

# AFFINITYFLOW: GUIDED FLOWS FOR ANTIBODY AFFINITY MATURATION

**Can (Sam) Chen<sup>\*†</sup>**  
MILA – Quebec AI Institute

**Karla-Luise Herpoldt**  
Amazon

**Chenchao Zhao**  
Amazon

**Zichen Wang**  
Amazon

**Marcus Collins<sup>‡</sup>**  
Amazon

**Shang Shang**  
Amazon

**Ron Benson**  
Amazon

## ABSTRACT

Antibodies are widely used as therapeutics, but their development requires costly affinity maturation, involving iterative mutations to enhance binding affinity. This paper explores a sequence-only scenario for affinity maturation, using solely antibody and antigen sequences. Recently AlphaFlow wraps AlphaFold within flow matching to generate diverse protein structures, enabling a sequence-conditioned generative model of structure. Building on this, we propose an *alternating optimization* framework that **(1)** fixes the sequence to guide structure generation toward high binding affinity using a structure-based affinity predictor, then **(2)** applies inverse folding to create sequence mutations, refined by a sequence-based affinity predictor for post selection. To address this, we develop a *co-teaching* module that incorporates valuable information from noisy biophysical energies into predictor refinement. The sequence-based predictor selects consensus samples to teach the structure-based predictor, and vice versa. Our method, *AffinityFlow*, achieves state-of-the-art performance in affinity maturation experiments.

## 1 INTRODUCTION

Natural antibodies protect organisms by specifically binding to target antigens such as viruses and bacteria with high affinity Murphy & Weaver (2016), while therapeutic antibodies bind various targets to inactivate them, recruit immune cells to them, or deliver an attached drug compound Chiu & Gilliland (2016). When developing a therapeutic antibody, *in vitro* affinity maturation—through targeted mutation and selection—improves the binding affinity of existing antibodies to target antigens Tabasinezhad et al. (2019); Chiu & Gilliland (2016).

These *in vitro* methods, such as random mutagenesis, are labor-intensive and time-consuming. Recent advancements in deep learning have propelled *in silico* affinity maturation forward. One line of research enhances affinity prediction for mutated antibodies Shan et al. (2022); Liu et al. (2021); Cai et al. (2024); Lin et al. (2024); Xiong et al. (2017); another investigates mutation strategies. Specifically, protein language models propose plausible mutations to enhance binding affinities, though they lack specificity for target antigens Hie et al. (2024); Ruffolo et al. (2021); Shuai et al. (2021). Similarly, diffusion models guide the sampling towards high-affinity antibody sequences but require the often unavailable or insufficiently accurate antigen-antibody complex structure Luo et al. (2022); Zhou et al. (2024). Our research aligns more with the second line of mutation strategies. In particular, we focus on enhancing antibody binding affinity through sequence mutations, relying solely on the antigen-antibody sequence.

Recognizing the crucial link between antibody structure and function, it is essential to integrate structure into the sequence mutation process. The recent release of AlphaFlow Jing et al. (2024) builds a sequence-conditioned generative model of protein structure, which opens pathways

<sup>\*</sup>can.chen@mila.quebec/chencan421@gmail.com

<sup>†</sup>Work done during an Amazon internship

<sup>‡</sup>collmr@amazon.com

for structure-based optimization of antibody sequences. Specifically, AlphaFlow repurposes AlphaFold Jumper et al. (2021) in flow matching to generate diverse protein conformations.

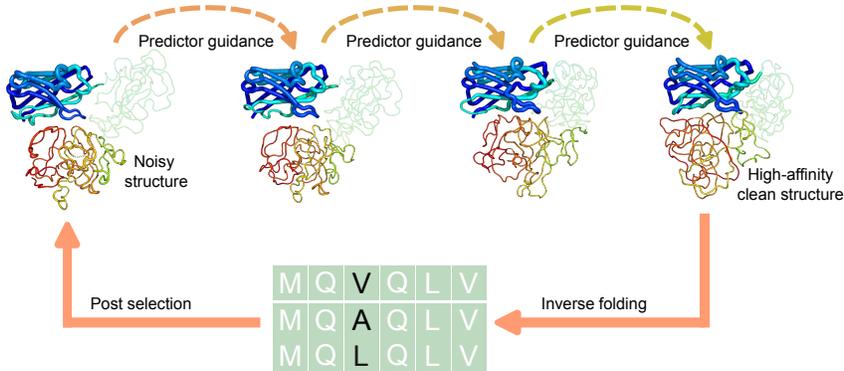


Figure 1: Illustration of *alternating optimization*.

This motivates the proposal of an *alternating optimization* framework, as illustrated in Figure 1: (1) We fix the sequence to guide noisy structures toward high-affinity clean structures. Rather than re-training the entire AlphaFlow model—a process that is inherently time-consuming—we achieve guided structure generation through predictor guidance Dhariwal & Nichol (2021). Specifically, a trained structure-based affinity predictor is integrated into the AlphaFlow sampling process to direct coordinate denoising. (2) With the high-affinity clean structure, we perform inverse folding to introduce targeted mutations, and use a sequence-based predictor for post selection, which identifies promising mutated sequences for the next iteration.

A significant challenge in training both predictors is the scarcity of labeled data. To address this, we develop a *co-teaching* module that leverages valuable information from noisy biophysical energies to refine the predictors, as shown in Figure 2. For any antigen  $i$  and antibodies  $j, k, m, n$ , we use Rosetta Alford et al. (2017) to compute the binding free energy  $\Delta G$  and then calculate the change in binding free energy  $\Delta\Delta G_{ijk} = \Delta G_{ij} - \Delta G_{ik}$  to form pairwise discrete labels. The sequence-based predictor selects pairs with which it concurs, considering them likely to be accurate and informative, and uses these consensus samples to enhance the structure-based predictor. For instance, if the sequence-based predictor predicts  $\Delta\Delta\hat{G}_{ijk} > 0$ , it selects  $\Delta\Delta G_{ijk} > 0$  for training the structure-based predictor. Similarly, the structure-based predictor reciprocates by informing the sequence-based predictor; for example, it selects  $\Delta\Delta G_{ijm} < 0$  to refine the sequence predictor, as shown in Figure 2. Noisy data, such as  $\Delta\Delta G_{ijn} > 0$ , are filtered out. This module effectively

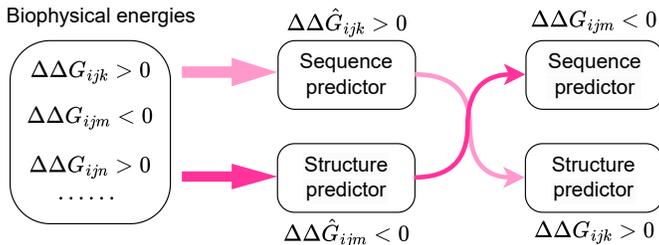


Figure 2: Illustration of *co-teaching*.

integrates biophysical insights into both predictors, enhancing their accuracy.

In summary, we introduce *AffinityFlow*, guided flows for antibody affinity maturation. *AffinityFlow* achieves state-of-the-art performance in affinity maturation experiments.

## 2 PRELIMINARIES

### 2.1 PROBLEM DEFINITION

Binding affinity between an antibody (Ab) and its antigen (Ag) is predominantly determined by the complementarity determining regions (CDRs) within these chains Akbar et al. (2022). We model an antibody chain as a sequence of amino acids, each characterized by a type  $a_i \in \{A, C, D, \dots, Y\}$ . While *AffinityFlow* is applicable to all antibody types, this study specifically focuses on single-domain antibodies (sdAb), which consist only of heavy chains Wesolowski et al. (2009). We select sdAb for their high specificity, solubility, stability, and lower toxicity and immunogenicity.

Our goal in affinity maturation is to effectively mutate the CDRs within the context of the entire Ab-Ag sequence complex to improve binding affinity.

### 2.2 ALPHAFLOW

AlphaFold Jumper et al. (2021) serves as a single-state protein structure predictor, and AlphaFlow Jing et al. (2024) repurposes AlphaFold within a flow matching framework to generate diverse protein conformations. Given a protein sequence  $\mathbf{a}$  of length  $N$ , the objective is to model the structural ensemble, denoted by  $p(\mathbf{x} | \mathbf{a})$ , where  $\mathbf{x} \in \mathbb{R}^{3 \times N}$  represents the protein 3D coordinates.

AlphaFlow defines the conditional probability path by sampling initial noise  $\mathbf{x}_0$  from  $q(\mathbf{x}_0)$  and linearly interpolating it with the data point  $\mathbf{x}_1$ :

$$\mathbf{x} | \mathbf{x}_1, t = (1 - t) \cdot \mathbf{x}_0 + t \cdot \mathbf{x}_1, \quad \mathbf{x}_0 \sim q(\mathbf{x}_0) \quad (1)$$

The vector field is derived as:

$$u_t(\mathbf{x} | \mathbf{x}_1) = (\mathbf{x}_1 - \mathbf{x}) / (1 - t) \quad (2)$$

The marginal vector field is parameterized in terms of a neural network  $\hat{\mathbf{x}}_1(\mathbf{x}, t; \boldsymbol{\theta})$  as:

$$\hat{v}(\mathbf{x}, t; \boldsymbol{\theta}) = (\hat{\mathbf{x}}_1(\mathbf{x}, t; \boldsymbol{\theta}) - \mathbf{x}) / (1 - t) \quad (3)$$

This approach allows the reuse of the AlphaFold2 template embedding stack to reconstruct the clean structure  $\mathbf{x}_1$  from the noisy input  $\mathbf{x}$ , with  $t$  serving as an additional time embedding. The model focuses on the 3D coordinates of  $\beta$ -carbons (or  $\alpha$ -carbon for glycine), defining the prior distribution  $q(\mathbf{x})$  over these positions as a harmonic prior Jing et al. (2023) to ensure that inputs to the neural network remain physically plausible. Since AlphaFlow is trained solely on single proteins, this study connects the antibody sequence and the antigen sequence into one sequence using a linker of 32 *GGGS* repeats Lin et al. (2023). The linked sequence complex is then input into the system.

### 2.3 AFFINITY PREDICTION

This paper focuses on enhancing binding affinity, determined by the difference in free energy between the bound and unbound states, denoted  $\Delta G$ . Thus, we predict  $\Delta G$  as a measure of binding affinity. Protein properties can be predicted from two views: sequence and structure.

Leading sequence-based models like ESM-2 Lin et al. (2022), AntiBERTy Ruffolo et al. (2021), and IgLM Shuai et al. (2023) are pre-trained on extensive unlabeled protein sequences. These models extract hidden representations to predict properties such as binding energy, denoted as  $f_\alpha(\Delta G | \mathbf{a})$ , where  $\alpha$  represents the model parameters. We choose ESM-2 as our sequence-based predictor due to its versatility, as the antigen is a general protein rather than an antibody. Specifically, we input the antibody and antigen sequences separately into ESM-2 to obtain embeddings, which are then concatenated and fed into a three-layer MLP for the final prediction.

For structure-based prediction, the GVP model is notable for utilizing features from the 3D graph of proteins to predict properties, denoted as  $f_\beta(\Delta G | \mathbf{x})$  Jing et al. (2021). Integrating the ESM2 model as a feature extractor within the GVP model further enhances performance Wang et al. (2022). Thus, we employ the ESM2-GVP model as our structure-based predictor in this study. The linked antibody-antigen complex is processed by the pre-trained ESM2 to generate residue embeddings, from which intersected residues are selected for the GVP model.

Related works on generative protein modeling and co-teaching are detailed in Appendix A.1.

### 3 METHOD

#### 3.1 ALTERNATING OPTIMIZATION

Initially, the sequence is fixed while we guide the Ab structure generation to achieve high binding affinity, supplemented with predictor-corrector refinement. Based on the generated structure, we then use inverse folding to introduce targeted mutations into the Ab, with the sequence-based predictor selecting promising sequences for the next iteration.

**Guided Structure Generation** While AlphaFlow generates structures unconditionally, we aim to steer structure generation toward improved binding affinity using predictor guidance. Following *Lemma 1* in Zheng et al. (2023), predictor guidance in flow matching is formulated as:

$$\tilde{v}(\mathbf{x}_t, t, \Delta G; \boldsymbol{\theta}) = \hat{v}(\mathbf{x}_t, t; \boldsymbol{\theta}) + \frac{1-t}{t} \nabla_{\mathbf{x}_t} \log p_{\beta}(\Delta G | \mathbf{x}_t, t). \quad (4)$$

where  $p_{\beta}(\Delta G | \mathbf{x}_t, t)$  denotes the target binding energy distribution. The derivation details are in Appendix A.2. Training the predictor at different time steps  $t$  is resource-intensive; instead, we approximate  $p_{\beta}(\Delta G | \mathbf{x}_t, t)$  directly from  $p_{\beta}(\Delta G | \hat{\mathbf{x}}_1(\mathbf{x}_t), 1)$ :

$$p_{\beta}(\Delta G | \mathbf{x}_t, t) \approx p_{\beta}(\Delta G | \hat{\mathbf{x}}_1(\mathbf{x}_t), 1). \quad (5)$$

This approximation, termed  $p_{\beta}(\Delta G | \hat{\mathbf{x}}_1(\mathbf{x}_t))$ , is effective when  $t$  is close to 1; therefore, we primarily apply predictor guidance in the later stages of sampling.

The desired binding energy distribution is formulated as Lee et al. (2023):

$$p_{\beta}(\Delta G | \hat{\mathbf{x}}_1(\mathbf{x}_t)) = e^{-\gamma \hat{f}_{\beta}(\hat{\mathbf{x}}_1(\mathbf{x}_t))} / Z, \quad (6)$$

where  $\gamma$  is a scaling factor and  $Z$  a normalization constant, with the negative sign indicating a preference for lower binding energy. Integrating this into Eq.(4) leads to:

$$\tilde{v}(\mathbf{x}_t, t, \Delta G; \boldsymbol{\theta}) = \hat{v}(\mathbf{x}_t, t; \boldsymbol{\theta}) - \gamma \frac{1-t}{t} \nabla_{\mathbf{x}_t} \hat{f}_{\beta}(\hat{\mathbf{x}}_1(\mathbf{x}_t)). \quad (7)$$

This vector field guides the sampling process towards lower binding energy. We target the predictor guidance only to CDR coordinates rather than the full protein to enhance its relevance.

**Sequence Mutation** Using the generated structure as a reference, we employ inverse folding with ProteinMPNN Dauparas et al. (2022) to identify potential mutations in the CDR regions. We introduce single-point, double-point, and triple-point mutations, and use the sequence-based predictor to select high-affinity variants for subsequent iterations. Since the generated structure is conditioned on the sequence, we avoid multiple simultaneous mutations to minimize disruptive structure changes.

#### 3.2 CO-TEACHING

A primary challenge is the scarcity of labeled data for training both structure-based and sequence-based affinity predictors. To address this, we enhance the predictors by incorporating insights from noisy biophysical energies.

**Complex Generation** To compute biophysical energies, initial protein complexes are required. We extract  $A$  sAb structures and  $B$  antigen structures from existing PDB files, and then use the docking tool GeoDock Chu et al. (2023) to generate  $AB$  complex structures. Next, we employ Rosetta Alford et al. (2017) to calculate the binding free energy  $\Delta G$  for each complex.

**Pairwise Discrete Data** Instead of relying on pointwise continuous samples, which can be highly variable and noisy, we generate robust pairwise discrete data. For the  $i$ -th antigen, we pair antibody  $j$  with antibody  $k$  and compute the change in binding free energy as  $\Delta \Delta G_{ijk} = \Delta G_{ij} - \Delta G_{ik}$ . We assign a pairwise label  $Y_{ijk}$  as 1 if  $\Delta \Delta G_{ijk} > 0$ , indicating stronger binding by antibody  $k$ , and 0 otherwise. This approach provides a more reliable measure than using absolute property values.

**Sample Selection** Given the potential noise from unreliable biophysical energy calculations, we implement a reciprocal filtering approach to refine the quality of input for each predictor. Each predictor selects samples that align with its predictions to inform the other. Specifically, the sequence-based predictor  $f_\alpha(\Delta G|\mathbf{a})$  computes  $\hat{Y}_{ijk}^a = (\Delta\Delta\hat{G}_{ijk}^a > 0)$ . If  $\hat{Y}_{ijk}^a = Y_{ijk}$ , this indicates probable accuracy, prompting us to use this consensus sample for the structure-based predictor. The structure-based predictor undergoes a similar process, creating a cyclical filtering system.

**Fine-tuning** With the selected samples, we aim to enhance the performance of our predictors. For the sequence-based predictor, we minimize the following loss function:

$$\mathcal{L}(\alpha) = - \sum_{i,j,k} \left[ Y_{ijk} \log p_\alpha(Y_{ijk} = 1) + (1 - Y_{ijk}) \log(1 - p_\alpha(Y_{ijk} = 1)) \right], \quad (8)$$

where  $p_\alpha(Y_{ijk} = 1) = \sigma(\Delta\hat{G}_{ij}^a - \Delta\hat{G}_{ik}^a)$  and  $\sigma(\cdot)$  is the sigmoid function. The structure-based predictor undergoes a similar fine-tuning process.

## 4 EXPERIMENTS

### 4.1 BENCHMARK

**Dataset** We conduct our experiments using a sdAb subset of the SABDab dataset Dunbar et al. (2014). Our study focuses on sdAbs, selecting PDB files of 120 labeled sdAb-antigen pairs to initially train our predictors. From these files, we extract 77 sdAbs and 54 antigens, resulting in 4, 158 docked complex structures generated by GeoDock. Rosetta is then used to calculate the  $\Delta G$  for these complexes. For maturation testing, we select 60 sdAb-antigen PDB files, ensuring that each antigen is unique and these antigens and antibodies were not included in the training set.

**Evaluation** Our evaluation considers mutations in CDR-H1, CDR-H2, CDR-H3, and the entire CDR region. Each method generates 3 mutated sequences per antigen, resulting in a total of 180 designs. We measure performance using three metrics: functionality, specificity, and rationality, following Ye et al. (2024). *Functionality* is assessed by the Improvement Percentage (*IMP*) as described in Luo et al. (2022). *IMP* reflects the proportion of mutated sdAbs with reduced binding energy compared to the original. Structures are predicted using IgFold Ruffolo et al. (2023), docked with GeoDock Chu et al. (2023), and binding energies are analyzed via Rosetta Alford et al. (2017). *Specificity* measures the sequence similarity among antibodies targeting different antigens. An effective method should generate distinct antibodies for different antigens, so lower similarity (*Sim*) indicates better specificity. *Rationality* is evaluated using inverse perplexity calculated by AntiBERTy Ruffolo et al. (2021). This metric, also referred to as naturalness (*Nat*), indicates that higher values of *Nat* generally reflect better rationality.

We report the baselines in Appendix A.4 and training details in Appendix A.5.

### 4.2 RESULTS AND ANALYSIS

Table 1: Overall performance comparison

Method	CDR-H1			CDR-H2			CDR-H3			All		
	IMP↑	Sim↓	Nat↑									
ESM	85.5%	0.559	<b>0.347</b>	72.9%	0.566	<b>0.358</b>	64.0%	0.573	<b>0.359</b>	84.1%	0.562	<b>0.361</b>
AbLang	88.0%	0.536	<u>0.330</u>	85.4%	0.537	<u>0.322</u>	<u>88.5%</u>	0.542	<u>0.336</u>	82.9%	0.548	<u>0.349</u>
nanoBERT	84.7%	<u>0.534</u>	0.322	85.9%	<u>0.536</u>	0.321	81.6%	0.537	0.328	86.0%	0.544	0.341
dWJS	82.7%	0.535	0.319	69.4%	0.537	0.304	66.1%	<u>0.522</u>	0.294	85.6%	0.545	0.317
DiffAb	85.5%	0.541	0.317	86.7%	0.548	0.318	85.6%	0.528	0.317	84.4%	<u>0.540</u>	0.316
AbDPO	<u>88.3%</u>	0.540	0.318	<u>91.1%</u>	0.545	0.318	87.8%	0.525	0.319	<u>90.0%</u>	<u>0.540</u>	0.315
GearBind	87.7%	0.543	0.315	<u>87.1%</u>	0.544	0.317	86.7%	0.527	0.317	<u>88.9%</u>	0.541	0.314
<i>AffinityFlow</i>	<b>88.9%</b>	<b>0.526</b>	0.320	<b>93.3%</b>	<b>0.528</b>	0.321	<b>89.7%</b>	<b>0.514</b>	0.322	<b>91.2%</b>	<b>0.528</b>	0.323

In Table 1, we present the experimental results on four settings CDR-H1, CDR-H2, CDR-H3 and all design positions. Delineating lines are drawn to distinguish between different groups of methods. The best and second-best performance are highlighted in **bold** and underlined, respectively. Our method demonstrates a clear advantage over the comparison methods. Comprehensive discussions

of the results presented in Table 1 can be found in Appendix A.6. Additionally, we provide ablation studies in Appendix A.7 and case studies in Appendix A.8.

## 5 CONCLUSION

We introduce *AffinityFlow*, an AlphaFlow-based framework for optimizing antibodies. It integrates *alternating optimization* for affinity-driven structure generation and sequence refinement, alongside a *co-teaching* module for enhancing predictors with biophysical insights. Our method achieves state-of-the-art performance in affinity maturation, excelling in functionality, specificity, and rationality.

## REFERENCES

- Josh Abramson, Jonas Adler, Jack Dunger, Richard Evans, Tim Green, Alexander Pritzel, Olaf Ronneberger, Lindsay Willmore, Andrew J Ballard, Joshua Bambrick, et al. Accurate structure prediction of biomolecular interactions with alphafold 3. *Nature*, 2024.
- Jared Adolf-Bryfogle, Oleks Kalyuzhnyi, Michael Kubitz, Brian D Weitzner, Xiaozhen Hu, Yumiko Adachi, William R Schief, and Roland L Dunbrack Jr. Rosettaantibodydesign (rabd): A general framework for computational antibody design. *PLoS computational biology*, 2018.
- Rahmad Akbar, Habib Bashour, Puneet Rawat, Philippe A Robert, Eva Smorodina, Tudor-Stefan Cotet, Karine Flem-Karlsen, Robert Frank, Brij Bhushan Mehta, Mai Ha Vu, et al. Progress and challenges for the machine learning-based design of fit-for-purpose monoclonal antibodies. In *MAbs*. Taylor & Francis, 2022.
- Rebecca F Alford, Andrew Leaver-Fay, Jeliuzko R Jeliuzkov, Matthew J O’Meara, Frank P DiMaio, Hahnbeom Park, Maxim V Shapovalov, P Douglas Renfrew, Vikram K Mulligan, Kalli Kappel, et al. The rosetta all-atom energy function for macromolecular modeling and design. *Journal of chemical theory and computation*, 2017.
- Nathaniel R Bennett, Joseph L Watson, Robert J Ragotte, Andrew J Borst, Déjenaé L See, Connor Weidle, Riti Biswas, Ellen L Shrock, Philip JY Leung, Buwei Huang, et al. Atomically accurate de novo design of single-domain antibodies. *bioRxiv*, 2024.
- Avrim Blum and Tom Mitchell. Combining labeled and unlabeled data with co-training. In *Proceedings of the eleventh annual conference on Computational learning theory*, 1998.
- Huiyu Cai, Zuobai Zhang, Mingkai Wang, Bozitao Zhong, Quanxiao Li, Yuxuan Zhong, Yanling Wu, Tianlei Ying, and Jian Tang. Pretrainable geometric graph neural network for antibody affinity maturation. *Nature Communications*, 2024.
- Andrew Campbell, Jason Yim, Regina Barzilay, Tom Rainforth, and Tommi Jaakkola. Generative flows on discrete state-spaces: Enabling multimodal flows with applications to protein co-design. *arXiv preprint arXiv:2402.04997*, 2024.
- Can Chen, Yingxue Zhang, Xue Liu, and Mark Coates. Bidirectional learning for offline model-based biological sequence design. In *International Conference on Machine Learning*. PMLR, 2023.
- Mark L Chiu and Gary L Gilliland. Engineering antibody therapeutics. *Current opinion in structural biology*, 38:163–173, 2016.
- Lee-Shin Chu, Jeffrey A Ruffolo, Ameya Harmalkar, and Jeffrey J Gray. Flexible protein-protein docking with a multi-track iterative transformer. *Protein Science*, pp. e4862, 2023.
- Justas Dauparas, Ivan Anishchenko, Nathaniel Bennett, Hua Bai, Robert J Ragotte, Lukas F Milles, Basile IM Wicky, Alexis Courbet, Rob J de Haas, Neville Bethel, et al. Robust deep learning-based protein sequence design using proteinmpnn. *Science*, 2022.
- Prafulla Dhariwal and Alexander Nichol. Diffusion models beat gans on image synthesis. *Advances in neural information processing systems*, 2021.

- James Dunbar, Konrad Krawczyk, Jinwoo Leem, Terry Baker, Angelika Fuchs, Guy Georges, Jiye Shi, and Charlotte M Deane. Sabdab: the structural antibody database. *Nucleic acids research*, 2014.
- Noelia Ferruz, Steffen Schmidt, and Birte Höcker. Protgpt2 is a deep unsupervised language model for protein design. *Nature communications*, 13(1):4348, 2022.
- Nathan C Frey, Daniel Berenberg, Karina Zadorozhny, Joseph Kleinhenz, Julien Lafrance-Vanasse, Isidro Hotzel, Yan Wu, Stephen Ra, Richard Bonneau, Kyunghyun Cho, et al. Protein discovery with discrete walk-jump sampling. *arXiv preprint arXiv:2306.12360*, 2023.
- Johannes Thorling Hadsund, Tadeusz Satława, Bartosz Janusz, Lu Shan, Li Zhou, Richard Röttger, and Konrad Krawczyk. nanobert: a deep learning model for gene agnostic navigation of the nanobody mutational space. *Bioinformatics Advances*, 2024.
- Bo Han, Quanming Yao, Xingrui Yu, Gang Niu, Miao Xu, Weihua Hu, Ivor Tsang, and Masashi Sugiyama. Co-teaching: Robust training of deep neural networks with extremely noisy labels. *Advances in neural information processing systems*, 31, 2018.
- Tomas Hayes, Roshan Rao, Halil Akin, Nicholas J Sofroniew, Deniz Oktay, Zeming Lin, Robert Verkuil, Vincent Q Tran, Jonathan Deaton, Marius Wiggert, et al. Simulating 500 million years of evolution with a language model. *bioRxiv*, pp. 2024–07, 2024.
- Brian L Hie, Varun R Shanker, Duo Xu, Theodora UJ Bruun, Payton A Weidenbacher, Shaogeng Tang, Wesley Wu, John E Pak, and Peter S Kim. Efficient evolution of human antibodies from general protein language models. *Nature Biotechnology*, 2024.
- Guillaume Huguet, James Vuckovic, Kilian Fatras, Eric Thibodeau-Laufer, Pablo Lemos, Riashat Islam, Cheng-Hao Liu, Jarrid Rector-Brooks, Tara Akhound-Sadegh, Michael Bronstein, et al. Sequence-augmented se (3)-flow matching for conditional protein backbone generation. *arXiv preprint arXiv:2405.20313*, 2024.
- Zarif Ikram, Dianbo Liu, and M Saifur Rahman. Antibody sequence optimization with gradient-guided discrete walk-jump sampling. In *ICLR 2024 Workshop on Generative and Experimental Perspectives for Biomolecular Design*, 2024.
- John B Ingraham, Max Baranov, Zak Costello, Karl W Barber, Wujie Wang, Ahmed Ismail, Vincent Frappier, Dana M Lord, Christopher Ng-Thow-Hing, Erik R Van Vlack, et al. Illuminating protein space with a programmable generative model. *Nature*, 623, 2023.
- Bowen Jing, Stephan Eismann, Patricia Suriana, Raphael John Lamarre Townshend, and Ron Dror. Learning from protein structure with geometric vector perceptrons. In *International Conference on Learning Representations*, 2021. URL <https://openreview.net/forum?id=1YLJDvSx6J4>.
- Bowen Jing, Ezra Erives, Peter Pao-Huang, Gabriele Corso, Bonnie Berger, and Tommi Jaakkola. Eigenfold: Generative protein structure prediction with diffusion models, 2023.
- Bowen Jing, Bonnie Berger, and Tommi Jaakkola. Alphafold meets flow matching for generating protein ensembles, 2024.
- John Jumper, Richard Evans, Alexander Pritzel, Tim Green, Michael Figurnov, Olaf Ronneberger, Kathryn Tunyasuvunakool, Russ Bates, Augustin Židek, Anna Potapenko, et al. Highly accurate protein structure prediction with alphafold. *nature*, 2021.
- Diederik P Kingma. Adam: A method for stochastic optimization. *arXiv preprint arXiv:1412.6980*, 2014.
- Rohith Krishna, Jue Wang, Woody Ahern, Pascal Sturmfels, Preetham Venkatesh, Indrek Kalvet, Gyu Rie Lee, Felix S Morey-Burrows, Ivan Anishchenko, Ian R Humphreys, et al. Generalized biomolecular modeling and design with rosettafold all-atom. *Science*, 2024.

- Paulina Kulytė, Francisco Vargas, Simon Valentin Mathis, Yu Guang Wang, José Miguel Hernández-Lobato, and Pietro Liò. Improving antibody design with force-guided sampling in diffusion models. *arXiv preprint arXiv:2406.05832*, 2024.
- Seul Lee, Jaehyeong Jo, and Sung Ju Hwang. Exploring chemical space with score-based out-of-distribution generation. In *International Conference on Machine Learning*. PMLR, 2023.
- Jinwoo Leem, Laura S Mitchell, James HR Farmery, Justin Barton, and Jacob D Galson. Deciphering the language of antibodies using self-supervised learning. *Patterns*, 2022.
- Jiahan Li, Chaoran Cheng, Zuofan Wu, Ruihan Guo, Shitong Luo, Zhizhou Ren, Jian Peng, and Jianzhu Ma. Full-atom peptide design based on multi-modal flow matching. *arXiv preprint arXiv:2406.00735*, 2024.
- Tingting Li, Hongmin Cai, Hebang Yao, Bingjie Zhou, Ning Zhang, Yuhuan Gong, Yapei Zhao, Quan Shen, Wenming Qin, Cedric A.J. Hutter, Yanling Lai, Shu-Ming Kuo, Juan Bao, Jiaming Lan, Markus A. Seeger, Gary Wong, Yuhai Bi, Dimitri Lavillette, and Dianfan Li. A potent synthetic nanobody targets rbd and protects mice from sars-cov-2 infection. *bioRxiv*, 2020. doi: 10.1101/2020.06.09.143438. URL <https://www.biorxiv.org/content/early/2020/09/24/2020.06.09.143438>.
- Haitao Lin, Lirong Wu, Yufei Huang, Yunfan Liu, Odin Zhang, Yuanqing Zhou, Rui Sun, and Stan Z Li. Geoab: Towards realistic antibody design and reliable affinity maturation. *bioRxiv*, 2024.
- Zeming Lin, Halil Akin, Roshan Rao, Brian Hie, Zhongkai Zhu, Wenting Lu, Allan dos Santos Costa, Maryam Fazel-Zarandi, Tom Sercu, Sal Candido, et al. Language models of protein sequences at the scale of evolution enable accurate structure prediction. *BioRxiv*, 2022.
- Zeming Lin, Halil Akin, Roshan Rao, Brian Hie, Zhongkai Zhu, Wenting Lu, Nikita Smetanin, Robert Verkuil, Ori Kabeli, Yaniv Shmueli, et al. Evolutionary-scale prediction of atomic-level protein structure with a language model. *Science*, 379, 2023.
- Xianggen Liu, Yunan Luo, Pengyong Li, Sen Song, and Jian Peng. Deep geometric representations for modeling effects of mutations on protein-protein binding affinity. *PLoS computational biology*, 2021.
- Shitong Luo, Yufeng Su, Xingang Peng, Sheng Wang, Jian Peng, and Jianzhu Ma. Antigen-specific antibody design and optimization with diffusion-based generative models for protein structures. *Advances in Neural Information Processing Systems*, 35:9754–9767, 2022.
- Eran Malach and Shai Shalev-Shwartz. Decoupling” when to update” from” how to update”. *Proc. Adv. Neur. Inf. Proc. Syst (NeurIPS)*, 2017.
- Kenneth Murphy and Casey Weaver. *Janeway’s immunobiology*. Garland science, 2016.
- Alexander Rives, Joshua Meier, Tom Sercu, Siddharth Goyal, Zeming Lin, Jason Liu, Demi Guo, Myle Ott, C. Lawrence Zitnick, Jerry Ma, and Rob Fergus. Biological structure and function emerge from scaling unsupervised learning to 250 million protein sequences. *PNAS*, 2019. doi: 10.1101/622803. URL <https://www.biorxiv.org/content/10.1101/622803v4>.
- Jeffrey A Ruffolo, Jeffrey J Gray, and Jeremias Sulam. Deciphering antibody affinity maturation with language models and weakly supervised learning. *arXiv preprint arXiv:2112.07782*, 2021.
- Jeffrey A Ruffolo, Lee-Shin Chu, Sai Pooja Mahajan, and Jeffrey J Gray. Fast, accurate antibody structure prediction from deep learning on massive set of natural antibodies. *Nature communications*, 2023.
- Sisi Shan, Shitong Luo, Ziqing Yang, Junxian Hong, Yufeng Su, Fan Ding, Lili Fu, Chenyu Li, Peng Chen, Jianzhu Ma, et al. Deep learning guided optimization of human antibody against sars-cov-2 variants with broad neutralization. *Proceedings of the National Academy of Sciences*, 2022.
- Richard W Shuai, Jeffrey A Ruffolo, and Jeffrey J Gray. Generative language modeling for antibody design. *bioRxiv*, pp. 2021–12, 2021.

- Richard W Shuai, Jeffrey A Ruffolo, and Jeffrey J Gray. Iglm: Infilling language modeling for antibody sequence design. *Cell Systems*, 2023.
- Jin Su, Chenchen Han, Yuyang Zhou, Junjie Shan, Xibin Zhou, and Fajie Yuan. Saprot: Protein language modeling with structure-aware vocabulary. *bioRxiv*, pp. 2023–10, 2023.
- Maryam Tabasinezhad, Yeganeh Talebkhan, Wolfgang Wenzel, Hamzeh Rahimi, Eskandar Omidinia, and Fereidoun Mahboudi. Trends in therapeutic antibody affinity maturation: From in-vitro towards next-generation sequencing approaches. *Immunology letters*, 2019.
- Iain H. Moal Tobias H. Olsen and Charlotte M. Deane. Ablang: An antibody language model for completing antibody sequences. *bioRxiv*, 2022. doi: <https://doi.org/10.1101/2022.01.20.477061>.
- Zichen Wang, Steven A Combs, Ryan Brand, Miguel Romero Calvo, Panpan Xu, George Price, Nataliya Golovach, Emmanuel O Salawu, Colby J Wise, Sri Priya Ponnappalli, et al. Lm-gvp: an extensible sequence and structure informed deep learning framework for protein property prediction. *Scientific reports*, 2022.
- Janusz Wesolowski, Vanina Alzogaray, Jan Reyelt, Mandy Unger, Karla Juarez, Mariela Urrutia, Ana Cauerhff, Welbeck Danquah, Björn Rissiek, Felix Scheuplein, et al. Single domain antibodies: promising experimental and therapeutic tools in infection and immunity. *Medical microbiology and immunology*, 2009.
- Peng Xiong, Chengxin Zhang, Wei Zheng, and Yang Zhang. Bindprofx: assessing mutation-induced binding affinity change by protein interface profiles with pseudo-counts. *Journal of molecular biology*, 2017.
- Hebang Yao, Hongmin Cai, Tingting Li, Bingjie Zhou, Wenming Qin, Dmitri Lavillette, and Dianfan Li. A high-affinity RBD-targeting nanobody improves fusion partner’s potency against SARS-CoV-2. *PLOS Pathogens*, 17(3):1–18, 2021. doi: [10.1371/journal.ppat.1009328](https://doi.org/10.1371/journal.ppat.1009328). URL <https://doi.org/10.1371/journal.ppat.1009328>.
- Fei Ye, Zaixiang Zheng, Dongyu Xue, Yuning Shen, Lihao Wang, Yiming Ma, Yan Wang, Xinyou Wang, Xiangxin Zhou, and Quanquan Gu. Proteinbench: A holistic evaluation of protein foundation models. *arXiv preprint arXiv:2409.06744*, 2024.
- Qinqing Zheng, Matt Le, Neta Shaul, Yaron Lipman, Aditya Grover, and Ricky TQ Chen. Guided flows for generative modeling and decision making. *arXiv preprint arXiv:2311.13443*, 2023.
- Xiangxin Zhou, Dongyu Xue, Ruizhe Chen, Zaixiang Zheng, Liang Wang, and Quanquan Gu. Antigen-specific antibody design via direct energy-based preference optimization. *arXiv preprint arXiv:2403.16576*, 2024.

## A APPENDIX

### A.1 RELATED WORK

**Generative Protein Modeling** Generative protein modeling primarily includes sequence-based language models and structure-based score generative models. Language models are trained on protein sequence datasets using masked prediction Rives et al. (2019) or auto-regressive prediction Ferruz et al. (2022). These models are often fine-tuned for specific domains like antibodies, with examples including AbLang Tobias H. Olsen & Deane (2022), AntiBERTa Leem et al. (2022), IgLM Shuai et al. (2021), and nanoBERT Hadsund et al. (2024). Language models have also been explored for modeling tokenized protein structures Hayes et al. (2024); Su et al. (2023).

Score-based models, such as diffusion-based and flow matching models, mainly focus on generating protein structures. (1) Diffusion-based models like RFdiffusionAA Krishna et al. (2024) and AlphaFold3 Abramson et al. (2024) generate structures through coordinate denoising. RFdiffusionAA has been applied to antibody design Bennett et al. (2024), but its code is not open-sourced. Chroma Ingraham et al. (2023) introduces property-specific guidance into diffusion models but does not research antibody design. Similarly, Kulytė et al. (2024) incorporates force-field guidance but

struggles to capture realistic structures due to the simplicity of the diffusion model. (2) Flow matching models have shown greater effectiveness and efficiency compared to diffusion models. Recent studies like AlphaFlow Jing et al. (2024) and FoldFlow-2 Huguette et al. (2024) explore sequence-conditioned flow matching for protein structure generation. In this work, we utilize the AlphaFlow framework for antibody sequence design due to its demonstrated effectiveness. It is worth noting that score-based generative models have also been applied to model discrete biological sequences Campbell et al. (2024); Frey et al. (2023); Li et al. (2024); Ikram et al. (2024).

**Co-teaching** Co-teaching Han et al. (2018) is a robust technique for addressing label noise by utilizing two collaborative models. Each model identifies small-loss samples from a noisy mini-batch to train the other. Co-teaching is conceptually related to decoupling Malach & Shalev-Shwartz (2017) and co-training Blum & Mitchell (1998), as all these approaches involve collaborative learning between two models. In this study, we adapt co-teaching to work with biophysical binding energy data rather than a noisy dataset. Specifically, the sequence-based predictor identifies clean samples for training the structure-based predictor, and vice versa.

## A.2 PREDICTOR GUIDANCE IN FLOW MATCHING

According to Lemma 1 in Zheng et al. (2023),

$$\tilde{v}(\mathbf{x}_t, t, \Delta G; \boldsymbol{\theta}) = a_t \mathbf{x}_t + b_t \nabla_{\mathbf{x}_t} \log p_{\beta}(\mathbf{x}_t, t \mid \Delta G) \quad (9)$$

Based on this, we can derive:

$$\begin{aligned} \tilde{v}(\mathbf{x}_t, t, \Delta G; \boldsymbol{\theta}) &= a_t \mathbf{x}_t + b_t \nabla_{\mathbf{x}_t} \log p_{\beta}(\mathbf{x}_t, t) + b_t \nabla_{\mathbf{x}_t} \log p_{\beta}(\Delta G \mid \mathbf{x}_t, t) \\ &= \hat{v}(\mathbf{x}_t, t; \boldsymbol{\theta}) + b_t \nabla_{\mathbf{x}_t} \log p_{\beta}(\Delta G \mid \mathbf{x}_t, t) \end{aligned} \quad (10)$$

In our case,  $b_t = \frac{1-t}{t}$ , and this leads to:

$$\tilde{v}(\mathbf{x}_t, t, \Delta G; \boldsymbol{\theta}) = \hat{v}(\mathbf{x}_t, t; \boldsymbol{\theta}) + \frac{1-t}{t} \nabla_{\mathbf{x}_t} \log p_{\beta}(\Delta G \mid \mathbf{x}_t, t). \quad (11)$$

## A.3 COMPUTATION APPROXIMATION

The guided vector field is defined by:

$$\tilde{v}(\mathbf{x}_t, t, \Delta G; \boldsymbol{\theta}) = \hat{v}(\mathbf{x}_t, t; \boldsymbol{\theta}) - \gamma \frac{1-t}{t} \nabla_{\mathbf{x}_t} \hat{f}_{\beta}(\hat{\mathbf{x}}_1(\mathbf{x}_t)). \quad (12)$$

We compute  $\nabla_{\mathbf{x}_t} \hat{f}_{\beta}(\hat{\mathbf{x}}_1(\mathbf{x}_t))$  as:

$$\nabla_{\mathbf{x}_t} \hat{f}_{\beta}(\hat{\mathbf{x}}_1(\mathbf{x}_t)) = \frac{\partial \hat{f}_{\beta}(\hat{\mathbf{x}}_1(\mathbf{x}_t))}{\partial \hat{\mathbf{x}}_1} \frac{\partial \hat{\mathbf{x}}_1(\mathbf{x}_t)}{\partial \mathbf{x}_t} \quad (13)$$

As  $t$  approaches 1,  $\hat{\mathbf{x}}_1$  closely approximates  $\mathbf{x}_t$ , allowing for the simplification:

$$\frac{\partial \hat{\mathbf{x}}_1(\mathbf{x}_t)}{\partial \mathbf{x}_t} \approx \mathbf{I}, \quad (14)$$

where  $\mathbf{I}$  represents the identity matrix. Consequently, we approximate the gradient as:

$$\nabla_{\mathbf{x}_t} \hat{f}_{\beta}(\hat{\mathbf{x}}_1(\mathbf{x}_t)) \approx \frac{\partial \hat{f}_{\beta}(\hat{\mathbf{x}}_1)}{\partial \hat{\mathbf{x}}_1} \quad (15)$$

## A.4 COMPARISONS WITH OTHER METHODS

In this paper, we primarily benchmark our method against language model-based methods, given our focus on sequence design. Since our method incorporates additional biophysical energies for training, we ensure fair comparisons by applying the same trained sequence-based predictor across all methods, unless stated otherwise. Each method generates a pool of candidate designs, and the sequence-based predictor selects the top three for final evaluation.

We consider the following language model-based methods:

1. **ESM Hie et al. (2024)**: This method uses a pre-trained language model to identify potential mutations. Mutation consensus among six ESM models is assessed, and all promising sequences are collected over nine rounds.
2. **AbLang Tobias H. Olsen & Deane (2022)**: Specifically trained on antibody sequences, the AbLang model includes separate models for heavy and light chains. For our purposes, we utilize the heavy chain model to identify promising mutations across nine rounds.
3. **nanoBERT Hadsund et al. (2024)**: Given our focus on sdAbs, nanoBERT, a model pre-trained on sdAb sequences, is employed. We conduct nine rounds of mutation identification.

Beyond language model-based methods, we include an additional sequence-design baseline:

4. **dWJS Frey et al. (2023)**: handles discrete sequences by learning a smoothed energy function, sampling from the smoothed data manifold, and projecting the sample back to the true data manifold with one-step denoising.

We also evaluate three structure-based methods. Although our approach is sequence-based and does not inherently require structures for design, we use AlphaFold2 Jumper et al. (2021) to predict the structures needed for these comparisons. The following methods are considered:

5. **DiffAb Luo et al. (2022)**: Trains a diffusion model on amino acid types, coordinates, and orientations. Antibody optimization is achieved by introducing small perturbations into the existing antibody-antigen complex and subsequently denoising the structure. We generate ten designs per antigen and use our predictor to select the top three for evaluation.
6. **AbDPO Zhou et al. (2024)**: Based on DiffAb, this model fine-tunes a pre-trained diffusion model using a residue-level decomposed energy preference to enable a low-energy protein sampling process. The sampling and selection processes are similar to those of DiffAb.
7. **GearBind Cai et al. (2024)**: Utilizes multi-level geometric message passing and contrastive pretraining to improve predictions of affinity. We employ AbDPO to produce ten designs per antigen, from which GearBind selects the three most promising for assessment.

## A.5 TRAINING DETAILS

We use a linker composed of 32 *GGGS* repeats to connect the sdAb and antigen. Our method utilizes the *alternating optimization* framework with three iterations, where each iteration introduces single-point, double-point, and triple-point mutations. This allows for producing 1 to 9 mutations in total. We set the AlphaFlow sampling steps  $T$  to 3 per iteration with a schedule of [1.0, 0.6, 0.3, 0.0] and use a default scaling factor  $\gamma$  of 5. We employ ESM2-8M, followed by a hidden-dim-320 three-layer MLP, as the sequence-based predictor. For the structure-based predictor, we use a five-layer GVP model, which takes the structure and ESM2-8M residue embeddings as input. For the co-teaching module, we use a batch size of 256 and a learning rate of  $1 \times 10^{-4}$  with the Adam optimizer Kingma (2014). Computational efficiency is detailed in Appendix A.9, and hyperparameter sensitivity is addressed in Appendix A.10.

## A.6 DETAILED RESULTS DISCUSSION

We make the following observations: **(1)** As shown in Table 1, our method consistently achieves the best performance in terms of *IMP* and *Sim*, thereby highlighting its effectiveness. **(2)** The notable *IMP* is mainly due to our effective predictor guidance, which directs the structure sample generation towards low binding energy. **(3)** The low *Sim* scores can be attributed to antigen-specific modeling and the diversity introduced by the AlphaFlow sampling process. Language-based methods like ESM, AbLang, and nanoBERT lack this feature, as they do not incorporate specific antigens into their design processes. Structure-based methods such as DiffAb, AbDPO, and GearBind consider specific antigens, but their simplistic diffusion models are less effective at capturing antigen information compared to our method.

**(4)** The language model-based methods ESM, AbLang, and nanoBERT achieve the highest *Nat* scores, as they are implicitly trained for this metric. Beyond these methods, our approach achieves the best *Nat*. We attribute this to the realistic structure modeling enabled by AlphaFlow and the

Table 2: Ablation Study of AffinityFlow on CDR-H3.

Methods	IMP $\uparrow$	Sim $\downarrow$	Nat $\uparrow$
<i>one-iteration</i>	73.3%	<b>0.512</b>	0.319
<i>w/o PC</i>	<u>83.3%</u>	0.521	0.316
<i>w/o AlphaFlow</i>	63.3%	0.528	0.314
<i>w/o energy</i>	66.7%	0.531	0.322
<i>w/o selection</i>	76.7%	0.523	<u>0.326</u>
Ours	<b>93.3%</b>	<u>0.514</u>	<b>0.330</b>

reliable inverse folding performed by ProteinMPNN, which together translate structures into natural sequences. (5) AbDPO, as a robust baseline, often achieves strong performance in *IMP*, likely due to incorporating energy information into its training, allowing for low-energy protein sampling. However, AbDPO requires training a separate diffusion model for each complex, adding complexity. (6) Lastly, the high *IMP* scores for baseline methods can largely be attributed to our trained sequence-based predictor. When using a standard predictor trained only on supervised data, *IMP* scores drop significantly. For example, in the CDR-H3 design setting, *IMP* drops from 64.0% to 22.7% for ESM, from 88.5% to 49.4% for AbLang, from 81.6% to 46.7% for nanoBERT, from 66.1% to 23.9% for dWJS, from 85.6% to 49.4% for DiffAb, from 87.8% to 50.6% for AbDPO, from 86.7% to 50.6% for GearBind, and from 89.7% to 68.3% for our method. In this context, our method demonstrates a clear advantage over the comparison methods.

#### A.7 ABLATION STUDIES

We use *AffinityFlow* as the baseline to evaluate the effect of removing specific modules, with results shown in Table 2. The ablation studies are conducted on CDR-H3, considering 10 antigens for efficiency. Our focus is primarily on the *IMP* metric, so the discussion centers around this metric.

**Alternating Optimization** This framework alternates between updating the structure with the sequence fixed, and mutating the sequence with the structure fixed. In this study, we perform a single iteration, applying multiple mutations simultaneously, referred to as *one-iteration*. We also evaluate the impact of the predictor-corrector technique by excluding the Amber relaxation step, denoted *w/o PC*. As shown in Table 2, both ablations reduce performance, demonstrating the predictor-corrector and Amber relaxation effectiveness.

We also evaluate the effect of directly removing the AlphaFlow framework. In this variant, we perform gradient optimization on the existing protein structure instead of using predictor guidance. This step is followed by Amber relaxation, after which we use ProteinMPNN to identify potential mutations. This variant is denoted by *w/o AlphaFlow* in Table 2, which shows that leaving out AlphaFlow leads to the greatest performance drop compared to the other two variants. We attribute this to AlphaFlow’s ability to capture the natural fluctuations of proteins, resulting in more realistic structures than those generated through direct gradient ascent alone, and accessing binding conformations that may be different from either a structure determined experimentally or predicted by a model like AlphaFold. Less realistic structures in turn yield less natural mutated sequences, as reflected by the *Nat* score decreasing from 0.330 to 0.314.

**Co-teaching** We evaluate the co-teaching module with two variants: (1) *w/o energy*: using the trained predictor on limited labeled data only. (2) *w/o selection*: training on pairwise discrete data without sample selection. As shown in Table 2, both variants reduce the *IMP* metric, highlighting the effectiveness of the module. Notably, *w/o energy* performs worse than *w/o selection*, demonstrating the value of biophysical energy data. We also observe that a better-trained predictor improves specificity: our method achieves the best *Sim*, while *w/o selection* ranks second. This likely results from the predictor’s role in estimating antigen-specific binding energy, leading to greater specificity.

Additionally, we report the Spearman’s rank correlation coefficient  $R$  (Spearmanr) on the test set. We isolate 10 antigens from the total dataset, with each antigen paired with 77 sdAbs. We calculate Spearman’s  $R$  for each antigen and present the average across the 10 antigens. The models

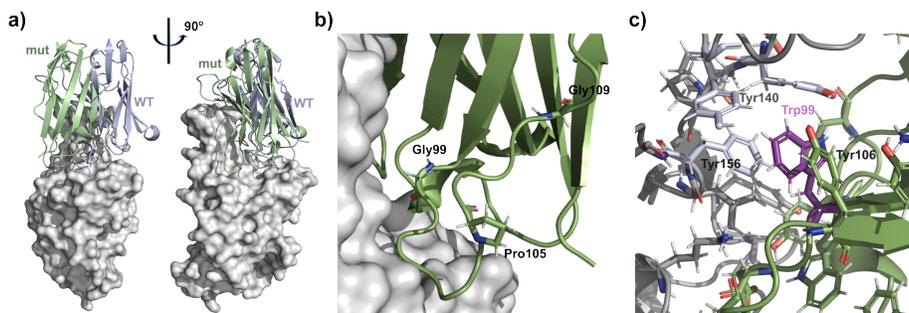


Figure 3: Visualizations of model-generated antibody structures bound to the SARS-CoV-2 RBD (a) Relative to a fixed antigen, most model-generated antibodies (green) are predicted to bind with a noticeable rotation in binding pose compared to the WT conformation (blue). (b) Our model suggests several mutations frequently, in particular Ala105Pro may stabilize the CDR loop. (c) The buried Lys99Trp mutation interacts with multiple other aromatic residues across the interface.

without energy data achieve  $R$  values of 0.0956 for the sequence-based predictor and  $-0.0043$  for the structure-based predictor, respectively, reflecting the limitations of the 120 labeled entries. By utilizing biophysical energy data for direct fine-tuning, the sequence-based predictor reaches a coefficient of 0.40, while the structure-based predictor achieves 0.50. While not state-of-the-art for antibody binding energy prediction in general, these values demonstrate the effectiveness of our approach when limited data is available. Sample selection further improves performance, with the sequence-based predictor achieving a coefficient of 0.51 and the structure-based predictor reaching 0.52. These results highlight the benefits of using biophysical energies and sample selection to enhance prediction accuracy.

#### A.8 CASE STUDY

To further understand how *AffinityFlow* generates mutations to improve binding, we analyze the structures of our proposed mutants and the wild-type of a single-domain antibody (sdAb) known to bind the SARS-CoV-2 receptor-binding domain (RBD) Yao et al. (2021). We generate 30 mutated structures, with half containing mutations only in the CDR3 loop and half having mutations across all CDRs. We use Rosetta to calculate binding energies ( $\Delta\Delta G$ ) and other interface metrics relative to the wild-type structure (PDB ID 7D30).

All computed structures show  $\Delta\Delta G < 0$ , suggesting that the designed antibodies bind the antigen more tightly than the native sequence. However, we do not observe any correlation between  $\Delta\Delta G$  and which CDRs are allowed to mutate. We measure other interface metrics (dSASA, shape complementarity) for all 30 structures and compare these values with those computed for native antibody-antigen interfaces in the PDB Adolf-Bryfogle et al. (2018). The results align well with natural structures, demonstrating that our model preserves the correct shape profile of the binding surface. Interestingly, despite conserving the binding interface shape, most mutants (21/30) dock with a rotated binding pose of approximately 67 degrees (Figure 3a). This rotation shifts interactions away from CDR1 and toward stronger interactions in CDR2 and CDR3.

Certain mutations occur frequently across all model-proposed antibodies, indicating that the model focuses attention on these residues. Notably, Lys99Gly, Ala105Pro, and Asp109Gly appear often, regardless of whether mutations are restricted to the CDR3 loop or allowed across all positions (Figure 3b). We believe that the Ala105Pro mutation stabilizes the CDR3 loop into an optimal conformation for this antigen. Using a Random Forest regression on mutation features, we find that the rarer Ala105Leu mutation contributes most to improving  $\Delta\Delta G$ , likely by increasing hydrophobicity at the interface and promoting assembly.

Most intriguingly, one model-generated sequence includes a Lys99Trp mutation, an unusual amino acid to insert within an interface. Visual examination reveals that this tryptophan residue is inserted such that it creates  $\pi$ - $\pi$  interactions with two aromatic residues across the interface as well as pro-

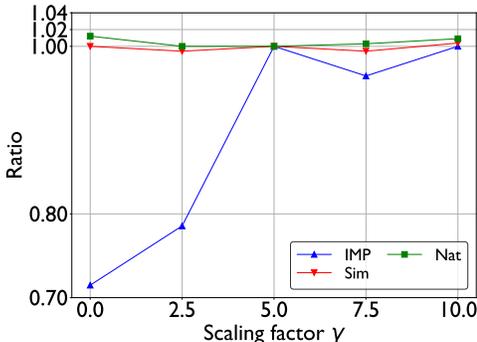


Figure 4: The antibody metrics versus scaling factor  $\gamma$ , normalized to their values at  $\gamma$  to those with  $\gamma = 5.0$ .

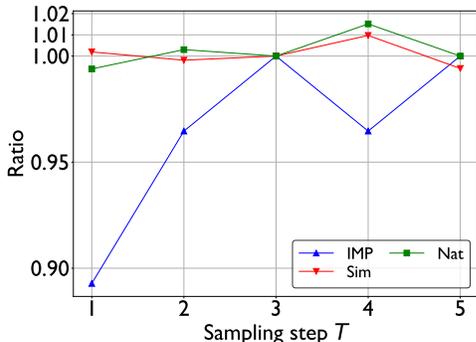


Figure 5: The three antibody metrics versus scaling factor  $T$ , normalized to their values at  $T = 3$ .

viding stabilizing interactions with a tyrosine on the antibody itself (Figure 3c). This mutation is particularly interesting since, in the development of the synthetic single domain antibody which we use as our case study, Li et al. (2020) made a single point mutation mutant, MR17m, with a single Lys99Tyr substitution. This mutant shows enhanced neutralization activity to the original MR17, with an IC50 of  $0.50 \mu\text{g}/\text{mL}$ . To further improve this activity, the authors suggest the same Lys99Trp mutation proposed by our model but do not appear to have tested it.

Our structural analysis of mutant and wild-type antibody structures reveals several key insights into the nature of mutations governing antibody-antigen binding. These results validate our computational approach and also highlight its potential to guide rational design of improved antibodies against SARS-CoV-2 and other pathogens, opening new avenues for therapeutic development.

#### A.9 COMPUTATIONAL EFFICIENCY

All experiments are conducted on a g5.24xlarge server equipped with GPUs with 23GB of memory. One iteration of our alternating optimization framework takes approximately 10 minutes for a protein of length 500. Language model-based methods are more computationally efficient, with processing times of 18.3 seconds for ESM, 13.0 seconds for Ablang, and 11.4 seconds for nanoBert per sample. However, our method consistently produces significantly better designs than these methods, as discussed. In applications such as antibody design, the most time-consuming and costly stage is often the evaluation of properties in wet-lab experiments. Thus, the differences in computation time between methods for generating high-performance designs are less significant in practical production settings, where optimization performance is prioritized over computational speed. This is consistent with the discussions in A.7.5 Computational Cost Chen et al. (2023).

#### A.10 HYPERPARAMETER ANALYSIS

This section examines the sensitivity of our method to various hyperparameters—namely, the scaling factor ( $\gamma$ ) and the number of sampling steps ( $T$ ) on CDR-H3 with 10 antigens. The reported metrics are normalized by dividing by the default hyperparameter result to facilitate comparative analysis.

**Scaling Factor ( $\gamma$ ):** The effect of varying  $\gamma$  is investigated with values 0.0, 2.5, 5.0, 7.5, and 10, and  $\gamma = 5.0$  as the standard setting. As indicated in Figure 4, the *Sim* and *Nat* metrics are stable across the range of  $\gamma$ . However, below  $\gamma \sim 5.0$  the *IMP* metric drops substantially, presumably because there is insufficient exploration of alternate backbone conformations when  $\gamma$  is small.

**Number of Sampling Steps ( $T$ ):** We analyze the impact of the number of sampling steps  $T$  on the effectiveness of our method. The normalized metric is plotted as a function of  $T$  in Figure 5. Again the *Sim* and *Nat* metrics are relatively unaffected by the choice of  $T$ , but *IMP* requires 3 sampling steps for maximum benefit. Again this suggests that more exploration of the conformational space improves the final design.