

# FROM EDUVISBENCH TO EDUVISAGENT: A BENCHMARK AND MULTI-AGENT FRAMEWORK FOR REASONING-DRIVEN PEDAGOGICAL VISUALIZATION

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## ABSTRACT

While foundation models (FMs), such as diffusion models and large vision-language models (LVLMs), have been widely applied in educational contexts, their ability to generate pedagogically effective visual explanations remains limited. Most existing approaches focus primarily on textual reasoning, overlooking the critical role of structured and interpretable visualizations in supporting conceptual understanding. To better assess the visual reasoning capabilities of FMs in educational settings, we introduce EduVisBench, a multi-domain, multi-level benchmark. EduVisBench features diverse STEM problem sets requiring visually grounded solutions, along with a fine-grained evaluation rubric informed by pedagogical theory. Our empirical analysis reveals that existing models frequently struggle with the inherent challenge of decomposing complex reasoning and translating it into visual representations aligned with human cognitive processes. To address these limitations, we propose EduVisAgent, a multi-agent collaborative framework that coordinates specialized agents for instructional planning, reasoning decomposition, metacognitive prompting, and visualization design. Experimental results show that EduVisAgent substantially outperforms all baselines, achieving a 40.2% improvement and delivering more educationally aligned visualizations.

## 1 INTRODUCTION

*"To truly teach is not to tell the answer, but to illuminate the path."*

While foundation models (FMs), such as diffusion models and large vision-language models (LVLMs), have been extensively adopted in educational domains (Chu et al., 2025; Wang et al., 2024), including pedagogical agents providing automated classroom assistance and science learning agents offering textual explanations of problem-solving processes (Wu et al., 2023), their applications have predominantly focused on text-based interactions (Wu et al., 2023; Xu et al., 2024). However, in education, especially K-12 settings, creating compelling visualizations is crucial for cognitive comprehension and overall learning effectiveness (Presmeg, 2006). Despite its importance, there is currently limited understanding of how FMs can effectively generate visually grounded elements (e.g., *diagrams, interactive education tools, illustrative graphics*) to support the pedagogical illustration of problem-solving processes.

Currently, generating visually grounded elements for pedagogical reasoning poses several challenges: (1) decomposing complex reasoning into representable steps that align closely with human cognitive processes is non-trivial (Yang et al., 2024; Chen et al., 2024d); (2) precisely producing visual aids for each sub-step to optimally support learners is challenging (Hong et al., 2025); and (3) different educational domains require distinct visualization styles and formats, which makes consistent and

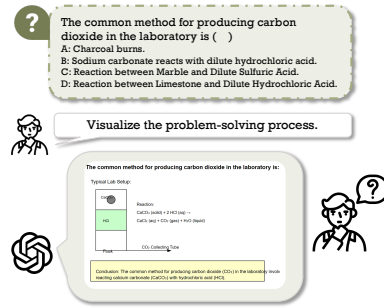


Figure 1: GPT-4o fails to illustrate its problem-solving with high-quality, logical, and explanatory visualization.

adequate visual aid delivery difficult (Pandey & Ottley, 2025). This difficulty stems not just from technical rendering challenges, but from the complex task of translating abstract pedagogical concepts into intuitive visual narratives. Addressing these obstacles first requires a picture of how current FMs perform, so that future models can be purpose-built to close the gaps. Consequently, a comprehensive evaluation platform is critical for systematically assessing FMs on visual pedagogical reasoning.

To bridge this gap, we introduce **EduVisBench**, a multi-domain, multi-level benchmark designed to evaluate the capacity of FMs to generate pedagogically effective, step-by-step visual reasoning. EduVisBench comprises structured problem sets across diverse domains, each requiring multimodal-centric reasoning and solutions that prioritize visualization principles such as *interpretability*, *cognitive alignment*, and *instructional clarity* to achieve high evaluation score. To facilitate a detailed evaluation, we further develop a fine-grained rubric enabling multidimensional assessments of AI-generated visual outputs, focusing explicitly on pedagogical criteria such as *contextual relevance*, *visual clarity*, *multimodal coherence*, *reasoning support*, and *interactive engagement*.

Utilizing this benchmark, we conduct extensive evaluations on a variety of FMs and agents. Our findings reveal that although current models achieve predominantly correct step-by-step textual analyses, they frequently fail to generate useful or faithful visualizations, as depicted in Figure 1. Specifically, our systematic analysis highlights recurring challenges including (1) semantic misalignments between textual explanations and visual components, (2) omissions of critical steps within rendered diagrams, and (3) structural inconsistencies in code-based visual outputs, collectively undermining accuracy, clarity, and interactivity. These shortcomings collectively compromise the pedagogical utility of the generated content, often leading to more confusion than clarity for the learner.

To address these limitations, we introduce a multi-agent collaborative framework, **EduVisAgent**, designed to simulate the complete learning journey from initial problem exposure to deep conceptual understanding. Specifically, a central planning agent orchestrates *five* specialized expert agents dedicated to *visualization design*, *cognitive scaffolding*, and *metacognitive regulation*. A synthesis module then integrates these expert outputs into interactive, personalized learning webpages tailored specifically to human learners. Experimental results demonstrate that our proposed method EduVisAgent achieves an average improvement of 40.2% than current SOTA method. This underscores the effectiveness of our approach leveraging modular specialization and collaborative integration to produce robust and visually grounded learning solutions.

## 2 EDUVISBENCH BENCHMARK

### 2.1 OVERVIEW

In this section, we introduce EduVisBench, a novel and challenging benchmark designed to evaluate the capability of models to generate logical and explanatory visualizations for educational purposes. As shown in Figure 2, EduVisBench comprises 1,154 carefully curated STEM questions across three academic subjects and 15 distinct domains, organized into three levels of difficulty. In addition to assessing accuracy in step-by-step problem solving, EduVisBench places particular emphasis on a model’s ability to communicate the reasoning process clearly and visually helping students understand problems through structured, interpretable visual outputs, as illustrated in Figure 3.

Specifically, EduVisBench adopts a multimodal setting in which models are provided with both textual and visual inputs and are tasked with producing diverse output formats, including interactive web pages and visual diagrams. Beyond evaluating the correctness of final answers, we introduce a fine-grained evaluation framework that assesses the quality of visualizations across five key dimensions: (1) the logical sequencing of visual elements, (2) the structural richness of the visuals, (3) semantic

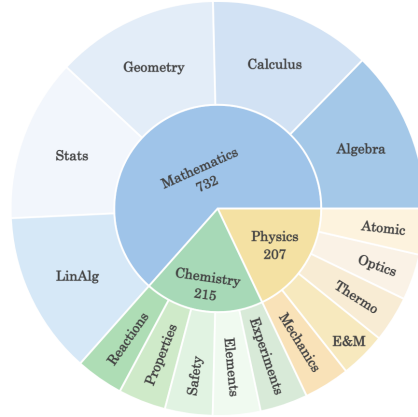


Figure 2: Dataset distribution of EduVisBench. Each domain encompasses various sub-domains, collectively covering 15 comprehensive pedagogical scenarios.

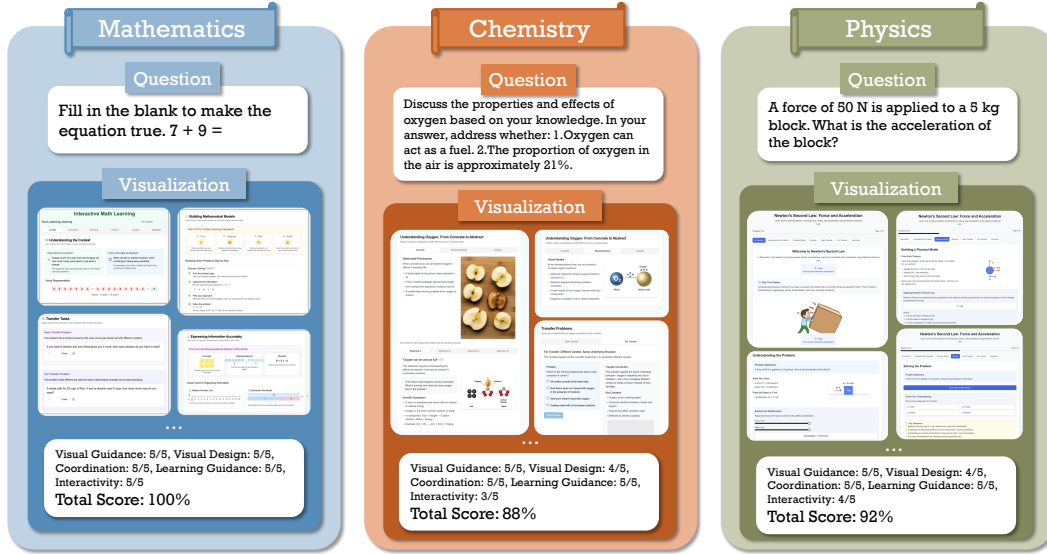


Figure 3: Representative examples from EduVisBench, featuring questions from Maths, Chemistry, and Physics alongside their corresponding high-scoring visual explanations. These interactive visualizations, generated by our multi-agent system EduVisAgent, exemplify well-designed, pedagogically effective outputs for STEM problems.

alignment with the underlying subject matter, (4) the clarity and guidance provided for problem-solving, and (5) the level of interactivity and engagement. In the following subsections, we describe our dataset curation process and the design of the evaluation rubric in detail.

## 2.2 DATASET CURATION

EduVisBench is built from several high-quality public educational resources that we carefully curated, translated, and adapted to support multimodal visualization learning tasks. Specifically, the chemistry questions are sourced from the *C-MHChem-Benchmark* (Zhang et al., 2024), originally presented in Chinese and meticulously translated into English with careful attention to scientific accuracy and terminology. The physics questions are drawn from the *high-school-physics* (Rohith, 2023) dataset, which includes a range of conceptual and quantitative exercises suitable for secondary-level learners. The mathematics component combines easy-level problems from the Illustrative Mathematics curriculum with medium- to hard-level questions selected from the *MATH-500* (Lightman et al., 2023) dataset. Furthermore, each domain encompasses diverse sub-domains, collectively covering 15 comprehensive scenarios, as illustrated in Figure 2. All data sources were standardized into a unified format and consolidated to enable consistent and comprehensive evaluation across subjects.

## 2.3 EVALUATION METRIC

In this subsection, we detail the performance evaluation rubrics in EduVisBench.

**Evaluation Dimensions.** To comprehensively evaluate the quality of generated visualizations in supporting student understanding and learning, we introduce a fine-grained scoring metric grounded in five pedagogically motivated dimensions: (1) **Context Visualization**: evaluates how clearly the visualization situates the problem within a relevant context; (2) **Diagram Design**: assesses the clarity, accuracy, and effectiveness of the diagrams used to represent information; (3) **Text-Graphic Integration**: measures the coherence between textual explanations and visual elements, ensuring mutual interaction; (4) **Thought Guidance**: examines the extent to which the visualization supports reasoning processes and highlights critical thinking steps; (5) **Interactivity**: evaluates whether and how the visualization invites students engagement, reflection, or active manipulation. Each dimension captures a distinct aspect of effective multimedia learning, with detailed rubrics provided in Appendix A.1 to guide the scoring process.

**Evaluation Protocol.** As shown in Figure 4, models are provided with a visualization prompt together with a question and are asked to generate visual outputs. To enable fair comparison across heterogeneous outputs, we first canonicalize every model result to a raster image prior to scoring. This standardization is a crucial step that ensures all systems are evaluated on a level playing field, independent of their native modality or file format, and prevents format-specific rendering artifacts from biasing the assessment. Visuals produced directly as SVG or PNG are used as-is. Web pages (HTML or Next.js) are rendered in a headless browser and captured as screenshots of the primary view; when lightweight interactivity is present (e.g., buttons, tabs, or toggles), we systematically traverse the reachable states and retain one representative screenshot per state. All resulting images are then evaluated by GPT-4o along five dimensions defined in Appendix A.2 to compute an overall performance score. Each dimension is rated on a 0-5 scale; the ratings are summed (0-25) and, when appropriate, normalized to a percentage to yield the final overall score.

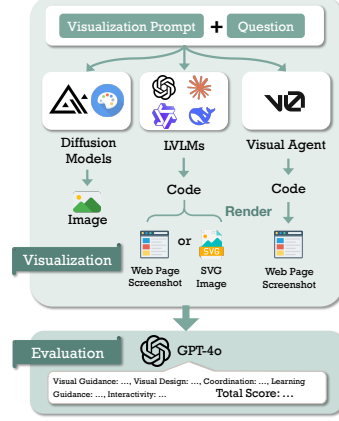


Figure 4: Workflow for evaluation.

### 3 EDUVISAGENT

Using EduVisBench we systematically evaluate the performance of existing text-to-image models and LVLMs (see detailed results in Table 1 in Section 4). We find that most models perform poorly, with average scores below 50 on a 0-100 scale. This significant performance gap serves as the primary motivation for developing a novel approach that moves beyond monolithic model architectures. This underperformance underscores the inherent challenge of decomposing complex reasoning and translating it into visual representations that align with human cognitive processes to effectively support educationa task that remains highly non-trivial.

To address these challenges, we propose a multi-agent system, EduVisAgent, inspired by pedagogical theories and designed to emulate the division of labor and collaborative reasoning found in expert instructional design. EduVisAgent consists of five specialized yet interdependent agents: a **Task Planning Agent**, which structures the instructional objective; a **Conceptual Mapping Agent**, which extracts and organizes key information; a **Reasoning Decomposition Agent**, which constructs step-by-step problem-solving logic; a **Metacognitive Reviewer**, which encourages summarization and learner reflection; and a **Visualization Agent**, which generates appropriate visual representations. This design introduces modularity and pedagogical interpretability by embedding distinct instructional roles directly into the agent workflow. The overall operation of EduVisAgent proceeds in two stages: (1) instructional flow construction and (2) collaborative solution generation, as detailed below.

#### 3.1 INSTRUCTIONAL FLOW CONSTRUCTION

The first stage of EduVisAgent focuses on formulating a well-structured instructional task based on the original problem. A key challenge lies in analyzing the underlying reasoning structure, identifying implicit logical dependencies, and associating each reasoning step with relevant conceptual knowledge. To address this, we employ the **Task Planning Agent**, which systematically organizes the problem into an instructional format suitable for multimodal visualization. Its main functions include: (1) breaking down the problem into coherent subgoals, (2) clarifying the reasoning expected at each step, (3) aligning each step with domain-specific principles or formulas, and (4) anticipating potential student misconceptions or cognitive needs. This structured formulation provides a pedagogically grounded foundation that guides the downstream agents in generating coherent, targeted, and educationally effective visual explanations.

#### 3.2 COLLABORATIVE SOLUTION GENERATION

In this stage, EduVisAgent executes the instructional task constructed by sequentially activating a set of specialized agents, each responsible for completing a specific aspect of the task. As shown in Figure 5, these agents operate in a coordinated manner to enhance the coherence of instructional



logic, improving the clarity of visual representation, and ensure alignment with educational objectives. Specifically, we detail each agent as follows.

**Conceptual Mapping Agent.** This agent is responsible for extracting and organizing the core components of the input problem. Drawing on the ConcreteRepresentationalAbstract (CRA) instructional model (Nugroho & Jailani, 2019), it classifies information into three categories: concrete entities, representational elements, and abstract constructs. This structured classification helps bridge the gap between the concrete elements of a problem and the abstract principles required to solve it. This progression from concrete to abstract is particularly valuable for an AI system, as it provides a structured pathway to ground complex concepts in relatable terms before generating symbolic representations. The agent conducts fine-grained categorization and semantic summarization to support downstream visualization modules.

**Reasoning Decomposition Agent.** This agent decomposes complex problems into manageable subcomponents and provides step-specific instructional guidance. It applies the memory-oriented FOPS strategy (Miller & Cohen, 2020) to find the problem type (e.g., equation solving, conceptual reasoning, commonsense application, or graphical interpretation), organize the structure via equations or diagrams, plan the solution path, and solve the task. Based on the decomposed steps, the agent also identifies critical instructional points that require additional support, especially those that benefit from visual scaffolding or interactive guidance.

**Metacognitive Reviewer.** Grounded in metacognitive theory (Schraw & Moshman, 1995), this agent supports learners in monitoring their comprehension and reasoning processes. It generates reflective prompts that foster self-questioning and self-correction, encouraging learners to evaluate the soundness of their problem-solving approaches.

**Visualization Agent.** This agent is responsible for constructing the visual guidance component of the instructional output. Instead of relying on decorative visuals, it emphasizes the use of abstract yet pedagogically effective representations such as number lines, bar charts, schematic object illustrations, graphic organizers, sketch diagrams, and structured data tables. The agent ensures that each visualization is tightly aligned with the underlying abstract concept being taught. All visuals are rendered using the v0 (Vercel, 2025) system for web-based deployment.

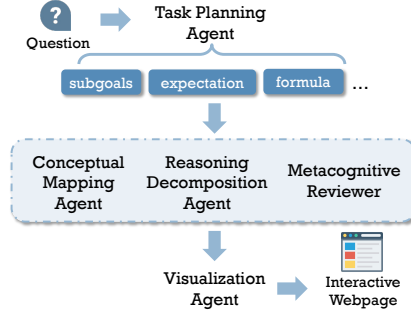


Figure 5: The structure of EduVisAgent.

## 4 EXPERIMENTS

This section outlines the experimental setup for benchmarking various foundation models on EduVisBench. We evaluate Diffusion Models, LVLMS, a specialized visualization agent (v0), and our proposed EduVisAgent. Our investigation seeks to address the following key questions: (1) How proficient are existing models at generating high-quality, explanatory visualizations within EduVisBench? (2) Can the proposed EduVisAgent system outperform current models? (3) What distinct performance patterns emerge across different model architectures, academic disciplines, and evaluation dimensions in EduVisBench?

### 4.1 EXPERIMENT SETUP

**Baseline Models.** Our experimental evaluation encompasses a range of FMs, categorized as follows: (1) Image Generation Models: This category includes Flux.1-dev (Labs, 2024), Stable Diffusion 3.5 Large (SD3.5) (IT Admin, 2024), and Stable Diffusion XL Base 1.0 (SDXL) (Podell et al., 2023). These models are tasked with generating static images directly from textual or visual inputs. (2) Large Vision-Language Models (LVLMS): We evaluate Deepseek-VL2 (Wu et al., 2024), GLM-4V-9B (GLM et al., 2024), MiniCPM-V2.6 (Yao et al., 2024), Mistral-Small-3.1-24B-Instruct-2503 (Mistral AI, 2025), Phi-3.5-Vision-Instruct (Abdin et al., 2024), Phi-4-Multimodal-Instruct (Abouelenin et al., 2025), Qwen2.5-VL-72B (Team, 2025), GPT-4o (Hurst et al., 2024), Claude 3.7 Sonnet (Anthropic, 2025), and Gemini 2.0 Flash (Mallick & Kilpatrick, 2025). These models are prompted

Table 1: Performance of Diffusion Models, Large Vision Language Models and v0 on EduVisBench.

Method	Vis. Type	Maths			Physics			Chemistry			Avg
		Easy	Medium	Hard	Easy	Medium	Hard	Easy	Medium	Hard	
Diffusion Model											
Flux.1-dev	Image	13.8	13.4	13.2	11.7	8.5	10.0	20.0	16.6	16.0	13.8
SD3.5	Image	17.3	20.3	18.8	16.8	13.0	12.0	22.8	21.7	34.0	18.4
SDXL	Image	17.3	23.3	25.5	18.9	15.4	24.0	33.6	30.2	24.0	21.8
Large Vision Language Model											
Deepseek VL2	Webpage	20.3	17.1	15.7	17.9	17.0	20.0	16.4	13.8	14.0	17.5
GLM-4V-9B	Webpage	22.3	21.1	19.4	24.5	21.5	24.0	22.3	21.5	16.0	21.9
MiniCPM-V-2.6	Webpage	24.1	17.3	15.5	19.1	17.4	20.0	14.5	15.2	12.0	19.3
Mistral-Small-3.1	Webpage	29.1	31.6	32.2	32.3	33.5	20.0	30.6	27.5	24.0	30.2
Phi-3.5	Webpage	25.3	20.7	19.1	21.2	19.5	12.0	20.0	18.6	20.0	21.8
Phi-4	Webpage	26.1	25.1	22.9	27.8	25.5	24.0	31.2	27.5	12.0	26.4
Qwen2.5-VL-72B	Webpage	24.3	18.1	15.8	19.7	17.1	24.0	18.2	16.4	12.0	20.0
Claude 3.7 Sonnet	SVG	61.2	26.7	23.6	18.5	16.9	14.0	47.5	47.2	18.0	42.0
Claude 3.7 Sonnet	Webpage	56.2	57.5	55.6	44.8	42.6	24.0	61.1	60.6	64.0	54.6
GPT-4o	Webpage	47.6	39.3	37.9	25.7	24.2	24.0	34.3	32.6	36.0	38.1
GPT-4o	SVG	36.1	19.7	19.5	13.0	12.8	4.0	30.0	27.5	22.0	26.3
Gemini 2.0 Flash	Webpage	46.9	9.5	15.7	31.7	26.5	24.0	32.0	25.8	30.0	43.6
Visualization Agent											
v0	Webpage	63.0	37.6	47.2	53.3	58.5	52.0	74.7	52.8	68.0	58.2

to generate SVG or HTML code, which is then rendered into visual outputs for evaluation. (3) Specialized Visualization Agent: We also assess v0 (Vercel, 2025), an AI agent specifically designed to create interactive web pages based on instructional content. This diverse selection of models was chosen to represent the current state-of-the-art across different architectural paradigms.

**Evaluation Setups.** During evaluation, all generated visualizations are standardized into image format. For interactive web pages containing buttons, an automated script navigates through all accessible sub-pages, capturing individual screenshots of each. This automated approach ensures that the evaluation is both scalable and free from subjective human bias during the rendering process. Performance is assessed using the evaluation metric described in Section 2.3, where GPT-4o scores the visual outputs based on predefined rubrics, assigning a score from 0 to 5 for each of the five dimensions. The cumulative score (maximum 25 points) is then normalized to a 0-100 scale for standardized reporting and comparison.

#### Reliability of GPT-based Scoring.

To validate the reliability of our automatic judge, we compared GPT-based evaluations with human evaluations. Specifically, we selected 50 samples from each subject category (Chemistry, Math, and Physics), and had both GPT and human evaluators independently rate them. Human evaluators were undergraduate students from top universities. We measured agreement using Cosine Similarity and Mean Squared Error (MSE). As shown in Table 2, high agreement average cosine similarity 0.9655 and MSE 0.5702 across subjects indicates negligible practical discrepancy.

Table 2: Cosine similarity and mean squared error across subjects. Math is the average of Math500 and IllustrativeMath, each with 50 samples.

Metric	Chemistry	Math	Physics	Average
Cosine Similarity	0.9742	0.9557	0.9666	<b>0.9655</b>
MSE	0.3895	0.7093	0.6118	<b>0.5702</b>

## 4.2 BASELINE BENCHMARKING

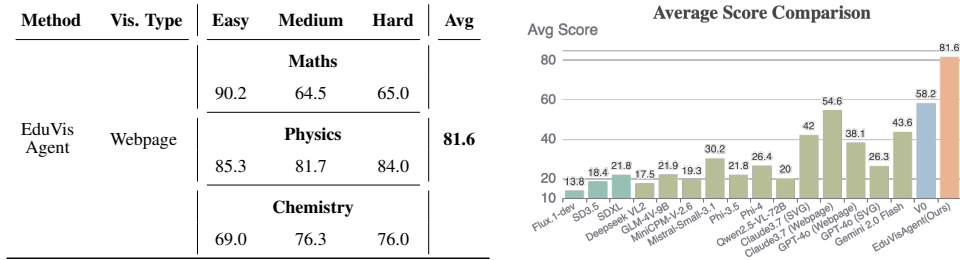
The performance of all evaluated baseline models is detailed in Table 1. Across all evaluated models, the average scores indicate significant room for improvement. Diffusion Models generally exhibited the lowest performance, with average scores ranging from 13.8% (Flux.1-dev) to 21.8% (SDXL). This suggests that direct static image generation, while capable of producing visual elements, struggles

substantially with the nuanced requirements of explanatory and guiding visualizations for complex logical problems in our benchmark.

LVLMS typically scored between 17.5% (Deepseek VL2) and 30.2% (Mistral-Small-3.1). Notable exceptions include Gemini 2.0 Flash (43.6%) and Claude 3.7 Sonnet; the latter’s significantly better performance with Webpages (54.6%) over SVG (42.0%). GPT-4o also showed a preference for Webpage generation (38.1%) over SVG (26.3%), suggesting that prompting advanced LVLMS for structured interactive webpages can yield more effective visual explanations. Nevertheless, even these top-tier LVLMS face considerable challenges in consistently meeting all of evaluation criteria. The visualization agent v0, specifically designed for webpage generation, achieved the highest average score among all baseline models at 58.2%. This result highlights the advantage of a specialized agent in this task over more general-purpose FMs.

Table 3: Overall comparison of models: left is our EduVisAgent performance, right is the bar chart. EduVisAgent achieves the highest average score among all models.

(a) Performance of our EduVisAgent on EduVisBench. (b) Comparison of average score across all models.



#### 4.3 PERFORMANCE ANALYSIS OF EDUVISBENCH

Building upon the insights gained from the baseline evaluations, we assessed our proposed multi-agent system, EduVisAgent. The results in Table 3 demonstrate a substantial leap in performance for generating explanatory and logically valuable visualizations for STEM problems. EduVisAgent achieved an impressive overall average score of 81.6%. Specifically, EduVisAgent surpasses the best-performing baseline v0 (58.2%), by a remarkable 23.4 percentage points. This constitutes an approximately 40.2% relative improvement, underscoring the efficacy of our multi-agent architecture and the integration of educational methodologies. Compared to the best performing LVM (Claude 3.7 Sonnet Webpage at 54.6%) and the top diffusion model (SDXL at 21.8%), the advancement offered by EduVisAgent is even more pronounced. These results clearly indicate that the design principles underlying EduVisAgent, which incorporate a multi-agent structure and pedagogical strategies, effectively address many of the limitations observed in existing generative models.

#### 4.4 CASE ANALYSIS

To further illustrate the limitations of existing baselines and how our approach addresses these challenges, we present two case studies in Figure 6. On the left, for a chemistry question, the GPT-4o-generated solution lacks intuitive visualization of the chemical processes, resulting in fragmented information without visual guidance reflected in a low score of just 28%. In contrast, EduVisAgent begins by displaying background images of the relevant chemical elements, activating students prior knowledge. This strategy effectively connects abstract chemical concepts to tangible, everyday experiences, a well-established method for enhancing comprehension and retention. It then contextualizes each of the four answer options with real-world scenarios, thereby enhancing students’ understanding of the underlying chemical transformations.

Conversely, for the Carnot cycle efficiency physics problem (right side of Figure 6), the Gemini solution presents a single, flawed chart. Its depiction of 300K and 400K temperatures with identical heights introduces visual misinformation, failing to accurately represent data differences and thereby diminishing its pedagogical value. In stark contrast, EduVisAgent employs a multi-agent collaborative approach: it first generates a concrete factory scene to activate students’ working memory of the “heat engine” concept. Subsequently, it constructs an accurate Carnot cycle diagram and offers a step-by-step problem breakdown, fostering clear conceptual understanding. Crucially, EduVisAgent

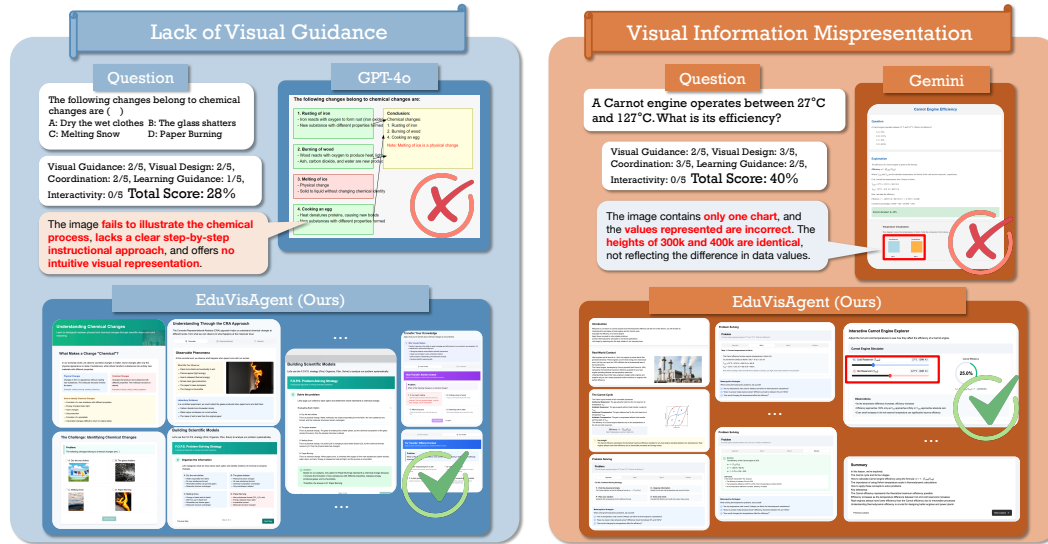


Figure 6: Baseline models versus our EduVisAgent. These examples clearly demonstrate the often poor output quality of baseline models, contrasting sharply with the high-quality, effective visualizations produced by EduVisAgent.

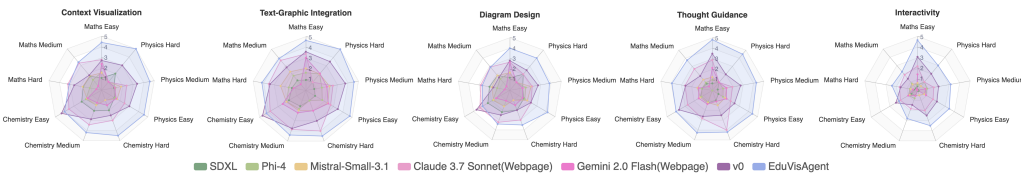


Figure 7: Fine-grained performance comparison across our five key evaluation dimensions.

provides interactive visualization components, enabling users to dynamically adjust temperatures via sliders and observe real-time changes in heat engine efficiency. This interactive element transforms the learner from a passive observer into an active participant, which is known to deepen engagement and learning. This interactive engagement significantly facilitates higher-order thinking skills.

Overall, through coordinated multi-agent optimization of image design, instructional structure, and learning pathways, EduVisAgent significantly outperforms traditional single-model approaches in accuracy, guidance, and interactivity.

#### 4.5 FINE-GRAINED ANALYSIS ON FIVE EVALUATION DIMENSIONS

Figure 7 reveals distinct performance profiles for eight high-performing evaluated models. In Context Visualization and Diagram Design, most baselines, including SDXL, Claude 3.7, and v0, exhibit moderate to low scores, often struggling with providing rich situational cues or pedagogically sound visual structures, especially for complex problems. v0 and Claude show relatively better capabilities in Text-Graphic Integration and Thought Guidance compared to other FMs, which generally offer minimal support in these areas. However, all baseline models, including v0, are significantly limited in the Interactivity dimension, primarily due to their output format (static images/SVG or less dynamic webpages). In contrast, our EduVisAgent demonstrates consistently strong performance across all five dimensions. It particularly excels in creating rich context visualizations, well-structured diagram designs, and ensuring seamless text-graphic integration. Furthermore, EduVisAgent provides superior thought guidance and achieves notably high scores in Interactivity, areas where baseline models significantly lag. This comprehensive strength highlights EduVisAgent’s advanced ability to generate not just visualizations, but truly effective and interactive pedagogical tools.

## 5 RELATED WORK

**LLM for Pedagogical Assistance.** Foundation models (FMs), including diffusion models and large vision-language models (LVLMs), have been increasingly adopted in educational contexts (Chu et al., 2025; Wang et al., 2024) to support teaching and classroom interactions. EduAgent (Xu et al., 2024) and TeachTune (Jin et al., 2025) enhance the problem-solving process through automated simulations of student-teacher dialogues, collaborative learning, and task-oriented reasoning. Agents such as SEFL (Zhang et al., 2025) and PROF (Nair et al., 2024) synthesize immediate, on-demand feedback to support large-scale instructional scenarios. Furthermore, domain-specific agents such as MathChat (Wu et al., 2023), NEWTON (Wang et al., 2023b), and MEDCO (Wei et al., 2024) further provide textual explanations tailored to scientific and medical education. While these systems address diverse pedagogical needs, their focus remains largely on text-based interactions (Wu et al., 2023; Xu et al., 2024; Cui et al., 2024), overlooking the critical role of visualization in fostering conceptual understanding and improving learning outcomes (Presmeg, 2006). While valuable, these text-centric systems do not address the large body of educational research highlighting the unique cognitive benefits of visual learning. Despite its pedagogical importance, the capacity of FMs and agents to generate logical, explanatory visual illustrations remains underexplored. EduVisBench is the first comprehensive benchmark designed to systematically evaluate FMs ability to produce pedagogically effective, step-by-step visual reasoning, covering 15 diverse visually grounded educational scenarios with multi-level problem sets and multimodal-centric solutions.

**LLM for Scientific Visualization.** While some existing works have preliminarily explored the potential of FMs in supporting visual scaffolding (Podo et al., 2024; Chen et al., 2024c; Pandey & Ottley, 2025; Hong et al., 2025), they are typically fragmented, lack pedagogical grounding, and fail to generalize across diverse educational tasks (Wang et al., 2023a; Ku et al., 2025). For instance, Visual Sketchpad (Hu et al., 2024) attempts to illustrate problem-solving processes with sketches generated from code. However, these visuals are often low in quality, lack logical coherence, and fall short in explanatory depth (Wang et al., 2025). Other approaches like MatplotAgent (Yang et al., 2024), PlotGen (Goswami et al., 2025), and OmniSVG (Yang et al., 2025) leverage plotting and SVG tools to produce more accurate, data-grounded visualizations. Still, these methods are limited in scope, often addressing only isolated steps rather than providing systematic, end-to-end visual explanations of multi-step problem-solving tasks (Vázquez, 2024; Chen et al., 2024a; 2025b). Our framework, in contrast, is designed to manage the entire pedagogical workflow, from problem deconstruction to the final interactive explanation. To overcome these limitations, we propose a multi-agent collaborative framework, EduVisAgent, that simulates the full learning journey from initial problem exposure to deep conceptual understanding by coordinating specialized agents to generate coherent, pedagogically aligned visualizations throughout the reasoning process.

**LLM-based Education Agents.** Recent advancements in LLM-based agents have led to the development of specialized architectures capable of long-horizon planning, tool use, and memory management across a range of real-world domains (Yao et al., 2023; Chan et al., 2024; Chen et al., 2024b; 2025a; Nie et al., 2025; Han et al., 2025; Zhou et al., 2025). In the educational domain, AI agents such as EduAgent (Xu et al., 2024) and TeachTune (Jin et al., 2025) simulate student-teacher dialogues, collaborative learning activities, and task-oriented reasoning to enhance problem-solving instruction. Agents like SEFL (Zhang et al., 2025) and PROF (Nair et al., 2024) generate on-demand feedback for large-scale educational settings, while domain-specific tools such as MathChat (Wu et al., 2023), NEWTON (Wang et al., 2023b), and MEDCO (Wei et al., 2024) provide textual explanations for scientific and medical learning. Despite these advances, limited research has investigated collaborative, multi-agent approaches tailored to educational reasoning and visualization. EduVisAgent is the first systematic multi-agent framework that coordinates specialized agents and provides a comprehensive approach to supporting step-by-step pedagogical problem-solving.

## 6 CONCLUSION

This paper addressed the challenge of generating pedagogically meaningful visual explanations with AI systems. We introduced EduVisBench, a benchmark revealing that existing models often produce inadequate visual outputs. This work provides a quantitative baseline for the field, clearly identifying the key areas where current technologies fall short. To overcome this, we proposed EduVisAgent, a collaborative multi-agent framework. Experiments show EduVisAgent significantly outperforms all baselines, demonstrating the potential of agent-based systems for advancing educational visualization.



## ETHICS STATEMENT

The primary goal of this research is to advance educational technology by improving the pedagogical quality of AI-generated visualizations, aiming for a positive societal impact. The benchmark developed, EduVisBench, is curated from publicly available and high-quality educational resources, including C-MHChem-Benchmark, high-school-physics, Illustrative Mathematics, and MATH-500. To validate our automated evaluation metric, we conducted a comparative study involving human evaluators, who were undergraduate students from top universities. All data used in the study was handled with care to ensure anonymity and was used solely for the purpose of validating the scoring system. The models and methods proposed are intended for beneficial educational applications. The authors are not aware of any other ethical issues and declare no competing interests or conflicts of interest associated with this research.

## REPRODUCIBILITY STATEMENT

To ensure the reproducibility of our work, we have provided detailed descriptions of our methodology and resources. The curation process for our benchmark, EduVisBench, is detailed in Section 2.2, with data sources explicitly cited. Our comprehensive evaluation framework, including the five key dimensions and scoring protocol, is described in Section 2.3 and Section 4.1. The detailed scoring rubrics and the exact prompt used for our GPT-4o-based evaluation are available in Appendix A.2 and Appendix A.3, respectively. The architecture of our proposed EduVisAgent and the roles of each specialized agent are thoroughly explained in Section 3. A complete list of all baseline models and their versions used in our experiments is provided in Section 4.1.

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## A APPENDIX

### A.1 VISUALIZATION DISCIPLINES

Table 4 illustrates the disciplines and types in our EduVisBench.

Discipline	Common Visualization Types
<i>Mathematics</i>	Number lines, function graphs, and other formalized visual tools.
<i>Physics</i>	Diagrams involving levers, rigid body motion, forces, and fields.
<i>Chemistry</i>	Molecular structures and schematic representations of standard laboratory apparatus.

Table 4: Representative Visualization Types Across Academic Disciplines

### A.2 EVALUATION METRIC

**Visual Scenario Design Guidance** The category of "Visual Scenario Design Guidance" outlines different levels of visualizing mathematical concepts, progressing from basic text-only representations to highly integrated visual-text formats. Through five defined levels, the framework demonstrates how visual elements can enhance students' understanding and engagement with abstract ideas, guiding instructional designers to gradually enrich scenarios, add annotations, and strengthen contextual connections ultimately achieving the goal of visually presenting the full flow and conceptual structure of the content. The five levels of Visual Scenario Design Guidance are as follows:

Level	Description
Level 1	The image contains no scenes or illustrations, presenting only text and formulas. It lacks contextual visual cues, failing to spark interest or connect the concepts to real-life situations.
Level 2	The image includes a single static illustration or low-fidelity mockup with minimal labeling that does not highlight variables or key objects, offering limited context and poor immersion.
Level 3	Multiple static schematic diagrams or sketch-style illustrations appear in the image, labeling core objects, variables, and simple steps, providing basic visual guidance but lacking layered coherence.
Level 4	The image integrates scenario illustrations, storyboard panels, and infographics to present the process in multiple views and steps, with annotations and captions guiding students through mapping abstract concepts to context.
Level 5	Storyboard-style illustrations and infographics are fused into a single image, including overview, detailed close-ups, and key pathway diagrams with comprehensive annotations, allowing students to grasp the entire flow and conceptual network at a glance.

Table 5: Five Levels of Visual Scenario Design Guidance

**Visual Illustration Design** The category of "Visual Illustration Design" describes progressive levels of visual elements used to support students systematic understanding of quantities and relationships. It ranges from no visual aids to complex integrated dashboards that deeply connect data and model



structures. Through five levels, the framework guides designers to improve clarity, coherence, and contextual richness of visual illustrations, enhancing students analytic and comparative abilities.

Level	Description
Level 1	The image contains no charts, axes, or flow diagrams only text. Without embedded visual tools, students cannot systematically organize or analyze quantities and relationships.
Level 2	The image presents a static number line and colored bar chart with complete scales and a legend, helping students gain a basic understanding of numerical changes. However, it lacks comparison and contextual layering.
Level 3	The image presents a static number line and colored bar chart with complete scales and legends, helping students grasp basic numerical changes visually, though comparison and context layering are absent.
Level 4	The image combines number lines, flowcharts, infographics, and arrow annotations; multiple visuals are juxtaposed or overlaid to show processes and variable changes for a coherent modeling view.
Level 5	The image presents a dashboard-style visualization integrating axes, bar charts, flow diagrams, heatmaps, etc., with linked elements that deeply visualize data relationships and model structure.

Table 6: Five Levels of Visual Illustration Design

**TextIllustration Coordination** The category of "TextIllustration Coordination" describes levels of alignment and integration between textual content and visual elements within images. This progression ranges from complete disconnection to seamless fusion, enabling students to effectively map and synthesize text, formulas, and graphics. The framework guides designers in strengthening links between verbal and visual information to enhance comprehension and structural understanding.

Level	Description
Level 1	Text and illustrations in the image are completely disconnected, with no labels, legends, or connectors students cannot use visuals to understand text or formulas.
Level 2	Text occasionally prompts see diagram or refer to the illustration, but the image lacks legends or clear labels, so mapping between text and graphics remains ambiguous.
Level 3	Text descriptions and image elements share consistent numbering, color blocks, or arrows linked to a simple legend, explaining core symbols and variables to support initial mapping.
Level 4	Text paragraphs are laid out alongside corresponding visuals within the same image, with detailed legends and color-coded annotations enabling simultaneous reading and mapping.
Level 5	Text, formulas, and legends are fully integrated in one image, using consistent colors, numbering, and layered layout to achieve seamless textgraphic fusion for complete structural understanding.

Table 7: Five Levels of TextIllustration Coordination

**Learning Thought Guidance** The category of "Learning Thought Guidance" describes the progressive inclusion of visualized problem-solving strategies and reflective cues in images. From presenting

only problem statements to complex integrated dashboards, this framework guides designers to scaffold students strategic thinking and metacognitive reflection through visual tools, enabling deeper reasoning and transfer of learning.

Level	Description
Level 1	The image offers no visualized problem-solving guidance, showing only the problem statement and formulas, leaving students without strategic cues or reflection prompts.
Level 2	The image embeds a simple flowchart or two title-style hints (e.g., Identify problem type, Check result), but the flowchart is overly simplistic and hints lack hierarchical detail.
Level 3	The image displays a step-by-step flowchart template with key thinking nodes and self-check checkpoints, leaving annotation space for students to visually record their reasoning.
Level 4	The image combines a near-transfer exercise with a comparative thought diagram, visually highlighting strategy differences so students can apply existing reasoning to a new context.
Level 5	The image fuses near- and far-transfer exercises, concept mind maps, and a reflection panel into a dashboard-style layout, allowing students to review and extend their problem-solving network visually.

Table 8: Five Levels of Learning Thought Guidance

**Interactivity and Personalized Support** The category of "Interactivity and Personalized Support" outlines levels of incorporating feedback, hints, and tailored assistance into images, evolving from static presentations to dynamic, student-responsive visual supports. This framework encourages designers to embed interactive elements that adapt to learner needs, promoting engagement and personalized problem-solving.

Level	Description
Level 1	The image includes no feedback or support components only a static problem statement and answer field offering no hints, examples, or error cues and resulting in a nonresponsive visual.
Level 2	The image shows fixed hint boxes (e.g., Hint: draw a number line, Hint: check rounding), but hints are not tailored to student responses, limiting personalized guidance.
Level 3	The image integrates multiple static correction tips and example solution modules (common mistakes and standard approaches), which students can reference visually but without intelligent recommendations.
Level 4	The image presents example solution workflows, text hints, and a common-errors analysis section highlighted with color blocks and arrows, providing diverse visual support in a single layout.
Level 5	The image displays a comprehensive visual support panel with difficulty suggestions, personalized hints, worked examples, and extension resource links, enabling students to select tailored guidance directly from the visual layout.

Table 9: Five Levels of Interactivity and Personalized Support

### A.3 EVALUATION PROMPT

The instructional web page evaluation prompt is structured as follows:

#### Evaluation Prompt

As a **professional evaluator of instructional web pages**, your task is to determine whether the generated web page meets expectations across five specific categories.

#### Instructions:

- Assign an **integer score from 0 to 5** for each of the five categories (15).
- **0 = completely missing or extremely poor**  
**5 = fully meets the highest standard**
- Evaluation should be based solely on the specified aspect: *{category}*.  
The definition of *{category}* is: *{description}*.
- **Do not include any explanation, justification, or additional commentary. Refusing to provide a score is not allowed.**

#### Evaluation Output Format

```
{{RATING: {"1":score, "2":score, "3":score, "4":score, "5":score}}}
```

### A.4 GENERATION PROMPTS FOR BASELINE MODELS

The following prompts are used to instruct baseline models to generate instructional visualizations for multiple-choice questions.

#### HTML Webpage Generation Prompt

Please generate a fully structured and styled HTML webpage for the following {subject} multiple-choice question, with a focus on clearly presenting the problem, visualizing key scientific concepts, and explaining the reasoning behind the correct choice.

The page should include:

- A prominently displayed question section.
- A clearly formatted list of answer choices (A, B, C, D).
- A step-by-step explanation section that helps users understand why the correct answer is right, and why the others are not. This section may include:
  - Diagrams or illustrations (e.g., molecules, environmental impact visuals),
  - Charts or data comparisons (e.g., particulate levels),
  - Flowcharts or labeled process diagrams,
  - Any other visual representation that supports comprehension.
- A clear highlight of the final correct answer (e.g., a visual cue or box).

Requirements:

- Use modern CSS styling (inline `<style>` block or external).
- Ensure layout is responsive and readable across devices.
- Use semantic HTML structure with headings and subheadings (`<h1>`, `<h2>`, etc.).
- Render scientific symbols or formulas correctly (e.g., MathJax or KaTeX).

- Visualization libraries such as Chart.js, D3.js, or SVG may be used to enhance explanations.

Question: {question}

Please output the full HTML + CSS + JavaScript code only, without any extra explanation or comments.

#### SVG Diagram Generation Prompt

Generate a **stand-alone SVG diagram** that visually explains the following question as a reasoning task.

The SVG must include:

- The full question text;
- Key reasoning steps, visual annotations, or illustrations that aid in understanding or solving the problem;
- If applicable, highlight the final answer or conclusion clearly.

Requirements:

- Output only a single `<svg> . . . </svg>` block, with no extra text outside it;
- SVG width between 800–1200px, layout should be clean and adaptive;
- Use `<text>` elements with readable font sizes for all text;
- Use arrows, symbols, and diagrams if they help communicate the solution process;
- You may omit multiple-choice options if not relevant.

Question: {question}

#### Visualization Agent Generation Prompt

Your task is to generate a complete webpage solution for the following problem. The page should include:

- Introduce a scenario to engage students.
- Explain the problem background and provide a step-by-step walkthrough of the solution.
- Give another similar problem to assess students' understanding.

Question: {question}

## A.5 MULTI-AGENT SYSTEM PROMPTS

### A.5.1 TASK PLANNING AGENT PROMPT

#### System Prompt

Transform learner's question into structured instructional task.

1. **Scenario & Understanding:** Real-world context + givens/goals/constraints
2. **Solution Strategy:** Analysis + step-by-step solution + reasoning
3. **Transfer Tasks:**

- Near-transfer: same structure, minor changes
- Far-transfer: different surface, same logic

#### 4. FOPS Structure (per step):

- **F**: Problem type
- **O**: Diagram/equation structure
- **P**: Solution path
- **S**: Execute + verify
- Specify: goal, action, concepts, pitfalls

#### 5. UI Layout: Shadcn/UI structure + sections + meta-prompt placement + math rendering

#### JSON Output Format

```
{
  "scenario": {
    "context": "Real-world scenario description",
    "givens": ["given1", "given2"],
    "goals": ["goal1"],
    "constraints": ["constraint1"]
  },
  "solution_strategy": {
    "analysis": "Problem analysis",
    "steps": [
      {
        "step_number": 1,
        "fops_label": "F/O/P/S",
        "description": "What to do",
        "reasoning": "Why this step"
      }
    ]
  },
  "transfer_tasks": {
    "near_transfer": {
      "problem": "Near-transfer problem statement",
      "explanation": "Why it's near-transfer"
    },
    "far_transfer": {
      "problem": "Far-transfer problem statement",
      "explanation": "Why it's far-transfer"
    }
  },
  "instructional_steps": [
    {
      "step_number": 1,
      "goal": "What learner should achieve",
      "action": "Expected reasoning/action",
      "concepts": ["concept1", "concept2"],
      "pitfalls": ["potential misconception1"]
    }
  ],
  "ui_layout_suggestion": {
    "structure": "Overall page flow",
    "key_components": ["Card", "Accordion", "Alert", "Table"],
    "content_organization": "Organize scenario/solution/practice",
    "math_rendering": "KaTeX/MathJax"
  }
}
```



## User Prompt

Give your analysis to the following question in JSON format.  
{Question}

## A.5.2 CONCEPTUAL MAPPING AGENT PROMPT

## System Prompt

Map concepts using **CRA framework** (ConcreteRepresentationalAbstract).

1. **Concrete:** Objects, quantities, situations (directly experienced)
2. **Representational + Visual Design:**
  - Tools: number lines, bar graphs, diagrams, organizers, sketches, tables
  - Visual design: form, purpose, concrete→abstract bridge
  - Avoid decorative; focus pedagogical
3. **Abstract:** Formulas, principles, theorems + connection to concrete
4. **Think Aloud:** Verbalization prompts

## JSON Output Format

```
{
  "cra_mapping": [
    {
      "step_number": 1,
      "step_name": "Step name",
      "concrete": {
        "entities": ["object1", "quantity1"],
        "description": "What can be directly experienced"
      },
      "representational": [
        {
          "tool": "Number line/Bar graph/etc",
          "purpose": "Why it helps",
          "represents": "What it shows",
          "visual_design": {
            "form": "Specific visual form to use",
            "elements": ["key visual elements"],
            "bridge": "How it bridges concrete to abstract"
          }
        }
      ],
      "abstract": {
        "constructs": ["formula1", "principle1"],
        "connection": "How abstract connects to concrete"
      },
      "think_aloud": ["prompt1", "prompt2"]
    }
  ]
}
```

## User Prompt

According to the following planning, give your analysis in JSON format.  
{Task Planning JSON}

## A.5.3 REASONING DECOMPOSITION AGENT PROMPT

## System Prompt

Decompose reasoning using design **scaffolded practice**.

1. **Step Guidance:**

- Action (what learner does)
- Link to CRA concepts
- **Visual support:** Which CRA visual + interaction (draggable, reveals, etc.)

2. **Practice Activities:**

- Types: fill-in, choice, judgment, explanation
- Gradual release strategy

3. **Math:** LaTeX in  $\$...\$$  or  $\$\$...\$\$$ **JSON Output Format**

```
{
  "fops_reasoning": [
    {
      "action": "What learner does",
      "concepts": ["linked concept1", "linked concept2"],
      "scaffolding_needed": true,
      "scaffolding_notes": "Why and how to scaffold",
      "visual_support": {
        "needed": true,
        "which_visual": "Reference to CRA mapping visual",
        "interaction": "Suggested interactive element if any"
      }
    }
  ],
  "practice_activities": [
    {
      "activity_number": 1,
      "name": "Activity name",
      "type": "fill-in/choice/judgment/explanation",
      "task": "Problem or task content",
      "gradual_release": "How independence builds"
    }
  ]
}
```

## User Prompt

According to the following planning and conceptual mapping, give your analysis in JSON format.

{Task Planning JSON}

{Conceptual Mapping JSON}

## A.5.4 METACOGNITIVE REVIEWER PROMPT

## System Prompt

Generate metacognitive prompts for **monitor, evaluate, regulate**.

1. **Reflective Prompts:** Check understanding, comprehension, strategy
2. **Self-Questioning:**
  - "What did I do?"
  - "Why does this work?"
  - "What did I miss?"
  - "How does this connect?"
  - "What if...?"
3. **Self-Correction:** Checkpoints + error identification
4. **Organize by Phase:**
  - **Before:** Understanding + planning
  - **During:** Monitoring + checking
  - **After:** Evaluating + reflecting
5. **Math:** LaTeX in  $\dots$  or  $\$ \$ \dots \$ \$$

## JSON Output Format

```
{
  "metacognitive_prompts": {
    "before_solving": [
      "Understanding check prompt 1",
      "Planning prompt 1"
    ],
    "during_solving": [
      "Step monitoring prompt 1",
      "Strategy adjustment prompt 1"
    ],
    "after_solving": [
      "Verification prompt 1",
      "Reflection prompt 1",
      "Improvement prompt 1"
    ]
  },
  "general_strategies": [
    {
      "strategy": "Self-monitoring technique",
      "when_to_use": "During which phase",
      "how_to_apply": "Specific actions"
    }
  ]
}
```

## User Prompt

According to the following planning, conceptual mapping and reasoning decomposition, give your analysis in JSON format.

```
{Task Planning JSON}
{Conceptual Mapping JSON}
{Reasoning Decomposition JSON}
```

### A.5.5 VISUALIZATION AGENT PROMPT

#### System Prompt

As the **Visual Representation Specialist**, generate the visualization teaching webpage of the given question.

1. **Abstract Visualization Tools:** Encourage number lines, bar graphs, object diagrams, organizers, sketches, and data tables.
2. **Avoid Decorative Imagery:** No photorealistic or cartoon-style images; visuals must remain schematic and pedagogical.
3. **Conceptual Mapping:** Explicitly explain how each visual corresponds to the underlying abstract concept (e.g., number line for quantity change).
4. **UI Integration:** Specify how visuals should appear in the web UI (placement, sequencing, interaction).
5. **Rendering:** math rendered with KaTeX/MathJax.

#### User Prompt

Using all of the given data, generate a visualized teaching webpage for the following question.

{Question}  
 {Task Planning JSON}  
 {Conceptual Mapping JSON}  
 {Reasoning Decomposition JSON}  
 {Metacognitive Reviewer JSON}

## B ADDITIONAL RESULTS

### B.1 ABLATION STUDIES ON EDUVISAGENT

We conduct ablation studies on the multi-agent teaching system in Table 10.

We compare the overall Total score of the complete system (**Full**) against six variants: **-TP** (without Task Planning), **-CM** (without Conceptual Mapping), **-RD** (without Reasoning Decomposition), **-MR** (without Metacognitive Review), **-VIS** (Using Claude 3.7 Sonnet as the underlying model while keeping the same multi-agent pipeline), and **Single** (a single-agent baseline that uses the same set of prompts without explicit modularization or inter-agent coordination).

**Impact of Removing Individual Modules.** The ablation results reveal clear and systematic evidence that each module in the multi-agent architecture contributes a distinct cognitive function whose removal leads to measurable degradation. Across all subjects and difficulty levels, dropping any single module results in a consistent decline of approximately 4–6 points relative to the full model, indicating that no component is redundant.

**Task Planning (-TP).** Removing the Task Planning module reduces the system’s ability to structure the solution trajectory at the outset. This manifests in weaker performance particularly on Medium and Hard problems, where multi-step planning is essential. Without this stage, the problem-solving process becomes more linear and less globally coherent, leading to incremental reasoning errors that accumulate throughout the solution.

**Conceptual Mapping (-CM).** The Conceptual Mapping module provides the system with an intermediate representational scaffold—a way to organize domain concepts, formulas, and symbolic relations before detailed reasoning begins. Its removal produces one of the largest degradations across domains, showing that the system heavily relies on this symbolic schema construction phase. Without CM, the

Table 10: Ablation study on EduVisAgent. **Full** denotes our complete multi-agent system. **Single** denotes a single-agent baseline using all prompts without modularization. The highest scores are in **bold**.

Subject	Difficulty	Full	-TP	-CM	-RD	-MR	-VIS	Single
<b>Chemistry</b>	Easy	<b>69.00</b>	64.60	63.80	63.00	64.20	64.80	59.30
	Medium	<b>76.27</b>	71.87	71.07	70.27	71.47	72.07	67.42
	Hard	<b>76.00</b>	71.60	70.80	70.00	71.20	71.80	66.85
<b>Physics</b>	Easy	<b>85.33</b>	80.94	80.14	79.34	80.54	81.14	76.10
	Medium	<b>81.71</b>	77.31	76.51	75.71	76.91	77.51	72.05
	Hard	<b>84.00</b>	79.60	78.80	78.00	79.20	79.80	74.32
<b>Maths</b>	Easy	<b>90.20</b>	85.80	85.00	84.20	85.40	86.00	81.05
	Medium	<b>64.50</b>	60.10	59.30	58.50	59.70	60.30	55.27
	Hard	<b>65.00</b>	60.60	59.80	59.00	60.20	60.80	53.88

reasoning tends to jump directly into procedural steps without establishing the underlying conceptual structure, which leads to misapplied rules, inconsistent variable usage, and missing constraints.

**Reasoning Decomposition (-RD).** This module creates explicit fine-grained segmentation of logical steps, and its absence consistently yields the largest drop among all ablations. Without RD, the model tends to condense multi-step reasoning into single large leaps, increasing the likelihood of hidden errors that are never surfaced or corrected. RD therefore serves as the backbone of reliable multi-hop reasoning, ensuring that intermediate steps are interpretable, verifiable, and less prone to compounding mistakes.

**Metacognitive Review (-MR).** The MR module acts as an internal critic, performing self-evaluation and error checking. Removing MR reduces the models ability to detect calculation inconsistencies, missing assumptions, or logical conflicts within its own output. While the primary reasoning path remains intact, the absence of this reflective layer leads to small but systematic accuracy losses, especially on tasks requiring unit checking, boundary conditions, or verification of derived results.

**Model Replacement (-VIS).** Replacing the underlying model with Claude 3.7 Sonnet while preserving the multi-agent structure produces a moderate drop across categories. The decline is smaller than removing core cognitive modules, demonstrating that the multi-agent pipeline itself contributes substantial performance stability. However, it also indicates that the pipeline and the underlying model are jointly responsible for peak performance.

**Single-Agent Baseline.** The **Single** baseline, which collapses all prompts into a single monolithic agent, performs the worst across all conditions. Its scores are consistently below every multi-agent ablation, averaging 8–15 points lower than the full system. This sharp decline highlights that the benefits of the multi-agent design arise not merely from the prompts themselves, but from the explicit architectural separation of planning, conceptual structuring, stepwise reasoning, and self-review.

## B.2 EVALUATION ON NON-STEM DATASETS

Table 11: Performance of Visualization Agents on EduVisBench.

Method	Vis. Type	Prehistory	Sociology	Avg
v0	Webpage	61.8	68.0	64.9
EduVisAgent	Webpage	79.4	84.8	82.1

To further explore EduVisAgent’s performance in non-STEM disciplines, we selected 100 problems from MMLU’s prehistory and sociology categories to evaluate EduVisAgent’s adaptability to narrative and conceptual reasoning tasks. Results in Table 11 show that EduVisAgent significantly outperforms



the current SOTA baseline (v0) by 17.2 points, demonstrating that our multi-agent framework effectively generalizes to humanities education.

B.3 EVALUATION ROBUSTNESS

We tested two other evaluators, Gemini 2.5 pro and Claude 3.7 Sonnet to score visualization results of SDXL, GPT-4o(SVG) and EduVisAgent. The results in Table 12 show consistent scoring patterns across different evaluator models. While there are minor numerical variations in the absolute scores, the overall trends and relative rankings remain highly consistent with the GPT-4o results.

Table 12: Evaluated by GPT-4o, Gemini 2.5 Pro and Claude 3.7 Sonnet on EduVisBench.

Method	Vis. Type	GPT-4o	Gemini 2.5 Pro	Claude 3.7 Sonnet
SDXL	Image	21.8	18.9	24.7
GPT-4o	SVG	25.4	26.3	27.4
EduVisAgent	Webpage	78.9	81.6	84.4

C ADDITIONAL MATHEMATICS EXAMPLES IN EDUVISBENCH

Figure 8, 9, 10 and 11 presents four representative problems from the Hard subset (MATH-500) in EduVisBench, illustrating the range and difficulty of the mathematical reasoning challenges in the benchmark.

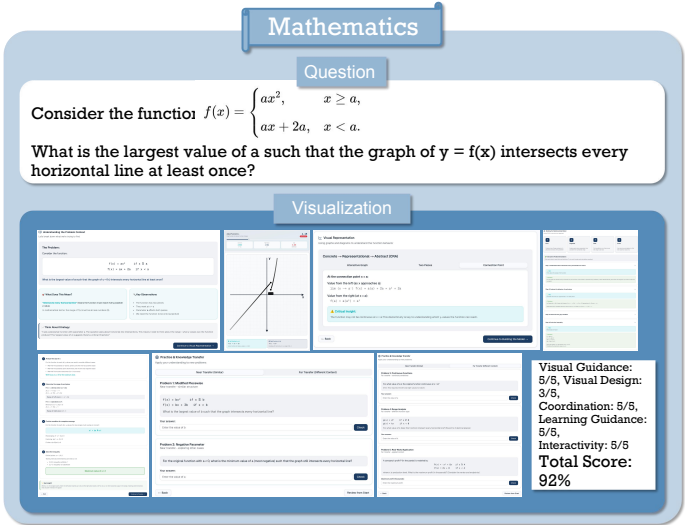


Figure 8: Representative example 1 from the Hard subset (MATH-500) of EduVisBench.

D REAL-WORLD DEPLOYMENT OPTIMIZATION

For real-world deployment, we identify several optimization directions: (1) reducing token consumption through more efficient prompt engineering, (2) optimizing the metacognitive reasoning depth to balance quality and efficiency, and (3) implementing caching mechanisms for frequently used educational concepts. Additionally, the system could operate asynchronously. Teachers prepare materials in advance rather than real-time generation, making latency less critical. Integration with existing LMS platforms would involve API-based deployment where visualization generation occurs server-side.

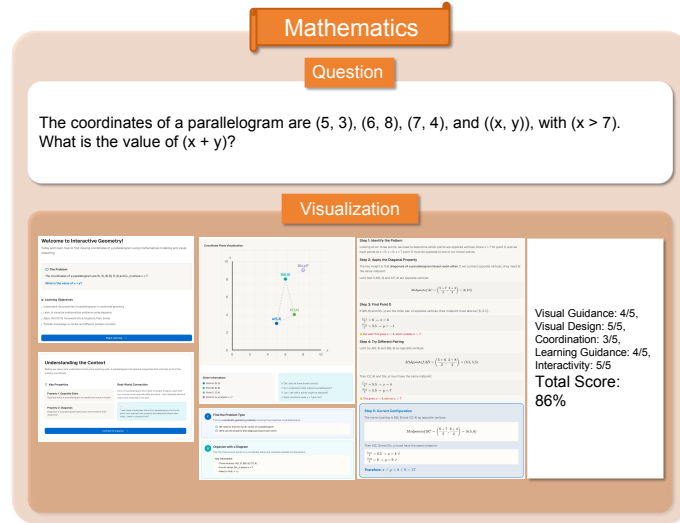


Figure 9: Representative example 2 from the Hard subset (MATH-500) of EduVisBench.

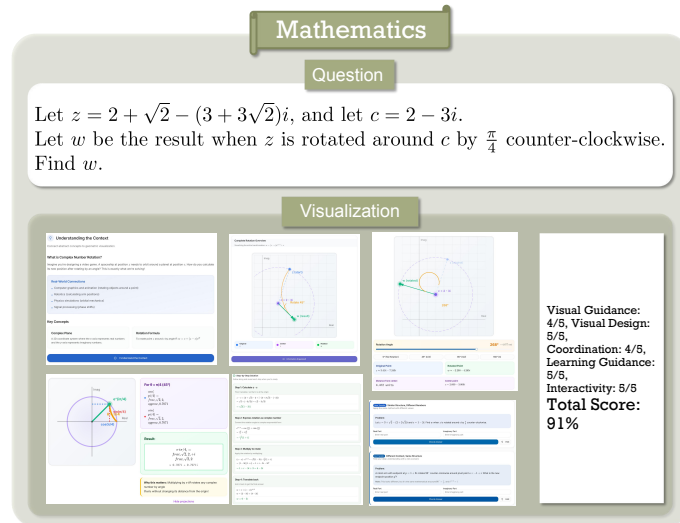


Figure 10: Representative example 3 from the Hard subset (MATH-500) of EduVisBench.

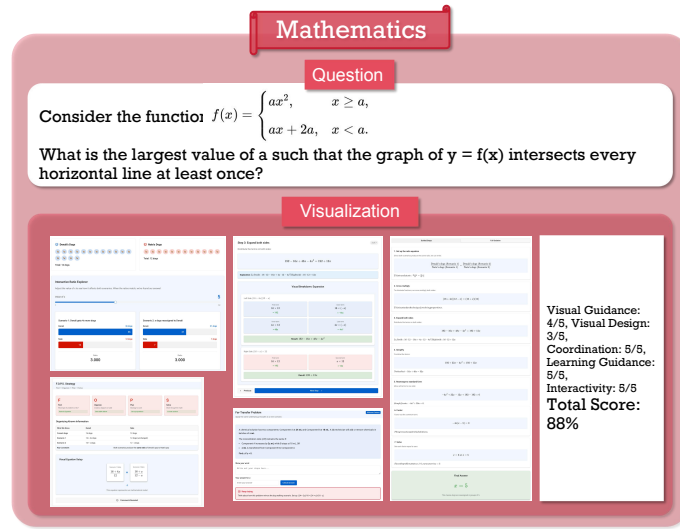


Figure 11: Representative example 4 from the Hard subset (MATH-500) of EduVisBench.

#### D.1 TASK PLANNING REPRESENTATION FOR AN ANGULAR MOTION PROBLEM

1458			
1459			
1460		<b>Scenario, givens, goals, constraints</b>	<b>Transfer tasks</b>
1461		<b>Scenario.</b> A wheel has given angular acceleration and initial angular velocity; we want its angular velocity after a specific time.	<b>Near transfer.</b> <b>Problem:</b> A wheel rotates with an angular acceleration of $3 \text{ rad/s}^2$ . If its initial angular velocity is $5 \text{ rad/s}$ , what is its angular velocity after 4 seconds? <b>Explanation:</b> This is a near-transfer task because it has the same structure as the original problem but with different numerical values (still using $\omega = \omega_0 + \alpha t$ ).
1462		<b>Givens.</b> <ul style="list-style-type: none"><li>Angular acceleration: <math>\alpha = 4 \text{ rad/s}^2</math></li><li>Initial angular velocity: <math>\omega_0 = 2 \text{ rad/s}</math></li><li>Time: <math>t = 5 \text{ s}</math></li></ul>	<b>Far transfer.</b> <b>Problem:</b> A car accelerates uniformly from rest at $3 \text{ m/s}^2$ . What is its velocity after 6 seconds? <b>Explanation:</b> This is a far-transfer task because it involves linear motion instead of angular motion, but uses the analogous kinematic equation $v = v_0 + at$ ; the reasoning pattern is the same.
1463		<b>Goal.</b> <ul style="list-style-type: none"><li>Find the angular velocity <math>\omega</math> after 5 seconds.</li></ul>	
1464		<b>Constraint.</b> <ul style="list-style-type: none"><li>Use the kinematic equation for angular motion: <math>\omega = \omega_0 + \alpha t</math>.</li></ul>	
1465			
1466		<b>Solution strategy</b>	<b>Instructional steps</b>
1467		<b>Analysis.</b> Angular motion with constant angular acceleration; use $\omega = \omega_0 + \alpha t$ directly, since $\omega_0$ , $\alpha$ , $t$ are given.	<b>Step 1.</b> Understand the problem and identify the given values. <u>Concrete.</u> <u>Entities:</u> <ul style="list-style-type: none"><li>wheel</li><li>angular acceleration</li><li>initial angular velocity</li><li>time</li></ul> <b>Description:</b> A rotating wheel with a given angular acceleration and initial angular velocity over a specific time. <u>Representational.</u> <u>Tool:</u> Table. <b>Purpose:</b> Organize the given values clearly for reference. <b>Represents:</b> Angular acceleration ( $\alpha$ ), initial angular velocity ( $\omega_0$ ), and time ( $t$ ). <b>Visual design:</b> <ul style="list-style-type: none"><li>Form: a simple table with columns for quantity, symbol, and value.</li><li>Elements:<ul style="list-style-type: none"><li>headers for quantity, symbol, and value</li><li>rows for <math>\alpha</math>, <math>\omega_0</math>, and <math>t</math></li></ul></li><li>Bridge: helps transition from the problem statement to identifying the variables needed for the equation.</li></ul> <u>Abstract.</u> <u>Constructs:</u> <ul style="list-style-type: none"><li>kinematic equation for angular motion: <math>\omega = \omega_0 + \alpha t</math></li></ul> <b>Connection:</b> The equation relates the given quantities ( $\alpha$ , $\omega_0$ , $t$ ) to the unknown angular velocity ( $\omega$ ). <u>Think-aloud.</u> <ul style="list-style-type: none"><li>What quantities are given in the problem?</li><li>What is the goal of the problem?</li></ul>
1468		<b>Step 1.</b> <u>FOPS label:</u> <ul style="list-style-type: none"><li>F: Angular motion with constant acceleration</li><li>O: <math>\omega = \omega_0 + \alpha t</math></li><li>P: Substitute values</li><li>S: Solve for <math>\omega</math></li></ul> <b>Description:</b> Choose the kinematic equation $\omega = \omega_0 + \alpha t$ . <b>Reasoning:</b> This equation links $\omega$ , $\omega_0$ , $\alpha$ , and $t$ , matching the given data.	<b>Step 2.</b> <u>Goal:</u> Apply the kinematic equation for angular velocity. <b>Action:</b> Write $\omega = \omega_0 + \alpha t$ and substitute the given values. <u>Concepts:</u> <ul style="list-style-type: none"><li>Kinematic equation for angular motion</li></ul> <b>Pitfalls:</b> <ul style="list-style-type: none"><li>Incorrect substitution of values</li><li>Forgetting to include the initial angular velocity</li></ul>
1469		<b>Step 2.</b> <u>FOPS label:</u> <ul style="list-style-type: none"><li>F: Substitution and calculation</li><li>O: <math>\omega = \omega_0 + \alpha t</math></li><li>P: Perform arithmetic</li><li>S: Verify result</li></ul> <b>Description:</b> Substitute $\omega_0 = 2 \text{ rad/s}$ , $\alpha = 4 \text{ rad/s}^2$ , $t = 5 \text{ s}$ : $\omega = 2 + (4 \times 5)$ . <b>Reasoning:</b> Direct substitution turns the symbolic relation into a numerical value.	<b>Step 3.</b> <u>Goal:</u> Calculate the final angular velocity. <b>Action:</b> Perform the arithmetic calculation to find $\omega$ . <u>Concepts:</u> <ul style="list-style-type: none"><li>Basic arithmetic</li><li>Angular velocity</li></ul> <b>Pitfalls:</b> <ul style="list-style-type: none"><li>Arithmetic errors</li><li>Misinterpreting the result</li></ul>
1470		<b>Step 3.</b> <u>FOPS label:</u> <ul style="list-style-type: none"><li>F: Final calculation</li><li>O: <math>\omega = 2 + 20</math></li><li>P: Simplify</li><li>S: Verify correctness</li></ul> <b>Description:</b> Compute $\omega = 2 + 20 = 22 \text{ rad/s}$ . <b>Reasoning:</b> Ensures the arithmetic is correct and consistent with possible answer options.	
1471		<b>Result:</b> $\omega = 22 \text{ rad/s}$ .	
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1507		<b>UI layout suggestion</b>	
1508		<b>Structure.</b> Step-by-step instructional layout with separate sections for scenario, solution strategy, and practice problems.	<b>Key components.</b> <ul style="list-style-type: none"><li>Card</li><li>Accordion</li><li>Alert</li><li>Table</li></ul>
1509		<b>Content organization.</b> Put the scenario at the top, followed by the solution strategy with stepwise explanations, and practice problems at the end.	<b>Math rendering.</b> Use KaTeX or MathJax for equations such as $\omega = \omega_0 + \alpha t$ .
1510			
1511			

Figure 12: Two-column task-planning view for the angular motion example.

## E FULL PROMPT AND INTERMEDIATE STRUCTURES FOR THE ANGULAR VELOCITY EXAMPLE

To make the behavior of each agent more transparent, we include below the full prompt structure for the angular velocity example discussed in reviewer v6KF Q3, covering task\_planning, conceptual\_mapping, reasoning\_decomposition, metacognitive\_reviewer, and the visualization\_page design.

### AGENT 1: TASK PLANNING (task\_planning)

```
task_planning
  scenario
    context
      A wheel is rotating with a given angular acceleration and initial angular
      velocity.
      The task is to determine its angular velocity after a specific time.
    givens
      - Angular acceleration ( $\alpha$ ) = 4 rad/s2
      - Initial angular velocity ( $\omega_0$ ) = 2 rad/s
      - Time (t) = 5 seconds
    goals
      - Find the angular velocity ( $\omega$ ) after 5 seconds
    constraints
      - Use the kinematic equation for angular motion
    solution_strategy
      analysis
        This problem involves angular motion with constant angular acceleration.
        The angular velocity can be calculated using the kinematic equation for
        angular motion  $\omega = \omega_0 + \alpha t$ .
      steps
        - step_number 1
          fops_label F Angular motion with constant acceleration / 0  $\omega = \omega_0 + \alpha t$  / P Substitute values / S Solve for  $\omega$ 
          description
            Use the kinematic equation for angular velocity  $\omega = \omega_0 + \alpha t$ .
            Substitute the given values into the equation.
          reasoning
            This equation relates angular velocity, initial angular velocity,
            angular acceleration, and time.
            It is directly applicable since all required values are provided.
        - step_number 2
          fops_label F Substitution and calculation / 0  $\omega = \omega_0 + \alpha t$  / P Perform arithmetic / S Verify result
          description
            Substitute  $\omega_0 = 2$  rad/s,  $\alpha = 4$  rad/s2, and  $t = 5$  s into
            the equation  $\omega = 2 + (4 \times 5)$ .
          reasoning
            Substituting the values allows us to calculate the final angular
            velocity directly.
        - step_number 3
          fops_label F Final calculation / 0  $\omega = 2 + 20$  / P Simplify / S
            Verify correctness
          description
            Simplify the equation  $\omega = 2 + 20 = 22$  rad/s.
```

```

1566     reasoning
1567         This step ensures the final value is calculated correctly and matches
1568         the given options.
1569 transfer_tasks
1570     near_transfer
1571         problem
1572             A wheel rotates with an angular acceleration of  $3 \text{ rad/s}^2$ .
1573             If its initial angular velocity is  $5 \text{ rad/s}$ , what is its angular velocity
1574             after 4 seconds?
1575         explanation
1576             This is a near-transfer task because it has the same structure as the
1577             original problem
1578             but with different numerical values.
1579     far_transfer
1580         problem
1581             A car accelerates uniformly from rest at a rate of  $3 \text{ m/s}^2$ .
1582             What is its velocity after 6 seconds?
1583         explanation
1584             This is a far-transfer task because it involves linear motion instead of
1585             angular motion,
1586             but the logic of using the kinematic equation remains the same.
1587 instructional_steps
1588     - step_number 1
1589         goal Understand the problem and identify the given values.
1590         action Extract angular acceleration, initial angular velocity, and time
1591         from the problem statement.
1592         concepts
1593             - Angular motion
1594             - Kinematic equations
1595         pitfalls
1596             - Confusing angular velocity with linear velocity
1597             - Misidentifying the given values
1598     - step_number 2
1599         goal Apply the kinematic equation for angular velocity.
1600         action Write the equation  $\omega = \omega_0 + \alpha t$  and substitute the
1601         given values.
1602         concepts
1603             - Kinematic equation for angular motion
1604         pitfalls
1605             - Incorrect substitution of values
1606             - Forgetting to include the initial angular velocity
1607     - step_number 3
1608         goal Calculate the final angular velocity.
1609         action Perform the arithmetic calculation to find  $\omega$ .
1610         concepts
1611             - Basic arithmetic
1612             - Angular velocity
1613         pitfalls
1614             - Arithmetic errors
1615             - Misinterpreting the result
1616 ui_layout_suggestion
1617     structure
1618         A step-by-step instructional layout with clear sections for scenario,
1619         solution strategy, and practice problems.
1620     key_components
1621         - Card
1622         - Accordion
1623         - Alert

```

```

1620     - Table
1621   content_organization
1622     Organize the scenario at the top, followed by the solution strategy with
1623     step-by-step explanations,
1624     and practice problems at the end.
1625   math_rendering
1626     Use KaTeX or MathJax to render equations like  $\omega = \omega_0 + \alpha t$ 
1627     .

```

## AGENT 2: CONCEPTUAL MAPPING (conceptual\_mapping)

```

1632 conceptual_mapping
1633   cra_mapping
1634     - step_number 1
1635       step_name Understand the problem and identify the given values
1636       concrete
1637         entities
1638           - wheel
1639           - angular acceleration
1640           - initial angular velocity
1641           - time
1642         description
1643           A rotating wheel with a given angular acceleration and initial angular
1644           velocity over a specific time.
1645       representational
1646         - tool Table
1647           purpose Organize the given values clearly for reference.
1648           represents Angular acceleration ( $\alpha$ ), initial angular velocity ( $\omega_0$ ), and time ( $t$ ).
1649         visual_design
1650           form A simple table with columns for quantity, symbol, and value.
1651           elements
1652             - Headers for quantity, symbol, and value
1653             - Rows for  $\alpha$ ,  $\omega_0$ , and  $t$ 
1654         bridge
1655           Helps transition from the problem statement to identifying the
1656           variables needed for the equation.
1657       abstract
1658         constructs
1659           - Kinematic equation for angular motion  $\omega = \omega_0 + \alpha t$ 
1660         connection
1661           The equation relates the given quantities ( $\alpha$ ,  $\omega_0$ ,  $t$ ) to the
1662           unknown angular velocity ( $\omega$ ).
1663       think_aloud
1664         - What quantities are given in the problem?
1665         - What is the goal of the problem?
1666     - step_number 2
1667       step_name Apply the kinematic equation for angular velocity
1668       concrete
1669         entities
1670           - angular velocity
1671           - kinematic equation
1672         description
1673           Using the equation  $\omega = \omega_0 + \alpha t$  to calculate the
           angular velocity.
1674       representational

```



```

1674 - tool Equation
1675   purpose Show the relationship between angular velocity, initial
1676   angular velocity, angular acceleration, and time.
1677   represents The kinematic equation for angular motion.
1678   visual_design
1679     form Equation written in standard mathematical notation.
1680     elements
1681       -  $\omega = \omega_0 + \alpha t$ 
1682     bridge
1683       Links the abstract formula to the concrete problem by substituting
1684       the given values.
1685 - tool Dynamic animation (optional)
1686   purpose Illustrate how angular velocity changes over time with
1687   constant acceleration.
1688   represents The growth of angular velocity as time progresses.
1689   visual_design
1690     form A graph or animation showing  $\omega$  increasing linearly with
1691     time.
1692     elements
1693       - Time on x-axis
1694       - Angular velocity on y-axis
1695     bridge
1696       Visualizes the relationship described by the equation.
1697 abstract
1698   constructs
1699     - Substitution of values into  $\omega = \omega_0 + \alpha t$ 
1700   connection
1701     Substituting concrete values into the abstract formula to find the
1702     solution.
1703 think_aloud
1704   - What is the equation we need to use?
1705   - How do we substitute the given values into the equation?
1706 - step_number 3
1707 step_name Calculate the final angular velocity
1708 concrete
1709   entities
1710     - arithmetic calculation
1711     - final angular velocity
1712   description
1713     Performing the calculation to find the final angular velocity.
1714 representational
1715   - tool Step-by-step arithmetic
1716   purpose Break down the calculation into smaller steps for clarity.
1717   represents The process of solving  $\omega = 2 + (4 \times 5)$ .
1718   visual_design
1719     form Sequential steps showing each part of the calculation.
1720     elements
1721       - Substitute values
1722       - Multiply  $\alpha$  and  $t$ 
1723       - Add to  $\omega_0$ 
1724     bridge
1725       Connects the abstract substitution to the concrete result.
1726 - tool Alert or feedback box
1727   purpose Highlight common errors in arithmetic or substitution.
1728   represents Potential pitfalls in the calculation process.
1729   visual_design
1730     form A colored box with tips or warnings.
1731     elements

```

```

1728         - Error examples
1729         - Corrective suggestions
1730     bridge
1731         Prevents errors and reinforces correct calculation methods.
1732     abstract
1733     constructs
1734         - Final result  $\omega = 22 \text{ rad/s}$ 
1735     connection
1736         The calculated result is the concrete realization of the abstract
1737         formula.
1738     think_aloud
1739         - What is the next step in the calculation?
1740         - Does the result make sense given the problem context?

```

### AGENT 3: REASONING DECOMPOSITION (reasoning\_decomposition)

```

1745 reasoning_decomposition
1746     fops_reasoning
1747     - action
1748         Extract angular acceleration, initial angular velocity, and time from
1749         the problem statement.
1750     concepts
1751         - Angular motion
1752         - Kinematic equations
1753     scaffolding_needed true
1754     scaffolding_notes
1755         Learners may confuse angular velocity with linear velocity or
1756         misidentify the given values.
1757         Provide a table to organize the values.
1758     visual_support
1759         needed true
1760         which_visual Table for organizing given values
1761         interaction Draggable labels to match quantities with their symbols and
1762         values
1763     - action
1764         Write the equation  $\omega = \omega_0 + \alpha t$  and substitute the given
1765         values.
1766     concepts
1767         - Kinematic equation for angular motion
1768     scaffolding_needed true
1769     scaffolding_notes
1770         Learners may struggle with identifying the correct equation or
1771         substituting values correctly.
1772         Provide a guided substitution exercise.
1773     visual_support
1774         needed true
1775         which_visual Equation with placeholders for substitution
1776         interaction Reveals for each substitution step
1777     - action
1778         Perform the arithmetic calculation to find  $\omega$ .
1779     concepts
1780         - Basic arithmetic
1781         - Angular velocity
1782     scaffolding_needed true
1783     scaffolding_notes

```

```

1782         Arithmetic errors are common. Break down the calculation into smaller
1783         steps and provide feedback on errors.
1784     visual_support
1785         needed true
1786         which_visual Step-by-step arithmetic breakdown
1787         interaction Dynamic reveals for each calculation step
1788
1789 practice_activities
1790     - activity_number 1
1791       name Identify Given Values
1792       type fill-in
1793       task
1794         Fill in the table with the given values for angular acceleration, initial
1795         angular velocity, and time.
1796       gradual_release
1797         Start with guided examples where learners match quantities to symbols,
1798         then move to independent identification.
1799
1800     - activity_number 2
1801       name Substitute Values into Equation
1802       type choice
1803       task
1804         Choose the correct substitution for  $\omega = \omega_0 + \alpha t$  given  $\alpha = 4 \text{ rad/s}^2$ ,  $\omega_0 = 2 \text{ rad/s}$ , and  $t = 5 \text{ s}$ .
1805       gradual_release
1806         Begin with hints and feedback for incorrect choices, then transition to
1807         independent substitution.
1808
1809     - activity_number 3
1810       name Calculate Angular Velocity
1811       type judgment
1812       task
1813         Perform the calculation  $\omega = 2 + (4 \times 5)$  and verify if the result is
1814         correct.
1815       gradual_release
1816         Provide step-by-step guidance initially, then allow learners to perform
1817         the calculation independently with feedback.
1818
1819     - activity_number 4
1820       name Near Transfer Problem
1821       type explanation
1822       task
1823         Solve a similar problem
1824         A wheel rotates with an angular acceleration of  $3 \text{ rad/s}^2$ .
1825         If its initial angular velocity is  $5 \text{ rad/s}$ , what is its angular velocity
1826         after 4 seconds?
1827       gradual_release
1828         Start with guided problem-solving steps, then transition to independent
1829         problem-solving.
1830
1831     - activity_number 5
1832       name Far Transfer Problem
1833       type explanation
1834       task
1835         Solve a far-transfer problem
1836         A car accelerates uniformly from rest at a rate of  $3 \text{ m/s}^2$ .
1837         What is its velocity after 6 seconds?
1838       gradual_release

```

Provide a comparison to angular motion initially, then allow learners to solve independently.

#### AGENT 4: METACOGNITIVE REVIEWER (metacognitive\_reviewer)

```
metacognitive_reviewer
  metacognitive_prompts
    before_solving
      - What quantities are given in the problem, and what do they represent?
      - What is the goal of the problem, and how can I achieve it?
    during_solving
      - Am I using the correct equation for this problem?
      - Have I substituted the values correctly into the equation?
    after_solving
      - Does my result make sense given the context of the problem?
      - What could I improve in my approach to solving similar problems?

  general_strategies
    - strategy Self-monitoring technique
      when_to_use During the substitution and calculation phases
      how_to_apply
        Pause after each step to verify the accuracy of substitutions and
        calculations.
    - strategy Error-checking routine
      when_to_use After completing the calculation
      how_to_apply
        Revisit the problem statement and verify that the result aligns with the
        given values and context.
    - strategy Visualization
      when_to_use During the understanding phase
      how_to_apply
        Organize the given values in a table or diagram to clarify relationships
        between quantities.
```

#### AGENT 5: VISUALIZATION PAGE DESIGN (visualization\_page)

```
visualization_page
  layout_overview
    structure
      description >
        The webpage uses a step-by-step instructional layout with clearly
        separated sections.
    sections
      - id scenario_overview
        title Scenario Overview
        content Problem statement and given values.
      - id step_by_step_solution
        title Step-by-Step Solution
        content Interactive visuals for each step of the solution.
      - id practice_problems
        title Practice Problems
        content Near-transfer and far-transfer tasks.
      - id reflection_prompts
        title Reflection Prompts
```

```

1890         content Metacognitive questions to guide learners.
1891     ui_components
1892     - Cards for each step in the solution strategy.
1893     - Accordion for expandable explanations and hints.
1894     - Alerts for common pitfalls and corrections.
1895     - Interactive visuals including tables, equations, and animations.
1896
1897     static_visuals
1898     step_1_organizing_values
1899     goal Organize given values for reference.
1900     visual_design
1901     type table
1902     columns
1903     - Quantity
1904     - Symbol
1905     - Value
1906     rows
1907     - Angular acceleration ( $\alpha$ )
1908     - Initial angular velocity ( $\omega_0$ )
1909     - Time ( $t$ )
1910     interaction
1911     description Learners drag and drop labels to match quantities with
1912     symbols and values.
1913     step_2_applying_equation
1914     goal Make the kinematic equation explicit and concrete.
1915     visual_design
1916     equation_form  $\omega = \omega_0 + \alpha t$ 
1917     substitution_example  $\omega = 2 + (4 \times 5)$ 
1918     dynamic_support
1919     description Equation initially shows placeholders; each placeholder
1920     reveals the substituted value when clicked.
1921     step_3_calculation
1922     goal Make the arithmetic process transparent.
1923     visual_design
1924     breakdown_steps
1925     -  $4 \times 5 = 20$ 
1926     -  $2 + 20 = 22$ 
1927     representation flowchart or sequential steps.
1928
1929     dynamic_behavior
1930     animation_angular_velocity_graph
1931     purpose >
1932     Show how angular velocity increases linearly over time with constant
1933     angular acceleration.
1934     design
1935     axes
1936     x_axis Time  $t$  (0 to 5 s)
1937     y_axis Angular velocity  $\omega$  (0 to 22 rad/s)
1938     behavior
1939     start_value 2 rad/s
1940     end_value 22 rad/s
1941     interaction
1942     on_load Line animates from  $t = 0$  to  $t = 5$ .
1943     animation_stepwise_substitution
1944     purpose Visualize the substitution process in the equation.
1945     design
1946     base_equation  $\omega = \omega_0 + \alpha t$ 
1947     placeholders
1948     -  $\omega_0 = 2$ 

```

```

- \alpha = 4
- t = 5
timing
effect short fade-in for each reveal.

user_interactions
interactive_table
description >
    Drag-and-drop interface to match quantities, symbols, and numerical
    values.
equation_substitution
description >
    Clickable placeholders in the equation that reveal each substituted
    value in sequence.
arithmetic_breakdown
description >
    "Next step" interaction revealing  $4 \times 5 = 20$ , followed by  $2 + 20 = 22$ ,
    with optional feedback messages.

```

## F QUALITATIVE SUCCESS AND FAILURE CASES

### SUCCESS CASES

**Problem**

What is the difference between isotopes of an element?

(A) Number of protons

(B) Number of neutrons

(C) Number of electrons

(D) Atomic number

The correct answer is (B) Number of neutrons. Isotopes of the same element have the same number of protons and electrons, but different numbers of neutrons.

**1 Understanding the Context**

**Scenario**  
Understanding the difference between isotopes of an element in the context of atomic structure.

**Given:**

- > Isotopes are variants of the same chemical element
- > They have the same number of protons and electrons
- > They differ in the number of neutrons

**Goal:**  
Identify the correct distinguishing factor between isotopes.

**Note:**  
The atomic number (number of protons) remains constant for isotopes of the same element. The number of electrons also remains constant in neutral atoms.

**Key Objects:**  
protons neutrons electrons atomic number mass number

**Before starting:**  
What do I already know about isotopes and atomic structure? | What is the goal of this task, and how can I approach it effectively?

Figure 13: Success case 1 illustrating coherent multi-agent collaboration.

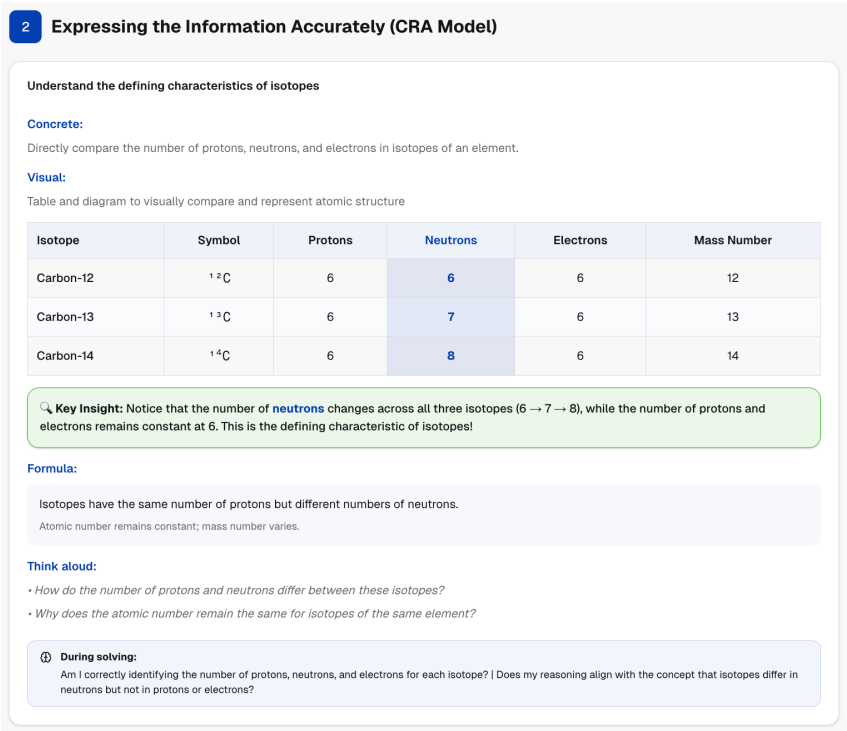


Figure 14: Success case 2 illustrating coherent multi-agent collaboration.

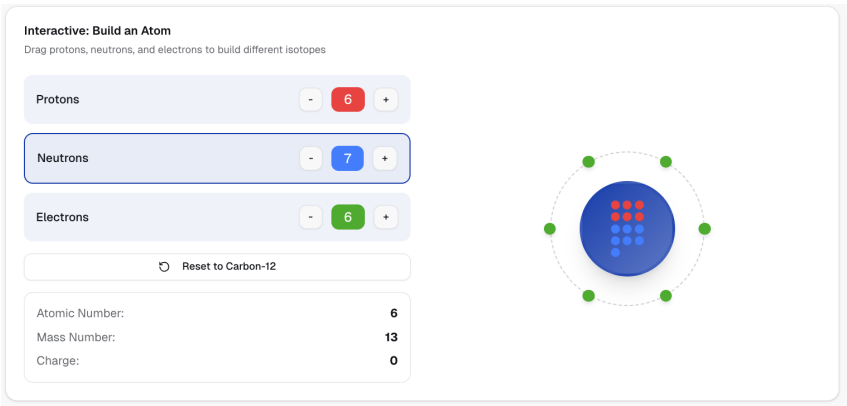


Figure 15: Success case 3 illustrating coherent multi-agent collaboration.



**Identify the correct distinguishing factor between isotopes**

**Concrete:**  
Directly analyze the properties of isotopes to identify the distinguishing factor.

**Visual:**

⚠ **Common Pitfall:**  
Confusing the number of protons with the number of neutrons, or assuming isotopes have different atomic numbers.

Property	Same in Isotopes?	Explanation
Number of Protons	✓	Defines the element's identity
Number of Neutrons	✗	This is what differs between isotopes!
Number of Electrons	✓	Same in neutral atoms
Atomic Number	✓	Equals number of protons

**Formula:**

Mass number varies among isotopes due to differing neutrons.  
Atomic number remains constant for isotopes of the same element.

**Think aloud:**

- Which property changes among isotopes: atomic number or mass number?
- Why does the number of neutrons affect the mass number but not the atomic number?

Figure 16: Success case 4 illustrating coherent multi-agent collaboration.

**3 Building Mathematical Models (FOPS)**

**Problem Type**

Isotopes of an element are defined as atoms with the same number of protons (and hence the same atomic number) but different numbers of neutrons. This difference in neutrons leads to a difference in atomic mass but not in chemical properties.

**Key Points:**

- > Understand the defining characteristics of isotopes.
  - ⚠ Watch: Confusing the number of protons with the number of neutrons
- > Identify the correct answer from the options provided.
  - ⚠ Watch: Misinterpreting the relationship between atomic number and isotopes

**Step 1: Compare Atomic Structure**

Compare the number of protons, neutrons, and electrons in isotopes

Use visual aids like tables and diagrams to clarify the differences.

⚠ **Learner Support:**  
Students may confuse protons with neutrons or assume isotopes have different atomic numbers. Use visual aids to clarify.

Carbon-12   Carbon-13   Carbon-14

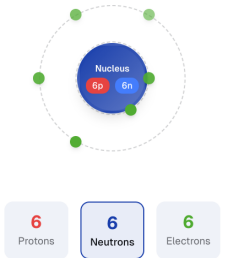


Figure 17: Success case 5 illustrating coherent multi-agent collaboration.

39

4

Transfer Tasks

Near-Transfer

Same Structure

What distinguishes isotopes of carbon (e.g., Carbon-12 and Carbon-14)?

This applies the same concept of isotopes to a specific element.

Far-Transfer

Different Context

How does the difference in the number of neutrons among isotopes affect their physical properties, such as stability or radioactivity?

This requires applying the concept to a broader context involving physical properties.

ⓘ After solving:

Did I correctly identify the distinguishing factor between isotopes? | What did I learn from this task, and how can I apply it to similar problems? | What mistakes did I make, and how can I avoid them in the future?

5

Practice Activities & Cognitive Support

Activity 1: Compare Isotopes

Fill in the table comparing Carbon-12 and Carbon-14

Carbon-12

Protons

Neutrons

Electrons

Carbon-14

Protons

Neutrons

Electrons

Check Answer

Figure 18: Success case 6 illustrating coherent multi-agent collaboration.

Activity 2: Identify the Factor

Which property distinguishes isotopes of the same element?

☐ A) Atomic number

☐ B) Mass number

☐ C) Number of electrons

Check Answer

Activity 3: Explain the Concept

Explain why isotopes have different mass numbers but the same atomic number

Write your explanation here...

Submit

Activity 4: Apply Your Knowledge

Which isotope of hydrogen (Protium, Deuterium, or Tritium) is most likely radioactive?

Isotope	Protons	Neutrons	Mass Number
Protium ( <sup>1</sup> H)	1	0	1
Deuterium ( <sup>2</sup> H)	1	1	2
Tritium ( <sup>3</sup> H)	1	2	3

Explain your answer and reasoning...

Submit

Figure 19: Success case 7 illustrating coherent multi-agent collaboration.

FAILURE CASE: ERROR ACCUMULATION IN THE MULTI-AGENT PIPELINE

**Problem**

A wheel rotates with an angular acceleration of **4 rad/s<sup>2</sup>**. If its initial angular velocity is **2 rad/s**, what is its angular velocity after **5 seconds**?

A10 rad/s

B12 rad/s

C14 rad/s

D16 rad/s

**1 Helping Students Understand the Context**

Breaking down the problem scenario and identifying key components

**Scenario:**

A wheel is rotating with a given angular acceleration and initial angular velocity. The task is to determine its angular velocity after a specific time.

**Given:**

- Angular acceleration ( $\alpha$ ) = 4 rad/s<sup>2</sup>
- Initial angular velocity ( $\omega_0$ ) = 2 rad/s
- Time ( $t$ ) = 5 seconds

**Goal:**

Find the angular velocity ( $\omega$ ) after 5 seconds

**Note:** Use the kinematic equation for angular motion

**Key objects:**

wheel

angular acceleration

initial angular velocity

time

angular velocity

kinematic equation

**Before starting:**

What quantities are given in the problem, and what do they represent? | What is the goal of the problem, and how can I achieve it?

Figure 20: Failure case step 1. The initial task\_planning agent proposes an inappropriate ui\_layout\_suggestion where elements such as Card, Accordion, Alert, and Table have no meaningful relation to the underlying concept of angular velocity.

**2 Expressing the Information Accurately**

Using the CRA Model: Concrete → Representational → Abstract

**Step 1: Understand the problem and identify the given values**

Concrete: wheel, angular acceleration, initial angular velocity

Quantity	Symbol	Value
Angular Acceleration	$\alpha$	4 rad/s <sup>2</sup>
Initial Angular Velocity	$\omega_0$	2 rad/s
Time	$t$	5 s
Angular Velocity (Unknown)	$\omega$	?

**Formula:** Kinematic equation for angular motion:  $\omega = \omega_0 + \alpha t$

**Step 2: Apply the kinematic equation for angular velocity**

Substituting values into  $\omega = \omega_0 + \alpha t$

$$\omega = \omega_0 + \alpha t$$

Click the buttons below to substitute each value:

$\omega_0$

$\alpha$   
4 rad/s<sup>2</sup>

$t$

Figure 21: Failure case step 2. Downstream reasoning agents infer the need for a rotating wheel visualization, but the earlier erroneous layout suggestion continues to impose irrelevant UI constraints.

**3 Guiding Students to Build Mathematical Models**

FOPS Framework: Framework for Organizing Problem Solving

**Problem Type**

This problem involves angular motion with constant angular acceleration. The angular velocity can be calculated using the kinematic equation for angular motion:  $\omega = \omega_0 + \alpha t$

**Key Points & Common Pitfalls**

- 1 Extract angular acceleration, initial angular velocity, and time from the problem statement**

Angular motion Kinematic equations

**Watch out:**  
Learners may confuse angular velocity with linear velocity or misidentify the given values. Provide a table to organize the values.
- 2 Write the equation  $\omega = \omega_0 + \alpha t$  and substitute the given values**

Kinematic equation for angular motion

**Watch out:**  
Learners may struggle with identifying the correct equation or substituting values correctly. Provide a guided substitution exercise.
- 3 Perform the arithmetic calculation to find  $\omega$** 

Basic arithmetic Angular velocity

**Watch out:**  
Arithmetic errors are common. Break down the calculation into smaller steps and provide feedback on errors.

**During solving:**  
Am I using the correct equation for this problem? | Have I substituted the values correctly into the equation?

Figure 22: Failure case step 3. Visualization Agent attempts to comply with upstream layout directives, resulting in non-physics-related components instead of correct angular-motion visuals.

Near-Transfer (Same Structure)

**Practice Problem 1**

Same problem structure with different numerical values

A wheel rotates with an angular acceleration of **3 rad/s<sup>2</sup>**. If its initial angular velocity is **5 rad/s**, what is its angular velocity after **4 seconds**?

Why this is near-transfer:

This problem has the same structure as the original problem but with different numerical values. You'll use the same equation ( $\omega = \omega_0 + \alpha t$ ) and follow the same steps.

▼ Show solution →

$$\omega = \omega_0 + \alpha t$$

$$\omega = 5 + 3 \times 4$$

$$\omega = 5 + 12$$

$$\omega = 17 \text{ rad/s}$$

Far-Transfer (Different Context)

**Practice Problem 2**

Same mathematical logic in a different physical context

A car accelerates uniformly from rest at a rate of **3 m/s<sup>2</sup>**. What is its velocity after **6 seconds**?

Why this is far-transfer:

This problem involves **linear motion** instead of angular motion, but the logic of using the kinematic equation remains the same ( $v = v_0 + at$ ). You're applying the same mathematical reasoning in a different physical context.

► Show solution →

Figure 23: Failure case step 4. The multi-agent chain amplifies the initial planning mistake: despite correct domain inference, the final UI is structurally misaligned.

**5 Learning Approach & Practice Activities**  
Interactive exercises to reinforce your understanding

**Activity 1: Identify Given Values**  
Fill in the table with the correct values for angular acceleration, initial angular velocity, and time.

Given:  $\alpha = 4 \text{ rad/s}^2$ ,  $\omega_0 = 2 \text{ rad/s}$ ,  $t = 5 \text{ s}$   
Which value represents the initial angular velocity?

4 rad/s <sup>2</sup>	2 rad/s
5 s	22 rad/s

**Activity 2: Substitute Values into Equation**  
Choose the correct substitution for  $\omega = \omega_0 + \alpha t$  given  $\alpha = 4 \text{ rad/s}^2$ ,  $\omega_0 = 2 \text{ rad/s}$ , and  $t = 5 \text{ s}$ .

$\omega = 4 + 2 \times 5$	$\omega = 2 + 4 \times 5$
$\omega = 5 + 2 \times 4$	$\omega = 2 + 5 \times 4$

**Activity 3: Calculate Angular Velocity**  
Perform the calculation  $\omega = 2 + (4 \times 5)$  and verify if the result is correct.

$\omega = 2 + (4 \times 5) = ?$

30 rad/s	22 rad/s
40 rad/s	12 rad/s

Figure 24: Failure case final outcome. Due to accumulated constraint errors, the system fails to produce any meaningful visualization related to angular velocity, demonstrating error propagation in multi-agent settings.