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# LoRA Merging with SVD: Understanding Interference and Preserving Performance

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#### Abstract

Merging Low-Rank Adaptation (LoRA) modules is a problem gaining significance as LoRA adapters proliferate. Despite various approaches showing benchmark improvements, the field lacks clear guiding principles for effective LoRA merging. Two predominant strategies exist: direct merging (DM), which preserves a memory efficient two-matrix structure but sacrifices performance, and multiplied merging (MM), which delivers superior results but abandons the memoryefficient, low-rank architecture. In this paper, we first show that DM introduces interfering crossterms that degrade performance, while MM exhibits linear mode connectivity in the loss landscape, making it an optimal strategy for merging. Then we demonstrate that merging with an SVD-based strategy combines MM's performance advantages with DM's memory efficiency, delivering the best of both approaches.

## 1. Introduction

The rise of Large Language Models (LLMs) (Touvron et al., 2023; Reid et al., 2024; Achiam et al., 2023) has popularized their use as assistants for a variety of knowledge-intensive tasks. However, for some tasks, users may find that an outof-the-box LLM is insufficient and requires additional training. Given that even the smallest usable models have billions of parameters, the computational cost of training them can be prohibitive. Thankfully, the recent rise of Parameter-Efficient Fine-Tuning (PEFT) methods – like LoRA (Hu et al., 2021) and DoRA (Liu et al., 2024) – enables LLMs to train at a fraction of the cost.

In practical applications requiring models to handle diverse queries, the development of specialized expert models for every task is often infeasible. Furthermore, employing PEFT for each task results in a number of models that scales linearly with the quantity of target tasks. Consequently, repositories like the Hugging Face Hub (Wolf et al., 2019) now host an expanding collection of these specialized PEFT modules. Serving this multitude of expert models presents

significant challenges, particularly under limited GPU memory constraints. Model merging (Tang et al., 2024) aims to mitigate this limitation by consolidating multiple fine-tuned PEFT modules into a single model, that generalizes across many tasks.

Given a pre-trained base model parametrized by W, LoRA fine-tunes the model by injecting two matrices:  $W + \Delta W =$ W + BA where W,  $BA \in \mathbb{R}^{n \times n}$ ,  $B \in \mathbb{R}^{n \times r}$  and  $A \in \mathbb{R}^{r \times n}$ . For LoRA merging, W remains consistent across all models and the adapters BA are trained on different tasks and then merged. In our setting, LoRA adapters are trained in image classification tasks but merging LoRA adapters can also extend to natural language processing and multimodal domains (Tang et al., 2024).

LoRA merging has generally been done in two ways. "Direct-Merge"  $(L_{DM})$  directly combines As and Bs from different adapters separately, while "Mutliplied-Merge"  $(L_{MM})$  first multiples A and B from the same adapter into BA before merging. For  $L_{MM}$ , the LoRA adapters lose their shape as well as any memory-efficiency from LoRA's low-rank structure (such as memory-efficient storage). Examples of  $L_{DM}$  include (Huang et al., 2023; Zhao et al., 2024; Prabhakar et al., 2024) and examples of  $L_{MM}$  include (Stoica et al., 2024; Shah et al., 2023; Wu et al., 2024).

Often, it is ambiguous which method is preferable.  $L_{DM}$  retains the low-rank matrix structure of LoRA, which enables better memory efficiency during the merging step and during storage. It also makes multi-LoRA serving cheaper as low rank matrices can be loaded and offloaded from the GPU (Yadav et al., 2023a). Additionally, in settings such as QLoRA (Dettmers et al., 2023), the shape of the original LoRA modules back to quantized base model weights. In contrast,  $L_{MM}$  does not preserve this low-rank structure of the LoRA matrices but often enables better performance. But *why* is there a performance gap? and is there a better way to retain LoRA's shape without performance degradation?

We strive to answer both these questions by analyzing the differences between  $L_{MM}$  and  $L_{DM}$ . Our analysis reveals that  $L_{DM}$  introduces interference terms absent in  $L_{MM}$  which severely degrade performance - when merging 8 Lo-

RAs, we observe  $L_{MM}$  outperforms  $L_{DM}$  by an +50.15% accuracy. Furthermore, we demonstrate how using SVD on 057 top of  $L_{MM}$  can retain the memory-efficient LoRA shape 058 with virtually no accuracy loss. We supplement this find-059 ing mathematically by demonstrating that the error from 060 SVD will be less than the interference error in  $L_{DM}$ . Em-061 pirically, our method outperforms state-of-the-art  $L_{DM}$  ap-062 proaches like LoRA LEGO by +7.12% on average. Finally, 063 we demonstrate that  $L_{MM}$  exhibits linear mode connectiv-064 ity (Frankle et al., 2019) in the loss landscape while  $L_{DM}$ 065 does not, providing additional theoretical justification for 066 preferring multiplied merging when combining LoRA. 067

## 2. Related Works

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070 There are two main approaches to model-merging - datadependent and data-free. Data-dependant approaches (Matena & Raffel, 2021; Yang et al., 2023; Prabhakar et al., 073 2024) use data to adjust or train the mixture of models. In 074 our setting, we focus on the data-free setting. Model Soups 075 (Wortsman et al., 2022) simply averages the model weights 076 together. Task-Arithmetic merging (Ilharco et al., 2022) 077 sums the base model with scaled task vectors (the differ-078 ence between the base model and the fine-tuned model). 079 TIES-Merging (Yadav et al., 2023b) merges models by min-080 imizing the interference of parameters. DARE (Yu et al., 081 2023) uses a dropout and rescale operation. More recent 082 model-merging methods (Matena & Raffel, 2021; Tam et al., 083 2023; Mavromatis et al., 2024; Lu et al., 2024; Yang et al., 084 2023; Feng et al., 2024; Daheim et al., 2023) have also explored fancier approaches to combining models. Methods 086 specific to merging LoRAs include KnOTS (Stoica et al., 087 2024) which aligns the LoRA into a common subspace with 088 SVD prior to merging, LoRA Soups (Prabhakar et al., 2024) 089 which learns a linear combination of concatenated LoRAs. 090 LoRA LEGO (Zhao et al., 2024) which clusters LoRAs be-091 fore merging, and ZipLora (Shah et al., 2023) which learns 092 optimal scaling coefficients. While these approaches are 093 each optimal in their own specific setting (e.g. data-free, 094 adaptable rank, post-hoc training etc), we articulate a framework for approaching LoRA-merging in general. 095 096

## 3. Method

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## 099 3.1. Preliminaries

**LoRA Fine-Tuning.** The shape and structure of LoRA was described in the introduction. Without LoRA, the activation for layer  $\mathbf{W}_i$  is  $z_i = \mathbf{W}_i z_{i-1}$ . With LoRA, this activation becomes  $z_i = \mathbf{W}_i z_{i-1} + \frac{\alpha}{r} \mathbf{B} \mathbf{A}$ , where  $\alpha$  is a scalar and ris the rank of the LoRA. During training, only **BA** is tuned and all weights **W** are frozen.

Linear Mode Connectivity. Linear Mode Connectivity
 (LMC) (Frankle et al., 2019) describes when two models

can be effectively combined through weight interpolation. This is measured by the barrier function:

$$B(\theta_1, \theta_2) = \sup_{\alpha} [L(\alpha \theta_1 + (1 - \alpha)\theta_2)] -[\alpha L(\theta_1) + (1 - \alpha)L(\theta_2)].$$
(1)

Here, sup indicates the supremum,  $\theta_1$  and  $\theta_2$  represent model parameters, L is the loss function, and  $B(\theta_1, \theta_2)$ quantifies the maximum elevation in loss along the linear interpolation path relative to the convex combination of endpoint losses. When  $B(\theta_1, \theta_2) \approx 0$ , the models are LMC, indicating they share the same loss landscape basin and are ideal candidates for parameter averaging techniques (Frankle et al., 2019; Entezari et al., 2021; Jordan et al., 2022).

#### 3.2. Merging Notation

In our context, we assume LoRA modules are merged via summation and is uniform across layers, but our results generalize to other merging functions as well. For simplicity, we define everything in terms of a single layer across multiple models. To merge N LoRA adapters, where subscript i indicates the *i*th LoRA module, MM and DM are defined:

$$L_{MM} = \sum_{i=1}^{N} \mathbf{B}_i * \mathbf{A}_i, L_{DM} = (\sum_i \mathbf{B}_i) (\sum_i \mathbf{A}_i) \quad (2)$$

#### 3.3. Noise in Direct-Merge

Expanding  $L_{DM}$  from Equation (2) yields:

$$L_{DM} = (\sum_{i} \mathbf{B}_{i})(\sum_{i} \mathbf{A}_{i}) = \sum_{i} (\mathbf{B}_{i} \mathbf{A}_{i}) + \sum_{i \neq j} \mathbf{B}_{i} \mathbf{A}_{j} \quad (3)$$

Let us also define  $M = \sum_{i \neq j} \mathbf{B}_i \mathbf{A}_j$ . Now, we rewrite (2) as  $L_{DM} = L_{MM} + M$ . Since M is composed of  $B_i$  and  $A_j$  terms that originate from different adapters, we hypothesize that their composition harms model performance. To test whether this interference term degrades model performance, we simulate M with gaussian noise and demonstrate that the decrease in performance due to the M is greater than or equal to the decrease resulting from the simulated noise.

#### 3.4. Multiplied-Merge with SVD

Given the noise inherent to  $L_{DM}$ , it may be optimal to retain the performance benefits of  $L_{MM}$  and then find a low rank decomposition back into structure of  $L_{DM}$ . Here, we demonstrate that a simple SVD-based method can accomplish this. Let  $SVD_r(\cdot) = U\Sigma_{[:r]}V^T$  indicate a function that takes the SVD of a matrix and retains only the *r* largest singular values.  $SVD_r(L_{MM})$  then defines **A** as  $\Sigma_{[:r]}V^T$ and **B** as *U*.

Mathematically, we will show that the magnitude of the error resulting from truncated SVD is bounded above by the mag-



Figure 1. Linear Mode Connectivity Analysis (LMC) of  $L_{MM}$  and  $L_{DM}$  on all dataset pairs. Lines show loss at different interpolation values.  $L_{MM}$  consistently exhibits LMC (loss below interpolated loss line), while  $L_{DM}$  shows higher loss barriers.

nitude of M. Empirically, we then show that  $SVD_r(L_{MM})$  outperforms the SOTA  $L_{DM}$  methods.

**Math Proof** Here, we show SVD truncation is a closer approximation to  $L_{MM}$  than  $L_{DM}$ . Definitionally:

$$SVD_r(L_{MM}) = SVD(L_{MM}) - SVD_{err}(L_{MM})$$
(4)

where  $SVD_{err}(L_{MM})$  is the error due to truncation. Specifically,  $SVD(L_{MM}) = U\Sigma V^T$  and  $SVD_{err}(L_{MM}) = U\Sigma_{[r+1:n]}V^T$  where  $\Sigma_{[i:j]}$  indicates the *i*th through *j*th singular values.

The Eckart-Young-Mirsky theorem indicates that SVD provides the closest rank r approximation to any matrix. Since  $SVD_r(L_{MM})$  and  $LoRA_{DM}$  are both rank r,  $SVD_r(L_{MM})$  is a closer approximation. Giving:

$$||L_{MM} - SVD_r(L_{MM})|| \le ||L_{MM} - L_{DM}||$$
 (5)

Substituting Equation (2) (right) and Equation (4) gives:

$$\frac{||L_{MM} - (SVD(L_{MM}) + SVD_{err}(L_{MM}))|| \le}{||L_{MM} - (L_{MM} + M)||}$$
(6)

$$||SVD_{err}(L_{MM})|| \le ||M|| \tag{7}$$

Thus the error due to approximating  $L_{MM}$  with SVD is bounded above by the error due to using  $L_{DM}$ .

#### 4. Results

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#### 4.1. Experimental Setup

We use openai/clip-vit-base-patch32 as our base model. We denote each dataset as  $D_i$  where { $D_1 =$ SVHN (Netzer et al., 2011),  $D_2 =$ GTSRB (Stallkamp et al., 2011),  $D_3$ = DTD (Cimpoi et al., 2013),  $D_4 =$ RESISC45 (Cheng et al., 2017),  $D_5 =$ Stanford-Cars (Krause et al., 2013),  $D_6$ = Sun397 (Xiao et al., 2014),  $D_7 =$  Eurosat (Helber et al., 2017),  $D_8 =$  MNIST (LeCun & Cortes, 2005)}. We used the LoRA adapters (rank=16) and evaluation benchmarks from in (Tang et al., 2024). Out of the 8 available datasets, we randomly select 4 pairs of datasets  $(D_i, D_j)$  and fix them for each experiment. We also evaluate all eight datasets  $D_1-D_8$ merged together. For each dataset, we use the respective LoRA. For each experiment, we apply four different merging methods: Averaging, Task-Arithmetic (TA) Merging, TIES-merging, and DARE merging. For TA, TIES, DARE, we tune the hyper-parameters via a linear search on the eight combined datasets and fix them for all experiments.

## 4.2. Performance Comparison Between Multiplied Merging and Direct Merging

First, we compare the accuracy of  $L_{MM}$  and  $L_{DM}$  for each merging method across each pair of datasets. In Table 1,  $L_{DM}$  outperforms  $L_{MM}$  by +0.09% when using TA merging on dataset pair (D5, D6), but has worse performance in the remaining 19 comparisons. When merging 2 LoRA,  $L_{MM}$  outperforms  $L_{DM}$  by +2.97% on average. Notably, when merging 8 LoRA,  $L_{MM}$  achieves, on average, +50.15% accuracy compared to  $L_{DM}$  across all merging methods. This error in merging multiple LoRAs is more thoroughly investigated in section 4.4.

## 4.3. Equivalence of SVD-Based Approximation to Multiplied Merging

Since  $L_{DM}$  lags behind  $L_{MM}$ , we hypothesize that merging with  $L_{MM}$  and then reducing the rank with a truncated SVD can help mitigate this gap. So, we compare  $SVD_{16}(L_{MM})$ with  $L_{MM}$ . We use r = 16 to match the rank of  $LoRA_{DM}$ . In Table 2,  $SVD_{16}(\cdot)$  has a negligible performance drop compared to  $L_{MM}$ .  $L_{MM}$  is on average +0.46% across all methods on paired LoRAs, while  $SVD_{16}(\cdot)$  is +0.52%compared to  $L_{MM}$  when merging all 8 LoRAs.

LoRA Merging with SVD

Dataset $(\rightarrow)$ Method $(\downarrow)$			(D3,	, D4)		(D5, D6)			( <b>D7, D8</b> )			Merge All				
	MM	DM	Noise	MN	A D	M N	loise M	M D	M N	loise N	/M	DM	Noise	MM	DM	Noi
Averaging	82.00	76.50	81.91	68.3	30 65	.64 6	8.27 69	.60 68	3.83 6	9.62 93	3.90	89.33	93.99	64.40	61.31	64.1
<b>Task Arithmetic</b>	85.50	81.90	85.89	72.2	20 71	.43 7	2.28 70	.60 70	).69 7	0.57 90	5.40	96.00	96.38	73.30	6.20	71.5
TIES	81.40	73.51	81.54	67.4	0 61	.90 6	7.26 69	.60 66	6.46 6	9.64 94	4.30	87.32	93.99	68.50	5.60	67.5
DARE	86.00	81.74	85.83	72.4	0 71	.23 7	2.24 70	.60 70	0.73 7	0.61 90	5.40	95.94	96.38	73.50	6.00	70.8
Average	83.73	78.41	83.79	70.0	08 67	.55 7	0.01 70	.10 69	0.18 7	0.11 95	5.25	92.15	95.19	69.93	19.78	68.5
Tabl	e 1. Acc	curacy curacy conset $(\rightarrow)$	ompari	son be	etween	Model	Merging	g (MM)	, Direc	t Mergin	$\frac{1}{100}$ (DM	I), and I	Noise S	Simulat 	ion	
	Met	Method $(\downarrow)$			SVD	MM	SVD	MM SVD		MM	SVD	MM	SVI	-		
	Aver	aging	8	2.00	81.80	68.30	67.90	69.60	69.60	93.90	93.90	64.40	) 64.1	0		
	Task	Arithn	netic 8	5.50	85.74	72.20	71.82	70.60	70.47	96.40	96.3	73.30	) 72.2	3		
	TIE	S	8	31.40	78.10	67.40	66.06	69.60	69.27	94.30	90.61	68.50	) 73.2	3		
	DAF	RE	8	6.00	85.68	72.40	71.99	70.60	70.49	96.40	96.30	73.50	) 72.2	0		
	Aver	age	8	3.73	82.83	70.08	70.00	70.10	70.08	95.25	94.40	69.93	3 70.4	4		
		Table	2. Acc	uracy	compa	rison b	etween c	f LoR	$A_{MM}$	vs SVD	$_{16}(Lo.$	$RA_{MM}$	<sub>1</sub> ).			
	Ran	nk (.l.)	Metho	od (.).	(D1.	D2)	(D3, D4	) (D5	. D6)	( <b>D7. D</b>	8)		Averag			
		(*)	T	r		, 00	(5.10	()	20	02.50	- /	10	70.16			
	8	8 LC M		MSVD 8		.90 40	67.20	68.20 69.40		82.50	61	2.70	77.00			
			IVIIVI V	510	01.	40	07.20	09	.40	95.70	0.	5.70	77.90			
	16	$     \begin{array}{c}                                     $		Lora Lego77.MM SVD81.Lora Lego76.MM SVD82.		77.90		68.40		82.30	61	1.90	71.08			
						.80	67.90	69.60 68.60 69.60		93.90	64	4.10	78.30			
	32					40	64.70			87.60 93.90	6	3.3	72.12			
	52					00	68.30				64.30		78.50			
	Table 3	. Accur	acy cor	nparis	on bety	ween S	$SVD_r(L)$	$pRA_M$	$_M$ ) (Lo	RA aver	aging)	and Lo	oRA L	EGO.		
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SVD-Based Approach Outperforms State-of-the-Art 197 **Methods**. Next, we compare  $SVD_r(L_{MM})$  with a SOTA LoRA<sub>DM</sub> merging method. LoRA LEGO (Zhao et al., 199 2024) is a method that decomposes LoRA modules into 200 rank-1 units and then clusters them together. The centroid of each cluster contributes 1 rank to the final merged-LoRA, thereby giving users fine-grain control of the merged rank. However, LoRA LEGO introduces the same noise present 204 in  $LoRA_{DM}$  as LoRA units from different adapters are averaged together. In our comparison, we select r = [8, 16, 16]206 32] and use simple averaging to compute  $L_{MM}$ . As shown in Table 3, for rank 8,  $SVD_r(L_{MM})$  achieves +7.74% ac-208 curacy compare to Lego LoRA, +7.22% at rank 16, and 209 +6.38% at rank 32. This indicates that  $SVD_r(L_{MM})$  is 210 able to outperform SOTA  $L_{DM}$  methods, while retaining 211 the ability to dynamically select merged LoRA rank. 212

Linear Mode Connectivity Analysis We demonstrate that  $L_{MM}$  is LMC while  $L_{DM}$  is not. For each task, we interpolated the pairs of LoRAs with coefficients  $a \in$  [0.1, 0.2, ...0.9, 1.0], and calculate the average cross entropy loss on the two test sets. We then plot the interpolated losses and the loss of the interpolated models. Models are LMC when the interpolated model's loss is less than the interpolated loss for all interpolation values. Fig. 1 shows that  $L_{MM}$  is LMC on all datasets, whereas  $L_{DM}$  is only LMC on a single dataset.

Interference Impact and Scaling Effects As shown in section 3.3,  $L_{DM} = L_{MM} + M$ . To simulate the impact of M, we sample a noise matrix  $N \in \mathbb{R}^{n \times n}$  with  $N_{ij} \sim \mathcal{N}(mean(M), std(M))$  and demonstrate that  $L_{MM} + N$ performs better than or equal to  $L_{DM}$ , indicating that the term M is source of degradation in merging performance. In Table 1, adding N to  $L_{MM}$  has a minimal effect on accuracy (-0.025% difference on average), however, when merging on eight LoRA, this noise actually does better by +0.143%.

# 5. Conclusion

We demonstrated that merging LoRA with Direct-Merge can maintain a memory-efficient low-rank structure but introduces interference terms that degrade model performance and break LMC. By using truncated SVD on top of Mutliplied-Merge, we show that it is easy to retain memoryefficient structure with virtually no performance cost.

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