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LoRA Merging with SVD: Understanding Interference and Preserving Performance

Anonymous Authors¹

Abstract

Merging Low-Rank Adaptation (LoRA) modules is a problem gaining significance as LoRA adapters proliferate. Despite various approaches showing benchmark improvements, the field lacks clear guiding principles for effective LoRA merging. Two predominant strategies exist: direct merging (DM), which preserves a memory efficient two-matrix structure but sacrifices performance, and multiplied merging (MM), which delivers superior results but abandons the memoryefficient, low-rank architecture. In this paper, we first show that DM introduces interfering crossterms that degrade performance, while MM exhibits linear mode connectivity in the loss landscape, making it an optimal strategy for merging. Then we demonstrate that merging with an SVD-based strategy combines MM's performance advantages with DM's memory efficiency, delivering the best of both approaches.

1. Introduction

The rise of Large Language Models (LLMs) (Touvron et al., 2023; Reid et al., 2024; Achiam et al., 2023) has popularized their use as assistants for a variety of knowledge-intensive tasks. However, for some tasks, users may find that an outof-the-box LLM is insufficient and requires additional training. Given that even the smallest usable models have billions of parameters, the computational cost of training them can be prohibitive. Thankfully, the recent rise of Parameter-Efficient Fine-Tuning (PEFT) methods – like LoRA (Hu et al., 2021) and DoRA (Liu et al., 2024) – enables LLMs to train at a fraction of the cost.

In practical applications requiring models to handle diverse queries, the development of specialized expert models for every task is often infeasible. Furthermore, employing PEFT for each task results in a number of models that scales linearly with the quantity of target tasks. Consequently, repositories like the Hugging Face Hub (Wolf et al., 2019) now host an expanding collection of these specialized PEFT modules. Serving this multitude of expert models presents

significant challenges, particularly under limited GPU memory constraints. Model merging (Tang et al., 2024) aims to mitigate this limitation by consolidating multiple fine-tuned PEFT modules into a single model, that generalizes across many tasks.

Given a pre-trained base model parametrized by W, LoRA fine-tunes the model by injecting two matrices: $W + \Delta W =$ W + BA where W, $BA \in \mathbb{R}^{n \times n}$, $B \in \mathbb{R}^{n \times r}$ and $A \in \mathbb{R}^{r \times n}$. For LoRA merging, W remains consistent across all models and the adapters BA are trained on different tasks and then merged. In our setting, LoRA adapters are trained in image classification tasks but merging LoRA adapters can also extend to natural language processing and multimodal domains (Tang et al., 2024).

LoRA merging has generally been done in two ways. "Direct-Merge" (L_{DM}) directly combines As and Bs from different adapters separately, while "Mutliplied-Merge" (L_{MM}) first multiples A and B from the same adapter into BA before merging. For L_{MM} , the LoRA adapters lose their shape as well as any memory-efficiency from LoRA's low-rank structure (such as memory-efficient storage). Examples of L_{DM} include (Huang et al., 2023; Zhao et al., 2024; Prabhakar et al., 2024) and examples of L_{MM} include (Stoica et al., 2024; Shah et al., 2023; Wu et al., 2024).

Often, it is ambiguous which method is preferable. L_{DM} retains the low-rank matrix structure of LoRA, which enables better memory efficiency during the merging step and during storage. It also makes multi-LoRA serving cheaper as low rank matrices can be loaded and offloaded from the GPU (Yadav et al., 2023a). Additionally, in settings such as QLoRA (Dettmers et al., 2023), the shape of the original LoRA modules back to quantized base model weights. In contrast, L_{MM} does not preserve this low-rank structure of the LoRA matrices but often enables better performance. But *why* is there a performance gap? and is there a better way to retain LoRA's shape without performance degradation?

We strive to answer both these questions by analyzing the differences between L_{MM} and L_{DM} . Our analysis reveals that L_{DM} introduces interference terms absent in L_{MM} which severely degrade performance - when merging 8 Lo-

RAs, we observe L_{MM} outperforms L_{DM} by an +50.15% accuracy. Furthermore, we demonstrate how using SVD on 057 top of L_{MM} can retain the memory-efficient LoRA shape 058 with virtually no accuracy loss. We supplement this find-059 ing mathematically by demonstrating that the error from 060 SVD will be less than the interference error in L_{DM} . Em-061 pirically, our method outperforms state-of-the-art L_{DM} ap-062 proaches like LoRA LEGO by +7.12% on average. Finally, 063 we demonstrate that L_{MM} exhibits linear mode connectiv-064 ity (Frankle et al., 2019) in the loss landscape while L_{DM} 065 does not, providing additional theoretical justification for 066 preferring multiplied merging when combining LoRA. 067

2. Related Works

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070 There are two main approaches to model-merging - datadependent and data-free. Data-dependant approaches (Matena & Raffel, 2021; Yang et al., 2023; Prabhakar et al., 073 2024) use data to adjust or train the mixture of models. In 074 our setting, we focus on the data-free setting. Model Soups 075 (Wortsman et al., 2022) simply averages the model weights 076 together. Task-Arithmetic merging (Ilharco et al., 2022) 077 sums the base model with scaled task vectors (the differ-078 ence between the base model and the fine-tuned model). 079 TIES-Merging (Yadav et al., 2023b) merges models by min-080 imizing the interference of parameters. DARE (Yu et al., 081 2023) uses a dropout and rescale operation. More recent 082 model-merging methods (Matena & Raffel, 2021; Tam et al., 083 2023; Mavromatis et al., 2024; Lu et al., 2024; Yang et al., 084 2023; Feng et al., 2024; Daheim et al., 2023) have also explored fancier approaches to combining models. Methods 086 specific to merging LoRAs include KnOTS (Stoica et al., 087 2024) which aligns the LoRA into a common subspace with 088 SVD prior to merging, LoRA Soups (Prabhakar et al., 2024) 089 which learns a linear combination of concatenated LoRAs. 090 LoRA LEGO (Zhao et al., 2024) which clusters LoRAs be-091 fore merging, and ZipLora (Shah et al., 2023) which learns 092 optimal scaling coefficients. While these approaches are 093 each optimal in their own specific setting (e.g. data-free, 094 adaptable rank, post-hoc training etc), we articulate a framework for approaching LoRA-merging in general. 095 096

3. Method

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099 3.1. Preliminaries

LoRA Fine-Tuning. The shape and structure of LoRA was described in the introduction. Without LoRA, the activation for layer \mathbf{W}_i is $z_i = \mathbf{W}_i z_{i-1}$. With LoRA, this activation becomes $z_i = \mathbf{W}_i z_{i-1} + \frac{\alpha}{r} \mathbf{B} \mathbf{A}$, where α is a scalar and ris the rank of the LoRA. During training, only **BA** is tuned and all weights **W** are frozen.

Linear Mode Connectivity. Linear Mode Connectivity
 (LMC) (Frankle et al., 2019) describes when two models

can be effectively combined through weight interpolation. This is measured by the barrier function:

$$B(\theta_1, \theta_2) = \sup_{\alpha} [L(\alpha \theta_1 + (1 - \alpha)\theta_2)] -[\alpha L(\theta_1) + (1 - \alpha)L(\theta_2)].$$
(1)

Here, sup indicates the supremum, θ_1 and θ_2 represent model parameters, L is the loss function, and $B(\theta_1, \theta_2)$ quantifies the maximum elevation in loss along the linear interpolation path relative to the convex combination of endpoint losses. When $B(\theta_1, \theta_2) \approx 0$, the models are LMC, indicating they share the same loss landscape basin and are ideal candidates for parameter averaging techniques (Frankle et al., 2019; Entezari et al., 2021; Jordan et al., 2022).

3.2. Merging Notation

In our context, we assume LoRA modules are merged via summation and is uniform across layers, but our results generalize to other merging functions as well. For simplicity, we define everything in terms of a single layer across multiple models. To merge N LoRA adapters, where subscript i indicates the *i*th LoRA module, MM and DM are defined:

$$L_{MM} = \sum_{i=1}^{N} \mathbf{B}_i * \mathbf{A}_i, L_{DM} = (\sum_i \mathbf{B}_i) (\sum_i \mathbf{A}_i) \quad (2)$$

3.3. Noise in Direct-Merge

Expanding L_{DM} from Equation (2) yields:

$$L_{DM} = (\sum_{i} \mathbf{B}_{i})(\sum_{i} \mathbf{A}_{i}) = \sum_{i} (\mathbf{B}_{i} \mathbf{A}_{i}) + \sum_{i \neq j} \mathbf{B}_{i} \mathbf{A}_{j} \quad (3)$$

Let us also define $M = \sum_{i \neq j} \mathbf{B}_i \mathbf{A}_j$. Now, we rewrite (2) as $L_{DM} = L_{MM} + M$. Since M is composed of B_i and A_j terms that originate from different adapters, we hypothesize that their composition harms model performance. To test whether this interference term degrades model performance, we simulate M with gaussian noise and demonstrate that the decrease in performance due to the M is greater than or equal to the decrease resulting from the simulated noise.

3.4. Multiplied-Merge with SVD

Given the noise inherent to L_{DM} , it may be optimal to retain the performance benefits of L_{MM} and then find a low rank decomposition back into structure of L_{DM} . Here, we demonstrate that a simple SVD-based method can accomplish this. Let $SVD_r(\cdot) = U\Sigma_{[:r]}V^T$ indicate a function that takes the SVD of a matrix and retains only the *r* largest singular values. $SVD_r(L_{MM})$ then defines **A** as $\Sigma_{[:r]}V^T$ and **B** as *U*.

Mathematically, we will show that the magnitude of the error resulting from truncated SVD is bounded above by the mag-



Figure 1. Linear Mode Connectivity Analysis (LMC) of L_{MM} and L_{DM} on all dataset pairs. Lines show loss at different interpolation values. L_{MM} consistently exhibits LMC (loss below interpolated loss line), while L_{DM} shows higher loss barriers.

nitude of M. Empirically, we then show that $SVD_r(L_{MM})$ outperforms the SOTA L_{DM} methods.

Math Proof Here, we show SVD truncation is a closer approximation to L_{MM} than L_{DM} . Definitionally:

$$SVD_r(L_{MM}) = SVD(L_{MM}) - SVD_{err}(L_{MM})$$
(4)

where $SVD_{err}(L_{MM})$ is the error due to truncation. Specifically, $SVD(L_{MM}) = U\Sigma V^T$ and $SVD_{err}(L_{MM}) = U\Sigma_{[r+1:n]}V^T$ where $\Sigma_{[i:j]}$ indicates the *i*th through *j*th singular values.

The Eckart-Young-Mirsky theorem indicates that SVD provides the closest rank r approximation to any matrix. Since $SVD_r(L_{MM})$ and $LoRA_{DM}$ are both rank r, $SVD_r(L_{MM})$ is a closer approximation. Giving:

$$||L_{MM} - SVD_r(L_{MM})|| \le ||L_{MM} - L_{DM}||$$
 (5)

Substituting Equation (2) (right) and Equation (4) gives:

$$\frac{||L_{MM} - (SVD(L_{MM}) + SVD_{err}(L_{MM}))|| \le}{||L_{MM} - (L_{MM} + M)||}$$
(6)

$$||SVD_{err}(L_{MM})|| \le ||M|| \tag{7}$$

Thus the error due to approximating L_{MM} with SVD is bounded above by the error due to using L_{DM} .

4. Results

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4.1. Experimental Setup

We use openai/clip-vit-base-patch32 as our base model. We denote each dataset as D_i where { $D_1 = SVHN$ (Netzer et al., 2011), $D_2 = GTSRB$ (Stallkamp et al., 2011), D_3 = DTD (Cimpoi et al., 2013), $D_4 = RESISC45$ (Cheng et al., 2017), $D_5 = Stanford-Cars$ (Krause et al., 2013), D_6 = Sun397 (Xiao et al., 2014), $D_7 = Eurosat$ (Helber et al., 2017), $D_8 = MNIST$ (LeCun & Cortes, 2005)}. We used the LoRA adapters (rank=16) and evaluation benchmarks from in (Tang et al., 2024). Out of the 8 available datasets, we randomly select 4 pairs of datasets (D_i, D_j) and fix them for each experiment. We also evaluate all eight datasets D_1-D_8 merged together. For each dataset, we use the respective LoRA. For each experiment, we apply four different merging methods: Averaging, Task-Arithmetic (TA) Merging, TIES-merging, and DARE merging. For TA, TIES, DARE, we tune the hyper-parameters via a linear search on the eight combined datasets and fix them for all experiments.

4.2. Performance Comparison Between Multiplied Merging and Direct Merging

First, we compare the accuracy of L_{MM} and L_{DM} for each merging method across each pair of datasets. In Table 1, L_{DM} outperforms L_{MM} by +0.09% when using TA merging on dataset pair (D5, D6), but has worse performance in the remaining 19 comparisons. When merging 2 LoRA, L_{MM} outperforms L_{DM} by +2.97% on average. Notably, when merging 8 LoRA, L_{MM} achieves, on average, +50.15% accuracy compared to L_{DM} across all merging methods. This error in merging multiple LoRAs is more thoroughly investigated in section 4.4.

4.3. Equivalence of SVD-Based Approximation to Multiplied Merging

Since L_{DM} lags behind L_{MM} , we hypothesize that merging with L_{MM} and then reducing the rank with a truncated SVD can help mitigate this gap. So, we compare $SVD_{16}(L_{MM})$ with L_{MM} . We use r = 16 to match the rank of $LoRA_{DM}$. In Table 2, $SVD_{16}(\cdot)$ has a negligible performance drop compared to L_{MM} . L_{MM} is on average +0.46% across all methods on paired LoRAs, while $SVD_{16}(\cdot)$ is +0.52%compared to L_{MM} when merging all 8 LoRAs.

LoRA Merging with SVD

Dataset ($ ightarrow$)		(D1, D2)			(D3, D4)			(D5, D6)			(D7, D8)			Merge All		
Method (↓)	MM	MM DM		se Mi	M D	M N	oise M	M D	M N	loise N	ſΜ	DM	Noise	MM	DM	No
Averaging	82.00	76.50	81.9	91 68.	30 65	.64 6	8.27 69	.60 68	.83 6	9.62 9.	3.90	89.33	93.99	64.40	61.31	64
Fask Arithmetic	85.50	81.90	85.8	39 72.	20 71	.43 7	2.28 70	.60 70	.69 7	0.57 9	5.40	96.00	96.38	73.30	6.20	71
TIES	81.40	73.51	81.5									87.32	93.99	68.50	5.60	67
DARE	86.00	81.74	85.8									95.94	96.38	73.50	6.00	70
Average	83.73	78.41	83.7	79 70.	08 67	.55 7	0.01 70	.10 69	.18 7	0.11 9	5.25	92.15	95.19	69.93	19.78	68
Table		uracy c set (\rightarrow)	ompa	(D1,			Merging		, Direc		ng (DM		Noise		ion	
	Method (↓)			MM	SVD	MM	SVD	MM	SVD	MM	SVD	MN	0			
		aging		82.00	81.80	68.30		69.60	69.60	93.90	93.90					
		Arithm	etic	85.50	85.74	72.20	71.82	70.60	70.47	96.40	96.3	73.3	0 72.2	23		
				01 40	78.10	67.40	66.06	69.60	69.27	94.30	90.61	68.5	0 73.2	23		
	TIES			81.40												
	DAR	E		86.00	85.68	72.40	71.99	70.60	70.49	96.40	96.30	73.5	0 72.2	20		
		E					71.99					73.5	0 72.2	20		
	DAR	E age	2. Ac	86.00 83.73	85.68 82.83	72.40 70.08	71.99	70.60 70.10	70.49 70.08	96.40 95.25	96.30 94.40	73.5 69.9	0 72.2 3 70.4	20		
	DAR Aver	E age		86.00 83.73	85.68 82.83 compa	72.40 70.08	71.99 70.00	70.60 70.10 f <i>LoR</i> 2	70.49 70.08	96.40 95.25	96.30 94.40 16(<i>Lo</i> .	73.5 69.9 RA _{MN}	0 72.2 3 70.4	20 14		
	DAR Aver	E age Table	Metl	86.00 83.73	85.68 82.83 compa	72.40 70.08 rison b	71.99 70.00 etween o	70.60 70.10 f <i>LoR</i>	70.49 70.08 4 _{MM}	96.40 95.25 vs SVD	96.30 94.40 16(Lo. 8)	73.5 69.9 RA _{MN}	$\begin{array}{ccc} 0 & 72.2 \\ 3 & 70.4 \\ \end{array}$	20 14 ge		
	DAR Aver	E age Table	Meta Lora	86.00 83.73 ccuracy	85.68 82.83 compa (D1 , 73	72.40 70.08 arison b	71.99 70.00 etween o (D3, D4)	70.60 70.10 f <i>LoR</i>	70.49 70.08 4 _{MM} , D6)	96.40 95.25 Vs SVD (D7, D 3	96.30 94.40 16(<i>Lo.</i> 8) A 61	73.5 69.9 RA_{MN}	0 72.2 3 70.4 1).	20 14 ge		
	DAR Aver Ran 8	E age Table	Metl Lora MM	86.00 83.73 ccuracy hod (↓) a Lego	85.68 82.83 (D1, 73 81	72.40 70.08 arison b , D2) .90	71.99 70.00 etween o (D3, D4) 65.10	70.60 70.10 f <i>LoR</i> (D5 68 69	70.49 70.08 4 _{MM} , D6)	96.40 95.25 vs SVD (D7, D 3 82.50	96.30 94.40 16(<i>Lo.</i> 8) 61 63	73.5 69.9 RA_{MN}	0 72.2 3 70.4 4). Averag 70.16	20 14 ge		
	DAR Aver	E age Table	Meta Lora MM	86.00 83.73 ccuracy hod (↓) a Lego I SVD	85.68 82.83 compa (D1, 73 81 77	72.40 70.08 arison b D2) .40	71.99 70.00 etween o (D3, D4) 65.10 67.20	70.60 70.10 f LoRA 0 (D5 68 69 68	70.49 70.08 4 _{MM} , D6) .20 .40	96.40 95.25 //s <i>SVD</i> (D7, D 3 82.50 93.70	96.30 94.40 16(<i>Lo.</i> 8) A 61 62 61	73.5 69.9 <i>RA_{MM}</i> All 1.10 3.70	0 72.2 3 70.4 1). Averag 70.16 77.90	20 14 ge		
	DAR Aver Ran 8	E age Table	Metl Lora MM Lora MM	86.00 83.73 ceuracy hod (↓) a Lego I SVD a Lego	85.68 82.83 compa (D1, 73 81 77 81	72.40 70.08 rison b , D2) .90 .40	71.99 70.00 etween o (D3, D4) 65.10 67.20 64.90	70.60 70.10 f <i>LoR</i> 2 0 (D5 68 69 68 69	70.49 70.08 4 _{MM} , D6) .20 .40 .40	96.40 95.25 Vs SVD (D7, D3 82.50 93.70 82.30	96.30 94.40 116 (Lo. 8) A 61 63 61 64	73.5 69.9 <i>RA_{MM}</i> All 1.10 3.70	0 72.2 3 70.4 4). Averag 70.16 77.90 71.08	20 44 ge		

SVD-Based Approach Outperforms State-of-the-Art 197 **Methods**. Next, we compare $SVD_r(L_{MM})$ with a SOTA LoRA_{DM} merging method. LoRA LEGO (Zhao et al., 199 2024) is a method that decomposes LoRA modules into 200 rank-1 units and then clusters them together. The centroid of each cluster contributes 1 rank to the final merged-LoRA, thereby giving users fine-grain control of the merged rank. However, LoRA LEGO introduces the same noise present 204 in $LoRA_{DM}$ as LoRA units from different adapters are averaged together. In our comparison, we select r = [8, 16, 16]206 32] and use simple averaging to compute L_{MM} . As shown in Table 3, for rank 8, $SVD_r(L_{MM})$ achieves +7.74% ac-208 curacy compare to Lego LoRA, +7.22% at rank 16, and 209 +6.38% at rank 32. This indicates that $SVD_r(L_{MM})$ is 210 able to outperform SOTA L_{DM} methods, while retaining 211 the ability to dynamically select merged LoRA rank. 212

Linear Mode Connectivity Analysis We demonstrate that L_{MM} is LMC while L_{DM} is not. For each task, we interpolated the pairs of LoRAs with coefficients $a \in$ [0.1, 0.2, ...0.9, 1.0], and calculate the average cross entropy loss on the two test sets. We then plot the interpolated losses and the loss of the interpolated models. Models are LMC when the interpolated model's loss is less than the interpolated loss for all interpolation values. Fig. 1 shows that L_{MM} is LMC on all datasets, whereas L_{DM} is only LMC on a single dataset.

Interference Impact and Scaling Effects As shown in section 3.3, $L_{DM} = L_{MM} + M$. To simulate the impact of M, we sample a noise matrix $N \in \mathbb{R}^{n \times n}$ with $N_{ij} \sim \mathcal{N}(mean(M), std(M))$ and demonstrate that $L_{MM} + N$ performs better than or equal to L_{DM} , indicating that the term M is source of degradation in merging performance. In Table 1, adding N to L_{MM} has a minimal effect on accuracy (-0.025% difference on average), however, when merging on eight LoRA, this noise actually does better by +0.143%.

5. Conclusion

We demonstrated that merging LoRA with Direct-Merge can maintain a memory-efficient low-rank structure but introduces interference terms that degrade model performance and break LMC. By using truncated SVD on top of Mutliplied-Merge, we show that it is easy to retain memoryefficient structure with virtually no performance cost.

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