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# Exploring Time Granularity on Temporal Graphs for Dynamic Link Prediction in Real-world Networks

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## Abstract

Dynamic Graph Neural Networks (DGNNs) have emerged as the predominant approach for processing dynamic graph-structured data. However, the influence of temporal information on model performance and robustness remains insufficiently explored, particularly regarding how models address prediction tasks with different time granularities. In this paper, we explore the impact of time granularity when training DGNNs on dynamic graphs through extensive experiments. We examine graphs derived from various domains and compare three different DGNNs to the baseline model across four varied time granularities. We mainly consider the interplay between time granularities, model architectures, and negative sampling strategies to obtain general conclusions. Our results reveal that a sophisticated memory mechanism and proper time granularity are crucial for a DGNN to deliver competitive and robust performance in the dynamic link prediction task. We also discuss drawbacks in considered models and datasets and propose promising directions for future research on the time granularity of temporal graphs. Our benchmark suite and codebase are available at <https://github.com/SilenceX12138/Time-Granularity-on-Temporal-Graphs>.

## 1 Introduction

Evolving connections and relationships pervade real-world scenarios, encompassing recommendation systems [1, 2], social networks [3], transportation systems [4, 5, 6], epidemic transmission [7, 8], and more [9]. Temporal graphs (also known as dynamic or evolutionary networks) can effectively model these dynamics, with nodes, edges, edge types, and associated attributes continuously changing over time due to various events. Analysing temporal evolution and its patterns can facilitate reliable predictions and informed decisions [9, 10]. In contrast to traditional graph-based models that assume fixed graph structures, dynamic graph neural network methods (DGNNs) have emerged in recent years to enable more efficient representation learning on dynamic networks [11].

Time granularity significantly influences the level of detail at which temporal information is captured, processed, and represented in a model [10, 12, 13]. It critically affects model performance, robustness, computational efficiency, and transferability. However, its impact on temporal graph analysis remains under-explored. We underscore the importance of understanding the time granularity of temporal graphs in the following aspects: **(i) Model Performance:** Coarser time granularities may sacrifice critical temporal information, whereas finer granularities could introduce noise into the training process [14]. Identifying the optimal choice of time granularity for a specific task can enhance model performance. **(ii) Robustness:** Assessing models at various time granularities enables evaluation of their robustness to information loss, which is crucial for determining how models generalise across time scales [14, 10] and their sensitivity to the provided temporal information. **(iii) Computational**

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**Efficiency:** Fine-grained models can be computationally intensive and slow to train due to numerous training instances; coarser granularities can reduce computational demands while retaining valuable insights [15]. Balancing granularity and efficiency can expedite the temporal graph analysis process. **(iv) Transferability:** Knowledge acquired at different time granularities can be transferred between domains and tasks [14, 16, 17]. Hence, understanding the impact of time granularity could assist researchers in selecting and adapting models for specific problems.

In this study, we focus on a fundamental task in dynamic graph analysis: dynamic link prediction. This task seeks to predict future connections and interactions based on prior and current information. While state-of-the-art (SOTA) methods [18, 19, 20] can achieve near-perfect performance on this task, previous studies [21] have shown that incorporating more challenging negative sampling techniques significantly reduces the performance of existing SOTA models. We extend this research by considering the impact of time granularity. Our primary objective is to provide a comprehensive understanding of how these models process temporal information and address the link prediction task in the absence of sufficiently fine-grained information. Our main contributions are as follows:

- We introduce a novel data-splitting approach that jointly considers durations and the coarsest common time granularities across different dynamic graphs. This framework ensures a fair comparison among various graphs without information leakage issues.
- We empirically investigate DGNNs’ performance and robustness under four predetermined time granularities. We conduct a series of controlled experiments, taking into account model architectures, dataset domains, and negative sampling strategies.
- We perform cross-granularity evaluations on trained models across different time granularities to gain a deeper understanding of the models’ mechanisms for processing temporal information at various granularity levels.
- We provide an insightful discussion on the identified problems and innate weaknesses for the model design and datasets.

## 2 Related Work

**Dynamic Graph Representation Learning** Over the past decade, learning effective representations that capture both structural properties and temporal information in dynamic graphs has been extensively studied, driven by the growing interest in temporal graphs. Several survey papers [22, 23, 9] document the advancements in this research field, offering various taxonomies for classifying different types of dynamic graphs based on network characteristics and domains. Numerous Dynamic Graph Neural Networks (DGNNs) have been proposed to address long-standing challenges in representation learning: (i) incorporating diverse types of events, and (ii) integrating temporal information into node, edge, or graph embeddings. These DGNNs can be broadly categorised into four groups: Recurrent Neural Network (RNN)-based methods [24, 19], memory-based methods [25, 26], attention-based methods [27, 28, 29], and convolution-based methods [30, 31]. In this study, we mainly focus on the Temporal Graph Networks (TGNs) because they generalise Message Passing Neural Networks (MPNNs) to temporal graphs with effective memory mechanism [18].

**Time Granularity for Graphs** Time granularity, which refers to the temporal resolution or time intervals at which dynamic graphs are observed or analyzed, significantly impacts the effectiveness of dynamic graph analysis by determining the level of temporal detail retained. Chapter 3 of the Handbook of Temporal Reasoning in AI [32] delivers a comprehensive introduction to time granularity and its applications in various domains. The authors present a mathematical formalization of the concept and provide a thoughtful discussion on the changes in semantic meanings of objects or concepts due to varying time granularities. In video representation learning, one pioneering work addresses the problem of choosing temporal granularity with advanced architectures. Specifically, Qian et al. [14] demonstrate that proper granularity is task-dependent and coarse-grained features can be effective for many tasks where fine-grained data are considered to be necessary.

The study of time granularity in dynamic graphs has attracted increasing attention in recent years [33, 21]. The pioneering work of Holme and Saramäki [34] in 2012 initiated the exploration of graph time granularity, examining the trade-offs between coarse and fine temporal resolutions. Concurrently, Casteigts et al. [35] investigated the impact of time granularity on graph structures and expressivity, evaluating scenarios with varying waiting times for information transition. Additionally, Skarding et al. [23] introduced a taxonomy for representing various temporal graphs across different

time granularities based on link duration. In recent years, several studies [36, 37, 38, 27] have presented novel time-aware embedding methods, primarily aimed at transforming static embeddings into continuous embeddings using temporal information with the consideration on different time intervals. This study aims to provide some insights into the impact of time granularity on learning representations from temporal graphs by focusing on the dynamic link prediction task.

### 3 Notations and Formalism

A dynamic graph  $\mathbf{G}_D$ , also known as a temporal graph, can be perceived as a sequence of operations guided by an ordered series of events acting upon the initial graph state  $\mathbf{G}_0$  (a Continuous-time Dynamic Graph  $\mathbf{G}_{CT}$ ), or a stream of snapshots over predetermined time slices (a Discrete-time Dynamic Graph  $\mathbf{G}_{DT}$ ). A continuous-time temporal graph can be formally defined as  $\mathbf{G}_{CT} = (G_0, O)$ , where  $G_0$  represents the initial state and  $O = \{(u_i, v_i, x_i, t_i, \Delta i), i = 1, 2, \dots\}$  indicates a sequence of events occurring at arbitrary time point. In this notation,  $(u_i, v_i)$  represents the pair of nodes involved in the  $i$ -th event,  $x_i$  denotes any feature associated with the event, including node and edge features, event types (communication, interaction, or other topological changes), and associated operations such as node/edge addition or deletion,  $t_i$  marks the event’s initiation timestamp, and  $\Delta i$  represents the event’s duration. In contrast, a discrete-time temporal graph can be expressed as an ordered sequence of  $N$  graph snapshots  $\mathbf{G}_{DT} = (G_0, G_1, \dots, G_N)$ . Each  $G_i$  in the sequence may capture a snapshot of the graph at a specific time point  $t_i$  or model the graph’s state during the time interval  $[t - \Delta t, t]$  for a configurable  $\Delta t$ . In the latter case,  $\mathbf{G}_i = (\oplus V_i, \oplus E_i, \oplus X_i, (t_i - t_{i-1}))$  offers an aggregated view of the dynamic graph  $\mathbf{G}_{TD}$  over the specified time interval, with  $\oplus$  denoting any possible method of combining events occurring within that time frame. The time interval may be fixed to represent different time granularities or adjusted over time to create overlapping snapshots, thereby facilitating more sophisticated analyses of the dynamic network.

In line with the data processing procedure in Poursafaei et al.’s work [21], we eliminate all node and edge features from the graph data and focus exclusively on edge additions while assuming their permanence. This approach streamlines the events to be  $O = \{(u_i, v_i, t_i), i = 1, 2, \dots\}$ . Furthermore, by permitting multiple identical edges between any pair of nodes, we can express any  $G_i \in G_{TD}$  as:

$$\begin{aligned} \oplus E_i &= \oplus E_{i-1} \uplus \{(u, v) \mid \exists t \in (t_{i-1}, t_i] \text{ s.t. } (u, v, t) \in O\} \\ \oplus V_i &= \cup \{u, v \mid (u, v) \in \oplus E_i\}, \end{aligned} \tag{1}$$

where  $\uplus$  is the union operation on multisets, signifying the multiplicities of edges in  $\oplus E_i$ ;  $\cup$  is the standard union operation for the set of vertices. This equation represents the aggregated view of the graph from time  $t_{i-1}$  to  $t_i$ , making it equivalent to an instantaneous snapshot of the graph at time  $t_i$ .

## 4 Methods

### 4.1 Datasets

In this study, we examine seven datasets of varying sizes from diverse domains, including social, interaction, and proximity. These datasets are widely employed for training and evaluating dynamic graph neural networks (DGNNs). Each dataset comprises directed edges listed by Unix timestamp, without any associated node or edge features. Additionally, the number of nodes in these datasets remains constant over time, simplifying the research scenario to focus exclusively on dynamic link predictions. Table A.1 in Appendix A.1 provides detailed statistics, as well as the semantic meanings of nodes and edges for each dataset.

To process the datasets, we first follow prior work [21] and aggregate their edges from the finest time granularity (second) to coarser granularities (minute, hour, day, month, year), and then adopt a 0.7-0.15-0.15 chronological split for training, validation, and test sets. The comprehensive breakdown is available in Appendix A.2. Our analysis reveals that "Day" represents the coarsest time granularity in this study, as it can meaningfully split all datasets without altering the semantic meanings of the original data. In contrast, the other coarser granularities might lead to insufficient samples of validation/test splits, e.g., the "Month" granularity of the Wikipedia dataset.

Table 1: Datasets split by "Day" with the split rate of 2/3-1/6-1/6 with respect to the number of days for training, validation, and testing.

Dataset	Train		Validation		Test		Total	
	# Days	# Edges	# Days	# Edges	# Days	# Edges	# Days	# Edges
Wikipedia	20	99,701	5	26,697	5	26,359	30	152,767
Reddit	20	432,543	5	110,004	5	126,518	30	669,075
MOOC	20	216,364	5	65,815	5	63,421	30	345,610
LastFM	1,216	916,312	304	340,736	305	26,566	1,825	1,284,223
Enron	730	6,224	182	6,357	183	10,051	1,095	22,997
Social Evo.	160	268,758	40	136,849	40	160,325	240	566,012
UCI	130	55,202	32	2,402	34	1,307	196	58,977

Therefore, we choose to divide the datasets by "Day". Specifically, we first split datasets by "Day" granularity with an approximate splitting rate equal to 2/3-1/6-1/6 for training, validation, and test sets. Within each data split, we further aggregate the events that happen within the same time interval according to the given granularity (second, minute, hour or day). This splitting mechanism effectively prevents data leakage issues, as the datasets for different time granularities are split at the identical timestamp. Simultaneously, the semantics of the edges remain unchanged, enabling fair cross-granularity comparisons. Table 1 outlines the specific dataset splits.

## 4.2 Evaluation Metrics

In order to provide a fair comparison, we employ the same evaluation metrics (AU-ROC and AP) as the benchmark paper [21] to assess the performance of the models. AU-ROC [39] (Area Under the Receiver Operating Characteristic Curve) summarizes the ROC curve into a single number that describes the performance of a model for multiple thresholds at the same time; while AP (Average Precision) is calculated as the weighted mean of precisions at each threshold. Both metrics range from 0 to 1, with higher scores indicating better performance. They are widely utilized in dynamic link prediction tasks due to their robustness against imbalanced data distribution and their adaptability across various classification thresholds.

## 4.3 The Baseline and DGNNs

As a natural extension of [21], we retain the EdgeBank [21] as our baseline and select three Dynamic Graph Neural Networks (DGNNs) for comparison, namely JODIE [19], DyRep [40], and TGN [18]. Note that EdgeBank is a non-parametric approach purely based on memorization, and other approaches are specifically designed to handle dynamic graphs and have achieved state-of-the-art performance in link prediction at the time of their release.

**EdgeBank [21]** stores observed edges in a dictionary and updates its memory at each timestamp. It predicts a test edge as positive if this edge was seen before and negative otherwise. It has two variants: **EdgeBank<sub>∞</sub>** stores all observed edges in memory and is more adept at identifying rare edges, while **EdgeBank<sub>tw</sub>** only remembers edges from the short-term past. We set the time window to be the same size as the validation set in our experiments. EdgeBank is a simple but strong baseline in the link prediction task; the recent work [21] argues that any valid DGNN method should outperform EdgeBank.

**JODIE [19]** tackles graph dynamics by predicting the embedding trajectory in temporal interaction networks. It captures the time-evolving nature of the interactions by jointly learning the embeddings and their projections in time, allowing the model to adapt to changes in the graph structure. By incorporating a recurrent architecture with a dedicated update mechanism, JODIE can efficiently learn and update node embeddings, making it highly effective in capturing temporal dependencies and predicting future interactions in dynamic graphs.

**DyRep [40]** introduces a novel framework that captures both topological and temporal dependencies by employing a graph attention mechanism for structural information and a point process-based approach for temporal dynamics. DyRep can learn node embeddings that effectively represent both the graph structure and the temporal evolution, allowing the model to generalise well on various dynamic graph tasks.

**TGN [18]** provides a generic, scalable and efficient framework to model dynamic graphs. It addresses the challenges of dynamic graphs by incorporating memory modules and a message-passing mechanism that can capture both structural and temporal information. The memory modules store historical node embeddings, while the message-passing mechanism allows nodes to exchange information with their neighbours. TGN can efficiently handle dynamic graphs by employing a combination of attention mechanisms and temporal aggregators to learn node representations that capture the local and global temporal dependencies.

#### 4.4 Negative Sampling

In this research, we employ the three negative sampling strategies proposed in [21] to conduct a comprehensive and robust evaluation of various methods across multiple time granularities. Specifically, **Random Negative Sampling (RandNS)** involves selecting negative edges at random from any node pairs within the graph. **Historical Negative Sampling (HistNS)** chooses negative edges that are previously observed but do not recur in the current testing phase, with the aim of assessing the model’s ability to predict recurring edges. **Inductive Negative Sampling (InduNS)** evaluates the model’s capacity to handle reoccurrence patterns of unseen edges by constructing edges not observed during training. The latter two sampling techniques address the inherent limitations of random sampling and challenge DGNNs in more stringent settings. Furthermore, these strategies do not interfere with time granularity, thus allowing us to maintain focus on this crucial aspect while still benefiting from the robustness offered by the diverse negative sampling approaches.

### 5 Experiment Results & Discussion

We conducted extensive experiments to evaluate the performance and robustness of various models for the dynamic link prediction task under different settings. Specifically, we trained baseline models and selected DGNN models on each dataset with four predetermined time granularities, resulting in a total of 140 models (5 methods  $\times$  7 datasets  $\times$  4 time granularities). To differentiate the models by their time granularity, we added a suffix (-s, -m, -h, or -d) to the model names, indicating training at the second, minute, hour, and day time granularities, respectively. We then evaluated the trained models across different time granularities for each of the three negative sampling settings. For example, a TGN model trained on the Wikipedia dataset under the "second" time granularity (TGN-s) would be compared with two baselines and two other competitive models (JODIE-s & DyRep-s) trained under the same setting, as well as with other TGNs (TGN-m/h/d) trained at different time granularities. Each comparison was conducted in three negative sampling settings to obtain a comprehensive view and a comparative ranking of the given model.

We tested models trained on fine-grained time granularities (referred to as "**fine models**", while models trained on coarse-grained time granularities are called "**coarse models**" in the following text) on coarse-grained test sets to examine the significance of time granularity in message passing and model training. We anticipated that fine models should achieve at least the same performance as coarse models when tested on the corresponding coarse time granularity used to train the coarse models. We also evaluated coarse models on fine-grained test sets to investigate their robustness to changes in time granularity. We expected that the performance of coarse models would be limited by the corresponding fine models’ performance due to the inevitable and irrecoverable information loss. Simultaneously, we calculated the relative gain or loss in performance when a model was tested on a time granularity different from the one used in its training.

All experiments were conducted using the same training configuration and hyperparameters to maintain consistency and comparability across the results; for more details, refer to Appendix A.3. The experiments were performed on Google Colab utilizing an A100 GPU, and the reported outcomes represent the average results obtained over three runs.

#### 5.1 Overall Performance of Dynamic Link Prediction

Table 2 shows the average rankings for model performance on different granularities based on AU-ROC. The model rankings for AP are consistent with the results obtained for AU-ROC. To conduct a meticulous evaluation of models trained on diverse granularities and negative sampling strategies, we have incorporated 24 supplementary tables presenting numerical results in Appendix B. Each table presents the numerical performance of different models under various time granularities for

Table 2: Average rank of AU-ROC on dynamic link prediction for different time granularities over three negative sampling strategies. Note that the top three methods are coloured by **First**, **Second** and **Third** respectively. Note that the absolute difference between any two given methods can be determined by calculating the difference in their numerical scores in Appendix B.

Granularity	Second			Minute			Hour			Day		
	Rand	Hist	Indu	Rand	Hist	Indu	Rand	Hist	Indu	Rand	Hist	Indu
NS												
JODIE-s	<b>3</b>	11	9	<b>2</b>	11	9	<b>3</b>	11	10	4	12	11
DyRep-s	12	7	6	11	7	6	14	7	6	14	7	5
TGN-s	6	<b>2</b>	<b>1</b>	5	<b>1</b>	<b>1</b>	6	5	<b>3</b>	9	5	4
JODIE-m	<b>1</b>	12	14	<b>1</b>	12	12	<b>2</b>	13	14	<b>1</b>	13	12
DyRep-m	13	9	8	12	8	7	13	8	7	12	9	8
TGN-m	5	<b>1</b>	<b>2</b>	4	<b>2</b>	<b>2</b>	7	5	4	7	4	<b>3</b>
JODIE-h	<b>2</b>	14	11	<b>3</b>	14	14	<b>1</b>	14	13	<b>2</b>	14	14
DyRep-h	14	8	7	13	6	5	11	6	5	13	8	6
TGN-h	8	5	<b>3</b>	7	5	<b>3</b>	5	<b>1</b>	<b>1</b>	6	<b>3</b>	<b>2</b>
JODIE-d	4	13	12	6	13	13	4	12	11	<b>3</b>	11	13
DyRep-d	11	6	5	14	9	8	12	9	8	11	6	7
TGN-d	9	4	4	10	4	4	8	<b>2</b>	<b>2</b>	5	<b>1</b>	<b>1</b>
EdgeBank <sub>tw</sub>	7	<b>3</b>	13	8	<b>3</b>	11	9	<b>3</b>	12	8	<b>2</b>	10
EdgeBank <sub>∞</sub>	10	10	10	9	10	10	10	10	9	10	10	9

each selected dataset, employing a specific negative sampling technique. These tables also exhibit the corresponding variations between different runs of experiments, as measured by standard deviation <sup>2</sup>. The performances of the models are ranked, and the average rankings are consolidated in Table 2.

We also notice that JODIE-x (including "JODIE-s", "JODIE-m", "JODIE-h", and "JODIE-d") models surpass other models across all granularities when the test set is randomly sampled. However, under alternative negative sampling strategies, their performance declines significantly, ranking near the bottom. DyRep-x models maintain consistent performance across all granularities. Although they do not have remarkable performance in any specific dataset, DyRep-x slightly outperforms JODIE-x in HistNS and InduNS settings. TGN-x demonstrates stable, robust performance across all datasets in any negative sampling setting and exhibits a substantial lead in challenging test environments. EdgeBank remains a competitive baseline in our experiments, particularly in the HistNS setting, where EdgeBank with a fixed time window, secures the top position.

## 5.2 Cross-granularity Comparison

It is noteworthy that certain coarse models achieve comparable or even marginally superior performance than their fine counterparts when evaluated on fine-grained test sets. For instance, JODIE-m and JODIE-h achieve similar performance to JODIE-s when tested on the "second" time granularity for all datasets. Likewise, TGN-s and TGN-m demonstrate no significant performance discrepancies in both the "second" and "minute" granularities. In fact, TGN-m yields marginally higher scores on the MOOC and LastFM datasets. These counter-intuitive instances indicate that training on the finest granularity may not always be the optimal choice, as fine-grained timestamps may not provide useful information for the underlying task and could introduce additional noise during training.

Another important observation is that the distance between the target time granularity and the current time granularity used in training has a considerable impact on model performance. For example, when handling predictions in the "day" time interval, a model trained in "day" or "hour" granularities typically outperforms models trained at finer granularities ("second" and "minute"), despite the coarse model experiencing information loss.

## 5.3 Model Design and Performance

To investigate the reasons behind performance gaps among the selected DGNNs, we explored their internal architectures for memorization and message passing. TGN selectively stores the memory for previously encountered edges through the forget gates in Gated Recurrent Units (GRUs), allowing it to remember crucial interactions over long distances while mitigating memory strain due to repeated updates. In contrast, JODIE and DyRep employ vanilla RNNs to memorize previous edges, with each

<sup>2</sup>Some standard deviations reported in the Appendix B are rounded to 0.000 due to their extremely small magnitudes ( $< 1e - 3$ ), aiming to maintain a neat and uniform format across all tables.

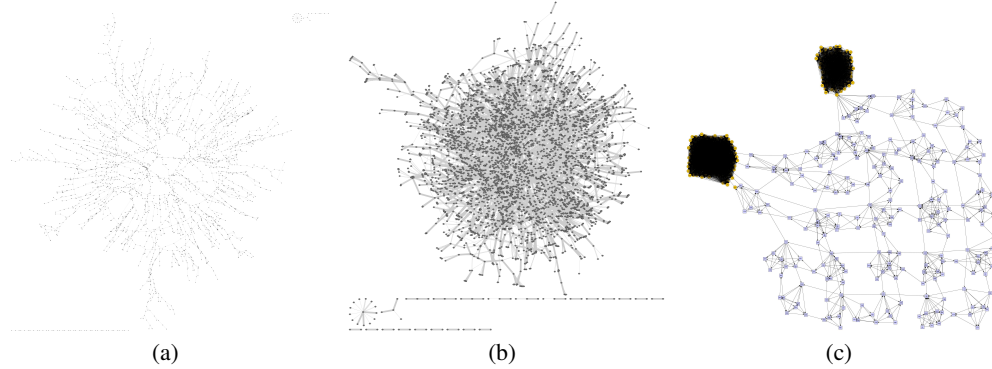


Figure 1: An example of "hairball" graph due to repetitive edge additions and aggregation. (a) Original Wikipedia graph used in our experiment (no edge repetition); (b) The "hairball" visualisation of the Wikipedia graph under our edge aggregation method; (c) A synthetic example of a globally sparse but locally dense graph, containing multiple "black holes". (a) and (b) are visualised using the Backbone layout [41] in Visone [42] without edge sparsification. The width of the edge indicates the number of communications between two designated nodes. (c) is visualised using the Organic layout [43] in yEd [44].

update potentially diluting their memory. This explains why TGN-x models consistently achieve strong and robust performance across various time granularities under different testing environments. DyRep-x models consistently rank lower in performance within the scope of our experiment. One plausible explanation for this is that when computing new messages for newly occurring events, DyRep disregards the interactions between the event and the destination node, while the other two approaches thoroughly consider both the involved nodes' embeddings, interactions and previous memory. To summarize, although JODIE and DyRep can be conceptualized as special cases of TGN, our experimental insights underscore that TGN offers a highly adaptable framework for addressing a wide range of dynamic network-related tasks across various domains.

All selected DGNNs update their node embeddings and memories for each batch during training. Given that no edge merging or de-duplication operations occur, the total number of training instances remains consistent for all models trained at different time granularities (refer to Section 3 for the edge aggregation method used in our experiments). This suggests that all models share the same complexity, and differences in training time can be disregarded. In our experiments, no trade-off exists between computational costs and model performance. Instead, we purely focus on evaluating whether the model can effectively address the problem at finer time granularities when the corresponding time information is eliminated. However, one could argue that these models, particularly the TGN-x models, capture superficial patterns from training instances, akin to "short-cut" learning observed in other research domains. As the total training instances remain unchanged, the model may attempt to recover lost timestamp information from the input sequence, leveraging the learned ordering information to predict link existence at finer granularities.

#### 5.4 Drawbacks of Benchmark Datasets

In all cases except for the RandNS setting, where test samples are too simplistic to differentiate between various methods, we observe a model's performance ranking on one dataset to be approximately consistent with its rankings on other datasets. This observation can be reasonably attributed to the fact that all selected datasets are large, complex networks extracted from the real world. Despite classifying them into different domains based on their associated meanings, these scale-free networks, which exhibit a power-law degree distribution, share many topological characteristics. It limits our capabilities in evaluating the model's robustness over varied time granularities across different network structures.

In our experiments, we consider dynamic graphs without edge or node deletion events and with edges added sequentially, resulting in a high prevalence of duplicated edges. Table 1 illustrates that, in extreme cases, over 90% of the edges are duplicated. In addition, our edge aggregation method ensures that each snapshot of the dynamic graph contains all edges present in the previous steps. Consequently, although the original graph in our datasets is sparse, as demonstrated in Fig. 1(a), the addition of numerous repeated edges transforms it into a complex "hairball" graph, shown in Fig. 1(b). Hairball graphs [45], characterized by overlapping and entangled vertices and edges, hinder the identification of meaningful patterns or structures and impede graph analysis.

Under our assumptions and simplifications, the aggregated view of the dynamic graph over time becomes a globally sparse but locally dense graph, containing multiple "black holes" due to repeated edge addition, as illustrated in Fig. 1(c). The majority of the edges reside in these "black holes," leading to biased link prediction. This could partially explain the decent performance of all selected models in the RandNS setting. These models may not require any understanding of temporal information; instead, for any sampled edge within a "black hole," the models can confidently predict it as Positive, otherwise as Negative. The InduNS approach mitigates this issue to some extent, resulting in a noticeable decrease in model performance. We question whether the selected models can truly capture temporal information under our edge aggregation method and RandNS setting, let alone manage time granularities. More experiments are needed to verify our conjecture.

Our experimental results highlight significant differences in model performance with the benchmark paper [21], particularly for HistNS and InduNS settings. Given that each method converges within 20 epochs and the performance standard deviations among different runs are minimal, we attribute these discrepancies in model performance primarily to different data splitting mechanisms and unbalanced distribution of edge occurrence over time shown in Table 1.

**Limitations** This research inherits several limitations from previous relevant study [21]. Firstly, all datasets were partitioned at a single point, which is a common practice but potentially weakens the influence of temporal information on the underlying task. Secondly, all models were evaluated in a transductive setting where all nodes were seen during training. Thirdly, our evaluation only focused on a narrow aspect of dynamic network analysis, specifically dynamic link prediction, thereby limiting the scope of our findings to this particular area. Our research also uncovered new limitations. We observed that all selected DGNNs share a similar training pipeline, and all datasets are structurally analogous. These factors restricted our ability to conduct a more comprehensive analysis of model performance. Therefore, our conclusions are limited to a specific type of graph and a specific category of GNNs. Another huge barrier lies in the high demand for computation resources. The number of experiments grows four times compared with the previous work, and each model requires an enormous amount of time for training and evaluation.

## 6 Conclusion & Future Work

In this study, we explored the influence of time granularity on dynamic link prediction tasks. Our methodology encompassed comprehensive experiments using EdgeBank as the baseline model, along with three dynamic graph neural networks (DGNNs) - JODIE, DyRep, and TGN - trained across seven datasets at four distinct time granularities (second, minute, hour, and day). The evaluation included three negative sampling strategies and extensive cross-granularity testing to assess the models' robustness against varying time information. Our findings revealed that TGN consistently outperformed other models across different settings, attributable to its sophisticated memorization mechanism and message-passing pipeline. Notably, we observed that models with coarser granularity sometimes matched or even exceeded the performance of finer-grained models, suggesting that fine-grained time information is not always beneficial and might introduce noise.

Our research marks a foundational step in understanding the role of time granularity in dynamic graph analysis, and there is significant potential for further investigation. Recent advancements in sophisticated models, including TREND [46], NAT [47], and CAWs [20], present opportunities for future exploration. Extending our experimental framework to different types of dynamic graphs across various domains and incorporating diverse model architectures would enrich our understanding of this field. Furthermore, conducting node-level or graph-level experiments could offer a more holistic view of time granularity's impact on dynamic graph analysis.

Some innovative modifications of our pipeline, such as avoiding fixed point split for datasets [48], modifying edge aggregation methods, or eliminating negative sampling for graphs with smaller scales [48], are promising directions for future research. Another intriguing possibility is to aggregate events within coarser time intervals, remove duplicate edges, and record occurrence frequencies or probabilities. This approach could reduce computational demands and enable more sophisticated prediction tasks, such as estimating the number of events (e.g., number of flights between cities) within a specified timeframe. Finally, considering the uneven distribution of edge occurrences, there is scope for designing models that aggregate events in a data-driven manner. Employing learnable time granularity, as opposed to deterministic aggregation at pre-set timestamps, could lead to more nuanced and effective dynamic graph analyses.



## 7 Acknowledgements

The authors would like to thank Prof. Pietro Lio, Dr. Petar Veličković, Dr. Farimah Poursafaei, and Shenyang (Andy) Huang for their insightful discussions regarding this work and valuable suggestions on polishing earlier versions of the manuscript.

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# Appendix for submission “Exploring Time Granularity on Temporal Graphs for Dynamic Link Prediction in Real-world Networks”

## A Reproducibility

### A.1 Real-word Datasets

Table A.1: Datasets Statistics with associated semantic meanings.

Dataset	Domain	Node	# Nodes	Edge	Total Edges	Unique Edges	Unique Steps	Duration
Wikipedia [19]	Social	Editors & Wiki Pages	9,227	Editing Request	157,474	18,257	152,757	1 Month
Reddit [19]	Social	Users & Posts	10,984	Posting Request	672,447	78,516	588,918	1 Month
MOOC [19]	Interaction	Students & Online Courses	7,144	Accessing a online course	411,749	178,443	345,600	1 Month
LastFM [19]	Interaction	Users & Songs	1,980	Listening a song	1,293,103	154,993	1,283,614	4 Years
Enron [49]	Social	Employees	184	Email communication	125,235	3,125	22,632	3 Years
Social Evo. [50]	Proximity	Students	74	Cellphone calls	2,099,519	4,486	565,932	1 Year
UCI [51]	Social	Students	1,899	Online Chats	59,835	20,296	58,911	196 Days

### A.2 Data Distribution

Table A.2: Data distribution in a 0.7-0.15-0.15 chronological split for different time granularities.

Granularity	Wikipedia			Reddit			MOOC		
	Train	Val	Test	Train	Val	Test	Train	Val	Test
Second	110,232	23,621	23,621	470,713	100,667	100,867	288,224	61,762	61,763
Minute	110,237	23,620	23,617	470,722	100,858	100,867	288,224	61,770	61,755
Hour	110,368	23,754	23,352	470,815	101,296	100,336	288,480	62,271	60,998
Day	112,937	22,904	21,633	475,299	114,325	82,823	301,509	62,868	47,372
Month	153,823	0	3,651	650,442	0	22,005	411,749	0	0
Year	157,474	0	0	672,447	0	0	411,749	0	0

Granularity	LastFM			Enron			Social Evo.			UCI		
	Train	Val	Test	Train	Val	Test	Train	Val	Test	Train	Val	Test
Second	905,172	193,965	193,966	87,664	18,786	18,785	1,469,665	314,930	314,924	41,884	8,975	8,976
Minute	905,174	193,963	193,966	87,664	18,786	18,785	1,469,671	314,924	314,924	41,885	8,974	8,976
Hour	905,232	193,919	193,952	87,665	18,808	18,762	1,470,682	314,396	314,441	41,895	8,964	8,976
Day	905,232	194,399	193,472	87,743	18,971	18,521	1,474,123	317,858	307,538	42,079	8,790	8,966
Month	936,951	182,053	174,099	89,523	24,162	11,550	1,668,041	424,508	6,970	49,409	3,323	7,103
Year	1,159,991	0	133,112	105,631	19,604	0	2,099,519	0	0	59,835	0	0

### A.3 Hyperparameters in Model Training

Table A.3: Training Configuration & Hyperparameter Setting for Experiments.

Hyperparameter	Value
Learning Rate	0.0001
Optimizer	Adam
Batch Size	200
Number of Epoches	20
Tolerance for Early Stopping	5 Epoches
Dropout Rate	0.1
Attention Heads	2
Node Embeddings	100
Time Embeddings	100
Memory Dimension (TGN)	172
Message Dimension (TGN)	100
Number of Runs	3

## B Numerical Results of Cross-granularity Evaluation

Table B.4: AU-ROC of dynamic link prediction on the "second" granularity data across three negative sampling strategies. Note that we report the mean AU-ROC over three runs with the standard deviations in parenthesis, and the rank is computed by averaging the ranks over all datasets.

(a) Random Sampling								
Method	Wikipedia	Reddit	MOOC	LastFM	Enron	Social Evo.	UCI	Rank
JODIE-s	0.992 (0.001)	0.999 (0.000)	0.857 (0.015)	0.999 (0.000)	0.930 (0.005)	0.996 (0.000)	0.994 (0.001)	3
DyRep-s	0.681 (0.010)	0.566 (0.000)	0.606 (0.005)	0.505 (0.009)	0.643 (0.011)	0.679 (0.053)	0.833 (0.001)	12
TGN-s	0.979 (0.001)	0.961 (0.000)	0.789 (0.012)	0.694 (0.013)	0.808 (0.019)	0.923 (0.001)	0.901 (0.006)	6
JODIE-m	0.993 (0.000)	0.999 (0.000)	0.865 (0.007)	0.999 (0.000)	0.926 (0.002)	0.995 (0.001)	0.995 (0.000)	1
DyRep-m	0.677 (0.011)	0.561 (0.000)	0.588 (0.010)	0.495 (0.005)	0.634 (0.019)	0.696 (0.015)	0.837 (0.008)	13
TGN-m	0.978 (0.001)	0.955 (0.000)	0.805 (0.029)	0.695 (0.016)	0.807 (0.020)	0.869 (0.007)	0.903 (0.039)	5
JODIE-h	0.992 (0.001)	0.996 (0.000)	0.845 (0.018)	0.997 (0.000)	0.923 (0.017)	0.914 (0.000)	0.995 (0.001)	2
DyRep-h	0.640 (0.011)	0.496 (0.000)	0.590 (0.012)	0.503 (0.000)	0.593 (0.057)	0.701 (0.000)	0.829 (0.016)	14
TGN-h	0.960 (0.001)	0.928 (0.000)	0.688 (0.000)	0.684 (0.000)	0.764 (0.027)	0.562 (0.000)	0.813 (0.023)	8
JODIE-d	0.976 (0.001)	0.886 (0.000)	0.623 (0.000)	0.928 (0.000)	0.920 (0.004)	0.633 (0.000)	0.994 (0.001)	4
DyRep-d	0.582 (0.032)	0.462 (0.000)	0.591 (0.000)	0.505 (0.000)	0.649 (0.006)	0.513 (0.000)	0.835 (0.009)	11
TGN-d	0.944 (0.005)	0.923 (0.000)	0.570 (0.000)	0.602 (0.000)	0.795 (0.016)	0.595 (0.000)	0.836 (0.024)	9
EdgeBank <sub>tw</sub>	0.888 (0.000)	0.924 (0.000)	0.607 (0.000)	0.840 (0.000)	0.867 (0.000)	0.600 (0.000)	0.733 (0.000)	7
EdgeBank <sub>∞</sub>	0.911 (0.000)	0.954 (0.000)	0.548 (0.000)	0.827 (0.000)	0.858 (0.000)	0.538 (0.000)	0.749 (0.000)	10

(b) Historical Sampling								
Method	Wikipedia	Reddit	MOOC	LastFM	Enron	Social Evo.	UCI	Rank
JODIE-s	0.360 (0.006)	0.373 (0.007)	0.147 (0.010)	0.415 (0.006)	0.443 (0.002)	0.621 (0.020)	0.431 (0.037)	11
DyRep-s	0.386 (0.003)	0.421 (0.000)	0.408 (0.008)	0.481 (0.017)	0.590 (0.018)	0.715 (0.064)	0.441 (0.016)	7
TGN-s	0.815 (0.014)	0.765 (0.000)	0.695 (0.042)	0.589 (0.008)	0.657 (0.003)	0.885 (0.009)	0.755 (0.011)	2
JODIE-m	0.364 (0.002)	0.372 (0.011)	0.138 (0.010)	0.410 (0.010)	0.445 (0.002)	0.606 (0.023)	0.386 (0.006)	12
DyRep-m	0.370 (0.014)	0.463 (0.000)	0.387 (0.003)	0.464 (0.011)	0.591 (0.011)	0.736 (0.010)	0.425 (0.031)	9
TGN-m	0.809 (0.003)	0.735 (0.000)	0.714 (0.049)	0.641 (0.031)	0.656 (0.004)	0.846 (0.044)	0.714 (0.063)	1
JODIE-h	0.360 (0.010)	0.315 (0.000)	0.119 (0.002)	0.328 (0.001)	0.444 (0.002)	0.528 (0.000)	0.383 (0.042)	14
DyRep-h	0.386 (0.008)	0.550 (0.000)	0.431 (0.034)	0.464 (0.001)	0.555 (0.046)	0.763 (0.000)	0.450 (0.031)	8
TGN-h	0.734 (0.023)	0.742 (0.000)	0.634 (0.001)	0.618 (0.001)	0.604 (0.017)	0.613 (0.000)	0.648 (0.031)	5
JODIE-d	0.403 (0.016)	0.381 (0.000)	0.223 (0.000)	0.195 (0.000)	0.441 (0.001)	0.521 (0.000)	0.339 (0.024)	13
DyRep-d	0.379 (0.001)	0.449 (0.000)	0.402 (0.000)	0.498 (0.000)	0.590 (0.011)	0.467 (0.000)	0.465 (0.017)	6
TGN-d	0.731 (0.014)	0.739 (0.000)	0.702 (0.000)	0.624 (0.000)	0.648 (0.030)	0.629 (0.000)	0.634 (0.079)	4
EdgeBank <sub>tw</sub>	0.754 (0.000)	0.748 (0.000)	0.564 (0.000)	0.694 (0.000)	0.606 (0.000)	0.710 (0.000)	0.717 (0.000)	3
EdgeBank <sub>∞</sub>	0.492 (0.000)	0.508 (0.000)	0.293 (0.000)	0.493 (0.000)	0.451 (0.000)	0.523 (0.000)	0.381 (0.000)	10

(c) Inductive Sampling								
Method	Wikipedia	Reddit	MOOC	LastFM	Enron	Social Evo.	UCI	Rank
JODIE-s	0.324 (0.004)	0.391 (0.005)	0.325 (0.030)	0.465 (0.004)	0.502 (0.001)	0.626 (0.020)	0.513 (0.020)	9
DyRep-s	0.607 (0.009)	0.448 (0.000)	0.561 (0.003)	0.505 (0.001)	0.586 (0.014)	0.712 (0.053)	0.480 (0.018)	6
TGN-s	0.803 (0.008)	0.802 (0.000)	0.654 (0.029)	0.557 (0.005)	0.691 (0.009)	0.880 (0.010)	0.746 (0.024)	1
JODIE-m	0.323 (0.002)	0.390 (0.008)	0.308 (0.026)	0.463 (0.006)	0.501 (0.002)	0.610 (0.025)	0.479 (0.007)	14
DyRep-m	0.584 (0.034)	0.493 (0.000)	0.521 (0.013)	0.499 (0.008)	0.583 (0.017)	0.729 (0.012)	0.471 (0.027)	8
TGN-m	0.783 (0.006)	0.790 (0.000)	0.632 (0.014)	0.597 (0.025)	0.690 (0.010)	0.837 (0.046)	0.741 (0.030)	2
JODIE-h	0.327 (0.001)	0.366 (0.000)	0.248 (0.018)	0.422 (0.001)	0.501 (0.005)	0.526 (0.000)	0.480 (0.036)	11
DyRep-h	0.590 (0.016)	0.577 (0.000)	0.546 (0.000)	0.497 (0.001)	0.561 (0.036)	0.751 (0.000)	0.490 (0.016)	7
TGN-h	0.701 (0.010)	0.743 (0.000)	0.518 (0.000)	0.543 (0.001)	0.657 (0.014)	0.593 (0.000)	0.648 (0.009)	3
JODIE-d	0.442 (0.013)	0.460 (0.000)	0.458 (0.000)	0.339 (0.000)	0.496 (0.001)	0.515 (0.000)	0.455 (0.011)	12
DyRep-d	0.576 (0.027)	0.438 (0.000)	0.534 (0.000)	0.514 (0.000)	0.593 (0.011)	0.468 (0.000)	0.507 (0.014)	5
TGN-d	0.706 (0.011)	0.724 (0.000)	0.468 (0.000)	0.527 (0.000)	0.672 (0.017)	0.602 (0.000)	0.642 (0.019)	4
EdgeBank <sub>tw</sub>	0.417 (0.000)	0.439 (0.000)	0.189 (0.000)	0.447 (0.000)	0.484 (0.000)	0.677 (0.000)	0.491 (0.000)	13
EdgeBank <sub>∞</sub>	0.435 (0.000)	0.465 (0.000)	0.219 (0.000)	0.463 (0.000)	0.468 (0.000)	0.566 (0.000)	0.515 (0.000)	10

Table B.5: AU-ROC of dynamic link prediction on the "minute" granularity data across three negative sampling strategies. Note that we report the mean AU-ROC over three runs with the standard deviations in parenthesis, and the rank is computed by averaging the ranks over all datasets.

(a) Random Sampling								
Method	Wikipedia	Reddit	MOOC	LastFM	Enron	Social Evo.	UCI	Rank
JODIE-s	0.992 (0.001)	0.999 (0.000)	0.856 (0.015)	0.999 (0.000)	0.930 (0.005)	0.996 (0.000)	0.994 (0.001)	2
DyRep-s	0.679 (0.009)	0.568 (0.000)	0.603 (0.007)	0.508 (0.008)	0.634 (0.015)	0.678 (0.055)	0.830 (0.002)	11
TGN-s	0.977 (0.001)	0.961 (0.000)	0.752 (0.026)	0.694 (0.013)	0.809 (0.017)	0.847 (0.004)	0.893 (0.009)	5
JODIE-m	0.993 (0.000)	0.999 (0.000)	0.864 (0.007)	0.999 (0.000)	0.927 (0.002)	0.995 (0.001)	0.995 (0.000)	1
DyRep-m	0.676 (0.010)	0.559 (0.000)	0.587 (0.008)	0.499 (0.004)	0.629 (0.009)	0.697 (0.016)	0.837 (0.010)	12
TGN-m	0.977 (0.001)	0.955 (0.000)	0.802 (0.027)	0.695 (0.015)	0.810 (0.017)	0.875 (0.007)	0.892 (0.034)	4
JODIE-h	0.992 (0.001)	0.996 (0.000)	0.844 (0.020)	0.997 (0.000)	0.923 (0.016)	0.909 (0.000)	0.995 (0.001)	3
DyRep-h	0.639 (0.012)	0.498 (0.000)	0.592 (0.014)	0.501 (0.000)	0.590 (0.058)	0.692 (0.000)	0.829 (0.017)	13
TGN-h	0.960 (0.001)	0.929 (0.000)	0.688 (0.000)	0.683 (0.000)	0.764 (0.027)	0.601 (0.000)	0.811 (0.022)	7
JODIE-d	0.976 (0.005)	0.884 (0.000)	0.629 (0.000)	0.930 (0.000)	0.921 (0.002)	0.633 (0.000)	0.994 (0.001)	6
DyRep-d	0.585 (0.032)	0.464 (0.000)	0.595 (0.000)	0.498 (0.000)	0.637 (0.013)	0.513 (0.000)	0.834 (0.009)	14
TGN-d	0.944 (0.005)	0.922 (0.000)	0.570 (0.000)	0.602 (0.000)	0.795 (0.015)	0.595 (0.000)	0.836 (0.023)	10
EdgeBank <sub>tw</sub>	0.888 (0.000)	0.924 (0.000)	0.607 (0.000)	0.840 (0.000)	0.867 (0.000)	0.600 (0.000)	0.733 (0.000)	8
EdgeBank <sub>∞</sub>	0.911 (0.000)	0.954 (0.000)	0.548 (0.000)	0.827 (0.000)	0.858 (0.000)	0.538 (0.000)	0.749 (0.000)	9

(b) Historical Sampling								
Method	Wikipedia	Reddit	MOOC	LastFM	Enron	Social Evo.	UCI	Rank
JODIE-s	0.363 (0.007)	0.373 (0.007)	0.148 (0.011)	0.415 (0.006)	0.442 (0.001)	0.620 (0.021)	0.431 (0.036)	11
DyRep-s	0.385 (0.005)	0.423 (0.000)	0.404 (0.010)	0.480 (0.019)	0.576 (0.024)	0.714 (0.065)	0.441 (0.017)	7
TGN-s	0.808 (0.015)	0.763 (0.000)	0.685 (0.043)	0.589 (0.007)	0.661 (0.001)	0.845 (0.013)	0.745 (0.013)	1
JODIE-m	0.366 (0.003)	0.372 (0.011)	0.139 (0.010)	0.410 (0.011)	0.443 (0.002)	0.603 (0.022)	0.386 (0.006)	12
DyRep-m	0.367 (0.012)	0.455 (0.000)	0.387 (0.003)	0.454 (0.007)	0.584 (0.011)	0.734 (0.015)	0.423 (0.032)	8
TGN-m	0.805 (0.002)	0.732 (0.000)	0.704 (0.052)	0.640 (0.030)	0.661 (0.002)	0.883 (0.021)	0.696 (0.062)	2
JODIE-h	0.362 (0.011)	0.316 (0.001)	0.119 (0.002)	0.327 (0.001)	0.443 (0.002)	0.526 (0.000)	0.384 (0.041)	14
DyRep-h	0.384 (0.011)	0.548 (0.000)	0.429 (0.033)	0.466 (0.001)	0.565 (0.050)	0.754 (0.000)	0.450 (0.032)	6
TGN-h	0.736 (0.022)	0.745 (0.000)	0.623 (0.001)	0.614 (0.002)	0.603 (0.017)	0.664 (0.000)	0.644 (0.028)	5
JODIE-d	0.404 (0.016)	0.381 (0.001)	0.220 (0.000)	0.197 (0.000)	0.441 (0.001)	0.521 (0.000)	0.339 (0.024)	13
DyRep-d	0.377 (0.003)	0.454 (0.000)	0.410 (0.000)	0.498 (0.000)	0.580 (0.015)	0.467 (0.000)	0.463 (0.018)	9
TGN-d	0.731 (0.016)	0.739 (0.000)	0.700 (0.000)	0.625 (0.000)	0.647 (0.031)	0.629 (0.000)	0.634 (0.078)	4
EdgeBank <sub>tw</sub>	0.754 (0.000)	0.748 (0.000)	0.570 (0.000)	0.700 (0.000)	0.606 (0.000)	0.710 (0.000)	0.717 (0.000)	3
EdgeBank <sub>∞</sub>	0.492 (0.000)	0.508 (0.000)	0.293 (0.000)	0.493 (0.000)	0.451 (0.000)	0.523 (0.000)	0.381 (0.000)	10

(c) Inductive Sampling								
Method	Wikipedia	Reddit	MOOC	LastFM	Enron	Social Evo.	UCI	Rank
JODIE-s	0.324 (0.004)	0.391 (0.005)	0.326 (0.030)	0.466 (0.004)	0.501 (0.001)	0.627 (0.021)	0.512 (0.020)	9
DyRep-s	0.608 (0.008)	0.450 (0.000)	0.556 (0.005)	0.510 (0.014)	0.577 (0.017)	0.712 (0.054)	0.479 (0.020)	6
TGN-s	0.795 (0.009)	0.801 (0.000)	0.631 (0.012)	0.557 (0.005)	0.695 (0.007)	0.837 (0.013)	0.734 (0.025)	1
JODIE-m	0.323 (0.002)	0.390 (0.008)	0.308 (0.027)	0.463 (0.006)	0.500 (0.002)	0.609 (0.025)	0.479 (0.007)	12
DyRep-m	0.583 (0.034)	0.485 (0.000)	0.520 (0.012)	0.485 (0.006)	0.577 (0.014)	0.727 (0.016)	0.470 (0.028)	7
TGN-m	0.779 (0.004)	0.789 (0.000)	0.622 (0.013)	0.596 (0.024)	0.694 (0.007)	0.875 (0.022)	0.722 (0.030)	2
JODIE-h	0.328 (0.001)	0.366 (0.000)	0.249 (0.018)	0.422 (0.001)	0.501 (0.004)	0.525 (0.000)	0.480 (0.035)	14
DyRep-h	0.589 (0.014)	0.575 (0.000)	0.544 (0.006)	0.485 (0.002)	0.566 (0.040)	0.741 (0.000)	0.489 (0.015)	5
TGN-h	0.702 (0.010)	0.749 (0.000)	0.514 (0.001)	0.542 (0.000)	0.656 (0.011)	0.644 (0.000)	0.643 (0.007)	3
JODIE-d	0.441 (0.014)	0.459 (0.001)	0.456 (0.000)	0.339 (0.000)	0.497 (0.001)	0.515 (0.000)	0.454 (0.011)	13
DyRep-d	0.581 (0.031)	0.445 (0.000)	0.540 (0.000)	0.516 (0.000)	0.585 (0.018)	0.468 (0.000)	0.504 (0.019)	8
TGN-d	0.705 (0.011)	0.725 (0.000)	0.461 (0.000)	0.528 (0.000)	0.673 (0.017)	0.602 (0.000)	0.642 (0.019)	4
EdgeBank <sub>tw</sub>	0.417 (0.000)	0.439 (0.000)	0.189 (0.000)	0.447 (0.000)	0.484 (0.000)	0.677 (0.000)	0.491 (0.000)	11
EdgeBank <sub>∞</sub>	0.435 (0.000)	0.465 (0.000)	0.219 (0.000)	0.463 (0.000)	0.468 (0.000)	0.566 (0.000)	0.515 (0.000)	10

Table B.6: AU-ROC of dynamic link prediction on the "hour" granularity data across three negative sampling strategies. Note that we report the mean AU-ROC over three runs with the standard deviations in parenthesis, and the rank is computed by averaging the ranks over all datasets.

(a) Random Sampling								
Method	Wikipedia	Reddit	MOOC	LastFM	Enron	Social Evo.	UCI	Rank
JODIE-s	0.991 (0.001)	0.987 (0.001)	0.765 (0.012)	0.993 (0.000)	0.932 (0.005)	0.781 (0.052)	0.994 (0.001)	3
DyRep-s	0.561 (0.011)	0.483 (0.000)	0.585 (0.011)	0.504 (0.007)	0.636 (0.013)	0.679 (0.057)	0.829 (0.003)	14
TGN-s	0.949 (0.005)	0.909 (0.000)	0.616 (0.012)	0.659 (0.015)	0.802 (0.025)	0.677 (0.018)	0.854 (0.005)	6
JODIE-m	0.993 (0.001)	0.986 (0.000)	0.760 (0.002)	0.993 (0.000)	0.928 (0.003)	0.783 (0.040)	0.995 (0.000)	2
DyRep-m	0.619 (0.027)	0.531 (0.000)	0.560 (0.033)	0.503 (0.009)	0.644 (0.002)	0.687 (0.023)	0.835 (0.013)	13
TGN-m	0.953 (0.001)	0.850 (0.000)	0.618 (0.041)	0.667 (0.013)	0.802 (0.025)	0.657 (0.045)	0.848 (0.057)	7
JODIE-h	0.992 (0.001)	0.992 (0.000)	0.785 (0.009)	0.993 (0.000)	0.926 (0.015)	0.898 (0.000)	0.995 (0.001)	1
DyRep-h	0.668 (0.016)	0.659 (0.000)	0.612 (0.013)	0.510 (0.000)	0.607 (0.052)	0.699 (0.000)	0.833 (0.013)	11
TGN-h	0.956 (0.001)	0.969 (0.000)	0.708 (0.000)	0.682 (0.000)	0.770 (0.025)	0.810 (0.000)	0.839 (0.019)	5
JODIE-d	0.978 (0.004)	0.929 (0.000)	0.709 (0.000)	0.939 (0.000)	0.922 (0.006)	0.770 (0.000)	0.994 (0.001)	4
DyRep-d	0.590 (0.020)	0.539 (0.000)	0.618 (0.000)	0.504 (0.000)	0.647 (0.014)	0.482 (0.000)	0.838 (0.008)	12
TGN-d	0.943 (0.004)	0.932 (0.000)	0.618 (0.000)	0.590 (0.000)	0.797 (0.017)	0.664 (0.000)	0.836 (0.024)	8
EdgeBank <sub>tw</sub>	0.888 (0.000)	0.924 (0.000)	0.607 (0.000)	0.840 (0.000)	0.867 (0.000)	0.600 (0.000)	0.733 (0.000)	9
EdgeBank <sub>∞</sub>	0.911 (0.000)	0.954 (0.000)	0.548 (0.000)	0.827 (0.000)	0.858 (0.000)	0.538 (0.000)	0.749 (0.000)	10

(b) Historical Sampling								
Method	Wikipedia	Reddit	MOOC	LastFM	Enron	Social Evo.	UCI	Rank
JODIE-s	0.362 (0.005)	0.401 (0.000)	0.133 (0.006)	0.417 (0.005)	0.444 (0.004)	0.451 (0.033)	0.431 (0.029)	11
DyRep-s	0.392 (0.010)	0.504 (0.000)	0.461 (0.035)	0.478 (0.021)	0.590 (0.016)	0.716 (0.068)	0.437 (0.014)	7
TGN-s	0.703 (0.023)	0.689 (0.000)	0.597 (0.049)	0.564 (0.015)	0.656 (0.011)	0.750 (0.058)	0.624 (0.019)	5
JODIE-m	0.364 (0.002)	0.401 (0.000)	0.125 (0.004)	0.410 (0.014)	0.446 (0.001)	0.441 (0.018)	0.385 (0.014)	13
DyRep-m	0.399 (0.013)	0.384 (0.000)	0.499 (0.082)	0.463 (0.002)	0.596 (0.007)	0.738 (0.013)	0.425 (0.037)	8
TGN-m	0.717 (0.004)	0.665 (0.000)	0.633 (0.022)	0.601 (0.035)	0.656 (0.011)	0.644 (0.068)	0.587 (0.102)	5
JODIE-h	0.360 (0.008)	0.319 (0.000)	0.116 (0.003)	0.326 (0.000)	0.446 (0.002)	0.517 (0.000)	0.382 (0.050)	14
DyRep-h	0.390 (0.002)	0.531 (0.000)	0.418 (0.032)	0.463 (0.000)	0.576 (0.042)	0.754 (0.000)	0.447 (0.041)	6
TGN-h	0.726 (0.014)	0.752 (0.000)	0.579 (0.001)	0.605 (0.001)	0.604 (0.023)	0.885 (0.000)	0.697 (0.022)	1
JODIE-d	0.402 (0.018)	0.425 (0.000)	0.128 (0.000)	0.195 (0.000)	0.441 (0.001)	0.493 (0.000)	0.338 (0.024)	12
DyRep-d	0.377 (0.009)	0.481 (0.000)	0.408 (0.000)	0.492 (0.000)	0.593 (0.016)	0.462 (0.000)	0.457 (0.025)	9
TGN-d	0.716 (0.019)	0.723 (0.000)	0.634 (0.000)	0.599 (0.000)	0.645 (0.037)	0.781 (0.000)	0.638 (0.077)	2
EdgeBank <sub>tw</sub>	0.754 (0.000)	0.748 (0.000)	0.564 (0.000)	0.694 (0.000)	0.606 (0.000)	0.710 (0.000)	0.717 (0.000)	3
EdgeBank <sub>∞</sub>	0.492 (0.000)	0.508 (0.000)	0.293 (0.000)	0.493 (0.000)	0.451 (0.000)	0.523 (0.000)	0.381 (0.000)	10

(c) Inductive Sampling								
Method	Wikipedia	Reddit	MOOC	LastFM	Enron	Social Evo.	UCI	Rank
JODIE-s	0.317 (0.003)	0.411 (0.000)	0.261 (0.028)	0.463 (0.004)	0.503 (0.001)	0.450 (0.035)	0.510 (0.020)	10
DyRep-s	0.604 (0.012)	0.535 (0.000)	0.530 (0.002)	0.508 (0.005)	0.584 (0.010)	0.715 (0.062)	0.478 (0.021)	6
TGN-s	0.680 (0.011)	0.675 (0.000)	0.497 (0.018)	0.530 (0.019)	0.690 (0.015)	0.744 (0.055)	0.628 (0.033)	3
JODIE-m	0.316 (0.002)	0.411 (0.001)	0.243 (0.012)	0.460 (0.009)	0.502 (0.003)	0.439 (0.020)	0.476 (0.007)	14
DyRep-m	0.634 (0.024)	0.425 (0.000)	0.516 (0.011)	0.512 (0.013)	0.587 (0.004)	0.729 (0.011)	0.472 (0.030)	7
TGN-m	0.681 (0.006)	0.663 (0.000)	0.524 (0.019)	0.553 (0.026)	0.690 (0.015)	0.641 (0.066)	0.633 (0.056)	4
JODIE-h	0.321 (0.001)	0.362 (0.001)	0.226 (0.013)	0.418 (0.002)	0.502 (0.003)	0.519 (0.000)	0.476 (0.036)	13
DyRep-h	0.598 (0.009)	0.596 (0.000)	0.554 (0.006)	0.509 (0.001)	0.571 (0.036)	0.746 (0.000)	0.485 (0.023)	5
TGN-h	0.692 (0.007)	0.800 (0.000)	0.586 (0.001)	0.531 (0.000)	0.658 (0.007)	0.878 (0.000)	0.688 (0.003)	1
JODIE-d	0.438 (0.015)	0.546 (0.001)	0.264 (0.000)	0.333 (0.000)	0.495 (0.001)	0.491 (0.000)	0.451 (0.010)	11
DyRep-d	0.569 (0.024)	0.469 (0.000)	0.551 (0.000)	0.507 (0.000)	0.595 (0.015)	0.468 (0.000)	0.495 (0.025)	8
TGN-d	0.700 (0.016)	0.731 (0.000)	0.454 (0.000)	0.513 (0.000)	0.671 (0.013)	0.762 (0.000)	0.642 (0.022)	2
EdgeBank <sub>tw</sub>	0.417 (0.000)	0.439 (0.000)	0.189 (0.000)	0.447 (0.000)	0.484 (0.000)	0.677 (0.000)	0.491 (0.000)	12
EdgeBank <sub>∞</sub>	0.435 (0.000)	0.465 (0.000)	0.219 (0.000)	0.463 (0.000)	0.468 (0.000)	0.566 (0.000)	0.515 (0.000)	9

Table B.7: AU-ROC of dynamic link prediction on the "day" granularity data across three negative sampling strategies. Note that we report the mean AU-ROC over three runs with the standard deviations in parenthesis, and the rank is computed by averaging the ranks over all datasets.

(a) Random Sampling								
Method	Wikipedia	Reddit	MOOC	LastFM	Enron	Social Evo.	UCI	Rank
JODIE-s	0.954 (0.006)	0.931 (0.014)	0.697 (0.003)	0.851 (0.009)	0.908 (0.001)	0.628 (0.057)	0.993 (0.001)	4
DyRep-s	0.582 (0.048)	0.500 (0.000)	0.583 (0.023)	0.510 (0.013)	0.624 (0.027)	0.582 (0.023)	0.828 (0.010)	14
TGN-s	0.916 (0.006)	0.876 (0.000)	0.607 (0.042)	0.631 (0.019)	0.738 (0.037)	0.581 (0.061)	0.846 (0.019)	9
JODIE-m	0.993 (0.002)	0.986 (0.001)	0.760 (0.006)	0.993 (0.005)	0.928 (0.006)	0.600 (0.040)	0.995 (0.000)	1
DyRep-m	0.619 (0.036)	0.531 (0.000)	0.560 (0.030)	0.503 (0.007)	0.644 (0.010)	0.611 (0.017)	0.835 (0.018)	12
TGN-m	0.953 (0.003)	0.850 (0.000)	0.618 (0.035)	0.667 (0.011)	0.802 (0.038)	0.534 (0.025)	0.848 (0.058)	7
JODIE-h	0.962 (0.004)	0.965 (0.000)	0.700 (0.008)	0.857 (0.000)	0.897 (0.014)	0.731 (0.053)	0.994 (0.001)	2
DyRep-h	0.641 (0.015)	0.524 (0.000)	0.592 (0.000)	0.501 (0.000)	0.590 (0.070)	0.615 (0.033)	0.831 (0.016)	13
TGN-h	0.923 (0.012)	0.952 (0.000)	0.703 (0.000)	0.631 (0.000)	0.766 (0.040)	0.625 (0.039)	0.800 (0.025)	6
JODIE-d	0.979 (0.002)	0.942 (0.000)	0.692 (0.000)	0.868 (0.000)	0.914 (0.001)	0.692 (0.003)	0.993 (0.001)	3
DyRep-d	0.692 (0.005)	0.610 (0.000)	0.615 (0.000)	0.519 (0.000)	0.654 (0.010)	0.532 (0.014)	0.834 (0.007)	11
TGN-d	0.947 (0.001)	0.963 (0.000)	0.638 (0.000)	0.636 (0.000)	0.783 (0.029)	0.761 (0.032)	0.843 (0.026)	5
EdgeBank <sub>tw</sub>	0.890 (0.000)	0.920 (0.000)	0.610 (0.000)	0.840 (0.000)	0.870 (0.000)	0.600 (0.000)	0.730 (0.000)	8
EdgeBank <sub>∞</sub>	0.910 (0.000)	0.950 (0.000)	0.550 (0.000)	0.830 (0.000)	0.860 (0.000)	0.540 (0.000)	0.750 (0.000)	10

(b) Historical Sampling								
Method	Wikipedia	Reddit	MOOC	LastFM	Enron	Social Evo.	UCI	Rank
JODIE-s	0.361 (0.002)	0.366 (0.008)	0.153 (0.003)	0.372 (0.001)	0.432 (0.003)	0.402 (0.043)	0.430 (0.030)	12
DyRep-s	0.408 (0.004)	0.476 (0.000)	0.479 (0.048)	0.463 (0.015)	0.580 (0.021)	0.613 (0.034)	0.440 (0.022)	7
TGN-s	0.688 (0.014)	0.684 (0.000)	0.590 (0.056)	0.533 (0.032)	0.633 (0.010)	0.657 (0.055)	0.637 (0.028)	5
JODIE-m	0.364 (0.003)	0.401 (0.005)	0.125 (0.006)	0.410 (0.001)	0.446 (0.001)	0.380 (0.030)	0.385 (0.023)	13
DyRep-m	0.399 (0.013)	0.384 (0.000)	0.499 (0.050)	0.463 (0.003)	0.596 (0.008)	0.645 (0.011)	0.425 (0.028)	9
TGN-m	0.717 (0.014)	0.665 (0.000)	0.633 (0.048)	0.601 (0.036)	0.656 (0.011)	0.583 (0.061)	0.587 (0.100)	4
JODIE-h	0.358 (0.001)	0.385 (0.001)	0.142 (0.011)	0.368 (0.000)	0.431 (0.001)	0.480 (0.046)	0.387 (0.040)	14
DyRep-h	0.383 (0.008)	0.576 (0.000)	0.461 (0.005)	0.441 (0.001)	0.570 (0.039)	0.651 (0.034)	0.448 (0.035)	8
TGN-h	0.692 (0.042)	0.739 (0.000)	0.494 (0.002)	0.618 (0.000)	0.603 (0.047)	0.721 (0.053)	0.646 (0.007)	3
JODIE-d	0.383 (0.010)	0.431 (0.001)	0.144 (0.000)	0.209 (0.000)	0.433 (0.001)	0.452 (0.013)	0.337 (0.020)	11
DyRep-d	0.391 (0.003)	0.485 (0.001)	0.404 (0.000)	0.500 (0.000)	0.599 (0.015)	0.489 (0.016)	0.452 (0.020)	6
TGN-d	0.702 (0.024)	0.764 (0.000)	0.627 (0.000)	0.588 (0.000)	0.637 (0.044)	0.830 (0.022)	0.637 (0.071)	1
EdgeBank <sub>tw</sub>	0.754 (0.000)	0.748 (0.000)	0.564 (0.000)	0.694 (0.000)	0.606 (0.000)	0.710 (0.000)	0.717 (0.000)	2
EdgeBank <sub>∞</sub>	0.492 (0.000)	0.508 (0.000)	0.293 (0.000)	0.493 (0.000)	0.451 (0.000)	0.523 (0.000)	0.381 (0.000)	10

(c) Inductive Sampling								
Method	Wikipedia	Reddit	MOOC	LastFM	Enron	Social Evo.	UCI	Rank
JODIE-s	0.310 (0.001)	0.433 (0.009)	0.209 (0.017)	0.426 (0.001)	0.490 (0.003)	0.414 (0.040)	0.500 (0.020)	11
DyRep-s	0.566 (0.015)	0.519 (0.000)	0.534 (0.050)	0.508 (0.008)	0.584 (0.017)	0.606 (0.026)	0.488 (0.025)	5
TGN-s	0.665 (0.009)	0.673 (0.000)	0.515 (0.039)	0.508 (0.027)	0.645 (0.030)	0.637 (0.043)	0.640 (0.024)	4
JODIE-m	0.316 (0.003)	0.411 (0.007)	0.243 (0.008)	0.460 (0.001)	0.502 (0.001)	0.389 (0.026)	0.476 (0.019)	12
DyRep-m	0.634 (0.010)	0.425 (0.000)	0.516 (0.032)	0.512 (0.009)	0.587 (0.014)	0.632 (0.008)	0.472 (0.024)	8
TGN-m	0.681 (0.011)	0.663 (0.000)	0.524 (0.009)	0.553 (0.009)	0.690 (0.031)	0.595 (0.068)	0.633 (0.063)	3
JODIE-h	0.306 (0.001)	0.453 (0.001)	0.191 (0.007)	0.424 (0.001)	0.484 (0.004)	0.494 (0.052)	0.472 (0.029)	14
DyRep-h	0.532 (0.017)	0.606 (0.000)	0.498 (0.014)	0.487 (0.002)	0.566 (0.037)	0.632 (0.040)	0.492 (0.017)	6
TGN-h	0.649 (0.017)	0.796 (0.000)	0.489 (0.001)	0.529 (0.001)	0.656 (0.014)	0.691 (0.046)	0.650 (0.004)	2
JODIE-d	0.338 (0.009)	0.562 (0.001)	0.212 (0.000)	0.321 (0.000)	0.489 (0.002)	0.461 (0.008)	0.439 (0.016)	13
DyRep-d	0.467 (0.011)	0.522 (0.000)	0.513 (0.000)	0.510 (0.000)	0.595 (0.011)	0.489 (0.019)	0.492 (0.019)	7
TGN-d	0.689 (0.015)	0.825 (0.001)	0.527 (0.000)	0.563 (0.000)	0.672 (0.020)	0.809 (0.027)	0.647 (0.021)	1
EdgeBank <sub>tw</sub>	0.417 (0.000)	0.439 (0.000)	0.189 (0.000)	0.447 (0.000)	0.484 (0.000)	0.677 (0.000)	0.491 (0.000)	10
EdgeBank <sub>∞</sub>	0.435 (0.000)	0.465 (0.000)	0.219 (0.000)	0.463 (0.000)	0.468 (0.000)	0.566 (0.000)	0.515 (0.000)	9



Table B.8: AP of dynamic link prediction on the "second" granularity data across three negative sampling strategies. Note that we report the mean AP over three runs with the standard deviations in parenthesis, and the rank is computed by averaging the ranks over all datasets.

(a) Random Sampling								
Method	Wikipedia	Reddit	MOOC	LastFM	Enron	Social Evo.	UCI	Rank
JODIE-s	0.993 (0.001)	0.999 (0.000)	0.840 (0.018)	1.000 (0.000)	0.931 (0.006)	0.995 (0.000)	0.993 (0.001)	3
DyRep-s	0.682 (0.008)	0.563 (0.000)	0.614 (0.005)	0.527 (0.003)	0.642 (0.014)	0.728 (0.032)	0.832 (0.002)	12
TGN-s	0.981 (0.001)	0.963 (0.000)	0.764 (0.014)	0.697 (0.014)	0.790 (0.021)	0.902 (0.001)	0.903 (0.005)	6
JODIE-m	0.994 (0.000)	1.000 (0.000)	0.848 (0.010)	0.999 (0.000)	0.926 (0.003)	0.995 (0.001)	0.994 (0.001)	1
DyRep-m	0.684 (0.005)	0.565 (0.000)	0.597 (0.008)	0.518 (0.004)	0.629 (0.020)	0.679 (0.034)	0.831 (0.006)	13
TGN-m	0.980 (0.001)	0.954 (0.000)	0.779 (0.024)	0.699 (0.015)	0.789 (0.022)	0.821 (0.008)	0.907 (0.036)	5
JODIE-h	0.994 (0.001)	0.996 (0.000)	0.847 (0.018)	0.998 (0.000)	0.925 (0.018)	0.861 (0.000)	0.994 (0.001)	2
DyRep-h	0.656 (0.014)	0.514 (0.000)	0.602 (0.007)	0.526 (0.000)	0.600 (0.042)	0.679 (0.000)	0.818 (0.020)	14
TGN-h	0.962 (0.001)	0.923 (0.000)	0.660 (0.000)	0.685 (0.000)	0.727 (0.029)	0.533 (0.000)	0.790 (0.019)	8
JODIE-d	0.978 (0.006)	0.884 (0.000)	0.643 (0.000)	0.936 (0.000)	0.920 (0.004)	0.611 (0.000)	0.994 (0.001)	4
DyRep-d	0.605 (0.027)	0.490 (0.000)	0.608 (0.000)	0.526 (0.000)	0.650 (0.003)	0.506 (0.000)	0.834 (0.006)	11
TGN-d	0.944 (0.004)	0.918 (0.000)	0.557 (0.000)	0.602 (0.000)	0.760 (0.014)	0.543 (0.000)	0.836 (0.027)	9
EdgeBank <sub>tw</sub>	0.887 (0.000)	0.921 (0.000)	0.576 (0.000)	0.784 (0.000)	0.826 (0.000)	0.556 (0.000)	0.730 (0.000)	7
EdgeBank <sub>∞</sub>	0.908 (0.000)	0.949 (0.000)	0.529 (0.000)	0.761 (0.000)	0.811 (0.000)	0.520 (0.000)	0.739 (0.000)	10

(b) Historical Sampling								
Method	Wikipedia	Reddit	MOOC	LastFM	Enron	Social Evo.	UCI	Rank
JODIE-s	0.417 (0.002)	0.435 (0.003)	0.336 (0.002)	0.454 (0.003)	0.440 (0.001)	0.517 (0.012)	0.457 (0.021)	11
DyRep-s	0.418 (0.001)	0.437 (0.000)	0.427 (0.003)	0.476 (0.011)	0.585 (0.021)	0.717 (0.040)	0.440 (0.007)	7
TGN-s	0.827 (0.019)	0.746 (0.000)	0.644 (0.043)	0.628 (0.010)	0.649 (0.014)	0.916 (0.010)	0.777 (0.013)	2
JODIE-m	0.419 (0.001)	0.434 (0.005)	0.334 (0.003)	0.451 (0.006)	0.441 (0.001)	0.508 (0.013)	0.430 (0.005)	12
DyRep-m	0.411 (0.006)	0.457 (0.000)	0.417 (0.002)	0.463 (0.006)	0.588 (0.011)	0.698 (0.029)	0.435 (0.016)	9
TGN-m	0.804 (0.016)	0.704 (0.000)	0.644 (0.046)	0.684 (0.034)	0.649 (0.014)	0.820 (0.060)	0.748 (0.056)	1
JODIE-h	0.416 (0.004)	0.403 (0.000)	0.329 (0.001)	0.407 (0.000)	0.441 (0.001)	0.469 (0.000)	0.429 (0.023)	14
DyRep-h	0.419 (0.004)	0.519 (0.000)	0.434 (0.012)	0.463 (0.001)	0.558 (0.032)	0.725 (0.000)	0.445 (0.014)	8
TGN-h	0.721 (0.023)	0.713 (0.000)	0.565 (0.001)	0.644 (0.001)	0.588 (0.011)	0.579 (0.000)	0.623 (0.036)	5
JODIE-d	0.417 (0.007)	0.409 (0.000)	0.354 (0.000)	0.347 (0.000)	0.440 (0.000)	0.471 (0.000)	0.405 (0.011)	13
DyRep-d	0.414 (0.001)	0.455 (0.000)	0.421 (0.000)	0.471 (0.000)	0.590 (0.005)	0.454 (0.000)	0.459 (0.013)	6
TGN-d	0.709 (0.037)	0.716 (0.000)	0.633 (0.000)	0.622 (0.000)	0.627 (0.029)	0.549 (0.000)	0.614 (0.091)	4
EdgeBank <sub>tw</sub>	0.689 (0.000)	0.676 (0.000)	0.541 (0.000)	0.627 (0.000)	0.568 (0.000)	0.633 (0.000)	0.701 (0.000)	3
EdgeBank <sub>∞</sub>	0.496 (0.000)	0.504 (0.000)	0.432 (0.000)	0.497 (0.000)	0.483 (0.000)	0.512 (0.000)	0.455 (0.000)	10

(c) Inductive Sampling								
Method	Wikipedia	Reddit	MOOC	LastFM	Enron	Social Evo.	UCI	Rank
JODIE-s	0.412 (0.002)	0.443 (0.003)	0.444 (0.028)	0.477 (0.002)	0.473 (0.000)	0.519 (0.012)	0.501 (0.013)	9
DyRep-s	0.626 (0.005)	0.481 (0.000)	0.599 (0.002)	0.519 (0.002)	0.586 (0.018)	0.714 (0.036)	0.491 (0.005)	6
TGN-s	0.840 (0.007)	0.833 (0.000)	0.658 (0.027)	0.601 (0.008)	0.693 (0.011)	0.910 (0.010)	0.782 (0.025)	1
JODIE-m	0.411 (0.001)	0.443 (0.004)	0.430 (0.014)	0.476 (0.004)	0.473 (0.001)	0.510 (0.015)	0.480 (0.006)	14
DyRep-m	0.614 (0.025)	0.509 (0.000)	0.558 (0.015)	0.511 (0.006)	0.582 (0.017)	0.691 (0.032)	0.499 (0.017)	8
TGN-m	0.807 (0.005)	0.807 (0.000)	0.628 (0.022)	0.640 (0.029)	0.692 (0.011)	0.808 (0.061)	0.779 (0.024)	2
JODIE-h	0.414 (0.000)	0.429 (0.000)	0.411 (0.018)	0.453 (0.000)	0.473 (0.002)	0.467 (0.000)	0.482 (0.020)	11
DyRep-h	0.617 (0.009)	0.584 (0.000)	0.586 (0.005)	0.510 (0.001)	0.563 (0.025)	0.712 (0.000)	0.500 (0.010)	7
TGN-h	0.704 (0.009)	0.764 (0.000)	0.532 (0.000)	0.576 (0.000)	0.641 (0.014)	0.565 (0.000)	0.633 (0.019)	3
JODIE-d	0.487 (0.012)	0.499 (0.000)	0.518 (0.000)	0.418 (0.000)	0.471 (0.000)	0.471 (0.000)	0.466 (0.004)	12
DyRep-d	0.608 (0.018)	0.472 (0.000)	0.561 (0.000)	0.524 (0.000)	0.595 (0.006)	0.458 (0.000)	0.516 (0.009)	5
TGN-d	0.716 (0.023)	0.744 (0.000)	0.487 (0.000)	0.538 (0.000)	0.659 (0.017)	0.533 (0.000)	0.644 (0.038)	4
EdgeBank <sub>tw</sub>	0.469 (0.000)	0.473 (0.000)	0.417 (0.000)	0.481 (0.000)	0.506 (0.000)	0.609 (0.000)	0.566 (0.000)	13
EdgeBank <sub>∞</sub>	0.477 (0.000)	0.485 (0.000)	0.417 (0.000)	0.487 (0.000)	0.497 (0.000)	0.536 (0.000)	0.570 (0.000)	10

Table B.9: AP of dynamic link prediction on the "minute" granularity data across three negative sampling strategies. Note that we report the mean AP over three runs with the standard deviations in parenthesis, and the rank is computed by averaging the ranks over all datasets.

(a) Random Sampling								
Method	Wikipedia	Reddit	MOOC	LastFM	Enron	Social Evo.	UCI	Rank
JODIE-s	0.993 (0.001)	0.999 (0.000)	0.840 (0.018)	1.000 (0.000)	0.931 (0.006)	0.995 (0.000)	0.993 (0.001)	2
DyRep-s	0.680 (0.006)	0.565 (0.000)	0.611 (0.007)	0.529 (0.005)	0.635 (0.014)	0.731 (0.033)	0.827 (0.003)	11
TGN-s	0.979 (0.001)	0.963 (0.000)	0.725 (0.023)	0.697 (0.013)	0.790 (0.020)	0.784 (0.011)	0.895 (0.009)	5
JODIE-m	0.994 (0.000)	1.000 (0.000)	0.848 (0.009)	0.999 (0.000)	0.928 (0.003)	0.994 (0.001)	0.994 (0.001)	1
DyRep-m	0.683 (0.004)	0.562 (0.000)	0.596 (0.007)	0.523 (0.002)	0.628 (0.010)	0.677 (0.032)	0.832 (0.008)	12
TGN-m	0.979 (0.001)	0.954 (0.000)	0.777 (0.024)	0.697 (0.016)	0.791 (0.020)	0.832 (0.009)	0.897 (0.033)	4
JODIE-h	0.994 (0.001)	0.996 (0.000)	0.846 (0.020)	0.998 (0.000)	0.924 (0.017)	0.853 (0.000)	0.994 (0.001)	3
DyRep-h	0.655 (0.016)	0.515 (0.000)	0.603 (0.007)	0.522 (0.000)	0.601 (0.042)	0.668 (0.000)	0.817 (0.022)	13
TGN-h	0.962 (0.001)	0.925 (0.000)	0.660 (0.000)	0.682 (0.000)	0.728 (0.029)	0.562 (0.000)	0.791 (0.018)	7
JODIE-d	0.979 (0.006)	0.882 (0.000)	0.648 (0.000)	0.939 (0.000)	0.921 (0.002)	0.607 (0.000)	0.994 (0.001)	6
DyRep-d	0.607 (0.026)	0.491 (0.000)	0.609 (0.000)	0.521 (0.000)	0.640 (0.011)	0.516 (0.000)	0.832 (0.008)	14
TGN-d	0.945 (0.004)	0.918 (0.000)	0.559 (0.000)	0.601 (0.000)	0.760 (0.014)	0.536 (0.000)	0.836 (0.027)	10
EdgeBank <sub>tw</sub>	0.887 (0.000)	0.921 (0.000)	0.576 (0.000)	0.784 (0.000)	0.826 (0.000)	0.556 (0.000)	0.730 (0.000)	8
EdgeBank <sub>∞</sub>	0.908 (0.000)	0.949 (0.000)	0.529 (0.000)	0.761 (0.000)	0.811 (0.000)	0.520 (0.000)	0.739 (0.000)	9

(b) Historical Sampling								
Method	Wikipedia	Reddit	MOOC	LastFM	Enron	Social Evo.	UCI	Rank
JODIE-s	0.418 (0.002)	0.435 (0.003)	0.337 (0.002)	0.454 (0.003)	0.440 (0.000)	0.516 (0.012)	0.456 (0.021)	11
DyRep-s	0.417 (0.002)	0.438 (0.000)	0.425 (0.004)	0.476 (0.013)	0.575 (0.024)	0.719 (0.041)	0.440 (0.007)	7
TGN-s	0.821 (0.020)	0.742 (0.000)	0.629 (0.043)	0.626 (0.008)	0.651 (0.012)	0.838 (0.017)	0.767 (0.014)	1
JODIE-m	0.420 (0.001)	0.434 (0.005)	0.335 (0.002)	0.451 (0.006)	0.440 (0.001)	0.507 (0.013)	0.430 (0.005)	12
DyRep-m	0.410 (0.005)	0.453 (0.000)	0.417 (0.001)	0.460 (0.004)	0.584 (0.011)	0.694 (0.027)	0.434 (0.016)	8
TGN-m	0.802 (0.020)	0.702 (0.000)	0.636 (0.047)	0.683 (0.033)	0.651 (0.012)	0.881 (0.039)	0.732 (0.056)	2
JODIE-h	0.417 (0.004)	0.403 (0.000)	0.330 (0.001)	0.407 (0.000)	0.440 (0.001)	0.467 (0.000)	0.429 (0.023)	14
DyRep-h	0.418 (0.005)	0.516 (0.000)	0.432 (0.011)	0.464 (0.000)	0.572 (0.038)	0.714 (0.000)	0.445 (0.015)	6
TGN-h	0.725 (0.022)	0.716 (0.000)	0.557 (0.001)	0.639 (0.002)	0.586 (0.012)	0.628 (0.000)	0.623 (0.035)	5
JODIE-d	0.418 (0.006)	0.409 (0.001)	0.354 (0.000)	0.347 (0.000)	0.439 (0.001)	0.484 (0.000)	0.405 (0.011)	13
DyRep-d	0.414 (0.002)	0.458 (0.000)	0.424 (0.000)	0.473 (0.000)	0.582 (0.006)	0.458 (0.000)	0.458 (0.014)	9
TGN-d	0.709 (0.038)	0.714 (0.000)	0.633 (0.000)	0.624 (0.000)	0.627 (0.030)	0.575 (0.000)	0.616 (0.090)	4
EdgeBank <sub>tw</sub>	0.688 (0.000)	0.675 (0.000)	0.541 (0.000)	0.627 (0.000)	0.567 (0.000)	0.634 (0.000)	0.701 (0.000)	3
EdgeBank <sub>∞</sub>	0.496 (0.000)	0.504 (0.000)	0.432 (0.000)	0.497 (0.000)	0.483 (0.000)	0.512 (0.000)	0.455 (0.000)	10

(c) Inductive Sampling								
Method	Wikipedia	Reddit	MOOC	LastFM	Enron	Social Evo.	UCI	Rank
JODIE-s	0.412 (0.002)	0.443 (0.003)	0.445 (0.028)	0.478 (0.002)	0.473 (0.000)	0.520 (0.013)	0.500 (0.013)	9
DyRep-s	0.625 (0.004)	0.483 (0.000)	0.594 (0.003)	0.527 (0.011)	0.579 (0.018)	0.716 (0.037)	0.491 (0.005)	6
TGN-s	0.833 (0.008)	0.832 (0.000)	0.630 (0.012)	0.601 (0.008)	0.695 (0.009)	0.825 (0.019)	0.771 (0.025)	1
JODIE-m	0.411 (0.001)	0.443 (0.004)	0.431 (0.015)	0.476 (0.004)	0.472 (0.001)	0.510 (0.015)	0.480 (0.006)	12
DyRep-m	0.611 (0.025)	0.504 (0.000)	0.557 (0.010)	0.502 (0.008)	0.580 (0.014)	0.688 (0.029)	0.498 (0.016)	7
TGN-m	0.805 (0.000)	0.807 (0.000)	0.620 (0.015)	0.640 (0.028)	0.695 (0.010)	0.870 (0.039)	0.763 (0.025)	2
JODIE-h	0.415 (0.001)	0.429 (0.000)	0.412 (0.018)	0.453 (0.000)	0.473 (0.002)	0.466 (0.000)	0.483 (0.020)	14
DyRep-h	0.615 (0.011)	0.579 (0.000)	0.586 (0.004)	0.501 (0.001)	0.572 (0.031)	0.699 (0.000)	0.499 (0.010)	5
TGN-h	0.708 (0.011)	0.771 (0.000)	0.531 (0.001)	0.572 (0.000)	0.640 (0.012)	0.612 (0.000)	0.630 (0.016)	3
JODIE-d	0.487 (0.012)	0.498 (0.000)	0.518 (0.000)	0.418 (0.000)	0.472 (0.000)	0.481 (0.000)	0.466 (0.005)	13
DyRep-d	0.614 (0.022)	0.479 (0.000)	0.566 (0.000)	0.524 (0.000)	0.589 (0.012)	0.461 (0.000)	0.514 (0.014)	8
TGN-d	0.715 (0.023)	0.746 (0.000)	0.483 (0.000)	0.539 (0.000)	0.659 (0.017)	0.558 (0.000)	0.644 (0.041)	4
EdgeBank <sub>tw</sub>	0.469 (0.000)	0.473 (0.000)	0.417 (0.000)	0.481 (0.000)	0.506 (0.000)	0.609 (0.000)	0.566 (0.000)	11
EdgeBank <sub>∞</sub>	0.477 (0.000)	0.485 (0.000)	0.417 (0.000)	0.487 (0.000)	0.497 (0.000)	0.536 (0.000)	0.570 (0.000)	10

Table B.10: AP of dynamic link prediction on the "hour" granularity data across three negative sampling strategies. Note that we report the mean AP over three runs with the standard deviations in parenthesis, and the rank is computed by averaging the ranks over all datasets.

(a) Random Sampling								
Method	Wikipedia	Reddit	MOOC	LastFM	Enron	Social Evo.	UCI	Rank
JODIE-s	0.992 (0.001)	0.989 (0.001)	0.779 (0.010)	0.994 (0.000)	0.933 (0.006)	0.760 (0.042)	0.993 (0.001)	3
DyRep-s	0.573 (0.013)	0.515 (0.000)	0.599 (0.006)	0.528 (0.004)	0.636 (0.014)	0.730 (0.037)	0.823 (0.002)	14
TGN-s	0.952 (0.005)	0.895 (0.000)	0.594 (0.015)	0.660 (0.012)	0.775 (0.031)	0.613 (0.024)	0.837 (0.003)	6
JODIE-m	0.994 (0.000)	0.988 (0.000)	0.778 (0.005)	0.994 (0.000)	0.929 (0.004)	0.772 (0.031)	0.994 (0.001)	2
DyRep-m	0.639 (0.018)	0.540 (0.000)	0.576 (0.028)	0.525 (0.004)	0.643 (0.004)	0.671 (0.047)	0.830 (0.015)	13
TGN-m	0.956 (0.002)	0.830 (0.000)	0.602 (0.035)	0.664 (0.015)	0.775 (0.031)	0.592 (0.048)	0.830 (0.070)	7
JODIE-h	0.993 (0.001)	0.993 (0.000)	0.802 (0.006)	0.994 (0.000)	0.927 (0.017)	0.882 (0.000)	0.994 (0.001)	1
DyRep-h	0.676 (0.006)	0.631 (0.000)	0.629 (0.002)	0.528 (0.000)	0.612 (0.038)	0.670 (0.000)	0.824 (0.015)	11
TGN-h	0.960 (0.001)	0.967 (0.000)	0.682 (0.000)	0.687 (0.000)	0.739 (0.023)	0.787 (0.000)	0.833 (0.015)	5
JODIE-d	0.981 (0.004)	0.926 (0.000)	0.738 (0.000)	0.946 (0.000)	0.922 (0.007)	0.738 (0.000)	0.994 (0.001)	4
DyRep-d	0.616 (0.022)	0.535 (0.000)	0.626 (0.000)	0.523 (0.000)	0.652 (0.012)	0.490 (0.000)	0.837 (0.008)	12
TGN-d	0.946 (0.003)	0.925 (0.000)	0.609 (0.000)	0.597 (0.000)	0.765 (0.016)	0.596 (0.000)	0.835 (0.027)	8
EdgeBank <sub>tw</sub>	0.887 (0.000)	0.921 (0.000)	0.576 (0.000)	0.784 (0.000)	0.826 (0.000)	0.556 (0.000)	0.730 (0.000)	9
EdgeBank <sub>∞</sub>	0.908 (0.000)	0.949 (0.000)	0.529 (0.000)	0.761 (0.000)	0.811 (0.000)	0.520 (0.000)	0.739 (0.000)	10

(b) Historical Sampling								
Method	Wikipedia	Reddit	MOOC	LastFM	Enron	Social Evo.	UCI	Rank
JODIE-s	0.421 (0.002)	0.449 (0.000)	0.334 (0.002)	0.455 (0.002)	0.441 (0.002)	0.441 (0.013)	0.457 (0.017)	11
DyRep-s	0.424 (0.006)	0.486 (0.000)	0.450 (0.014)	0.474 (0.012)	0.583 (0.019)	0.720 (0.047)	0.437 (0.006)	7
TGN-s	0.689 (0.034)	0.638 (0.000)	0.551 (0.036)	0.588 (0.012)	0.635 (0.025)	0.658 (0.073)	0.587 (0.034)	5
JODIE-m	0.422 (0.001)	0.449 (0.000)	0.332 (0.001)	0.451 (0.007)	0.442 (0.000)	0.436 (0.006)	0.431 (0.009)	13
DyRep-m	0.424 (0.006)	0.416 (0.000)	0.478 (0.054)	0.465 (0.003)	0.592 (0.002)	0.695 (0.036)	0.436 (0.018)	8
TGN-m	0.704 (0.008)	0.638 (0.000)	0.571 (0.016)	0.627 (0.036)	0.635 (0.024)	0.552 (0.056)	0.572 (0.114)	5
JODIE-h	0.420 (0.003)	0.405 (0.000)	0.330 (0.001)	0.407 (0.000)	0.442 (0.001)	0.466 (0.000)	0.430 (0.027)	14
DyRep-h	0.422 (0.002)	0.496 (0.000)	0.430 (0.016)	0.461 (0.000)	0.575 (0.034)	0.705 (0.000)	0.445 (0.019)	6
TGN-h	0.728 (0.008)	0.712 (0.000)	0.516 (0.001)	0.643 (0.000)	0.591 (0.022)	0.854 (0.000)	0.695 (0.021)	1
JODIE-d	0.421 (0.007)	0.426 (0.000)	0.333 (0.000)	0.347 (0.000)	0.440 (0.001)	0.458 (0.000)	0.406 (0.010)	12
DyRep-d	0.415 (0.004)	0.471 (0.000)	0.426 (0.000)	0.470 (0.000)	0.593 (0.013)	0.461 (0.000)	0.456 (0.017)	9
TGN-d	0.707 (0.043)	0.689 (0.000)	0.573 (0.000)	0.609 (0.000)	0.627 (0.034)	0.678 (0.000)	0.619 (0.087)	2
EdgeBank <sub>tw</sub>	0.689 (0.000)	0.676 (0.000)	0.541 (0.000)	0.627 (0.000)	0.568 (0.000)	0.633 (0.000)	0.701 (0.000)	3
EdgeBank <sub>∞</sub>	0.496 (0.000)	0.504 (0.000)	0.432 (0.000)	0.497 (0.000)	0.483 (0.000)	0.512 (0.000)	0.455 (0.000)	10

(c) Inductive Sampling								
Method	Wikipedia	Reddit	MOOC	LastFM	Enron	Social Evo.	UCI	Rank
JODIE-s	0.412 (0.002)	0.454 (0.000)	0.421 (0.029)	0.477 (0.002)	0.474 (0.001)	0.441 (0.013)	0.500 (0.013)	10
DyRep-s	0.606 (0.009)	0.555 (0.000)	0.572 (0.004)	0.519 (0.002)	0.584 (0.013)	0.720 (0.045)	0.488 (0.006)	6
TGN-s	0.686 (0.020)	0.649 (0.000)	0.519 (0.012)	0.560 (0.015)	0.679 (0.019)	0.654 (0.069)	0.620 (0.047)	3
JODIE-m	0.411 (0.001)	0.454 (0.000)	0.406 (0.010)	0.475 (0.005)	0.474 (0.001)	0.436 (0.007)	0.479 (0.005)	14
DyRep-m	0.650 (0.017)	0.460 (0.000)	0.545 (0.023)	0.524 (0.010)	0.587 (0.008)	0.689 (0.036)	0.493 (0.014)	7
TGN-m	0.691 (0.005)	0.675 (0.000)	0.539 (0.017)	0.581 (0.024)	0.679 (0.019)	0.551 (0.054)	0.625 (0.075)	4
JODIE-h	0.415 (0.001)	0.426 (0.000)	0.403 (0.016)	0.452 (0.001)	0.474 (0.002)	0.467 (0.000)	0.481 (0.020)	13
DyRep-h	0.623 (0.005)	0.576 (0.000)	0.584 (0.000)	0.516 (0.001)	0.572 (0.028)	0.696 (0.000)	0.496 (0.015)	5
TGN-h	0.710 (0.007)	0.820 (0.000)	0.589 (0.000)	0.576 (0.001)	0.643 (0.006)	0.847 (0.000)	0.692 (0.006)	1
JODIE-d	0.489 (0.013)	0.552 (0.000)	0.446 (0.000)	0.416 (0.000)	0.471 (0.000)	0.458 (0.000)	0.466 (0.003)	11
DyRep-d	0.606 (0.013)	0.482 (0.000)	0.587 (0.000)	0.511 (0.000)	0.597 (0.010)	0.466 (0.000)	0.509 (0.020)	8
TGN-d	0.719 (0.029)	0.731 (0.000)	0.484 (0.000)	0.537 (0.000)	0.659 (0.014)	0.661 (0.000)	0.646 (0.042)	2
EdgeBank <sub>tw</sub>	0.469 (0.000)	0.473 (0.000)	0.417 (0.000)	0.481 (0.000)	0.506 (0.000)	0.609 (0.000)	0.566 (0.000)	12
EdgeBank <sub>∞</sub>	0.477 (0.000)	0.485 (0.000)	0.417 (0.000)	0.487 (0.000)	0.497 (0.000)	0.536 (0.000)	0.570 (0.000)	9

Table B.11: AP of dynamic link prediction on the "day" granularity data across three negative sampling strategies. Note that we report the mean AP over three runs with the standard deviations in parenthesis, and the rank is computed by averaging the ranks over all datasets.

(a) Random Sampling								
Method	Wikipedia	Reddit	MOOC	LastFM	Enron	Social Evo.	UCI	Rank
JODIE-s	0.958 (0.006)	0.934 (0.013)	0.717 (0.001)	0.882 (0.007)	0.909 (0.001)	0.587 (0.056)	0.991 (0.002)	4
DyRep-s	0.587 (0.047)	0.522 (0.000)	0.592 (0.015)	0.531 (0.004)	0.630 (0.023)	0.621 (0.037)	0.814 (0.009)	14
TGN-s	0.922 (0.005)	0.847 (0.000)	0.584 (0.034)	0.635 (0.017)	0.699 (0.044)	0.532 (0.046)	0.835 (0.026)	9
JODIE-m	0.969 (0.002)	0.936 (0.003)	0.711 (0.007)	0.876 (0.004)	0.898 (0.008)	0.556 (0.037)	0.993 (0.001)	1
DyRep-m	0.616 (0.033)	0.546 (0.000)	0.575 (0.025)	0.526 (0.006)	0.633 (0.010)	0.612 (0.031)	0.813 (0.021)	12
TGN-m	0.941 (0.004)	0.857 (0.000)	0.599 (0.027)	0.643 (0.008)	0.700 (0.044)	0.493 (0.016)	0.820 (0.070)	7
JODIE-h	0.966 (0.004)	0.965 (0.000)	0.724 (0.006)	0.888 (0.000)	0.897 (0.014)	0.682 (0.052)	0.993 (0.001)	2
DyRep-h	0.648 (0.005)	0.539 (0.000)	0.600 (0.003)	0.518 (0.000)	0.599 (0.053)	0.649 (0.019)	0.818 (0.015)	13
TGN-h	0.929 (0.010)	0.947 (0.000)	0.676 (0.000)	0.645 (0.000)	0.730 (0.033)	0.568 (0.045)	0.788 (0.025)	6
JODIE-d	0.982 (0.002)	0.933 (0.000)	0.720 (0.000)	0.894 (0.000)	0.913 (0.001)	0.642 (0.015)	0.993 (0.001)	3
DyRep-d	0.691 (0.002)	0.592 (0.000)	0.615 (0.000)	0.539 (0.000)	0.655 (0.009)	0.538 (0.015)	0.828 (0.007)	11
TGN-d	0.951 (0.000)	0.961 (0.000)	0.620 (0.000)	0.655 (0.000)	0.752 (0.029)	0.704 (0.036)	0.840 (0.029)	5
EdgeBank <sub>tw</sub>	0.887 (0.000)	0.921 (0.000)	0.576 (0.000)	0.784 (0.000)	0.826 (0.000)	0.556 (0.000)	0.730 (0.000)	8
EdgeBank <sub>∞</sub>	0.908 (0.000)	0.949 (0.000)	0.529 (0.000)	0.761 (0.000)	0.811 (0.000)	0.520 (0.000)	0.739 (0.000)	10

(b) Historical Sampling								
Method	Wikipedia	Reddit	MOOC	LastFM	Enron	Social Evo.	UCI	Rank
JODIE-s	0.421 (0.001)	0.411 (0.002)	0.339 (0.001)	0.432 (0.000)	0.438 (0.001)	0.418 (0.016)	0.457 (0.017)	12
DyRep-s	0.434 (0.002)	0.465 (0.000)	0.459 (0.022)	0.464 (0.008)	0.582 (0.022)	0.621 (0.033)	0.440 (0.009)	7
TGN-s	0.690 (0.027)	0.633 (0.000)	0.552 (0.041)	0.559 (0.029)	0.601 (0.014)	0.565 (0.045)	0.603 (0.034)	5
JODIE-m	0.421 (0.001)	0.412 (0.002)	0.337 (0.002)	0.431 (0.000)	0.438 (0.000)	0.409 (0.011)	0.436 (0.012)	13
DyRep-m	0.427 (0.006)	0.476 (0.000)	0.502 (0.057)	0.451 (0.001)	0.589 (0.011)	0.631 (0.023)	0.435 (0.014)	9
TGN-m	0.679 (0.005)	0.699 (0.000)	0.564 (0.042)	0.626 (0.033)	0.601 (0.015)	0.512 (0.044)	0.553 (0.106)	4
JODIE-h	0.420 (0.000)	0.417 (0.000)	0.336 (0.003)	0.430 (0.000)	0.437 (0.000)	0.450 (0.022)	0.432 (0.023)	14
DyRep-h	0.419 (0.003)	0.531 (0.000)	0.449 (0.012)	0.449 (0.001)	0.573 (0.036)	0.656 (0.027)	0.445 (0.016)	8
TGN-h	0.688 (0.047)	0.693 (0.000)	0.467 (0.001)	0.648 (0.001)	0.581 (0.033)	0.631 (0.063)	0.627 (0.008)	3
JODIE-d	0.415 (0.004)	0.426 (0.000)	0.337 (0.000)	0.353 (0.000)	0.438 (0.000)	0.436 (0.006)	0.407 (0.009)	11
DyRep-d	0.421 (0.001)	0.467 (0.000)	0.420 (0.000)	0.485 (0.000)	0.604 (0.016)	0.488 (0.008)	0.455 (0.015)	6
TGN-d	0.690 (0.044)	0.725 (0.001)	0.562 (0.000)	0.591 (0.000)	0.620 (0.044)	0.776 (0.036)	0.619 (0.089)	1
EdgeBank <sub>tw</sub>	0.689 (0.000)	0.676 (0.000)	0.541 (0.000)	0.627 (0.000)	0.568 (0.000)	0.633 (0.000)	0.701 (0.000)	2
EdgeBank <sub>∞</sub>	0.496 (0.000)	0.504 (0.000)	0.432 (0.000)	0.497 (0.000)	0.483 (0.000)	0.512 (0.000)	0.455 (0.000)	10
EdgeBank <sub>∞</sub>	0.908 (0.000)	0.949 (0.000)	0.529 (0.000)	0.761 (0.000)	0.811 (0.000)	0.520 (0.000)	0.739 (0.000)	10

(c) Inductive Sampling								
Method	Wikipedia	Reddit	MOOC	LastFM	Enron	Social Evo.	UCI	Rank
JODIE-s	0.400 (0.000)	0.441 (0.003)	0.377 (0.024)	0.458 (0.000)	0.469 (0.001)	0.423 (0.015)	0.497 (0.012)	11
DyRep-s	0.589 (0.014)	0.522 (0.000)	0.565 (0.037)	0.523 (0.003)	0.586 (0.017)	0.617 (0.034)	0.492 (0.009)	5
TGN-s	0.667 (0.019)	0.644 (0.000)	0.532 (0.029)	0.543 (0.029)	0.631 (0.032)	0.555 (0.035)	0.637 (0.023)	4
JODIE-m	0.401 (0.001)	0.442 (0.003)	0.363 (0.011)	0.458 (0.000)	0.469 (0.000)	0.413 (0.009)	0.482 (0.010)	12
DyRep-m	0.602 (0.010)	0.522 (0.000)	0.544 (0.024)	0.507 (0.008)	0.582 (0.013)	0.620 (0.023)	0.486 (0.011)	8
TGN-m	0.675 (0.013)	0.709 (0.000)	0.542 (0.009)	0.558 (0.007)	0.631 (0.032)	0.527 (0.050)	0.605 (0.080)	3
JODIE-h	0.399 (0.000)	0.448 (0.000)	0.366 (0.015)	0.457 (0.001)	0.467 (0.002)	0.457 (0.026)	0.480 (0.017)	14
DyRep-h	0.572 (0.009)	0.592 (0.000)	0.537 (0.015)	0.501 (0.001)	0.570 (0.033)	0.644 (0.026)	0.498 (0.011)	6
TGN-h	0.654 (0.011)	0.797 (0.000)	0.503 (0.000)	0.565 (0.001)	0.633 (0.016)	0.610 (0.056)	0.656 (0.003)	2
JODIE-d	0.426 (0.007)	0.527 (0.001)	0.402 (0.000)	0.408 (0.000)	0.469 (0.001)	0.440 (0.004)	0.463 (0.005)	13
DyRep-d	0.530 (0.009)	0.507 (0.000)	0.545 (0.000)	0.520 (0.000)	0.599 (0.010)	0.490 (0.004)	0.504 (0.015)	7
TGN-d	0.702 (0.020)	0.832 (0.001)	0.529 (0.000)	0.591 (0.000)	0.662 (0.024)	0.749 (0.036)	0.649 (0.040)	1
EdgeBank <sub>tw</sub>	0.469 (0.000)	0.473 (0.000)	0.417 (0.000)	0.481 (0.000)	0.506 (0.000)	0.609 (0.000)	0.566 (0.000)	10
EdgeBank <sub>∞</sub>	0.477 (0.000)	0.485 (0.000)	0.417 (0.000)	0.487 (0.000)	0.497 (0.000)	0.536 (0.000)	0.570 (0.000)	9