Evolving Alignment via Asymmetric Self-Play

Scalable Preference Fine-Tuning Beyond Static Human Prompts

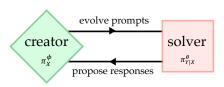
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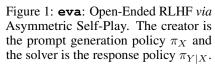
Abstract

Current RLHF approaches for aligning large language models (LLMs) typically assume a fixed prompt distribution, which is sub-optimal and limits the generalization capabilities for language models. To address this issue, we introduce a general framework that casts alignment as an asymmetric game between two players: (i) a creator that generates increasingly informative prompt distributions using the reward model, and (ii) a solver that learns to produce more preferred responses on prompts produced by the creator. This framework of Evolving Alignment via Asymmetric Self-Play (eva), results in a simple and efficient approach that can utilize any existing RLHF algorithm. eva outperforms state-of-the-art methods on widely-used benchmarks, without the need of any additional human crafted prompts. Specifically, eva improves the win rate of GEMMA2-9B-IT on Arena-Hard from 51.6% to 60.1% with DPO, from 55.7% to 58.9% with SPPO, from 52.3% to 60.7% with SimPO, and from 54.8% to 60.3% with ORPO, surpassing its 27B version and matching claude-3-opus. This improvement is persistent even when new human crafted prompts are introduced. Finally, we show eva is effective and robust under various ablation settings.

What I cannot create, I do not understand.

Richard P. Feynman





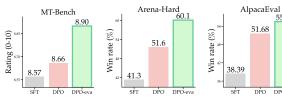


Figure 2: **Results**: Our method **eva** achieves concrete performance gain especially on *hard* alignment benchmarks, without relying on any additional human prompts. Here, we report results for DPO-**eva**; see more in §3.

1 Introduction

Long-lived artificial intelligence must deal with an ever-evolving, open-ended world, yet currently face constraints in both the *scale* and *quality* of available data, and the *growth rate* at which new, useful information is created. High quality human data, crucial for scaling large language model (LLM) based intelligence, is projected to run out in the next few years [Villalobos et al., 2024]; the quality of such data is also expected to stagnate: as LLMs become more capable, they need to solve increasingly complex or new challenges, requiring training data beyond abilities of humans to create. This necessitates a new fundamental mechanism for self-improving, where models can continuously self-generate and self-solve harder problems. We thereby investigate the research question below:

Can language models self-create new, learnable tasks to work on, to self-improve to generalize better for human preferences alignment?

^{*}Work done during an internship at Google.

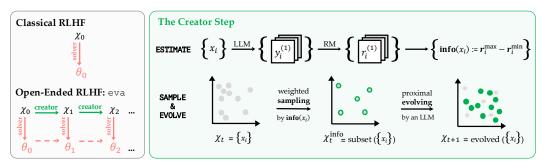


Figure 3: **Pipeline**: **eva** generalizes classical RLHF with open-ended RLHF, optimized *via* a creator-solver game for self-improving language models. See more on the objective and principle in § 2.

Many preference optimization algorithms [Christiano et al., 2017, Zhao et al., 2023] have been proposed to improve the alignment of language models, however, they all default to fixed prompt training distributions. Such fixed training paradigm inevitably leads to: (i) *generalization issues* (models may underperform or hack on insufficiently represented instructions) and (ii) *efficiency issues* (data annotation and model training are costly, however not all prompt provide the same utility, and identifying informative prompts by human efforts is nontrivial) [Team et al., 2023, 2024].

The objective thereby should not only be to optimize over a specific, static distribution of prompts, rather, to design an agent that can autonomously evolve the training distribution for self-improvement, to align well across unseen, novel environments or tasks (instantiated by prompts).

We develop **eva** (Evolving Alignment \underline{via} Asymmetric Self-Play), as in Figure 1, 3. Central to **eva** is a game with the minimax-regret objective, achieved by alternating optimization of creating prompts and solving them. The interplay encourages evolving curricula [Parker-Holder et al., 2022], potentially benefits both generalization and efficiency (see § C). Orthogonal to many recent self-play studies in LLM alignment [Munos et al., 2023, Wu et al., 2024], **eva** is *asymmetric* [Sukhbaatar et al., 2017], with two policies of different goals; and in contrast to many self-training works [Gulcehre et al., 2023] focusing on improving in $\mathcal{Y} \mid \mathcal{X}$, we jointly optimize in $(\mathcal{X}, \mathcal{Y})$ by generative exploration.

Our main contributions are: (i) **a new principle** of open-ended RLHF that generalize classical RLHF; (ii) **a new algorithm** with asymmetric self-play that can be plugged into any alignment pipeline; and (iii) **the new state-of-the-art** especially on *hard* alignment benchmarks across various algorithms.

eva is easy to deploy. We hope it can serve as a scalable method for the AI community to build robust, open-ended, sample-efficient and self-improving intelligence, that aligns with human values.

2 Method

Algorithm overview. On a high level, **eva** extends RLHF to open-ended RLHF *via* a creator that adapts prompt distributions with an easy-to-implement *estimate*, *sample then evolve* procedure, mimicking the *minimax-regret* policy of asymmetric self-play games, as detailed in §B.

```
Algorithm 1 eva: Evolving Alignment via Asymmetric Self-Play
      Input: initial policy \pi_{\theta_0}, initial prompt set \mathcal{X}_0
 1: for iteration t = 1, 2, \dots do
                     /* creator step */
             estimate informativeness:
 2:
                                                                  \mathcal{X}_t \leftarrow \mathcal{X}_t \cup \{\mathtt{info}(\mathbf{x}_i)\}
                                                                   \mathcal{X}_t^{\text{info}} \leftarrow \mathtt{sample}(\mathcal{X}_t)
             sample subset:
                                                                  \mathcal{X}_t' \leftarrow \mathtt{evolve}(\mathcal{X}_t^{\mathtt{info}})
             self-evolve prompts:
                   /* solver step */
                                                                   orall ~m{x}_i \in \mathcal{X}_t', generate \{m{y}_i^{(j)}\} \sim \pi_{m{	heta}_{t-1}}(\cdot \mid m{x}_i)
 3:
             self-generate responses:
                                                                    \mathcal{X}_t' \leftarrow \mathcal{X}_t' \cup \{(\boldsymbol{y}_i^{(j)}, r_i^{(j)})\}
 4:
             annotate rewards:
                                                                    oldsymbol{	heta}_t \leftarrow oldsymbol{	heta}_{t-1} - \eta 
abla_{oldsymbol{	heta}} \mathcal{L}_{\mathcal{X}_t'}(oldsymbol{	heta})
 5:
             preference optimization:
 6: end for
```

2.1 The Principle: Open-ended RLHF for Joint Self-Improvement

Motivation. Classical RLHF optimizes over a *static* prompt set, thus brittle in ever-changing worlds. To have an agent that *generalizes* well across *unseen*, *novel* tasks, we must design a new objective.

Formalization. We thus formally introduce *optimizable* prompt generation policy $\pi_{\phi}(\mathbf{x})$, which is *jointly* optimized with the response policy $\pi_{\theta}(\mathbf{y} \mid \mathbf{x})$ with regard to the *joint reference policy*²:

Definition 1 (Open-ended RLHF) Let $\pi_{\phi,\theta}(\mathbf{x},\mathbf{y}) := \pi_{\phi}(\mathbf{x}) \cdot \pi_{\theta}(\mathbf{y} \mid \mathbf{x})$ and $\pi_{ref}(\mathbf{x},\mathbf{y}) := p_{ref}(\mathbf{x}) \cdot \pi_{ref}(\mathbf{y} \mid \mathbf{x})$. We define evolving alignment^a as the open-ended joint optimization on the prompt and response policy for alignment w.r.t the joint reference policy:

$$\max_{\boldsymbol{\phi},\boldsymbol{\theta}} \mathbb{E}_{\mathbf{x} \sim \pi_{\boldsymbol{\phi}}(\mathbf{x}), \mathbf{y} \sim \pi_{\boldsymbol{\theta}}(\mathbf{y}|\mathbf{x})} \left[r(\mathbf{x}, \mathbf{y}) \right] - \beta \cdot \mathbb{D}_{KL} \left[\pi_{\boldsymbol{\phi}, \boldsymbol{\theta}}(\mathbf{x}, \mathbf{y}) \parallel \pi_{ref}(\mathbf{x}, \mathbf{y}) \right], \quad (1)$$

^aThis generalizes RLHF (Eq. 4), which is a special case if π_{ϕ} is static as p_{ref} , by expanding Eq. 1:

$$\max_{\boldsymbol{\phi},\boldsymbol{\theta}} \; \mathbb{E}_{\mathbf{x} \sim \pi_{\boldsymbol{\phi}}(\cdot), \mathbf{y} \sim \pi_{\boldsymbol{\theta}}(\cdot | \mathbf{x})} \big[r(\mathbf{x}, \mathbf{y}) \big] - \beta \cdot \big(\mathbb{E}_{\mathbf{x} \sim \pi_{\boldsymbol{\phi}}(\cdot)} \big[\; \mathbb{D}_{\mathrm{KL}} \big[\pi_{\boldsymbol{\theta}}(\mathbf{y} | \mathbf{x}) \| \pi_{\mathrm{ref}}(\mathbf{y} | \mathbf{x}) \big] \; \big] - \mathbb{D}_{\mathrm{KL}} \big[\; \pi_{\boldsymbol{\phi}}(\mathbf{x}) \| p_{\mathrm{ref}}(\mathbf{x}) \; \big] \big).$$

2.2 The Mechanism: Asymmetric Self-Play via the Creator v.s. Solver Game

Intuition. It is hard to directly optimize Eq. 1, due to (i) the **intractability** of the unspecified reference [Dennis et al., 2020]; (ii) the **instability** of joint differentiation [Goodfellow et al., 2014]. We present an *alternating optimization* objective by casting it as an asymmetric creator-solver game.

- Intuitively, the creator can guide the solver by prompt curricula with *increasing complexity*, encouraging efficient and general learning to handle the diversity in the wild.
- Mathematically, this resembles RL optimization *via* expectation-maximization [Dayan and Hinton, 1997, Singh et al., 2023], where ϕ for the prompt distribution is fixed at each step.

Formalization. We formalize the alternating optimization as an asymmetric game as follows:

- Creator: the prompt player π_{χ} that strategically generate prompts for the solver.
- **Solver**: the response player $\pi_{\mathcal{Y}|\mathcal{X}}$ (or π) that learn to generate preferred responsess.

We use *minimax regret* strategy [Savage, 1951, Dennis et al., 2020], where the solver minimizes and the creator maximizes regret (see § A). At the equilibrium [Nash et al., 1950], there is:

Remark 1 (Minimax Regret) If the solver-creator game reaches an equilibrium, the solver follows a minimax regret strategy, i.e., it optimizes to perform well under all cases:

$$\boldsymbol{\pi}^{\star} \in \arg\min_{\boldsymbol{\pi} \in \Pi_{\mathcal{V}|\mathcal{X}}} \max_{\boldsymbol{\pi}_{\mathcal{X}} \in \Pi_{\mathcal{X}}} \mathbb{E}_{\mathbf{x} \sim \pi_{\mathcal{X}}} \Big[\operatorname{Regret}(\mathbf{x}, \boldsymbol{\pi}) \Big].$$
 (2)

However, without access to the true optimal policy, we must approximate the regret. Leveraging the *stochastic policy* and the *reward model*, we design the advantage-based proxy:

Definition 2 (Informativeness Proxy) We measure the informativeness of a prompt by the (absolute) empirical worst-case optimal advantage, approximating the minimax regret:

$$info(\mathbf{x}) \leftarrow \widehat{A}_{\min}^{\star} := |\min_{\mathbf{y}} r(\mathbf{x}, \mathbf{y}) - \max_{\mathbf{y}'} r(\mathbf{x}, \mathbf{y}')|,$$
 (3)

which is estimated by sampling multiple responses for \mathbf{x} from the solver and calculating gap between the maximal reward (from the best \mathbf{y}) and the minimal reward (from the worst \mathbf{y}).

In sum, our open-ended RLHF allow for an evolving joint distribution for better generalization; the minimax regret objective adds *robustness* on such evolving curricula by *incentivizing agents to align well in all cases*. We use the informativeness proxy (see § C for more; an attentive reader may want to distinguish it from Shannon's [Shannon, 1948]) to guide learning. Together, it is a mechanism that the creator keeps challenging the solver, and the solver learns to improve.

²Here, $p_{ref}(\mathbf{x})$ represents an idealized, potentially intractable probability measure over all possible tasks (instantiated *via* prompts) in the wild, as a conceptual reference or a guiding target for alignment.

3 Main Experimental Results

eva brings notable gains in alignment without relying on any human-crafted data, thus offering data efficiency as well. In the base setup, from the one-iteration finetuned model $(\theta_{0\rightarrow 1})$, **eva** adds a creator to self-evolve prompts of the initial iteration and optimizes for an additional open-ended RLHF iteration, resulting in $\theta_{1\rightarrow \tilde{1}}$. See detailed settings in § D.

eva achieves self-improvement. As shown in red rows in Table 1, **eva** yields notable performance improvement over $\theta_{0\to 1}$ across different optimization algorithms, especially on the harder Arena-Hard benchmark, which is recognized to be more challenging and distinguishable among others due to the complexity of its prompts and its fairer scoring system [Li et al., 2024b]. For example, **eva** brings 8.5% gain with DPO as the solver, surpassing its 27B version and matching claude-3-opus as in the AH leaderboard, while using fully self-automated joint generation.

eva can surpass human-crafted prompts. We further show that **eva**-prompt-trained models $(\theta_{1 \to \tilde{1}})$ can match and even outperform those trained on additional new prompts from UltraFeedback $(\theta_{1 \to \tilde{2}})$ (which we denoted as human prompts), while being much cheaper and more efficient. Additionally, on MT-Bench, training with new human prompts typically show decreased performance in the first turn and only modest gains in the second turn. In contrast, **eva** notably enhances second-turn performance. We hypothesize that **eva** evolves novel, learnable prompts that include characteristics of second-turn questions, reflecting emergent skills like handling follow-up interactions.

$\color{red} \overline{\text{Model Family } (\rightarrow)}$			Gемма	-2-9B-IT		
Benchmark (\rightarrow)	Arena-Hard		MT-Benc	AlpacaEval 2.0		
$\mathbf{Method} \ (\downarrow) \ \mathbf{/} \ \mathbf{Metric} \ (\rightarrow)$	WR (%)	avg. score 1st turn 2nd turn			LC-WR (%)	WR (%)
θ_0 : SFT	41.3	8.57	8.81	8.32	47.11	38.39
$\overline{\theta_{0 \to 1}}$: DPO	51.6	8.66	9.01	8.32	55.01	51.68
$ heta_{ extstyle 1 o ilde{1}}$: + eva	60.1 (+8.5)	8.90	9.04	8.75 (+0.43)	55.35	55.53
$ heta_{1 o 2}$: +new human prompts	59.8	8.64	8.88	8.39	55.74	56.15
$\overline{\boldsymbol{\theta}_{0 \to 1}}$: SPPO	55.7	8.62	9.03	8.21	51.58	42.17
$ heta_{1 o ilde{1}}$: + eva	58.9 (+3.2)	8.78	9.11	8.45 (+0.24)	51.86	43.04
$ heta_{1 o 2}$: +new human prompts	57.7	8.64	8.90	8.39	51.78	42.98
$\theta_{0 \to 1}$: SimPO	52.3	8.69	9.03	8.35	54.29	52.05
$ heta_{ extstyle 1 o ilde{1}}$: + eva	60.7 (+8.4)	8.92	9.08	8.77 (+0.42)	55.85	55.92
$ heta_{1 ightarrow2}$: + new human prompts	54.6	8.76	9.00	8.52	54.40	55.72
$\overline{\boldsymbol{\theta}_{0 \to 1}}$: ORPO	54.8	8.67	9.04	8.30	52.17	49.50
$ heta_{1 o ilde{1}}$: + eva	60.3 (+5.5)	8.89	9.07	8.71 (+0.41)	54.39	50.88
$ heta_{1 o 2}$: +new human prompts	57.2	8.74	9.01	8.47	54.00	51.21

Table 1: **Main results.** Our **eva** achieves notable alignment gains and can surpass human prompts on major benchmarks across a variety of representative direct preference optimization algorithms.

We then conduct in-depth ablation studies on eva, with findings below in the Appendix:

- § E.1 informativeness metric: our *regret*-based metric outperforms other alternatives.
- § E.2 sample-then-evolve procedure: our method outperforms greedy selection.
- § E.3 scaling w/ reward models: the alignment gain of eva scales with reward models.
- § E.4 **continual training**: our method has monotonic gain with incremental training; the *evolved data and schedule* by **eva** serves as an *implicit regularizer* for better local minima.

4 Concluding Remarks

eva is a new, simple framework for aligning language models, and can be plugged into any existing alignment pipeline. The primary takeaway may be that RLHF can be made open-ended: (i) self-evolving joint data distributions can bring significant gain (as shown across various preference optimization algorithms), and (ii) reward advantage acts as an effective metric informing the collection and creation of *future* prompts for alignment. **eva** presents a new view of alignment by framing it as an asymmetric game between a creator generating *new* and *learnable* prompts and a solver producing preferred responses. **eva** also *incentivizes agents to create problems* rather than to simply *solve problems*, which is a key feature of intelligence, yet model trainers often neglect.

Appendix

A Preliminaries

We hereby review major concepts, which we later in $\S 2$ use *regret* and the proxy by *advantage* to identify informative prompts, leading to learning curricular implicitly maximizing *contrastive ratio*.

Alignment by RLHF. Classical RLHF [Ouyang et al., 2022] optimizes on a fixed distribution \mathcal{D} :

$$\max_{\pi_{\theta}} \mathbb{E}_{\mathbf{x} \sim \mathcal{D}, \mathbf{y} \sim \pi_{\theta}(\mathbf{y}|\mathbf{x})} \left[r(\mathbf{x}, \mathbf{y}) \right] - \beta \cdot \mathbb{D}_{KL} \left[\pi_{\theta}(\mathbf{y} \mid \mathbf{x}) \parallel \pi_{ref}(\mathbf{y} \mid \mathbf{x}) \right], \tag{4}$$

where x and y denote the prompts and responses, and $r(\cdot, \cdot)$ is the reward function.

Reward. Let the *optimal policy* of Eq. 4 be $\pi^*(\cdot)$ and $Z(\cdot)$ be the partition function, we have:

$$r(\mathbf{x}, \mathbf{y}) = \beta \cdot \log \frac{\pi^{\star}(\mathbf{y} \mid \mathbf{x})}{\pi_{\text{ref}}(\mathbf{y} \mid \mathbf{x})} + \beta \cdot \log Z(\mathbf{x}).$$
 (5)

Regret. Let $r^*(\mathbf{x}) = \max_{\mathbf{y}'} r(\mathbf{x}, \mathbf{y}')$ be the optimal reward achievable at \mathbf{x} , the regret to take \mathbf{y} is:

$$Regret(\mathbf{x}, \mathbf{y}) = r^{\star}(\mathbf{x}) - r(\mathbf{x}, \mathbf{y}). \tag{6}$$

The regret with regard to policy is defined as:

$$\operatorname{Regret}(\mathbf{x}, \pi) = \mathbb{E}_{\mathbf{y}' \sim \pi(\mathbf{y}'|\mathbf{x})} \left[r(\mathbf{x}, \mathbf{y}') \right] - \mathbb{E}_{\mathbf{y}' \sim \pi^{\star}(\mathbf{y}'|\mathbf{x})} \left[r(\mathbf{x}, \mathbf{y}') \right]. \tag{7}$$

Advantage. The *advantage* function quantifies how much better a response y is w.r.t. a baseline:

$$A(\mathbf{x}, \mathbf{y}) = r(\mathbf{x}, \mathbf{y}) - \mathbb{E}_{\mathbf{y}' \sim \pi(\mathbf{y}'|\mathbf{x})} \left[r(\mathbf{x}, \mathbf{y}') \right].$$
(8)

Variants of advantage (e.g., the worst-case advantage A_{\min}^{\star}) are related to regret, as shown in Table 2.

Direct preference optimization. The DPO [Rafailov et al., 2023] objective for RLHF is:

$$\mathcal{L}_{\beta}^{\text{DPO}}(\pi_{\boldsymbol{\theta}}) = \sum_{(\mathbf{y}_{+}, \mathbf{y}_{-}, \mathbf{x}) \in \mathcal{D}} -\log \left[\sigma \left(\beta \cdot \Delta_{\boldsymbol{\theta}; \text{ ref}}^{\mathbf{x}}\right)\right],\tag{9}$$

where we use +, - to denote chosen and rejected responses, and denote the **contrastive ratio** as:

$$\Delta_{\boldsymbol{\theta}; \text{ ref}}^{\mathbf{x}} := \log \frac{\pi_{\boldsymbol{\theta}} \left(\mathbf{y}_{+} \mid \mathbf{x} \right)}{\pi_{\text{ref}} \left(\mathbf{y}_{+} \mid \mathbf{x} \right)} - \log \frac{\pi_{\boldsymbol{\theta}} \left(\mathbf{y}_{-} \mid \mathbf{x} \right)}{\pi_{\text{ref}} \left(\mathbf{y}_{-} \mid \mathbf{x} \right)}. \tag{10}$$

By reward reparameterization with Eq. 5, advantage also relates to contrastive ratio, as in § C.

B The Practical Algorithm

We now illustrate **eva** of Algorithm 1 (cf., Fig 3), with specifications in Appendix I.

B.1 The Creator Step: Estimate, Sample then Evolve

Plainly, the creator finds most useful prompts and generate variants of them for preference optimization. One may relate this to **evolution strategies** [Schwefel, 1977] which find the most promising species, then mutate and crossover, or to **curriculum RL** [Parker-Holder et al., 2022] which finds environments with high-regret levels, then edits within some distance. As in Section 2.2, we do not seek a differentiable creator in this work. The creator is implemented in three steps as in Figure 3.

Step 1: $info(\cdot)$ – estimate the informativeness. For each x in the prompt set \mathcal{X}_t , we generate responses, annotate rewards and estimate a informativeness metric to x by Eq. 3 (see also Table 2).

Step 2: $sample(\cdot)$ – weighted sampling for an informative subset. Using the informativeness metric as the weight, we sample a informative prompt subset \mathcal{X}_t^{info} to be evolved later.

Step 3: $evolve(\cdot)$ – evolving for a proximal region of high-advantage prompts. Our algorithm is agnostic to and does not rely on any specific evolving method. We take EvolInstruct [Xu et al., 2023a] as an off-the-shelf method, which conducts in-depth (*i.e.*, adding constraints, deepening, concretising, complicating) and in-breadth evolving (*i.e.*, mutation) for prompts. Specifically, we iterate over each prompt in the $\mathcal{X}_t^{\text{info}}$, where each one is evolved to multiple variations, then optionally mix the newly generated prompts with a uniformly sampled buffer from \mathcal{X}_t to create \mathcal{X}_t' .

B.2 The Solver Step: Solve then Optimize

This step is the classical preference optimization [Rafailov et al., 2023], where responses are generated and the gradient descent is performed. Take the pointwise reward model setting as an example, for every prompt, we sample n responses with reward annotated for each; we take the responses with the maximal and the minimal reward to construct the preference pairs, then optimize upon.

Put together, **eva** can unify existing iterative optimization pipeline [Tran et al., 2023] with a new creator module, which can either share the same network as the solver policy or operate independently.

C Understanding eva in Different Intuitive Ways

Learning potential. Our metric intuitively identifies the learning potential of a prompt by measuring the gap between the best and worst response to it from the solver. We reason, that prompts eliciting *both* high-reward and low-reward outcomes, reflect *learnable* tasks where the model is capable of improving but has not yet mastered, thereby implying learning potential (*cf.*, Jiang et al. [2021b]).

Worst-case guarantees. The minimax-regret objective, by design, leads to solvers that perform robustly across the prompt space, thus gives the worst-case guarantee. While exact equilibrium may not be attainable with approximation, our empirical results in § E.1 demonstrate robustness.

Auto-curricula for the players. With the stochastic policy, the advantage may be heuristically understood as the reward difference between *a base solver* and *a reference solver*. Rather than optimizing separate solvers [Dennis et al., 2020], we sample multiple times from the same policy to create the pair. In this way, the creator is incentivized to produce new prompts that are just out of the comfort zone of solvers [Chaiklin et al., 2003]:

- For overly challenging prompts, both solutions perform poorly, leading to a low proxy.
- For overly easy prompts, the base solution already performs well, again giving a low proxy.
- The optimal strategy is to find prompts that are just beyond the solver's current capability.

Auto-curricula inherent to Contrastive Optimization. Contrastive preference optimization generalizes DPO and a family of algorithms (*c.f.*, Hejna et al. [2023], Rafailov et al. [2023], Tang et al. [2024]), many of whose losses monotonically decrease as the contrastive ratio increases. Here, by Eq. 5 and Eq. 10, the *contrastive ratio* can be written via the *advantage-based proxy*:

$$A_{\min}^{\star}(\mathbf{x}) = \beta \cdot \Delta_{\boldsymbol{\theta}^{\star}: \, \text{ref}}^{\mathbf{x}}. \tag{11}$$

By our proxy, we implicitly incentivize the creator to generate prompts that *bring the most contrastive responses*, which decrease the loss the most. This matches the curriculum learning literature, which prioritizes (in our case, *generatively* prioritizes) examples with smaller losses for better convergence and generalization [Bengio et al., 2009]. We hereby suggest the Contrastive Curriculum Hypothesis: in contrastive preference optimization, prioritizing prompts with higher contrastive ratio improves sample efficiency and generalization. We show initial empirical results on this in § E.1 and § E.4.

D Additional Experimental Settings

Datasets and models for training. We use **UltraFeedback** [Cui et al., 2023] as the training dataset, which contains diverse high-quality prompts that are primarily human-generated. We use the instruction-finetuned GEMMA-2-9B [Team et al., 2024] as the primary model, which is a strong baseline for models of its size. In training, Each iteration uses 10K prompts (*i.e.*, 1/6 partition from UltraFeedback in classical training). We denote $\theta_{t \to t+1}$ as the model trained w/ new human prompts based on the t-th checkpoint, and $\theta_{t \to \tilde{t}}$ as the one trained w/ evolved prompts from the t-th checkpoint w/o adding any new human prompts. Detailed re-implementation instructions can be found in § I.

Evaluation settings. We choose: (i) **AlpacaEval 2.0** [Dubois et al., 2024], which assesses general instruction following with 805 questions; (ii) **MT-Bench** [Zheng et al., 2023], which evaluates multi-turn instruction following with 80 hard questions in 8 categories; (iii) **Arena-Hard** [Li et al., 2024b], which is derived from 200K user queries on Chatbot Arena with 500 challenging prompts across 250 topics. We use gpt-4-1106 as the judge and gpt-4-0314 as the baseline for win rate.

Optimization algorithms. We focus on direct preference optimization and consider the following:

- With reference policy: DPO [Rafailov et al., 2023], SPPO [Wu et al., 2024].
- Without reference policy: SimPO [Meng et al., 2024], ORPO [Hong et al., 2024].

Reward models as preference oracles. We use ARMORM-8B [Wang et al., 2024] as our default reward model as the human-preference proxy, and consider the following for ablation studies:

- Pointwise: ARMORM-8B [Wang et al., 2024], SKYWORKRM-27B [Liu and Zeng, 2024].
- Pairwise: PAIRRM-0.4B [Jiang et al., 2023], PAIRRM-8B [Dong et al., 2024].

E Ablation Studies

E.1 The Choice of Informativeness Metrics: info(·)

Metric	$\mathbf{info}(\mathbf{x})$	Related Interpretations
A_{\min}^{\star} : worst-case optimal advantage	$ \min_{\mathbf{y}} r(\mathbf{x}, \mathbf{y}) - \max_{\mathbf{y}'} r(\mathbf{x}, \mathbf{y}') $	minimax regret [Savage, 1951]
A_{avg}^{\star} : average optimal advantage	$\left \frac{1}{N}\sum_{\mathbf{y}}r(\mathbf{x},\mathbf{y})-\max_{\mathbf{y}'}r(\mathbf{x},\mathbf{y}')\right $	Bayesian regret [Banos, 1968]
$A_{\rm dts}^{\star}$: dueling optimal advantage	$ \max_{\mathbf{y} \neq \mathbf{y}^*} r(\mathbf{x}, \mathbf{y}) - \max_{\mathbf{y}'} r(\mathbf{x}, \mathbf{y}') $	dueling regret [Wu and Liu, 2016]

Table 2: The reward-advantage-based metrics that serve as the informativeness proxies for prompts.

$\overline{\text{Model Family } (\rightarrow)}$							
Benchmark (\rightarrow)	Arena-Hard MT-Bench			h	AlpacaEval 2.0		
$Method (\downarrow) / Metric (\rightarrow)$	WR (%)	avg. score	1 st turn	2 nd turn	LC-WR (%)	WR (%)	
$\overline{oldsymbol{ heta}_{0 ightarrow 1}}$: DPO	51.6	8.66	9.01	8.32	55.01	51.68	
$\overline{ heta_{1 o ilde{1}}}$: +eva (uniform)	57.5	8.71	9.02	8.40	53.43	53.98	
$\begin{array}{cccc} & & & & \\ & \theta_{1 \rightarrow \tilde{1}} \colon & + \operatorname{eva} \ (\operatorname{var}(r)) & & \\ & \theta_{1 \rightarrow \tilde{1}} \colon & + \operatorname{eva} \ (\operatorname{avg}(r)) & & \\ & \theta_{1 \rightarrow \tilde{1}} \colon & + \operatorname{eva} \ (1/\operatorname{avg}(r)) & & & \end{array}$	54.8 58.5 56.7	8.66 8.76 8.79	9.13 9.13 9.13	8.20 8.40 8.45	54.58 55.01 55.04	52.55 55.47 54.97	
$\overline{\theta_{1 o ilde{1}}}$: + eva $(1/A_{\min}^{\star})$	52.3	8.64	8.96	8.31	53.84	52.92	
$\begin{array}{cccc} \boldsymbol{\theta}_{1 \rightarrow \tilde{1}} \colon & + \operatorname{\textbf{eva}} \ (A_{\operatorname{avg}}^{\star}) \ \text{(our variant)} \\ \boldsymbol{\theta}_{1 \rightarrow \tilde{1}} \colon & + \operatorname{\textbf{eva}} \ (A_{\operatorname{dts}}^{\star}) \ \text{(our variant)} \end{array}$	60.0 60.0	8.85 8.86	9.08 9.18	8.61 8.52	56.01 55.96	56.46 56.09	
$oldsymbol{ heta}_{1 ightarrow ilde{1}}$: + eva (A^\star_{\min}) (our default)	60.1 (+8.5)	8.90	9.04	8.75 (+0.43)	55.35	55.53	

Table 3: **Choice of informativeness metric.** Our informativeness metric by *advantage* achieves the best performances, comparing with others as the weight to sample prompts to evolve by the creator.

Advantage as the informativeness metric outperforms baselines. As in Table 3, eva offers an effective curriculum by the advantage-based proxy as the informativeness metric (bottom row):

- Comparing w/ uniform evolving (brown): Existing baselines generate prompts in a uniform manner [Yuan et al., 2024] w/o informativeness measure (cf., the principle of insufficient reason [Keynes, 1921, Tobin et al., 2017]). Ours (red) concretely outperform, corroborating Das et al. [2024] that uniform learners can suffer sub-optimality gaps.
- Comparing w/ other heuristics (blue): Prior practices [Team et al., 2023] tried heuristics like prioritizing prompts w/ the most variance in its rewards or w/ the lowest/highest average. We find our advantage based methods (red) outperforms those heuristics.
- Comparing w/ the *inverse advantage* (purple): Contrary to curriculum learning, a line of works conjecture that examples w/ higher losses may be prioritized [Jiang et al., 2019,

Kawaguchi and Lu, 2020], which can be done by inverting our metric. We find it significantly *hurt* the alignment gain, corroborating Mindermann et al. [2022] that those examples are often noisy, unlearnable or irrelevant, meaning our curriculum is effective and practical.

Among our advantage variants (red): We designed variants of our default advantage-based metric, as in Table 2; the default A^{*}_{min} remains competitive among its peers. Together, the advantage-based principle provides a robust guideline for prompt sampling and evolving.

The lesson is that we must be selective about which are the promising to evolve, otherwise unlearnable, noisy or nave prompts may hinder learning. Our regret-inspired metric represents a solid baseline.

E.2 The Effect of the sample-then-evolve procedure

Benchn	nark (→)	Arena-Hard	N	MT-Bench			AlpacaEval 2.0		
Method	$\mathbf{I}\left(\downarrow\right)$ / Metric $(ightarrow)$	WR (%)	avg. score	1 st turn	2 nd turn	LC-WR (%)	WR (%)		
$\overline{oldsymbol{ heta}_{0 ightarrow1}}$: Γ	OPO	51.6	8.66	9.01	8.32	55.01	51.68		
$oldsymbol{ heta_{1 o ilde{1}}:} oldsymbol{ heta_{1 o ilde{1}}:}$	<pre>[no evolve]-greedy [no evolve]-sample</pre>	56.1 55.3	8.68 8.69	8.98 9.00	8.38 8.38	54.11 54.22	53.66 54.16		
$\overline{oldsymbol{ heta}_{1 ightarrow ilde{1}}}$:	+ eva-greedy (our variant)	59.5	8.72	9.06	8.36	54.52	55.22		
$\theta_{1\rightarrow\tilde{1}}$:	+ eva-sample (our default)	60.1	8.90	9.04	8.75	55.35	55.53		

Table 4: **Effect of evolving.** The blue are those training w/ only the informative subset and w/o evolving); we denote <code>-sample</code> for the default weighted sampling procedure in Algo 1, while using <code>-greedy</code> for the variant from the classical active data selection procedure (*cf.*, a recent work [Muldrew et al., 2024] and a pre-LLM work [Kawaguchi and Lu, 2020]), which selects data by a high-to-low ranking via the metric greedily. We show evolving brings a remarkable alignment gain (the red v.s. the blue); and as we evolve, sampling is more robust than being greedy (*cf.*, Russo et al. [2018]).

The design of evolve (·) in eva is effective. As in Table 4, we show:

- Removing the evolve(·) step: if we only do subset sampling or ordered selection, we still have gain, but not as much as w/ evolving (e.g., eva brings 4.8% additional wins on AH).
- Altering the sample(·) step: if we greedily select prompts by the metric instead of using them as weights for importance sampling, the performance will be weaker as we evolve.

This shows that simply adaptive training within a fixed prompt distribution is unsatisfactory; our openended RLHF with *generative* prompt exploration gives a substantial headroom for self-improvement.

E.3 Scaling Pointwise and Pairwise Reward Models

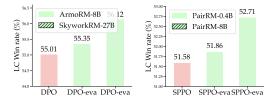


Figure 4: **eva scales with quality of reward models**, under pointwise RMs w/ DPO (*left*) and pairwise RMs w/ SPPO (*right*). Note SPPO handles general preferences thus requires pairwise RMs, and DPO relies on the Bradley-Terry assumption, for which pointwise RMs are suitable.

Figure 4 presents the length-controlled win rate of **eva** on AlpacaEval using pointwise and pairwise reward models of varying scales. The results give a clear trend: as the quality of reward models improve, **eva** brings higher alignment gain. The scaling observation shows the effectiveness of **eva** in exploiting more accurate reward signals to choose informative prompts for better alignment. One takeaway is interaction w/ the external world is essential for intelligence. The more accurate reward signals observed, the better the agent incentivize themself to improve (cf., Silver et al. [2021]).

E.4 eva Improves Both Sample Efficiency and Generalization

We then continuously run the default *incremental training* (*i.e.*, trainining from the last checkpoint w/ the evolved set in each iteration), as in Fig 5, **eva** presents *monotonic performance gain* over iterations, and surpasses that trained w/ new human prompts, implying the generalization benefit. Specifically, we conjecture that behaviors of the dashed/dotted lines relate to *loss of plasticity* [Ash and Adams, 2019, Dohare et al., 2023, Abbas et al., 2023, Xue et al., 2024]. Classical works resolve it by the optimization view (*e.g.*, weight perturbing), whereas **eva** provides a view from data scheduling, potentially mimicking an *implicit regularizer for better generalization*.

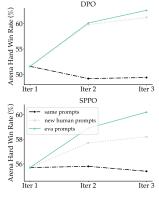


Figure 5: **Continual training. eva** stays robust w/ more iterations in incremental training.

The solutions found by **eva** cannot be recovered by training longer w/a fixed distribution (the dashed), nor by navely sourcing new prompts w/o examining informativeness (the gray dotted), thus our generative data schedule is effective.

In Table 5, we ablate **eva** in *scratch training*, *i.e.*, training w/ the full set (the evolved and the original data). **eva** is competitive in incremental training, thus *learns more effective* with *less data* – a nice bonus via minimax regret [Jiang et al., 2021a].

$\overline{\text{Benchmark}\left(\rightarrow\right)}$	Arena-Hard	MT-Bench	AlpacaEval 2.0 LC-WR (%)	
$Method \left(\downarrow \right) / Metric \left(\rightarrow \right)$	WR (%)	avg. score		
θ_0 : SFT	41.3	8.57	47.11	
$\theta_{0\rightarrow 1}$: DPO	51.6	8.66	55.01	
$\theta_{0 \to \tilde{1}}$: eva (scratch) $\theta_{1 \to \tilde{1}}$: eva (incremental)	59.8 60.1	8.88 8.90	54.59 55.35	

Table 5: Ablation on incremental v.s. scratch training.

F Additional Experimental Results

In general, **eva** maintains the accuracy on downstream tasks and is robust on those reasoning-heavy tasks, and the scaling with reward models is more prominent on AlpacaEval, possibly due to the training sources for such reward models [Wang et al., 2024, Liu and Zeng, 2024].

$\overline{\mathbf{Method}\left(\downarrow\right)/\mathbf{Dataset}\left(\rightarrow\right)}$	MUSR-TA	TruthfulQA-Gen	WMDP	GSM8K	GSM-Plus	MMLU-Pro
θ_0 : SFT	38.80	34.76	58.62	24.64	18.62	52.08
$\theta_{0\rightarrow 1}$: DPO	38.40	34.76	58.45	24.56	18.50	52.63
$ heta_{1 o ilde{1}}$: + eva	38.40	34.15	58.40	24.26	17.96	53.03
$\theta_{0\rightarrow 1}$: SPPO	40.80	34.15	58.72	24.79	18.42	52.70
$\theta_{1 \rightarrow \tilde{1}}$: + eva	41.20	34.64	58.94	25.40	18.88	52.47

Table 6: Performance on Downstream tasks.

Model Family (\rightarrow)	GEMMA-2-9B-IT							
Benchmark (→) MT-Bench		MT-Bench Arena-Hard			Al	pacaEval 2	.0	
$Method (\downarrow) / Metric (\rightarrow)$	avg. score	1st turn	2 nd turn	WR (%)	avg. len	LC (%)	WR (%)	avg. len
$\theta_{0\rightarrow 1}$: DPO	8.66	9.01	8.32	51.6	651	55.01	51.68	1883
$\theta_{1\rightarrow \bar{1}}$: + eva-i (ARMO-8B)	8.90	9.04	8.75	60.1	725	55.35	55.53	2089
$\theta_{1 \rightarrow \tilde{1}}$: + eva-i (SKYWORKRM-27B)	8.75	9.07	8.43	60.3	744	56.12	56.40	2097

Table 7: Effect of (pointwise) reward models.

Model Family (\rightarrow)	GEMMA-2-9B-IT							
Benchmark (\rightarrow)	MT-Bench Arena-Hard AlpacaEval				pacaEval 2.	.0		
$Method \left(\downarrow \right) / Metric \left(\rightarrow \right)$	avg. score	1st turn	2 nd turn	WR (%)	avg. len	LC (%)	WR (%)	avg. len
$\theta_{0\rightarrow 1}$: SPPO	8.62	9.03	8.21	55.7	560	51.58	42.17	1850
$\theta_{1\rightarrow \bar{1}}$: + eva-i (PAIRRM-0.4B) $\theta_{1\rightarrow \bar{1}}$: + eva-i (PAIRRM-8B)	8.78 8.89	9.11 9.08	8.45 8.70	58.9 60.2	567 563	51.86 52.71	43.04 44.52	1870 1848

Table 8: Effect of (pairwise) reward models.

G Related Works

Self-improving algorithms and iterative optimization. This line of work focuses on iteratively generating samples from the response policy and continuously re-training the policy by selected self-generated samples. Major works include ReST [Gulcehre et al., 2023, Singh et al., 2023], STaR [Zelikman et al., 2022], RFT [Yuan et al., 2023], RAFT [Dong et al., 2023], self-improving LLMs [Huang et al., 2022, Yuan et al., 2024]; in the context of preference optimization, iterative DPO [Xu et al., 2023b, Tajwar et al., 2024, Tran et al., 2023, Xiong et al., 2024, Pang et al., 2024] has proven effective. Most works focus on self-training by improving in $\mathcal{Y} \mid \mathcal{X}$, while we *jointly optimize* both responses and prompts via generative exploration in the $(\mathcal{X}, \mathcal{Y})$ space. Among them, we also distinctly present a game-theoretic framework with the minimax-regret principle as the guidance.

Prompt synthesis for language models. Existing works include Self-Instruct [Wang et al., 2022], WizardLM [Xu et al., 2023a, Luo et al., 2023], Self-Align [Sun et al., 2024], Glan [Li et al., 2024a], EvoPrompt [Guo et al., 2023], Magpie [Xu et al., 2024] and others [Long et al., 2024]. **eva** is an orthogonal contribution since any synthesis method can be plugged in as the evolve(·) for the creator. Importantly, our work presents a new reward-related metric to endow prompt the notion of informativeness, with new implications as in § C. We also focus on preference optimization algorithms, while those existing works primarily use synthesized prompts in an SFT-only way.

Self-play and curriculum RL. Agents trained on a fixed data distribution are often brittle and may struggle to adapt to the real world [Hughes et al., 2024]. Self-play [Samuel, 1959, Goodfellow et al., 2014, Silver et al., 2016] addresses this by having the agent learn through self-interaction, thus creating more diverse experiences and automatic curricula. In asymmetric self-play, the paradigm centers on "Alice proposing a task, and Bob doing it" [Sukhbaatar et al., 2017, Samvelyan et al., 2023, Beukman et al., 2024, Dennis et al., 2020]. Other nice game-theoretic frameworks that guide learning agents include Bai et al. [2020], Anil et al. [2021], Rajeswaran et al. [2020]. We revive the classical asymmetric self-play principle [Sutton et al., 2011] in optimizing language models. Unlike traditional curriculum RL [Parker-Holder et al., 2022], which usually renders environments from specified levels [Dennis et al., 2020], our approach is *generative* by nature, as we directly generate contexts from the auto-regressive language models.

Self-play in RLHF. A growing line of research frames RLHF as a *symmetric* self-play game, where both players are response players [Munos et al., 2023, Wu et al., 2024, Choi et al., 2024, Rosset et al., 2024]. However, these methods still rely on a fixed prompt distribution thus is sub-optimal. In contrast, we solve this by *asymmetric* self-play, enabling evolving prompt distributions for more generalizable language agents. During our work, we notice one concurrent paper adopting the asymmetric two-player setup [Zheng et al., 2024], however (i) it applies to adversarial attack tasks instead of general alignment benchmarks, (ii) it is incompatible w/ direct preference optimization, and (iii) it relies on the maxmin principle (which is known to be producing unlearnable environments [Dennis et al., 2020]) instead of the minimax *regret* principle [Fan, 1953, Savage, 1951] as we do. We also first precisely defined the new problem of open-ended RLHF, which generalizes over classical RLHF.

H Future Directions

eva defines a new paradigm for alignment, opening up many new directions, e.g., (i) extending to differentiable creator policies, combining w/ other evolve(·) methods; (ii) evolving for more iterations w/ on-policy solvers like RLOO [Ahmadian et al., 2024]; (iii) investigating exploration bonuses for diversity, coverage and extrapolation, and self-consuming loops [Gerstgrasser et al., 2024]; (iv) extending the game with more players for full automation (e.g., rewarders, critics, rewriters, verifiers, retrievers); (v) extending from alignment to reasoning (e.g., auto-conjecturing in theorem proving [Poesia et al., 2024] can be cast as asymmetric games), w/ process reward models and hierarchical tree search for creator and solver generations; (vii) exploring other metric like Fisher information for theoretical guarantees; (vii) scaling up w/ million-level data.

I Appendix on Reproducibility

As mentioned, currently we put supplementary materials and additional experiment results on anonymous.4open.science/r/eva-i-workshop/, where we intend to release code there, and all the datasets (generated prompts and responses) and models (with other models beyond the current family), *upon approval* – before then, we are more than happy to provide any clarification requested to help re-implement **eva** and replicate our results.

Our code base is made to be simple to use for practitioners, requiring **only a creator module addition** within the commonly adopted Alignment Handbook pipeline.

Hyperparameter settings. We follow the original hyperparameter settings as in [Hong et al., 2024, Meng et al., 2024, Wu et al., 2024], default to be:

$\overline{\text{Hyperparameter } (\downarrow) / \text{Loss } (\rightarrow)}$	DPO	ORPO	SimPO	SPPO
learning rate	5e-7	5e-7	8e-7	5e-7
learning rate scheduler	cosine	cosine	cosine	linear
β	0.05	/	10	0.001
γ	/	/	5	/
$\dot{\lambda}$	/	0.5	/	/
no. epochs per iter	2	1	1	6
warmup ratio per iter	0.1	0.1	0.1	0.1
effective batch size	8	8	32	8
max length	2048	2048	2048	1024
max prompt length	1024	1024	1024	512
optimizer	adamw	adamw	adamw	rmsprop

Iterative Training Settings. By default [Tran et al., 2023, Yuan et al., 2024], we train with equal-size prompt subset in each iteration. Unless otherwise specified, we use 10K prompts from the UltraFeedback dataset [Cui et al., 2023] per iteration. The incremental training proceeds as follows:

- θ_0 : Base SFT model.
- θ_{0→1}: initialize with θ₀; then train with the prompt split X₁ by self-generated responses from the initial model θ₀.
- $\theta_{1\to 2}$: initialize with $\theta_{0\to 1}$; trained with the prompt split \mathcal{X}_2 via by self-generated responses from the initial model $\theta_{0\to 1}$.

For evolving prompts (e.g., evolving \mathcal{X}_1 to $\mathcal{X}_{\bar{1}}$), with the calculated informativeness metric for each prompt, we normalize them as the weight to do weighted sampling for a 25% informative subset to get $\mathcal{X}_1^{\text{info}}$. We then iterate over in $\mathcal{X}_1^{\text{info}}$ and call <code>EvolInstrut</code> [Xu et al., 2023a] as the plug-in evolving method (with the number of evolutions as 4) using the default mutation templates for (i) in-depth evolving (constraints, deepening, concretizing, increased reasoning steps) and (ii) in-breadth evolving (extrapolation) as implemented in <code>tasks/evol_instruct/utils.py</code> of <code>distilabel==1.3.2</code>. Next we uniformly select 80% prompts from this evolved dataset and 20% from the original dataset (i.e., the buffer) to form $\mathcal{X}_{\bar{1}}$. We do not seek extensive parameter search (e.g., the number of evolutions, the evolving ratio) in this stage and encourage future works on exploring this and other plug-in evolving methods. For solver we generate 6 responses per prompt.

Software environments. All our experiments are conducted on 8xNVIDIA H100 SXM GPUs. Our codebase primarily relies on transformers==4.40.0. For the response generation of GEMMA models at the training stage, we use vllm==0.5.4 with flashinfer backend for CUDA 12.4 and torch 2.4. For evolving prompts, we use distilabel==1.3.2, and use LiteLLM to serve Gemini, OpenAI (default to be gpt-4o-mini) and transformers models. For evaluation on all benchmarks, we use sglang==0.2.10 and openai==1.35.14, with gpt-4-1106-preview as the judge model and gpt-4-0314-preview as the baseline model. Specifically for AlpacaEval 2.0, we use alpaca_eval_gpt4_turbo_fn as the annotator config. We use 42 as the random seed.

J Examples on Prompts and Model Generations

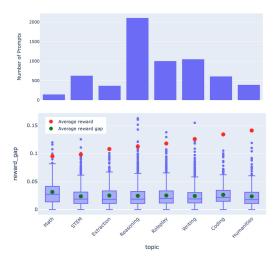


Figure 6: The initial prompt distribution of AlpacaEval by bart-large-mnli with 0-shot classification, which is imbalanced. For the reward distribution, the category with lowest average reward has the highest reward gap (*i.e.*, the default informativeness proxy), implying the potential to improve.

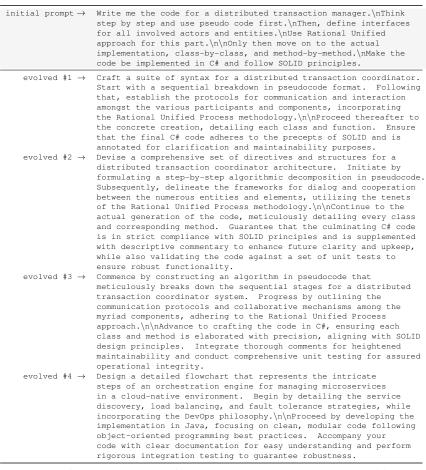


Table 9: Examples of evolved prompts from AlpacaEval. We suggest practitioners to include generated responses with oracle rewards and self-critique in the context for better prompt evolving, which is helpful for mitigating the effect of potential self-consuming loops in synthetic data training.

1st-turn prompt: When a number is divided by 10, the remainder is 4. What is the remainder when twice the number is divided by 4?

```
Answer from gemma-2-9b-it-dpo
                                       Answer from gemma-2-9b-it-dpo-eva
Here's how to solve this problem:
                                       Here's how to solve this problem:
1. Understand the first statement:
                                       1. Understand the first statement:
                                       - "When a number is divided by 10,
* "When a number is divided by 10,
the remainder is 4" means the number
                                       the remainder is 4" means the number
can be represented as 10 * k + 4,
                                       can be represented as 10 * k + 4,
where k is an integer.
                                       where k is an integer.
2. Double the number:
                                       2. Double the number:
* Twice the number is 2*(10*k + 4) =
                                       - Twice the number is 2*(10*k + 4) =
20*k + 8
                                       20*k + 8
3. Divide by 4:
                                       3. Divide by 4:
* (20*k + 8) divided by 4 is (20*k)/4
                                       - When (20*k + 8) is divided by 4,
                                        the 20*k term is perfectly divisible
+ 8/4 = 5 * k + 2
                                       by 4.
4. Find the remainder:
* Since 5*k is a multiple of 4, the
                                       - The remainder will be the same as
remainder when twice the number is
                                       the remainder when 8 is divided by 4,
divided by 4 is 2.
                                       which is 0.
Let me know if you'd like to try
                                       Therefore, the remainder when twice
another example!
                                       the number is divided by 4 is 0.
```

2nd-turn prompt: What about when twice the number is divided by 5?

```
Answer from gemma-2-9b-it-dpo
Here's how to solve that:

1. We know: Twice the number
is 20*k + 8 (from the previous
calculation).

2. Divide by 5: (20*k + 8) divided
by 5 is (20*k)/5 + 8/5 = 4*k + 1.6

3. Find the remainder: Since 4*k
is a multiple of 5, the remainder
when twice the number is divided by
5 is 1.
Let me know if you have any more
```

Answer from gemma-2-9b-it-dpo-eva

Here's how to solve that:

1. Twice the number: We know twice the number is 20*k + 8 (from the previous steps).

2. Divide by 5:

* 20*k is divisible by 5.

* 8 divided by 5 leaves a remainder of 3.

Therefore, the remainder when twice the number is divided by 5 is 3.

number theory puzzles!

Judgment (by gpt-4)

Judgment for gemma-2-9b-it-dpo

The assistant's response is incorrect. The assistant incorrectly calculated the remainder when twice the number is divided by 5. The assistant calculated the decimal part of the division operation, not the remainder. The correct calculation should be (20n + 8) % 5 = (20n % 5) + (8 % 5) = 0 + 3 = 3. Therefore, the remainder when twice the number is divided by 5 is 3, not 1 as the assistant stated.

is 20*k + 8 (from the previous calculation). 2. Divide by 5: (20*k + 8) divided by 5 gives us a remainder of (20*k % 5) + (8 % 5) = 0 + 3 = 3. 3. Find the remainder: The remainder when twice the number is

The corrected response would be:

1. We know: Twice the number

divided by 5 is 3.

Rating: [[3]], "score": 3, "turn": 2, "tstamp": 1722737011.7768948

Judgment for gemma-2-9b-it-dpo-eva

The assistant's answer is correct and matches the reference answer. The assistant correctly explains that twice the number is 20*k + 8 and that when this is divided by 5, the remainder is 3. The assistant's explanation is clear and easy to understand, making it helpful for the user. There are no mistakes to correct.

Rating: [[10]], "score": 10, "turn": 2, "tstamp": 1722846518.5543818

Table 10: Comparison of model generations on examples from MT-Bench.

Answer from gemma-2-9b-it-dpo

Smartphone Showdown: [Model A] vs. [Model B] $\n\cdot$ n**I. Introduction** $\n\cdot$ * Briefly introduce the two smartphone models being compared, highlighting their popularity and target audience.\n* State the purpose of the comparison: to help readers decide which phone best suits their needs.\n\n**II. Design and Display **\n* Physical dimensions, weight, and build quality comparison. $\n \star$ Screen size, resolution, and display technology (e.g., OLED, LCD). $\n*$ Design aesthetics and user preferences.\n\n**III. Performance and Specs** $\n*$ Processor, RAM, and storage comparison.\n* Benchmark scores and real-world performance analysis.\n* Battery life and charging capabilities. $\n\n**IV$. Camera Capabilities**\n* Rear and front camera specs (megapixels, aperture, features).\n* Image quality comparison in various lighting conditions.\n* Video recording capabilities. $\n\$ n**V. Software and User Experience**\n* Operating system and user interface comparison.\n* App ecosystem and availability.\n* Software features and customization options.\n\n**VI. Price and ${\tt Value**} \backslash n \star \ {\tt Compare} \ {\tt the} \ {\tt price} \ {\tt points} \ {\tt of} \ {\tt both}$ models. $\n*$ Analyze the value proposition based on features and performance. $\n\n**VII$. Conclusion**\n* Summarize the key differences and similarities.\n* Recommend the best phone for specific user profiles (e.g., budget-conscious, photography enthusiasts, gamers).

Answer from gemma-2-9b-it-dpo-eva

iPhone 14 Pro vs. Samsung Galaxy S23: Which Flagship Reigns Supreme? $\n\$ n**I. Introduction **\n* Briefly introduce both smartphones and their position in the market.\n* State the purpose of the comparison: to help readers decide which phone best suits their needs. $\n\$ n**II. Design and Display** $\n*$ Physical dimensions, weight, and build quality comparison.\n* Screen size, resolution, refresh rate, and display technology (OLED vs. Super AMOLED).\n* Design aesthetics and unique features (e.g., notch vs. punch-hole, color options). $\n\$ n**III. Performance and Camera**\n* Processor comparison (Apple A16 Bionic vs. Snapdragon 8 Gen 2).\n* RAM and storage options.\n* Camera specs: megapixels, lens types, aperture, and special features (e.g., telephoto, macro). $\n*$ Image quality comparison based on sample photos and user reviews.\n\n**IV. Software and User Experience**\n* Operating systems: iOS 16 vs. Android 13.\n* User interface comparison: intuitiveness, customization options, and app ecosystems.\n* Special features: Face ID vs. in-display fingerprint sensor, voice assistants. $\n\n**V$. Battery Life and Charging** $\n*$ Battery capacity and real-world usage comparison.\n* Fast charging speeds and wireless charging capabilities.\n\n**VI. Price and Value ** \n * Compare starting prices and different storage configurations.\n* Assess the overall value for money based on features and performance.\n\n**VII. Conclusion**\n* Summarize the key differences and strengths of each phone.\n* Recommend the best phone for specific user types (e.g., photography enthusiasts, gamers, budget-conscious consumers).

 $2nd\mbox{-turn prompt:}$ Take your previous response and rephrase it as a limerick.

Answer from gemma-2-9b-it-dpo

Two phones, a showdown so grand, \n[Model A] and [Model B], hand in hand.\nDesign, specs, and price,\nWe'll analyze nice,\nTo help you choose, understand?\n\nLet me know if you'd like me to try filling in the bracketed parts with specific model names!

Answer from gemma-2-9b-it-dpo-eva

\nTwo phones, a Pro and a Galaxy,\nFor flagships, they truly are spacy.\nWith cameras and screens,\nAnd processors keen,\nWhich one wins? Read on, and be savvy! \nLet me know if you'd like another limerick!

Judgment (by gpt-4)

Judgment for gemma-2-9b-it-dpo

The assistant's response is creative and relevant to the user's request. The user asked the assistant to rephrase the previous response, which was a detailed outline for a blog post, into a limerick. The assistant successfully did so, maintaining the essence of the original response in a limerick format. The assistant also offered to further customize the limerick by filling in the bracketed parts with specific model names, showing a willingness to provide additional detail if needed. However, the limerick does not fully capture the depth and detail of the original response, which is understandable given the constraints of the limerick format.

Rating: [[8]], "score": 8, "turn": 2, "tstamp": 1722737024.0327556

Judgment for gemma-2-9b-it-dpo-eva

The assistant's response is creative and relevant to the user's request. The assistant successfully rephrased the previous response, which was a detailed outline for a blog post comparing two smartphone models, into a limerick. The limerick is playful and engaging, and it maintains the essence of the original response, which is to compare the two phones and help the reader make an informed decision. The assistant also offers to create another limerick if the user wants, showing a willingness to continue the interaction.

Rating: [[9]], "score": 9, "turn": 2, "tstamp": 1722846542.9437995

Table 11: (Continued) comparison of model generations on examples from MT-Bench.

1st-turn prompt: Each problem consists of three statements. Based on the first two statements, the third statement may be true, false, or uncertain.\n1. Oranges cost more than apples.\n2. Oranges cost less than bananas.\n3. Bananas cost more than apples and bananas cost more than orange.\nIf the first two statements are true, then the third statement is?

Answer from gemma-2-9b-it-dpo

Here's how to break down the logic:\n\n*

Statement 1: Oranges > Apples (Oranges
cost more than apples)\n* **Statement
2:** Oranges < Bananas (Oranges cost less
than bananas)\n\nThis means the price
order is: Bananas > Oranges > Apples\n\n*

Statement 3: Bananas > Apples AND Bananas
> Oranges\n\nStatement 3 is **partially
true**.\n\n* The part "Bananas > Apples" is
true based on our price order.\n* The part
"Bananas > Oranges" is also true based on our
price order.\n\n\nLet me know if you'd like to
try another one!

Answer from gemma-2-9b-it-dpo-eva

Here's how to break down the logic:\n\n*
Statement 1: Oranges > Apples (Oranges
cost more than apples)\n* **Statement 2:**
Oranges < Bananas (Oranges cost less than
bananas)\n\nThese statements tell us that
bananas are the most expensive, then oranges,
and apples are the least expensive.\n\n*
Statement 3: Bananas > Apples AND Bananas
> Oranges\n\nSince bananas are indeed more
expensive than both apples and oranges,
statement 3 is **true**.\n\n\nLet me know
if you'd like to try another one!

Answer from gemma-2-9b-it-dpo

If the third statement is true, the first statement is **false**.\n\nHere's why:\n\n*
Statement 3: States that bananas cost more than both apples AND oranges.\n\nThis means the price order is: Bananas > Oranges
> Apples.\n\n* **Statement 1:** States that oranges cost more than apples.\n\nIf bananas are the most expensive, and oranges are second, then oranges cannot be more expensive than apples.\n\n\nLet me know if you have any other logic puzzles!

Answer from gemma-2-9b-it-dpo-eva

If the third statement is true, then the first statement is **uncertain**.\n\nHere's why:\n\n*
Statement 3: Bananas > Apples AND Bananas >
Oranges\n\nThis tells us bananas are the most expensive, but it doesn't explicitly state the relative prices of apples and oranges.\n\n*
Statement 1: Oranges > Apples\n\nThis statement claims oranges are more expensive than apples.\n\nStatement 3 doesn't contradict statement 1, but it also doesn't confirm it.
It's possible that oranges *are* more expensive than apples, but statement 3 alone doesn't give us enough information to be sure.

Judgment (by gpt-4)

Judgment for gemma-2-9b-it-dpo

The assistant's response is incorrect. The assistant states that if the third statement is true, the first statement is false. However, the third statement only establishes that bananas cost more than both apples and oranges. It does not provide information about the relative costs of apples and oranges. Therefore, the first statement could be true (if oranges cost more than apples), false (if oranges cost less than apples), or uncertain (if oranges and apples cost the same). The assistant's explanation is flawed because it incorrectly assumes that the order of costs must be Bananas > Oranges > Apples, when in fact the order could also be Bananas > Apples = Oranges or Bananas > Apples > Oranges. \n\nCorrected Assistant's Answer: If the third statement is true, then bananas cost more than apples and bananas cost more than oranges. This means that oranges could still cost more than apples, making the first statement true. However, it's also possible that oranges and apples have the same cost, which would make the first statement false. Therefore, based on the third statement alone, the first statement is

Rating: [[2]], "score": 2, "turn": 2, "tstamp": 1722737017.2808955

Judgment for gemma-2-9b-it-dpo-eva

The assistant's response is correct and helpful. The assistant explains that the first statement is uncertain if the third statement is true. which aligns with the reference answer. The assistant provides a clear explanation of why this is the case, stating that the third statement doesn't contradict the first statement, but it also doesn't confirm it. Therefore, the assistant's response is accurate and informative. \n\nThe assistant's response: "If the third statement is true, then the first statement is **uncertain**. Here's why: Statement 3: Bananas > Apples AND Bananas > Oranges. This tells us bananas are the most expensive, but it doesn't explicitly state the relative prices of apples and oranges. Statement 1: Oranges > Apples. This statement claims oranges are more expensive than apples. Statement 3 doesn't contradict statement 1, but it also doesn't confirm it. It's possible that oranges *are* more expensive than apples, but statement 3 alone doesn't give us enough information to be sure.

Rating: [[10]], "score": 10, "turn": 2, "tstamp": 1722846527.2339694

Table 12: (Continued) comparison of model generations on examples from MT-Bench.

1st-turn prompt: Implement a function to find the median of two sorted arrays of different sizes with O(1) space complexity and O(n) time complexity.

Answer from gemma-2-9b-it-dp

python\n\def find_median_sorted_arrays(nums1, nums2):\n """\n Finds the median of two sorted arrays of different sizes. $\n\$ Args:\n nums1: The first sorted array.\n nums2: The second sorted array.\n\n Returns:\n The median of the two sorted arrays.\n """\n\n m, n = len(nums1), len(nums2)\n if m > n:\n nums1, nums2, m, n = nums2, nums1, n, m # Ensure m <- $n\n$ imin, imax, half-len = 0, m, (m + n + 1) // $2\n$ while $imin \leftarrow imax: \ i = (imin + imax) // 2 \ j = half_len$ - i\n if i < m and nums2[j - 1] > nums1[i]:\n imin = i + 1 # i is too small, increase it\n elif i > 0 and nums1[i - 1] > # i is perfect\n\n if i == 0:\n max_left = nums2[j - 1]\n elif i == 0:\n max_left = nums1(i - 1)\n else:\n max_left = $max(nums1[i - 1], nums2[j - 1]) \n if (m + n) % 2 == 1:\n$ return max_left\n\n if i -- m:\n min_right - nums2[j]\n elif j -- n:\n min_right - nums1[i]\n else:\n min_right min(nums1[i], nums2[j])\n\n return (max_left + min_right) / 2.0\n\n# Example usage\nnums1 = [1, 3]\nnums2 = [2]\nmedian = find_median_sorted_arrays(nums1, nums2)\nprint(f"The median of {nums1} and {nums2} is: {median}")\n\n\n**Explanation:**\n\n1 **Handle Unequal Lengths:** \n - If 'nums1' is longer than 'nums2', swap them to ensure 'nums1' is always the shorter array. This simplifies the logic.\n\n2. **Binary Search:**\n - The core idea is to use binary search on the shorter array ('nums1').\n - 'imin' and 'imax' define the search range for the partition point 'i' in 'numsl'.\n - 'half-len' calculates the desired total number of elements on the left side of the partition (to find the median).\n\n3. **Partitioning:**\n - In each iteration, 'i' divides 'nums1' into two parts: 'nums1[0:i]' the total number of elements on the left side is 'half-len'.\n\n4. **Adjusting the Partition: **\n - We compare elements at the boundaries of the partitions to see if 'i' is in the correct position: $\n - If 'nums2[j-1] > nums1[i]', 'i' is too small,$ so we move 'imin' to 'i + 1'.\n - If 'nums1 $\{i - 1\}$ > nums2 $\{j\}$ ', 'i' is too large, so we move 'imax' to 'i - 1'.\n\n5. **Finding the Median: **\n - Once 'i' is in the correct position, we find:\n - 'max_left': The maximum element in the left partitions of both arrays.\n - 'min_right': The minimum element in the right partitions of both arrays. \n - If the total length is odd, 'max_left' is the median.\n - If the total length is even, the median is the average of 'max_left' and 'min_right'.\n\n**Time Complexity: ** O(log(min(m, n))) because we perform binary search on the shorter array. $\n\$ use a constant amount of extra space for variables.

Answer from gemma-2-9b-it-dpo-ev

python\n\def find.median.sorted.arrays(nums1, nums2):\n """\n Finds the median of two sorted arrays of different sizes.\n\n Args:\n nums1: The first sorted array.\n nums2: The second sorted array.\n\n Returns:\n The median of the two sorted arrays. \n """ \n n m, n = len(nums1), len(nums2) \n if m > n:\n nums1, nums2, m, n = nums2, nums1, n, m # Ensure m <- n\n\n imin, imax, half_len = 0, m, (m + n + 1) // $2\n$ while imin <= imax: \n i = (imin + imax) // $2\n$ j = half-len - i\n if i < m and nums2[j - 1] > nums1[i]:\n imin = i + 1 # i is too small, increase it \n elif i > 0 and numsl[i - 1] > nums2[j]:\n imax = i - 1 # i is too big, decrease it\n else:\n # i is perfect\n\n if i == 0:\n max_left = nums2[j - 1]\n elif j == 0: \n max_left = nums1[i - 1] \n else: \n max_left - max(nums1[i - 1], nums2[j - 1])\n\n if (m + n) % 2 --1:\n return max_left\n\n if i == m:\n min_right = nums2[j]\n elif j -- n:\n min_right - nums1{i}\n else:\n min_right min(nums1[i], nums2[j])\n\n return (max_left + min_right) 2.0\n\n# Example usage\nnums1 = [1, 3]\nnums2 = [2]\nmedian = find_median_sorted_arrays(nums1, nums2)\nprint(f"The median of {nums1} and {nums2} is: {median}")\n\n**Explanation:**\n\n1. **Handle Unequal Lengths:**\n - If 'nums1' is longer than 'nums2', swap them to ensure 'nums1' is always the shorter array. This simplifies the logic.\n\n2. **Binary Search:**\n - The core idea is to use binary search on the shorter array ('nums1').\n - 'imin' and 'imax' define the search range for the partition point 'i' in 'nums1'.\n - 'half_len' calculates the desired total number of elements on the left side of the partition (to find the median).\n\n3. **Partitioning:**\n - In each iteration, 'i' divides 'nums1', and 'j' divides 'nums2' such that the total number of elements on the left side is 'half len' \n\n4 **Adjusting the Search Range:** \n - If 'nums2[j - 1] > nums1[i]', it means 'i' is too small, so we need to move the partition point in 'nums1' to the right ('imin = i + 1').\n - If 'nums1[i - 1) > nums2[1]', 'i' is too large, so we move it to the left ('imax = i - 1').\n\n5. **Finding the Median:**\n - When the correct partition is found ('i' is in the right position), we find:\n - 'max_left': The maximum element on the left side of the partition.\n - 'min_right': The minimum element on the right side of the partition.\n - If the total number of elements is odd, 'max_left' is the median.\n - If even, the median is the average of 'max_left' and 'min_right'.\n\n**Time Complexity:** $O(\log(\min(m, n)))$ because we are performing binary search on the shorter array.\n\n**Space Complexity:** O(1) as we are only using a constant amount of extra space for variables.

Judgment (by gpt-4)

Judgment for gemma-2-9b-it-dpo

The assistant's answer is correct and provides a detailed explanation of the code. The assistant correctly states that the time complexity is O(log(min(m, n))) and the space complexity is O(l), which aligns with the reference answer. The assistant also provides an example usage of the function, which is helpful for understanding how to use it. The assistant's code is a different implementation than the reference answer, but it achieves the same result and meets the same complexity requirements. However, the assistant's answer does not address the user's original question about achieving O(n) time complexity. The assistant should have clarified that it's not possible to find the median of two sorted arrays of different sizes with O(1) space complexity and O(n) time complexity, as stated in the reference answer.

Rating: [[8]], "score": 8, "turn": 1, "tstamp":

Judgment for gemma-2-9b-it-dpo-eva

The assistant's answer is correct and provides a detailed explanation of the code. The assistant correctly states that the time complexity is $O(\log(\min(m, n)))$ and the space complexity is O(1), which aligns with the reference answer. The assistant also provides a step-by-step explanation of the code, which is very helpful for understanding the logic behind the solution. The assistant's code is also correct and will correctly find the median of two sorted arrays of different sizes. Therefore, there are no corrections needed for the assistant's response.

Rating: [[10]], "score": 10, "turn": 1, "tstamp": 1722846533.772981

Table 13: (Continued) comparison of model generations on examples from MT-Bench.

1st-turn prompt: You are given two sorted lists of size m and n. Implement a function to find the kth smallest element in the union of the two lists with linear complexity.

Answer from gemma-2-9b-it-dpo

""python\n\def find_kth_smallest(list1, list2, k):\n """ $\backslash n$ Finds the kth smallest element in the union of two sorted lists.\n\n Args:\n list1: The first sorted list.\n list2: The second sorted list.\n k: The desired kth smallest element. $\n\$ The kth smallest element in the union of the two lists. \n """ \n \n m, n = len(list1), len(list2) \n i, j = 0, 0 $n = n_n = [] n\n # Build a min-heap$ with the first elements of both lists $\ensuremath{\backslash} n$ for x in $range (min (m, n)): \\ \ \ \, heapq.heappush (min_heap, (list1[x],$ x, 0)) # (value, list_index, position_in_list)\n heapq.heappush(min_heap, (list2[x], x, 1))\n\n # Extract k smallest elements from the heap\n for \cdot in range $(k - 1): n _, _, _ = heapq.heappop(min_heap) n #$ The top element of the heap is the kth smallest \n return heapq.heappop(min_heap)[0]\n\n# Example usage:\nlist1 = [2, 5, 8, 12]\nlist2 = [1, 3, 7, 9,101\nk = 5\nkth_smallest = find_kth_smallest(list1. list2, k)\nprint(f"The $\{k\}$ th smallest element is: $\{kth_smallest\}$ ") $\n\n\n**Explanation:**\\\n\n1.$ **Initialization: **\n - 'm' and 'n' store the lengths of the input lists.\n - 'i' and 'j' are pointers to track the current position in each list. \n 'min_heap' is a min-heap used to efficiently store and retrieve the smallest elements encountered so far.\n\n2. **Building the Min-Heap:**\n - The code iterates through the first 'min(m, n)' elements of both lists.\n - For each element, a tuple '(value, list_index, position_in_list) ' is pushed onto the 'min_heap'. This tuple helps us keep track of the element's value, the list it belongs to, and its original position. $\n\n3$. **Extracting k-1 Smallest Elements:** \n - The 'for' loop runs 'k -1' times, effectively extracting the 'k-1' smallest elements from the 'min_heap'.\n\n4. **Finding the kth Smallest: **\n - After the loop, the top element of the 'min_heap' contains the 'k'th smallest element.\n - 'heapq.heappop (min_heap) ' removes and returns this element. $\n\n**Time$ Complexity:** $\n\n-$ Building the min-heap: O(m + n)\n- Extracting k-1 elements: O(k * log(k)) n- Overall: **O(m + n + k * log(k))**, whichis approximately **O(m + n) ** since 'k' is usually much smaller than 'm + n'.\n\n\nLet me know if you have any other questions!

Answer from gemma-2-9b-it-dpo-eva

'''python\n\def find_kth_smallest(list1, list2, k):\n """\n Finds the kth smallest element in the union of two sorted lists. $\n\$ Args: \n list1: The first sorted list.\n list2: The second sorted list.\n k: The desired rank of the smallest element. $\n\$ Returns:\n The kth smallest element in the union of the lists. $\n """\n\n i = 0 # Index for list1<math>\n i =$ 0 # Index for list2n merged = [] # Store the merged elements $\n\$ n while i < len(list1) and j < len(list2): \n if list1[i] <= list2[j]:\n merged.append(list1[i])\n i += 1\n else:\n merged.append(list2[i])\n i += $1\n$ # Add any remaining elements from list1\n while i < len(list1): \n merged.append(list1[i]) \n i += $1\n\$ # Add any remaining elements from list $2\n$ while j < len(list2):\n merged.append(list2[j])\n $j += 1 \n \n$ return merged[k - 1] # Return the kth element (index k-1)n# Example usage:nlist1 = $[2, 5, 8, 12] \ln 1 = [1, 3, 7, 9, 10] \ln k$ = 5\n\nkth_smallest = find_kth_smallest(list1, list2, k)\nprint(f"The {k}th smallest element is: $\{kth_smallest\}$ ") $\\n\\n**Explanation:**\\n\\n1$. **Initialization:** $\n - \i'$ and 'j' are index pointers for 'list1' and 'list2' respectively, starting at 0.\n - 'merged' is an empty list to store the merged sorted elements.\n\n2. **Merging:**\n - The 'while' loop continues as long as both 'i' and 'j' are within the bounds of their respective lists. $\n -$ In each iteration, it compares the elements at 'list1[i] and 'list2[j]'.\n - The smaller element is appended to 'merged', and the corresponding index ('i' or 'j') is incremented.\n\n3. **Adding Remaining Elements:**\n - After one list is exhausted, the remaining elements from the other list are directly appended to 'merged'.\n\n4. **Returning the kth Element: **\n - Finally, 'merged[k - 1]' is returned. which represents the kth smallest element in the union (remember that list indices start from 0).\n\n**Linear Complexity:** \n^n The algorithm iterates through each element in both lists at most once during the merging process. \n - The time complexity is therefore O(m + n), which is linear in the total number of elements (m + n), making it efficient for large lists.

Judgment (by gpt-4)

Judgment for gemma-2-9b-it-dpo

The assistant's answer is incorrect. The user asked for a solution with linear complexity, but the assistant provided a solution with a time complexity of $O(m+n+k+\log(k))$, which is not linear. The assistant's solution uses a min-heap, which is not necessary and adds unnecessary complexity to the solution.

Rating: [[2]], "score": 2, "turn": 1, "tstamp": 1722737030.6411152

Judgment for gemma-2-9b-it-dpo-eva

The assistant's answer is correct and helpful. It provides a Python function that implements the two-pointer approach to find the kth smallest element in the union of two sorted lists. The assistant's function is slightly different from the reference, but it achieves the same goal. The assistant's function merges the two lists into a new list and then returns the kth element from the merged list. The assistant also provides a detailed explanation of how the function works and confirms that the time complexity is linear, which is what the user asked for. However, the assistant's function uses extra space to store the merged list, which is not necessary and not as efficient as the reference.

Rating: [[8]], "score": 8, "turn": 1, "tstamp": 1722846543.867601

Table 14: (Continued) comparison of model generations on examples from MT-Bench.

2nd-turn prompt: Does there exist an algorithm with better time complexity? If so, implement it.

Answer from gemma-2-9b-it-dpg

with a time complexity of **O(m + n)** without using a heap.\n\nHere's the implementation:\n\npython\n\def find_kth_smallest_optimized(list1, list2, k):\n """\n Finds the kth smallest element in the union of two sorted lists\n with O(m + n) time complexity. $\n\n$ Args: \n list1: The first sorted list.\n list2: The second sorted list.\n k: The desired kth smallest element.\n\n Returns:\n The kth smallest element in the union of the two lists. $\n """ \n m, n = len(list1), len(list2) \n i,$ j = 0, $0 \le result = [] \le m \le merge the lists while keeping track$ of the kth smallest \n while len(result) < k: \n if i < m and j < $n:\n$ if $list1[i] \leftarrow list2[j]:\n$ result.append(list1[i])\n $i \leftarrow 1 \ n = 1 \ n = 1 \ n = 1 \ n = 1 \ n = 1 \ n$ elif i < m:\n result.append(list1[i])\n i += 1\n else:\n result.append(list2[j]) $\n j += 1\n\n return result[k - 1]\\\n\n\#$ Example usage: nlist1 = [2, 5, 8, 12] nlist2 = [1, 3, 7, 9, 12]10]\nk = 5\nkth_smallest = find_kth_smallest_optimized(list1, list2, k) \n the {k}th smallest elem is: $\{kth_smallest\}$ ") $\n\n\n**Explanation:**\n\n1$. **Initialization:**\n - 'm' and 'n' store the lengths of the lists.\n - 'i' and 'j' are pointers for 'list1' and 'list2', respectively. \n - 'result' is a list to store the merged and sorted elements. $\n\n^2$. **Merging and Tracking:** \n - The 'while loop continues until 'k' elements are in the 'result' list.\n -In each iteration, it compares the current elements from 'list1' and 'list2'.\n - The smaller element is appended to 'result'. and the corresponding pointer ('i' or 'j') is incremented.\n other list are appended to 'result'.\n\n3. **Returning the kth Smallest:**\n - Finally, 'result[k - 1]' contains the 'k'th smallest element. $\n\n**Time Complexity:**\n\n- The algorithm$ iterates through both lists once, resulting in a time complexity questions!

You are absolutely right! There's a more efficient algorithm

Answer from gemma-2-9b-it-dpo-eva

You are right to ask! While the previous algorithm has linear time complexity, we can achieve an even better solution with **O(log(min(m, n))) ** time complexity using a slightly more sophisticated approach.\n\nThe key idea is to leverage the sorted nature of the lists and use a **binary search*: find_kth_smallest_optimized(list1, list2, k): \n """ \n Finds the kth smallest element in the union of two sorted lists with $O(\log(\min(m, n)))$ time complexity. $\n\$ Args: \n list1: The first sorted list.\n list2: The second sorted list.\n k: The desired rank of the smallest element. $\n\n$ Returns: \n The kth smallest element in the union of the lists.\n """\n m, n = len(list1), len(list2)\n if m > n:\n list1, list2, m, n = list2, list1, n, m # Ensure list1 is the shorter one\n\n left, right - 0, m\n while left <- right:\n partitionX - (left + right) // $2\n partitionY = k - partitionX\n\n maxLeftX = list1[partitionX]$ - 1] if partitionX > 0 else float('-inf') \n minRightX = list1[partitionX] if partitionX < m else float('inf')\n\n maxLeftY = list2[partitionY - 1] if partitionY > 0 else $\verb|float('-inf') \n minRightY = list2[partitionY] if partitionY|$ < n else float('inf') $\n\$ if maxLeftX <= minRightY and maxLeftY <= minRightX:\n if partitionX == 0:\n return list2[partitionY - 1]\n elif partitionY -- 0:\n return list1[partitionX - 1]\n else:\n return max(list1[partitionX - 1], list2[partitionY - 1])\n elif maxLeftX > minRightY:\n right = partitionX - 1 # Too many elements on the right side of list1\n else:\n left = partitionX + 1 # Too many elements on the right side of list2\n\n\n**Explanation:**\n\n1. **Shorten Lists:** If 'list1' is longer than 'list2', swap them to ensure 'list1' is alway the shorter one. This simplifies the logic. $\n\n2$. **Binary Search: **\n - 'left' and 'right' pointers define the search space within 'list1'. \n - 'partitionX' is the middle point in 'list1'. and 'partitionY' is calculated to divide the remaining elements in 'list2' such that 'partitionX + partitionY = k'.\n - 'maxLeftX', 'minRightX', 'maxLeftY', and 'minRightY' represent the largest element to the left and smallest element to the right of the partitions in both lists.\n\n3. **Comparison and Adjustment:**\n - If the 'maxLeftX' is less than or equal to 'minRightY' and smallest element lies within the current partitions. We return the larger of 'maxLeftX' and 'maxLeftY'.\n - If 'maxLeftX' is greater than 'minRighty', it indicates that we need to search in the left subarray of 'listl' (i.e., decrease 'right'). \n Otherwise, we search in the right subarray of 'list1' (i.e., increase 'left').\n\n4. **Termination:** The binary search continues until 'left' crosses 'right', indicating the correct partition has been found.\n\n**Time Complexity:**\n\n- The binary search divides the search space in half at each step.\n-Therefore, the time complexity is O(log(min(m, n))), which is significantly faster than linear time for large lists where on list is much smaller than the other.

Judgment (by gpt-4)

Judgment for gemma-2-9b-it-dpc

The assistant's first response to the user's question is incorrect. The user asked for a function to find the kth smallest element in the union of two sorted lists with linear complexity. The assistant provided a function that uses a min-beap, which has a time complexity of $O(m+n+k+\log(k))$. This is not linear complexity, as the user requested. The assistant's second response to the user's question is also incorrect. The user asked if there exists an algorithm with better time complexity than linear. The assistant provided a function that has a time complexity of O(m+n), which is linear, not better than linear. The assistant should have provided a function that uses a binary search approach, which has a time complexity of $O(\log(m) + \log(n))$, as the reference answer correctly does.

Rating: [[2]], "score": 2, "turn": 2, "tstamp": 1722737031.5033472

Judgment for gemma-2-9b-it-dpo-eva

The assistant's response is correct and helpful. The assistant provided a Python function that uses a binary search approach to find the kth smallest element in the union of two sorted lists. The assistant also provided a detailed explanation of how the function works, including the time complexity of the function. The assistant's answer matches the reference answer in terms of the algorithm used and the explanation provided. The assistant also correctly identified that the binary search approach has a better time complexity than the linear approach. However, the assistant's code has a minor issue. The assistant's code does not handle the case when 'k' is greater than the sum of the lengths of the two lists. In such a case, the code will raise an 'IndexError'. This can be fixed by adding a check at the beginning of the function to return 'None' if 'k' is greater than the sum of the lengths of the two lists.

Rating: [[9]], "score": 9, "turn": 2, "tstamp": 1722846556.6828268

Table 15: (Continued) comparison of model generations on examples from MT-Bench.

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