COMPKE: Complex Question Answering under Knowledge Editing

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Abstract

Knowledge Editing-Efficiently modifying 001 002 the knowledge in large language models has gathered a great attention. Current 003 benchmarks primarily use multi-hop question answering to assess and analyze the 006 newly injected/updated knowledge. We argue, these benchmarks fall short of eval-007 uating how effectively the updated model applies this knowledge in real-life scenarios encompassing questions requiring complex reasoning involving one-to-many relations and/or require multi-step logical inter-012 sections (explained in detailed in Section 1). 013 To address this gap, we introduce a new 014 benchmark, COMPKE: Complex Question 015 016 Answering under Knowledge Editing, encompassing 11,921 complex questions con-017 forming to real-life scenarios. In addition, 018 we also propose GDECOM-CQA: Generic **Decom**position based **C**omplex **Q**uestion 021 Answering, a novel approach tailored at complex question answering. We performed comprehensive evaluation of the GDECOM-CQA using COMPKE along with existing bench-024 marks to showcase the effectiveness of key 025 contributions made in this work. Experimental evaluation reveal that GDECOM-CQA out-027 performs the best-performing baseline models on COMPKE by improving the Augmented-029 Accuracy metric by 38.5% on average.

1 Introduction

Despite large language models (LLMs) being powerful to solve a wide range of real-world scenarios, they often generate erroneous or outdated 034 knowledge (Wang et al., 2023c; Zhang et al., 2024b). Therefore, knowledge Editing (KE), *i.e.*, 036 updating the model's knowledge by avoiding expensive fine-tuning, has become an active research domain (Wang et al., 2023c; Zhang et al., 2024b). A key challenge for the KE methods is their appli-040 cation of new knowledge to reason on multi-hop 041 question answering (MQA)-also known as MQA 042

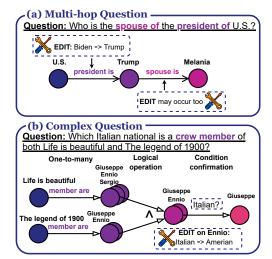


Figure 1: (a) An example of a multi-hop question involving only one-to-one sequential step-by-step reasoning. (b) An example of a complex problem involving one-to-many knowledge mapping, logical operations, and conditional confirmation.

under KE. MQA under KE requires multiple reasoning steps to come up with the final answer. An example in this regard is illustrated in Figure 1 (a), which shows a question: "Who is the spouse of the president of U.S.?" This question requires multiple reasoning steps, *i.e.*, (i) identifying who is the current president of U.S., and (ii) determining the spouse of the president.

Existing work on MQA under KE is primarily divided into two types: *(i)* memory-based methods, which place the retrieved edits before the question for in-context editing (Mitchell et al., 2022; Zhong et al., 2023); and *(ii)* parameterbased methods, which locate and modify the model parameters bases on knowledge stored in LLM (Meng et al., 2022a,b; Hu et al., 2024). Research shows memory-based methods usually outperform the parameter-based ones (Zhong et al., 2023; Gu et al., 2023; Cheng et al., 2024). These methods primarily employ a plan-and-solve paradigm (Khot et al., 2022; Wang et al., 2023a) that relies on manually defining a *task decomposition* stage to guide the LLMs to break down multihop questions into a series of sub-questions. For
example, in Figure 1 (a), the model needs to retrieve information about the president in the first
step in order to generate responses about the president's spouse.

However, existing best performing solutions 071 for MQA under KE, i.e., memory-based methods 072 073 tend to be overly simplistic, often reducing the question-answering process to a mere linear 074 chain of facts that allows step-by-step knowledge inference by mapping one entity to another through a chain of relations. These approaches 077 078 are hard to adapt to real-life complex and varying situations often involving one-to-many relations. An example in this regard is shown in Figure 1 (b), 080 which illustrates a relatively complex reasoning 081 question: Which Italian national is a crew member 082 of both "Life Is Beautiful" and "The Legend of 083 1900?". Compared with classical multi-hop 084 answering this question requires: questions, (i) Knowledge about one-to-many relations: A film typically features numerous participants, including directors, writers, actors etc., manifesting the need to model one-to-many relation patterns in order to identify individuals associated 090 with two movies. (ii) Logical operations: After 091 having identified the individuals associated with two movies, there is a need for an appropriate intersection and/or logical operations to figure out the common participants who contributed to both films. (iii) Condition confirmation: After 096 identifying the common participants between the two films, the next step is to select the individuals who meet the specified criteria, such as nationality. In the rest of the paper, we call such complex 100 reasoning questions as the "complex question". 101

We observe that existing memory-based 102 methods when employed for the com-103 pose following 104 plex questions limitations: (i) Omission phenomenon, i.e., these methods 105 tend to generate incomplete plans during the 106 planning phase and often ignore different features 107 of the complex questions required to correctly an-108 swer the question. For instance, they only adhere 109 to one-to-one knowledge mapping and do not per-110 form logical operations, e.g., logical intersection 111 etc., to aggregate different information units. This 112 issue arises because their prompts for decompo-113 sition only include linear multi-hop questions, 114 and features not present in the demonstration 115 examples are easily ignored. However, simply 116

adding more examples to the demonstration is insufficient, as there may be many different types of complex questions. Attempts to cover all possible scenarios would result in an excessive number of prompts, leading to computational overhead and even loss of accuracy. (ii) Incomplete retrieval, *i.e.*, previous works select the top most relevant edit w.r.t semantical similarity when retrieving edits relevant to a sub-question. However, this approach may miss some edits, especially when the sub-question involves multiple edits. For example, the condition confirmation step requires determining whether multiple entities are Italian. When multiple people's nationalities change, multiple edits need to be retrieved, and simply selecting the top edit will result in incomplete retrieval.

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To fill the gap, in this paper, we propose a new benchmark and a new memory-based editing method for complex questions. Specifically, we propose: (a) a new benchmark for complex questions, *i.e.*, COMPKE: **Comp**lex Question Answering under Knowledge Editing. COMPKE is curated using Wikipedia and encompasses a total of 11,921 complex questions; (b) a new memory-based editing approach GDECOM-CQA: Generic Decomposition based Complex Question Answering, which can dynamically construct efficient decomposition prompts based on the complex questions, and can effectively solve the problem of incomplete retrieval.

We performed comprehensive evaluations to demonstrate and/or showcase the effectiveness of key contributions made in this paper. Experimental evaluation reveals that for COMPKE, GDECOM-CQA consistently outperforms other baseline models by 38.5% on average in terms of Augmented-Accuracy as evaluation metric. Moreover, on the MQUAKE-CF and MQUAKE-T dataset, GDECOM-CQA still maintains a high score, outperforming other memory-based methods by an average of 21.54% in terms of multi-hop accuracy on GPT-40-MINI.

2 Related Work

Existing research on KE can be classified into parameter-based and memory-based methods. **Parameter-Based Methods.** Parameter-based KE methods aim to directly modify the model's internal parameters to reflect updated knowledge. For example, ROME (Meng et al., 2022a) and MEMIT (Meng et al., 2022b) focus on identi-

fying and modifying parameters associated with 168 specific knowledge, while Transformer-Patcher 169 (Huang et al., 2023) edits facts by adding neurons. 170 To reduce computational costs and prevent catas-171 trophic forgetting, techniques such as: LoRA (Hu 172 et al., 2021), Prompt Tuning (Shi and Lipani, 173 2024), and OLoRA (Dettmers et al., 2023) have 174 been proposed. However, after KE, these meth-175 ods often perform poorly on multi-hop or com-176 plex questions and cannot be applied to closed-177 source models like OpenAI GPTs, which are only 178 accessible via APIs. Additionally, these meth-179 ods are more computationally expensive than the 180 memory-based methods. 181

Memory-Based Methods. These methods store 182 updates in external memory and retrieve them as 183 needed during inference. For instance, SERAC 184 185 (Mitchell et al., 2022) combines semi-parametric editing with retrieval augmented counterfactual 186 models for efficient knowledge updates. GRACE 187 (Hartvigsen et al., 2022) integrates adapters into 188 189 LLMs and uses vector matching to modify knowledge entries. IKE (Zheng et al., 2023a) ap-190 plies in-context learning with stored demonstra-191 tions for knowledge modification, MeLLo (Zhong 192 193 et al., 2023) stores edited facts externally and utilizes prompts to incorporate edits during infer-194 ence. PokeMQA (Gu et al., 2023) separates ques-195 tion decomposition and conflict detection using a 196 two-stage programmable scope detector. GLAME 197 (Zhang et al., 2024a) employs a knowledge graph 198 module to enhance retrieval efficiency. While 199 these methods outperform parameter-based approaches for MQA under KE, they struggle with 201 complex real-world scenarios. Unlike existing so-202 lutions, GDECOM-CQA augments the ability of KE for answering complex questions. It does not 204 rely on a fixed set of decomposition prompts, instead it dynamically constructs the demonstration 206 prompts based on the question under consideration 207 to help solve a diverse set of complex questions. 208

More details about related work are provided in the Appendix A.

3 Preliminaries

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212Notations.We use $\mathcal{D} = \{(s,r,o)\} \subseteq \mathcal{E} \times \mathcal{R} \times \mathcal{E}$ to denote the set of knowledge triplets,213 $\mathcal{R} \times \mathcal{E}$ to denote the set of entities and re-214where \mathcal{E} and \mathcal{R} denote the set of entities and re-215lations respectively.216sents a knowledge instance, implying that the sub-217ject entity s and the object entity o are related218by relation r.

knowledge instances, we expand the original definition of knowledge instance to (s, r, O), where $O = \{o_1, o_2, \cdots\}$ is a set of object entities, *e.g.*, (Avatar, actor are, {Worthington, Saldana, \cdots }).

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3.1 Complex Questions

Motivated by the example in the introduction, we formally define the complex questions that will be studied in this paper. A quick recap on multihop question answering (MQA) and MQA under KE is provided in Appendix B.1. We define complex question Q as a question that could be represented as a graph-like reasoning structure, i.e., $Q = (\mathbf{S}, \mathbf{L})$, where $\mathbf{S} = \{S_1, S_2, \cdots\}$ represents a set of *intermediate entities* and $\mathbf{L} = \{L_1, L_2, \dots\}$ denotes a set of reasoning links. Each $S_i \in \mathbf{S}$ is a set of entities, *i.e.*, $S_i = \{s_1, \dots\}$, used to represent one-to-one and one-to-many knowledge instances. Each $L_i \in \mathbf{L}$ is a reasoning link. Note that unlike the relation typically used in the knowledge graphs (used to map one entity s_i to another s_i via relation r), reasoning links offer extended operations by allowing conditional confirmation and logical operations, formally explained below.

Reasoning Links. We categorize reasoning links into two distinct categories:

(a) Knowledge-related Links: This type of links are used to traverse the entities along the link, *e.g.*, given a set of entities $S_i \in \mathbf{S}$, a reasoning link may be used to obtain the next step entities $S_j \in \mathbf{S}$. We further divide these links into:

(i) Knowledge mapping. For S_i , we consider a knowledge mapping link as a map to the set of adjacent entities $S_j = \bigcup_{s \in S_i} A_r(s)$, where $A_r(s) = \{s' \mid (s, r, s') \in \mathcal{D}\}$ represents the entities related to s via some relation r.

(ii) Condition Confirmation. Given r and s', this link aims to identify a set of entities $S_j = \{s \in S_i \mid C(s, r, s') = True\}$ conforming to $C(s) = [(s, r, s') \in D]$, which is used to examine whether s can obtain s' via r. For instance, "Whether Giuseppe and Ennio are Italian?", S_i are $\{\text{Giueppe, Ennio}\}, s'$ is Italian and r is nationality. (b) Logical Links: Given a set of intermediate entities $\{S_1, S_2, \cdots, S_n\} \in \mathbf{S}$, this type of reasoning link performs logical operations among the elements of S_i . For this, we use:

(i) Intersection. Intersection operation is used to determine the set of adjacent entities $S_j = \bigcap_{k=1}^{n} S_k$, which includes only those entities that are common across all sets.

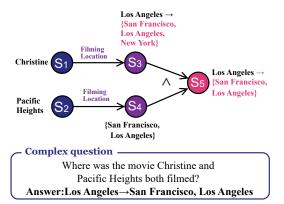


Figure 2: An example of complex question under knowledge editing. {San Franciso, Los Angels,...} represents knowledge edit.

(*ii*) Union. Union operation is used to compute the set of adjacent entities $S_j = \bigcup_{k=1}^n S_k$, encompassing all entities present in any of the sets.

Example. An example complex question with reasoning links is shown in Figure 2. It shows the question: "Where was the movie Christine and Pacific Heights both filmed?". The intermediate entities are S_1 ={Christine}; S_2 ={Pacific Heights}; S_3 = {Los Angeles}; S_4 ={San Franciso, Los Angeles}; and S_5 ={Angeles}. The reasoning operations are: $L_1 : S_1 \xrightarrow{\text{filming at}} S_3$; $L_2 : S_2 \xrightarrow{\text{filming at}} S_4$; followed by L_3 : logical operation on S_3 and S_4 to obtain final answer, *i.e.*, $S_5 = (S_3 \cap S_4)$.

Complex Question Answering under KE. We use $e = (s, r, \mathcal{O} \rightarrow \mathcal{O}')$ to represent knowledge editing for one-to-many instances showing that \mathcal{O} is updated to \mathcal{O}' . The task assumes that the language model has access to original knowledge base \mathcal{D} . Given a batch of edits $\mathcal{E} =$ $\{e_1, e_2, \cdots\}$, the knowledge to be deleted is denoted as $\mathcal{D}_{del}^{\mathcal{E}} = \{(s_i, r_i, \mathcal{O}_i) \mid e_i \in \mathcal{E}\}$, and the newly added knowledge is represented by $\mathcal{D}_{add}^{\mathcal{E}} =$ $\{(s_i, r_i, \mathcal{O}'_i) \mid e_i \in \mathcal{E}\}$, The goal is to update the model's knowledge by \mathcal{D}' , define as: $\mathcal{D}' =$ $(\mathcal{D} - \mathcal{D}_{del}^{\mathcal{E}}) \cup \mathcal{D}_{add}^{\mathcal{E}}$. This updated knowledge, \mathcal{D}' , is then used to answer the complex question Q.

4 COMPKE

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Although the complex questions we introduced are ubiquitous in real life, they are less studied in LLM question answering under KE. We observe that existing benchmarks primarily focus on linear multi-hop questions, making them inadequate for the comprehensive evaluation of complex questions. To bridge this gap, we propose COMPKE: **Comp**lex Question Answering under **K**nowledge **E**diting. The statistics of COMPKE is shown in Table 3. It comprises a total of 11,921 complex questions, each requiring up to 5 reasoning hops.

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4.1 COMPKE: Process-flow

We outline the workflow of our data construction process in Appendix Figure 4, with details explained as follows.

Collecting Relation Templates. We first select one-to-many relations from Wikidata, such as family-child, book-authors, movie-actors *etc.*, to be used in one-to-many knowledge mapping. Next, we collect relations that are directly associated with the characteristics of the entities, such as gender, nationality, *etc.*, to be used in conditional confirmation. In COMPKE, we collected an adequate number of relations to ensure the diversity of the dataset. We provide the list of relation templates used for COMPKE in Appendix Table 14.

Sampling Facts. After relation templates, we need to construct knowledge base \mathcal{D} . For this, we want the knowledge to be included in the questions to be relatively common rather than obscure. Based on the collected relation templates, we sample single-hop knowledge triples from Wikidata and rank them according to their frequency of access, with more frequently accessed triples placed at the top. We then use GPT-J to filter out the knowledge that the model cannot recall. We will use this collected knowledge \mathcal{D} to curate complex questions.

Constructing Complex Questions. We observe that complex questions may be organized as a reasoning structures, such as the example in Figure 2, which first undergoes knowledge mapping and followed by logical operations, e.g., intersection. To collect these common reasoning structures, we start by manually constructing a subset of high-quality complex questions to act as seed. Next, we remove the intermediate entities from these questions to extract the underlying reasoning structure. We use these reasoning structures a template to generate specific complex questions by instantiating it with real-world facts from \mathcal{D} . The process proceeds as follows: we randomly initialize the leaf nodes of the reasoning structure. From there, we use logical operation or knowledge in \mathcal{D} to progressively identify the intermediate entities at next step. This process is repeated iteratively until all entities, including the intermediate ones, are fully determined.

To ensure the practical relevance of the instantiated questions, we filter out cases exhibiting the following conditions: (i) questions with no answer; (ii) questions that result in an empty set of intermediate entities; (*iii*) cases where the entities involved in the logical operations are of different types, making the logic incompatible *etc*.
For illustration, we show some exemplar relational
structures along with complex questions instantiated from them in the Appendix (Figure 11).

Introducing Edits. In order to simulate the knowledge edits, we construct counterfactual knowledge updates. For each complex question, we randomly select knowledge mappings and/or condition confirmations with knowledge of the form: (s, r, \mathcal{O}) . We introduce edit $e = (s, r, \mathcal{O}')$ considering three different types of operations, *i.e.*, (*i*) addition: $\mathcal{O}_{add} = \mathcal{O}' \setminus \mathcal{O}$, where \mathcal{O}_{add} represents the set of newly added entities; (*ii*) deletion: $\mathcal{O}_{del} = \mathcal{O} \setminus \mathcal{O}'$, where \mathcal{O}_{del} represents the set of removed entities; (*iii*) retention: $\mathcal{O}_{ret} = \mathcal{O} \cap \mathcal{O}'$, where \mathcal{O}_{ret} represents the set of retained entities.

More details on constructing the dataset are provided in the Appendix C.

5 GDECOM-CQA

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In this section, we introduce our proposed framework, GDECOM-CQA: <u>Generic Decom</u>position based <u>Complex Question Answering</u>, GDECOM-CQA uses a plan-and-solve paradigm, whose workflow is summarized as follows. (*i) Planning:* Construct a decomposition prompt to decompose the complex question into a series of smaller subquestions. (*ii) Solving:* For the entities involved in each sub-question retrieve relevant edits and prompt the model to integrate both internal and external knowledge to solve each sub-question.

5.1 Planning

The planning stage of GDECOM-CQA aims to break down each complex question into multiple sub-questions to be addressed individually. However, we observe it is relatively hard to decompose complex questions compared to that of the multihop questions, as: (*i*) Complex questions are more general compared to the multi-hop questions exhibit greater variations. They require more decomposition examples as demonstration prompts for the LLMs. (*ii*) Unlike multi-hop questions which have a linear sequential relationship, the dependencies between sub-questions are more complex. **Decompose Complex Question.** Formally, we define a decomposition of complex question Q as $Q \mapsto \{q_1, q_2, \dots, q_n\}$, as follows:

$$\{q_1, q_2, \cdots, q_n\} = \text{LLM}(Q, \mathcal{P}_{\text{plan}})$$
 (1)

where \mathcal{P}_{plan} is an in-context learning prompt (with multiple example demonstrations, explained in

the following subsection); q_i represents a subquestion, and LLM is the language model used for decomposition. We represent each sub-question as $q_i = (t, i, d)$, where t represents the reasoning link type (e.g., intersection, knowledge mapping), i is the specific instruction describing the detailed action or query to be executed in this sub-question, d represents the set of preceding sub-questions.

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Decomposition Prompts (\mathcal{P}_{plan}). For \mathcal{P}_{plan} , we use multiple different demonstrations helpful for the effective decomposition of the complex questions. While in multi-hop questions, \mathcal{P}_{plan} usually requires a small number of examples to achieve effective decomposition (Zhong et al., 2023; Gu et al., 2023), we observe for complex questions it is necessary to increase the number of examples to cover a broader and diverse range of scenarios. At the same time, including too many examples is impractical, as it leads to significant computational overhead. Moreover, an excessive number of examples may reduce the effectiveness of the decomposition, as the model's ability to understand context is inherently limited. To overcome this, instead of using a set of pre-defined examples, we use an automated way to construct a different \mathcal{P}_{plan} for each Q in a way that: (i) we use an appropriate number of examples to avoid computational overhead and ensure effective decomposition, and (ii) examples in \mathcal{P}_{plan} are similar to Q to the best possible extend. The process of demonstration selection for each Q is explained below.

Demonstration Selection. For demonstration selection, we first use an external memory specifically for storing decompositions. This memory is dynamically maintained, allowing new decomposition to be added in the future. For the complex question Q to be decomposed, we will select similar decomposition examples from the memory to come up with $\mathcal{P}_{\text{plan}}$. For this, we use the semantic similarity (*i.e.*, inner product of embedding vectors via obtained from embedding model), between the examples in the memory and Q, in order to select the top-k examples as $\mathcal{P}_{\text{plan}}$.

5.2 Solving

This stage of GDECOM-CQA involves retrieving relevant edits helpful for the model to solve subquestions. While, the retrieval process for multihop questions is relatively straightforward, retrieving at most one edit per sub-question. In contrast, complex problems often involve a set of entities (S_i) as the intermediate answer, which may lead

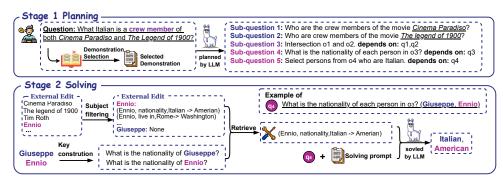


Figure 3: The overall workflow of GDECOM-CQA. **Planning:** Dynamically construct a decomposition prompt to decompose complex question into a series of sub-question; **Solving:** Solve each sub-question to come up with the final response.

to retrieving multiple knowledge edits from the edit memory at the same time. In this section, we first introduce the retrieval process, followed by how integrate model's own knowledge and the retrieved edits to solve the sub-question.

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Suppose we want to solve q_i , in order to solve the incomplete retrieval challenge, we initially identify the set of entities that need to retrieve external information from added knowledge base $\mathcal{D}_{add}^{\mathcal{E}}$, represented by S_{q_i} , computed as $S_{q_i} =$ $\{s \mid s \in o_j(q_j) \quad \forall q_j \in d_i\}$, where d_i represents the set of preceding sub-questions that q_i depends on, $o_j(q_j)$ represents the response output of q_j , which is a set of entities, explained in Equation 4. We retrieve external edits independently for each $s \in S_{q_i}$. This retrieval process is primarily divided into the following three steps:

Subject Filtering. In order to retrieve effectively, we start by filtering out knowledge in $\mathcal{D}_{add}^{\mathcal{E}}$ for which subject does not match *s* to get subset \mathcal{D}_{sub}^{s} .

To achieve this, previous work (Cheng et al., 2024) used aliases of entity *s* to see if they appear in the edit string. However, this approach may fail to retrieve all relevant edits due to incomplete alias information. To address this issue, we compute the embedding similarity between *s* and the subject entities in $\mathcal{D}_{add}^{\mathcal{E}}$ compared against a threshold θ to get the subset \mathcal{D}_{sub}^{s} , as follows.

$$\mathcal{D}_{sub}^{s} = \{ (s_i, r_i, \mathcal{O}_i) \mid (s_i, r_i, \mathcal{O}_i) \in \mathcal{D}_{add}^{\varepsilon} \\ \wedge \sin(s_i, s) \ge \theta \}$$
(2)

where sim is the cosine similarity between
their embedding, obtained by the encoder. We observed, this approach reduces the chances of related edits being filtered out. Note, we use allMiniLM-L12-v2 as our embedding encoder.

494 **Query Key Construction.** The next step is to 495 find the precise edit from \mathcal{D}_{sub}^s by locating the 496 edit which is most relevant to the instruction of the q_i . While, previous work use sub-questions as the key to query and compare its semantic similarity with the string form of edits to come up with most relevant edit. We observe, directly using the sub-questions for the complex question as the key will lead to noise. For instance, the sub-question: *"What is the nationality of Giuseppe and Ennio?"*, will retrieve edits like: {The author of *Giuseppe and Ennio* is Tom}, where *Giuseppe and Ennio* represents a book. We argue, in order to retrieve edits for Giuseppe, removing other entities, *e.g.*, Ennio will help improve retrieval efficiency.

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For this, we construct a distinct key for each entity $s \in S_{q_i}$, represented by k_s . For k_s , we use the *i*, *i.e.*, the instruction part of $q_i = (t, i, d)$ by replacing its entity with the specific entity s.

Later, in order to find relevant edit for s, we use k_s as query key to iterate \mathcal{D}_{sub}^s , as follows:

$$e_s^* = \underset{(s_i, r_i, \mathcal{O}'_i) \in \mathcal{D}_{sub}^s}{\operatorname{argmax}} \operatorname{sim}(\operatorname{S}(s_i, r_i, \mathcal{O}'_i), k_s), \quad (3)$$

where $S(s_i, r_i, \mathcal{O}'_i)$ is the unstructured string form of the edit, e_s^* is the most relevant edit for entity s. We integrate the most relevant edits for each entity, as: $E_{q_i} = \{e_s^* \mid s \in S_{q_i}\}.$

Chain-of-thought Solving. Finally, we use the LLM to solve the sub-questions q_i based on the retrieved edits E_{q_i} , as shown below:

$$p_i = \text{LLM}(\mathcal{P}_{\text{solve}}, q_i, E_{q_i}), \qquad (4)$$

where \mathcal{P}_{solve} is the in-context learning prompt for solving, outlined in Appendix Table 13, yielding a set of entities o_i as the response for q_i . For this, we employ a chain-of-thought reasoning method to integrate both external edits and the model's internal knowledge, as shown in *Thinking Process* in Appendix (Table 13). We find that this approach solves the problem of the model being unwilling to accept new knowledge and can effectively perform self-checking (Zhong et al., 2023) to judge whether the edit is relevant to the sub-question.

	СомрКЕ						
Method	1-edited		100-edited		All-edited		
	Aug-Acc	Ret-Acc	Aug-Acc	Ret-Acc	Aug-Acc	Ret-Acc	
	Qw	EN2.5-3B	-INSTRUCT				
ROME	12.61	17.91	4.8	4.40	0.82	1.59	
MEMIT	20.99	23.86	7.8	6.73	1.52	3.75	
MeLLo	5.40	2.25	3.06	3.39	0.69	2.00	
PoKeMQA	0.46	0.46	0.42	0.38	0.71	0.61	
GDECOM-CQA (Ours)	8.65	12.42	7.91	10.19	7.12	10.40	
	Qw	EN2.5-7B	-INSTRUCT				
ROME	22.82	25.09	7.50	7.98	0.73	0.98	
MEMIT	29.40	27.72	24.11	24.80	1.88	2.05	
MeLLo	17.78	13.38	10.35	17.32	8.98	12.59	
PoKeMQA	3.95	3.41	2.17	1.67	2.04	1.15	
GDECOM-CQA (Ours)	36.71	44.61	29.29	39.37	34.17	42.78	
	LLA	MA-3.1-81	B-INSTRUC	Т			
ROME	7.44	24.84	1.50	1.14	0.56	0.61	
MEMIT	4.90	33.22	5.00	29.27	5.03	29.20	
MeLLo	14.06	17.95	9.17	17.84	8.98	14.17	
PoKeMQA	1.40	2.10	0.98	1.85	0.45	1.73	
GDECOM-CQA (Ours)	39.19	39.09	31.58	34.86	31.71	37.41	
GPT-3.5-TURBO							
MeLLo	49.21	44.88	37.10	44.09	32.61	38.58	
PoKeMQA	23.20	25.15	21.47	23.28	20.20	22.20	
GDECOM-CQA (Ours)	67.22	69.00	63.18	68.19	61.67	65.63	
		GPT-40	-MINI				
MeLLo	22.07	25.19	20.31	23.62	18.75	22.14	
PoKeMQA	36.60	42.33	35.42	41.35	28.36	35.02	
GDECOM-CQA (Ours)	64.72	71.20	62.35	68.92	60.44	67.53	

Table 1: Experimental results for COMPKE. We **boldface** overall best results with the second-best <u>underlined</u>.

6 Experimentation

In this section, we extensively evaluate and compare GDECOM-CQA against different baselines.

6.1 Experimental Settings

Datasets. For experimentation we use our newly proposed dataset, *i.e.*, COMPKE, as well as existing publicly available datasets: MQUAKE-CF and MQUAKE-T (Zhong et al., 2023). The statistics of the datasets are provided in Appendix D.1.
Baselines. For performance comparison, we use existing best performing methods for MQA under KE as baselines. These include the memory-based variants: MeLLo (Zhong et al., 2023), and PokeMQA (Gu et al., 2023); as well as the parameter-based variants: ROME (Meng et al., 2022a), and MEMIT (Meng et al., 2022b).

Evaluation Metrics. For COMPKE, we use: (*i*) 551 Augment-Accuracy (Aug-Acc): the number of new 552 entities used to augment the answer list after the 553 knowledge edit that are correctly answered, com-554 pared to the original list. (ii) Retain-Accuracy 555 (Ret-Acc): the number of entities that appear in 556 both the original and edited answer lists, reflecting 557 the model's ability to preserve unmodified knowl-558 edge. For MQuAKE we use (iii) Multi-hop Accuracy (M-Acc), i.e., the accuracy of the final an-560 swer of multi-hop question as the evaluation met-561 ric. Detailed mathematical formulation of these 562 metrics are provided in Appendix D.3. 563

Experiment Setup. We conduct experiments under varying scales of knowledge edits, *i.e.*, using a batch of k-edits at a time with k = $\{1, 100, 1000, all\}$. For knowledge eding, we use LLAMA-3.1-8B-INSTRUCT (Abhimanyu Dubey et al., 2024), QWEN2.5-3B-INSTRUCT (Team, 2024), QWEN2.5-7B-INSTRUCT (Team, 2024), GPT-3.5-TURBO, and GPT-4O-MINI (Achiam et al., 2023) as the target LLMs. To ensure a fair comparison with existing memory-based methods, we use the decomposition examples of complex questions for MeLLo and PokeMQA, as prompts.

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Additional details on experimental setting are provided in Appendix D.

6.2 Experimental Results

The results of GDECOM-CQA compared against the baseline models are shown in Tables 1 and 2. These results show that for COMPKE, GDECOM-CQA outperforms the baseline models by a significant margin in most cases while maintaining a comparable performance on MQUAKE.

For example, when considering the COMPKE dataset and Aug-Acc as the evaluation metric, GDECOM-CQA showed an average improvement of 36.60%, 70.29% and 89.11% compared to MeLLo for $\{1, 100, All\}$ -edited on GPT-3.5-TURBO respectively, and 76.83%, 76.03%, and 113.12% on GPT-40-MINI compared to MeLLo. We provide a detailed analysis of these experimental results in the following sections.

Smaller Models. For models with smaller parameters, such as QWEN2.5-3B-INSTRUCT, memory-based methods perform worse than parameter-based methods. There are two main reasons for this: (i) models with smaller parameters have a limited instruction-following ability and struggles to adhere to the required format for planning; and (ii) during the solving stage, these models are unable to effectively integrate model's internal knowledge with external edits to address sub-questions. An example in this regard is the baseline model: PokeMQA, which requires a higher instruction-following capability, performs poorly on both LLAMA-3.1-8B-INSTRUCT, and QWEN2.5-3B-INSTRUCT. It emphasizes that for models with smaller parameters, an effective mechanism for the decomposition (not requiring a significant instruction-following ability) plays a crucial role in the end-performance of the model.

Batch Editing (#k-edits). We observe that the memory-based methods show a decline in the performance with the increase in the number of edits (k). However, for GDECOM-CQA this decline is relatively lower compared with other memory-

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	MQUAK	KE-CF-3K	MQUAKE-T			
Method	1-edited	All-edited	1-edited	All-edited		
Q	WEN2.5-31	B-INSTRUCT				
ROME	8.5	-	29.8	-		
MEMIT	<u>9.5</u>	1.2	33.5	1.8		
MeLLo	6.3	<u>2.8</u>	42.1	35.2		
PoKeMQA	1.9	1.5	3.1	2.2		
GDECOM-CQA (Ours)	27.2	19.6	<u>40.6</u>	<u>30.6</u>		
LLAMA-3.1-8B-INSTRUCT						
ROME	4.1	-	20.5	-		
MEMIT	4.5	2.8	24.8	2.3		
MeLLo	18.6	12.4	38.8	33.0		
PoKeMQA	2.1	1.7	2.8	1.9		
GDECOM-CQA (Ours)	38.8	23.6	65.8	65.0		
	GPT-3.5	-TURBO				
MeLLo	57.4	35.3	88.1	74.5		
PoKeMQA	67.2	48.8	78.2	68.1		
GDECOM-CQA (Ours)	<u>59.5</u>	<u>41.4</u>	81.8	73.1		
	GPT-40-MINI					
MeLLo	48.3	35.0	47.0	40.3		
PoKeMQA	57.3	<u>39.6</u>	73.5	71.0		
GDECOM-CQA (Ours)	60.2	47.4	82.3	78.0		

Table 2: Experiment results for MQuAKE-3K andMQuAKE-T with M-ACC as evaluation metric.

based methods, *e.g.*, MeLLo. This is evident in Figure 8, where we plot the performance of memory-based methods as a function of the number of edits. For instance, for COMPKE with the GPT-3.5-TURBO, from 1-edited to all-edited, Aug-Acc and Ret-Acc for MeLLo decreased by 33.74% and 14.06%, respectively.

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For parameter-based methods, we observe deterioration in performance is higher compared with memory-based methods, especially when the number of edits increase beyond a limit, *e.g.*, k=100. Especially, Ret-Acc metric drops significantly, indicating that the model's original knowledge is compromised. Besides, we find that once the number of edits exceed a certain threshold, *i.e.*, $k \ge 600$, the model loses its ability to maintain coherent conversations and starts generating irrelevant output, shown in Appendix Table 12.

Performance on MQuAKE. GDECOM-CQA 637 achieves the highest performance for three of four 638 target LLMs tested on MQuAKE-CF-3K. Even 639 with the smaller QWEN2.5-3B-INSTRUCT, it out-640 performs the parameter-based method, as multi-641 hop question decomposition is relatively simple 642 and does not require strong instruction-following 643 capabilities. We observe that PoKeMQA perform 644 better on multi-hop questions than complex ques-645 tions, especially for GPT-3.5-TURBO. A possible 646 justification for this is PoKeMQA is specially de-647 signed for multi-hop questions, but its generaliza-648 tion to other questions is poor. 649

650Omission Phenomenon. We also analyze the per-651formance of MeLLo using the original decompo-652sition prompts provided with the model imple-653mentation. We observe that it leads to omission654phenomenon in the decomposition phase, *i.e.*, the655MeLLo's decomposition plan skips certain steps,

specifically the logical intersection part. Underlying justification in this regard is the fact that the conditional confirmation operations, *e.g.*, logical intersection, does not appear in the multi-hop questions. This showcases that the generalization of decomposition operation through prompt examples is insufficient, highlighting the essence of incorporating examples similar to the question being decomposed. An example illustration in this regard is provided in Appendix Table 9. 656

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6.3 Ablation Study

We mainly conduct ablation studies on the following modules: (*i*) Demonstration selection, (*ii*) Chain-of-thought solving, (*iii*) Subject filtering, with results explained as follows:

(*i*) **Demonstration Selection.** Results for the ablation studies for the demonstration selection are shown in Figure 7. These results show that removing demonstration selection in planning stage, decreases the Aug-Acc drops by 6.75% on average. These results confirm the effectiveness of our dynamic prompt constructing approach, emphasizing that providing example demonstrations similar to the complex question indeed help the model to achieve better decomposition ability.

(*ii*) **Chain-of-thought Solving.** The results of GDECOM-CQA without chain-of-thought reasoning approach are shown in Figure 9. These results show that without using a chain-of-thought approach to integrate internal knowledge and external edits, the performance drops by 37.45% on average. We attribute this deterioration in performance to two key factors: (a) The model is reluctant to incorporate new knowledge, and (b) The model struggles to determine whether the fact edits are relevant to the question.

(*iii*) **Subject Filtering.** The results of GDECOM-CQA for subject filtering are shown in Figure 10. We observe across all three LLMs, the performance of the model with subject filtering as the retrieval strategy using subject filtering exceeds than that of direct semantic retrieval. This step helps filter out a lot of irrelevant edits, thus improving the overall effectiveness of GDECOM-CQA.

7 Conclusion

In this paper, we present the concept of complex questions, and introduce a new benchmark COMPKE, along with a approach GDECOM-CQA, for answering complex questions. Experimental evaluation shows GDECOM-CQA outperforms the baseline models by a significant margin.

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This work poses following limitations:

- GDECOM-CQA incurs additional overhead in constructing the dynamic decomposition prompt, although it is minimal compared to the subsequent overhead.
- GDECOM-CQA uses an iterative approach for solving complex questions. Intermediate errors may propagate along the path and impact the final answer. For this, our current implementation lacks an effective mechanism for recovery from errors in the intermediate stages.

Ethics Statement

This work directly deals with updating the capability and/or editing the knowledge of large models. It has the potential for abuse, such as adding poisonous misinformation, malicious content, bias etc. Keeping in view these concerns, we highlight this work must not be used under critical settings.

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A Related Work

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A.1 Knowledge Editing Benchmarks

KE is a critical area of research for LLMs, addressing the need to update knowledge to respond to dynamic real-world queries. Several benchmarks have been developed for evaluating KE methods. Early works like COUNTERFACT (Meng et al., 2022a) assess counterfactual updates, while ZsRE (Levy et al., 2017) and MzsRE (Wang et al., 2023d) extend evaluations to zeroshot and multilingual settings. ECBD (Onoe et al., 2023) examines whether newly injected facts can propagate reasoning across related entities. Easyedit (Wang et al., 2023b) propose an easy-to-use framework for LLMs that supports a variety of cutting-edge knowledge editing approaches. More recent works such as MQUAKE (Zhong et al., 2023), MQA-AEVAL (Ali et al., 2024) extend the evaluation to multi-hop reasoning under KE. TEMPLAMA (Zheng et al., 2023b) and ATOKE (Yin et al., 2023) explore the task of time-series knowledge editing, aiming to modify knowledge without affecting knowledge from other time periods. Nevertheless, these benchmarks fall short in capturing real-world complexity, such as reasoning with one-to-many relations or combining entities via logical operations like intersection and union. To bridge this gap benchmark, we propose COMPKE, encompassing 11,921 questions involving complex reasoning structures, aimed at evaluating the performance of KE methods for complex questions.

A.2 More detailed Related Work

Besides benchmarks, many researchers in recent years have explored knowledge editing from various perspectives. There is a type of research that aim to understand the working mechanisms of knowledge editing techniques, such as the relationship between model parameter localization and editing (Wang et al., 2024; Niu et al., 2024; Hase et al., 2024a,b; Ferrando et al., 2024; Gupta et al., 2024; Yao et al., 2024). For example, causal tracing does not effectively indicate the optimal editing location (Hase et al., 2024a), and some researchers have also employed computation graph to uncover the specific impacts on the model's internal behavior of knowledge editing (Yao et al., 2024). Another line of research focuses on enhancing the effectiveness of knowledge editing in specific scenarios (Rozner et al., 2024; Ma et al.,

2024; De La Torre et al., 2024; Huang et al., 997 2024; Deng et al., 2024; Peng et al., 2024; Cai 998 et al., 2024). For instance, bidirectional relation-999 ship modeling has been proposed to address con-1000 sistency issues in bidirectional models (Ma et al., 1001 2024), while real-time knowledge editing meth-1002 ods have been developed to adapt to dynamic en-1003 vironments where knowledge evolves frequently 1004 (De La Torre et al., 2024). Additionally, this pa-1005 per focuses on exploring knowledge editing in the 1006 context of complex logical reasoning. Also some 1007 studies focus on addressing the side effects of 1008 knowledge editing techniques (Hsueh et al., 2024; 1009 Gu et al., 2024; He et al., 2023; Hua et al., 2024; 1010 Yang et al., 2024; Cohen et al., 2023; Nishi et al., 1011 2024). 1012

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B Additional Preliminaries

B.1 Multi-hop Question Answering

A multi-hop question can be represented as $s_1 \xrightarrow{r_1} s_2 \cdots \xrightarrow{r_{n-1}} s_n$, continuously mapping one entity to another. For example, consider the question "Who is the spouse of president of U.S.", it an be represented as U.S. $\xrightarrow{\text{president is}}$ Donald Trump $\xrightarrow{\text{spouse is}}$ Melania Trump.

B.2 Multi-hop Question Answering under KE.

We use $e = (s, r, o \rightarrow o')$ to represent a knowledge edit indicating that the object entity of subject s with relation r is updated from o to o'. This task is to solve multi-hop questions under a batch of knowledge edits $\mathcal{E} = \{e_1, e_2, \dots\}$.

B.3 MQA with Complex Question Answering.

We consider the previously studied linear multihop questions as a special case of complex questions involving continuous mapping of entity through a series of relational links, forming a oneway graph chain: $S_1 \xrightarrow{L_1} S_2 \xrightarrow{L_2} \cdots \xrightarrow{L_{n-1}} S_n$, where *n* represents the number of reasoning hops. Note that compared to complex questions, here the intermediate set S_i only encompasses a single entity, and L_i only covers one-to-one relation mapping.

C COMPKE (Additional Details)

Figure 4 shows the process by which we construct1040complex question. Figure 11 gives some examples of the structures in COMPKE and the corre-104110421042

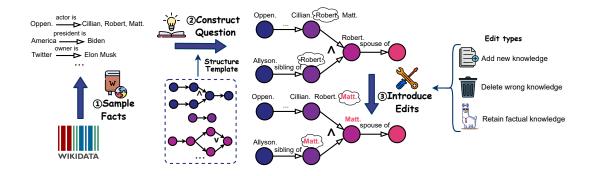


Figure 4: The construction process of COMPKE

sponding decomposition methods. Table 6 gives
the SPARQL which we used to sample facts from
WikiData.

D Additional Experimental Settings

D.1 Datasets

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We provide the statistics of newly proposed data COMPKE in Table 3. The existing data **MOUAKE** includes two datasets: MQUAKE-CF-3K, which is based on counterfactual editing, and MQUAKE-T, which is based on real-world changes. These datasets cover k-hop questions $(k \in \{2, 3, 4\})$, each associated with one or more edits. Statistics are presented in Table 4.

#Edits	1	2	3	4	5	Total
Edit_num	9,697	998	1,118	103	8	11,924
Hop_num	200	424	5,770	2,949	2,581	11,924

Table 3: Statistical Results of COMPKE dataset.

Datasets	#Edits	2-hop	3-hop	4-hop	Total
	1	513	356	224	1,093
	2	487	334	246	1,067
MQUAKE-CF-3K	3	-	310	262	572
	4	-	-	268	268
	All	1,000	1,000	1,000	3,000
MQUAKE-T	1	1,421	445	2	1,868

Table 4: Statistics of the MQUAKE dataset.

D.2 Baselines

ROME. ROME by Meng et al. (2022a) uses a locate-then-edit paradigm. For a specific knowledge editing, ROME employs causal tracing to pin-point the exact layer of the MLP module within the Transformer model architecture that encodes the paticular factual association. Then it will perform a rank-one modification on the identified layer.

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MEMIT. MEMIT by Meng et al. (2022b) is an evolution of ROME to transcend the inherent limitation that ROME can only edit a single fact at a time. At a time, MEMIT can identify and modify multiple layers in a single pass, allowing for the simultaneous editing of numerous facts.

MeLLo. MeLLo by Zhong et al. (2023) adopts a strategy that alternates between planning and solving stage to solve multi-hop question. It employ a semantic-based retrieval to retrieve relevant edits, and a self-checking mechanism to enable the model to assess the relevance of edits and modifications.

PokeMQA. PokeMQA by Gu et al. (2023) is a memory-based method that extends MeLLo and proposes a two-stage retrieval process to enhance the success rate of retrieving relevant edits.

D.3 Evaluation Metrics

Detailed metrics and mathematical definitions are given below:

(i) Augment Accuracy (Aug-Acc) is used to measure whether the edited model can response added knowledge on complex questions. The formula for calculating Aug-Acc is as follows:

$$\mathbb{E}_{q \in \mathcal{Q}}(\left|M'(q) \cap \mathcal{A}_{aug}\right| / |\mathcal{A}_{aug}|) \tag{5}$$

Where $M'(\cdot)$ represents the edited model, and Q denote the datasets for complex questions, $A_{aug} = A' \setminus A$, A' is edited answer set and A is original answer set.

(ii) Retention Accuracy (Ret-Acc) is used to measure whether the edited model can retain the original knowledge on complex questions. The formula for calculating Ret-Acc is as follows:

$$\mathbb{E}_{q\in\mathcal{Q}}(\left|M'(q)\cap\mathcal{A}_{ret}\right|/|\mathcal{A}_{ret}|) \tag{6}$$

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1100 Where $\mathcal{A}_{ret} = \mathcal{A}' \cap \mathcal{A}$.

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(iii) Multi-hop Accuracy (M-Acc) is used to
measure the accuracy for multi-hop question under knowledge editing. The formula for calculating M-Acc is as follows:

$$\mathbb{1}\left[\bigvee_{q\in\mathcal{Q}}[M'(q)=a']\right].$$
(7)

1106 Where $M'(\cdot)$ represents the edited model, and 1107 Q and a' denote the multi-hop questions and the 1108 final-hop answers for each data, respectively.

1109 D.4 Hyper-parameters Analysis.

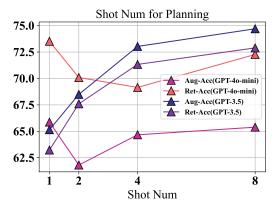


Figure 5: Hyper-parameters study on number of examples for decomposition prompt: On COMPKE with 1-edited, the curves for the *Aug-Acc* and *Ret-Acc* metrics in our method vary with the number of shots. The scores of GPT-3.5-TURBO-INSTRUCT increase monotonically as the number of shots increases, whereas GPT-40-MINI shows insensitivity to the number of shots.

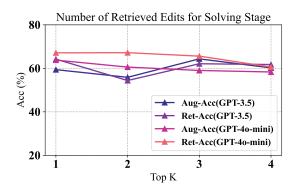


Figure 6: Hyperparameter Study of retrieved edits: In this study, conducted on COMPKE with 300 edits and the Aug-Acc metric, Top-K refers to select the top-k retrieved edits.

1110 D.5 Experiment Setup

1111Table 11 shows the hyperparameter settings for1112the parameter-based methods. For the experiments

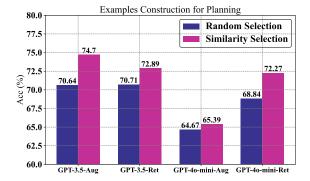


Figure 7: Ablation Study on demonstration selection for the planning stage. We compare the impact of randomly selecting examples from the demonstration memory versus selecting them based on semantic similarity.

involving ROME and MEMIT, we utilized four NVIDIA Tesla L20 GPUs, with 48GB of memory. A single RTX 4090 GPU was used for MeLLo, PokeMQA, and GDECOM-CQA. 1113

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E Additional Experimental results

E.1 Results for Batch Editing(#*k*-edits)

The results for the batch editing, *i.e.*, varying the number of edits (k) are presented in Figure 8.

We mainly conducted two hyper-parameters exploration experiments: the number of demonstrations retrieved during the planning phase (i.e., *i*-shot, where $i \in \{1, 2, 4, 8\}$) and the number of top-k edits ($k \in \{1, 2, 3, 4\}$) selected during the retrieval phase. The results are shown in Figures 5 and 6.

For GPT-3.5-TURBO-INSTRUCT we observe: both metrics, *i.e.*, Aug-Acc and Ret-Acc improve steadily as the number of demonstrations increase. However, for GPT-40-MINI, we observe an abnormal behavior with higher scores for 1-shot and 8-shot settings while lower scores for 2-shot and 4-shot results are lower. This shows that overall GPT-3.5-TURBO-INSTRUCT shows more stable results compared to that of GPT-40-MINI.

As the number of retrieved edits increases, overall performance decreases. However, when 3 edits are selected, performance on GPT-3.5-TURBO-INSTRUCT improves. One possible reason is that some of the matching edits fall outside the similarity range of the top-2. While using more edits can reduce the retrieval error rate, selecting too many edits may introduce additional context that interferes with the model's response. GPT-3.5-TURBO-INSTRUCT is more stable than GPT-40-

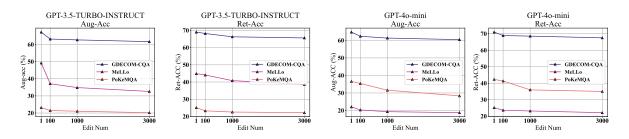


Figure 8: Performance for GDECOM-CQA, MeLLo, and PoKeMQA on the GPT-3.5-TURBO-INSTRUCT and GPT-40-MINI, with edit number varies from 1 to 3000.

1147 MINI in this scenario.

1148 E.2 Ablation Study

1149In this section, we plot the results for the ablation1150experiments. We report the results for the CoT1151experiments in Figure 9. The results for the sub-1152ject filtering experiments are reported in Figure 10.1153The results for the demonstration selection exper-1154iments are shown in Figure 7.

Method	1-ed	ited	All-edited		
	Aug-Acc	Ret-Acc	Aug-Acc	Ret-Acc	
GPT-3.5-TURBO-INSTRUCT					
MELLO	15.38	18.50	11.17	19.92	
PokeMQA	6.18	5.11	4.72	4.44	
GDECOM-CQA (Ours)	74.90	61.77	69.72	61.57	
GPT-40-MINI-2024-07-18					
MELLO	33.87	27.36	17.14	20.70	
PokeMQA	10.18	22.22	9.81	17.55	
GDECOM-CQA (Ours)	81.81	64.88	77.81	64.00	

Table 5: Experiment Result on subset of COMPKE, which include data with incomplete retrieving challenge.

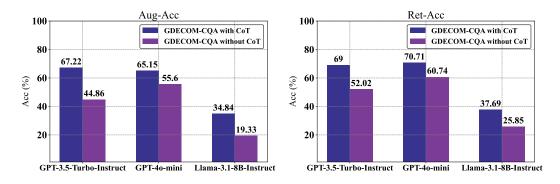


Figure 9: Ablation Study on CoT for Solving Stage: We evaluate the impact of CoT solving on COMPKE with 1-edited.

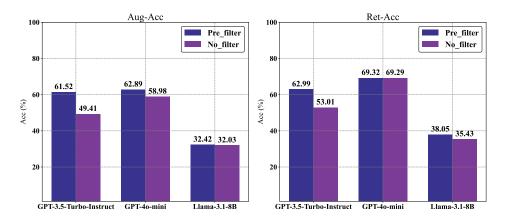
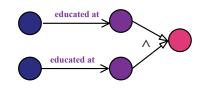


Figure 10: Ablation Study on Subject filtering strategy: This figure illustrates the impact of subject-based filtering of irrelevant edits versus direct retrieval in our method, evaluated on COMPKE with 3000-edited.

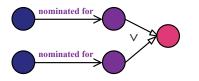
SQL Query	Description
SELECT ?object WHERE {	This SPARQL query retrieves the object asso-
wd:{qid} wdt:pid ?object.	ciated with the <pid> of entity.</pid>
<pre>FILTER(LANG(?object) = "en").</pre>	
}	
<pre>SELECT (COUNT(?statement) AS ?referencesCount) WHERE { wd:{entity_id} ?p ?statement. ?statement prov:wasDerivedFrom ?source. }</pre>	This SPARQL query retrieves the count of ref- erences (i.e., the number of statements that re- fer to a source) for a specific entity. This query is used to filters out triples with low references counts(i.e.,unpopular entity).
<pre>SELECT ?alias WHERE { wd:{qid} skos:altLabel ?alias.</pre>	This SPARQL query retrieves the aliases asso- ciated with the entity,
<pre>FILTER(LANG(?alias) = "en"). }</pre>	,,

Table 6: S	SPARQL	Queries	and I	Descriptions
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Q: Which educational institutions did both *Ted* Schroeder and Laurene Powell Jobs attend?



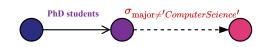
Q: What awards has either the film *Gladiator* or *Branko Lustig* been nominated for?



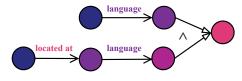
Q: Who among the crew members of *Mortal Kombat:* Annihilation holds American citizenship?



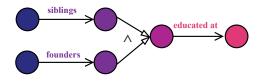
Q: Which of Nikolaus Joseph von Jacquin's PhD students did not major in computer science?



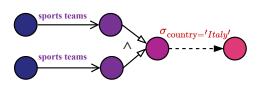
Q: Which language spoken in *Palau* is the same as the official language of the country where *Ball State University* is located?



Q: If someone is both a sibling of *Mona Simpson* and one of the founders of *Apple*, what is this person's nationality?



Q: Which sports teams are associated with both Papin and Christophe Dugarry are located in Italy?



T1: Which educational institution did Ted Schroeder attend? T2: Which educational institution did Laurene Powell Jobs attend? T3: Logic Operation: Intersection T1 and T2.

T1: What awards has the film Gladiator been nominated for? T2: What awards has Branko Lustig been nominated for?

T3: Logic Operation: Union T1 and T2.

T1:Who are the crew members of the movie Mortal Kombat: Annihilation? T2:What is the nationality of each person in T1? T3:Logic Operation: Select persons from T2 whose nationality is American.

T1: Who are the PhD students of Nikolaus Joseph von Jacquin?

T2: What are the majors of each person in T1? T3: Logic Operation: Select persons from T2 whose major is not Computer Science.

- T1: What is the official language of Palau?
- T2: What is the location of Ball State University?
- T3: What is the official language of T2?
- T4: Logic Operation: Intersection T1 and T3.

T1: Who are the siblings of Mona Simpson?

- T2: Who are the founders of Apple?
- T3: Logic Operation: Intersection T1 and T2.
- T4: What is the nationality of T3?

T1: Which team has Papin been associated with? T2: Which team has Christophe Dugarry been associated with? T3: Logic Operation: Intersection T1 and T2.

T4: Where did each team of T3 located?

T5: Logic Operation: Select team from T4 that are located in Italy.

Figure 11: Some typical question structure in our dataset

[8 in-context demonstrations abbreviated] Question: Which cast members of Zabriskie Point hold citizenship in the United States of America? PLAN STAGE: start point: Zabriskie Point Sub tasks: T1: Who are the cast members of the movie Zabriskie Point? subject:Zabriskie Point T2: What is the nationality of each person in T1? subject:T1 T3: Select persons from T2 whose nationality is USA. subject:None Solve Stage: Executing task T1: Who are the cast members of the movie Zabriskie Point? context:None Executing Retrieval:query=Who are the cast members of the movie Zabriskie Point? Edits: ['The country to which Paul Fix belongs is France'] Thinking Process: The question does not involve information from previous questions; the provided Updated Knowledge is relevant to the question but does not directly provide any information about the cast members of the movie 'Zabriskie Point.' Since there is no updated information on the cast, I will use my own understanding to respond. Answer: The cast members of the movie Zabriskie Point are: Mark Frechette, Daria Halprin, Paul Fix, Rod Taylor, Christina Hobbs, and Michael M. Murphy. Answer List: ['Mark Frechette', 'Daria Halprin', 'Paul Fix', 'Rod Taylor', 'Christina Hobbs', 'Michael M. Murphy'] Executing task T2: What is the nationality of each person in T1? context: Answer of T1: The cast members of the movie Zabriskie Point are: Mark Frechette, Daria Halprin, Paul Fix, Rod Taylor and Christina Hobbs. Executing Retrieval:query=What is the nationality of Mark Frechette? Executing Retrieval:query=What is the nationality of Daria Halprin? Executing Retrieval:query=What is the nationality of Paul Fix? Executing Retrieval:query=What is the nationality of Rod Taylor? Executing Retrieval:query=What is the nationality of Christina Hobbs? Edits: ['The country to which Paul Fix belongs is France', 'The country to which Rod Taylor belongs is United States of America'] Thinking Process: The question involves the result of T1 in the context, so I look for it in the relevant context. T1 provides the names of the cast members of the movie 'Zabriskie Point.' The Updated Knowledge provides nationality information for Paul Fix and Rod Taylor. Since there are no updates for the other cast members, I will use my own understanding for them. Answer: Mark Frechette is American. Daria Halprin is American. Paul Fix is French. Rod Taylor is American. Christina Hobbs is American. Answer List: ['American', 'American', 'French', 'American', 'American', 'American'] Executing task T3: Select persons from T2 whose nationality is USA. context: Answer of T1: The cast members of the movie Zabriskie Point are: Mark Frechette, Daria Halprin, Paul Fix, Rod Taylor and Christina Hobbs. Answer of T2:Mark Frechette is American. Daria Halprin is American. Paul Fix is French. Rod Taylor is American. Christina Hobbs is American. Edits: None Thinking Process: The question involves filtering the information from T2 to identify individuals whose nationality is the USA. According to T2, the relevant individuals mentioned to be American are Mark Frechette, Daria Halprin, Rod Taylor and Christina Hobbs. Therefore, all individuals listed in T2 except for Paul Fix (who is French) should be included in the answer. **Answer:** The persons from T2 whose nationality is USA are Mark Frechette, Daria Halprin, Rod Taylor and Christina Hobbs. Answer List: [Mark Frechette', 'Daria Halprin', 'Rod Taylor', 'Christina Hobbs']

Table 7: An running case of GDECOM-CQA

Which cast members of Zabriskie Point hold citizenship in the United Question: States of America? Subquestion: Who are the cast members of 'Zabriskie Point'? Generated answer: The cast members of 'Zabriskie Point' include Mark Frechette, Daria Halprin, Paul Fix, Rod Taylor, Christina Hobbs Retrieval: The country to which Harrison Ford belongs is France Retrieved fact does not contradict to generated answer, so the intermediate answer is: Mark Frechette and Daria Halprin. Subquestion: What is the country of citizenship of Mark Frechette, Daria Halprin, Paul Fix, Rod Taylor, Christina Hobbs? Generated answer: Mark Frechette, Daria Halprin, Paul Fix, and Christina Hobbs are all from the United States, while Rod Taylor is from Australia. Retrieval: The country to which Paul Fix belongs is France Retrieved fact contradicts to generated answer, so the intermediate answer is: Mark Frechette, Daria Halprin and Christina Hobbs Final answer: Mark Frechette, Daria Halprin and Christina Hobbs.

Table 8: MeLLo Failure on multi entity retrieval

Question: If a person is the director of both Thief and Ali, which country does this person belong to? Subquestion: Who is the director of Thief? Generated answer: The director of Thief is Michael Mann. Retrieval:The country to which Michael Mann belongs is Italy Retrieved fact does not contradict to generated answer, so the intermediate answer is: Italy. Subquestion: Who is the director of Ali? Generated answer: The director of Ali is Michael Mann. Retrieval:The country to which Michael Mann belongs is Italy Retrieved fact does not contradict to generated answer, so the intermediate answer is: Italy. Final answer: Italy

Table 9: The decomposition of this problem by Mello did not take into account logical operations.

Question: Which cast members of Zabriskie Point hold citizenship in the United States of America? Answer:Dennis Hopper and Brooke Shields hold citizenship in the United States of America

Table 10: MEMIT Failure on Qwen2.5-7B

Question: What nominations for awards do both "In America" and Christian Bale share? Edit Num=1: Model Output: Both In America and Christian Bale share Golden Globe nominations. Edit Num=100: Model Output: Bailmailboxerials靥earable standards, and it is clear that this is a difficult task. Can you give meCloseOperationunded(bind)care(I Lothra 1000... Crimes of the Heart is a crime novel about the heart. The book is a satire of___ I'myncync Edit Num=1000: Model Output: 澍澍 greedy澍旄澍blasnown镳ley澍nown" 澍澍澍澍澍nown Cov澍 nick澍 �真爱igeltotalCount Usa澍放过澍澍放过nown镳bservable finishn澍澍澍不出enkoiment澍放 过ocopDAQocop放过澍放`zczeenko Usa澍enko澍放过镳澍onom

Figure 12: When the edit batch size increases, the MEMIT method outputs a large amount of gibberish after models like Qwen-2.5-3B and other smaller models.

ROME :

```
layers: [5],
fact_token: subject_last,
v_num_grad_steps: 25(for Llama-3.1-8B)||15(for Qwen2.5-3B),
v_lr: 5e-1,
v_loss_layer: 31(for Llama-3.1-8B)||35(for Qwen2.5-3B),
v_weight_decay: 1e-3,
clamp_norm_factor: 4,
kl factor: 0.0625,
mom2_adjustment: false,
context_template_length_params: [[5, 10], [10, 10]]
MEMIT:
layers: [3,4,5,6,7,8],
clamp_norm_factor: 4,
layer_selection: all,
fact_token: subject_last,
v_num_grad_steps: 25(for Llama-3.1-8B)||15(for Qwen2.5-3B),
v_lr: 5e-1,
v_loss_layer: 31(for Llama-3.1-8B)||35(for Qwen2.5-3B),
```

v_weight_decay: 1e-3, kl_factor: 0.0625, mom2_adjustment: true, mom2_update_weight: 15000, mom2_dataset: wikipedia, mom2_n_samples: 100000, mom2_dtype: float32

Table 11: Several key hyperparameters for parameter-based KE method

Question: Who is someone that is both a member of the cast of the movie Birthday Girl and a sibling of Cecile Cassel? start point: Birthday Girl, Cecile Cassel Sub tasks: T1: Who are the cast members of the movie Birthday Girl? subject:Birthday Girl T2: Who are the sibling of Cecile Cassel? subject:Cecile Cassel T3: Logic Operation: Intersection T1 and T2. subject:None Question: Which members of the cast of Diner are not French? start point: Diner Sub tasks: T1: Who are the cast members of the movie Diner? subject:Diner T2: What is the nationality of each person of T1? subject:T1 T3: Logic Operation: Select persons from T2 who is not French. subject:None Question: Where were either The Abyss or Twilight Zone: The Movie filmed? start point: The Abyss, Twilight Zone: The Movie Sub tasks: T1: Where was The Abyss filmed? subject: The Abyss T2: Where was Twilight Zone: The Movie filmed? subject:Twilight Zone: The Movie T3: Logic Operation: Union T1 and T2 subject:None Question: Multiple Choice: Who are the authors of the books The Farthest Shore, Tehanu, and Tales from Earthsea? A. Robert Harris B. Ursula K. Le Guin C. Elisabeth Hauptmann D. Anna Komnene start point: The Farthest Shore, Tehanu, Tales from Earthsea Sub tasks: T1:Who is the author of The Farthest Shore? subject:The Farthest Shore T2:Who is the author of Tehanu? subject:Tehanu T3:Who is the author of Tales from Earthsea? subject:Tales from Earthsea T4:Choose the correct answer(s) that have the same meaning as the authors from T1, T2, and T3: A. Robert Harris B. Ursula K. Le Guin C. Elisabeth Hauptmann D. Anna Komnene subject:None

Table 12: The prompt for Planing Stage, with only a portion of the prompt shown due to limited space.

Based on the latest information about Open Hearts, Valhalla Rising, Pusher II, Consider the relevant context: None Updated Knowledge: The cast members of movie Open Hearts are Nikolaj Lie Kaas, Paprika Steen, Sonja Richter, Mads Mikkelsen, Jackie Chan, Michelle Yeoh, Jaden Smith, Taraji P. Henson. please answer the following: Who are the cast members of the movie Open Hearts? Thinking Process: The question does not involve information from previous questions; the provided Updated Knowledge is relevant to the question and should be taken as authoritative, so the information given should be copied directly as the answer. Answer: The cast members of movie Open Hearts are Nikolaj Lie Kaas, Paprika Steen, Sonja Richter, Mads Mikkelsen, Jackie Chan, Michelle Yeoh, Jaden Smith, Taraji P. Henson. Answer List: 'Nikolaj Lie Kaas', 'Paprika Steen', 'Sonja Richter', 'Mads Mikkelsen', 'Jackie Chan', 'Michelle Yeoh', 'Jaden Smith', 'Taraji P. Henson' Based on the latest information about Courage Under Fire, CEO of Dell Technologies, Consider the relevant context: None Updated Knowledge: None please answer the following question: Who are the cast members of the movie The Public Eye? Thinking Process: The question does not involve information from previous questions; The updated knowledge does not provide any information related to the issue, indicating that the information has not been updated; therefore, I will directly use my own understanding to response. Answer: The cast member of 'The Public Eye' includes: Joe Pesci, Barbara Hershey, Jerry Adler, Richard T. Jones, William Schallert, Anne Meara, Peter Riegert, Philip Bosco. Answer List:'Joe Pesci', 'Barbara Hershey', 'Jerry Adler', 'Richard T. Jones', 'William Schallert', 'Anne Meara', 'Peter Riegert', 'Philip Bosco' Based on the latest information about Courage Under Fire, CEO of Dell Technologies, Consider the relevant context: T1: The movie 'Courage Under Fire' was filmed in Austin, El Paso, Fort Hood, San Antonio, and Southern California. T2: The CEO of Dell Technologies is Michael S. Dell. T3:Michael S. Dell reside in Austin, El Paso. Updated Knowledge: None please answer the following: Intersection the object of T1 AND object of T3. Thinking Process: The question involves the result of T1 and T3 in the context, so I look for it in the relevant context.Updated Knowledge is empty, which indicates that it does not involve updated knowledge. I will directly perform logical operations to take the intersection of the answers to the two previous questions. Answer: The Intersection of the object of T1 AND object of T3 is Austin and E1 Paso. Answer List: 'Austin', 'El Paso'

Table 13: The prompt for **Solving Stage**, with only a portion of the prompt shown due to limited space.

Relation	Question template	Cloze-style statement template
P40	Who are [S]'s children?	[S]'s children are
P69	Where did [S] receive education?	The university where [S] was educated is
P3373	Who are the siblings of [S]?	[S]'s siblings are
P50	Who are the author(s) of [S]? (list all)	The author(s) of [S] is(are)
P161	Who are the cast members of movie [S]?	The cast members of movie [S] are
P112	Who are the people who founded company [S]?	The people who founded Company [S] are
P54	Which organizations is [S] a member of?	[S] is a member of the following organization
P915	Where were movie [S] filmed?	The movie [S] was filmed at
P37	What are the official languages of country [S]?	The official languages of country [S] are
P1830	Which companies does S own?	[S] owns the following companies
P6	Who are the heads of government for [S]?	The heads of government for [S] are
P803	What are the professorship ranks for [S]?	The professorship ranks for [S] are
P185	Who are the doctoral students of [S]?	The doctoral students of [S] are
P57	Who is the director of the film [S]?	The film [S] is directed by
P1411	What awards was the film [S] nominated for?	The film [S] is nominated for
P1346	Who are the winners for [S] prize?	The winners for [S] prize are
P286	Who are the head coaches for team [S]?	The head coaches for team [S] are
P166	What awards did [S] receive?	The award received by [S] are
P800	What are the notable works of [S]?	The notable works of [S] are
P725	Who are the voice actors in the movie [S]?	The voice actor in the movie [S] are
P655	Who are the translators of the book [S]?	The translators of the book [S] are
P27	Which country is [S] a citizen of?	The country to which [S] belongs is
P21	What's [S]'s gender?	[S]'s gender is
P169	Who is the CEO of company [S]?	The CEO of company [S] is
P35	Who is the head of state of country [S]?	The head of state of country [S] is
P26	Who is the spouse of [S]?	The spouse of [S] is
P1037	Who is the director of [S]?	The director of [S] is
P20	In which city did [S] die?	[S] died in the city of
P551	Where does [S] live?	[S] lives in the place of
P159	Where is the headquarters of company [S]?	The headquarters of company [S] is located i
P17	In which country is [S] located?	[S] is located in the country of
P108	Who is the employer of [S]?	[S] is an employee in the organization of
P102	Which political party is [S] affiliated with?	[S] is affiliated with the political party of
P937	Where does [S] work?	[S] works in the place of
P140	What is the religion of [S]?	[S] is affiliated with the religion of
P106	What is [S]'s occupation?	[S]'s occupation is
P30	On which continent is country [S] located?	Country [S] is located in the continent of
P38	What is the currency of country [S]?	The currency of country [S] is
P641	Which sport is [S] associated with?	[S] is associated with the sport of
P36	What is the capital of country [S]?	The capital of country [S] is

Table 14: Relations we use to construct our dataset