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# Beyond Gradient and Priors in Privacy Attacks: Leveraging Pooler Layer Inputs of Language Models in Federated Learning

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## Abstract

1 Federated learning (FL) emphasizes decentralized training by storing data locally  
2 and transmitting only model updates, underlining user privacy. However, a line  
3 of work on privacy attacks undermines user privacy by extracting sensitive data  
4 from large language models during FL. Yet, these attack techniques face distinct  
5 hurdles: some work chiefly with limited batch sizes (e.g., batch size of 1), and  
6 others can be easily defended or are transparently detectable. This paper introduces  
7 an innovative approach that is challenging to detect and defend, significantly  
8 enhancing the recovery rate of text in various batch-size settings. Building on  
9 fundamental gradient matching and domain prior knowledge, we enhance the  
10 recovery by tapping into the input of the Pooler layer of language models, offering  
11 additional feature-level guidance that effectively assists optimization-based attacks.  
12 We benchmark our method using text classification tasks on datasets such as CoLA,  
13 SST, and Rotten Tomatoes. Across different batch sizes and models, our approach  
14 consistently outperforms previous state-of-the-art results.

## 15 1 Introduction

16 Language models trained under the Federated Learning paradigm play a pivotal role in diverse  
17 applications such as next-word predictions on mobile devices and electronic health record analysis in  
18 hospitals (Ramaswamy et al., 2019; Li et al., 2020). This training paradigm prioritizes user privacy  
19 by restricting raw data access to local devices and centralizing only the model’s updates, such as  
20 gradients and parameters (McMahan et al., 2017). While the FL framework is created to protect user  
21 privacy, vulnerabilities still persist. In the realm of Computer Vision (CV), there has been significant  
22 exploration, especially regarding image reconstruction attacks (Geiping et al., 2020; Yin et al., 2021;  
23 Jeon et al., 2021). In contrast, the Natural Language Processing (NLP) domain remains largely  
24 uncharted (Balunovic et al., 2022; Gupta et al., 2022).

25 Recent studies have investigated vulnerabilities of training data in Federated Learning when applied  
26 to language models (Zhu et al., 2019; Deng et al., 2021). These researches generally fall into two  
27 categories: **Malicious Attack** and **Eavesdropping Attack**. Malicious attacks typically come from  
28 compromised servers that release malicious parameter updates or even alter model architectures to  
29 covertly acquire user data (Fowl et al., 2021, 2022; Boenisch et al., 2023). They are usually obvious  
30 and can be easily detected by examining predefined architectures or using real-time local feature  
31 monitoring (Fowl et al., 2022). On the other hand, eavesdropping attacks are subtle, making them  
32 harder to detect. Adhering to the honest-but-curious principle, adversaries leverage gradient data  
33 and prior knowledge to extract sensitive information (Zhu et al., 2019; Deng et al., 2021; Balunovic  
34 et al., 2022; Gupta et al., 2022). However, their efficacy is contingent on conditions like minimal  
35 batch sizes, with performance degradation as batch sizes grow, as noted by Balunovic et al. (2022).

36 Different from these findings, our research introduces a robust strategy that is difficult to both detect  
 37 and counteract, significantly amplifying the effectiveness of the attack.

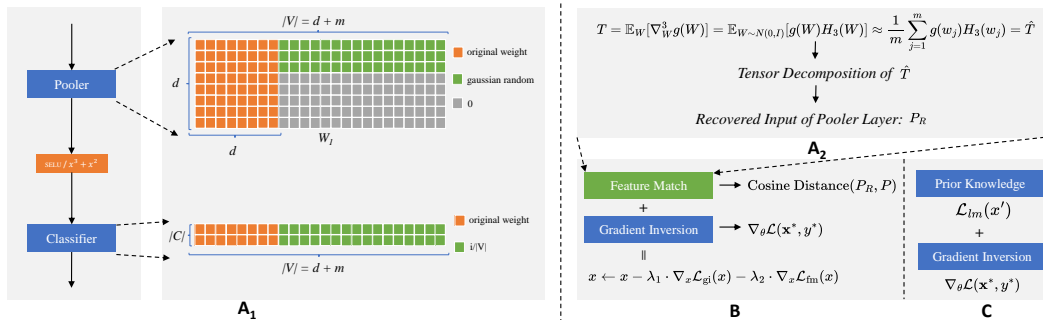


Figure 1: Architecture overview of our proposed attack mechanism on language models. **A<sub>1</sub>**: Subtle modification of architecture and strategic weight initialization. **A<sub>2</sub>**: Two-layer-neural-network-based reconstruction. **B**: Continuous optimization with gradient inversion and feature match. **C**: Discrete optimization with gradient matching loss and perplexity from pre-trained language models.

38 **Improved text privacy attack by leveraging unique feature information** Upon examining the  
 39 current vulnerabilities in FL, we have identified an issue with the gradient-based attack: the gradient  
 40 will be averaged in the context of large batch sizes and long sentences, thereby diluting the embedded  
 41 information and reducing the attack’s effectiveness. To address this challenge, we propose an innova-  
 42 tive solution by recovering the intermediate feature to provide enhanced supervisory information.  
 43 Specifically, we focus on Transformer-based language models equipped with a unique Pooler layer.  
 44 This layer handles the final hidden state of the [CLS] token, capturing a comprehensive representation  
 45 of the input text. Subsequently, we employ a two-layer-neural-network-based reconstruction tech-  
 46 nique to meticulously retrieve the inputs destined for this layer. In this way, our method introduces  
 47 a fresh continuous supervisory signal besides gradients by leveraging the recovered intermediate  
 48 features as a reference point. When combined with gradient inversion and prior knowledge, our ap-  
 49 proach consistently outperforms previous ones on a range of benchmark datasets and varied scenarios  
 50 (where batch size  $> 1$ ), underlining its resilience and versatility.

51 **Main Contributions** Our main contributions are described as follows:

- 52 1. **Technical Contribution in Attack Method:** We are the first to suggest utilizing intermedi-  
 53 ate features as continuous supervised signals for text privacy attacks.
- 54 2. **Advancement in Intermediate Features Recovery:** We pioneered refining a two-layer-  
 55 neural-network-based reconstruction method in practical deep language models, successfully  
 56 recovering intermediate features.
- 57 3. **Superiority in Diverse Settings:** Our method consistently outperforms others across  
 58 various benchmarks and settings by leveraging gradients, priors knowledge, and intermediate  
 59 features, highlighting its robustness and adaptability.

## 60 2 Related Work

61 Federated learning, while emphasizing data privacy, is still vulnerable to privacy attacks. Specifically,  
 62 in the realm of computer vision, model updates can be manipulated to reveal sensitive data, enabling  
 63 almost perfect image recreation (Phong et al., 2017; Zhao et al., 2020). Textual data, particularly with  
 64 prevalent Transformer architectures, presents distinct challenges, as their design inherently conceals  
 65 specific token details (Huang et al., 2021; Geiping et al., 2020). Two primary types of attacks for text  
 66 emerge: **Malicious Attacks**, where the central server itself is the threat, embedding backdoors or  
 67 facilitating training data reconstruction (Fowl et al., 2021, 2022; Boenisch et al., 2023; Balunovic  
 68 et al., 2022); and **Eavesdropping Attacks**, where even a trustable central server’s shared parameters  
 69 can be exploited to unearth private data (Zhu et al., 2019; Deng et al., 2021; Balunovic et al., 2022;  
 70 Gupta et al., 2022). Unlike them, Wang et al. (2023) focus on theoretical models with limitations  
 71 in real-world applicability. To overcome these limitations, this study introduces an attack approach

72 that aims to be difficult to detect and counter while improving the success rate of such attacks across  
 73 diverse datasets and settings. **More details about related work can be found in the appendix.**

### 74 3 Preliminaries

#### 75 3.1 Gradient Inversion and Prior Knowledge

76 Gradient inversion poses a privacy threat in federated learning by potentially allowing for the recon-  
 77 struction of input training data from once-queried gradients and known models. Despite federated  
 78 learning’s decentralized approach to ensuring local data privacy, gradient inversion demonstrates  
 79 vulnerabilities in this system. When recovering textual information, researchers often complement  
 80 gradient inversion with prior knowledge from pre-trained language models like GPT-2, using their  
 81 predictive capabilities to enhance text quality assessment. More details are provided in appendix.

#### 82 3.2 Two-layer-neural-network-based Reconstruction

83 Wang et al. (2023) identified a gap in existing literature regarding the capability of gradient information  
 84 to unveil training data. Their study demonstrates that it might be possible to reconstruct training data  
 85 solely from gradient data using a theoretical approach within a two-layer neural network.

86 Consider a two-layer neural network:  $f(x; \Theta) = \sum_{j=1}^m a_j \sigma(w_j \cdot x)$ , with parameters defined as  
 87  $\Theta = (a_1, \dots, a_m, w_1, \dots, w_m)$ . Here,  $m$  represents the hidden dimension. The objective function is  
 88 represented as:  $L(\Theta) = \sum_{i=1}^B (y_i - f(x_i; \Theta))^2$ . A notable finding is that the gradient for  $a_j$  is solely  
 89 influenced by  $w_j$ , making it independent from other parameters. This gradient is represented as:

$$g_j := \nabla_{a_j} L(\Theta) = \sum_{i=1}^B r_i \sigma(w_j^\top x_i) \quad (1)$$

90 where the residual  $r_i$  is given by  $r_i = f(x_i; \Theta) - y_i$ . For wide neural networks with random  
 91 initialization from a standard normal distribution, the residuals  $r_i$  concentrate to a constant,  $r_i^*$ . By set  
 92  $g(w) := \sum_{i=1}^B r_i^* \sigma(w^\top x_i)$ ,  $g_j$  can be expressed as  $g_j = g(w_j) + \epsilon$ , where  $\epsilon$  represents noise. Then  
 93 the third derivative of  $g_w$  is represented as:

$$\nabla^3 g(w) = \sum_{i=1}^B r_i^* \sigma^{(3)}(w^\top x_i) x_i^{\otimes 3} \quad (2)$$

94 The researchers postulated that if they can accurately estimate  $\nabla^3 g(w)$ , it is possible to determine  
 95  $\{x_i\}_{i=1}^B$  by using tensor decomposition techniques, especially when these features are independent.  
 96 They used Stein’s Lemma, expressed as:  $\mathbb{E}[g(X)H_p(X)] = \mathbb{E}[g^{(p)}(X)]$  to approximate  $\nabla^3 g(w)$  as:

$$T = \mathbb{E}_W[\nabla_W^3 g(W)] = \mathbb{E}_{W \sim N(0, I)}[g(W)H_3(W)] \approx \frac{1}{m} \sum_{j=1}^m g(w_j)H_3(w_j) = \hat{T} \quad (3)$$

97 Where  $H_3(w_j)$  is the p-th order tensor product of  $w_j$ . By leveraging this approach, they successfully  
 98 reconstructed each unique  $x_i$ . Their approach is predominantly theoretical and is mostly restricted to  
 99 two-layer fully connected networks. Specifically, when applied to deeper networks, their method uses  
 100 identity modules and other transparently detectable weight manipulations, which limits its practical  
 101 use. In this work, instead of attempting to recover the input of a deep neural network directly, we  
 102 aim to retrieve the intermediate features that serve as the subsequent optimization-based supervisory  
 103 signals. Because we concentrate solely on a specific segment of the deep neural network, it becomes  
 104 simpler to meet certain constraints. Further details will be provided in Section 4.1.

### 105 4 Methodology

106 Gradient inversion aims to reconstruct original training data using the gradients of deep-learning  
 107 models, but it faces challenges due to nonconvexity and the problem’s over-determined nature, making

108 it an NP-complete issue (Wang et al., 2023). Additionally, in recovering text input, averaging gradients  
109 for entire batches obscures individual token patterns, complicating precise token reconstruction. This  
110 raises the question: **can a method offer an accurate feature-level supervisory signal to improve**  
111 **data reconstruction?**

#### 112 4.1 Reconstruct Input of Pooler Layer

113 The earlier research highlighted the potential to retrieve training data using only gradient data from  
114 a broad two-layer neural network (Wang et al., 2023). Notwithstanding its constraints, detailed in  
115 Section 3.2, and its inability to recover actual features (only their direction in the feature space), we  
116 shifted our focus. Instead of directly recovering deep neural network inputs, we now aim to recover  
117 their intermediate features. Intrigued by the prevalent Transformer architecture in language models  
118 like BERT, which commonly have a Pooler and Classifier, our goal is to reconstruct features for  
119 the Pooler layer. We hypothesize that these recovered intermediate features can present a unique  
120 supervisory signal, distinct from gradients and prior knowledge. This new pursuit entails adapting  
121 and honing techniques to cater to the specific needs of deep language models.

122 **Subtle Modification of Architecture:** The initial configuration of language models often sets the  
123 hidden dimension of the Pooler layer to match the input dimension (For BERT<sub>BASE</sub>, it’s 768). This  
124 setting is insufficient to promise the accuracy of tensor decomposition when applying the two-layer-  
125 neural-network-based reconstruction method. To address this limitation, we expand the dimension  
126 of the Pooler layer to match the vocabulary size of the language models (For BERT<sub>BASE</sub>, this was  
127 adjusted from 768 to 30,522). The rationale behind this change is grounded in enhancing the model’s  
128 expressiveness while ensuring our modifications are not easily detectable.

129 Moreover, our empirical observations indicated that the original activation function struggles to work  
130 harmoniously with the recovery method, leading to inaccurate information retrieval. This challenge  
131 arises due to its  $i_{th}$  derivatives resulting in zero expectations, expressed as  $\mathbb{E}_{Z \sim N(0,1)}[\sigma^{(i_{th})}(Z)] = 0$ ,  
132 and leads to an inaccurate estimation of  $\hat{T}$  as described in Equation 3. To counter these challenges,  
133 we replace the Tanh function after the Pooler layer with two alternative functions: SELU or  $\sigma(x) =$   
134  $x^3 + x^2$ . Neither of these functions is strictly odd or even, which counter issues from derivatives. It’s  
135 worth noting that SELU, a commonly used activation function in deep learning, is less likely to draw  
136 attention. On the other hand, our empirical tests of the cube+square function indicate that while it  
137 compromises concealability, it offers enhanced attack performance in specific scenarios.

138 **Strategic Weight Initialization:** We introduce key notations first:  $X$  is the input to the Pooler layer  
139 with a shape of  $(B, d)$ , where  $B$  is the batch size and  $d$  is the feature dimension. The weights  $W_1$  and  
140  $W_2$  correspond to the Pooler and Classifier layers, respectively, with shapes  $(|V|, d)$  and  $(N, |V|)$ .  
141 Here,  $|V|$  is the vocabulary size and  $N$  is the number of classification classes.

142 As mentioned in Section 3.2,  $m$  signifies the hidden dimension in a two-layer neural network. Ideally,  
143  $|V|$  should be equivalent to  $m$  in our setting. However, during our computation of  $\hat{T}$  as outlined  
144 in Equation 3, we noticed an anomaly in  $g_j$ . Due to the random initialization of  $W_1$ , a substantial  
145 portion of  $g_j$  approached a value close to 0. This side effect impacts the subsequent decomposition  
146 procedure. To address this issue, rather than setting  $|V| = m$ , we determined  $m = |V| - d$ . This  
147 approach ensures the remaining dimensions are randomly initialized and adequate to promise the  
148 accuracy of tensor decomposition. Simultaneously, the original weights are retained in the new  
149 weight matrix, allowing us to obtain optimal gradients for  $W_1$  and  $W_2$ . For the classifier layer, we  
150 utilize a strategy similar to that of the Pooler layer, adjusting the remaining dimensions to a constant  
151  $(i/m)$ , where  $i$  represents the class index for the classification task).

152 **Flexibility of the Recovered Dimension:** Wang et al. (2023) suggests significantly expanding the  
153 hidden dimension  $m$  in comparison to the input dimension  $d$  to reduce the tensor decomposition  
154 error. In our setting, we let  $m = |V| - d$ . Given that  $|V|$  represents the vocabulary size, it sounds  
155 straightforward to utilize this value as the dimension of the Pooler layer. Any other configuration  
156 for  $m$  appears less intuitive. Thus, it’s reasonable for our choice, and there is no reason to adjust the  
157 hidden dimension any further. On the other hand, for a fixed  $d$  (768 for BERT<sub>BASE</sub>), determining  
158 the optimal value for  $m$  can be challenging without adjustments. Recognizing these constraints, we  
159 kept  $m$  constant and explored alternative methods to tweak  $d$ . Specifically, instead of attempting to  
160 recover the full dimension  $d$ , our strategy focuses on recovering a dimension  $d'$  where  $d' \leq d$ . This  
161 approach sets the subweights  $(d: , d': )$  of  $W_1$  to zero. Then the gradient  $g_j$  in Equation 3 remains

162 functional but is exclusively tied to the subweights ( $\cdot, \cdot, d'$ ) of  $W_1$ . As a result, we embrace a more  
163 directed and efficient methodology by centering our reconstruction on the feature subset  $(B, d')$ .

164 **Challenges in Order Recovery of Features :** When applying tensor decomposition techniques  
165 to retrieve features from  $\hat{T}$ , a significant issue arises when the batch size exceeds one: the exact  
166 order of the recovered features remains uncertain. Under adversarial conditions, one might try  
167 every conceivable permutation as a reference. However, we simplify the procedure by sequentially  
168 comparing each recovered feature to the actual input features with cosine similarity until the best order  
169 is discerned. In certain cases, a single recovered feature displayed a notably high cosine similarity  
170 with multiple actual inputs simultaneously. Interestingly, although a 1-m greedy relationship might  
171 exhibit a high correlation, it did not exceed the attack performance of a straightforward 1-1 match in  
172 the final outcome. Consequently, we adopted the 1-1 relationship to achieve the best attack result.

## 173 4.2 Feature Match

174 Following Balunovic et al. (2022), we have segmented our entire text retrieval process into three  
175 phases: Initialization, Optimization, and Token Swap. In the initialization and token swap stages, we  
176 aim to leverage certain metrics to identify optimal starting or intermediary points for the subsequent  
177 optimization phase. This method is also commonly recognized as discrete optimization. In this setting,  
178 we've chosen a mix of metrics to guide the choice, including gradient match loss and perplexity  
179 obtained from pre-trained language models. More details can be found in Balunovic et al. (2022).  
180 In the optimization stage, we propose to optimize the embeddings derived from input IDs and the  
181 features directed into the Pooler layer simultaneously. We use gradient match loss and cosine distance  
182 between the input of the Pooler layer with the recovered intermediate features from Section 4.1 to  
183 guide the optimization. Moreover, we oscillate between continuous and discrete optimization phases  
184 to bolster the final attack performance.

## 185 5 Experiments

### 186 5.1 Set Up

187 In our study, we focus on three primary binary text classification datasets for a thorough evaluation,  
188 namely **CoLA** and **SST-2** from the **GLUE** benchmark, and the **RottenTomatoes** dataset, each varying  
189 in sequence lengths Balunovic et al. (2022); Warstadt et al. (2018); Socher et al. (2013); Wang et al.  
190 (2019); Pang & Lee (2005). From these datasets, we randomly draw a subset of 100 sequences from  
191 the training sets for evaluation, a method supported by Balunovic et al. (2022). The main architecture  
192 we experiment on is **BERT<sub>BASE</sub>** (Devlin et al., 2018), using models that have undergone fine-tuning  
193 for two epochs, even adopting those models fine-tuned by Balunovic et al. (2022). GPT-2 is our  
194 chosen auxiliary language model to garner prior knowledge (Radford et al., 2019). We adopt the  
195 ROUGE metric suite, particularly **ROUGE-1**, **ROUGE-2**, and **ROUGE-L** for evaluating attack  
196 performance, where padding tokens are disregarded (Deng et al., 2021; Lin, 2004). Our methodology  
197 is benchmarked against three primary baselines: **DLG**, **TAG**, and **LAMP**, with the latter considered  
198 the pinnacle. We utilize the open-source LAMP's framework for implementation, ensuring parity  
199 in experimental conditions when juxtaposing our approach with these baselines. All experimental  
200 aspects, including the choice of hyperparameters and evaluation, are designed for a fair and consistent  
201 comparison, with results averaged across five random seeds. More details can be found in appendix.

### 202 5.2 Results and Analysis

203 We present experimental results in Table 1. These findings clearly demonstrate that our approach  
204 outperforms all baselines (DLG, TAG, and LAMP) across various datasets and batch sizes. There's  
205 an average improvement of up to **9.3%** for ROUGE-1, **6%** for ROUGE-2, and **7%** for ROUGE-L.

206 Examining the impact of batch size variations, we notice that launching an attack becomes more  
207 challenging as the batch size increases. All attack methods, including ours, exhibit a decline in attack  
208 performance. However, our method brings a more noticeable improvement at batch sizes 2 and 4,  
209 surpassing its efficacy at batch sizes 1 and 8. We posit that for a batch size of 1, where the gradient is  
210 only averaged solely over tokens, the benefit of incorporating the feature information is less evident

211 because the gradient information still plays a leading role in the optimization process. For a batch size  
 212 of 8, the improvement scale is also not pronounced, we explore the background reason in Section ??.

Table 1: Text privacy attack on BERT<sub>BASE</sub> with Different Batch Sizes and Datasets. R-1, R-2, and R-L, denote ROUGE-1, ROUGE-2, and ROUGE-L scores respectively.

Method	B=1			B=2			B=4			B=8		
	R-1	R-2	R-L	R-1	R-2	R-L	R-1	R-2	R-L	R-1	R-2	R-L
<b>CoLA</b>												
DLG	59.3	7.7	46.2	36.9	2.6	31.4	35.3	1.4	31.9	16.5	0.8	7.9
TAG	78.9	10.2	53.3	45.6	4.6	36.9	35.3	1.6	31.3	33.3	1.6	30.4
LAMP <sub>COS</sub>	84.8	46.2	73.1	57.2	21.9	49.8	40.4	6.4	36.2	36.4	5.1	34.4
<b>Ours<sub>SELU</sub></b>	<b>86.6</b>	<b>51.5</b>	<b>76.7</b>	<b>69.5</b>	<b>31.2</b>	<b>60.6</b>	<b>50.5</b>	<b>11.8</b>	<b>43.9</b>	<b>40.8</b>	<b>8.3</b>	<b>38.1</b>
<b>Ours<sub>x<sup>3</sup>+x<sup>2</sup></sub></b>	84.6	45.2	72.4	57.3	19.2	49.8	43.9	11.4	40.1	37.8	5.9	34.8
<b>SST-2</b>												
DLG	57.7	11.7	48.2	39.1	7.6	37.2	38.7	6.5	36.4	36.6	4.7	35.5
TAG	71.8	16.1	54.4	46.1	10.9	41.6	44.5	9.1	40.1	41.4	6.7	38.9
LAMP <sub>COS</sub>	87.7	54.1	76.4	59.6	26.5	53.8	48.9	17.1	45.4	39.7	10.0	38.2
<b>Ours<sub>SELU</sub></b>	90.3	59.0	78.2	71.0	35.3	63.4	58.6	<b>26.3</b>	54.2	45.4	11.5	43.2
<b>Ours<sub>x<sup>3</sup>+x<sup>2</sup></sub></b>	<b>93.1</b>	<b>61.6</b>	<b>81.5</b>	<b>78.3</b>	<b>40.9</b>	<b>67.9</b>	<b>60.6</b>	23.1	<b>54.9</b>	<b>49.5</b>	<b>16.5</b>	<b>47.3</b>
<b>Rotten Tomatoes</b>												
DLG	20.1	0.4	15.2	18.9	0.6	15.4	18.7	0.4	15.7	20.0	0.3	16.9
TAG	31.7	2.5	20.1	26.9	1.0	19.1	27.9	0.9	20.2	22.6	0.8	18.5
LAMP <sub>COS</sub>	63.4	13.8	42.6	38.4	6.4	28.8	24.6	2.3	20.0	20.7	0.7	17.7
<b>Ours<sub>SELU</sub></b>	71.9	19.2	48.7	<b>48.1</b>	<b>8.2</b>	<b>34.2</b>	<b>33.0</b>	<b>4.23</b>	<b>25.3</b>	<b>24.6</b>	<b>2.0</b>	<b>20.6</b>
<b>Ours<sub>x<sup>3</sup>+x<sup>2</sup></sub></b>	<b>72.2</b>	<b>21.0</b>	<b>49.3</b>	44.6	7.0	31.8	29.9	3.5	24.3	23.6	1.7	19.8

213 Turning our attention to variations in sequence length across datasets, we notice a clear trend: as  
 214 sequences get longer, the benefit from intermediate features at a batch size of 1 becomes more  
 215 pronounced. Specifically, for the CoLA dataset with token counts between 5-9, we see an average  
 216 improvement in ROUGE metrics of **3%**. This improvement grows to **5%** for the SST-2 dataset  
 217 with token counts from 2 to 13. For the Rotten Tomatoes dataset, which features even longer  
 218 sequences with token counts ranging from 14 to 27, the average ROUGE metric improvement further  
 219 increases to **8%**. This suggests a correlation between sequence length and the extent of improvement  
 220 observed. However, when the batch size exceeds one, the benefits observed for these three datasets  
 221 are consistently notable. Recall that gradient averaging occurs only over tokens at a batch size of  
 222 1, it implies that with longer sentences, the gradient information becomes less effective, leading  
 223 to greater benefits from intermediate feature supervision signals. When batch sizes are larger than  
 224 1, averaging happens over tokens and sentences simultaneously. This broadened scope results in  
 225 our method consistently yielding pronounced benefits across sequences with different lengths. Our  
 226 findings further reinforce the idea that relying exclusively on gradient information diminishes efficacy  
 227 with larger batch sizes and longer sequences.

228 Additionally, with the inclusion of feature information as a supervision signal, our method can recover  
 229 not only a greater number of tokens but also more accurate token orderings. In comparison to other  
 230 baselines, we can recover longer text sequences. The improvement in ROUGE-2 and ROUGE-L  
 231 metrics supports these observations.

## 232 6 Conclusion

233 This paper presents a novel method for text privacy attacks that is difficult to detect and defend.  
 234 Instead of solely relying on traditional gradients and prior knowledge, our approach incorporates  
 235 unique feature-level information. Comprehensive empirical studies across various model architectures,  
 236 datasets, and batch sizes affirm the effectiveness of our method.

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## 313 A Appendix

### 314 A.1 Federated Learning

315 Introduced by McMahan et al. (2017), federated learning solves data privacy concerns by promoting  
316 decentralized model training. In this approach, models are refined using local updates from individual  
317 clients, which are then merged at a central server (Konečný et al., 2015, 2016, 2017). This field has  
318 attracted significant attention due to its potential business applications, underlining its relevance and  
319 promise in academia and industry (Ramaswamy et al., 2019; Li et al., 2020).

### 320 A.2 Data Privacy Attack

321 While federated learning features with data privacy, recent studies show that model updates (gradients  
322 and parameters) can be intentionally leveraged to uncover sensitive data (Phong et al., 2017; Zhao  
323 et al., 2020; Zhu & Blaschko, 2020; Zhu et al., 2019). This susceptibility is especially pronounced in  
324 the field of CV. In fact, some researchers have been able to recreate images almost perfectly by using  
325 gradients along with prior knowledge (Huang et al., 2021; Geiping et al., 2020; Yin et al., 2021; Jeon  
326 et al., 2021).

327 Textual data poses unique challenges in the context of private data attacks, especially given the  
328 prevalence of Transformer architectures. In Transformer, gradients average across sequences and  
329 tokens, which inherently masks specific token details. Furthermore, the inputs, expressed as discrete  
330 token IDs, starkly contrast the continuous features found in image data. Nonetheless, numerous  
331 studies have highlighted the risks associated with textual information. Current research on this topic  
332 can be broadly categorized into two groups.

333 **Malicious Attacks:** In this category, the central server has malicious intent. It may distribute  
334 networks with embedded backdoors or parameters that facilitate easy reconstruction of training  
335 data (Fowl et al., 2021, 2022; Boenisch et al., 2023). However, one can employ prefixed, recognized  
336 architectures to counter the former attack and guard against potential backdoor threats. For the latter  
337 attack, consistently monitoring statistics of features across different layers can help detect malicious  
338 parameter (Balunovic et al., 2022).

339 **Eavesdropping Attacks:** This approach assumes a trustworthy central server. Even with its integrity,  
340 the shared parameters and gradients could still be leveraged to extract private data (Zhu et al., 2019).  
341 For example, methods introduced by Zhu et al. (2019) and Deng et al. (2021) employ optimization-  
342 based strategies using finely-tuned objective functions for data retrieval. Balunovic et al. (2022)  
343 leverages prior knowledge from extensive language models for data recovery. However, these  
344 methods tend to be less effective with larger batch sizes. Notably, the method introduced by (Gupta  
345 et al., 2022) remains effective even with considerable batch sizes. Nevertheless, this vulnerability can  
346 be easily defended by suspending updates to the language model’s embedding matrix.

347 Recently, Wang et al. (2023) proposed a method that can reconstruct the inputs of a two-layer neural  
348 network using only the model structure and gradients. However, their approach is heavily theoretical,  
349 relying on various assumptions about the model. Moreover, when extended to deeper networks, their  
350 method imposes additional constraints by requiring more identity modules, significantly hindering its  
351 practical applicability. To address the shortcomings of prior research, our paper introduces a practical  
352 attack method that is not only challenging to detect and counteract but also aims to improve the  
353 success rate of attacks across diverse batch sizes and datasets.

### 354 A.3 Re-Think Gradient Inversion

355 Gradient inversion seeks to reconstruct the original training data by harnessing the gradients of a  
356 known deep-learning model. A closer look at this method reveals several challenges. Central to these  
357 is the nonconvexity of the issue, marked by the presence of numerous local minima that complicate  
358 the pursuit of the global optimum. Additionally, the problem is over-determined because it has  
359 more equations to resolve than unknown parameters. While these equations remain consistent, they  
360 complicate the optimization process. This complexity persists even when reduced to a single-sample  
361 scenario. As a result, gradient inversion remains an NP-complete problem, implying that procuring  
362 an exact solution within a feasible time frame is difficult (Wang et al., 2023).

363 When we take a broader perspective, a distinct challenge arises in recovering text input. Language  
 364 models typically handle batches of sentences, each containing multiple tokens. In the gradient  
 365 inversion technique, the gradients of the entire batch are averaged. However, this doesn’t only average  
 366 the gradients for whole sentences but also for individual tokens within them. This process obscures  
 367 the unique gradient patterns of each token, making their retrieval more complex. While the averaged  
 368 gradient provides a general picture of the data, it conceals the finer details vital for precise token  
 369 reconstruction. Given this intricacy, a pivotal question emerges: **can we design a clever method by  
 370 providing an accurate feature-level supervisory signal to enhance data reconstruction?**

#### 371 A.4 Extend to Cross Entropy Loss

372 Wang et al. (2023) grounded their research on the assumption that the loss function of the neural  
 373 network is Mean Square Error (MSE). Building upon this foundation, we extend the method to the  
 374 scenario of classification tasks utilizing Cross-Entropy Loss (CEL). In the classification context, the  
 375 gradient of  $g_j$  is calculated for all class outputs. While a straightforward approach might only random  
 376 choose the gradient for a single class to satisfy the equation 3, we chose a more holistic method,  
 377 leveraging the gradient of the pooler layer to compute  $\hat{T}$  rather than the classifier layer. Based on this  
 378 methodology, the gradient of  $w_j$  we derived is as follows:

$$\hat{g}_j = \nabla_{w_j} L(\Theta) = \sum_{i=1}^B r_i a_j \sigma'(w_j^\top x_i) x_i \quad (4)$$

379 Let  $a_j = \frac{1}{m}, \forall j \in [m]$  and  $w_j \in N(0, 1)$ , by Stein’s lemma, we have:

$$T_1 = \sum_{i=1}^m \hat{g}_j H_2(w_j) \quad (5)$$

$$= \frac{1}{m} \sum_{i=1}^B r_i^* x_i \otimes \left[ \sum_{j=1}^m \sigma'(w_j^\top x_i) (w_j \otimes w_j - I) \right] \quad (6)$$

$$\approx \sum_{i=1}^B r_i^* x_i \otimes \mathbb{E} [\sigma'(w_j^\top x_i) (w_j \otimes w_j - I)] \quad (7)$$

$$= \sum_{i=1}^B r_i^* \mathbb{E} [\sigma^{(3)}(w^\top x_i)] x_i^{\otimes 3} \quad (8)$$

$$= T \quad (9)$$

380 By defining the tensors  $T_2$  and  $T_3$  such that:  $T_2(i, j, k) = T_1(k, i, j)$  and  $T_3(i, j, k) =$   
 381  $T_1(j, k, i)$ , we can deduce:  $\hat{T} = \frac{T+T_2+T_3}{3} \approx T$ . This computation results in  $\hat{T}$  being symmet-  
 382 ric. Wang et al. (2023) even observed that this method offers a more precise estimation when  
 383 attempting to recover features. We also adopt this strategy in all our experiments.

#### 384 A.5 Set Up

385 **Datasets:** Following previous work Balunovic et al. (2022), our experimental design incorporates  
 386 three binary text classification datasets to ensure a comprehensive evaluation. Specifically, we utilize  
 387 **CoLA** and **SST-2** from the **GLUE** benchmark (Warstadt et al., 2018; Socher et al., 2013; Wang  
 388 et al., 2019), with their sequences predominantly ranging between 5-9 and 3-13 words, respectively.  
 389 Additionally, the **RottenTomatoes** dataset presents a more complex scenario with sequence lengths  
 390 oscillating between 14 and 27 words (Pang & Lee, 2005). You may find more details about datasets  
 391 in the appendix. Within the scope of our experiments, we utilize a subset of 100 randomly selected  
 392 sequences from the training sets of these datasets as our evaluation benchmark, a method also  
 393 endorsed by Balunovic et al. (2022).

394 **Models:** We conduct experiments primarily on the **BERT<sub>BASE</sub>** (Devlin et al., 2018) architecture.  
 395 Consistent with Balunovic et al. (2022), we use models that have undergone fine-tuning for down-  
 396 stream tasks over two epochs. To ensure a fair comparison, we even adopt the same fine-tuned

397 models from Balunovic et al. (2022). As for the auxiliary language model employed to extract prior  
398 knowledge, we choose GPT-2 (Radford et al., 2019), a choice also used by Balunovic et al. (2022).

399 **Metrics:** Following Deng et al. (2021) and Balunovic et al. (2022), we evaluate attack performance  
400 using the ROUGE metric suite (Lin, 2004). Specifically, we present the collective F-scores for  
401 **ROUGE-1**, **ROUGE-2**, and **ROUGE-L**. These metrics respectively assess the retrieval of unigrams,  
402 bigrams, and the proportion of the longest continuous matching subsequence relative to the entire  
403 sequence’s length. We omit all padding tokens in the reconstruction and evaluation phases.

404 **Baselines:** We benchmark our approach against three key baselines: **DLG**, **TAG**, and **LAMP**. Among  
405 them, LAMP represents the state-of-the-art. We employ the open-sourced implementation from  
406 LAMP, which encompasses the implementations for all three baselines (Deng et al., 2021; Zhu  
407 et al., 2019; Balunovic et al., 2022). Following previous work, we assume the lengths of sequences  
408 are known for both baselines and our attacks, as an adversary can run the attack for all possible  
409 lengths (Balunovic et al., 2022).

410 **Implementation:** Our method is implemented based on LAMP’s framework, utilizing the exact same  
411 datasets, evaluation metrics, and similar models. To ensure a fair comparison, we standardized the  
412 experimental conditions and settings when comparing our approach with baselines, particularly the  
413 state-of-the-art LAMP. We adopt all of LAMP’s hyperparameters, including the optimizer, learning  
414 rate, learning rate schedule, regularization coefficient, optimization steps, and random initialization  
415 numbers. For hyperparameters unique to our method, we made selections using a grid search on  
416 BERT<sub>BASE</sub> and shared them in different settings (LAMP also adopts this strategy). It’s also important  
417 to note that all our experiment results are averaged over five different random seeds.

## 418 A.6 Datasets Details

419 **CoLA:** The CoLA (Corpus of Linguistic Acceptability) dataset is a seminal resource for evaluating  
420 the grammatical acceptability of machine learning models in natural language processing. Consisting  
421 of approximately 10,657 English sentences, these annotations are derived from various linguistic  
422 literature sources and original contributions. The sentences are categorized based on their grammatical  
423 acceptability. Spanning a comprehensive range of linguistic phenomena, CoLA provides a robust  
424 benchmark for tasks requiring sentence-level acceptability judgments. Its diverse set of grammatical  
425 structures challenges models to demonstrate both depth and breadth in linguistic understanding,  
426 making it a popular choice in the field.

427 **SST-2:** The SST-2 (Stanford Sentiment Treebank Version 2) dataset is a widely recognized benchmark  
428 for sentiment analysis tasks in natural language processing. Originating from the Stanford NLP  
429 Group, this dataset contains around 67,000 English sentences, drawn from movie reviews, annotated  
430 for their sentiment polarity. Unlike its predecessor which had fine-grained sentiment labels, SST-2  
431 has been simplified to a binary classification task, where sentences are labeled as either positive or  
432 negative. This dataset not only provides sentence-level annotations but also contains a unique feature:  
433 a parsed syntactic tree for each sentence. By leveraging both sentiment annotations and syntactic  
434 information, we can investigate various dimensions of sentiment understanding and representation in  
435 machine learning models.

436 **Rotten Tomatoes:** The Rotten Tomatoes dataset is a compilation of movie reviews sourced from  
437 the Rotten Tomatoes website. This dataset has been instrumental in sentiment analysis research.  
438 In its various versions, the most notable being SST-2, the dataset consists of sentences from these  
439 reviews, annotated for their sentiment polarity. These sentences are labeled either as positive or  
440 negative, making it a binary classification challenge. The dataset’s value lies in its representation of  
441 real-world opinions, rich in diverse sentiment expressions, and has been a cornerstone for evaluating  
442 the performance of natural language processing models in sentiment classification tasks.

## 443 A.7 More Discussion

444 **Impact of Recovery Dimension:** In Section 4.1, we propose fixing  $m$  and adjusting  $d'$  to identify  
445 the optimal mapping for  $d'$  (where  $d' < d$ ) and  $m$ . Accordingly, we conduct experiments using  
446 BERT<sub>BASE</sub> with various batch sizes to investigate the quality of the recovered intermediate features  
447 by calculating their cosine similarity with the ground truth. The results are illustrated in Figure 2.  
448 Our findings suggest that when the batch size is 1, the recovered quality gradually degrades as the

449 recovery dimension  $d'$  increases, yet it remains as high as 0.99 across all configurations. However,  
 450 this pattern does not hold when the batch size exceeds 1. We also observed that the recovered quality  
 451 consistently declines as the batch size increases. We hypothesize that multiple inputs might exhibit  
 452 some undisclosed dependencies, particularly features within the deeper layers of language models,  
 453 thereby affecting the efficacy of tensor decomposition. For simplicity, we set  $d' = 100$  across all  
 454 experiments. However, under adversarial conditions, attackers might experiment with various  $d'$   
 455 settings to enhance their attack performance.

Table 2: Influence of cosine distance in different text retrieval phases on BERT<sub>BASE</sub> and SST-2 dataset

Phase	R-1	R-2	R-L
<b>Batch Size=1</b>			
Non-use (LAMP)	87.7	54.1	76.4
Only Discrete	92.5	59.3	79.9
Only Continuous	<b>93.1</b>	<b>61.6</b>	<b>81.5</b>
Both	90.0	53.9	76.8
<b>Batch Size=4</b>			
Non-use (LAMP)	48.9	17.1	45.4
Only Discrete	57.9	23.4	52.3
Only Continuous	60.6	23.1	54.9
Both	<b>61.7</b>	23.0	<b>55.7</b>

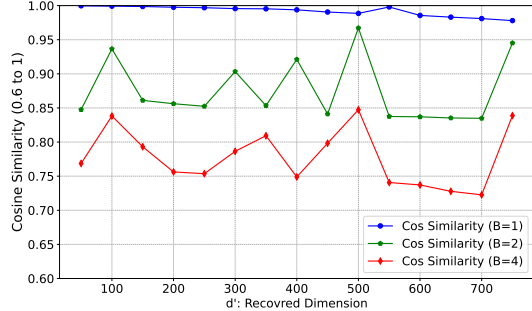


Figure 2: Cosine similarity between recovered features and ground Truth on BERT<sub>BASE</sub> across varying dimensions (50-750 in 50-step intervals) and batch sizes (1, 2, 4)

458 **Impact of Feature Match in Different Optimization Phase:** In Section 4.2, we propose a novel  
 459 optimization objective: the cosine distance between the input of the Pooler layer and the recovered  
 460 intermediate features from Section 4.1. It’s worth noting that we can also apply this distance as  
 461 a new metric like gradient match loss in the discrete optimization stage to select the best starting  
 462 or intermediary points for the subsequent training phase. Therefore, we add the new metric to the  
 463 discrete and continuous optimization phases separately to observe its impact on the final attack  
 464 performance. The results are illustrated in Table 2. Notably, our introduced metric has a positive  
 465 effect on both phases. However, when the new metric is used in discrete and continuous optimization  
 466 together, the results are not always two-win.

Table 3: Text privacy attack on RoBERTa<sub>BASE</sub>. R-1, R-2, and R-L are same within Table 1. Cos<sub>S</sub> indicates the average cosine similarity between references and recovered samples.

Dataset	Method	R-1	R-2	R-L	Cos <sub>S</sub>	Recovered Samples
CoLA	reference sample: <a href="#">The box contains the ball</a>					
	LAMP	15.5	2.6	14.4	0.36	likeTHEtw box contains divPORa
	<b>Ours</b>	<b>17.4</b>	<b>3.8</b>	<b>15.9</b>	<b>0.41</b>	<a href="#">like Mess box contains contains balls</a>
SST2	reference sample: <a href="#">slightly disappointed</a>					
	LAMP	<b>20.1</b>	<b>2.2</b>	15.9	0.56	likeslightly disappointed a
	<b>Ours</b>	19.7	2.1	<b>16.8</b>	<b>0.59</b>	<a href="#">like lightly disappointed a</a>
Toma	reference sample: <a href="#">vaguely interesting, but it’s just too too much</a>					
	LAMP	19.9	1.6	15.1	0.48	vagueLY?, interestingtooMuchbuttoojusta
	<b>Ours</b>	<b>21.5</b>	<b>1.8</b>	<b>16.0</b>	<b>0.51</b>	vagueLY, interestingBut seemsMuch Toolaugh

467 **Impact on Other Models:** To demonstrate the effectiveness of our attack method on various model  
 468 architectures, we also apply our method on the RoBERTa (Liu et al., 2019). While RoBERTa shares  
 469 similarities with BERT, it distinguishes itself through unique training configurations and datasets.  
 470 Notably, unlike BERT<sub>BASE</sub>, RoBERTa does not have a Pooler layer. Instead, it employs a classifier  
 471 composed of two linear layers in the head. In our experiments, we treat the first layer as an analogous  
 472 Pooler layer and endeavor to reconstruct its input. All the models used in this experiment are from  
 473 Hugging Face, contributed by TextAttack. As for the auxiliary model, we employ RoBERTa itself  
 474 due to a specific challenge: we can’t locate another generative model using the same tokenizer with  
 475 RoBERTa. However, it’s essential to note that we use the exact same settings for baselines and

our method. We present the experiment results in Table 3. While the overall attack performance significantly decreases due to the auxiliary masked language model, our approach still outperforms the baseline. Furthermore, in numerous instances (as illustrated in Table 3), our method appears to restore the essence of the reference sample almost flawlessly. However, due to the limitation of traditional evaluation metrics, they may have equal or even worse evaluation numbers than some obvious bad recovery. Therefore, we propose to use the cosine similarity between the embeddings of reference and recovery generated by SBERT (Reimers & Gurevych, 2019).

### 483 A.8 Impact of Activation Function

484 When applying the two-layer-neural-network-based reconstruction method to the Pooler layer of  
 485 language models, we also substitute the original Tanh activation function with the ReLU. However, the  
 486 third-order derivative of the ReLU function is odd, leading to zero expectation  $\mathbb{E}_{Z \sim N(0,1)}[\sigma^{(3)}(Z)] =$   
 487 0. This property of the ReLU renders it unstable for third-order tensor decomposition. To address  
 488 this challenge, we follow the approach proposed by Wang et al. (2023), instead of using a third-order  
 489 Hermite function to estimate  $T$ , we use a fourth-order function. The estimation is represented as:

$$\hat{T} := \frac{1}{m} \sum_{j=1}^m g_j(w_j) H_4(w_j)(I, I, I, a) \quad (10)$$

490 where  $a$  is a unit vector, pointing in a specific direction in space. However, the result of the experiment  
 491 is not ideal even compared with baselines, which means we need to find a more practical method to  
 492 resolve this problem.

### 493 A.9 Influence of Data Dependence

494 We made a noteworthy observation during our implementation of the two-layer-neural-network-  
 495 based reconstruction technique. When the batch size goes beyond a single data point, ensuring the  
 496 independence of features across various data points becomes crucial. However, there’s an inherent  
 497 challenge in achieving this. Delving deeper into the language model, particularly close to the Pooler  
 498 layer, we find that dominant features are those closely aligned with the downstream task. Using  
 499 sentiment analysis as an example, features directed to the Pooler layer somewhat have characteristics  
 500 that describe similar emotions. Unfortunately, this similarity can degrade the quality of the features  
 501 we are trying to recover. As a result, the reliability of these recovered features might be diminished  
 502 when they are used as ground truth during optimization.

503 Wang et al. (2023)’s analysis also underscores this puzzle: the reconstruction quality is closely tied  
 504 to the condition number, defined by the data matrix’s smallest singular value. To elaborate further,  
 505 if a sample is heavily influenced by or dependent on other samples (like two sentences mirroring  
 506 each other or belonging to identical classes), the assurance of accurate recovery falters. This decline  
 507 is attributed to the inherent limitation of tensor decomposition when faced with almost identical  
 508 data. For instance, with two strikingly similar sentences, tensor decomposition might only be able to  
 509 discern the collective span of the sentences, failing to distinguish between them. Resorting to feature  
 510 matching in such scenarios would invariably perform negatively.

Reference	Recovery
slightly disappointed	slightly disappointed
splendidly	splendidly
gaining much momentum	gaining much momentum
flawless film	flawless film
tiresomely	tiresomely
enjoyable ease	ease enjoyable
grayish	grayish
no cute factor here ... not that i mind ugly ; the problem is he has no character , loveable or otherwise .	he no problem is here i really love cute, not ugly the mind or no character ; the loveable love factor cute has.

Reference	Recovery
of softheaded metaphysical claptrap	softhead of metaphysical clap claptrap
ably balances real-time rhythms with propulsive incident .	time ably balances incident with real incident.ulsive rhythms.
was being attempted here that stubbornly refused to gel	here was attempted stubbornly that being refused to gel
that will be seen to better advantage on cable , especially considering its barely	, that better to barely advantage will be seen on cable considering its advantage
point at things that explode into flame	point things flame that explode into explode
undeniably intriguing film	undeniably intriguing film
efficient , suitably anonymous chiller .	efficient, suitably anonymous chiller shady
all of this , and more	this and all this more,
want to think too much about what s going on	think want to think too much about what s going on
invigorating	invigorating
to infamy	to infamy
the perverse pleasure	the perverse pleasure
the way this all works out makes the women look more like stereotypical caretakers and moral teachers , instead of serious athletes .	the stereotypical this way all works out ( the more like oxygenmissible caretaker makes teachers of athletes instead look moral. women instead
a successful adaptation and an enjoyable film in its own right	a successful and enjoyable film adaptation right in its own right
while some will object to the idea of a vietnam picture with such a rah-rah , patriotic tone , soldiers ultimately achieves its main strategic objective : dramatizing the human cost of the conflict that came to define a generation .	will achieve object main while idea conflict drama with the such tone a political picture cost : vietnam thetih ra, vietnam insulted achieves objective objective, some patriotic dramazing a tone of soldiers generation that strategic its drama ultimately generation to define.
taken outside the context of the current political climate ( see : terrorists are more evil than ever ! )	the climate terrorists than outside the context of current political climate ( see : are evil ever taken! )
strange and beautiful film	strange and beautiful film
this ) meandering and pointless french coming-of-age import from writer-director anne-sophie birot	this meander pointless director - anne french - coming from pointless importing of writer ) and ageing - -rot
are so generic	are so generic
for only 71 minutes	for 71 minutes only
i also believe that resident evil is not it .	it is also i not.. believe resident evil
fizzability	fizzability
a better vehicle	a better vehicle
pull together easily accessible stories that resonate with profundity	hand together stories resonate with pullclun-dity easily accessible
higher	higher
build in the mind of the viewer and take on extreme urgency .	build urgency in the extreme of viewer urgency and take on mind.
we ve seen it all before in one form or another , but director hoffman , with great help from kevin kline , makes us care about this latest reincarnation of the world s greatest teacher .	these greatest of form seen before all rein-nationdirector we, directorstand wele great hoffman in ve latest makes us help teacher care about greatestnation in this the lancenation, but one of

<b>Reference</b>	<b>Recovery</b>
s horribly wrong	shorribly wrong
eccentric and	eccentric and
scare	scare
finds one of our most conservative and hide-bound movie-making traditions and gives it new texture , new relevance , new reality .	gives our finds new finds, conservative new-bound movie making traditions - and reality texture it hide. reality texture and one movie relevance
pummel us with phony imagery or music	imagery pummel us or phony with music
consistently sensitive	consistently sensitive
the project s filmmakers forgot to include anything even halfway scary as they poorly rejigger fatal attraction into a high school setting .	s scary filmmakers forgot anything forgot to include even halfway fatal attraction as they poorlyjigger regger into high school scary project setting
narcissistic	narcissistic
has been lost in the translation ... another routine hollywood frightfest in which the slack execution italicizes the absurdity of the premise .	slack has the includesity in the executionalnic translation. another frightfest. the absurd premise which lost, it routineizes the premise of hollywood.
– bowel movements than this long-on-the-shelf , point-and-shoot exercise in gimmicky crime drama	movements - - than long - shoot - - this exercise, and this - the bowel shelf - on gimmick in crime drama point
visually striking and slickly staged	visually striking and slickly staged
downright transparent	downright transparent
rotting underbelly	underbelly rotting
could possibly be more contemptuous of the single female population .	could possibly be more contemptuous of the single female population.

<b>Reference</b>	<b>Recovery</b>
what the english call ‘ too clever by half	what ‘ call call by clever english too half
sucks , but has a funny moment or two .	has funny sucks but moment or two funny sucks.
trailer-trash	trash trailer -
flinching	flinching
hot topics	hot topics
settles too easily	settles too easily
films which will cause loads of irreparable damage that years and years of costly analysis could never fix	films which will cause loads ofparable damage that years and years of costly analysis irre could never fix
wears	wears
is an inspirational love story , capturing the innocence and idealism of that first encounter	innocence is an inspirational story capturing the idealism of first encounter, and love that
has the charisma of a young woman who knows how to hold the screen	has the thea of char young who knows how hold of screen womanism
circuit is the awkwardly paced soap opera-ish story .	h - is awkwardly paced circuit story is the soap opera story
, beautiful scene	beautiful scene,
grace to call for prevention rather than to place blame , making it one of the best war movies ever made	to call for prevention rather than to place blame, grace making it one of the best war movies ever made
looking for a return ticket	looking for a return ticket

Reference	Recovery
the strange horror	the strange horror
, joyous romp of a film .	, a joyous romp of film.
a longtime tolkien fan	a longtime tolkien fan
heartwarming , nonjudgmental kind	heartwarming, nonmingjudgmental kind
uncouth , incomprehensible , vicious and absurd	absurdhensible, uncouth, vicious and incompbled
a real winner – smart , funny , subtle , and resonant .	a winner. resonant and funny - ami subtle, smart, real res
gets clunky on the screen	gets on screenunk clunky
there s not a single jump-in-your-seat moment and	there s not a single jump and seat in your seat - - - moment
has a tougher time balancing its violence with kafka-inspired philosophy	acter has a tough time balancing itsfka philosophy with violence - inspired
bad filmmaking	bad filmmaking
share	share
this excursion into the epicenter of percolating mental instability is not easily dismissed or forgotten .	this excursionenter is the mentaleter into instability or iserving easily dismissed or not easily forgotten.
s as if allen , at 66 , has stopped challenging himself .	as if regarding sums, allen has stopped s 66, challenging himself.
is its make-believe promise of life that soars above the material realm	its promise that life is promiseence make soars above the material realm -
exit the theater	exit the theater
is fascinating	fascinating is
wise , wizened	wise, wizened
is not the most impressive player	is not the most impressive player
it s undone by a sloppy script	its undone by a sloppy script
know what it wants to be when it grows up	know what grows up when it wants it to be
people have lost the ability to think	people have lost the ability to think
unfortunately , it s also not very good .	. very, unfortunately it also s not very good
clarity and emotional	and emotional clarity
propulsive	propulsive
p.t. anderson understands the grandness of romance and how love is the great equalizer that can calm us of our daily ills and bring out joys in our lives that we never knew were possible .	l of will understands joy is our romance. daily we ill of how of t a grand anderson. the anderson romanceing calms never at us lives guest bearings daily and ofness of coulds p the grand.
tactic to cover up the fact that the picture is constructed around a core of flimsy – or , worse yet , nonexistent – ideas	tactic to cover up the fact picture the core or the coreim constructed,‘ - none worse yet - - aroundum orstensyim. and central ideas
how ridiculous and money-oriented	how ridiculous and - money oriented
muy loco , but no more ridiculous	muy loco, but no more ridiculous
deceit	deceit
in its understanding , often funny way	understanding in its often funny way,
a caper that s neither original nor terribly funny	s that original a caper neither original nor terribly funny
( denis ) story becomes a hopeless , unsatisfying muddle	denis use ) becomes a hopeless muddle story, unsatisfying (
force himself on people and into situations that would make lesser men run for cover	would himself / people run for cover of situations and make force on lesser men



<b>Reference</b>	<b>Recovery</b>
and unforgettable characters	unforgettable and characters
unfulfilling	unfulfilling
walked out muttering words like “ horrible and “ terrible , but had so much fun dissing the film that they did nt mind the ticket cost	walked out muttering words words like di fun the ‘ ‘ mind the horrible filmbut had so much fun that they did tired, the terrible nssing ticket the film cost