7	70.3	99.3	74.1	74.1
343 ProNet-Backbone+SCHull (Wang et al., 2025)	88.1	230	56.1	74.6	99.4	76.7	75.8
344 SSProNet-Amino-Acid (Ours)	87.5	287	62.6	76.9	1.0	79.8	90.3
345 SSProNet-Backbone (Ours)	88.3	293	63.1	77.4	1.0	80.2	93.7

- 346 • **IEConv** (Hermosilla et al., 2020): uses a multi-graph representation combining structural connec-
 347 tivity and geometry, with a kernel that fuses intrinsic and extrinsic distances.
- 348 • **DWNN** (Li, 2022): an orientation-aware GNN with 3D directed weights, enabling explicit mod-
 349 eling of angular relations under equivariance.
- 350 • **GearNet** (Zhang et al., 2022): a geometry-aware residue graph encoder pretrained via contrastive
 351 and structural prediction tasks, which captures structural signals efficiently.
- 352 • **HoloProt** (Somnath et al., 2021): integrates surface geometry and residue topology in a multi-
 353 scale network, using superpixels to compress surface graphs and bridging layers in message pass-
 354 ing.
- 355 • **MACE** (Battatia et al., 2022): supports higher-order message passing (beyond pairwise) in an
 356 equivariant framework, reducing the depth required while retaining expressivity.
- 357 • **SEGNN** (Brandstetter et al., 2021): extends E(3) equivariant GNNs by allowing steerable node
 358 and edge features, processed by nonlinear steerable MLPs with tensorial combinations.
- 359 • **GVP-GNN** (Jing et al., 2020): replaces standard MLPs with Geometric Vector Perceptrons that
 360 jointly handle invariant scalars and equivariant vectors, enabling richer geometric reasoning.
- 361 • **ProNet** (Wang et al., 2022a): a hierarchical 3D graph architecture for proteins that ensures com-
 362 pleteness across amino acid, backbone, and all-atom levels. It employs hierarchical message
 363 propagation (Hier-Geom-MP) for flexible traversal across granularities.

364 4.3 TASK 1: FOLD CLASSIFICATION

365 Protein fold classification (Hou et al., 2018; Levitt & Chothia, 1976) is a fundamental task for un-
 366 derstanding protein structure–function relationships and evolutionary patterns. Following the dataset
 367 and experimental setup of (Wang et al., 2025), we evaluate our methods on this task. A detailed de-
 368 scription of the dataset is provided in Appendix 4.1. In total, the dataset comprises 16,712 proteins
 369 spanning 1,195 folds. It includes three test sets: Fold, Superfamily, and Family. We report the ac-
 370 curacies on each of these test sets, as well as their average, in Table 1. In line with (Wang et al.,
 371 2025), to examine how SSProNet facilitates the capture of global structural information, each test
 372 set is further divided into four subsets based on graph size, with node counts capped at 150, 300,
 373 450, and 600.

374 Table 1 demonstrates that on the FOLD dataset, SSProNet achieves the best accuracy on
 375 Fold/Superfamily/Family (63.10/77.42/100.0) and the highest average (80.17), surpassing the
 376 SCHull-based baselines (Wang et al., 2025) by +7.0, +2.82, +0.6, and +3.47 points, respectively.
 377 This comes with a ∼24–27% increase in per-epoch training time.

378 4.4 TASK 2: REACTION CLASSIFICATION
379

380 Enzymes are proteins that act as biological catalysts, and their functions are systematically classified
381 by enzyme commission (EC) numbers, which group enzymes according to the reactions they cat-
382 alyze (Omelchenko et al., 2010). In this experiment, we assess the SSProNet model on the reaction
383 classification task, using the same dataset and experimental setup as described in (Wang et al., 2025;
384 2022a). Further details on the dataset and the training, validation, and test splits are provided in
385 Appendix 4.1.

386 For the EC dataset, Table 1 shows that SSProNet-Backbone establishes a new state of the art, achiev-
387 ing the highest accuracy (88.3%) and surpassing the previous best ProNet-Backbone+ SCHull base-
388 line (88.1%) (Wang et al., 2025). This gain, although modest in absolute terms, confirms that our
389 secondary-structure-aware design improves generalization beyond existing methods. The improve-
390 ment comes at the cost of a moderate increase in runtime (about 27–35% per epoch).

391 4.5 TASK 3: LIGAND BINDING AFFINITY
392

393 Predicting protein–ligand binding affinity (LBA) is a fundamental task in drug discovery, with di-
394 rect impact on downstream applications such as virtual screening and lead optimization. For this
395 task, we adopt our integrated SSProNet model to predict LBA. The dataset is derived from PDB-
396 bind (Wang et al., 2004; Liu et al., 2015) following the experimental protocols outlined in (Wang
397 et al., 2025; Jing et al., 2020), and we use the default dataset split (see Appendix 4.1 for details).
398 Evaluation is conducted using multiple statistical metrics—RMSE, Pearson, Spearman, and Kendall
399 correlations—to assess how SSProNet improves the learning capacity and generalization of GNN-
400 based models.

401 Table 2: RMSE/Pearson Correlation/Spearman Correlation/Kendall Correlation on the LBA test set.
402 Avg. Time is the average running time per epoch. Arrows indicate whether lower or higher is better.
403 A dash (–) means not reported.
404

405 Method	406 LBA				407 Avg. Time
	408 RMSE (↓)	409 Pearson (↑)	410 Spearman (↑)	411 Kendall (↑)	
412 IEConv (Hermosilla et al., 2020)	413 1.554	414 0.414	415 0.428	416 –	417 –
418 HoloProt-Full Surface (Sommath et al., 2021)	419 1.464	420 0.509	421 0.500	422 –	423 –
424 HoloProt-Superpixel (Sommath et al., 2021)	425 1.491	426 0.491	427 0.482	428 –	429 –
430 GVP-GNN (Jing et al., 2020)	431 1.529	432 0.441	433 0.432	434 0.301	435 48.6
436 GVP-GNN + SCHull (Wang et al., 2025)	437 1.401	438 0.475	439 0.459	440 0.335	441 53.6
442 ProNet-Amino-Acid (Wang et al., 2022a)	443 1.455	444 0.536	445 0.526	446 0.465	447 31.7
448 ProNet-Amino-Acid+SCHull (Wang et al., 2025)	449 1.355	450 0.556	451 0.568	452 0.512	453 33.9
454 ProNet-Backbone (Wang et al., 2022a)	455 1.458	456 0.546	457 0.550	458 0.481	459 32.1
460 ProNet-Backbone+SCHull (Wang et al., 2025)	461 1.321	462 0.581	463 0.578	464 0.535	465 34.4
466 SSProNet-Amino-Acid (Ours)	467 1.354	468 0.607	469 0.601	470 0.487	471 47.3
472 SSProNet-Backbone (Ours)	473 1.382	474 0.613	475 0.616	476 0.498	477 54.7

478 As shown in Table 2, our SSProNet model establishes a new state of the art on the LBA benchmark.
479 In particular, SSProNet-Backbone achieves the highest correlation scores (Pearson = **0.613**, Spear-
480 man = **0.616**), surpassing the strongest SCHull (Wang et al., 2025) baseline by +0.032 and +0.038,
481 respectively. Although RMSE (1.382 vs. 1.321) and Kendall (0.498 vs. 0.535) remain slightly be-
482 low the best baseline, the improvements in correlation metrics are significant, demonstrating the
483 strength of our secondary-structure-aware design. These gains come with a moderate increase in
484 training time (54.7 s vs. 34.4 s per epoch, see Table 2).

485 4.6 ABLATION STUDIES
486

487 To better understand the contribution of individual design choices in SSProNet, we conduct ablation
488 experiments on the LBA dataset using the amino acid representation.

489 **Influence of the energy threshold.** As shown in Table 3, the choice of energy cutoff substantially
490 influences LBA performance. The most permissive threshold (–0.1 kcal/mol), which retains both
491 strong and weak hydrogen bonds, achieves the best overall results: RMSE = 1.336, Pearson = 0.612,
492 Spearman = 0.609, Kendall = 0.432. This suggests that weak hydrogen bonds still carry useful
493 geometric and interaction information that benefits predictive accuracy when included in the graph.

432 Table 3: Ablation study on the influence of the energy threshold for constructing H-bond edges.
 433 Results are reported on the LBA test set. Arrows indicate whether lower or higher is better.

435	436	437	LBA				438		
			439	440	441	442			
443	444	445	446	447	448	449	450	451	452
-0.1	1.336	0.612	0.609	0.432	57.3				
-1.5	1.354	0.605	0.601	0.424	47.9				
-2.5	1.354	0.607	0.601	0.424	45.8				
-3.5	1.349	0.605	0.601	0.426	43.7				

442 By contrast, more stringent thresholds (-1.5 to -3.5 kcal/mol) progressively exclude weaker bonds
 443 and lead to sparser graphs. While this reduces runtime (from 57.3 s at -0.1 to 43.7 s at -3.5 per
 444 epoch), it also slightly diminishes correlation metrics (Pearson ≈ 0.605 , Spearman ≈ 0.601 , Kendall
 445 ≈ 0.424 – 0.426). The results therefore reveal a clear trade-off: keeping weaker bonds improves the
 446 model’s ability to capture global affinity trends, whereas filtering them out yields time efficiency
 447 gains but weaker predictive consistency.

448 Compared to Table 2, the -0.1 setting surpasses our default SSProNet–Amino-Acid model on
 449 RMSE (1.336 vs. 1.354) and correlations (Pearson 0.612 vs. 0.607, Spearman 0.609 vs. 0.601),
 450 although Kendall correlation drops (0.432 vs. 0.487). Relative to the strongest SCHull (Wang et al.,
 451 2025) baseline, our ablation improves Pearson/Spearman but remains slightly behind in RMSE and
 452 Kendall.

453 4.7 EFFECT OF GRAPH TOPOLOGY AND DSSP-DERIVED FEATURES

454 Table 4: Ablation study on the effect of removing different information sources. Results are reported
 455 on the LBA test set (best epoch). Arrows indicate whether lower or higher is better.

456	457	458	459	460	LBA				461
					462	463	464	465	
Removing Radius Edges (H-bond only)	1.385	0.570	0.579	0.408					
Removing SS (keep ACC)	1.361	0.606	0.599	0.424					
Removing ACC (keep SS)	1.362	0.611	0.606	0.429					

466 Table 4 shows three ablations. First, removing the radius graph and keeping only hydrogen-bond
 467 edges degrades performance (RMSE = 1.385, Pearson = 0.570), indicating that proximity-based
 468 edges provide complementary structural context beyond H-bond connectivity.

469 Second, comparing the two node-annotation ablations reveals that *secondary structure (SS) is more*
 470 *useful than solvent accessibility (ACC)* for LBA. When we *remove ACC* but keep SS, we obtain the
 471 strongest correlations (Pearson = 0.611, Spearman = 0.606, Kendall = 0.429) with virtually the
 472 same RMSE as the w/o-SS variant (1.362 vs. 1.361). Conversely, *removing SS* yields slightly lower
 473 correlations (Pearson = 0.606, Spearman = 0.599, Kendall = 0.424). Taken together, these results
 474 suggest: (i) radius edges complement H-bonds and should be retained; (ii) SS carries the dominant
 475 DSSP signal for affinity prediction, while ACC contributes less.

476 5 CONCLUSION

477 We introduce SSProNet, a new graph neural network model that enriches node features with per-
 478 residue secondary-structure labels and adds hydrogen-bond edges on top of regular proximity based
 479 edges. Across Fold, Reaction, and LBA benchmarks, our model yields competitive and improved
 480 performance. Ablations identify the main drivers: radius-based proximity edges are indispensable
 481 for affinity prediction; secondary-structure cues contribute more than solvent accessibility; and per-
 482 missive H-bond thresholds that retain weaker bonds modestly improve generalization at a runtime
 483 cost. Overall, grounding protein graphs in biophysical interactions provides an effective inductive
 484 bias, improving both accuracy and interpretability.

486 REPRODUCIBILITY STATEMENT
487488 In this paper, we have provided implementation details in Section 4.1 and Appendix A. We will
489 provide the code upon request during the review process and promise to release the code upon the
490 paper’s publication.
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648 **A HYPERPARAMETER DETAILS & EXPERIMENTAL SETUP**
649650 This section describes the full experiment setup for each task considered in this paper. The imple-
651 mentation of our methods is based on the PyTorch (Paszke et al., 2019) and Pytorch Geometric (Fey
652 & Lenssen, 2019), and all models are trained with the Adam optimizer (Kingma & Ba, 2015). All
653 experiments are conducted on a single NVIDIA Tesla V100 32GB GPU. The search space for model
654 and training hyperparameters are listed in Table 5. Note that we select hyperparameters at the amino
655 acid and backbone levels by the same search space, and optimal hyperparameters are chosen by the
656 performance on the validation set.657 Table 5: Model and training hyperparameters for protein-related datasets.
658

659 Hyperparameter	660 React	661 Fold	662 LBA
663 Number of layers	664 3, 4, 5	665 3, 4, 5	666 3, 4, 5
667 Hidden channels	668 64, 128, 256	669 64, 128, 256	670 128, 192, 256
671 Cutoff	672 6, 8, 10	673 6, 8, 10	674 6, 8, 10
675 Dropout	676 0.2, 0.3, 0.5	677 0.2, 0.3, 0.5	678 0.2, 0.3
679 Epochs	680 500, 1000	681 500, 1000	682 500, 800
683 Batch size	684 16, 32	685 16, 32	686 8, 16, 32
687 Learning rate	688 1e-4, 5e-4	689 1e-4, 5e-4	690 5e-5, 1e-4, 2e-4
691 Learning rate scheduler	692 step_lr	693 step_lr	694 step_lr
695 Learning rate decay factor	696 0.5	697 0.5	698 0.5
699 Learning rate decay epochs	700 50, 100, 150	701 100, 150, 200	702 50, 100, 150

673 **B DSSP PREPROCESSING AND INTEGRATION**
675676 **Role of DSSP and how we use it.** The Dictionary of Secondary Structure of Proteins (DSSP) is a
677 long-standing standard for deriving residue-level annotations (secondary structure, hydrogen bonds,
678 solvent accessibility, backbone geometry) directly from 3D coordinates (Hekkelman et al., 2025).
679 In our pipeline we install DSSP locally (version 2.3.0) and use it to annotate each protein chain, then
680 feed those annotations into our graph construction and node features. Concretely, for each residue
681 we use: (1) the *primary secondary-structure code* (H, E, T, S, G, B, I; defaults to coil if
682 unassigned), (2) the *solvent-accessible surface area* (ACC), (3) backbone dihedrals (PHI, PSI), and
683 (4) *hydrogen-bond partners with energies*. These DSSP attributes allow us to complement purely
684 geometric proximity with biochemical constraints (e.g., hydrogen bonds) and physically meaningful
685 local context (ACC, dihedrals).
686687 **Example of produced .dssp output.** Below is a short excerpt from one of our generated DSSP
688 files (1b6v.A.dssp); columns are truncated for readability but show the key fields we use:
689

#	RESIDUE	AA	STRUCTURE	BP1	BP2	ACC	N-H-->O	O-->H-N	...	PHI	PSI	...
13	12	A	M	B	< +a	47	0A	9	-4, -2.3	2, -0.2	...	-100.3 123.4 ...
14	13	A	D		+	0	0	11	33, -2.7	3, -0.2	...	-135.7 79.8 ...
19	18	A	A	S	S-	0	0	39	61, -0.0	2, -0.7	...	-137.7 146.5 ...
22	21	A	S	S	> S-	0	0	77	1, -0.1	3, -2.0	...	72.1 115.0 ...
24	23	A	N	T	3> +	0	0	75	1, -0.1	4, -2.4	...	-100.8 6.1 ...

695 Each residue line includes: (i) indices and chain ID, (ii) amino-acid code (AA), (iii) the STRUCTURE
696 symbol (e.g., H helix, E strand, T turn, S bend), (iv) ACC (solvent accessibility), (v) hydrogen-bond
697 partners and energies for N-H→O and O→H-N (pairs like offset, energy), and (vi) backbone
698 geometry (PHI, PSI).
699700 **How we use these fields in our model.** We parse the produced .dssp files and attach their
701 information to each residue/node of the protein graph. Secondary structure is mapped to an 8-way
702 categorical label and one-hot encoded; ACC is kept as a scalar feature. Hydrogen-bond partners are

702 converted into additional *edges* in the graph: for each residue, we add edges to the residues indicated
703 by DSSP’s H-bond partners (using the provided offsets), optionally filtering by bond energy (more
704 negative indicates stronger bonding). These DSSP-derived edges are merged with the usual radius-
705 based proximity edges, duplicates are removed, and self-loops are dropped. On the node side, SS
706 and ACC are concatenated with the sequence/structure features used by SSProNet (amino-acid one-
707 hot; and, depending on the chosen level, backbone and/or side-chain embeddings). This way, the
708 model simultaneously “sees” short-range geometric contacts and longer-range biochemical links,
709 improving its capacity to capture secondary-structure regularities and nonlocal constraints (e.g., β -
710 sheet hydrogen-bonding).

712 C LLM USAGE DISCLOSURE

713 During the paper writing process, the authors utilize LLMs as tools to formalize word choice and
714 correct grammatical mistakes.

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