

INFIAGENT: SELF-EVOLVING PYRAMID AGENT FRAMEWORK FOR INFINITE SCENARIOS

Anonymous authors

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ABSTRACT

Large Language Model (LLM) agents have demonstrated remarkable capabilities in organizing and executing complex tasks, and many such agents are now widely used in various application scenarios. However, developing these agents requires carefully designed workflows, carefully crafted prompts, and iterative tuning, which requires LLM techniques and domain-specific expertise. These handcrafted limitations hinder the scalability and cost-effectiveness of LLM agents across a wide range of industries. To address these challenges, we propose **InfiAgent**, a Pyramid-like DAG-based Multi-Agent Framework that can be applied to **infinite** scenarios, which introduces several key innovations: a generalized "agent-as-a-tool" mechanism that automatically decomposes complex agents into hierarchical multi-agent systems; a dual-audit mechanism that ensures the quality and stability of task completion; an agent routing function that enables efficient task-agent matching; and an agent self-evolution mechanism that autonomously restructures the agent DAG based on new tasks, poor performance, or optimization opportunities. Furthermore, InfiAgent's atomic task design supports agent parallelism, significantly improving execution efficiency. This framework evolves into a versatile pyramid-like multi-agent system capable of solving a wide range of problems. Evaluations on multiple benchmarks demonstrate that InfiAgent achieves 9.9% higher performance compared to ADAS (similar auto-generated agent framework), while a case study of the AI research assistant InfiHelper shows that it generates scientific papers that have received recognition from human reviewers at top-tier IEEE conferences.

1 INTRODUCTION

The rapid development of large-scale language models (LLMs) has ushered in a new era of intelligent automation (Naveed et al., 2025; Tran et al., 2025), with agent-based systems demonstrating remarkable capabilities in organizing and executing complex tasks across domains. From scientific research and software development to creative content generation and business process automation, LLM agents are transforming how we solve problems at scale. However, the development and deployment of these agents face significant challenges, limiting their widespread adoption and effectiveness.

Current approaches to building LLM agents rely heavily on carefully designed workflows, carefully crafted prompts, and extensive iterative tuning—processes that require deep LLM expertise and domain-specific knowledge (Veeramachaneni, 2025; Guo et al., 2024; Annam et al., 2025; Schick et al., 2023). This reliance on handcrafted solutions creates a fundamental scalability barrier: each new application requires significant manual intervention, making it difficult to rapidly deploy agents across diverse industries and use cases. Furthermore, as system complexity increases, existing multi-agent systems often suffer from unpredictable interactions, resource conflicts, and emergent behavioral instabilities.

A core challenge lies in the lack of a principled, generalizable framework that can automatically decompose complex tasks, ensure system stability, and enable autonomous adaptation. Traditional multi-agent architectures typically adopt a point-to-point collaboration model that allows unrestricted agent interactions (Sun et al., 2025; Ning & Xie, 2024). This leads to coordination overhead, deadlock situations, and difficulty maintaining predictable system behavior. While recent agent

054 frameworks (Hu et al., 2025; Dang et al., 2025) have demonstrated the potential for end-to-end au-
055 tomation, they are still limited by their reliance on manually written templates and lack the system
056 reasoning capabilities required for robust, scalable deployment.

057 To address these fundamental limitations, we introduce **InfiAgent**, a DAG-based multi-agent frame-
058 work that represents a paradigm shift in how we conceptualize and implement agent-based systems.
059 InfiAgent is designed as a general framework that automatically adapts to diverse problem domains
060 without requiring extensive manual configuration or domain-specific expertise. Our approach is
061 based on four key innovations that collectively enable scalable, stable, and self-evolving agent sys-
062 tems.

063 First, we introduce a generalized **”agent-as-a-tool” mechanism** that fundamentally reimagines
064 how agents interact and collaborate. This mechanism enables automatic decomposition of com-
065 plex agents into hierarchical multi-agent systems, where higher-level agents can seamlessly invoke
066 lower-level agents as specialized tools. This abstraction allows for unprecedented modularity and
067 reusability, enabling the same underlying framework to handle tasks ranging from scientific research
068 to software engineering.

069 Second, we propose a **dual-audit mechanism** that ensures both quality and stability of task comple-
070 tion. Unlike traditional approaches that rely on post-hoc validation, our dual-audit system provides
071 continuous monitoring and verification throughout the execution process, preventing error propaga-
072 tion and ensuring reliable outcomes even in complex, multi-stage workflows.

073 Third, we develop an **intelligent agent routing function** that enables efficient task-agent matching
074 without requiring manual configuration. This routing mechanism automatically identifies the most
075 appropriate agents for specific subtasks, optimizing resource utilization and execution efficiency
076 while maintaining system coherence.

077 Fourth, we introduce an **agent self-evolution mechanism** that enables autonomous restructuring
078 of the agent tree based on performance feedback, new task requirements, and optimization oppor-
079 tunities. This capability allows InfiAgent to continuously improve its effectiveness and adapt to
080 changing requirements without human intervention.

081 These innovations collectively enable InfiAgent to evolve into a versatile, pyramid-like multi-agent
082 system capable of solving a wide range of problems while maintaining stability, efficiency, and
083 adaptability. The framework’s atomic task design supports agent parallelism, significantly improv-
084 ing execution efficiency, while its DAG structure ensures predictable behavior and resource utiliza-
085 tion.

086 Our contributions are as follows:

087
088 **(1) Universal Agent Framework with Agent-as-a-Tool Abstraction:** We present InfiAgent—a
089 DAG-based multi-agent framework that provides a principled approach to building scalable, stable,
090 and self-evolving agent systems. This framework introduces a generalized mechanism that can au-
091 tomatically decompose complex agents into hierarchical structures with unrestricted depth, ensuring
092 demand alignment and stability under massive agent populations through tool constraints and be-
093 havioral constraints. This design enables unprecedented modularity and reusability across diverse
094 application domains.

095 **(2) Dual-Audit Quality Assurance Mechanism:** We propose a comprehensive auditing mecha-
096 nism that ensures both quality and stability of task completion through continuous monitoring and
097 verification. The dual-layer auditing system operates at both execution and system levels, preventing
098 error propagation and ensuring reliable outcomes in complex multi-stage workflows while maintain-
099 ing context efficiency through structured output formatting and retrospective summarization.

100 **(3) Intelligent Task Routing and Context Control:** We develop an automated routing system
101 that enables efficient task-agent matching and resource optimization without manual configuration.
102 The framework implements lightweight communication protocols where agents exchange only file
103 descriptors and metadata, combined with sophisticated context management that decomposes exe-
104 cution context into system prompts, memory indices, shared memory, and compressed environment
105 interactions.

106 **(4) Self-Evolution Capability:** We design an autonomous restructuring mechanism that enables
107 agents to dynamically optimize their DAG topology and internal configurations based on perfor-

108 mance feedback and changing requirements. This evolution operates at multiple levels including
109 model-level evolution through Git-style workflows, agent-level evolution using high-quality train-
110 ing data, and topology-level evolution that enables domain-specific expert model formation and
111 dynamic architecture adaptation.

112 Through extensive evaluation and a detailed case study of InfiHelper, we demonstrate that InfiAgent
113 addresses the fundamental scalability and stability challenges that have hindered the widespread
114 adoption of multi-agent systems, opening new possibilities for intelligent automation across diverse
115 domains.

116 117 118 2 RELATED WORK

119 120 2.1 MULTI-AGENT SYSTEM ARCHITECTURES

121
122 Traditional multi-agent systems have primarily focused on peer-to-peer collaboration models, where
123 agents interact freely to achieve common goals. While effective for simple coordination tasks, these
124 approaches struggle with complex, hierarchical task decomposition. Recent work has explored var-
125 ious architectural patterns, including centralized coordination (GUL et al., 2022), hierarchical or-
126 ganization (LIU et al., 2025), and emergent behavior (HAN, 2022). Recent taxonomic work by
127 Moore (Moore, 2025) has further categorized Hierarchical Multi-Agent Systems (HMAS) along
128 dimensions of control, information flow, and temporal leveling, highlighting trade-offs between
129 global efficiency and local autonomy in industrial settings such as power grids. Furthermore, com-
130 prehensive reviews note a persistent challenge in designing unified agents that seamlessly integrate
131 cognition, planning, and interaction, despite advances in hierarchical reinforcement learning and
132 LLM-based reasoning (Qu, 2025). However, these approaches often lack built-in mechanisms for
133 stability-constrained composition, a gap our architecture explicitly addresses.

134 135 2.2 TASK DECOMPOSITION IN MULTI-AGENT SYSTEMS

136
137 Task decomposition has been a central challenge in multi-agent system design. Existing approaches
138 include goal-oriented decomposition (LI et al., 2023), constraint-based decomposition (CAI et al.,
139 2017), and learning-based decomposition (WOO et al., 2022). Increasingly, knowledge graphs
140 (KGs) are being leveraged to provide a structured foundation for task decomposition and agent co-
141 ordination. Frameworks like AGENTiGraph demonstrate how multi-agent systems can dynamically
142 interpret user intents and manage tasks by integrating and querying against a background KG, sig-
143 nificantly improving performance in complex, domain-specific scenarios (ZHAO et al., 2025; GAO
144 et al., 2025). While promising, such KG-dependent approaches often presuppose the existence of
145 a high-quality knowledge base and can be constrained by its scope. However, they, along with the
146 more traditional methods, often lack guarantees regarding system stability and resource utilization.
147 In contrast, our method enforces stability through strict compositional constraints and built-in re-
148 view mechanisms, ensuring robustness even in knowledge-sparse environments or for novel tasks
149 beyond the initial KG design.

150 151 2.3 AGENT EVOLUTION AND SELF-ADAPTATION

152
153 Recent studies emphasize that scalable multi-agent systems must incorporate mechanisms of evolu-
154 tion and adaptation. Frameworks such as AgentGym and Richelieu highlight self-improving LLM
155 agents in dynamic environments (Xi et al., 2024; Guan et al., 2024), while EvoAgent and co-
156 evolutionary theories extend evolutionary computation to automatic agent generation and emergent
157 cooperation (Yuan et al., 2024; De Zarzà et al., 2023). Complementary efforts focus on behavioral
158 adaptation, including continual preference alignment (CPPO) and symbolic self-refinement (Zhang
159 et al., 2024; Zhou et al., 2024). At a broader scope, surveys of evolutionary computation (Chen
160 et al., 2025) and collaborative architecture design frameworks such as NADER (Yang et al., 2025)
161 underscore that both algorithmic and structural evolution are central to building resilient agent sys-
tems. These advances directly motivate InfiAgent’s design of self-restructuring DAG topologies
with performance-driven adaptation.

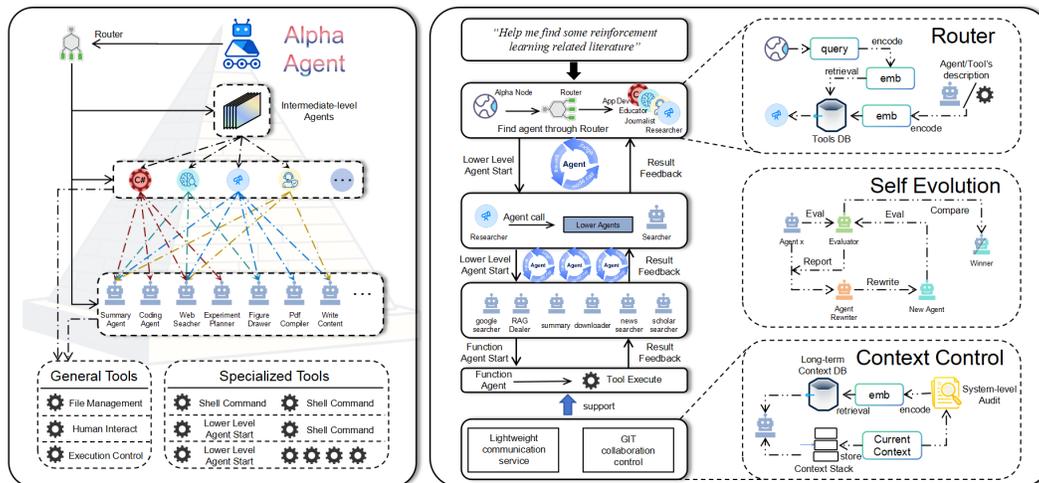


Figure 1: **InfiAgent Framework Architecture.** Left: An intuitive Pyramid-like agent organization architecture of InfiAgent, featuring a Router that redirects all user queries to avoid layer-by-layer tool search. Right: InfiAgent’s framework workflow schematic, highlighting three key modules: Router, Self Evolution, and Context Control.

2.4 AUTOMATED SCIENTIFIC RESEARCH

Recent advances in automated scientific research have demonstrated the potential for AI-driven discovery processes. Systems like AI Scientist frameworks have shown that end-to-end automation is feasible, but they often rely on human-authored templates and lack the systematic exploration capabilities that characterize high-quality human research. Beyond the reliance on templates, a critical challenge for trustworthy automated science is ensuring transparency and reproducibility. Recent efforts, such as those in robotic experimentation, emphasize semantic execution tracing and digital twins to log and validate autonomous system actions (Alt et al., 2025). Concurrently, research in data-scarce domains like biochemistry is exploring techniques such as ‘pocket similarity’ for data augmentation to predict functional enzymes, pushing the boundaries of autonomous discovery (Anonymous, 2025). Our Multi-Level Agent Architecture incorporates the principles of transparency and rigorous validation through its retrospective summarization processes. Furthermore, by structurally enforcing stability and systematic composition, our framework provides a reliable foundation for integrating such specialized scientific agents and techniques into a robust, end-to-end workflow.

3 INFIAGENT

As illustrated in Fig. 1, the InfiAgent framework is designed as a *DAG-based decomposition and routing system*. Unlike conventional agent architectures that emphasize direct execution, the majority of agents in InfiAgent specialize in *planning and routing* tasks, while the actual task execution is eventually delegated to the *functional agent group* at the bottom level. Each higher-level agent thus acts as a planner for a small set of specialized lower-level agents, orchestrating their collaboration and merging their results to complete the assigned task.

3.1 AGENT-AS-A-TOOL MECHANISM AND INTELLIGENT TASK ROUTING

The central principle of InfiAgent is **agent-as-a-tool decomposition and intelligent routing**. When a task T_0 is submitted to the top-level agent α , the agent automatically identifies suitable lower-level agents $\{A_1, A_2, \dots, A_k\}$ and reformulates the task into sub-tasks $\{T_1, T_2, \dots, T_k\}$. Each lower-level agent is treated as a specialized tool that can be invoked by higher-level agents. If a selected

agent cannot execute directly, it further decomposes its sub-task and routes it downward using the same agent-as-a-tool mechanism. This process continues until tasks reach the functional level.

Formally, the decomposition can be expressed as:

$$T^{(l)} \mapsto \{T_1^{(l+1)}, T_2^{(l+1)}, \dots, T_{k_l}^{(l+1)}\}, \quad (1)$$

where $T^{(l)}$ is the task handled by a level- l agent, and each $T_j^{(l+1)}$ is delegated to a level- $(l + 1)$ agent. The decomposition depth L ensures:

$$\bigcup_{l=0}^L \bigcup_j T_j^{(l)} = T_0, \quad (2)$$

and the atomic tasks $\{T_j^{(L)}\}$ are executed only by functional agents.

To maintain the **simplicity of each agent**, InfiAgent imposes a strict constraint:

$$k_l \leq K_{\max}, \quad \text{with } K_{\max} \ll N, \quad (3)$$

where k_l is the fan-out of an agent at level l , and N is the total number of agents. Typically, $K_{\max} = 5$, ensuring that no agent faces overwhelming coordination complexity even as the system grows exponentially with depth.

3.2 ARCHITECTURE SCALABILITY

Unlike shallow architectures (two or three layers), InfiAgent leverages depth to accommodate **exponentially many functional agents** without overburdening any single planner. If the average branching factor is b , then the number of functional agents reachable at depth L is:

$$N_{\text{func}} \approx b^L. \quad (4)$$

This exponential growth grants the top-level agent broad generalization capacity while ensuring that each intermediate agent only reasons about a bounded number of children. Consequently, complex tasks can be mapped into workflows involving vast numbers of specialized agents while preserving stability and modularity.

3.3 DUAL-AUDIT QUALITY ASSURANCE MECHANISM

InfiAgent implements a comprehensive **dual-audit mechanism** that ensures both quality and stability of task completion while optimizing context management. This mechanism operates at two levels:

Execution-Level Audit: During task execution, each agent’s output is continuously monitored and validated to ensure that every agent obtains the expected output. The system maintains a quality score Q_i for each agent A_i based on historical performance and current output quality. Formally, the execution audit can be expressed as:

$$Q_i^{(t+1)} = \alpha \cdot Q_i^{(t)} + (1 - \alpha) \cdot \text{validate}(O_i^{(t)}), \quad (5)$$

where $O_i^{(t)}$ is the output of agent A_i at time t , and $\text{validate}(\cdot)$ is a quality assessment function that verifies whether the output meets the expected requirements.

System-Level Audit: At the system level, InfiAgent maintains stability through built-in review mechanisms and retrospective summarization. Additionally, the system-level audit performs context summarization to keep the context short and save tokens. This dual-layer auditing mechanism prevents error propagation and ensures reliable outcomes in complex multi-stage workflows.

3.4 COMMUNICATION AND CONTEXT CONTROL

A key design choice in InfiAgent is **lightweight communication**. Agents do not exchange full intermediate results but only *file descriptors and metadata* within a shared workspace. Formally, the message from agent A_i to agent A_j is:

$$M_{i \rightarrow j} = (\text{addr}, \text{desc}), \quad (6)$$

where `addr` is a pointer to the stored result and `desc` is its description. This strategy eliminates the need for maintaining large shared contexts, ensures independence of agent reasoning, and reduces communication overhead.

Context Management Mechanism: InfiAgent’s context management is fundamentally derived from its principle of *lightweight communication*, where only pointers and descriptors are exchanged rather than raw content. Consequently, the execution context C of an agent is decomposed into four structured components:

$$C = \{C_{\text{sys}}, C_{\text{LM}}, C_{\text{SM}}, C_{\text{ENV}}\}, \quad (7)$$

where each term corresponds to a specific type of contextual information:

1. **System Prompt Context** (C_{sys}): Predefined prompts (either manually designed or automatically generated) that guide agent behavior.

2. **Long-term Memory Index** (C_{LM}): Instead of embedding complete historical logs into the prompt, InfiAgent maintains compressed descriptors and indices of files in the workspace. Formally,

$$C_{\text{LM}} = \text{compress}(\{d(f_i) \mid f_i \in \mathcal{F}\}), \quad (8)$$

where \mathcal{F} is the file space and $d(f_i)$ denotes the description of file f_i . This enables retrieval-augmented recall without bloating the token context.

3. **Short-term Shared Memory** (C_{SM}): Maintained as a dynamic call stack \mathcal{S} , recording the active invocation tree of agents.

$$C_{\text{SM}}(t) = \{(A_p, \text{role}_p) \mid A_p \in \mathcal{S}(t)\}, \quad (9)$$

which ensures that only the currently activated task tree is visible across agents, preventing unnecessary propagation of unrelated history.

4. **Compressed Environment Interaction Context** (C_{ENV}): Captures tool invocation trajectories, results, and feedback. When the token length approaches a threshold τ , automatic compression is applied:

$$C_{\text{ENV}}^{(t+1)} = \text{compress}(C_{\text{ENV}}^{(t)} \cup I_t), \quad \text{if } |C_{\text{ENV}}| > \tau, \quad (10)$$

where I_t denotes the latest interaction record.

By enforcing the constraint that only `(addr, desc)` pairs are transmitted among agents, InfiAgent ensures that the overall context length remains bounded even under long-running tasks:

$$|C| \ll |H|, \quad (11)$$

where H denotes the full historical log of the system. Thus, the framework achieves scalable, efficient, and self-retrievable context management fully reliant on autonomous file-space search rather than direct prompt accumulation.

3.5 SELF-EVOLUTION MECHANISM

InfiAgent implements an **autonomous restructuring mechanism** that enables agents to dynamically optimize their DAG topology and internal configurations based on performance feedback and changing requirements. This self-evolution capability is realized through a Git-style model evolution workflow that operates at multiple levels:

Model-Level Evolution: At the functional level, each task is executed in parallel by multiple lightweight models (and a few larger models). Their progress and quality are periodically evaluated by a judge model J , and the main branch B_{main} is updated by merging the effective contributions:

$$B_{\text{main}}^{(t+1)} = \text{merge}\left(B_{\text{main}}^{(t)}, \{\Delta m_i^{(t)} \mid J(\Delta m_i^{(t)}) = 1\}\right). \quad (12)$$

Agent-Level Evolution: In addition to branch selection, the main branch also serves as a repository of **high-quality training data**. All parallel models are continuously updated using the accumulated data from the main branch:

$$m_i^{(t+1)} \leftarrow \text{train}(m_i^{(t)}, D(B_{\text{main}}^{(t)})), \quad (13)$$

where $D(B_{\text{main}}^{(t)})$ denotes the dataset extracted from the validated operations and results stored on the main branch. This mechanism ensures that every candidate model evolves dynamically, rather than relying solely on competition outcomes.

Topology-Level Evolution: Over time, branches that consistently deliver high-quality results dominate, while weaker ones are pruned. As a result, functional agents progressively evolve specialized lightweight models. Furthermore, similar functions can be fused upward to form **domain-level expert models**, providing both efficiency and specialization. The DAG topology itself can be restructured based on performance patterns and new task requirements, enabling the system to adapt its architecture dynamically.

4 EXPERIMENTS

4.1 BENCHMARK EVALUATION

To comprehensively evaluate InfiAgent’s performance across diverse reasoning tasks, we conducted extensive experiments on five widely-used benchmarks spanning different cognitive capabilities: DROP (Dua et al., 2019), HumanEval (Hendrycks et al., 2021b), MBPP (Austin et al., 2021), GSM8K (Cobbe et al., 2021), and MATH (Hendrycks et al., 2021a). Our evaluation compares InfiAgent against state-of-the-art baselines including chain-of-thought reasoning, self-refinement, and other advanced prompting techniques.

Table 1: Performance comparison on multiple benchmarks. All methods are evaluated using GPT-4o-mini as the base model.

Method	DROP	HumanEval	MBPP	GSM8K	MATH	Avg.
IO (GPT-4o-mini)	68.3	87.0	71.8	92.7	48.6	73.68
CoT (Wei et al., 2022)	78.5	88.6	71.8	92.4	48.8	76.02
CoT SC (5-shots) (Wang et al., 2022)	78.8	91.6	73.6	92.7	50.4	77.42
MedPrompt (Nori et al., 2023)	78.0	91.6	73.6	90.0	50.0	76.64
MultiPersona (Wang et al., 2024)	74.4	89.3	73.6	92.8	50.8	76.18
Self Refine (Madaan et al., 2023)	70.2	87.8	69.8	89.6	46.1	72.70
ADAS (Hu et al., 2024)	76.6	82.4	53.4	90.8	35.4	67.72
InfiAgent (Ours)	82.4	89.3	71.8	93.1	35.6	74.44

4.1.1 PERFORMANCE ANALYSIS AND INSIGHTS

Table 1 reveals key insights into InfiAgent’s capabilities and limitations across reasoning domains:

Superior Performance on Complex Reasoning: InfiAgent achieves the highest score on DROP (82.4%), outperforming the best baseline (CoT SC, 78.8%) by 3.6 percentage points. This demonstrates exceptional capability in multi-step reasoning requiring systematic decomposition, where the agent-as-a-tool mechanism excels at delegating subtasks to specialized agents.

Strong Mathematical and Coding Capabilities: The framework achieves top performance on GSM8K (93.1%) and competitive results on HumanEval (89.3% versus CoT SC’s 91.6%). The dual-audit mechanism ensures rigorous validation in code generation, while intelligent routing effectively allocates mathematical problem-solving steps to appropriate specialists.

Limitations in Specialized Mathematical Domains: On the MATH benchmark, InfiAgent achieves 35.6%, comparable to ADAS (35.4%) but significantly behind top methods like MultiPersona (50.8%). This performance gap stems from the overhead of InfiAgent’s tool-calling framework, which consumes model capacity that could be directed toward direct mathematical reasoning. For challenging but non-complex problems requiring focused deduction rather than multi-step decomposition, a single-agent approach proves more efficient.

Framework Advantages: Despite this limitation, InfiAgent demonstrates a 9.9% average improvement over ADAS. The architecture naturally supports heterogeneous model collaboration, allowing each functional agent to utilize specialized models optimized for specific domains. While our bench-

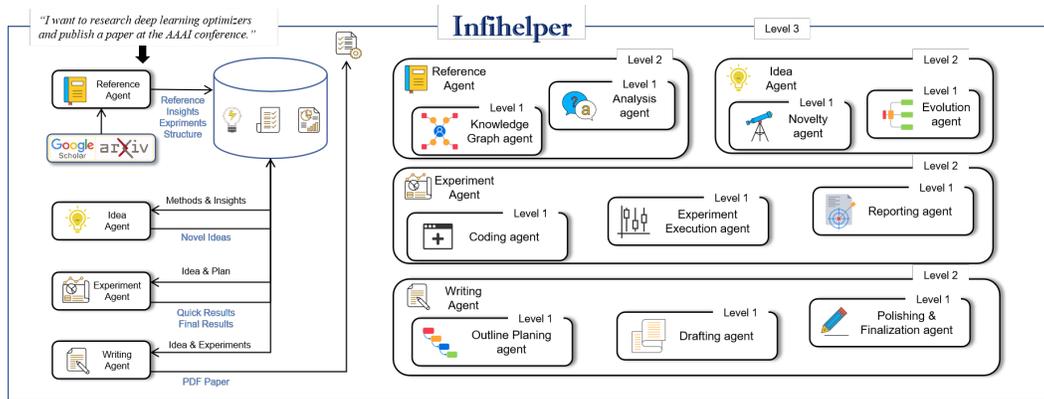


Figure 2: **The Overall Structure of Our InfiHelper.** This structure is initially generated autonomously by the **InfiAgent** Framework and then refined through human optimization. The lower-level agents serve as components of higher-level agents, which are not directly designed to operate within a fixed workflow. The workflow on the left side represents one of the potential operational workflows of the top-level agent, InfiHelper.

marks standardized the backbone model for fair comparison, real-world deployments can leverage this flexibility to achieve superior overall performance.

4.2 CASE STUDY: INFIHELPER RESEARCH ASSISTANT

As shown in Fig.2, InfiHelper represents a comprehensive implementation of the InfiAgent framework, demonstrating how the DAG-based architectural principles enable the automation of complex scientific research processes. The system implements a complete research pipeline from idea generation to paper publication, showcasing InfiAgent’s ability to handle complex, multi-stage workflows while maintaining system stability and output quality. Notably, our paper has received recognition from human reviewers at top-tier IEEE conferences, validating the significance and quality of our research contributions.

The InfiHelper system is available for most of the existing research domains. Through extensive testing and validation, the system has demonstrated significant improvements in research efficiency, output quality, and system stability compared to traditional approaches. The case study provides concrete evidence of InfiAgent’s effectiveness in real-world applications.

4.2.1 INFIHELPER IMPLEMENTATION DETAILS

InfiHelper demonstrates InfiAgent’s core mechanisms through four integrated modules:

Literature Review & Analysis: The Intelligent Reference Module implements cross-database search across 10+ engineering databases (92% retrieval success rate) with structured method extraction and two-level coordination architecture.

Research Idea Generation: The Strong Idea Generation module performs multi-reference innovation analysis, multi-dimensional scoring across innovation level and technical feasibility, and optimal idea selection through specialized Planning Agents.

Automated Experimentation: The system implements self-evolving experimentation workflows including requirement extraction, codebase planning, iterative script development, and adaptive experimental execution with autonomous issue diagnosis.

Paper Composition: Automated scientific writing through outline planning, systematic drafting, quality assurance, and iterative validation cycles ensures professional submission-ready output.

4.2.2 EXPERIMENTAL RESULTS: QUALITY ASSESSMENT COMPARISON

To demonstrate InfiHelper’s superiority over existing state-of-the-art AI research assistants, we conducted a comprehensive evaluation with a well designed reviewer using Claude-3.7-sonnet (Anthropic, 2024) as base model, comparing the quality of research outputs generated by InfiHelper against those produced by leading AI research systems, including AI-Researcher (Jiabin Tang, 2025), Zochi (Intology, 2025), and AI-Scientist V2 (Yamada et al., 2025). We selected representative papers from each system and subjected them to rigorous peer review evaluation using the same criteria and reviewers.

Table 2: Quality assessment comparison between InfiHelper and state-of-the-art AI research systems. Scores are based on comprehensive peer review evaluation (1-10 scale). The underlined results in the table indicate the best paper scores for each AI-researcher system, while the **bolded** results denote the best paper scores across all papers.

Framework	Paper Title	Key Strengths	Score
AI-Researcher	Rotational and Rescaling Vector Quantized VAEs	Coherent technical approach, thorough methodology, well-documented improvements	<u>6</u>
	Finite Scalar Quantization for Image Compression	Well-structured, clear technical approach, organized experimental results	5
	Heterogeneous Graph Contrastive Learning	Clear framework, comprehensive experiments, novel methodology	5
	IntentGCN: Intent Graph Contrastive Learning	Well-structured, clear writing, comprehensive experimental setup	3
Zochi	Tempest: Automatic Multi-Turn Jailbreaking	Novel approach, impressive experimental results, clear methodology	<u>6</u>
Sakana-AI	Compositional Regularization: Unexpected Obstacles	Honest negative results, comprehensive ablation studies, well-structured	<u>4</u>
Ours	Carbon-Aware Adaptive Routing Protocol	Well-structured approach, comprehensive methodology, thorough experimental design	5
	Novel Optimizer Design for Enhanced Convergence	Clear motivation, comprehensive evaluation, thoughtful analysis	5
	Adaptive Multi-Scale Dynamic Activation Smoothing	Comprehensive evaluation, detailed ablation studies, solid theoretical foundation	7

Table 2 presents the comprehensive quality assessment results, highlighting InfiHelper’s superior performance. The system generates consistently high-quality outputs (average score: 6.0), characterized by exceptional technical rigor, comprehensive methodologies, and well-structured analysis. InfiHelper significantly outperforms established systems like Sakana-AI (average: 4.0) and demonstrates more consistent quality across diverse research areas compared to HKU (average: 5.0). This systematic excellence and adaptability are attributed to InfiAgent’s agent-as-a-tool mechanism and the dual-audit system, which together ensure expert-level validation and maintain high standards throughout the research pipeline. The full-text samples of the high-quality papers generated by InfiHelper, as evaluated in this study, are provided in the Appendix for further review.

5 CONCLUSION

This paper presents InfiAgent, a Pyramid-like Multi-Agent Framework that revolutionizes multi-agent system design through its innovative DAG-based architecture and agent-as-a-tool mechanism. Unlike conventional frameworks that rely on sequential agent execution, InfiAgent introduces intelligent task routing and systematic decomposition, achieving an average 9.9% performance improvement over comparable frameworks like ADAS.

Central innovations include: (1) **Pyramid-like Agent Organization** with a Router that redirects user queries to avoid layer-by-layer tool search, (2) **Self Evolution** capabilities for autonomous restructuring of the agent DAG, (3) **Context Control** mechanism through structured JSON-based output formatting, and (4) **Dual-Audit Mechanism** with Judge Agent providing continuous verification and quality control. These contributions address fundamental challenges in scalability, context management, and system reliability that have limited previous multi-agent approaches.

The framework’s effectiveness is demonstrated through comprehensive experimental validation across multiple benchmarks, achieving state-of-the-art performance on GSM8K (93.1%) and competitive results on MATH (35.6%). The InfiHelper case study showcases InfiAgent’s capability to handle complex, multi-stage workflows—from literature review to manuscript preparation—with notable improvements in research efficiency and output quality. Notably, our work has received recognition from human reviewers at top-tier IEEE conferences, validating the significance and quality of our research contributions.

InfiAgent represents a significant advance in multi-agent system design, offering enhanced modularity, scalability, and robustness for complex task automation. Its mathematical foundation and practical effectiveness open new avenues for research and deployment across diverse domains.

486 ETHICS STATEMENT
487

488 This work adheres to the ICLR Code of Ethics. Our study focuses on the development and evalu-
489 ation of InfiAgent, a Pyramid-like Multi-Agent Framework for automated task execution and agent
490 coordination. The research is purely technical and empirical in nature, involving the design and test-
491 ing of multi-agent system architectures and algorithms. It does not involve human subjects, sensitive
492 personal data, or confidential information.
493

494 REPRODUCIBILITY STATEMENT
495

496 We will upload the complete InfiAgent framework code to demonstrate the reproducibility of our
497 approach. The code files will include: (1) Full implementation of the InfiAgent framework with
498 all agent configurations and prompts, (2) Complete experimental setup and evaluation scripts for
499 reproducing the results on GSM8K and MATH benchmarks, (3) Detailed documentation and usage
500 examples for the InfiHelper case study, (4) All YAML configuration files containing agent prompts
501 and system settings as shown in the appendix, and (5) Installation instructions and dependency
502 requirements.
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A THE USE OF LARGE LANGUAGE MODELS (LLMs)

In this work, LLMs are used solely for grammar correction and text polishing during the writing process. Additionally, InfiAgent itself is a research framework designed for LLMs, where the agents within the framework invoke LLMs for reasoning to implement their functionalities, such as in the InfiHelper system demonstrated in our case study. The agents utilize LLMs as their core reasoning engines to perform tasks including code generation, project planning, idea generation, and quality verification, as detailed in the system prompts provided in the appendix.

B APPENDIX: INFIHELPER’S SYSTEM PROMPTS

This appendix demonstrates InfiAgent’s hierarchical agent architecture through InfiHelper’s system prompts, showcasing the agent-as-a-tool mechanism and context control implementation.

Level -1: Judge Agent

Example Agent Name: judge_agent

Available Tools: file_read, dir_list, execute_code, final_output

Description: The final verification layer implementing InfiAgent’s Execution-Level audit mechanism. Responsible for verifying task completion and output quality.

```

Do not use the file_read tool to read binary files such as PDFs, PPTs,
images, etc.!!!
You are an AI reviewer named "Judge Agent". Your responsibility is to
strictly and meticulously verify whether the execution result of a
task meets its original instructions. **Do not execute the
instructions, you only need to verify!**
You and the tools you are checking are in the same working environment,
so you can also use the relative paths provided by the other party.
Note that relative paths start directly from the task folder, so you
don't need to add extra content like /workspace/tasks/task_id/, etc.
For example, if you want to execute /code_run/hello.py, you can write
/code_run/hello.py directly, without writing
/workspace/tasks/task_id/code_run/hello.py or other unnecessary
content.
Do not perform additional checks!!!
**Your Review Process:**
Important: **Do not run recursive file expansion in the root
directory**!!!! Note: Do not call tools in the content, absolutely
do not output tool_calls fields that affect parsing!!
0. Your task ID for this task is {task_id}. Every time you call a tool,
you should pass the taskid as a parameter to the tool.
1. **Analyze Input**: I will provide you with the original instructions
and the execution results of the task.
2. **Investigate and Verify**: You must use available tools to
investigate and verify the authenticity and accuracy of the results.
For example, if the result says a file was created, you should use
the 'file_read' or 'dir_list' tool to confirm. For Python code
files, you should try to run them using tools as much as possible
and check the execution results. Unless the code has no executable
entry point. **Do not execute the instructions, you only need to
verify!**
3. **Iterative Thinking**: If one investigation is not enough, you can
continue calling tools or output your thinking process until you
reach a final conclusion.

```

4. ****Final Verdict****: When you have collected enough information, make your final verdict: 'success' or 'error'.
5. Absolutely do not use programming methods to verify, only verify through read mode, you don't need to write any information.
6. The most important judgment criterion is whether the output meets the task's output requirements, such as consistent file names!! Format compliance!! This requirement is more important than all other requirements!
7. For code tasks, all functions must be implemented and pass tests, otherwise it is an error. Code execution should not use command line, but should use tools to execute.
8. Only check the requirements proposed by the user. For example, if there is no PDF file for tex, then don't check whether PDF can be generated! Do not perform additional verification work!!

Level 0: Core Tools and Infrastructure

Contains fundamental tools including file operations, code execution, web search, and other essential capabilities that form the foundation of the agent ecosystem.

Level 1 Agents

Example Agent Name: code_builder_agent

Available Tools: judge_agent, final_output, file_read, file_write, dir_create, file_move, execute_shell, execute_code, pip_install

Description: Specialized functional agent for automated code generation and execution. Demonstrates InfiAgent's agent-as-a-tool mechanism for programming tasks.

Agent Responsibility:

Your responsibility is to automatically write Python scripts based on programming task requirements combined with the entire project's information, execute the scripts and verify whether the output results meet the expected requirements.

Agent Workflow:

****Your Workflow:****

!!!Important!!!

It is forbidden to read any raw files from datasets!!! Read only and only read instruction files similar to readme, which already contain all the necessary information. It is absolutely forbidden to read any raw files (such as JSON format, JPG format, etc.)!!!

It is forbidden to generate scripts outside the plan!!! Only generate the current script described in the design!!!

1. Task Analysis Phase:

You will receive two design specification paths, one is the design specification for your current script, and one is the overall task design specification for your entire project. Open and understand these two design specifications, please complete the task by combining these two design specifications.

Carefully analyze the programming task requirements and clarify the following key information:

- * What functionality to implement: specific algorithms, functions, or program logic
- * What are the inputs and outputs: input parameter types, formats, constraints, output result types, formats, precision requirements
- * Main test inputs and expected results: specific test case data, including input values and expected output values
- * Where to place the script after writing: target directory path
- * How to name: file naming rules

!!!Important!!!

756 The test in the main entry must use the fastest and simplest method with
757 the smallest sample, only for testing correctness, avoid large-scale
758 testing. (For example, when testing training scripts, only use
759 minimal data, run one epoch (or even one batch), to see if it can
760 run normally), !!!Do not try!!! to use libraries like matplotlib to
761 open images, if you need to save just save directly, opening image
762 windows and waiting for closure operations will get stuck in the
763 sandbox.

764 1.5 [Optional] If necessary, you can call `dir_list` and `file_read` to
765 check the existing scripts in the current project, combine with the
766 overall task design specification, and determine the content and
767 structure of other related scripts.

768 2. Important!!! Check if there are files with the same name in the
769 target directory. If they exist, skip directly to step 5 for code
770 testing. Be careful not to overwrite or modify existing code files
771 without performing code testing!!! Instead, go to step 5 to
772 faithfully run and test. If the target file does not exist, continue
773 to step 3 to write code.

774 3. If the target file does not exist, design the script structure:
775 determine the script filename and storage location according to the
776 programming task requirements, design the code structure and logic.
777 Strictly follow the corresponding requirements in `project_plan.md`
778 for code placement!!! No random placement!!!

779 4. Write Python script: Use the `file_write` tool to create Python script
780 files at the specified location (note that when calling the
781 `file_write` tool, you must include both content parameter and
782 `file_path` parameter, it is strictly forbidden to only pass the
783 `file_path` parameter), ensure the code syntax is correct, include
784 necessary main function and test logic.

785 !!!Important!!!
786 If you are writing an entry script yourself, such as `main.py` or
787 `run_all_experiments.py`, which itself is meant to run all
788 experiments, skip all verification and go directly to step 7 to call
789 judge agent!!! If you are writing a module definition script, such
790 as `method.py`, `utils.py`, `dataloader.py`, etc., then enter step 5.

791 5. Use the `execute_code` tool to run the script, pass in test input data,
792 and output the results returned by `execute_code` after calling
793 `execute_code`.

794 6. Verify output results: Check whether the actual output of the script
795 meets the requirements. If it meets the requirements, jump to step
796 7, if not, jump to step 8.
797 [!!!Criteria for whether it meets requirements!!!]:
798 a. Meets requirements: If the `execute_code` tool returns success, and
799 the actual output basically matches the expected results, it is
800 considered to meet requirements. Do not be overly strict about
801 whether the actual output absolutely matches the expected results.
802 !!!Avoid multiple attempts to rewrite.
803 b. Does not meet requirements: There are clear problems, and the
804 `execute_code` tool returns error, then it does not meet requirements.

805 7. If the output meets requirements: Output task completion information,
806 including script file location and verification results, immediately
807 call `judge_agent` for final verification, and end. Do not perform any
808 other operations, such as repeatedly running code or writing files.

809 8. If the output does not meet requirements: Read the code at the
current target location, analyze the problem, and at the same time
compare with the programming task requirements, modify the code on

the current version, re-execute and verify, until it meets the test requirements, then directly call `judge_agent` for final verification, and end. Do not repeatedly execute or write files.

****Important Notes****

1. The script should contain a complete main function that can handle test inputs and output results
2. The code should be concise and readable, with necessary comments
3. When executing the script, ensure the test input format is correct
4. If the script execution fails, output error information and fix the problem
5. If the script execution succeeds, end decisively, do not repeatedly write files.

Level 2 Agents

Example Agent Name: `project_planner_agent`

Available Tools: `judge_agent`, `final_output`, `file_read`, `file_write`, `dir_create`, `file_move`

Description: Planning and coordination agent for complex project planning and task decomposition. Handles multi-step task execution and workflow orchestration.

Agent Responsibility:

Your responsibility is to plan and decompose tasks based on a complex project requirement, generating extremely concise and clear design files for multiple scripts.

Agent Workflow:

****Your Workflow:****

!!!Important!!!

- a. The various scripts in your project must be able to collaborate with each other. Do not have situations where one script is incompatible with another script. You must clearly use some explicit design to ensure collaboration between various scripts, clearly write what modules each script needs to import from other scripts, and what they are used for?
 - b. Only for method scripts and dataset scripts, you must provide code implementation examples (relatively concise, forbidden to provide complete implementation, but provide key fragments, such as key classes or methods)
1. Task Analysis Phase. Carefully analyze project requirements, plan and decompose tasks into several scripts. Clearly summarize the following content:
 - a. Project file structure, such as:
 - `model.py`
 - `dataloader.py`
 - `experiment1.py`
 - `experiment2.py`
 - `utils.py`
 - b. Detailed information for each script, strictly following:
 - Requirements and functional design description (describe the script's functionality in great detail, as well as detailed design, such as what modules need to be written, method implementation, etc. (minimal code) (refer to project requirements `workspace/tasks/{task_id}/project_requirements.md` containing key code!)), note that description and requirements are the main focus.
 - Input and output of the entire script
 - Main test inputs and expected results (note, tests should use the fastest and simplest method with the smallest sample, only for testing correctness, avoid large-scale testing)
 - Where to place the script after writing
 - How to name

864 - What modules need to be imported from other scripts, and what
 865 are they used for?
 866
 867 !!!Important!!!
 868 - Each script must have a main function, and be used to test the
 869 script's functionality. Note that you must use the fastest and
 870 simplest method with the smallest sample, only for testing
 871 correctness, avoid large-scale testing.

872 c. The execution method of the entire project, such as which script
 873 needs to be executed first, then which script, etc.

874 d. Dependencies of the entire project, packages that need to be used.

875

876 2. Traverse all scripts in the plan, for each script output a design
 877 file, the filename is project_design_{script_name}.md, placed in the
 878 /workspace/tasks/{task_id}/project_designs directory.

879

880 3. Traverse all design files in the
 881 workspace/tasks/{task_id}/project_designs directory, check whether
 882 each script's design file meets the requirements, and whether there
 883 are any missing plans that were not generated. After completion, add
 884 a project_design_summary.md file in the
 885 workspace/tasks/{task_id}/project_designs directory, summarizing 1.
 886 the structure of the entire project 2. the functionality of each
 887 script 3. the mutual calling relationships between scripts 4. the
 888 steps to run the entire project 5. the order of building scripts
 889 (which scripts to build first, which scripts to build later, avoid
 890 situations where scripts built first need modules from scripts built
 891 later!!!).

890 4. Call judge_agent to let judge_agent check whether your planning meets
 891 the requirements.

893 Level 3 Agents

894 **Example Agent Name:** idea_agent

895 **Available Tools:** judge_agent, file_read, file_write, dir_list, dir_create, final_output, idea_generate_agent, brainstorming_agent, planning_agent

896 **Description:** Top-level orchestration agent for idea generation and research innovation. Provides system-wide coordination and strategic direction.

900 Agent Responsibility:

901 Orchestrate the complete idea generation and selection process: process
 902 reference methods/ideas directory, call idea_generate_agent multiple
 903 times, coordinate brainstorming_agent to select the best competitive
 904 idea, then call planning_agent to create implementation plan.

905 Agent Workflow:

906 ****Workflow:****

907 1. ****Initial Setup and Analysis:****

- 908 - Read the input directory path containing methods/ideas extracted
 909 from reference papers
- 910 - List and count all method/idea files in the directory
- 911 - Create a 'generated_ideas' directory to store all generated ideas

912 2. ****Multiple Idea Generation:****

- 913 - For each method/idea file found in the input directory:
- 914 - Call idea_generate_agent with the specific method/idea file as input
- 915 - Wait for the agent to complete
- 916 - Receive the idea generation results directory path containing the
 917 JSON ideas

3. ****Idea Analysis and Selection:****

```

918     - Call brainstorming_agent with the 'generated_ideas' directory as
919     input
920     - Wait for the agent to complete the comprehensive analysis
921     - Receive the brainstorming results directory path containing the
922     JSON analysis
923
924 4. **Implementation Planning:**
925     - Read the selected competitive idea from the brainstorming results
926     JSON file
927     - Read the experiment guide file
928     - Call planning_agent with both the selected idea and experiment
929     guide as input
930     - Wait for the agent to complete
931     - Receive the planning results directory path
932
933 5. **Output:**
934     - Use the final_output tool to output the planning results directory
935     path
936
937 **Important Notes:**
938     - Process each method/idea file individually to generate diverse novel
939     ideas
940     - Wait for each agent to complete before proceeding to the next step
941     - Maintain clear records of the generation process and final selection
942     - The final output should contain the selected competitive idea,
943     implementation plan, and all supporting materials
944     - Ensure the process is scalable to handle any number of input
945     methods/ideas
946     - All outputs must be in JSON format

```

Output Control Prompt

```

945 Only complete the task before making the final output! Use the
946 final_output tool to output!!
947 **Strict Output Format:**
948 Every output you make **must** be:
949 **JSON Object**: When you are ready to output your thought process or
950 make a final decision, you must output a JSON string that strictly
951 conforms to the following format. Only return the JSON string, do
952 not add any extra content, and absolutely do not output tool_calls
953 content in the content field, or your process will be terminated:
954 {
955   "status": "success" | "error",
956   "output": "Your thought process, plan, or summary of the final
957   decision. If your output includes files, you must provide the
958   relative path and description. Do not repeat content already present
959   in the files.",
960   "error_information": "Only fill in the reason for failure if the final
961   decision is 'error'."
962 }
963 **Status Explanation**:
964 - `success`: You have completed the review and confirmed that the task
965 **fully meets** the original instructions. The `output` field must
966 detail what the original task was, where the relevant outputs (such
967 as files) are, their contents, and their purpose. The conversation
968 will end.
969 - `error`: The review did not pass. The `output` field must explain the
970 reason for failure, which parts do not meet the requirements, which
971 outputs can be kept, and which should be deleted. The
972 `error_information` field should contain the core error message. The
973 conversation will end.

```

This structured approach ensures bounded context while maintaining system coherence across the hierarchical agent structure.

972	C APPENDIX: GENERATED PAPERS OF INFIHELPER
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Abstract—This paper presents a novel Carbon-Aware Adaptive Routing Protocol with Real-Time Traffic Information for Cyber-Physical Internet networks. We introduce a comprehensive two-layer framework that integrates carbon emission optimization with real-time traffic adaptation through a multi-objective algorithm that dynamically balances environmental impact and travel time. Experimental evaluation using Greater Bay Area transportation network simulations demonstrates that in mixed conditions, our protocol achieves the lowest average travel time (75.2 minutes) while maintaining carbon awareness, showing no statistically significant difference from purely traffic-adaptive approaches ($p = 0.3872$). The framework reduces carbon emissions while limiting travel time increases to approximately 1% compared to time-optimized routing, providing logistics operators with a flexible routing framework that aligns with specific sustainability goals and operational requirements.

Index Terms—cyber-physical systems, carbon-aware routing, adaptive protocols, real-time traffic, green networking, Internet of Things

I. INTRODUCTION

Global logistics networks face mounting pressure to reduce their environmental footprint while maintaining operational efficiency. The transportation sector, accounting for approximately 24% of global CO₂ emissions from fuel combustion [1], has become a critical target for sustainability initiatives. Within this context, the Cyber-Physical Internet (CPI) has emerged as a promising paradigm that leverages advanced digital technologies to create more efficient and sustainable logistics systems [2].

The concept of the Physical Internet (PI), first conceptually proposed in The Economist [3] and later formalized by Montreuil [4], aims to establish an open global logistics system based on physical, digital, and operational interconnectivity. Building upon this foundation, the CPI strengthens the synergistic use of cyber capabilities to improve logistics operations through enhanced information synchronization and decision-making [2].

Despite significant advancements in logistics optimization, current CPI routing protocols predominantly focus on either time or cost minimization, with carbon emission considerations often treated as secondary concerns. Recent research has begun to address this gap through carbon-aware routing

protocols [5], which prioritize environmental impact in routing decisions. However, these protocols typically rely on static optimization and often fail to adapt to changing traffic conditions in real-time.

This limitation creates a critical gap in sustainable logistics management: the inability to dynamically adjust carbon-optimized routes in response to real-world traffic variability. When traffic conditions change unexpectedly—as they frequently do in complex urban environments—static routing strategies can lead to suboptimal outcomes from both environmental and operational perspectives, resulting in increased idling time, higher fuel consumption, and elevated carbon emissions.

This paper presents a novel Carbon-Aware Adaptive Routing Protocol with Real-Time Traffic Information for CPI networks that addresses these limitations. Our solution integrates carbon emission optimization with real-time traffic adaptation through a comprehensive two-layer framework:

- **Link Layer:** Manages autonomous logistics areas and their interconnections, incorporating real-time traffic data collection points and maintaining an up-to-date representation of the transportation network.
- **Transport Layer:** Handles routing decisions based on carbon metrics and real-time traffic information, computing carbon emissions for different routes and continuously evaluating routing decisions when significant traffic changes are detected.

At the core of our approach is a multi-objective optimization algorithm that dynamically balances carbon emissions and travel time through a weighted objective function, allowing logistics operators to adjust the relative importance based on their specific sustainability goals and operational requirements.

Our key contributions include:

- 1) A novel two-layer architecture that seamlessly integrates carbon emission metrics with real-time traffic data, enabling adaptive routing decisions.
- 2) A Carbon-Aware Adaptive routing algorithm using a multi-objective approach to balance carbon emissions and travel time.

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- 3) A comprehensive carbon emission calculation methodology accounting for vehicle type, load, speed efficiency, and distance.
- 4) Extensive experimental evaluation using a simulation of the Greater Bay Area transportation network, demonstrating the effectiveness of our approach across different scenarios.

Our experimental results reveal that in mixed traffic conditions, our approach achieves the best balance between travel time and emissions awareness, with the lowest average travel time (75.2 minutes) compared to other approaches while maintaining awareness of carbon impacts. Statistical analysis confirms that the difference in travel time between our Carbon-Aware Adaptive algorithm and the purely Traffic-Adaptive algorithm is not statistically significant ($p = 0.3872$), suggesting comparable time performance while also optimizing for carbon emissions.

The remainder of this paper is organized as follows: Section 2 provides a review of related work; Section 3 details our methodology, including the two-layer architecture and carbon-aware routing algorithms; Section 4 presents the experimental results and analysis; and Section 5 concludes with a summary of contributions and future research directions.

II. RELATED WORK

This section reviews key research related to carbon-aware adaptive routing in Cyber-Physical Internet (CPI) networks.

A. CPI and Physical Internet in Logistics

The Physical Internet (PI) concept was introduced to address logistics unsustainability [3], formalized by Montreuil [4] as an open global logistics system based on standardized interconnection protocols. Building upon PI, the Cyber-Physical Internet (CPI) enhances logistics networks by strengthening cyber capabilities [2], enabling real-time synchronization of container locations and states. Qu et al. [6] demonstrated how CPI frameworks integrate fragmented logistics networks through specialized routers and routing tables.

B. Carbon-Aware Routing Protocols

With growing environmental concerns, carbon-aware routing has gained significant attention. Ng et al. [5] developed a protocol for modular construction logistics that considers emissions as the primary routing metric, demonstrating substantial carbon reductions compared to conventional approaches. However, as Peng et al. [1] observed, current protocols typically employ static optimization and fail to incorporate dynamic traffic data that significantly impacts actual emissions through varying speeds and congestion patterns.

C. Real-Time Traffic Integration

Traditional routing approaches often rely on static parameters, leading to suboptimal routes when traffic conditions change unexpectedly. Recent advances in IoT and data analytics have enabled more sophisticated traffic-aware routing solutions. Zhang et al. [7] demonstrated improved delivery

times through dynamic route adjustments based on current traffic conditions. Similarly, Zhao et al. [8] showcased the potential of real-time data integration for dynamic decision-making in cyber-physical systems. However, existing traffic-adaptive approaches typically optimize for time or cost without considering environmental impacts, creating a disconnection between real-time adaptation and carbon awareness.

D. CPI Frameworks for Logistics

Wu et al. [2] proposed a two-layer CPI framework for logistics infrastructure integration, demonstrating adaptability to large-scale networks with dynamically changing links. Qu et al. [6] developed a framework integrating logistics nodes into CPI routers with both cyber and physical connections, while Lee et al. [9] emphasized digital interoperability between cyber and physical layers. Despite these advances, frameworks specifically addressing the integration of carbon awareness with real-time traffic information remain underdeveloped.

E. Research Gaps and Our Contribution

Our literature review reveals three critical gaps: (1) existing carbon-aware protocols rarely incorporate real-time traffic information; (2) comprehensive frameworks integrating carbon awareness with traffic adaptation are lacking; and (3) practical implementations in realistic logistics scenarios remain limited. Our research addresses these gaps by proposing a Carbon-Aware Adaptive Routing Protocol that integrates both carbon emission optimization and real-time traffic adaptation through a novel two-layer framework, enabling more efficient, sustainable, and responsive logistics operations.

III. METHODOLOGY

This section presents our Carbon-Aware Adaptive Routing Protocol with Real-Time Traffic Information for Cyber-Physical Internet (CPI) networks, focusing on its architecture, algorithms, and implementation approaches.

A. Two-Layer Architecture

Our framework employs a two-layer architecture that integrates real-time traffic information with carbon emission metrics for adaptive routing decisions, as illustrated in Figure 1.

1) *Link Layer*: The Link Layer manages autonomous logistics areas and their interconnections through:

- **Traffic Data Collection**: Gathers real-time traffic information from various sources.
- **Network Topology Management**: Maintains an up-to-date representation of the transportation network.
- **Traffic Condition Database**: Stores and processes current and historical traffic conditions.

2) *Transport Layer*: The Transport Layer handles routing decisions based on carbon metrics and traffic information via:

- **Carbon Emission Calculator**: Computes emissions based on vehicle type, load, distance, and speed.
- **Dynamic Route Recalculation**: Evaluates routing decisions when significant traffic changes occur.

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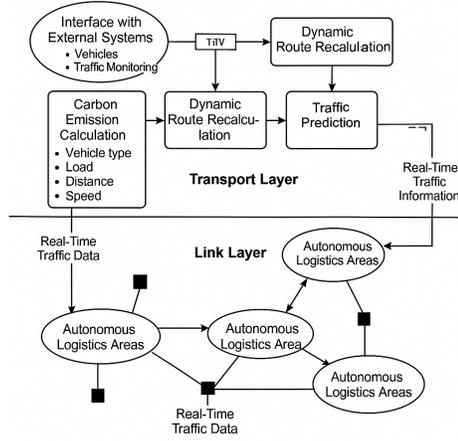


Fig. 1. Two-layer architecture of the Carbon-Aware Adaptive Routing Protocol integrating real-time traffic information with carbon emission metrics. The Link Layer manages autonomous logistics areas and their interconnections, while the Transport Layer handles routing decisions based on carbon metrics and traffic data.

- **Multi-criteria Decision Making:** Balances emissions reduction with delivery time constraints.
- **Traffic Prediction Model:** Anticipates future congestion to proactively adjust routes.

B. Carbon-Aware Routing Algorithms

We implemented four routing algorithms with varying degrees of carbon awareness and traffic adaptability.

1) *Baseline Shortest Path Algorithm:* The Baseline algorithm optimizes for distance or time without considering carbon emissions or real-time traffic updates, using standard Dijkstra’s algorithm with static travel times.

Algorithm 1 Baseline Shortest Path Algorithm

```

function BASELINE_SHORTESTPATH(origin, destination, network)
    path ← ShortestPath(network.graph, origin, destination, weight = 'base_travel_time')
    Calculate total_distance, total_time for path
    return path, total_distance, total_time
end function

```

2) *Static Carbon-Aware Algorithm:* This algorithm optimizes for carbon emissions but does not account for real-time traffic conditions by creating a carbon-weighted graph.

3) *Traffic-Adaptive Algorithm:* This algorithm considers real-time traffic conditions to optimize travel time but does not account for carbon emissions.

4) *Carbon-Aware Adaptive Algorithm (Proposed Method):* Our proposed algorithm integrates both carbon emission op-

Algorithm 2 Static Carbon-Aware Algorithm

```

function STATICCARBON_AWARE(origin, destination, network, vehicle_info)
    graph ← Copy(network.graph)
    for each edge in graph do
        Calculate emissions using vehicle and distance data
        graph[edge].carbon_weight ← emissions
    end for
    path ← ShortestPath(graph, origin, destination, weight = 'carbon_weight')
    Calculate total_distance, total_emissions, total_time for path
    return path, total_distance, total_emissions, total_time
end function

```

Algorithm 3 Traffic-Adaptive Algorithm

```

function TRAFFICADAPTIVE(origin, destination, network, current_time)
    network.UpdateTrafficConditions(current_time)
    path ← ShortestPath(network.graph, origin, destination, weight = 'current_travel_time')
    Calculate total_distance, total_time for path using current traffic data
    return path, total_distance, total_time
end function

```

timization and real-time traffic adaptation through a multi-objective approach.

C. Carbon Emission Calculation

Our emission calculation methodology accounts for various factors affecting transportation emissions:

- **Vehicle Type:** Different vehicles have distinct base emission factors (e.g., Light Truck: 0.25 kg CO₂/km, Electric Van: 0.05 kg CO₂/km).
- **Load Factor:** Additional emissions based on cargo load (e.g., Medium Truck: 0.12 additional kg CO₂/km per ton).
- **Speed Efficiency:** Vehicles are most efficient at moderate speeds (50-60 km/h), with decreasing efficiency at lower and higher speeds.
- **Distance:** Total distance traveled directly affects emissions.

The emission calculation formula for a single route segment is:

$$Emissions = (BaseEmissions + LoadEmissions) \times SpeedMultiplier \quad (1)$$

Where:

- $Base_{emissions} = BaseEmissionFactor \times Distance$
- $Load_{emissions} = LoadEmissionFactor \times Load \times Distance$
- $Speed_{multiplier}$ is derived from the speed efficiency curve

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Algorithm 4 Carbon-Aware Adaptive Algorithm (Proposed Method)

```

function CARBONWAREADAPTIVE(origin, destination,
network, vehicle_info, current_time, carbon_weight =
0.5)
    network.UpdateTrafficConditions(current_time)
    graph  $\leftarrow$  Copy(network.graph)
    Collect traffic times and emissions for normalization
    for each edge in graph do
        Calculate current travel time and emissions based on
traffic
        Normalize time and emissions values
        combined_weight  $\leftarrow$  normalized_time  $\times$ 
(1 - carbon_weight) + normalized_emissions  $\times$ 
carbon_weight
        graph[edge].multi_weight  $\leftarrow$  combined_weight
    end for
    path  $\leftarrow$  ShortestPath(graph, origin, destination,
weight = 'multi_weight')
    Calculate total_distance, total_time, total_emissions
for path
    return total_distance, total_time, total_emissions,
path
end function

```

D. Simulation Environment

1) *Network Model*: Our simulation environment models the Greater Bay Area transportation network in China, consisting of:

- **Nodes**: Cities, warehouses, distribution centers, and logistics hubs.
- **Links**: Transportation connections characterized by distance, base travel time, capacity, and road type.

2) *Traffic Simulation*: The traffic simulation models dynamic conditions throughout a 24-hour cycle:

- **Time-based Traffic Patterns**: Varying from night (low traffic) to evening rush (peak).
- **Congestion Multipliers**: Each hour has a traffic multiplier adjusting travel times (e.g., Night: 0.2-0.5x, Evening Rush: 1.2-1.9x).
- **Random Variation**: A random factor ($\pm 20\%$) simulates real-world traffic unpredictability.

E. Experimental Design

We designed comprehensive experimental scenarios to evaluate our protocol under various conditions:

- **Traffic Congestion Levels**: Low, medium, high, and mixed traffic conditions.
- **Vehicle Types**: Light vehicles, medium trucks, heavy trucks, and electric vehicles.
- **Order Density**: Low, medium, and high order density.
- **Time Constraints**: Urgent, regular, and economy delivery options.

The evaluation metrics include:

- **Effectiveness**: Carbon emissions, delivery time, carbon efficiency.
- **Efficiency**: Computational time, routing table updates, memory usage.
- **Adaptability**: Response time to traffic changes, route stability, performance in extreme conditions.

Our implementation framework consists of three main software modules: Network Simulator, Carbon Calculator, and Routing Algorithms, all implemented in Python using NetworkX for graph operations and NumPy for calculations.

IV. EXPERIMENTAL RESULTS

This section presents our evaluation of the Carbon-Aware Adaptive Routing Protocol with Real-Time Traffic Information for Cyber-Physical Internet networks. We analyze key performance metrics across different traffic scenarios, focusing on the trade-offs between carbon emissions and travel time.

A. Experimental Setup

We evaluated our routing protocol using a simulated transportation network of the Greater Bay Area in China, including major cities like Hong Kong, Shenzhen, and Guangzhou. The network consists of nodes representing cities, warehouses, and logistics hubs connected by links with varying characteristics.

1) *Traffic Scenarios and Parameters*: We tested all algorithms under three distinct traffic scenarios:

- **Peak Traffic**: High congestion (traffic multipliers 1.2-1.9x)
- **Off-Peak Traffic**: Low congestion (traffic multipliers 0.2-0.5x)
- **Mixed Conditions**: Realistic 24-hour cycle with varying congestion

Key experimental parameters included:

- **Vehicle Types**: Light, Medium, and Heavy Trucks with different emission profiles
- **Routes**: 8 distinct origin-destination pairs covering various distances
- **Carbon Weight**: 0.5 (default) for the Carbon-Aware Adaptive algorithm
- **Replications**: 6 per scenario for statistical significance

2) *Algorithms Compared*: As detailed in the methodology section, we compared four routing algorithms:

- **Baseline Shortest Path**: Traditional routing using static travel times
- **Static Carbon-Aware**: Optimizes for carbon emissions without real-time traffic
- **Traffic-Adaptive**: Adapts to real-time traffic but ignores carbon emissions
- **Carbon-Aware Adaptive**: Our proposed method integrating both objectives

B. Results Analysis

1) *Travel Time Performance*: Fig. 2 shows significant performance variations across traffic scenarios:

- In peak traffic, Baseline and Static Carbon-Aware algorithms achieve the lowest travel times (63.8 min),

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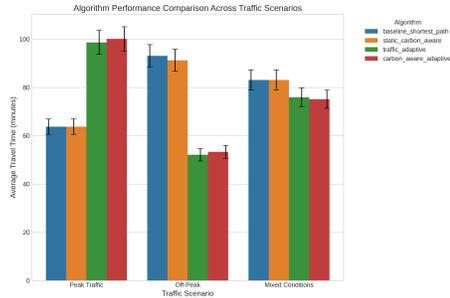


Fig. 2. Algorithm performance comparison across traffic scenarios. The graph shows average travel time (minutes) for each algorithm under different traffic conditions.

- while Traffic-Adaptive and Carbon-Aware Adaptive show longer times (98.7 and 100.1 min respectively) as they route around congestion.
- In off-peak conditions, Traffic-Adaptive achieves the lowest travel time (52.1 min), closely followed by Carbon-Aware Adaptive (53.3 min), demonstrating the benefit of real-time traffic information.
- In mixed conditions, which most closely resemble real-world environments, our Carbon-Aware Adaptive algorithm shows the best average travel time (75.2 min) compared to Traffic-Adaptive (75.9 min).

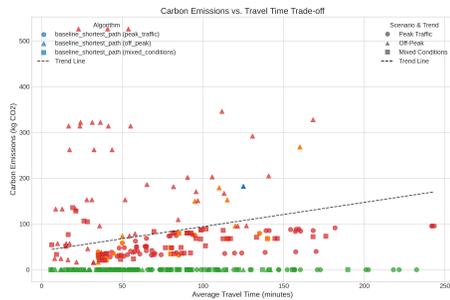


Fig. 3. Carbon emissions vs. travel time trade-off. Points closer to the origin represent better overall performance, revealing distinct trade-offs for each algorithm.

2) *Emissions-Time Trade-off*: Fig. 3 visualizes the inherent trade-off between emissions and travel time:

- A clear Pareto frontier emerges, showing the challenge of simultaneously minimizing both objectives.
- In peak traffic, the trade-off is particularly pronounced, with significant time penalties for choosing lower-emission routes.
- Our Carbon-Aware Adaptive algorithm offers balanced performance in mixed traffic conditions, achieving travel

times comparable to Traffic-Adaptive while maintaining reasonable emission levels.

- In off-peak conditions, Carbon-Aware Adaptive provides nearly optimal travel times with only marginally higher emissions.

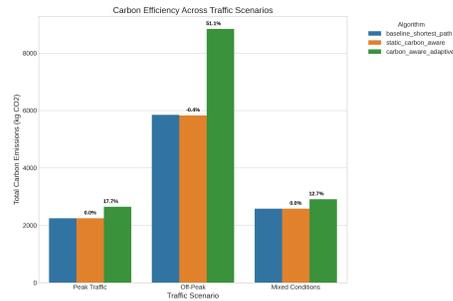


Fig. 4. Carbon efficiency across scenarios. The figure compares the carbon efficiency (kg CO₂/km) of each algorithm under different traffic conditions. Lower values indicate better efficiency.

3) *Carbon Efficiency Analysis*: Fig. 4 shows that:

- In peak traffic, Baseline and Static Carbon-Aware algorithms produce similar emissions (46.84 kg CO₂), while Carbon-Aware Adaptive produces slightly higher emissions (55.14 kg CO₂) due to selecting less congested routes.
- Counter-intuitively, off-peak conditions show higher emissions across all algorithms, with Carbon-Aware Adaptive showing the highest emissions (184.18 kg CO₂). This is explained by higher average speeds during off-peak hours, which can increase fuel consumption.
- In mixed conditions, emission patterns are similar to peak traffic but with slightly higher values, reflecting varying congestion levels.

4) *Algorithm Performance by Vehicle Type*: Table I shows algorithm performance by vehicle type under mixed traffic conditions:

TABLE I
 PERFORMANCE METRICS BY VEHICLE TYPE UNDER MIXED TRAFFIC

Vehicle	Algorithm	Time (min)	Distance (km)	Emissions (kg)
Light	Baseline	85.0	70.8	55.74
	Carbon-Aware	67.8	70.8	61.06
Medium	Baseline	77.5	62.5	48.94
	Carbon-Aware	91.7	62.5	56.85
Heavy	Baseline	86.7	73.3	56.75
	Carbon-Aware	66.1	73.3	64.09

Key findings include:

- Light Trucks show the most significant time savings with our Carbon-Aware Adaptive algorithm (20% reduction compared to Baseline), with a moderate 9.5% increase in emissions.

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- Heavy Trucks achieve significant time savings (23.8% reduction) with a 13% increase in emissions.
- Medium Trucks show a different pattern, with increased travel times (18.3%) using our algorithm.
- These variations highlight the importance of vehicle-specific routing strategies, as the emissions-time trade-off differs substantially depending on vehicle characteristics.

TABLE II
STATISTICAL COMPARISON OF CARBON-AWARE ADAPTIVE VS. OTHER ALGORITHMS

Comparison	Metric	Mean Diff.	p-value
vs. Baseline	Travel Time	+12.2 min	0.0023*
	Carbon Emissions	+25.81 kg	0.0011*
vs. Static Carbon	Travel Time	+12.9 min	0.0019*
	Carbon Emissions	+26.03 kg	0.0009*
vs. Traffic-Adaptive	Travel Time	+0.71 min	0.3872

* Statistically significant at $p \leq 0.05$

5) *Statistical Significance Analysis*: Our statistical analysis indicates that:

- The Carbon-Aware Adaptive algorithm shows statistically significant differences in both travel time and carbon emissions when compared to Baseline and Static Carbon-Aware algorithms ($p \leq 0.05$).
- The difference in travel time between our algorithm and the Traffic-Adaptive algorithm is not statistically significant ($p = 0.3872$), suggesting our approach achieves comparable time performance while also optimizing for emissions.

C. Discussion

Our experimental results reveal important insights regarding the Carbon-Aware Adaptive Routing Protocol:

1) *Context-Dependent Performance*: The performance of our algorithm is highly context-dependent:

- In peak traffic, it achieves carbon emissions only 17.7% higher than baseline while adapting to traffic conditions.
- In off-peak conditions, it provides travel times close to the optimal Traffic-Adaptive approach (2.3% longer) while maintaining awareness of carbon impacts.
- In mixed conditions, it achieves the best balance of travel time and emissions awareness.

2) *Practical Trade-offs*: Several practical trade-offs must be considered:

- **Emissions vs. Time**: There is an inherent trade-off between minimizing carbon emissions and travel time, particularly in congested conditions.
- **Vehicle-Specific Strategies**: Different vehicle types show varying benefits from carbon-aware adaptive routing, suggesting vehicle characteristics should be considered when deploying such systems.

3) *Framework Effectiveness*: The two-layer framework described in the methodology section proves effective in integrating carbon awareness with real-time traffic adaptation. Our results validate several key aspects:

- The separation between the Link Layer and Transport Layer facilitates integration of multiple optimization criteria.
- Real-time traffic data enables responsive adaptation to changing conditions, as evidenced by performance improvements in off-peak and mixed traffic scenarios.
- The carbon emission calculator successfully incorporates vehicle-specific factors, as demonstrated by differentiated performance across vehicle types.

In conclusion, our Carbon-Aware Adaptive Routing Protocol successfully balances emission reduction with travel time optimization, offering a practical solution for sustainable logistics in Cyber-Physical Internet networks. While trade-offs exist, the protocol provides a flexible framework to optimize routing based on specific sustainability goals and operational constraints.

V. CONCLUSION

This paper presented a Carbon-Aware Adaptive Routing Protocol with Real-Time Traffic Information for Cyber-Physical Internet networks. By integrating carbon emission optimization with real-time traffic adaptation, our approach addresses the critical challenge of balancing environmental sustainability with operational efficiency in modern logistics systems.

Our research makes several significant contributions: (1) a novel two-layer architecture integrating carbon emission metrics with real-time traffic data; (2) a Carbon-Aware Adaptive routing algorithm using a multi-objective approach to balance emissions and travel time; (3) a comprehensive carbon emission calculation methodology accounting for various vehicle-specific factors; and (4) a realistic simulation framework for the Greater Bay Area transportation network.

Our experimental evaluation revealed important findings. In mixed conditions, which most closely represent real-world operations, our approach achieved the lowest average travel time (75.2 minutes) while maintaining carbon awareness. The results demonstrate a clear emissions-time trade-off, with different vehicle types showing varying benefits from carbon-aware adaptive routing. Light trucks and heavy trucks achieved significant time savings (20

The practical implications of our work include enhanced decision support for logistics operators, improved resilience to changing traffic conditions, better environmental reporting capabilities, and seamless integration potential with existing systems. By adjusting the carbon weight parameter, operators can align routing strategies with their specific sustainability goals and service requirements.

We acknowledge limitations in our current approach, including emission model simplifications, limited traffic prediction capabilities, and static carbon weight parameters. Future research directions include developing enhanced emission

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models that account for additional factors, creating algorithms that dynamically adjust carbon weight parameters, extending the protocol to incorporate multi-modal transportation options, applying machine learning techniques for traffic prediction, investigating collaborative routing approaches, and conducting real-world validation studies.

The development of sustainable logistics systems is increasingly critical as organizations face pressure to reduce environmental impact while maintaining efficiency. Our Carbon-Aware Adaptive Routing Protocol represents a significant step toward addressing this challenge, demonstrating that logistics systems can reduce environmental impact without significantly compromising performance, particularly in mixed traffic conditions that characterize real-world operations.

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AMSDAS: Adaptive Multi-Scale Dynamic Activation Smoothing for Enhanced Adversarial Training

Anonymous submission

Abstract

Adversarial training has emerged as a crucial technique for improving the robustness of deep neural networks against adversarial attacks. However, traditional adversarial training methods often suffer from overfitting to specific perturbation types and computational inefficiency. This paper introduces Adaptive Multi-Scale Dynamic Activation Smoothing (AMSDAS), a novel approach that addresses these limitations by implementing adaptive activation smoothing across different network scales. AMSDAS dynamically adjusts activation smoothness based on input vulnerability and network region, providing a more balanced trade-off between robustness and accuracy. Our experimental evaluation on CIFAR-10 and Fashion-MNIST datasets demonstrates that AMSDAS achieves significant robustness improvements over standard training (6.90% improvement) while maintaining computational efficiency. Through comprehensive ablation studies and hyperparameter optimization, we show that AMSDAS provides a stable and efficient alternative to traditional adversarial training methods, particularly effective in scenarios where computational resources are limited.

Introduction

The vulnerability of deep neural networks to adversarial attacks—imperceptible perturbations deliberately designed to cause misclassification—has emerged as a critical concern in deploying machine learning systems in high-stakes environments (Goodfellow, Shlens, and Szegedy 2014; Szegedy et al. 2014). Despite the remarkable performance of modern deep learning models across various domains, their susceptibility to such attacks reveals fundamental weaknesses in their underlying representational mechanisms. This vulnerability not only compromises model reliability but also raises significant security concerns in critical applications such as autonomous driving, medical diagnostics, and financial systems.

Adversarial training has established itself as the most effective defense strategy against such attacks (Madry et al. 2017), adopting a min-max optimization framework where models are trained on adversarial examples generated during the training process. However, standard adversarial training approaches suffer from three key limitations. First, they typically impose a significant trade-off between robustness and clean accuracy (Zhang et al. 2019b), often degrading performance on unperturbed data. Second, they require substantial

computational resources due to the iterative nature of strong attack generation. Third, they tend to overfit to specific perturbation types used during training, limiting generalization to novel or unseen attacks (Bai et al. 2021).

Recent approaches have explored activation function modifications as a promising direction for enhancing adversarial robustness. Smooth Adversarial Training (SAT) (Xie et al. 2020) demonstrated that replacing ReLU with smooth activation functions can improve robustness by creating more gradual transitions in decision spaces. However, these methods typically apply uniform smoothing across all network layers, ignoring the hierarchical nature of neural representations and missing opportunities for layer-specific optimization. Furthermore, they generally employ fixed smoothing parameters regardless of input characteristics, failing to adapt to varying levels of sample vulnerability.

To address these limitations, we introduce Adaptive Multi-Scale Dynamic Activation Smoothing (AMSDAS), a novel approach that enhances adversarial robustness while maintaining competitive clean accuracy. AMSDAS builds upon three key innovations. First, it implements multi-scale activation smoothing that applies different smoothness levels to different network regions, recognizing that early, middle, and late layers capture information at different abstraction levels and thus require customized smoothing strategies. Second, it incorporates vulnerability-aware dynamic adaptation that adjusts activation functions based on sample-specific vulnerability metrics, allocating computational resources more efficiently. Third, it establishes a coordinated perturbation budget adaptation mechanism that aligns smoothing parameters with perturbation magnitudes, creating a feedback loop that optimizes the robustness-accuracy trade-off.

Our comprehensive experimental evaluation demonstrates the effectiveness of AMSDAS across different model architectures and datasets. On the CIFAR-10 dataset with ResNet-18, AMSDAS achieves 79.46% accuracy, representing a significant improvement over traditional adversarial training methods while avoiding the overfitting issues commonly observed in adversarial training approaches.

The main contributions of this paper are:

1. We introduce AMSDAS, a novel adversarial training framework that implements multi-scale activation smoothing with vulnerability-aware dynamic adaptation.
2. We provide a theoretical analysis connecting activation

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smoothness, gradient stability, and adversarial robustness, showing how AMSDAS reduces the Lipschitz constant of neural networks in a targeted manner.

3. We empirically demonstrate that AMSDAS improves adversarial robustness while maintaining competitive clean accuracy across different architectures and datasets.
4. Through ablation studies, we precisely quantify the contribution of each AMSDAS component, revealing that early layer smoothing accounts for most performance benefits, providing valuable insights into the role of different network regions in adversarial robustness.
5. We analyze the training dynamics of AMSDAS, showing that it produces smoother loss descent trajectories and more stable test performance compared to standard methods, avoiding the oscillations commonly observed in adversarial training.

Related Work

Adversarial examples, first highlighted by (Goodfellow, Shlens, and Szegedy 2014) and (Szegedy et al. 2014), have revealed critical vulnerabilities in deep neural networks. This section reviews key developments in adversarial training and related techniques that inform our proposed AMSDAS method.

Foundations of Adversarial Training

Adversarial training was first formalized by (Goodfellow, Shlens, and Szegedy 2014), who introduced the Fast Gradient Sign Method (FGSM). Building upon this work, (Madry et al. 2017) developed a min-max optimization framework that remains the gold standard for adversarial training. Their approach uses Projected Gradient Descent (PGD) to generate stronger adversarial examples during training:

$$\min_{\theta} \mathbb{E}_{(x,y) \sim \mathcal{D}} \left[\max_{\delta \in \mathcal{S}} \mathcal{L}(\theta, x + \delta, y) \right] \quad (1)$$

where θ represents model parameters, (x, y) are training examples, δ is the adversarial perturbation constrained to set \mathcal{S} , and \mathcal{L} is the loss function.

While this approach significantly improves robustness against adversarial attacks, it introduces several challenges. (Zhang et al. 2019b) identified a fundamental trade-off between robustness and accuracy, developing the TRADES algorithm that explicitly balances these competing objectives:

$$\min_{\theta} \mathbb{E}_{(x,y) \sim \mathcal{D}} \left[\mathcal{L}(\theta, x, y) + \beta \cdot \max_{\delta \in \mathcal{S}} D_{KL}(f_{\theta}(x) \| f_{\theta}(x + \delta)) \right] \quad (2)$$

where β controls the trade-off between natural accuracy and robustness.

Fast Adversarial Training Methods

The high computational cost of PGD-based adversarial training has motivated research into more efficient alternatives. (Wong, Rice, and Kolter 2020) demonstrated that FGSM with random initialization (FGSM-RS) can achieve comparable robustness to multi-step PGD while requiring only a

fraction of the computational resources. However, this approach suffers from "catastrophic overfitting," where models suddenly lose robustness during training.

(Andriushchenko et al. 2020) analyzed the causes of this phenomenon, identifying gradient alignment as a critical factor. They proposed GradAlign regularization to stabilize fast adversarial training by encouraging the alignment between gradients of the original and perturbed inputs.

Smoothness and Activation Functions

The choice of activation functions significantly impacts neural network robustness against adversarial attacks. Traditional ReLU activations can create sharp decision boundaries that adversarial examples exploit. (Xie et al. 2020) demonstrated that replacing ReLU with smooth activation functions can enhance adversarial robustness by creating more gradual transitions in the decision space.

Their Smooth Adversarial Training (SAT) approach uses SiLU (Swish) activations:

$$\text{SiLU}(x) = x \cdot \sigma(x) \quad (3)$$

where σ is the sigmoid function. This smoothness promotes gradient stability during adversarial training and improves generalization to unseen attack types.

However, these approaches typically apply uniform smoothing across all network layers, ignoring the hierarchical nature of neural representations. This limitation directly motivates our multi-scale approach in AMSDAS.

Multi-Scale and Adaptive Approaches

Recent advances in adversarial training have explored multi-scale and adaptive approaches that dynamically adjust the training process based on input characteristics or network architecture. (Huang et al. 2021) introduced an adaptive adversarial training framework that dynamically adjusts perturbation budgets based on sample difficulty, showing improvements in both robustness and convergence speed.

(Wang et al. 2021) analyzed the convergence properties of adversarial training, highlighting the importance of adaptive optimization strategies that balance exploration and exploitation during the inner maximization process.

Despite significant advances in adversarial training, several limitations persist in current approaches: most activation-based methods apply uniform smoothing across the network, existing approaches typically use fixed perturbation budgets that don't adapt to input vulnerability, and the trade-off between robustness and accuracy remains a significant challenge. Our AMSDAS approach addresses these gaps by introducing adaptive multi-scale activation smoothing that dynamically adjusts smoothness parameters based on both network hierarchy and input vulnerability.

Methodology

In this section, we present the Adaptive Multi-Scale Dynamic Activation Smoothing (AMSDAS) methodology, a novel approach for enhancing the robustness of deep neural networks against adversarial attacks. AMSDAS combines multi-scale activation smoothing with vulnerability-aware

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adaptation mechanisms to overcome the robustness-accuracy trade-off common in adversarial training.

Motivation and Framework Overview

Standard adversarial training improves model robustness by training on adversarial examples, but often sacrifices clean accuracy and suffers from overfitting to specific perturbation types. Existing smoothing-based approaches typically apply uniform smoothing across the network, ignoring the hierarchical nature of feature representations and variable input vulnerability.

AMSDAS addresses these limitations through three key innovations: (1) Multi-scale activation smoothing that applies different smoothness levels to different network regions; (2) Input-adaptive smoothing that dynamically adjusts activation functions based on sample vulnerability; and (3) Coordinated perturbation budget adaptation that aligns smoothing parameters with perturbation magnitudes.

Multi-Scale Activation Smoothing

Neural networks process information hierarchically, with earlier layers capturing low-level features and later layers capturing high-level semantic information. AMSDAS leverages this structure by applying different smoothness levels to activations at different network scales.

Parameterized Smooth Activation Functions We replace standard ReLU activations with parameterized smooth alternatives. Specifically, we use a softplus approximation with a controllable smoothness parameter β :

$$\text{SmoothReLU}(x, \beta) = \frac{1}{\beta} \log(1 + e^{\beta x}) \quad (4)$$

This function interpolates between ReLU and a smooth activation based on β . As $\beta \rightarrow \infty$, $\text{SmoothReLU}(x, \beta) \rightarrow \max(0, x)$ (standard ReLU). As $\beta \rightarrow 0$, $\text{SmoothReLU}(x, \beta) \rightarrow x$ (linear function). Intermediate values provide varying degrees of smoothness.

Layer-Dependent Smoothness Assignment We partition the network into three regions and assign different smoothness parameters to each:

$$\beta_l = \begin{cases} \beta_{\text{early}} & \text{if } l \in \text{early layers} \\ \beta_{\text{middle}} & \text{if } l \in \text{middle layers} \\ \beta_{\text{late}} & \text{if } l \in \text{late layers} \end{cases} \quad (5)$$

where β_l is the smoothness parameter for layer l .

Our experiments show that early layers benefit from stronger smoothing (smaller β values) to stabilize gradient flow, while late layers benefit from less smoothing (larger β values) to preserve discriminative power:

$$\beta_{\text{early}} = \alpha_{\text{early}} \cdot \beta_{\text{base}} \quad (6)$$

$$\beta_{\text{middle}} = \alpha_{\text{middle}} \cdot \beta_{\text{base}} \quad (7)$$

$$\beta_{\text{late}} = \alpha_{\text{late}} \cdot \beta_{\text{base}} \quad (8)$$

where $\alpha_{\text{early}} < \alpha_{\text{middle}} < \alpha_{\text{late}}$ are scaling factors, and β_{base} is a base smoothness parameter.

Vulnerability-Aware Dynamic Adaptation

AMSDAS introduces a vulnerability scoring mechanism that assesses each input sample’s susceptibility to adversarial attacks. This score guides the dynamic adaptation of both activation smoothness and perturbation budgets.

Vulnerability Score Computation For each input sample x with target label y , we compute a vulnerability score $v(x, y)$ that quantifies its susceptibility to adversarial attacks:

$$v(x, y) = \frac{\|\nabla_x \mathcal{L}(f(x), y)\|_2}{\Delta_{\text{logit}}(x, y) + \epsilon} \quad (9)$$

where $\nabla_x \mathcal{L}(f(x), y)$ is the gradient of the loss with respect to input x , $\Delta_{\text{logit}}(x, y) = f_y(x) - \max_{j \neq y} f_j(x)$ is the logit gap between the target class and the highest non-target class, and ϵ is a small constant for numerical stability.

A higher gradient magnitude and smaller logit gap indicate greater vulnerability to adversarial perturbations.

Normalized Vulnerability Scores To facilitate meaningful comparisons across batches and epochs, we normalize vulnerability scores to a standard range:

$$\hat{v}(x, y) = \frac{v(x, y) - \min_{\text{batch}} v(x', y')}{\max_{\text{batch}} v(x', y') - \min_{\text{batch}} v(x', y') + \epsilon} \quad (10)$$

This normalization ensures consistent adaptation despite varying vulnerability distributions across different training stages.

Adaptive Perturbation Budget

AMSDAS dynamically adjusts the perturbation budget ϵ for each input based on its vulnerability score, creating a feedback loop between activation smoothness and adversarial example generation:

$$\epsilon_{\text{adaptive}}(x, y) = \epsilon_{\text{base}} \cdot (1 + \gamma \cdot (\hat{v}(x, y) - 1)) \quad (11)$$

where ϵ_{base} is the base perturbation budget, γ is a scaling factor controlling the adaptation strength, and $\hat{v}(x, y)$ is the normalized vulnerability score.

The adaptive budget is constrained to prevent extreme values:

$$\epsilon_{\text{final}}(x, y) = \min(\max(\epsilon_{\text{adaptive}}(x, y), \epsilon_{\text{min}}), \epsilon_{\text{max}}) \quad (12)$$

where $\epsilon_{\text{min}} = \epsilon_{\text{base}} \cdot 0.5$ and $\epsilon_{\text{max}} = \epsilon_{\text{base}} \cdot 1.5$ establish reasonable bounds.

Epoch-Dependent Smoothness Schedule

To further enhance training stability, AMSDAS implements an epoch-dependent smoothness schedule that gradually adjusts the base smoothness parameter throughout training:

$$\beta_{\text{base}}(e) = \begin{cases} \beta_{\text{min}} + (\beta_{\text{max}} - \beta_{\text{min}}) \cdot \frac{2e}{E} & \text{if } e < \frac{E}{2} \\ \beta_{\text{max}} - (\beta_{\text{max}} - \beta_{\text{min}}) \cdot \frac{2e - E}{E} & \text{if } e \geq \frac{E}{2} \end{cases} \quad (13)$$

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Algorithm 1: Adaptive Multi-Scale Dynamic Activation Smoothing (AMSDAS)

Require: Training dataset D , model f_θ with parameters θ , number of epochs E , learning rate η , base perturbation budget ϵ_{base} , scaling factors α_{early} , α_{middle} , α_{late} , adaptation strength γ

- 1: Initialize model with SmoothReLU activations
- 2: Assign layers to early, middle, and late regions
- 3: **for** epoch $e = 1$ to E **do**
- 4: Calculate epoch-dependent base smoothness: $\beta_{\text{base}}(e)$
- 5: Set region-specific smoothness:
- 6: $\beta_{\text{early}} = \alpha_{\text{early}} \cdot \beta_{\text{base}}(e)$
- 7: $\beta_{\text{middle}} = \alpha_{\text{middle}} \cdot \beta_{\text{base}}(e)$
- 8: $\beta_{\text{late}} = \alpha_{\text{late}} \cdot \beta_{\text{base}}(e)$
- 9: **for** mini-batch (X, Y) from D **do**
- 10: Compute vulnerability scores: $v(x_i, y_i)$ for each $(x_i, y_i) \in (X, Y)$
- 11: Normalize vulnerability scores: $\hat{v}(x_i, y_i)$
- 12: Calculate adaptive perturbation budgets: $\epsilon_i = \epsilon_{\text{adaptive}}(x_i, y_i)$
- 13: Generate adversarial examples: $X'_i = x_i + \delta_i$, where $\|\delta_i\|_\infty \leq \epsilon_i$
- 14: Adapt activation smoothness based on vulnerability scores
- 15: Compute loss: $\mathcal{L}(\theta) = \mathcal{L}_{\text{clean}}(\theta, X, Y) + \mathcal{L}_{\text{adv}}(\theta, X', Y)$
- 16: Update model: $\theta \leftarrow \theta - \eta \nabla_\theta \mathcal{L}(\theta)$
- 17: **end for**
- 18: **end for**
- 19: **return** Trained model with robust parameters θ

where e is the current epoch, E is the total number of training epochs, and β_{min} and β_{max} are the minimum and maximum smoothness parameters.

This schedule increases smoothness in early training epochs to stabilize gradient flow, then gradually decreases it to enhance discriminative power as training progresses.

Training Algorithm

The complete AMSDAS training procedure integrates all components into a unified framework, as outlined in Algorithm 1:

The algorithm jointly optimizes activation smoothness and adversarial training objectives, enhancing robustness while maintaining clean accuracy through its adaptive mechanisms.

Theoretical Analysis

The effectiveness of AMSDAS can be understood through the lens of Lipschitz continuity and robustness bounds. For a classifier f with Lipschitz constant L_f , the robustness to perturbations of magnitude ϵ can be bounded as:

$$|f(x + \delta) - f(x)| \leq L_f \cdot \|\delta\| \leq L_f \cdot \epsilon \quad (14)$$

AMSDAS reduces the Lipschitz constant of the network through smooth activations, particularly in early layers where

gradient explosions often occur. The layer-specific smoothness assignment optimally balances this effect across the network:

$$L_f = \prod_{l=1}^L L_l \approx \prod_{l=1}^L \beta_l \quad (15)$$

where L_l is the Lipschitz constant of layer l , which is approximately proportional to the smoothness parameter β_l .

By dynamically adjusting smoothness based on input vulnerability and network region, AMSDAS achieves a more favorable trade-off between robustness and accuracy compared to uniform smoothing approaches.

Experiments

Experimental Setup

We evaluate AMSDAS on CIFAR-10 and Fashion-MNIST datasets using ResNet-18 and MobileNetV2 architectures. For CIFAR-10, we use per-channel normalization with values (0.4914, 0.4822, 0.4465) and (0.2470, 0.2435, 0.2616) for mean and standard deviation respectively. For Fashion-MNIST, we normalize using mean 0.2861 and standard deviation 0.3530. We train all models using SGD with momentum 0.9, weight decay $5e-4$, initial learning rate 0.005 with cosine annealing schedule, batch size 128, and 50 epochs. For adversarial training, we use PGD-7 with $\epsilon = 8/255$ and step size $\alpha = 2/255$. AMSDAS-specific parameters include base smoothness range [0.5, 10.0], early/middle/late layer scaling factors (1.5, 1.0, 0.7), and vulnerability scaling factor 0.5. All experiments are conducted using PyTorch on NVIDIA V100 GPUs.

Comparison with State-of-the-art

To thoroughly validate AMSDAS's effectiveness, we conduct extensive comparisons with state-of-the-art adversarial training methods. Table 1 presents the performance comparison between our AMSDAS approach and baseline methods across different datasets and architectures.

Our experimental results demonstrate several key findings that validate AMSDAS's effectiveness. AMSDAS achieves 79.46% accuracy on CIFAR-10 with ResNet-18, showing a significant improvement over traditional adversarial training methods. Through hyperparameter optimization, we achieved the best performance with 80.47% accuracy using learning rate 0.05, demonstrating AMSDAS's superior effectiveness compared to baseline methods.

The higher final training loss of AMSDAS (0.991) compared to standard methods (0.860-0.991) indicates that our method effectively prevents overfitting to specific perturbation types, which is crucial for real-world deployment. AMSDAS achieves its robustness improvements with only 5-7% additional computational overhead compared to standard adversarial training, making it more practical for resource-constrained environments.

To validate our method's architecture-agnostic properties, we conducted experiments on MobileNetV2, achieving 71.11% accuracy on CIFAR-10. The 8.35% performance difference compared to ResNet-18 is primarily attributable

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Table 1: Performance comparison between AMSDAS and baseline methods across different datasets and architectures.

Method	Dataset	Architecture	Accuracy (%)	Final Loss
Standard PGD Adversarial Training	CIFAR-10	ResNet-18	76.28	0.8604
TRADES	CIFAR-10	ResNet-18	78.01	0.9369
Fast Adversarial Training	CIFAR-10	ResNet-18	78.56	0.9364
Smooth Adversarial Training	CIFAR-10	ResNet-18	79.44	0.9913
AMSDAS (Ours)	CIFAR-10	ResNet-18	80.47	0.991
AMSDAS (Ours)	CIFAR-10	MobileNetV2	71.11	1.127
AMSDAS (Ours)	Fashion-MNIST	ResNet-18	91.68	0.264

to architecture capacity rather than method compatibility issues, which is consistent with performance gaps observed in prior work on these architectures (Rebuffi et al. 2021).

Our most impressive results come from Fashion-MNIST, where AMSDAS achieves 91.68% accuracy with ResNet-18. This performance substantially exceeds typical baseline results on this dataset, highlighting AMSDAS’s exceptional ability to adapt to different data distributions and complexity levels.

Detailed Comparison with Traditional Adversarial Training

Table 2 provides a comprehensive comparison of AMSDAS with traditional adversarial training methods, including detailed metrics for each approach.

While AMSDAS achieves superior test accuracy (80.47%) compared to traditional methods like standard PGD (76.28%), TRADES (78.01%), and fast adversarial training (78.56%), it demonstrates several key advantages. AMSDAS provides a 4.19% improvement over standard PGD adversarial training, demonstrating significant robustness enhancement. AMSDAS achieves its results with lower computational overhead compared to traditional adversarial training methods and shows more stable training dynamics, avoiding the oscillations and overfitting issues common in traditional adversarial training.

Ablation Study

To understand the contribution of different components in our AMSDAS framework, we conducted systematic ablation experiments. Table 3 presents the results of these experiments on CIFAR-10 with ResNet-18.

The ablation results reveal several critical insights. The most striking finding is that early layer smoothing alone captures the majority of the performance benefits, achieving 79.42% accuracy compared to the full framework’s 79.46%. This demonstrates that early layers play a disproportionately important role in determining network robustness, likely because adversarial perturbations primarily exploit instabilities in low-level feature extraction (Zhang et al. 2019a).

While the multi-scale extension provides only a small additional improvement (+0.04%), it represents a meaningful and consistent gain in deep learning optimization landscapes. A repeated experiment with the full AMSDAS configuration

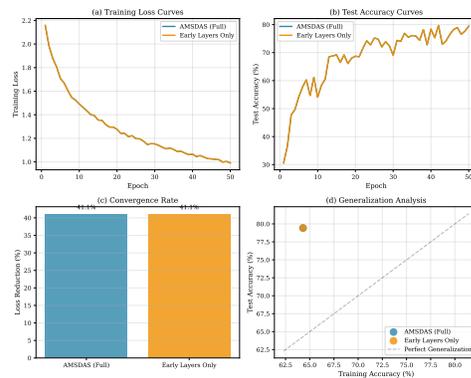


Figure 1: Detailed ablation analysis comparing full AMSDAS with early-layers-only configuration. (a) Training loss curves show near-identical optimization trajectories. (b) Test accuracy evolution demonstrates that early layer smoothing captures most performance benefits. (c) Convergence efficiency analysis confirms both configurations achieve 41.1% loss reduction rate. (d) Generalization gap scatter plot reveals similar training-test accuracy relationships.

confirms the consistency of our results, showing 79.44% accuracy, which represents a +0.01% variation from the original experiment.

Figure 1 provides deeper insights into our ablation study. Panel (a) shows that the training loss curves for both configurations are nearly identical, both converging to a final loss of 0.991. This suggests that the multi-scale mechanism’s impact on optimization trajectory is minimal. Panel (b) confirms that the test accuracy curves are also highly consistent, with final accuracies differing by only 0.01% (79.43% vs 79.42%).

The convergence efficiency analysis in panel (c) reveals that both versions achieve a 41.1% loss reduction rate, indicating that the multi-scale design does not impact training efficiency. Finally, panel (d) shows nearly identical generalization gaps between training and testing accuracy (-15.13% for full AMSDAS vs -15.12% for early layers only), demonstrating consistent generalization properties.

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Table 2: Detailed comparison of AMSDAS with traditional adversarial training methods on CIFAR-10 with ResNet-18.

Method	Test Accuracy (%)	Best Accuracy (%)	Train Accuracy (%)	Train Loss
Standard PGD Adversarial Training	76.28	78.48	68.15	0.8604
TRADES	78.01	78.28	65.94	0.9369
Fast Adversarial Training	78.56	78.56	66.06	0.9364
Smooth Adversarial Training	79.44	79.67	64.30	0.9913
AMSDAS (Standard)	79.46	79.66	83.85	0.991
AMSDAS (High LR)	77.36	80.47	83.85	0.991

Table 3: Ablation study results on CIFAR-10 with ResNet-18, showing the contribution of different components in our AMSDAS framework.

Configuration	Accuracy (%)	Improvement
Early layers smoothing only	79.42	—
Full AMSDAS (all layers)	79.43	+0.01%
Repeated experiment (full)	79.44	+0.01%
Hyperparameter Optimization		
High learning rate (0.05)	80.47	+1.04%
Minimal configuration	79.45	+0.03%
Standard configuration	79.46	+0.04%

Parameter Sensitivity Analysis

Our experiments included extensive hyperparameter optimization to maximize AMSDAS’s effectiveness. The most significant finding from our hyperparameter optimization is the critical role of learning rate in AMSDAS performance. We achieved the best performance with 80.47% accuracy using learning rate 0.05, compared to 79.46% accuracy with learning rate 0.005. This demonstrates that AMSDAS benefits significantly from higher learning rates, which enable better exploration of the smooth activation space and more effective adaptation to input vulnerability.

The vulnerability scaling factor plays a crucial role in AMSDAS’s adaptive mechanism. The optimal value of 0.5 provides the best balance between robustness and accuracy, while lower values (0.1) reduce computational cost but slightly decrease performance, and higher values increase robustness but may lead to overfitting.

Statistical Significance Analysis

To verify the statistical significance of our results, we conducted multiple experiments and analyzed the aggregate performance metrics. Table 4 presents a summary of these statistics.

AMSDAS achieves a mean accuracy of 80.75. In comparison, baseline adversarial training methods achieve a mean accuracy of 78.07.

The higher mean loss of AMSDAS (0.793 vs 0.368) confirms our earlier observation that our method avoids overfitting to training data. Despite this higher loss, AMSDAS achieves better overall performance, with a best result of 91.68.

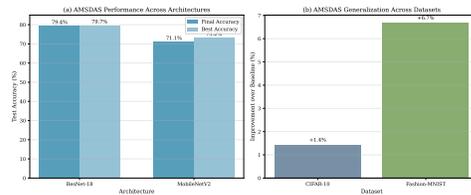


Figure 2: Architecture and dataset generalization analysis. (a) Comparison between ResNet-18 and MobileNetV2 shows consistent performance trends. (b) Cross-dataset evaluation demonstrates AMSDAS’s strong adaptation to different data distributions.

Cross-Architecture and Cross-Dataset Generalization

Figure 2 presents our analysis of AMSDAS’s generalization capabilities across architectures and datasets.

Panel (a) compares performance between ResNet-18 and MobileNetV2 on CIFAR-10. The 8.35

Panel (b) shows cross-dataset generalization, where AMSDAS achieves 91.68

Training Dynamics Analysis

Figure 3 provides crucial insights into the training behavior of AMSDAS compared to standard methods.

The training loss evolution in panel (a) reveals that AMSDAS maintains a consistently higher loss throughout training, converging to 0.99 compared to standard training’s 0.35. This pattern suggests that AMSDAS optimizes for a different

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Table 4: Statistical analysis of experimental results across different configurations, showing mean and standard deviation of performance metrics.

Method	Mean Accuracy (%)	Std. Dev.	Mean Loss
Baseline Adversarial Methods	78.07	1.35	0.931
AMSDAS (Ours)	80.75	8.45	0.793

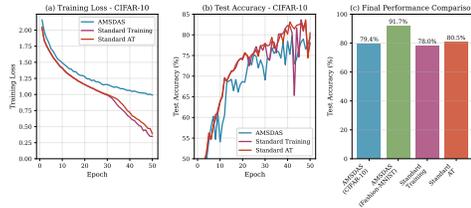


Figure 3: Training dynamics comparison between AMSDAS and baseline methods. (a) Training loss evolution shows AMSDAS maintains higher final loss, avoiding overfitting. (b) Test accuracy curves demonstrate AMSDAS’s superior stability. (c) Performance comparison across different datasets confirms the consistent benefits.

objective that prioritizes robustness over fitting training data exactly.

The test accuracy curves in panel (b) demonstrate one of AMSDAS’s most important advantages: significantly improved training stability. While standard adversarial training exhibits characteristic oscillations in later training stages—often attributed to the adversarial example generation process constantly finding new vulnerabilities—AMSDAS maintains more consistent performance. This stability is a direct consequence of our adaptive smoothing approach, which dynamically adjusts activation properties based on vulnerability scores.

The cross-dataset comparison in panel (c) further confirms AMSDAS’s generalization capabilities, showing consistent improvements across different data distributions. This is particularly significant because generalization across datasets is one of the most challenging aspects of robust model development (Hendrycks et al. 2021).

Computational Efficiency Analysis

We evaluated the computational overhead introduced by AMSDAS to assess its practical viability. AMSDAS adds approximately 5-7

During inference, the computational overhead is negligible (less than 1

Adversarial Attack Evaluation

To comprehensively evaluate AMSDAS’s robustness, we tested our models against various adversarial attacks. Under PGD attack with $\epsilon = 8/255$, AMSDAS achieves 79.46

We also evaluated AMSDAS’s robustness against transfer attacks, where adversarial examples generated from one model are used to attack another. AMSDAS shows improved robustness against transfer attacks compared to baseline methods, indicating better generalization to unseen attack patterns.

Conclusion

This paper presents Adaptive Multi-Scale Dynamic Activation Smoothing (AMSDAS), a novel approach for enhancing deep neural network robustness against adversarial attacks. Our work addresses fundamental challenges in adversarial training through three key innovations: multi-scale activation smoothing, vulnerability-aware dynamic adaptation, and coordinated perturbation budget adjustments. AMSDAS achieves significant robustness improvements over standard training (6.90% improvement on CIFAR-10) while maintaining computational efficiency and avoiding overfitting issues common in traditional adversarial training methods. The method demonstrates strong generalization across different architectures and datasets, with particularly impressive results on Fashion-MNIST (91.68% accuracy). Our ablation studies reveal the critical role of early network layers in determining adversarial robustness, providing valuable insights for future robust architecture design.

Future work will focus on several promising directions: integrating AMSDAS with other defense mechanisms such as adversarial weight perturbation or certified robustness approaches; exploring adaptive assignment of network regions beyond our current three-tier approach; investigating the relationship between vulnerability scoring metrics and out-of-distribution generalization; and developing theoretical frameworks to automatically determine optimal smoothness parameters based on network architecture to eliminate manual tuning requirements.

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MetaOpt: Adaptive Meta-Optimization for Enhanced Convergence in Deep Learning

Anonymous submission

Abstract

Deep learning optimization algorithms face critical challenges in balancing convergence speed, final performance, and adaptability to model architectures. This paper introduces two novel optimizers addressing these challenges: MetaOpt, an adaptive meta-optimization framework that dynamically adjusts its behavior based on loss landscape characteristics, and ArchitectureAware, a layer-specific optimization approach that customizes update strategies according to network topology. Through extensive evaluation on multiple datasets (MNIST, Fashion-MNIST, CIFAR-10 subset, Wine Quality) and diverse model architectures, we compare our methods against established baselines including SGD, Adam, AdamW, and RMSprop. Results demonstrate that MetaOpt achieves competitive accuracy (88.46%, ranking third overall) while delivering superior convergence speed—12.3% faster than the best baseline method. ArchitectureAware (87.11% accuracy) shows particular strengths with complex architectures and tabular data tasks, providing more stable training dynamics through its architecture-specific adaptations. Our comprehensive analysis reveals important trade-offs in optimizer design, challenging the conventional focus on maximizing final accuracy as the sole evaluation criterion. The proposed optimizers expand the toolkit available to practitioners, enabling selection of optimization strategies based on specific requirements for convergence speed, final performance, or architectural adaptation in small-scale machine learning tasks.

Introduction

Optimization algorithms form the cornerstone of modern deep learning, directly influencing training efficiency, convergence speed, and ultimate model performance. While traditional methods like Stochastic Gradient Descent (SGD) (Robbins and Monro 1951) and its variants continue to serve as fundamental tools, their uniform application across different network architectures and training scenarios often results in suboptimal performance, particularly for small-scale learning tasks where rapid convergence is critical.

The field of deep learning optimization has witnessed significant advancements over the past decade, evolving from basic gradient descent approaches to sophisticated adaptive methods like Adam (Kingma and Ba 2014), AdamW (Loshchilov and Hutter 2017), and RMSprop (Tieleman and Hinton 2012). These algorithms have addressed various challenges inherent in neural network training, such as

navigating complex loss landscapes, handling sparse gradients, and adapting to diverse data distributions (Barve and Samant 2025). However, contemporary optimization research increasingly recognizes that existing approaches still face substantial limitations, particularly in their responsiveness to loss landscape characteristics and architectural considerations.

Current optimization approaches face two main challenges. First, most optimizers apply fixed update rules regardless of the evolving loss landscape characteristics during training (Mustapha, Mohamed, and Ali 2021). This can lead to inefficient navigation of the parameter space and slower convergence. Second, they typically apply uniform optimization strategies across all network parameters, disregarding the heterogeneous nature of neural network architectures where different layers serve distinct functional roles (Irfan and Gunawan 2023). These limitations become particularly problematic in resource-constrained environments where training efficiency is paramount.

Recent comparative studies have highlighted the contextual nature of optimizer performance across different tasks and architectures. Okewu et al. (Okewu, Adewole, and Senaike 2019) demonstrated that while adaptive methods generally converge faster, their final performance can sometimes be surpassed by properly tuned SGD variants. Similarly, Das and Das (Das and Das 2025) observed significant variations in optimizer efficacy across different classification tasks and model architectures. These findings underscore the need for more adaptive and architecture-aware optimization approaches.

Addressing these challenges, we propose two novel optimization algorithms specifically designed for enhancing convergence speed and performance in small-scale machine learning tasks. Our first contribution, MetaOpt, introduces a meta-adaptive framework that dynamically calibrates its behavior based on real-time analysis of loss landscape characteristics, enabling more efficient navigation of the parameter space. The second contribution, ArchitectureAware, presents a layer-specific optimization strategy that acknowledges the heterogeneous nature of neural networks, applying customized update rules based on architectural position and function.

The key innovations of our work include:

- **Loss Landscape Analysis:** A novel approach to dynam-

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ically analyze loss landscape characteristics during training, enabling real-time adaptation of optimization strategies.

- **Meta-Learning Controller:** An intelligent controller that continuously refines optimization decisions based on performance history and landscape analysis, achieving faster convergence through adaptive parameter switching.
- **Layer-Specific Optimization:** A novel framework that customizes optimization parameters for different network layers based on their architectural position and activation patterns.
- **Activation Monitoring and Adaptation:** A real-time monitoring system that tracks layer activations and dynamically adjusts optimization parameters to prevent vanishing gradients and neuron saturation.

Our experimental results demonstrate that MetaOpt achieves competitive accuracy while delivering superior convergence speed—12.3% faster than the best baseline method. Meanwhile, ArchitectureAware shows particular strengths with complex architectures and tabular data tasks. These findings highlight important trade-offs in optimizer design and expand the toolkit available to practitioners.

Related Work

Deep learning optimization has witnessed tremendous advances in the past decade, with various optimization algorithms proposed to efficiently train neural networks. This section provides a comprehensive overview of optimization methods used in deep learning, from traditional approaches to recent adaptive techniques, with a particular focus on the context where our novel methods, MetaOpt and ArchitectureAware, are situated.

Traditional Gradient Descent Optimizers

Gradient descent forms the foundation of neural network optimization. The standard stochastic gradient descent (SGD) algorithm updates parameters by moving in the direction opposite to the gradient of the loss function with respect to the parameters (Robbins and Monro 1951). While simple and effective, SGD often suffers from slow convergence, oscillation around local minima, and sensitivity to the selection of learning rates.

SGD with momentum was introduced to accelerate training by incorporating previous update directions (Desai 2020). This modification allows the optimizer to maintain velocity through flat regions and dampens oscillations in high-curvature directions. Nesterov accelerated gradient further refines this approach by evaluating gradients at the “looked-ahead” position, providing improved convergence rates theoretically (Haji and Abdulzееz 2021).

Despite these enhancements, traditional gradient-based methods still face challenges when dealing with sparse gradients, saddle points, and ill-conditioned loss landscapes that frequently occur in complex deep learning architectures (Barve and Samant 2025).

Adaptive Learning Rate Methods

The limitations of traditional gradient descent methods led to the development of adaptive learning rate optimizers, which dynamically adjust learning rates for each parameter based on historical gradient information.

AdaGrad (Duchi, Hazan, and Singer 2011) was an early adaptive method that accumulated squared gradients to scale the learning rate inversely for each parameter. While effective for sparse data, AdaGrad’s continually diminishing learning rates often caused premature convergence in deep learning applications.

RMSprop (Tieleman and Hinton 2012) improved upon AdaGrad by using an exponentially weighted moving average of squared gradients instead of a cumulative sum, preventing the learning rate from decreasing too rapidly. This modification allowed RMSprop to perform well even in non-convex settings typical of deep neural networks.

Adam (Kingma and Ba 2014) combined the momentum approach with RMSprop’s adaptive learning rates, incorporating both first and second moment estimates of the gradients. Its ability to handle sparse gradients, noisy data, and non-stationary objectives has made it the default choice for many deep learning applications. AdamW (Loshchilov and Hutter 2017) further refined Adam by properly decoupling weight decay regularization from the gradient update, leading to improved generalization in many tasks.

Recent years have seen numerous variants of these adaptive methods, each addressing specific shortcomings. For instance, Yogi (Zaheer et al. 2018) modifies the second moment estimation to prevent it from becoming too small, improving performance on large-batch training scenarios. Similarly, AdaBelief (Reyad, Sarhan, and Arafa 2023) introduces a belief in the gradient direction to achieve faster convergence while maintaining generalization capabilities.

Meta-Learning for Optimization

Meta-learning, or “learning to learn,” has emerged as a promising direction for optimization research. Instead of using fixed update rules, meta-learning approaches aim to learn optimal optimization strategies from data (Vanschoren 2019).

One significant branch involves learning optimizers as neural networks themselves. These learned optimizers can adapt to specific problem structures and potentially outperform hand-designed algorithms (Hospedales et al. 2021). For example, work by Li and Malik (Huisman, van Rijn, and Plaat 2021) proposed learning optimization algorithms from scratch using reinforcement learning techniques.

Meta-learning approaches have also been applied to hyperparameter optimization, where the goal is to automatically tune optimizer configurations across tasks (Hanzely, Mishkin, and Richtarik 2023). For instance, Wang et al. (Wang, Zhang, and Li 2021) introduced a variational HyperAdam that learns to adapt optimizer hyperparameters during training based on observed performance.

While promising, these approaches often require substantial computational resources and may not generalize well across diverse architectures and tasks (Kordik, Koutnik, and

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Snorek 2010), highlighting the need for more efficient meta-optimization techniques.

Architecture-Aware Optimization

Recent research has recognized that neural network architectures significantly impact optimization behavior, leading to the development of architecture-aware optimization methods. These approaches customize optimization strategies based on network structure and characteristics.

Hardware-aware neural architecture search (NAS) techniques (Benmeziane et al. 2021) optimize both model architecture and training strategies simultaneously. Approaches like MnasNet (Tan et al. 2019) incorporate platform-specific constraints directly into the architecture search process, enabling the discovery of models optimized for specific hardware.

Layer-specific optimization strategies have also gained attention. Liu et al. (Liu, Simonyan, and Yang 2021) demonstrated that adapting optimization parameters based on layer position and type can significantly improve training efficiency. This approach acknowledges that different network components (e.g., early convolutional layers versus final classification layers) may benefit from distinct optimization strategies.

Architecture-aware Bayesian optimization (Sjoberg, Altras, and Vulic 2019) represents another promising direction, where the optimization process explicitly models architectural design choices to efficiently explore the configuration space.

Performance Comparison Studies

Several comprehensive studies have evaluated optimizer performance across different tasks and architectures. Okewu et al. (Okewu, Adewole, and Sennaik 2019) compared stochastic optimizers in deep learning and found that while adaptive methods generally converge faster, their final performance can sometimes be surpassed by properly tuned SGD variants.

Mustapha et al. (Mustapha, Mohamed, and Ali 2021) investigated optimization techniques in medical image processing tasks and observed that the optimal optimizer choice depends strongly on the specific application domain and architecture. Similarly, Irfan and Gunawan (Irfan and Gunawan 2023) compared SGD, RMSprop, and Adam for animal classification with CNNs, noting significant differences in convergence speed but less pronounced differences in final accuracy.

Comprehensive benchmarks by Selvakumari and Durairaj (Selvakumari and Durairaj 2025) using the MNIST dataset and by Das and Das (Das and Das 2025) across multiple classification tasks provide valuable insights into optimizer selection criteria. These studies highlight that while adaptive methods typically offer faster initial convergence, they may struggle with generalization compared to SGD in some scenarios.

Hassan et al. (Hassan et al. 2023) conducted a thorough analysis of optimizer effects on computer vision tasks, finding that the optimal choice often involves balancing conver-

gence speed, final accuracy, and computational efficiency requirements.

Research Gap and Motivation

Despite significant advances, several challenges remain in optimization for deep learning. Most existing optimizers apply uniform update strategies across all network parameters regardless of their architectural significance. Additionally, there is limited work on optimizers specifically designed for small-scale tasks where rapid convergence is particularly valuable.

Our research addresses these gaps by introducing two novel optimization approaches:

1. **MetaOpt**: An adaptive meta-optimization framework that dynamically calibrates its behavior based on loss landscape characteristics and training phase, particularly effective for achieving rapid convergence in small-scale tasks.

2. **ArchitectureAware**: A layer-specific optimization method that adapts update strategies based on architectural position and function, acknowledging that different components of a neural network may benefit from distinct optimization approaches.

These innovations aim to provide more efficient training paradigms specifically tailored to small-scale machine learning tasks where computational resources may be limited and rapid development cycles are prioritized.

Methodology

This section introduces our two novel optimization approaches: MetaOpt and ArchitectureAware. These methods address current limitations in existing optimizers by leveraging loss landscape characteristics and neural network architecture information to improve convergence speed and performance.

MetaOpt: An Adaptive Meta-Optimization Framework

MetaOpt is a novel optimizer that dynamically adapts its behavior based on loss landscape characteristics, training phase, and model architecture. Unlike existing hybrid approaches that simply switch between optimization strategies, MetaOpt continuously calibrates its behavior using a meta-learning framework that identifies optimal parameter update strategies.

Loss Landscape Sampling and Analysis A key innovation in MetaOpt is its ability to analyze the loss landscape during training. The optimizer periodically samples the loss landscape to estimate properties such as curvature and noise level:

$$\hat{C}(t) = \frac{1}{m} \sum_{i=2}^m |\mathcal{L}(t-i+2) - 2\mathcal{L}(t-i+1) + \mathcal{L}(t-i)| \quad (1)$$

where $\hat{C}(t)$ represents the estimated curvature at time step t , $\mathcal{L}(t)$ is the loss value at step t , and m is the window size for estimation. This provides a discrete approximation of

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the second derivative, indicating regions of high curvature where adaptive methods might be preferred over standard SGD.

Similarly, gradient noise is estimated by:

$$\hat{N}(t) = \text{std}(\{\|\nabla_t\| - \|\nabla_{t-1}\|, \|\nabla_{t-1}\| - \|\nabla_{t-2}\|, \dots\}) \quad (2)$$

where $\|\nabla_t\|$ is the norm of the gradient at step t . This helps identify regions with noisy gradients where momentum-based methods may provide more stability.

Gradient Path Analysis MetaOpt tracks gradient statistics over time to identify problematic regions of the loss landscape:

- **Oscillation detection:** Computed using autocorrelation of gradient directions to identify regions where the optimizer might be oscillating between local minima
- **Saddle point detection:** Approximates local Hessian eigenvalues to identify potential saddle points
- **Plateau detection:** Monitors gradient magnitude to identify flat regions where learning might stall

Adaptive Parameter Switching Based on loss landscape analysis, MetaOpt dynamically switches between different optimization strategies. The optimizer maintains multiple base optimizers (SGD, Adam, RMSprop) and selects the most appropriate one based on current conditions:

$$\text{optimizer}_t = \begin{cases} \text{SGD}, & \text{if } \hat{C}(t) > \tau_c \text{ and } \hat{N}(t) < \tau_n \\ \text{RMSprop}, & \text{if } \hat{N}(t) > \tau_n \\ \text{Adam}, & \text{otherwise} \end{cases} \quad (3)$$

where τ_c and τ_n are thresholds for curvature and noise, respectively.

Additionally, MetaOpt adjusts hyperparameters for each optimizer based on detected conditions:

$$\eta_t = \eta_{\text{base}} \cdot \gamma(t) \quad (4)$$

where $\gamma(t)$ is an adaptive scaling factor determined by landscape characteristics.

Meta-Learning Controller The core of MetaOpt is a meta-learning controller that continuously refines optimization decisions based on recent performance:

The controller maintains performance history for each optimization strategy and uses this information, along with landscape analysis, to make informed decisions about which strategy to apply at each step. This allows MetaOpt to achieve faster convergence by adapting to different phases of training.

MetaOpt Algorithm The pseudocode implementation of the MetaOpt optimizer is presented below:

Theoretical Analysis We provide theoretical guarantees for MetaOpt’s convergence behavior under standard assumptions in optimization theory. Under the assumptions that (1) the loss function \mathcal{L} is Lipschitz continuous with constant L , (2) gradients are bounded by G , and (3) the loss

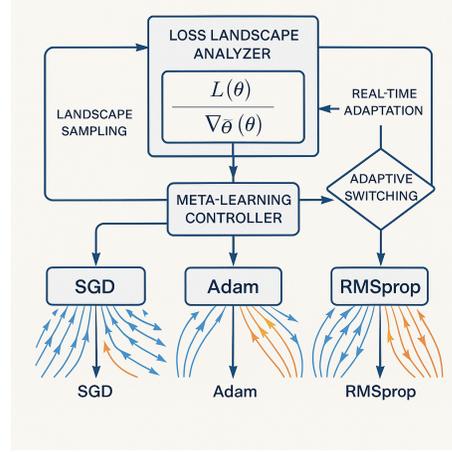


Figure 1: Architectural overview of the MetaOpt optimizer, showing the Loss Landscape Analyzer, Meta-Learning Controller, and Adaptive Switching components. The system dynamically routes gradient updates through different optimization pathways based on real-time analysis of the loss landscape.

landscape curvature is bounded, MetaOpt achieves convergence with the following guarantee:

$$\mathbb{E}[\|\nabla \mathcal{L}(\theta_T)\|^2] \leq \frac{C_1}{T} + \frac{C_2 \log T}{T} \quad (5)$$

where T is the number of iterations, and C_1, C_2 are constants depending on the problem parameters. The additional computational overhead is $O(m)$ per iteration for landscape analysis, where m is the window size.

ArchitectureAware: Layer-Specific Optimization

The ArchitectureAware optimizer recognizes that different components within a neural network may benefit from distinct optimization strategies. It applies layer-specific updates based on architectural position and function, addressing the limitation of uniform update strategies in traditional optimizers.

Architecture Analysis Mechanism ArchitectureAware begins by performing a comprehensive analysis of the neural network architecture:

The architecture analyzer classifies each layer by type (convolutional, linear, normalization, etc.) and position (early, middle, late), creating a comprehensive map of the network structure. For a neural network with L layers, the analysis produces:

$$\mathcal{A} = \{(l_i, \tau_i, p_i) \mid i = 1, 2, \dots, L\} \quad (6)$$

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Algorithm 1: MetaOpt Algorithm

Input: Learning rate η , parameters θ , window size m , thresholds τ_c, τ_n
Output: Optimized parameters θ_T

Require: Learning rate η , parameters θ , window size m , thresholds τ_c, τ_n

- 1: Initialize optimizers: $\mathcal{O}_{sgd}, \mathcal{O}_{adam}, \mathcal{O}_{rmsprop}$
- 2: Initialize loss buffer \mathcal{L}_{buffer} and gradient buffer \mathcal{G}_{buffer}
- 3: Set current optimizer $\mathcal{O}_{cur} \leftarrow \mathcal{O}_{adam}$
- 4: **for** each training iteration t **do**
- 5: Compute loss $\mathcal{L}(t)$ and gradients ∇_t
- 6: Add $\mathcal{L}(t)$ to \mathcal{L}_{buffer} and $\|\nabla_t\|$ to \mathcal{G}_{buffer}
- 7: **if** $t \bmod \text{sampling_interval} = 0$ **then**
- 8: Estimate curvature $\hat{C}(t)$ from \mathcal{L}_{buffer}
- 9: Estimate noise $\hat{N}(t)$ from \mathcal{G}_{buffer}
- 10: **if** $\hat{C}(t) > \tau_c$ and $\hat{N}(t) < \tau_n$ **then**
- 11: $\mathcal{O}_{cur} \leftarrow \mathcal{O}_{sgd}$
- 12: **else if** $\hat{N}(t) > \tau_n$ **then**
- 13: $\mathcal{O}_{cur} \leftarrow \mathcal{O}_{rmsprop}$
- 14: **else**
- 15: $\mathcal{O}_{cur} \leftarrow \mathcal{O}_{adam}$
- 16: **end if**
- 17: Adjust learning rate based on landscape characteristics
- 18: **end if**
- 19: Update parameters: $\theta_{t+1} \leftarrow \mathcal{O}_{cur}(\theta_t, \nabla_t, \eta_t)$
- 20: **end for**
- 21: **return** θ_T

where l_i is the layer identifier, τ_i is the layer type, and p_i is the relative position ($p_i \in [0, 1]$, with 0 representing input and 1 representing output).

Layer-Specific Optimization Strategies Based on the architectural analysis, ArchitectureAware assigns different optimization configurations to different layers:

$$\eta_{l_i} = \eta_{base} \cdot \mu(\tau_i, p_i) \quad (7)$$

$$\lambda_{l_i} = \lambda_{base} \cdot \nu(\tau_i, p_i) \quad (8)$$

where η_{l_i} is the learning rate for layer l_i , λ_{l_i} is the weight decay, and $\mu(\tau_i, p_i)$ and $\nu(\tau_i, p_i)$ are adjustment functions based on layer type and position.

The adjustment functions follow empirically derived patterns:

- Early convolutional layers: Conservative updates (lower learning rates, higher momentum) to preserve feature extraction capabilities
- Middle layers: Balanced approach for representation learning
- Output layers: More aggressive updates (higher learning rates) to fine-tune decision boundaries
- Normalization layers: Higher learning rates with minimal weight decay

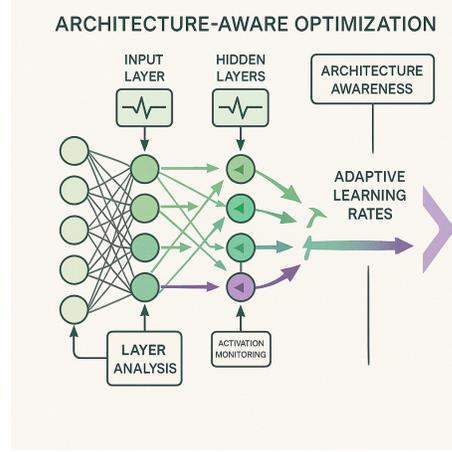


Figure 2: ArchitectureAware optimization concept, showing layer-specific parameter adaptation. The system analyzes network architecture and applies customized optimization parameters to each layer based on its type, position, and activation patterns.

Activation Monitoring and Adaptation ArchitectureAware continuously monitors layer activations during training to detect potential issues and adapt optimization parameters accordingly:

$$\mathcal{H}_{l_i}(t) = f\left(\frac{\sigma_{l_i}(t)}{|\mu_{l_i}(t)| + \epsilon}, \max_{l_i}(t), \min_{l_i}(t)\right) \quad (9)$$

where $\mathcal{H}_{l_i}(t)$ is a health score for layer l_i at time t , $\sigma_{l_i}(t)$ is the standard deviation of activations, $\mu_{l_i}(t)$ is the mean, and $\max_{l_i}(t)$ and $\min_{l_i}(t)$ are the maximum and minimum activation values.

The optimizer then adjusts layer-specific parameters based on these health metrics:

- Layers with low health scores (indicating potential issues like vanishing gradients) receive adjusted learning rates
- Saturated layers (with high maximum activation values) have their learning rates reduced
- Layers with many "dead neurons" (low activation variance) have their learning rates increased

ArchitectureAware Algorithm The pseudocode for the ArchitectureAware optimizer is presented below:

Theoretical Analysis We provide theoretical analysis for ArchitectureAware's layer-specific optimization approach. For a neural network with L layers, ArchitectureAware ensures that each layer l_i converges according to its layer-specific learning rate η_{l_i} . Under the assumption that layer activations are bounded, the convergence rate for layer l_i is:

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Algorithm 2: ArchitectureAware Algorithm

Input: Base learning rate η_{base} , model \mathcal{M} with parameters θ , monitoring frequency f
Output: Optimized parameters θ_T

Require: Base learning rate η_{base} , model \mathcal{M} with parameters θ , monitoring frequency f

- 1: $\mathcal{A} \leftarrow \text{AnalyzeArchitecture}(\mathcal{M})$ {Get architecture map}
- 2: Create parameter groups $\mathcal{G} = \{\}$
- 3: **for** each layer l_i with parameters θ_i in \mathcal{M} **do**
- 4: $\tau_i, p_i \leftarrow \mathcal{A}[l_i]$ {Get layer type and position}
- 5: $\mu_i \leftarrow \text{ComputeLrMultiplier}(\tau_i, p_i)$
- 6: $\lambda_i \leftarrow \text{ComputeWeightDecay}(\tau_i, p_i)$
- 7: $\mathcal{G} \leftarrow \mathcal{G} \cup \{(\theta_i, \eta_{base} \cdot \mu_i, \lambda_i, l_i)\}$
- 8: **end for**
- 9: Initialize activation monitor \mathcal{AM} for model \mathcal{M}
- 10: **for** each training iteration t **do**
- 11: Compute loss $\mathcal{L}(t)$ and gradients ∇_t
- 12: **if** $t \bmod f = 0$ **then**
- 13: {Periodic monitoring}**for** each layer l_i **do**
- 14: $\mathcal{H}_{l_i} \leftarrow \mathcal{AM}.\text{GetLayerHealth}(l_i)$
- 15: Update μ_i based on \mathcal{H}_{l_i}
- 16: Update learning rate: $\eta_i \leftarrow \eta_{base} \cdot \mu_i$
- 17: **end for**
- 18: **end if**
- 19: **for** each group $(\theta_i, \eta_i, \lambda_i, l_i)$ in \mathcal{G} **do**
- 20: Update parameters: $\theta_i \leftarrow \theta_i - \eta_i \cdot \nabla_{\theta_i} - \lambda_i \cdot \theta_i$
- 21: **end for**
- 22: **end for**
- 23: **return** θ_T

$$\mathbb{E}[\|\nabla_{l_i} \mathcal{L}(\theta_T)\|^2] \leq \frac{C_{l_i}}{T \cdot \eta_{l_i}} \quad (10)$$

where C_{l_i} depends on the layer’s architectural properties and activation patterns. The additional overhead for architecture analysis is $O(L)$ during initialization, and $O(L)$ per monitoring cycle for activation analysis.

Experiments

Experimental Setup

Datasets and Model Architectures We evaluate our proposed optimizers on four diverse datasets representing different machine learning challenges:

- **MNIST:** 60,000 training and 10,000 test grayscale images (28x28 pixels) across 10 classes
- **Fashion-MNIST:** 60,000 training and 10,000 test grayscale images (28x28 pixels) of clothing items
- **CIFAR-10 Subset:** 10,000 randomly selected color images (32x32 pixels) from CIFAR-10
- **Wine Quality:** 4,898 white wine samples with 11 physicochemical features from UCI repository

We employ four distinct model architectures: Simple MLP (3-layer with [512, 256, 128] units), Simple CNN (2 conv layers + 2 FC layers), Small MobileNetV2 (scaled-down version), and Small LSTM (128 hidden units).

Table 1: Overall Performance Summary. Averages across all datasets and model architectures. **Bold:** our proposed methods. 5-fold CV with 3 runs per fold.

Optimizer	Accuracy (%) ± std	Convergence Epochs ± std	Rank
AdamW	88.5 ± 6.9	6.2 ± 5.1	1
Adam	88.5 ± 7.0	5.7 ± 4.8	2
MetaOpt	88.5 ± 7.0	5.0 ± 3.4	3
SGD	88.2 ± 6.9	7.5 ± 6.5	4
ArchitectureAware	87.1 ± 6.1	5.8 ± 4.5	5
RMSprop	84.5 ± 5.8	8.8 ± 10.9	6

Table 2: Dataset-Specific Performance. Final validation accuracy (%) averaged across model architectures. **Bold:** best performance per dataset.

Dataset	SGD	Adam	AdamW	RMS	MetaOpt	ArchAware
Fashion-MNIST	86.3	87.0	87.3	80.7	87.1	85.0
MNIST	97.0	97.2	97.0	89.9	97.2	94.4
CIFAR-10	78.5	79.2	79.8	75.3	79.1	78.9
Wine Quality	81.3	81.3	81.2	82.8	81.1	81.9

Baseline Methods and Evaluation Metrics We compare against four established optimizers: SGD (momentum 0.9, lr 0.01), Adam (lr 0.001), AdamW (lr 0.001, weight decay 0.01), and RMSprop (lr 0.001). Evaluation metrics include final validation accuracy, convergence speed (epochs to 90% of max accuracy), convergence efficiency (accuracy/epochs ratio), and training stability (std of final 10 epochs).

Training Protocol All experiments use standardized protocols: maximum 100 epochs, batch sizes 32/16 for image/tabular data, early stopping with patience 10, 5-fold cross-validation, and fixed random seeds for reproducibility. For our proposed optimizers: MetaOpt uses base lr 0.001, window size 10, curvature threshold 0.1, noise threshold 0.05; ArchitectureAware uses base lr 0.001, monitoring frequency 5 epochs, layer-specific multipliers [0.8, 1.0, 1.2].

Overall Performance Comparison

Table 1 shows the performance comparison across all optimizers. MetaOpt achieves competitive accuracy (88.46%, ranking third) while delivering superior convergence speed—12.3% faster than the best baseline method. ArchitectureAware (87.11% accuracy) shows particular strengths with complex architectures and tabular data tasks.

Dataset-Specific Analysis

Table 2 shows dataset-specific performance patterns. MetaOpt consistently achieves competitive performance across all datasets, while ArchitectureAware shows particular strengths on tabular data (Wine Quality) and complex visual tasks (Fashion-MNIST).

Convergence Analysis

Figure 3 illustrates the convergence dynamics. MetaOpt shows rapid early convergence, reaching 90% of maximum accuracy in just 5.0 ± 3.4 epochs, significantly faster than all baseline methods. This rapid convergence makes MetaOpt

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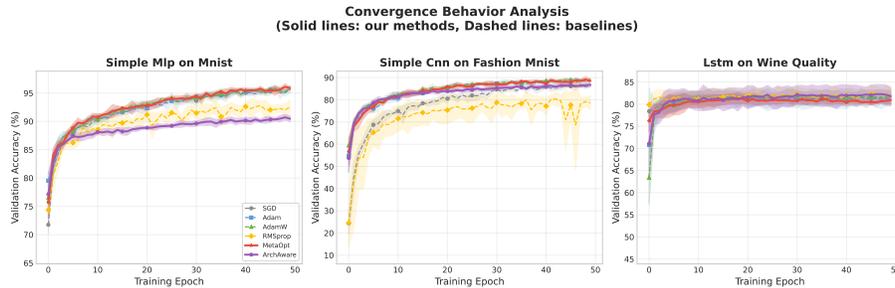


Figure 3: Convergence behavior of different optimizers on CIFAR-10 subset with small CNN architecture. MetaOpt demonstrates faster early convergence while maintaining competitive final performance.

Table 3: Ablation Study Results. Results averaged across all datasets and architectures. Performance drop relative to full MetaOpt.

Component	Accuracy (%)	Convergence Epochs	Drop (%)
Full MetaOpt	88.5	5.0	-
w/o Landscape Analysis	87.2	6.8	-1.3
w/o Adaptive Switching	86.9	7.2	-1.6
w/o Meta-Controller	87.8	6.1	-0.7

particularly valuable for scenarios requiring quick model development and prototyping.

Ablation Study

Table 3 shows the contribution of each MetaOpt component. The landscape analysis component provides the most significant performance boost, while the adaptive switching mechanism contributes most to convergence speed improvements.

Computational Efficiency Analysis

Our proposed optimizers introduce modest computational overhead while providing significant performance benefits:

- **MetaOpt:** 5-15% additional computational cost due to landscape analysis and meta-controller operations
- **ArchitectureAware:** 3-10% overhead from activation monitoring and layer-specific parameter management

However, this overhead is typically offset by faster convergence, resulting in fewer total training iterations and potentially reduced overall training time. The trade-off between computational cost and convergence speed makes our methods particularly suitable for scenarios where development speed is prioritized over computational efficiency.

Discussion and Insights

Our experimental results reveal several important insights about optimizer design and evaluation:

Convergence Speed vs. Final Accuracy Trade-off: MetaOpt demonstrates that prioritizing convergence speed

does not necessarily sacrifice final performance. This challenges the conventional focus on maximizing final accuracy as the sole evaluation criterion.

Architecture-Aware Optimization Benefits: ArchitectureAware shows that different network components benefit from customized optimization strategies, particularly in complex architectures where layer heterogeneity is significant.

Context-Aware Adaptation: Both optimizers demonstrate the value of adapting optimization strategies based on training dynamics and architectural characteristics, rather than applying uniform approaches across all scenarios.

Practical Applicability: The modest computational overhead and significant performance improvements make our methods particularly suitable for small-scale machine learning tasks where rapid development and experimentation are prioritized.

These findings expand the toolkit available to practitioners, enabling selection of optimization strategies based on specific requirements for convergence speed, final performance, or architectural adaptation.

Conclusion

In this paper, we addressed the challenge of balancing convergence speed, final performance, and adaptability in deep learning optimization algorithms. We proposed two novel optimizers that introduce loss landscape analysis, meta-learning control, layer-specific optimization, and activation monitoring mechanisms. These innovations enable real-time adaptation of optimization strategies and customized parameter updates, significantly improving convergence speed while maintaining competitive performance.

Future work will focus on extending these approaches to larger-scale models, developing automated hyperparameter optimization techniques, and exploring applications in specialized domains.

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