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Paper under double-blind review

ABSTRACT

Unlearning in Large Language Models (LLMs) has gained increasing attention in recent years due to its critical role in ensuring ethical and legal compliance. Although significant progress has been made in developing unlearning algorithms, relatively little attention has been devoted to the *data perspective*. In particular, the role of retain-set selection in preserving *model utility* remains underexplored, even though it is critical for making unlearning practical in real-world applications. In this work, we explore strategies for constructing effective retain sets by adapting methods from coresets selection and prior unlearning research. We evaluate these approaches on two complementary datasets: *(i)* a monotonic dataset built from a benchmark dataset, and *(ii)* a mixed, larger-scale dataset combining WPU, TOFU, and Dolly, which better reflects realistic scenarios where forget and retain samples are not explicitly defined. We find that *model utility* is strongly influenced by the model’s representations within the selected retain set for heterogeneous dataset. Moreover, we show that simply choosing data samples with high semantic or syntactic similarity to the forget set can yield substantially better results than standard coresets techniques. To the best of our knowledge, this work represents the first systematic study of practical retain-set selection for LLM unlearning, highlighting its importance and the challenges it poses in practical settings.

1 INTRODUCTION

Large Language Models (LLMs) (Vaswani et al., 2017), with their remarkable capabilities across a wide range of tasks and training on vast amounts of web data, inevitably face alignment challenges. These models often memorize undesirable information (Carlini et al., 2021; Golatkar et al., 2020) such as personal data, copyrighted material, and harmful content which can be outputted and potentially misused (Staab et al., 2024). Alignment techniques, such as Reinforcement Learning from Human Feedback (RLHF) (Ouyang et al., 2022) and red teaming, have been introduced to mitigate these risks, but they require substantial human effort. Furthermore, these methods do not fully address legal requirements, such as the GDPR’s *Right to be Forgotten* or the AI Act. Machine unlearning (Yao et al., 2024; Miranda et al., 2025) has emerged as a promising alternative, aiming to remove specific undesired information and abilities while preserving overall model utility.

LLM unlearning generally has two key objectives: (1) eliminating the specified target knowledge along with its associated capabilities, and (2) preserving the model’s overall integrity by preventing degradation of non-target knowledge and abilities Liu et al. (2025). Achieving these objectives at the same time, requires two datasets: the *forget set* D_f , containing the data to be removed, and the *retain set* D_r , containing the knowledge to be preserved. By definition D_r and D_f are disjoint, and together they cover the complete corpus D , i.e., $D_r = D \setminus D_f$ and $D_f = D \setminus D_r$. Since D_f is usually smaller than D_r , there is often a disproportionality in the dataset sizes. Mainstream unlearning approaches (Zhang et al., 2024; Yuan et al., 2025; Maini et al., 2024; Liu et al., 2022; Jang et al., 2023) address the two objectives through a weighted combination of losses: maximizing the forget loss on D_f while minimizing the retain loss on D_r , typically formulated as (Ji et al., 2024).

$$\min_{\theta} \mathbb{E}_{(x,y) \in \mathcal{D}_f} [\ell_f(y | x; \theta)] + \lambda \mathbb{E}_{(x,y) \in \mathcal{D}_r} [\ell_r(y | x; \theta)], \quad (1)$$

054 θ denotes the model parameters subject to update during unlearning, initialized from the pretrained
 055 model. The terms \mathcal{L}_f and \mathcal{L}_r denote the forget loss (unlearning objective) and the retain loss (utility-
 056 preserving objective), respectively. Both are evaluated when generating a response y from an input
 057 x under parameters θ . The coefficient $\lambda > 0$ functions as a regularization parameter, balancing the
 058 trade-off between forgetting and retention. Based on the above, unlearning performance is measured
 059 along the two objectives, **Forget Quality (FQ)** focuses on objective (1) capturing how effectively the
 060 model forgets the targeted knowledge, i.e., the extent to which the undesired information is no longer
 061 recoverable through direct or indirect queries. In contrast, **Model Utility (MU)** focuses on objective
 062 (2), reflecting how well the model retains its general capabilities, ensuring that unlearning does not
 063 significantly impair its performance on unrelated tasks or knowledge domains. *FQ* is applied on D_f
 064 and *MU* applied on D_r .

065 Early unlearning methods (Yao et al., 2024; Zhang et al., 2024) focused solely on maximizing the
 066 loss on D_f , often leading to **degeneration behavior** and **catastrophic forgetting** (Jang et al., 2023;
 067 Ji et al., 2024). D_r was later introduced as a regularization set to mitigate these issues. The retain
 068 loss \mathcal{L}_r is typically defined as the standard cross-entropy next-token prediction loss computed over
 069 D_r . Much of the research in LLM unlearning has focused on developing algorithms to balance
 070 the forgetting and retention objectives. Prominent approaches include: (i) Gradient Ascent and its
 071 variants (Jin et al., 2025; Wang et al., 2025), which reverse the training loss to enforce forgetting;
 072 (ii) preference optimization methods such as DPO (Rafailov et al., 2023) and its extensions NPO
 073 (Zhang et al., 2024) and SimNPO (Fan et al., 2024), which indirectly bound the forgetting objective
 074 by increasing preference for desired responses; (iii) representation misdirection techniques such as
 075 RMU (Li et al., 2024), which disrupt internal representations tied to the undesired knowledge; (iv)
 076 logit-based methods that leverage auxiliary models to reduce preference for D_f (Ji et al., 2024);
 077 and (v) model-editing strategies employing task vectors or surgical weight modifications to remove
 078 specific knowledge (Wu et al., 2023; Jia et al., 2024; Hase et al., 2023). Across these approaches,
 079 D_r is incorporated either directly in the loss function or as part of separate training stages to mitigate
 080 catastrophic forgetting.

080 Although these algorithmic advances are significant, they have been primarily evaluated on bench-
 081 mark datasets that are relatively simple, i.e., monotonic in structure, and offering a clear separation
 082 between forget and retain sets. In addition to this, they typically rely on the full retain set provided.
 083 In contrast, real-world scenarios are far more complex: the pre-training dataset D may span giga-
 084 bytes of data and contain hundreds of thousands of samples, especially in specialized domains such
 085 as law or medicine, making it impractical to use the entire dataset (excluding D_f) as the retain set.
 086 This challenge motivates the question: **“How can we select a subset D_s from D_r that faithfully**
 087 **reflects D_r while preserving model utility?”** Recent works (Ren et al., 2025; Geng et al., 2025)
 088 have raised this question but no comprehensive methodology has been established to address it.

089 In this work, we address the bottleneck problem of retain set selection from a *pre-unlearning* per-
 090 spective. We perform *early selection* of D_r . We draw on established research of “coreset” selection
 091 methods, adapting it to the unlearning domain and conduct extensive empirical studies on these se-
 092 lected retain sets and on their impact. More specifically, we investigate which samples are selected
 093 for retention and examine which properties of the retained data influence model utility.

094 Our analysis indicates a key pattern: a statistically significant negative correlation between the vari-
 095 ance of the model’s hidden state representations (hidden state variance, HSV) for data-points in the
 096 selected retain set and the model’s overall utility, suggesting that higher variance in retained data
 097 can reduce model utility; In other words, unlearning with widely distributed retain data points tends
 098 to reduce model utility. Building on this insight, and informed by prior work showing that syntac-
 099 tically similar samples are most affected during unlearning (Chang & Lee, 2025), we propose two
 100 simple selection strategies: retaining semantically closer samples and retaining syntactically closer
 101 samples. We then perform extensive empirical studies on D_r using coresnet-based methods.

102 2 RELATED WORK

103 2.1 DATA SELECTION

104 Data selection involves choosing a subset of data from a larger dataset to train machine learning
 105 models efficiently. These methods aim to reduce computational costs without compromising per-

108 formance. Typical paradigms range from heuristic-based selection (e.g., statistical properties, distances) to optimization-based methods (e.g., ranking samples based on loss values, gradients, or forgetting events). Common goals in data selection include **distribution matching** and **distribution diversification** (Albalak et al., 2024).
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114 2.1.1 DATA SELECTION IN LARGE LANGUAGE MODELS

115
 116 In LLMs, data selection is critical for achieving state-of-the-art performance across tasks such as
 117 reasoning, instruction tuning, and alignment (e.g., Deepseek V3 (DeepSeek-AI et al., 2025), WizardLM (Xu et al., 2025), Vicuna (Peng et al., 2023), Zephyr (Tunstall et al., 2023)). Typical pipelines
 118 include filtering (e.g., language, toxicity, PII), de-duplication, and data mixing. Instruction-tuning
 119 datasets often exploit larger models (e.g., GPT-4) for sample annotation, as in DEITA (Liu et al.,
 120 2024a), Instag (Lu et al., 2024), and AlpagaSus (Chen et al., 2024), which assess sample complexity,
 121 diversity, and quality. While effective, these methods still require costly tagging and pre-selection
 122 procedures.
 123

124 2.1.2 CORESET SELECTION

125
 126 Coreset selection aims to identify a representative subset of data that preserves key distributional
 127 properties while maintaining near full-data performance. Approaches in the literature assign impor-
 128 tance scores to samples using training dynamics (e.g., gradient norm, error vector norms, forgetting
 129 scores) (Paul et al., 2021; Toneva et al., 2019) or emphasize diversity through clustering distances
 130 and coverage criteria (Xia et al., 2023; Zheng et al., 2023). Optimization-based methods lever-
 131 age gradient information to construct subsets (Mirzaoleiman et al., 2020; Killamsetty et al., 2021;
 132 Pooladzandi et al., 2022). In LLMs, sample influence can be estimated via gradient similarity with
 133 validation data (Xia et al., 2024).
 134

135 Recently, coresnet selection has been applied to unlearning: Patil et al. (2025) prune forget sets using
 136 anomaly detection on hidden representations, balancing forgetting and utility preservation, while
 137 Pal et al. (2025) investigate underlying coresnet behaviour (in D_f) in LLM unlearning benchmarks.
 138

139 2.1.3 LLM UNLEARNING AND DATA PERSPECTIVES

140
 141 Dynamic unlearning methods (Bărbulescu & Triantafillou, 2024) iteratively select highly memorized
 142 forget-set samples, and gradient-based approaches (Tian et al., 2024) target sensitive parameters for
 143 unlearning. While these methods focus on the model perspective, they highlight the importance of
 144 data selection. From a retain-set perspective, Chang & Lee (2025) show syntactic neighbors are
 145 highly influential and should be included in benchmark datasets. Bushipaka et al. (2025) explore
 146 constructing D_r with multiple neighbors for benchmarks.
 147

148 Compared with existing studies, our approach differs in two key aspects. First, we select D_r using
 149 coresnet mechanisms in realistic unlearning scenarios rather than relying on neighbor-based construc-
 150 tions for benchmark datasets. Second, coresnet selection does not require well-maintained datasets to
 151 identify syntactic or semantic relationships, making it more practical for real-world applications.
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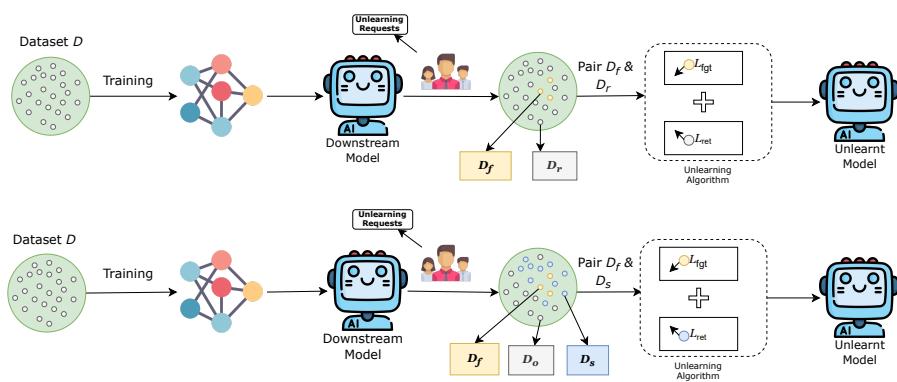
153 2.1.4 IMPORTANCE OF RETAIN SET

154
 155 (Ko et al., 2024)’s work on text-to-image diffusion model unlearning shows that unlearning without
 156 a diverse D_r leads to degraded image quality and poor text-image alignment, showing how retain
 157 data stabilizes model outputs when concepts are removed. In LLMs, (Thaker et al., 2025) show that
 158 narrowly defined forget and retain sets lead unlearning to overfit on the test queries. Beyond MU
 159 preservation, D_r is also used in adversarial attacks on the forgotten samples. For instance, (Łucki
 160 et al., 2024) find that an unlearned model via RMU shows a significant drop in FE, when finetuned
 161 with just 5 unrelated samples from the D_r .

162 3 METHOD
163164 3.1 PROBLEM STATEMENT
165

166 Assume we have a downstream task LLM, instruction-tuned on general knowledge, which has been
167 further fine-tuned on a dataset D containing undesired knowledge that must be removed. Our ob-
168 jective is to select a subset of the retain set, $D_s \subset D_r$, that preserves the model's knowledge and
169 capabilities as they were prior to unlearning.

170 Here, $D_r = D \setminus D_f$ is the retain set, and a sample $s_i = (x_r, y_r) \in D_r$ is selected if $s_i \in D_s$. The
171 final subset D_s should be substantially smaller than D_r yet sufficient to maintain model utility. In
172 our experiments, we focus on **entity-level unlearning**, removing all knowledge related to a specific
173 concept or individual. Figure 1 illustrates this process.



188 Figure 1: Top: the retain set D_r is traditionally the full dataset D minus the forget set D_f . Bottom:
189 our goal is to select a smaller subset $D_s \subset D_r$ that effectively represents D and preserves knowledge
190 after unlearning.

192 3.2 CORESET-BASED DATA SELECTION FOR UNLEARNING
193

194 To construct a reliable D_r in practical unlearning scenarios, we employ a rich set of coresets selection
195 methods, specifically **EL2N** and **MODERATE**. We observe a strong correlation between selected
196 D_s hidden state representation variance and model utility.

197 Additionally, we perform two alternative D_s selections:

198 1. Greedily selecting the top-n semantically closest samples to each forget sample.
199 2. Greedily selecting the top-n syntactically closest samples to each forget sample.

200 These strategies aim to maintain model knowledge while supporting efficient unlearning.

205 4 EXPERIMENTAL SETUP
206

207 We conduct entity-level unlearning experiments across two data regimes:

208 **(a) Monotonic Dataset:** We use the Wikipedia Person Unlearn (WPU) dataset (Liu et al., 2024b),
209 which consists of 100 entities along with their corresponding question-answer pairs extracted from
210 Wikipedia. This dataset follows a monotonic template, similar to other benchmark datasets such as
211 (Maini et al., 2024; Jin et al., 2024), providing Forget-Retain samples in a structured format covering
212 attributes like birthplace, profession, and other factual details.

214 **(b) Mixed Dataset:** To evaluate performance in a more heterogeneous setting, we combine WPU
215 with TOFU (Maini et al., 2024) and DOLLY (Ouyang et al., 2022). This mixed dataset introduces
diversity in content and format, better reflecting real-world unlearning scenarios.

Overall, this setting provides us with a realistic scenario where Unlearning has to be done in a downstream task such as generalized instruction tuning. The mixed dataset contains approximately 21k samples, with the majority sourced from DOLLY. For selecting Forget samples, we follow the splits provided by WPU (Liu et al., 2024b), namely (2, 20, 100) entities. Specifically, for the monotonic dataset, we designate $D_f = 2$ entities for unlearning. For the mixed dataset, we use $D_f = 20$ entities from WPU as the forget set.

Assessing MU across the full 21k samples is computationally expensive and unrealistic. Therefore, we create a test set that includes representative portions from each dataset to enable efficient evaluation. Further details on dataset construction and splits are provided in Appendix A.1.

4.1 UNLEARNING SETUP

Our experiments require a retain dataset for regularization. Accordingly, we focus on fine-tuning-based algorithms across three different paradigms. We employ **Gradient Difference** (Liu et al., 2022), **Simple Negative Preference Optimization** (Fan et al., 2024) and **Representation Misdirection Unlearning** (Li et al., 2024) for our experiments.

We do not perform vanilla unlearning (i.e., excluding the retain set) and always include the retain set for regularization. Unlike common practice, which randomly selects retain samples equal in number to forget samples for each epoch (Maini et al., 2024; Liu et al., 2024b; Yuan et al., 2025), we adopt a **Cyclic** setup (Jang et al., 2023). In this setup, D_f is repeatedly cycled until all D_s samples are paired with one forget sample during unlearning. Under the standard implementation (Maini et al., 2024), each epoch uses a retain batch matching the size of the forget batch, with retain examples randomly sampled from the D_r . The cyclic approach has been shown to outperform the standard implementation (Prempitis et al., 2025; Bushipaka et al., 2025), though it is computationally more expensive. In our setup, it is important to note that dataset partitions vary in cardinality, which implies that the number of steps per epoch is not constant across the 5%, 10%, and 20% splits.

4.2 METRICS

Unlearning behavior is best assessed using multiple complementary metrics. We employ a stack of metrics and aggregate them into two scores: **Forget Quality (FQ)** and **Model Utility (MU)**.

The individual metrics are as follows:

- **ROUGE-L**: measures verbatim memorization via word-level overlap.
- **Conditional Probability**: likelihood of the ground-truth answer.
- **Truth Ratio**: likelihood of choosing the correct answer over an incorrect one.¹
- **Cosine Similarity**: measures semantic similarity in the embedding space.

Following Yuan et al. (2025); Maini et al. (2024), we compute *Forget Quality (FQ)* as *1-Arithmetic mean* of ROUGE-L, Conditional Probability, and Truth Ratio on D_f excluding Cosine Similarity, where Cosine Similarity is excluded for robustness².

For *Model Utility (MU)*, we calculate the harmonic mean of ROUGE-L, Conditional Probability, and Cosine Similarity on D_r , excluding Truth Ratio.

Our primary focus is on preserving model utility, which requires analyzing the drop in MU before and after unlearning. To quantify this, we follow Chang & Lee (2025) and compute the *Relative Utility Drop (RUD)*:

$$RUD = \frac{MU_{pre} - MU_{post}}{MU_{pre}} \times 100$$

where MU_{pre} and MU_{post} denote model utility before and after unlearning, respectively.

¹In contrast to Maini et al. (2024), we do not adopt the p-value from the Kolmogorov–Smirnov test as FQ, since our setting does not allow comparison with a perfectly unlearned model—something even less feasible in real-world scenarios.

²We observe that embedding models may return non-zero similarity scores even for nonsensical generations (e.g., continuous dots).

270 Table 1: Baseline performance on WPU and Mix datasets before and after unlearning (using the full
 271 retain set D_r) for GradDiff, SimNPO, and RMU.

Method	WPU		Mix	
	FQ	MU	FQ	MU
Pre-unlearning	0.17	0.97	0.30	0.75
GradDiff	0.90	0.92	0.94	0.65
SimNPO	0.80	0.94	0.84	0.76
RMU	0.89	0.55	0.93	0.46

282 Further details about the metrics are provided in Appendix A.5.

284 4.3 CORESET METHODS

286 For our experiments, we evaluate three data selection strategies: **RANDOM**, **MODERATE** (Xia
 287 et al., 2023), and **EL2N** (Paul et al., 2021). Both MODERATE and EL2N were originally developed
 288 for computer vision classification tasks, but have been applied to LLM unlearning by Pal et al.
 289 (2025), from whom we gather the implementation procedure.

290 In particular, EL2N requires an initial warm-up run for a few epochs with the desired loss function.
 291 Since unlearning algorithms operate by manipulating loss functions, extracting a coresset with EL2N
 292 necessitates running the unlearning loss for several steps. To test whether this warm-up step can
 293 be simplified, we additionally experiment with using the standard cross-entropy loss during coresset
 294 extraction.

296 4.4 EXPERIMENTAL SETTING

298 We use the LLaMA 3.1 8B Instruct model (Grattafiori et al., 2024) as our base LLM. Both fine-
 299 tuning on the datasets and unlearning are performed using **LoRA** (Hu et al., 2022). All experiments
 300 are conducted on a single 40 GB A100 GPU. More details in Appendix A.2.

302 5 RESULTS

304 We conduct experiments using three splits of the retain set, D_r , corresponding to **5%, 10%, and**
 305 **20%**³ for the selection of D_s . **To maintain comparable evaluation across splits, we filter unlearnt**
 306 **models using method-specific *Forget Quality (FQ)* criteria: GradDiff models with FQ > 0.90 Sim-**
 307 **NPO with FQ > 0.85 and RMU with FQ > 0.90.** The number of training epochs is treated as
 308 a hyperparameter to reach this FQ threshold for all splits. This is crucial, as we are looking into
 309 preserving the *Model Utility*, when Forgetting is implemented successfully.

310 Note that we aim to recover the pre-unlearning MU, which is 0.97 for WPU and 0.75 for Mix. Using
 311 the full retain set D_r typically preserves MU closer to its pre-unlearning level. For the Mix dataset,
 312 we evaluate MU on the constructed test set. The results of these baseline runs are reported in Table 1.

314 5.0.1 PERFORMANCE WITH FULL-RETAIN (BASELINE UNLEARNING)

316 Table 1 shows the baseline utility on WPU and Mix using the full retain set before and after unlearn-
 317 ing. All three unlearning methods introduce a measurable degradation relative to the pre-unlearning
 318 model, but the magnitude varies substantially. **SimNPO** preserves utility the best across splits,
 319 matching or exceeding pre-unlearning MU on Mix and remaining close on WPU. **GradDiff** induces
 320 moderate degradation, with utility reductions on both datasets but still performing competitively in
 321 MU. In contrast, **RMU** exhibits the largest utility drop, especially in MU (0.55 on WPU vs. 0.97
 322 pre-unlearning), indicating instability even when the full retain set is available.

323 ³Initial experiments with 1% and 2% did not yield meaningful results and were therefore discarded.

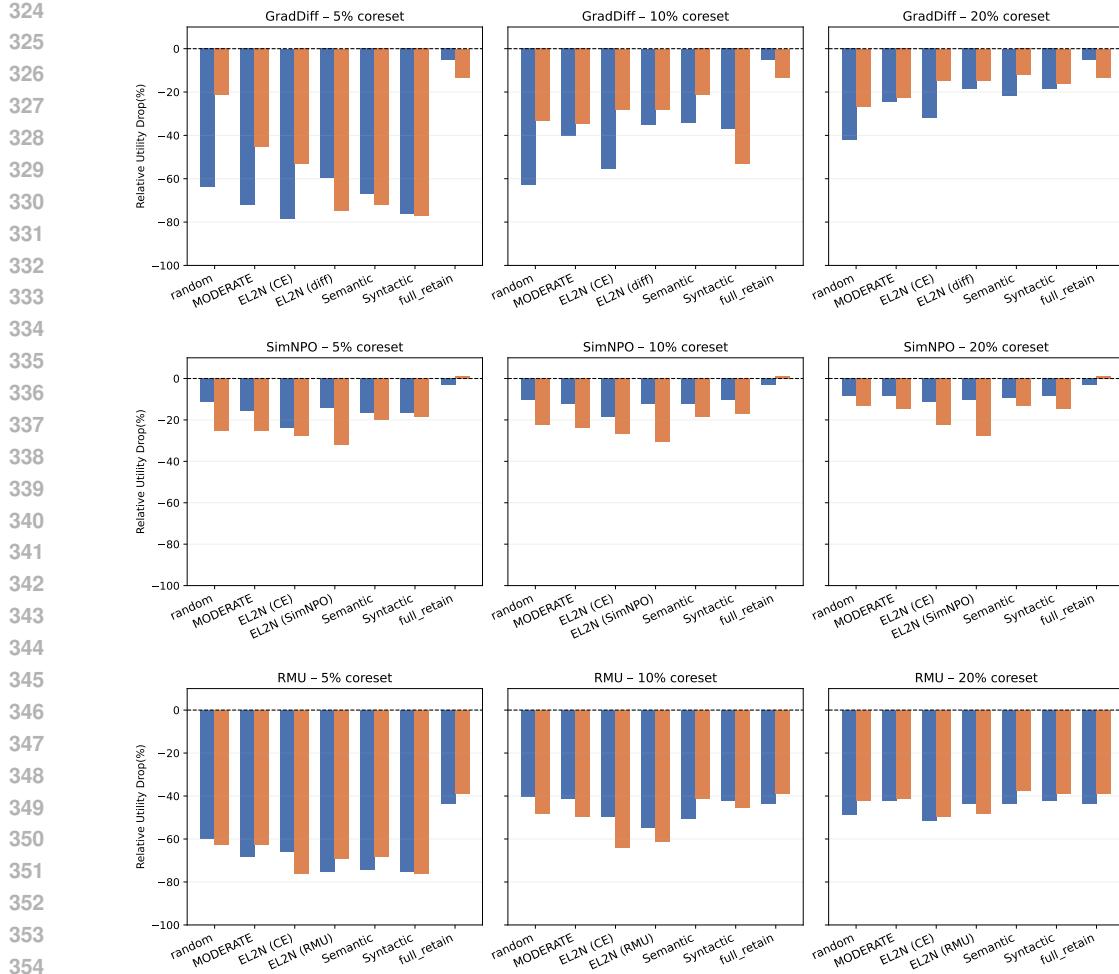


Figure 2: RUD scores for **WPU** **Mix** across 5,10,20% datasets for three unlearning algorithms. We find that targeted selection with semantic and syntactic consistently performs better than other selection mechanisms. However, full retain performs the best and often better than pre-unlearning (SimNPO) showing overfitting of retain set.

5.0.2 RELATIVE UTILITY DROP WITH CORESETS

Figure 2 reports the relative utility loss when using coresets subsets of size 5%, 10%, and 20%. Across all methods, **WPU consistently exhibits larger utility drops than Mix**, confirming it is the harder split to preserve performance on. For **Gradient Diff**, utility is highly sensitive to coresset size and selection strategy. At 5%, drops are large (60–80% on WPU), but increasing the coresset size substantially improves stability. At 20%, informed selection strategies—especially **EL2N (diff)**, **Semantic**, and **Syntactic** achieve the best performance, reducing Mix utility drop to as low as 12%. **SimNPO** shows the most stable behavior: utility drops are substantially smaller (often 8–13% at 20%) and vary minimally across selection methods. Syntactic and Semantic coressets consistently perform well, closely matching random sampling at larger sizes. For **RMU**, utility drops remain high across all coresset sizes and strategies, with limited improvement even at 20%. Even the best-performing subsets (Semantic, Syntactic) only reduce the Mix drop to 37–39%, while WPU remains above 42%, signaling persistent sensitivity to data reduction.

Finally, we examine the cluster-level distribution of selected retain samples. Figure 3 shows the log-preference ratio (logPref) for each cluster in the Mix (left) and WPU (right) datasets. Clusters with $\logPref(c) \geq 1$ are over-represented (red), $\logPref(c) = 0$ are neutral (grey), and $\logPref(c) \leq 1$ are

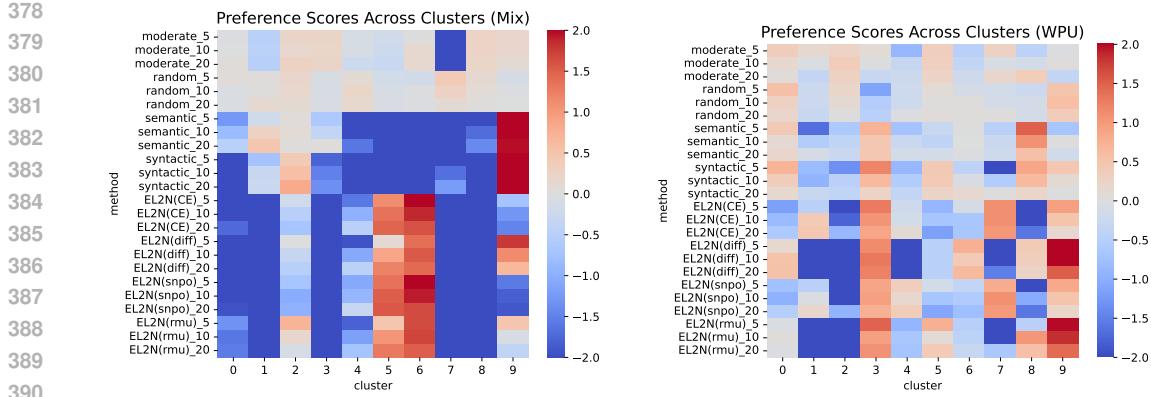


Figure 3: Log-preference ratio (logPref) for clusters in Mix (left) and WPU (right). Clusters with $\logPref(c) \geq 1$ are over-represented (red), $\logPref(c) = 0$ neutral (grey), and $\logPref(c) \leq 1$ under-represented (blue).

under-represented (blue). This visualization allows us to compare how different selection methods distribute samples across clusters without interpreting their effect on utility or forgetting.

6 DISCUSSION

Our experimental results reveal important insights regarding data selection strategies for unlearning in LLMs. In the following, we analyze the effectiveness of different coresets methods, examine per-source behavior in heterogeneous datasets, investigate the role of hidden state variance, explore semantic and syntactic selection strategies, and study the impact of cluster-level preferences on model utility and forgetting performance.

Effectiveness of Coreset Methods and Unlearning Algorithms. Across both the full-retain-set and coresset experiments, several consistent patterns emerge. First, SimNPO is the most robust and utility-preserving method, both when using the full retain set and when approximating it via a coresset. Its relative utility drop remains small even with only 5–10% of the data, and it shows little sensitivity to the choice of selection heuristic. This suggests that SimNPO’s update rule is inherently stable to data sparsification.

Second, Gradient Diff benefits the most from high-quality selection signals. Its performance varies widely depending on coresset choice, especially at small sizes. However, when paired with targeted selection strategies like EL2N (diff) or semantics-driven sampling, GradDiff approaches low relative utility loss at larger coresset sizes, indicating that the gradients it relies on can be well-approximated by carefully chosen examples.

Third, RMU remains the least stable method, showing substantial degradation even with the full retain set and only marginal improvements from any selection strategy. The method appears fundamentally sensitive to removing data from the retain distribution, suggesting its objective does not generalize well under distribution thinning.

Finally, the results highlight a dataset-level trend: WPU is uniformly harder to maintain utility on than Mix, with larger degradations across all methods, coressets, and sizes. This indicates that WPU’s distribution has higher dependency on the retained samples, making it more susceptible to information loss during unlearning.

Hidden State Variance as a Heuristic. Following (Skean et al., 2025; Tang & Yang, 2025; Duan et al., 2024) we use the last token penultimate layer hidden state representations for our analysis. We observe that **Hidden State Variance (HSV)** of D_s correlates strongly with **Relative Utility Drop (RUD)** across all the three unlearning algorithms with GradDiff ($\rho = 0.71, p = 0.01$), RMU ($\rho =$

432 0.62, $p = 0.03$) and SimNPO ($\rho = 0.7, p = 0.01$). In contrast, HSV correlates with Forget Quality
 433 only for GradDiff ($\rho = 0.64, p = 0.02$), with no significant relationship for RMU or SimNPO. This
 434 suggests that Variance in D_s consistently amplifies utility degradation, and in case of GradDiff, also
 435 improves the forgetting performance, revealing a method specific trade off. and moderately with
 436 Forget Quality on the Mix dataset, but not on WPU. This suggests that higher variance in D_s leads
 437 to greater utility drop but also facilitates forgetting, highlighting a trade-off.

438 Additionally, we conducted a controlled experiment in which we partitioned the full retain set into
 439 three subsets based on HSV: low, medium, and high. Using the 10% split, we ran Unlearning
 440 experiments across all the three algorithms and observed a consistent pattern: the medium-variance
 441 subset yielded the best performance, followed by the high-variance subset, with the low-variance
 442 subset performing the worst. Together with the correlation results, this experiment suggests that
 443 HSV does not exert a purely linear effect on unlearning, instead performance peaks at intermediate
 444 variance, indicating a non-linear, possibly inverted-U relationship. Apart from this, we also find the
 445 expected correlations such as RUD negatively correlated to Retain length and FQ. More details in
 446 Appendix:7.

447
 448

449 **Semantic and Syntactic Selection.** Semantic and syntactic selection methods are more effective
 450 than coresnet-based approaches, especially on the Mix dataset. Semantic similarity, in particular with
 451 GradDiff, achieves comparable performance to full-retain with only 20% D_s . However, when the
 452 full_retain is unlearnt for *same number of epochs* as semantic, it performs substantially better (2%
 453 RUD). The downside is computational cost: full-retain requires 13 hours, whereas semantic method
 454 finishes just under 2 hours. This demonstrates that semantic selection can recover approximately
 455 85% of pre-unlearning utility while using an order of magnitude less compute. Finally, we note that
 456 relying on full-retain undermines the purpose of unlearning, since it effectively amounts to retraining
 457 or fine-tuning the model on the entire D_r again excluding D_f .
 458

459 **Cluster Preferences.** Cluster-level analysis shows that semantic and syntactic methods dispropor-
 460 tionately select samples from clusters heavily populated by forget samples (e.g., clusters 9 and 2 in
 461 Mix). This selective over-representation explains their effectiveness, while coresnet methods—which
 462 aim to diversify—suffer higher utility drop A.6.3.

463 **7 CONCLUSION**
 464

465 In this study, we address a key limitation in LLM unlearning: the selection of a retain set that
 466 preserves Model Utility. We leverage techniques from the coresnet selection literature and apply
 467 them to entity-level unlearning, evaluating performance on two data regimes: a monotonic dataset
 468 (WPU) and a diverse, mixed dataset (Mix). Across both regimes, we find that it is challenging to
 469 fully recover the pre-unlearning Model Utility. For the monotonic dataset, the selected subset D_s
 470 shows no significant correlation with utility, indicating that standard coresnet strategies may not be
 471 informative in highly structured or homogeneous data regimes.

472 In contrast, for the mixed dataset, hidden state variance (HSV) analysis reveals that increasing
 473 $Var(D_s)$ leads to a higher Relative Utility Drop (RUD) but also improves Forget Quality. Moti-
 474 vated by this, we implement simple semantic and syntactic-based selection strategies that choose
 475 top samples most similar to each forget sample. These approaches consistently outperform tradi-
 476 tional coresnet methods and, in some cases, even exceed the performance of using the full retain set,
 477 demonstrating that targeted retain set selection based on embedding proximity can effectively bal-
 478 ance utility preservation and forgetting. Cluster-level analysis further indicates that these methods
 479 preferentially select samples from clusters containing forget data, highlighting the importance of
 480 considering both dataset structure and relationships between retain and forget samples.

481 Our findings suggest that while coresnet methods provide a strong starting point, understanding the
 482 distribution of forget samples in the embedding space and leveraging semantic or syntactic proximity
 483 can lead to superior results, especially in heterogeneous datasets, which can be considered as a proxy
 484 of real-world scenarios. However, we acknowledge that the observed behavior may not generalize to
 485 all unlearning scenarios, such as those involving copyrighted, or harmful content, where additional
 486 constraints and safeguards may be required.

In other words, while our study demonstrates the effectiveness of semantic and syntactic-based retain set selection, several avenues remain for future exploration. First, extending these techniques to handle unlearning requests beyond entity-level data—such as instance-level privacy sensitive, copyrighted, or harmful content—would test their generality and robustness. Second, adaptive or dynamic selection strategies that take into account model feedback or embedding evolution during fine-tuning could further improve the trade-off between Model Utility and Forget Quality. Finally, evaluating these methods on larger-scale, multi-domain LLM benchmarks and integrating interpretability or explainability techniques may provide additional insights into why certain selections succeed and inform best practices for practical LLM unlearning.

8 LIMITATIONS

LLM unlearning is inherently a dynamic process, requiring continual updates to the model. In contrast, most existing data selection methods are designed as one-time procedures, often involving computationally expensive setups performed prior to training. These static methods are not directly suited for unlearning and would require adaptation to accommodate continuous model updates. Additionally, existing selection strategies are optimized for diversity, ensuring broad dataset coverage, but unlearning requests, particularly entity-level privacy may instead involve densely clustered or non diverse samples. Our experiments show that despite constructing a mixed dataset, the post-training hidden state representations of D_f tend to cluster closely, making diversity oriented selection mechanisms less effective in this context.

As mentioned above, Unlearning is a dynamic process and requires continuous recycling of the model. Often LLM Unlearning is tested in Sequential Setup and found that it is more effective than batch Unlearning. We did not test this setting and would be testing in the later works.

while we show that 20% of the retain set (D_r) is sufficient to achieve model utility comparable to that of the full D_r , this proportion becomes impractically large for large-scale datasets (e.g., 800k samples). In such scenarios, allocating 20% of the data to unlearn only a small forget set (e.g., 100 samples) is inefficient. Future work should therefore focus on identifying and selecting the most relevant subset of D_r , which could substantially reduce this overhead while maintaining unlearning effectiveness. Our work uses only a single Unlearning method and also only one regularization method. Additionally, our experiments are conducted only on single LLM and on only two data regimes. We acknowledge that Unlearning requests can often be varied, such as in Privacy or Copyright contexts. These scenarios require a robust testing of various use cases and D_s selection mechanism.

9 REPRODUCIBILITY STATEMENT

We provide code in both notebooks and python scripts. Notebooks consist of the dataset creation, coresnet methods for selecting D_s and ablation studies. Python scripts consist of the unlearning and evaluation. We provide a config file, which helps in configuring the settings for the Unlearning. Our anonymized code can be found at - link to the repo

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800 A APPENDIX

801 A.1 DETAILS ON THE DATA SET CREATION

802
 803 For the monotonic unlearning setting, we employed the Wikipedia Person Unlearn (WPU) dataset
 804 (Liu et al., 2024b), which contains 2,302 samples, including 10 designated samples corresponding
 805 to two entities that are intended to be forgotten. The WPU dataset was originally proposed for
 806 entity-level unlearning and is therefore well aligned with our objective.

807
 808 To simulate a more realistic downstream scenario, we further constructed a mixed dataset by com-
 809 bining WPU with the TOFU dataset (Maini et al., 2024) and the Dolly dataset (Ouyang et al.,
 810 2022). This mixture serves two purposes: Dolly contributes general-purpose question–answering

Table 2: Num epochs for each D_s on WPU and Mix datasets across coresets sizes.

Coreset	5%		10%		20%		Full Retain	
	WPU	Mix	WPU	Mix	WPU	Mix	WPU	Mix
random	25	4	15	4	10	4	—	—
MODERATE	25	5	30	5	25	5	—	—
EL2N (CE)	30	5	25	5	25	5	—	—
EL2N (diff)	40	5	60	5	55	5	—	—
Semantic	30	5	15	5	15	5	—	—
Syntactic	20	5	15	5	15	5	—	—
Full Retain	—	—	—	—	—	—	8	2

data, while WPU introduces sensitive information that needs to be unlearned. Prior to merging, we assigned unique identifiers to each sample, derived from the dataset and entity of origin, to maintain traceability. We also incorporated the extended version of WPU introduced by Bushipaka et al. (2025), which includes indirect neighbor samples and a predefined test set. For computational tractability, samples exceeding 512 tokens were discarded. The final combined corpus consisted of approximately 21k samples: 14.2k from Dolly, 4k from TOFU, and 2.8k from WPU. From WPU, we selected 20 entities (98 samples) as the forgetting set.

Evaluating model utility on the entire 21k-sample corpus would have been computationally prohibitive. Instead, we curated a balanced test set. Specifically, for WPU we adopted the test partition provided by Bushipaka et al. (2025). From TOFU, we randomly sampled 500 instances, while for Dolly we applied stratified sampling across categories to preserve distributional diversity. This resulted in a test set comprising 1,992 samples in total.

A.2 HYPERPARAMETERS FOR FINE-TUNING & UNLEARNING

For both Fine-tuning and Unlearning, we use LoRA Hu et al. (2022) since full fine-tuning and full unlearning is computationally expensive. For Fine-tuning, we used a batch size of 32, learning rate of 2e-5, LoRA rank=64, alpha =64 and for 10 epochs. Where as for Unlearning, we used a fixed batch size of 8, learning rate 1e-5, rank = 8, alpha = 16 for all the experiments. We used epochs as an hyperparameter (Table:2) to reach the FQ threshold of 0.90.

A.3 UNLEARNING ALGORITHMS

A.3.1 GRADIENT DIFFERENCE

Proposed by Liu et al. (2022) to mitigate the issues of Gradient ascent. It builds on the concept of Gradient Ascent, but not only aims to maximize the loss on forget set D_f , simultaneously minimizes the loss on the retain set D_r . This maintains the balance of forgetting and retaining. The loss function can be written as in equation 1.

Given D and its samples (x, y) , x is question and y is the answer. A pair $p_i = p(x_i, y_i) \in D$ and y_1, \dots, y_T are the answer tokens, we calculate Negative-Log-Likelihood (NLL) loss for p_i

$$\mathcal{L}(y \mid x; \theta) = \text{NLL}(y \mid x; \theta) = - \sum_{t=1}^T \log p(y_t \mid x, y_{<t}; \theta) \quad (2)$$

Gradient Ascent's main idea is to maximize the loss as opposed to the training objective of minimization by negating the loss. We can write it as

$$\mathcal{L}_{GA}(D_f; \theta) = - \mathcal{L}(y_f \mid x_f; \theta) \quad (3)$$

From eq 1 and eq 3 we can write **Gradient Difference** as:

864
865
866

$$\mathcal{L}_{GD}(\theta) = -\mathcal{L}(D_f; \theta) + \mathcal{L}(D_r; \theta) \quad (4)$$

867 A.3.2 SIMPLE NEGATIVE PREFERENCE
868869 A modified variant of Negative Preference Optimization (NPO) (Zhang et al., 2024) that retains its
870 core forgetting behavior by replacing the reference model with δ in the loss formulation of NPO.871 NPO which is already an optimized algorithm of DPO made for unlearning eliminates the use of
872 positive samples (often they are "IDK" samples), can be written as:
873

$$\mathcal{L}_{NPO, \beta}(\theta) = -\frac{2}{\beta} \mathbb{E}_{D_f} \left[\log \sigma \left(-\beta \log \frac{p(y | x; \theta)}{p(y | x; \theta_{ref})} \right) \right] \quad (5)$$

874 SimNPO is optimized version of NPO, removes the need for reference model θ_{ref} .
875

$$\mathcal{L}_{\text{SimNPO+retain}} = -\frac{2}{\beta} \mathbb{E}_{D_f} \left[\log \sigma \left(-\frac{\beta}{|y_f|} \log p(y | x; \theta) - \delta \right) \right] + \gamma \mathcal{L}(D_r; \theta) \quad (6)$$

876 A.3.3 REPRESENTATION MISDIRECTION UNLEARNING
877878 RMU (Li et al., 2024) assumes knowledge is encoded in model parameters and manipulates these
879 representations to suppress memorization signals for the forget set while preserving knowledge in
880 the retain set. Let $\phi(s; \theta)$ denote the embedding features of the model, the loss is given by
881

$$\mathcal{L}_{\text{RMU+retain}} = \mathbb{E}_{D_f} \frac{1}{|y_f|} \sum_{i=1}^{|y_f|} \|\phi([x, y^{<i}]; \theta) - c.u\|_2^2 + \mathcal{L}(D_r; \theta) \quad (7)$$

882 where u has elements randomly sampled from $[0,1)$ and c is a scaling hyper-parameter.
883884 A.4 DETAILS ON THE DATA SELECTION METHODS
885886 A.4.1 MODERATE
887888 The moderate coresset selection strategy was originally introduced in the context of classification
889 tasks, wherein samples are partitioned into clusters according to their class labels. Since, our setting
890 is instruction tuning, class labels are unavailable. We take the last token penultimate-layer repre-
891 sentations from the pre-unlearned model for the full retain set (excluding D_f). We then partition
892 it into four clusters using K-means algorithm. For each cluster, we determine its centroid and rank
893 samples according to their distance from this centroid. To identify representative points, we select
894 those whose distances are closest to the median within their respective clusters.
895896 A.4.2 EL2N
897898 The central idea of the EL2N method is that the importance of each forget sample z_f is quantified
899 by the expected early-learning loss, measured as the ℓ_2 -norm of the model's prediction error during
900 the early stages of training. Accordingly, the EL2N score for a forget sample is defined as
901

$$\chi(z_f) = \mathbb{E}_{\theta_t} \|f_{\theta_t}(x_f) - y_f\|_2, \quad \text{where } z_f = (x_f, y_f) \sim \mathcal{D}_f. \quad (8)$$

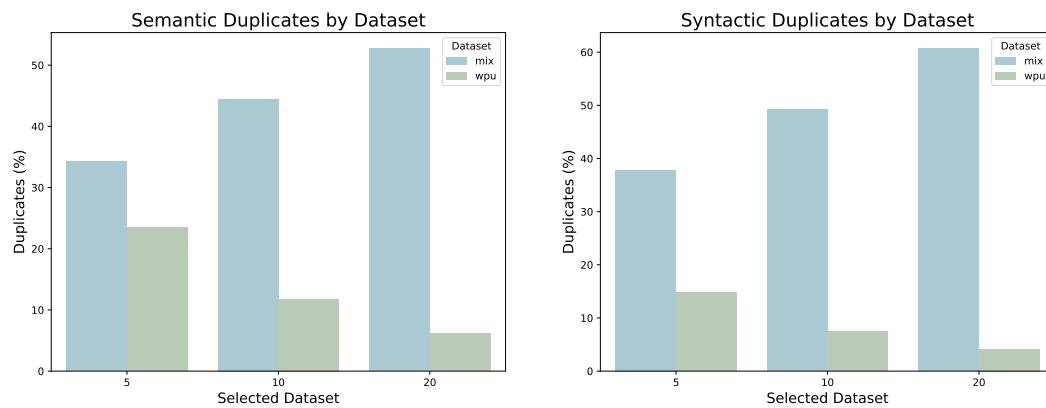
912 Here, the expectation is taken over snapshots of the model parameters θ_t from the early optimization
913 trajectory, which captures how easily each sample is learned. Samples with higher EL2N scores
914 correspond to those the model struggles to fit early on, and are therefore considered more influential.
915 In practice, we compute this expectation over the unlearning trajectory, approximating it using 2
916 epochs for the monotonic setting and 1 epoch for the mixed setting in our experiments. As in our
917 unlearning pipeline, this early trajectory includes a warmup phase based on the cross-entropy loss
918 and also with Unlearning loss.
919

918 A.4.3 SEMANTIC SIMILARITY
919

920 To calculate semantically closest samples to the forget samples, we used SBERT models. *all-
921 MiniLM-L6-V2* (Reimers & Gurevych, 2019) for WPU dataset and *bge-small-en-v1.5* (Xiao et al.,
922 2023) for Mix dataset. Then we picked the top semantically close samples to each forget sample by
923 allocating a certain sample size for each until globally we reach the desired D_s length. We didn't re-
924 move the duplicates cause multiple forget samples can be semantically closer to a few retain samples
925 and increase in variance of the samples leads to low Model Utility (look into section6).
926

927
928 A.4.4 SYNTACTIC SIMILARITY
929

930 In the light of recent analysis (Chang & Lee, 2025), that syntactic similarity is the most impacted
931 by LLM Unlearning, we opted to do pick top syntactically similar samples as a D_s . To assess
932 syntactic similarity between the forget and retain sets, each text was transformed into a sequence of
933 part-of-speech tags and pairwise distances were computed using the normalized edit distance. This
934 metric provides a principled quantification of structural correspondence, enabling a fine-grained
935 comparison of syntactic patterns across the two sets (Zhang et al., 2017). Similar to Semantic, we
936 allocate a certain sample size for each forget sample and incrementally increase it until we globally
937 reach the desired D_s length and we do not remove the duplicates.
938



940
941 Figure 4: Percentage of duplicates in the Semantic and Syntactic D_s . As the D_s size for Mix grows,
942 duplicates increases, whereas in WPU we find the opposite trend.
943
944

945 A.4.5 COMPUTATIONAL COSTS OF THE DATA SELECTION
946

947 From our empirical analysis, Random emerges as the least computationally expensive selection
948 strategy, whereas EL2N with Gradient Difference incurs the highest cost (fig: 5). We quantify this
949 cost as the total time required to identify the subset D_s , accounting for all pre-selection operations
950 specific to each method. For instance, EL2N necessitates a warm-up phase, while syntactic selection
951 requires part-of-speech tagging. Summing these pre-processing components provides a fair measure
952 of computational overhead across methods.

953 Interestingly, Semantic selection ranks among the most efficient approaches—second only to Ran-
954 dom—requiring only 30 seconds on the Mix dataset. Moreover, recent advances in semantic re-
955 trieval, particularly those leveraging vector databases, have made these methods increasingly practi-
956 cal and easier to implement compared to coresnet-based alternatives. By contrast, Syntactic selection
957 is considerably more time-intensive due to its reliance on CPU-bound processing rather than GPU
958 acceleration.

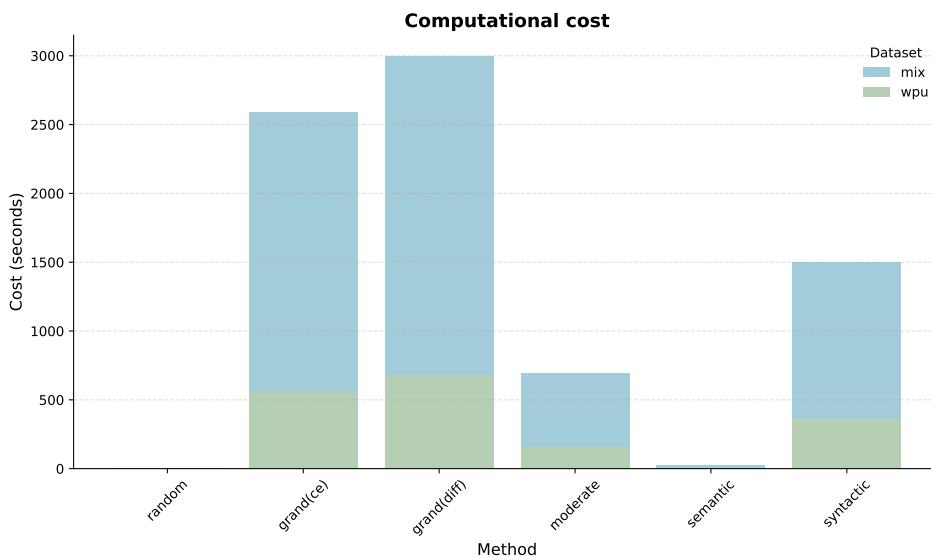


Figure 5: *Lower is better*, Time Taken for each method to select the D_s in seconds. EL2N methods require significant amount of time compared to others. Note: EL2N is misspelled as GrAND here.

A.5 EVALUATION METRICS

Following closely with (Maini et al., 2024; Yuan et al., 2025), we utilize a stack of metrics. All these scores are in range of $[0, 1]$.

A.5.1 ROUGE

We use ROUGE-L recall, which quantifies the model’s output and the ground-truth answer. Given a generated response $g(x; \theta_*)$ and the ground-truth answer y , we employ $ROUGE - L(g(x; \theta_*), y)$.

A.5.2 PROBABILITY

Following (Maini et al., 2024) we compute the conditional probability $P(a|q)$ for the forget and retain sets and normalize the score by raising it to the power of $1/|a|$. Therefore the Probability can be written as $P(a|q)^{1/|a|}$.

A.5.3 COSINE-SIMILARITY

Provides the semantic similarity between $g(x; \theta_*)$ and y . Following (Yuan et al., 2025), we embed both the responses with a Sentence-BERT model (Reimers & Gurevych, 2019), and calculate the cosine-similarity between them. For evaluation, we used gte-small (Li et al., 2023). To keep the scores in $[0, 1]$, we truncate the values less than 0. It can be written as

$$\max(\cos(g(x; \theta_*), y), 0)$$

A.5.4 TRUTH RATIO

Introduced by (Maini et al., 2024), is often used to compute a ratio comparing the likelihood of the correct answer to incorrect ones. As stated in their work, since fine-tuning may inflate the probability of the exact ground-truth phrasing, they suggest to use a paraphrased version of the y and average probabilities over multiple similarly formatted wrong answer. Let \tilde{a} is the paraphrased answer and \mathcal{A}_{pert} denote a set of five perturbed answers generated by GPT-4o. The truth ratio \mathcal{R}_{truth} is calculated as:

$$R_{truth} = \frac{\frac{1}{|\mathcal{A}_{pert}|} \sum_{\hat{a} \in \mathcal{A}_{pert}} P(\hat{a} | q)^{q/|\hat{a}|}}{P(\tilde{a} | q)^{q/|\tilde{a}|}}$$

1026 where $\mathcal{A}_{\text{pert}}$ is the perturbed answer set.
 1027

1028 A.5.5 RELATIVE MODEL UTILITY

1030 Introduced by Chang & Lee (2025) to understand the behaviour of neighbor sets. It is a simple ratio
 1031 to calculate the Utility drop pre-unlearning and post-unlearning.
 1032

$$1033 \text{RelativeUtilityDrop} = \frac{MU_{\text{pre}} - MU_{\text{post}}}{MU_{\text{pre}}} \times 100 \quad (9)$$

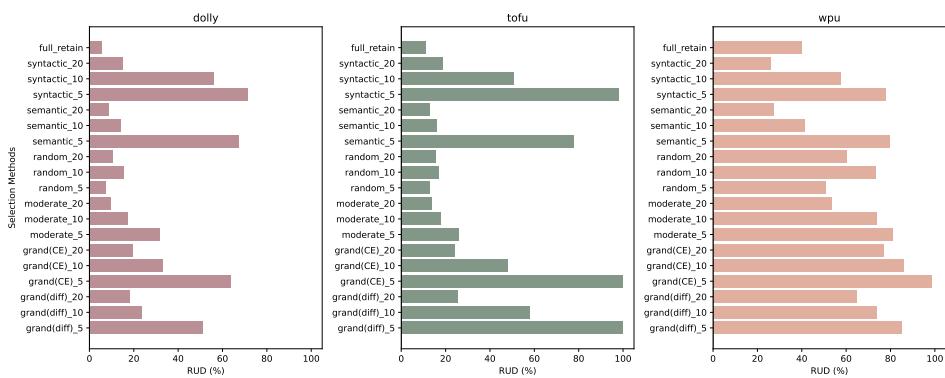
1036 A.6 RESULTS

1038 A.6.1 FORGET QUALITY AND MODEL UTILITY

1040 Table 3: Forget Quality and Model Utility for WPU and Mixed Datasets
 1041

1042 Coreset (\rightarrow)	FQ \uparrow			MU \uparrow		
	5	10	20	5	10	20
WPU Dataset						
random	0.94	0.94	0.94	0.35	0.37	0.56
MODERATE	0.94	0.95	0.96	0.27	0.58	0.74
EL2N (CE)	0.90	0.95	0.93	0.21	0.43	0.68
EL2N (diff)	0.95	0.95	0.95	0.30	0.64	0.79
Semantic	0.96	0.93	0.93	0.32	0.64	0.76
Syntactic	0.92	0.93	0.95	0.23	0.61	0.79
Mix Dataset						
random	0.92	0.93	0.93	0.59	0.50	0.55
MODERATE	0.94	0.93	0.93	0.41	0.49	0.58
EL2N (diff)	0.94	0.95	0.93	0.21	0.40	0.50
EL2N (CE)	0.94	0.94	0.93	0.13	0.35	0.46
Semantic	0.94	0.91	0.92	0.21	0.59	0.66
Syntactic	0.93	0.94	0.94	0.17	0.35	0.63

1062 A.6.2 RELATIVE UTILITY DROP FOR CORESET METHODS



1077 Figure 6: *Lower is better*, Relative Utility Drop (RUD) on the Mixed Test dataset across all the
 1078 different sources. WPU has the highest and Dolly has the lowest RUD across all the settings. Note:
 1079 EL2N is misspelled as GrAND here.

1080 Table 4: Relative Utility Drop ($\downarrow\%$) on WPU and Mix datasets across coresets sizes for Gradient Diff,
 1081 SimNPO, and RMU. Lower is better.

Coreset	5%		10%		20%	
	WPU	Mix	WPU	Mix	WPU	Mix
GradDiff						
random	63.92	21.33	62.89	33.33	42.27	26.67
MODERATE	72.16	45.33	40.21	34.67	24.74	22.67
EL2N (CE)	78.35	53.33	55.58	28	31.96	14.67
EL2N (diff)	59.59	74.67	35.05	28	18.56	14.6
Semantic	67	72	34.02	21.33	21.65	12
Syntactic	76.29	77.33	37.11	53.33	18.56	16
SimNPO						
random	11.34	25.33	10.31	22.67	8.25	13.33
MODERATE	15.46	25.2	12.37	24	8.25	14.67
EL2N (CE)	23.71	28	18.56	26.67	11.34	22.67
EL2N (SimNPO)	14.13	32	12.37	30.67	10.31	28.0
Semantic	16.49	20	12.37	18.67	9.28	13.33
Syntactic	16.49	18.67	10.31	17.33	8.25	14.67
RMU						
random	59.79	62.67	40.21	48	48.45	42
MODERATE	68.04	62.5	41.24	49.33	42.27	41.33
EL2N (CE)	65.98	76	49.48	64	51.55	49.33
EL2N (RMU)	75.26	69.33	54.64	61.33	43.3	48
Semantic	74.23	68	50.52	41.33	43.3	37.33
Syntactic	75.26	76	42.27	45.33	42.26	38.67

1111 In the main sections of the paper, we provided *RUD*, we report all the results in Table:3 that include
 1112 *Forget Quality* and *Model Utility*. As mentioned in previously in section:5, we made sure all the
 1113 Unlearning experiments crossed the threshold of $FQ > 0.90$. The FQ ranges from 0.90-0.95. We
 1114 also provide per source RUD scores for the Mix dataset. We find that WPU is the most impacted and
 1115 DOLLY is the least impacted. Given that all our forget samples are from WPU, this can be expected.

A.6.3 CLUSTERING

1116 Since investigating and finding relations between every pair is an NP-hard problem, we approach
 1117 this with clustering the HSV representations to $k = 10$ clusters with k-means algorithm. We chose
 1118 $k = 10$ based on the elbow method. We find that best performing methods select samples mostly
 1119 from clusters 9 and 2 (for Mix). A strange behavior is from Random (on mix), which selects almost
 1120 uniformly from all the clusters. Although small, Random 5 outperforms 10 and 20 (Mix). However
 1121 this selection needs to be studied more.

A.6.4 LOG PREFERENCE RATIO

1122 To analyze how different selection strategies distribute their retain sets across the representation
 1123 space, we introduce the *preference ratio*. For each cluster c , we compute the retain cluster share

$$p_{\text{retain}}(c) = \frac{\text{retain_count}(c)}{\text{retain_total}},$$

1124 and compare it to the baseline cluster share in the non-forget pool

$$q_{\text{pool}}(c) = \frac{\text{pool_count}(c)}{\text{pool_total}}.$$

1134 The preference ratio is then defined as
 1135

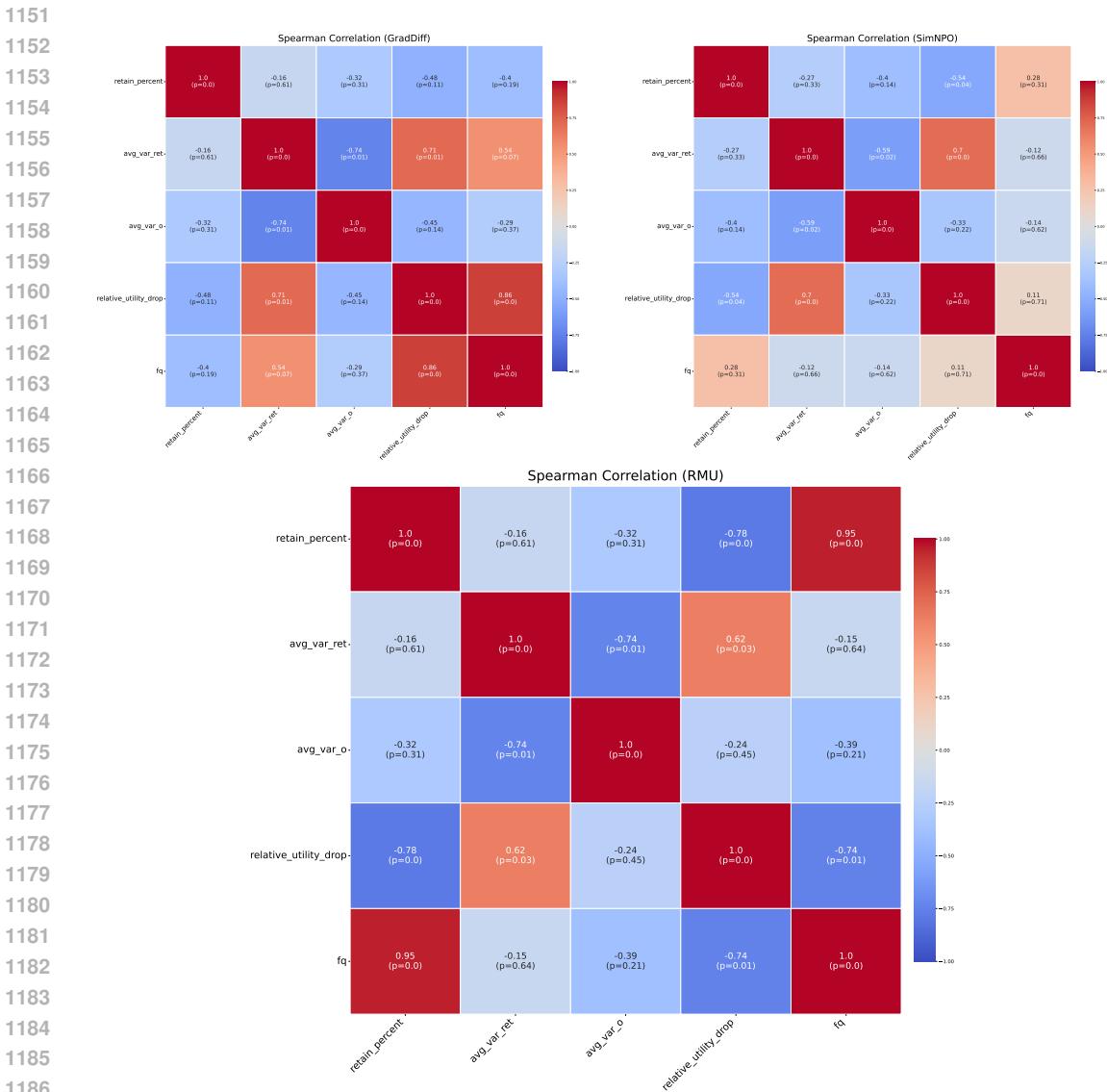
$$\text{pref_ratio}(c) = \frac{p_{\text{retain}}(c)}{q_{\text{pool}}(c)}.$$

1139 To improve interpretability, we report results in logarithmic scale:
 1140

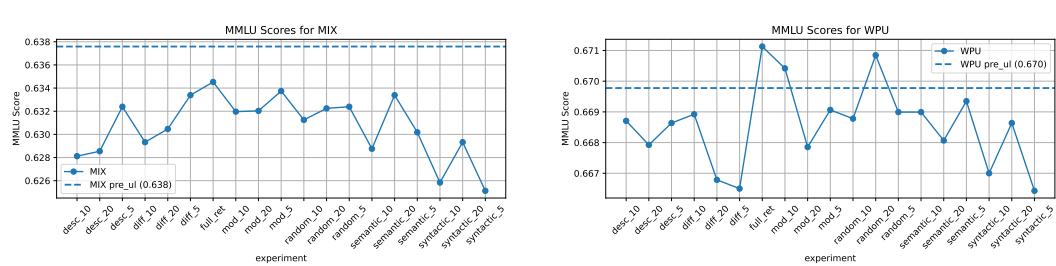
$$\text{pref_log2}(c) = \log_2(\text{pref_ratio}(c)).$$

1144 Here, $\text{pref_ratio}(c) > 1$ indicates that the method oversamples cluster c , $\text{pref_ratio}(c) < 1$ indicates undersampling, and $\text{pref_log2}(c) = 0$ denotes neutral selection. This formulation allows us
 1145 to visualize selection biases at the cluster level and to relate them to model utility and forgetting
 1146 efficacy.
 1147

1149 A.6.5 CORRELATIONS



1187 Figure 7: The correlations of $Var(D_s)$ data points with RUD and FQ for all the algorithms.

1188 A.7 MMLU SCORES
11891199 Figure 8: MMLU scores for GradDiff experiment. We do not find significant deviation in the scores
1200 of MMLU post-unlearning for all the methods.1201 A.8 CAUSALITY LINK
1202

Unlearning Method	Low		Medium		High	
	FQ	MU	FQ	MU	FQ	MU
GradDiff	0.94	0.51	0.93	0.58	0.93	0.57
SimNPO	0.87	0.51	0.85	0.54	0.84	0.54
RMU	0.91	0.34	0.92	0.38	0.92	0.35

1211 Table 5: Comparison across unlearning methods with low, medium, and high difficulty (FQ and
1212 MU).1213 A.9 LLM USAGE
12141215 In our study, we utilized LLMs for polishing the writing, research paper gathering, and coding.
1216 We used LLM to polish writing in all the sections of the paper, however we made sure it didn't
1217 hallucinate and add made up information. In the initial stages of our study, we used deep research
1218 tool for research papers gathering on coresets. For mix dataset construction, investigations, and parts
1219 of Unlearning we used LLM for coding.
1220