QP-SNN: QUANTIZED AND PRUNED SPIKING NEURAL NETWORKS

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Paper under double-blind review

ABSTRACT

Brain-inspired Spiking Neural Networks (SNNs) leverage sparse spikes to encode information and operate in an asynchronous event-driven manner, offering a highly energy-efficient paradigm for machine intelligence. However, the current SNN community focuses primarily on performance improvement by developing large-scale models, which limits the applicability of SNNs in resource-limited edge devices. In this paper, we propose a hardware-friendly and lightweight SNN, aimed at effectively deploying high-performance SNN in resource-limited scenarios. Specifically, we first develop a baseline model that integrates uniform quantization and structured pruning, called QP-SNN baseline. While this baseline significantly reduces storage demands and computational costs, it suffers from performance decline. To address this, we conduct an in-depth analysis of the challenges in quantization and pruning that lead to performance degradation and propose solutions to enhance the baseline's performance. For weight quantization, we propose a weight rescaling strategy that utilizes bit width more effectively to enhance the model's representation capability. For structured pruning, we propose a novel pruning criterion using the singular value of spatiotemporal spike activities to enable more accurate removal of redundant kernels. Extensive experiments demonstrate that integrating two proposed methods into the baseline allows QP-SNN to achieve state-of-the-art performance and efficiency, underscoring its potential for enhancing SNN deployment in edge intelligence computing.

1 Introduction

Inspired by the information processing paradigm of biological systems, Spiking Neural Networks (SNNs) encode information via binary spikes and process them in a sparse spike-driven manner (Gerstner & Kistler (2002); Izhikevich (2003)). paradigm simplifies the matrix computations of weight and spike activity in SNNs from computationally intensive multiplyaccumulate (MAC) operations to computationally efficient accumulate (AC) operations. Therefore, SNNs are regarded as a promising energy-efficient solution for achieving next-generation machine intelligence (Pfeiffer & Pfeil (2018); Roy et al. (2019b)). Furthermore, the energy efficiency of SNNs has driven the development of neuromorphic

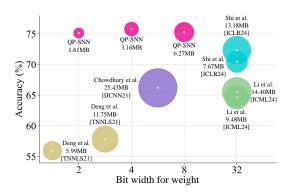


Figure 1: Comparison of accuracy and model size between our QP-SNN and related work on CIFAR-100. The bubble size represents the model size.

hardware, such as SpiNNaker (Painkras et al. (2013)), TrueNorth (Akopyan et al. (2015)), Loihi (Davies et al. (2018)), Tianjic (Pei et al. (2019)) etc. These neuromorphic hardware can fully exploit the energy efficiency potential of SNNs. Despite these advantages, the application scenarios and performance of SNNs still require improvement compared to artificial neural networks (ANNs).

In the past few years, the SNN community has focused primarily on designing complex SNNs architectures to achieve impressive performance across various application tasks, such as image clas-

sification (Yao et al. (2024b;a)), object detection (Kim et al. (2020); Luo et al. (2024)), and temporal modeling (Yin et al. (2024b); Zhang et al. (2024)). While these studies have yielded satisfactory performance, they typically come at the cost of large model parameters, high memory consumption, and increased computational complexity (Shi et al. (2024); Li et al. (2024)). This undermines the inherent energy efficiency of SNNs and restricts their applicability in resource-limited scenarios. To achieve effective deployment, a growing number of researchers have worked on compressing large-scale SNNs. Existing methods to improve SNN energy efficiency primarily fall into two categories: (1) reducing the precision of parameter representations (Deng et al. (2021); Yin et al. (2024a); Hu et al. (2024); Wei et al. (2024)) and (2) reducing redundant parameters within the model (Shi et al. (2024); Yan et al. (2024); Liu et al. (2024); Li et al. (2024)).

Quantization is a key technique for the first category, which reduces memory storage and computational complexity by storing full-precision values in low bit-width precision (Gholami et al. (2022)). Based on whether an equal-size interval is used to discretize full-precision values, it can be divided into non-uniform and uniform quantization (Rokh et al. (2023)). Non-uniform quantization divides discretization intervals unevenly, enabling a more precise capture of critical information and leading to improved performance. However, it is challenging to deploy this approach on general computing hardware efficiently (Cai et al. (2017); Kulkarni et al. (2022)). In contrast, uniform quantization maps full-precision values to equal-sized discrete intervals, offering advantages such as simplicity, low computational cost, and efficient mapping to hardware (Zhu et al. (2016); Jain et al. (2020)).

Pruning is one of the effective methods for reducing redundant parameters in a model, which reduces the model size by removing unimportant connections (Li et al. (2016)). Pruning can be classified into unstructured and structured pruning (Vadera & Ameen (2022)). Unstructured pruning removes individual nodes like a single neuron of networks, resulting in unstructured sparsity. This often leads to a high compression rate, but requires specialized hardware or library support for acceleration (Han et al. (2015)). In contrast, structured pruning removes entire convolutional filters, ensuring model's structure. This avoids complex sparse matrix operations, enabling acceleration with standard hardware by taking advantage of a highly efficient library (He & Xiao (2023); Xu et al. (2020)).

Real-world deployments are typically limited by size, weight, area, and power. This makes combined quantization and pruning a promising approach for maximizing SNN compression. Existing research on integrating quantization and pruning in SNNs faces two challenges. Firstly, they do not sufficiently account for hardware-friendliness, for example, (Rathi et al. (2018)) and (Deng et al. (2021)) adopt unstructured pruning. Secondly, despite significant energy efficiency, these studies suffer from severe performance degradation, with evaluations limited to simple datasets like MNIST (Rathi et al. (2018)) or CIFAR (Chowdhury et al. (2021); Deng et al. (2021)). Thus, integrating both techniques for maximal compression while ensuring hardware efficiency and high performance remains challenging. In this paper, we introduce the QP-SNN, a hardware-efficient and lightweight SNN tailored for effective deployment in resource-limited environments. We first build a QP-SNN baseline that integrates uniform quantization and structured pruning. While this baseline offers substantial efficiency gains, it suffers from reduced performance. To address this, we investigate the root causes of performance degradation in quantization and pruning, and propose solutions to enhance the QP-SNN baseline's performance. As shown in Figure 1, QP-SNN utilizing the proposed solutions achieves excellent accuracy and model size. We summarize our main contributions as,

- We first develop a hardware-efficient and lightweight QP-SNN baseline by integrating uniform quantization and structured pruning. This baseline significantly reduces storage and computational demands, but suffers from performance limitations.
- To improve performance through quantization, we reveal that the vanilla uniform quantization in the QP-SNN baseline constrains the model's representation capability due to inefficient bit-width utilization. To address this, we propose a weight rescaling strategy (ReScaW) that optimizes bit-width usage for improved representation.
- To further boost performance through pruning, we introduce a novel structured pruning criterion for the QP-SNN baseline that leverages the singular value of spatiotemporal spike activity (SVS). This SVS criterion provides greater robustness across varying input samples and allows more precise removal of redundant convolutional kernels.
- Extensive experiments show that integrating ReScaW-based quantization and the SVS-based criterion into the baseline allows QP-SNN to achieve state-of-the-art performance and efficiency, revealing its potential for advancing edge intelligence computing.

2 RELATED WORK

Quantization technique Early research on quantization in SNNs is primarily based on ANN-to-SNN conversion algorithms, where a quantized ANN is first trained and then converted into the corresponding quantized SNN version (Sorbaro et al. (2020); Roy et al. (2019a)). To mitigate the performance loss associated with the conversion, researchers have proposed many strategies, such as the utilization of activation penalty term (Sorbaro et al. (2020)) and the weight-threshold balancing method (Wang et al. (2020)). However, these quantized SNNs still experience significant performance degradation and long latency issues. To address these limitations, some studies have explored directly training quantized SNNs and introduced different strategies to enhance performance, such as alternating direction method of multipliers (Deng et al. (2021)), accuracy loss estimator (Pei et al. (2023)), and suitable activation function (Hu et al. (2024)). Despite performance improvement, the above studies fail to effectively leverage the allocated bit-width, resulting in the limited expressive capability of models. Therefore, there still remains significant room for performance improvement.

Pruning technique Existing research on pruning SNNs can be broadly divided into two groups. The first group is unstructured pruning. For example, (Yin et al. (2021)) use a magnitude-based method to remove insignificant weights, and (Shi et al. (2024)) propose a fine-grained pruning framework that integrates unstructured weight and neuron pruning to enhance SNN energy efficiency. Additionally, there are some biologically inspired unstructured pruning works (Bellec et al. (2017); Chen et al. (2022)). While these studies achieve great sparsity and performance, they lead to irregular memory access in forward propagation, requiring specialized hardware for acceleration. The second group is structured pruning that offers better hardware compatibility. (Chowdhury et al. (2021)) use principal component analysis on membrane potentials to evaluate channel correlations and eliminate redundant ones. However, it suffers from long latency and cannot handle neuromorphic datasets. Recently, (Li et al. (2024)) evaluate the importance of kernels based on spike activity, advancing the performance of pruned SNNs to a new level. However, this evaluation criterion exhibits high dependency on inputs and may not accurately reflect the importance of kernels.

Compression with joint quantization and pruning Several studies have explored combining quantization and pruning to maximize the compression of SNNs. First, (Rathi et al. (2018)) adopt the STDP learning rule and a predefined pruning threshold to remove insignificant connections, and then quantizes retained important weights. Then, (Chowdhury et al. (2021)) perform principal component analysis on membrane potentials for spatial pruning and gradually decreases the time step during training for temporal pruning. They also use post-training quantization to compress retained weights. Moreover, (Deng et al. (2021)) formulate pruning and quantization as a constraint optimization problem in supervised learning, and address it with the alternating direction method of multipliers. However, these existing studies combining quantization and pruning face two main problems. Firstly, the unstructured pruning methods in (Rathi et al. (2018)) and (Deng et al. (2021)) require specialized hardware for efficient acceleration. Secondly, (Rathi et al. (2018)) only evaluate their method on very simple datasets, and (Chowdhury et al. (2021)) and (Deng et al. (2021)) only extend their methods to CIFAR (88.6% and 87.84% accuracy on CIFAR-10 with 5, 3 bits respectively), leading to significant room for improvement in both performance and efficiency.

3 QUANTIZED AND PRUNED SNN BASELINE

In this section, we develop the QP-SNN baseline by combining uniform quantization and structured pruning. These two compression techniques are highly compatible with existing hardware accelerators, significantly improving the model's deployment efficiency.

Neuron model. We use the Leaky Integrate-and-Fire (LIF) model in our QP-SNN due to its high computational efficiency (Wu et al. (2018)). The membrane potential of LIF model is computed as,

$$\tilde{\mathbf{U}}^{l}[t] = \tau \mathbf{U}^{l}[t-1] + \mathbf{X}^{l}[t], \tag{1}$$

where $\mathbf{U}^{l}[t]$ represents the membrane potential of neurons in layer l at time t, τ is the constant leaky factor, and $\mathbf{X}^{l}[t] = \mathbf{W}^{l}\mathbf{S}^{l-1}[t]$ denotes the input current. Neurons integrate incoming signals and generates a binary spike (i.e., 0 or 1) when the membrane potential surpasses the firing threshold θ .

The spike generation function is described as,

$$\mathbf{S}^{l}[t] = \begin{cases} 1, & \text{if } \mathbf{U}^{l}[t] \ge \theta, \\ 0, & \text{otherwise.} \end{cases}$$
 (2)

After spike emission, we use the hard reset mechanism to update the membrane potential. This mechanism resets membrane potential to zero when a spike occurs and remains inactive otherwise.

$$\mathbf{U}^{l}[t] = \tilde{\mathbf{U}}^{l}[t] \cdot (1 - \mathbf{S}^{l}[t]). \tag{3}$$

Vanilla uniform quantization. Quantization can be grouped into non-uniform and uniform quantization. Non-uniform quantization exhibits superior performance, but requires specialized hardware support. In contrast, uniform quantization maps weights to integer grids with equal size, simplifying both computational complexity and hardware implementation (Zhu et al. (2016)). In this study, we explore the uniform quantization in QP-SNNs. The vanilla uniform quantization for weights in layer l, i.e., \mathbf{W}^l , can be formulated as follows,

$$\mathbf{W}_{int}^{l} = \left\lceil \frac{s(b)}{2} \cdot \left(\text{clamp}(\mathbf{W}^{l}; -1, 1) + z \right) \right\rceil, \tag{4}$$

where $\operatorname{clamp}(\cdot)$ is a clipping operator, $\lceil \cdot \rfloor$ is a rounding operator, z is the zero-point, b is the bit width, and $s(b) = 2^b - 1$ is the number of integer grids. We set z to 1 and explore bit widths b of 8, 4, 2. Therefore, Eq.(4) maps \mathbf{W}^l onto the unsigned integer grid $\{0, \cdots, 2^b - 1\}$. To reconstruct \mathbf{W}^l through their quantized counterparts, the de-quantization is defined as,

$$\hat{\mathbf{W}}^l = 2 \cdot \frac{\mathbf{W}_{int}^l}{s(b)} - z. \tag{5}$$

Consequently, the general definition for the quantization used in the QP-SNN baseline is stated as,

$$\mathbf{W}^{l} \approx \hat{\mathbf{W}}^{l} = \frac{2}{s(b)} \left\lceil \frac{s(b)}{2} \cdot \left(\text{clamp}(\mathbf{W}^{l}; -1, 1) + z \right) \right\rceil - z. \tag{6}$$

The vanilla quantization greatly reduces the baseline's storage and computation demands, but suffers from the limited weight precision. This constrains the model's representation capability, reducing performance. In the next section, we resolve this issue by effectively using the assigned bit-width.

Structured pruning. Pruning can be classified as unstructured and structured pruning. Unstructured pruning enables high sparsity and excellent performance but requires specialized design for hardware acceleration. In contrast, structured pruning preserves the model's structure and is highly compatible with existing hardware accelerators. Currently, the most advanced structured pruning method in SNN is presented by (Li et al. (2024)). They prune convolutional kernels according to the spiking channel activity (SCA) criterion. We use this criterion in our QP-SNN baseline for the following analysis and comparison. For the weight tensor $\mathbf{W}^l \in \mathbb{R}^{c_l \times c_{l-1} \times k \times k}$, the SCA-based criterion evaluates and prunes kernels based on the magnitude of membrane potential. The importance evaluation for the f-th kernel, i.e., $\mathbf{W}^{l,f} \in \mathbb{R}^{c_{l-1} \times k \times k}$, is defined as,

$$Score(\mathbf{W}^{l,f}) = \frac{1}{B \cdot T} \cdot \left(\sum_{k=1}^{B} \sum_{t=1}^{T} \left\| \tilde{\mathbf{U}}^{l,f}[t] \right\| \right), \tag{7}$$

where B is the number of samples per mini-batch, T is the time step, $\|\cdot\|$ is the L1-norm, and $\tilde{\mathbf{U}}^{l,f}[t]$ is the membrane potential of the f-th feature map. As shown in Eq.(7), the SCA-based criterion regards positive values in $\tilde{\mathbf{U}}^{l,f}$ as excitatory postsynaptic potentials and negative values as inhibitory postsynaptic potentials, thus removing kernels that contribute less to the membrane potential. By unifying the SCA-based criterion, the number of parameter and computation in baseline is further reduced. Noteworthy, the performance of the pruned QP-SNN baseline model relies strongly on the scoring function. Therefore, the idea $\mathrm{Score}(\mathbf{W})^{l,f}$ should accurately identify the important kernels.

4 Method

To enhance the performance of the QP-SNN baseline, we analyze and resolve the underlying issues in quantization and pruning that cause performance reduction. In quantization, we reveal that the baseline suffers from limited representation capability due to inefficient bit-width utilization, and propose the weight rescaling strategy to use bit-width more effectively. In pruning, we propose a novel pruning criterion for the QP-SNN baseline to more accurately remove redundant kernels.

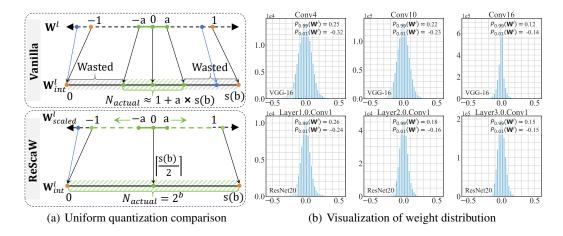


Figure 2: (a) Vanilla uniform quantization exhibits inefficient bit-width utilization, while ReScaW-based quantization can fully leverage the allocated bit-width. Green dots represent normal weights within the 1st and 99th percentiles, orange dots are boundary values, and blue dots are outliers. (b) Distribution is plotted to show that weights are concentrated in a narrow range around zero.

4.1 WEIGHT RESCALING STRATEGY

Problem analysis. The vanilla uniform quantization in the QP-SNN baseline minimizes resource usage, but suffers from inefficient bit-width utilization. This weakens the discrimination of the quantized weights in the QP-SNN baseline, limiting the model's representation capability. To evaluate the bit-width utilization efficiency, we define a metric as,

$$R_{utilize} = \frac{N_{actual} \left(\mathbf{W}_{int}^{l} \right)}{N_{total} \left(\mathbf{W}_{int}^{l} \right)}, \tag{8}$$

where $N_{actual}(\cdot)$, $N_{total}(\cdot)$ are the actual, available number of distinct values that \mathbf{W}_{int}^l represents. Next, we analyze $R_{utilize}$ for QP-SNN baseline to assess bit-width utilization efficiency. We compute $N_{actual}(\mathbf{W}_{int}^l)$ using the range of full precision weights, shown in Figure 2(a)(top). We consider full precision weights between the 1st and 99th percentiles to eliminate outliers. For clarity, we denote $\mathbf{W}^l \in [-a,a]$, where $a = \max\left(\left|P_{0.01}(\mathbf{W}^l)\right|,\left|P_{0.99}(\mathbf{W}^l)\right|\right)$. Typically, a is a positive value near zero (LeCun et al. (2002); He et al. (2015)). This means that the clamp function in Eq.(4) doesn't alter weight values. Based on this, we can deduce $\mathbf{W}_{int}^l \in \left[\left|\frac{z-a}{2}s(b)+\frac{1}{2}\right|,\left|\frac{z+a}{2}s(b)+\frac{1}{2}\right|\right]$. Therefore, $N_{actual}(\mathbf{W}_{int}^l)$ is approximately $(1+a\cdot s(b))$, leading to a utilization rate of $\frac{s(b)\cdot a+1}{s(b)+1}$.

To clearly show the low bit-width utilization of the baseline, we analyze the weight distribution and determine the value of a. We plot the weight distributions of VGG-16 and ResNet20 in Figure 2(b), and also label the 1st and 99th percentiles. In Figure 2(b), the smallest value of a is 0.14 (VGG-16.conv16), and the largest is 0.32 (VGG-16.conv4). This indicates that under 8-bit quantization, the QP-SNN baseline uses less than half of the assigned bit width, with a minimum of 14.33% and a maximum of 32.26%. This inefficient utilization causes a large number of weights to be quantized to the same integer grid, reducing the discrimination of quantized weights. This limits the representation capacity of the QP-SNN baseline, leading to decreased performance. The complete weight distributions are provided in Appendix E.1.

ReScaW-based uniform quantization. To resolve the limited representation capacity, we propose a simple yet effective weight rescaling (ReScaW) strategy for the QP-SNN baseline that uses bit-width more efficiently. Specifically, we introduce a scale coefficient γ to regulate the weight distribution to a wider range before quantization. The proposed ReScaW strategy is defined as,

$$\mathbf{W}_{scaled}^{l} = \frac{\mathbf{W}^{l}}{\gamma}.$$
 (9)

The scaling coefficient γ can assume any positive value within the range $0 < \gamma < 1$. We provide three options for γ : (1) the maximum absolute value: $max(|\mathbf{W}^l|)$; (2) the maximum absolute value of the

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Figure 4: Proposed pruning criterion based on the singular value of spatiotemporal spike activity.

x-th and (1-x)-th percentiles: $\Psi_x(\mathbf{W}^l) = \max\left(\left|P_{1-x}(\mathbf{W}^l)\right|, \left|P_x(\mathbf{W}^l)\right|\right)$; and (3) 1-norm mean value: $\frac{\|\mathbf{W}^l\|_1}{\|\mathbf{W}^l\|_1}$, where $\|\mathbf{W}^l\|_1$ is the number of entries in \mathbf{W}^l . These three options can scale weights to span the range of [-1,1], thereby ensuring more efficient bit width utilization. The impact of these three options on performance will be explored in the experimental section. Consequently, we formulate the ReScaW-based uniform quantization as,

$$\mathbf{W}^{l} \approx \gamma \cdot \left(\frac{2}{s(b)} \left\lceil \frac{s(b)}{2} \cdot \left(\text{clamp}(\frac{\mathbf{W}^{l}}{\gamma}; -1, 1) + z \right) \right\rfloor - z \right). \tag{10}$$

We compare vanilla uniform quantization in the QP-SNN baseline with the ReScaW in Figure 2(a). Clearly, the ReScaW method utilizes the allocated bit width more efficiently. This efficient bitwidth utilization preserves the discrimination of quantized weights, enhancing the representation capability and performance of the QP-SNN baseline.

4.2 PRUNING CRITERION BASED ON THE SINGULAR VALUE OF SPIKE ACTIVITY

Problem analysis. The structured pruning work (Li et al. (2024)) employing the SCAbased criterion can produce high-performance pruned models, but the performance is ensured through multiple iterative pruning and regrowth processes. In fact, we observe that the SCAbased pruning criterion exhibits a high dependency on inputs. Specifically, it generates varying importance scores for the same convolutional kernel when processing different inputs. To prove this observation, we plot the importance scores of different kernels under varying inputs, as shown in Figure 3. The strong input dependency of SCA criterion can lead to biases in kernel evaluation, posing a risk of erroneously identifying crucial kernels as insignif-

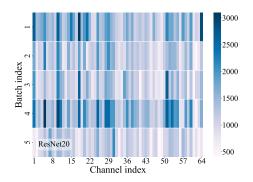


Figure 3: SCA assigns different scores to the same kernel for different input samples. The colors in the figure represent the value of importance score.

icant or misjudging unimportant kernels as essential. These misidentifications can affect the reliability of pruning, ultimately diminishing the performance of the QP-SNN baseline. Complete importance scores are available in Appendix F.1.

SVS-based pruning criterion. Several studies suggest that the number of singular values correlates with information richness (Sadek (2012); Baker (2005); Jaradat et al. (2021)). Inspired by this, we propose a novel pruning criterion for QP-SNN baseline using the singular value of spike activity (SVS) to remove redundant kernels precisely. As shown in Figure 4, the SVS-based criterion applies singular value decomposition to the average spike matrix over a given time window T, defined as,

$$\mathbf{S}_{avg}^{l,f} = \frac{1}{T} \sum_{t=1}^{T} \mathbf{S}^{l,f}[t] = \mathbf{P} \mathbf{\Sigma}_{h \times w} \mathbf{Q}^{\top}, \tag{11}$$

Algorithm 1: The overall workflow of QP-SNN.

Input: Initial SNN model: $\mathcal{M} = \{\mathbf{W}^1, \dots, \mathbf{W}^L\}$; Bit width: b; Pruning channel ratio: r; Number of training epoch: N_{epoch} ; Number of training iteration per epoch: I_{train} . **Output:** The trained QP-SNN $\mathcal{M}_{q\&p}$. \triangleright Step 1: Get quantized SNN \mathcal{M}_q by using the ReScaW-based uniform quantization; 2 for $epoch \leftarrow 1$ to N_{epoch} do for $i \leftarrow 1$ to I_{train} do for $l \leftarrow 1$ to L do $\gamma \in \{\max(|\mathbf{W}^l|), \Psi_x(\mathbf{W}^l), \frac{\|\mathbf{W}^l\|_1}{|\mathbf{W}^l|}\};$ \triangleright The selection is fixed during training; $\mathbf{W}_{scaled}^{l} = \frac{\mathbf{W}^{l}}{\gamma}; \qquad \qquad \text{Rescale 32-bit weight param}$ $\mathbf{W}^{l} \approx \gamma \cdot \left(\frac{2}{s(b)} \left\lceil \frac{s(b)}{2} \cdot \left(\text{clamp}(\frac{\mathbf{W}^{l}}{\gamma}; -1, 1) + z \right) \right\rfloor - z \right);$ ⊳ Rescale 32-bit weight parameters to a wide range; Calculate $\tilde{\mathbf{U}}^{l}[t]$, $\mathbf{S}^{l}[t]$, and $\mathbf{U}^{l}[t]$ according to Eq.(1 \sim 3) end end Perform backpropagation and update the quantized model parameters \mathcal{M}_a ; end 14 end \triangleright Step 2: Get the pruned QP-SNN $\mathcal{M}_{q\&p}$ with the SVS-based pruning criterion;

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16 for l \leftarrow 1 to L do
             Initialize an array \mathcal{F};
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             for f \leftarrow 1 to n_l do
                     Perform a inference process with mini-batch data, get spatiotemporal spike activity;
19
                    Get the singular value matrix \Sigma: \frac{1}{T} \sum_{t=1}^{T} \mathbf{S}^{l,f}[t] = \mathbf{P} \mathbf{\Sigma}_{h \times w} \mathbf{Q}^{\top};

\operatorname{Score}(\mathbf{W}^{l,f}) = \mathbb{E}_{B} \left( \sum_{i=1}^{\min(H,W)} \mathbb{I}(\sigma_{i} > \epsilon) \right);
21
                    \mathcal{F}[f] = \operatorname{Score}(\mathbf{W}^{l,f});
22
23
             I_{prun} = [r * n_l]; s_{index} = argsort(\mathcal{F})[I_{prun} :];

    Select kernels with high score;

24
             \mathbf{W}_{q\&p}^l \leftarrow \text{Kernels with index in } s_{index};
25
26 end
```

function $Finetune(\mathcal{M}_{q\&p});$ \triangleright Fine-tune the pruned model to optimize performance.

where h, w are the height and width of the spike matrix. $\mathbf{P} = [\mathbf{p}_1, \dots, \mathbf{p}_h] \in \mathbb{R}^{h \times h}$ and $\mathbf{Q} = [\mathbf{q}_1, \dots, \mathbf{q}_w] \in \mathbb{R}^{w \times w}$ are orthogonal matrices representing the left and right singular vectors. $\mathbf{\Sigma} \in \mathbb{R}^{h \times w}$ is a diagonal matrix containing the singular values of $\mathbf{S}_{avg}^{l,f}$ in descending order, denoted as,

$$\Sigma = \operatorname{diag}\left(\sigma_{1}, \sigma_{2}, \cdots, \sigma_{\min(h, w)}\right),$$
with $\sigma_{1} \geq \sigma_{2} \geq \cdots \geq \sigma_{r^{*}} \geq \epsilon > \sigma_{r^{*}+1} \geq \cdots \geq \sigma_{\min(h, w)} \geq 0.$
(12)

Here, ϵ serves as a threshold to distinguish significant and negligible singular values, and it is generally set to a positive value near zero. Based on the threshold ϵ , $\mathbf{S}^{l,f}_{avg}$ can be expressed as two components: $\mathbf{S}^{l,f}_{avg} = \sum_{i=1}^{r^*} \sigma_i \mathbf{p}_i \mathbf{q}_i^\top + \sum_{i=r^*+1}^{min(H,W)} \sigma_i \mathbf{p}_i \mathbf{q}_i^\top$. The first term captures the core feature dictated by the significant singular values, while the second term reflects potentially noise-related information (Jaradat et al. (2021)). Based on this decomposition, we define our pruning criterion as,

$$Score(\mathbf{W}^{l,f}) = \mathbb{E}_B\left(\sum_{i=1}^{\min(H,W)} \mathbb{I}(\sigma_i > \epsilon)\right), \tag{13}$$

where \mathbb{E}_B denotes the average over the mini-batch, and $\mathbb{I}(\cdot)$ is the indicator function that counts only significant singular values (those exceeding ϵ) for importance evaluation. We will demonstrate in the experimental section that the proposed SVS-based pruning criterion achieves more accurate removal of unimportant convolutional kernels.

By integrating the ReScaW strategy and the SVS-based pruning criterion into the baseline, we develop QP-SNN, with its workflow outlined in Algorithm 1. In summary, the proposed QP-SNN is lightweight and hardware-friendly, while also achieving high performance. Therefore, our QP-SNN offers an efficient solution for applications in resource-constrained scenarios like edge computing devices and low-power systems.

5 EXPERIMENT

In this section, we first present the experiment setup, including the datasets, network structures, and learning algorithms. Then, we evaluate the performance of our QP-SNN by comparing it to existing methods. Finally, we conduct extensive ablation studies to verify the effectiveness of the proposed ReScaW strategy and the SVS-based pruning criterion.

5.1 Experiment setup

We evaluate our method on image classification tasks, including static datasets like CIFAR-10, CIFAR-100 (Krizhevsky et al. (2009)), TinyImageNet, and ImageNet-1k (Deng et al. (2009)), along-side neuromorphic dataset DVS-CIFAR10 (Li et al. (2017)). These datasets serve as standard benchmarks in machine learning and neuromorphic computing for evaluating various methods. For architecture, we use classical structures VGGNet and Spiking ResNet (Zheng et al. (2021)), with details provided in Table 1. We use SEW-ResNet (Fang et al. (2021)) on ImageNet-1k for a fair comparison with (Shi et al. (2024)). As for ϵ in Eq.(13), we observe minimal variation in the singular values, so we set it to a small value of 1e-6 (Jaradat et al. (2021)). For the learning of QP-SNN, we use the surrogate gradient (Wu et al. (2018)) and straight-through estimator (Bengio et al. (2013)) to handle the nondifferentiability of spike and quantization. We provide additional details in the appendix, with the learning algorithm described in Appendix D and experimental setups in Appendix G.

5.2 Performance comparison

As shown in Table 1, we compare QP-SNN with related work in performance and model size to prove the effectiveness and efficiency. We use 8, 4, and 2-bit weight configurations in experiments across all datasets. Compared to ANN2SNN conversion and hybrid algorithms, QP-SNN achieves top-1 performance with fewer timesteps, such as 2 or 4 on static datasets. When compared to direct algorithms, QP-SNN also performs well. On CIFAR-10 and CIFAR-100, QP-SNN outperforms previous methods (Shi et al. (2024); Li et al. (2024)) with smaller models and shorter timesteps (e.g., CIFAR-10: 1.61 MB, Acc=95.06%, T=2; CIFAR-100: 1.79 MB, Acc=75.13%, T=2). On TinyImageNet, using the same timesteps and architecture, QP-SNN reduces model size by 90.26% and increase accuracy by 3.71% compared to (Li et al. (2024)). On ImageNet, we are the first study to report results for structured pruning in SNNs, achieving comparable performance to unstructured pruning method (Shi et al. (2024)) with a 15.55% reduction in model size. On DVS-CIFAR10, QP-SNN achieves an 88.55% smaller model size and a 0.2% higher accuracy compared to (Shi et al. (2024)). To intuitively demonstrate QP-SNN's improvements, we plot comparison results in Figure 1. These results show that QP-SNN achieves superior results in both efficiency and performance, positioning it as a leading approach for compact and high-performance SNNs.

5.3 ABLATION STUDY

To prove the effectiveness of QP-SNN, we conduct extensive ablation studies. Firstly, we analyze the three options for γ in the ReScaW strategy to select the optimal one. Then, we perform thorough ablation experiments to validate the effectiveness of the proposed ReScaW strategy and SVS-based pruning criterion. Finally, we visualize the effect of the ReScaW strategy and the SVS-based criterion to demonstrate that they have effectively addressed the above mentioned issues. All ablation experiments are conducted on the CIFAR-100 dataset using ResNet20 with 1.20 MB model size.

Analysis of three options for γ . We compare the performance of quantized SNNs (not involve pruning process) with different γ settings to determine the optimal one as the default experimental setting. As depicted in Figure 5(a), the quantized SNN using $max(|\mathbf{W}^l|)$ achieves an accuracy of 77.85%, the one using $\Psi_x(\mathbf{W}^l)$ achieves an accuracy of 77.8%, and the one using $\|\mathbf{W}^l\|_1/|\mathbf{W}^l|$ achieves an accuracy of 79.16%. Clearly, the accuracy differences between them are minimal, with the 1-norm mean value performs best. This may be because $\|\mathbf{W}^l\|_1/|\mathbf{W}^l|$ can effectively capture the characteristics of the full precision distribution (Rastegari et al. (2016); Qin et al. (2020)). Therefore, we choose the 1-norm mean value as the default experimental setting.

Effectiveness of two proposed methods. As shown in Table 2, we conduct extensive ablation experiments to validate the effectiveness of two proposed methods in QP-SNN, i.e., the ReScaW strat-

Table 1: Performance comparison on static and neuromorphic datasets. **Note:** 'H', 'D', and 'C' represent hybrid, direct, and conversion learning, respectively. 'HardF' denotes 'hardware-friendly'.

Chowdhury et al. (2021) VGG-9 H 32 V 90.02 100 44.52		ent hybrid, direct, and co				-			
Deng et al. (2021) Clowy Clows Clow	Dataset	Method	Network	Train	Bits	HardF	Accuracy(%)	Timestep	Size (MB)
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Shi et al. (2024) VGG-16 D 32 X 90.65 8 28.40					5		88.60	25	12.59
Shi et al. (2024) VGG-16 D 32 X 90.65 8 28.40		Deng et al. (2021)	7Conv2FC	D			90.19	8	62.16
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Proposed QP-SNN VGG-16 D 8, 4, 2 V 94.56, 94.65, 94.44 2 3.92, 1.98, 1.02		[ICML24]							
VGG-16 D 8, 4, 2 V 91.98, 91.90, 91.61 4 4.28, 2.16, 1.10 D 8, 4, 2 V 91.30, 91.19, 90.59 4 1.45, 0.74, 0.39 1.45, 0.74, 0.45 1.45, 0.45, 0.45 1.45, 0.4			ResNet20						
Chowdhury et al. (2021) (IJCNN21) VGG-11 H 32		Proposed QP-SNN							
Chowdhury et al. (2021) VGG-11 H 5			VGG-16			,			
Deng et al. (2021) Proposed QP-SNN VGG-16 Deng et al. (2024) Proposed QP-SNN VGGSNN Deng et al. (2024)									
Deng et al. (2021) 7Conv2FC D 3 X 57.83 8 11.75			VGG-11						
Shi et al. (2024) Shi et				Н					
Shi et al. (2024) Shi et		Deng et al. (2021)	7Conv2FC	D					
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Proposed QP-SNN VGG-16 D 32 V 64.64 4 9.48	R-1	Shi et al. (2024)	ResNet18						
Proposed QP-SNN VGG-16 D 32 V 64.64 4 9.48	IFA								
Proposed QP-SNN ResNet20 D 8, 4, 2 V 75.29, 75.77, 75.13 2 6.45, 3.35, 1.79	ū		VGG-16						
Proposed QP-SNN VGG-16 D 8, 4, 2 V 74.78, 74.73, 73.89 2 4.10, 2.17, 1.20		[ICML24]							
VGG-16 D			ResNet20						
NGG-16 D 8, 4, 2		Proposed QP-SNN				,			
Kundu et al. (2021) VGG-16 C 32			VGG-16						
Li et al. (2024) VGG-16 D 32 V 49.36 4 27.92		W 1 (2021)		ע	8, 4, 2		04.70, 04.22, 03.08	4	1.85, 1.04, 0.05
Shi et al. (2024) ResNet18 D 8, 4, 2 V 51.99, 51.78, 51.67 4 4.67, 3.17, 2.41 Shi et al. (2024) ResNet18 D 32 X 60.00 4 12.40 D 32 X 58.99 4 10.48 Proposed QP-SNN ResNet18 D 8 V 61.36 4 13.28 D 4 V 58.06 4 7.71 Shi et al. (2024) VGGSNN D 32 X 78.30 10 14.08 [ICLR24] VGGSNN D 32 X 78.30 10 7.24 Li et al. (2024) 5Conv1FC D 32 V 73.00 20 3.92 [ICML24] 5 D 8, 4, 2 V 82.10, 81.80, 81.30 10 1.61, 0.90, 0.55 Proposed QP-SNN VGGSNN D 8, 4, 2 V 81.50, 80.90, 80.50 10 1.05, 0.62, 0.41 ResNet18 D 32 X 60.00 4 12.40 D 32 X 58.99 4 10.48 D 4 V 58.06 4 7.71 Shi et al. (2024) VGGSNN D 32 X 71.90 20 0.32 D 8, 4, 2 V 82.10, 81.80, 81.30 10 1.61, 0.90, 0.55 Proposed QP-SNN VGGSNN D 8, 4, 2 V 81.50, 80.90, 80.50 10 1.05, 0.62, 0.41	eNet	[WACV21]	VGG-16	C			52.70	150	24.21
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$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		Shi et al. (2024)	VGGSNIN	D	32		81.90	10	14.08
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				D	8, 4, 2	√	75.90, 75.40, 74.90	10	0.40, 0.29, 0.24

egy and the SVS-based pruning criterion. First, we demonstrate the effectiveness of the ReScaW strategy. A and B are models that apply vanilla and ReScaW quantization for SNN respectively, without involving pruning process. Their comparison shows that ReScaW-based quantization improves the performance of the quantized SNN by 0.63% over vanilla quantization, highlighting its effectiveness. Moreover, the comparison between Models C and D indicates that merely replac-

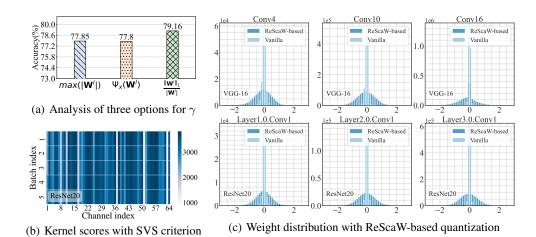


Figure 5: Visualization of ablation experiments.

Table 2: Ablation study on the effectiveness of two proposed methods. **Note:** 'Increment' represents the accuracy improvement relative to the specified model; 'r.w./' denotes 'replaced with'.

	Model	Accuracy(%)	Compared to	Increment(%)
\overline{A} .	only vanilla quant	78.53	-	-
В.	only ReScaW quant	79.16	A.	0.63 ↑
C.	baseline	69.16	-	=
D.	r.w./ ReScaW	73.40	<i>C</i> .	4.24 ↑
E.	r.w./ SVS	73.32	C.	4.16↑
F.	r.w./ ReScaW & SVS	73.89	<i>C</i> .	4.73 ↑

ing the quantization in the baseline also results in a significant performance gain of 4.24%, further validating the ReScaW strategy. Second, we demonstrate the effectiveness of the SVS-based pruning criterion. The comparison between Models C and E reveals that the SVS criterion enhances the baseline performance by 4.16%, confirming its ability to remove kernels accurately and preserve model performance. By integrating these two methods into baseline, the performance is significantly improved by 4.73%, underscoring their importance for preserving QP-SNN performance.

Impact of the ReScaW strategy and the SVS-based pruning criterion. To demonstrate that the ReScaW strategy and SVS-based criterion effectively address the previously mentioned issues, we present the weight distribution and importance scores of QP-SNN. We depict the weight distribution of QP-SNN in Figure 5(c). This indicates that ReScaW-based quantization results in a broader weight distribution compared to vanilla quantization, indicating improved bit-width utilization efficiency. In addition, Figure 5(b) depicts the importance scores of QP-SNN, showing that the SVS-based pruning criterion produces stable scores with minimal fluctuation across different inputs. This input-insensitive characteristic enables QP-SNN to remove redundant kernels accurately. Complete visualization of weight distributions and kernel scores are provided in Appendix E.2 and F.2.

6 Conclusion

SNNs offer energy-efficient solutions for artificial intelligence. However, the current SNN community focuses mainly on building large-scale SNNs to increase performance, which limits their feasibility in resource-constrained edge devices. To tackle this limitation, we first developed a QP-SNN baseline using uniform quantization and structured pruning, which significantly reduces resource usage. Furthermore, we analyzed and addressed the underlying issues of the QP-SNN baseline in quantization and pruning to improve performance. For quantization, we revealed that the vanilla uniform quantization suffers from limited representation capability due to inefficient bit-width utilization and proposed a weight rescaling strategy to resolve it. For pruning, we observed that the SCA criterion exhibits low robustness on inputs and introduced a novel criterion using the singular value of spike activity to remove unimportant kernels more accurately. By integrating the ReScaW and SVS pruning criteria, our QP-SNN achieved superior efficiency and performance, demonstrating its potential for advancing neuromorphic intelligent systems and edge computing.

REFERENCES

- Filipp Akopyan, Jun Sawada, Andrew Cassidy, Rodrigo Alvarez-Icaza, John Arthur, Paul Merolla, Nabil Imam, Yutaka Nakamura, Pallab Datta, Gi-Joon Nam, et al. Truenorth: Design and tool flow of a 65 mw 1 million neuron programmable neurosynaptic chip. *IEEE transactions on computer-aided design of integrated circuits and systems*, 34(10):1537–1557, 2015.
- Kirk Baker. Singular value decomposition tutorial. The Ohio State University, 24:22, 2005.
- Guillaume Bellec, David Kappel, Wolfgang Maass, and Robert Legenstein. Deep rewiring: Training very sparse deep networks. *arXiv preprint arXiv:1711.05136*, 2017.
- Yoshua Bengio, Nicholas Léonard, and Aaron Courville. Estimating or propagating gradients through stochastic neurons for conditional computation. *arXiv* preprint arXiv:1308.3432, 2013.
- Zhaowei Cai, Xiaodong He, Jian Sun, and Nuno Vasconcelos. Deep learning with low precision by half-wave gaussian quantization. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pp. 5918–5926, 2017.
- Yanqi Chen, Zhaofei Yu, Wei Fang, Zhengyu Ma, Tiejun Huang, and Yonghong Tian. State transition of dendritic spines improves learning of sparse spiking neural networks. In *International Conference on Machine Learning*, pp. 3701–3715. PMLR, 2022.
- Sayeed Shafayet Chowdhury, Isha Garg, and Kaushik Roy. Spatio-temporal pruning and quantization for low-latency spiking neural networks. In 2021 International Joint Conference on Neural Networks (IJCNN), pp. 1–9. IEEE, 2021.
- Ekin D Cubuk, Barret Zoph, Dandelion Mane, Vijay Vasudevan, and Quoc V Le. Autoaugment: Learning augmentation policies from data. *arXiv preprint arXiv:1805.09501*, 2018.
- Mike Davies, Narayan Srinivasa, Tsung-Han Lin, Gautham Chinya, Yongqiang Cao, Sri Harsha Choday, Georgios Dimou, Prasad Joshi, Nabil Imam, Shweta Jain, et al. Loihi: A neuromorphic manycore processor with on-chip learning. *Ieee Micro*, 38(1):82–99, 2018.
- Jia Deng, Wei Dong, Richard Socher, Li-Jia Li, Kai Li, and Li Fei-Fei. Imagenet: A large-scale hierarchical image database. In *2009 IEEE conference on computer vision and pattern recognition*, pp. 248–255. Ieee, 2009.
- Lei Deng, Yujie Wu, Yifan Hu, Ling Liang, Guoqi Li, Xing Hu, Yufei Ding, Peng Li, and Yuan Xie. Comprehensive snn compression using admm optimization and activity regularization. *IEEE transactions on neural networks and learning systems*, 34(6):2791–2805, 2021.
- Shikuang Deng, Yuhang Li, Shanghang Zhang, and Shi Gu. Temporal efficient training of spiking neural network via gradient re-weighting. *arXiv preprint arXiv:2202.11946*, 2022.
- Terrance DeVries. Improved regularization of convolutional neural networks with cutout. *arXiv* preprint arXiv:1708.04552, 2017.
- Yifu Ding, Haotong Qin, Qinghua Yan, Zhenhua Chai, Junjie Liu, Xiaolin Wei, and Xianglong Liu. Towards accurate post-training quantization for vision transformer. In *Proceedings of the 30th ACM international conference on multimedia*, pp. 5380–5388, 2022.
- Wei Fang, Zhaofei Yu, Yanqi Chen, Tiejun Huang, Timothée Masquelier, and Yonghong Tian. Deep residual learning in spiking neural networks. *Advances in Neural Information Processing Systems*, 34:21056–21069, 2021.
- Wulfram Gerstner and Werner M Kistler. Spiking neuron models: Single neurons, populations, plasticity. Cambridge university press, 2002.
- Amir Gholami, Sehoon Kim, Zhen Dong, Zhewei Yao, Michael W Mahoney, and Kurt Keutzer. A survey of quantization methods for efficient neural network inference. In *Low-Power Computer Vision*, pp. 291–326. Chapman and Hall/CRC, 2022.
- Song Han, Jeff Pool, John Tran, and William Dally. Learning both weights and connections for efficient neural network. *Advances in neural information processing systems*, 28, 2015.

- Kaiming He, Xiangyu Zhang, Shaoqing Ren, and Jian Sun. Delving deep into rectifiers: Surpassing human-level performance on imagenet classification. In *Proceedings of the IEEE international conference on computer vision*, pp. 1026–1034, 2015.
- Yang He and Lingao Xiao. Structured pruning for deep convolutional neural networks: A survey. *IEEE transactions on pattern analysis and machine intelligence*, 2023.
- Geoffrey Hinton, Li Deng, Dong Yu, George E Dahl, Abdel-rahman Mohamed, Navdeep Jaitly, Andrew Senior, Vincent Vanhoucke, Patrick Nguyen, Tara N Sainath, et al. Deep neural networks for acoustic modeling in speech recognition: The shared views of four research groups. *IEEE Signal processing magazine*, 29(6):82–97, 2012.
- Yangfan Hu, Qian Zheng, and Gang Pan. Bitsnns: Revisiting energy-efficient spiking neural networks. *IEEE Transactions on Cognitive and Developmental Systems*, 2024.
- Eugene M Izhikevich. Simple model of spiking neurons. *IEEE Transactions on neural networks*, 14(6):1569–1572, 2003.
- Sambhav Jain, Albert Gural, Michael Wu, and Chris Dick. Trained quantization thresholds for accurate and efficient fixed-point inference of deep neural networks. *Proceedings of Machine Learning and Systems*, 2:112–128, 2020.
- Yousef Jaradat, Mohammad Masoud, Ismael Jannoud, Ahmad Manasrah, and Mohammad Alia. A tutorial on singular value decomposition with applications on image compression and dimensionality reduction. In 2021 international conference on information technology (ICIT), pp. 769–772. IEEE, 2021.
- Seijoon Kim, Seongsik Park, Byunggook Na, and Sungroh Yoon. Spiking-yolo: spiking neural network for energy-efficient object detection. In *Proceedings of the AAAI conference on artificial intelligence*, volume 34, pp. 11270–11277, 2020.
- Alex Krizhevsky, Geoffrey Hinton, et al. Learning multiple layers of features from tiny images. 2009.
- Uday Kulkarni, Abhishek S Hosamani, Abhishek S Masur, Shashank Hegde, Ganesh R Vernekar, and K Siri Chandana. A survey on quantization methods for optimization of deep neural networks. In 2022 international conference on automation, computing and renewable systems (ICACRS), pp. 827–834. IEEE, 2022.
- Souvik Kundu, Gourav Datta, Massoud Pedram, and Peter A Beerel. Spike-thrift: Towards energy-efficient deep spiking neural networks by limiting spiking activity via attention-guided compression. In *Proceedings of the IEEE/CVF winter conference on applications of computer vision*, pp. 3953–3962, 2021.
- Yann LeCun, Léon Bottou, Genevieve B Orr, and Klaus-Robert Müller. Efficient backprop. In *Neural networks: Tricks of the trade*, pp. 9–50. Springer, 2002.
- Hao Li, Asim Kadav, Igor Durdanovic, Hanan Samet, and Hans Peter Graf. Pruning filters for efficient convnets. *arXiv preprint arXiv:1608.08710*, 2016.
- Hongmin Li, Hanchao Liu, Xiangyang Ji, Guoqi Li, and Luping Shi. Cifar10-dvs: an event-stream dataset for object classification. *Frontiers in neuroscience*, 11:244131, 2017.
- Yaxin Li, Qi Xu, Jiangrong Shen, Hongming Xu, Long Chen, and Gang Pan. Towards efficient deep spiking neural networks construction with spiking activity based pruning. *arXiv* preprint *arXiv*:2406.01072, 2024.
- Yuhang Li, Youngeun Kim, Hyoungseob Park, Tamar Geller, and Priyadarshini Panda. Neuromorphic data augmentation for training spiking neural networks. In *Computer Vision–ECCV 2022:* 17th European Conference, Tel Aviv, Israel, October 23–27, 2022, Proceedings, Part VII, pp. 631–649. Springer, 2022.

- Qianhui Liu, Jiaqi Yan, Malu Zhang, Gang Pan, and Haizhou Li. Lite-snn: Designing lightweight and efficient spiking neural network through spatial-temporal compressive network search and joint optimization. *arXiv preprint arXiv:2401.14652*, 2024.
 - Xinhao Luo, Man Yao, Yuhong Chou, Bo Xu, and Guoqi Li. Integer-valued training and spikedriven inference spiking neural network for high-performance and energy-efficient object detection. arXiv preprint arXiv:2407.20708, 2024.
 - Eustace Painkras, Luis A Plana, Jim Garside, Steve Temple, Francesco Galluppi, Cameron Patterson, David R Lester, Andrew D Brown, and Steve B Furber. Spinnaker: A 1-w 18-core system-on-chip for massively-parallel neural network simulation. *IEEE Journal of Solid-State Circuits*, 48(8):1943–1953, 2013.
 - Jing Pei, Lei Deng, Sen Song, Mingguo Zhao, Youhui Zhang, Shuang Wu, Guanrui Wang, Zhe Zou, Zhenzhi Wu, Wei He, et al. Towards artificial general intelligence with hybrid tianjic chip architecture. *Nature*, 572(7767):106–111, 2019.
 - Yijian Pei, Changqing Xu, Zili Wu, and Yintang Yang. Albsnn: ultra-low latency adaptive local binary spiking neural network with accuracy loss estimator. *Frontiers in Neuroscience*, 17:1225871, 2023.
 - Michael Pfeiffer and Thomas Pfeil. Deep learning with spiking neurons: opportunities and challenges. *Frontiers in neuroscience*, 12, 2018.
 - Haotong Qin, Ruihao Gong, Xianglong Liu, Xiao Bai, Jingkuan Song, and Nicu Sebe. Binary neural networks: A survey. *Pattern Recognition*, 105:107281, 2020.
 - Haotong Qin, Yifu Ding, Mingyuan Zhang, Qinghua Yan, Aishan Liu, Qingqing Dang, Ziwei Liu, and Xianglong Liu. Bibert: Accurate fully binarized bert. *arXiv preprint arXiv:2203.06390*, 2022.
 - Mohammad Rastegari, Vicente Ordonez, Joseph Redmon, and Ali Farhadi. Xnor-net: Imagenet classification using binary convolutional neural networks. In *European conference on computer vision*, pp. 525–542. Springer, 2016.
 - Nitin Rathi, Priyadarshini Panda, and Kaushik Roy. Stdp-based pruning of connections and weight quantization in spiking neural networks for energy-efficient recognition. *IEEE Transactions on Computer-Aided Design of Integrated Circuits and Systems*, 38(4):668–677, 2018.
 - Babak Rokh, Ali Azarpeyvand, and Alireza Khanteymoori. A comprehensive survey on model quantization for deep neural networks in image classification. *ACM Transactions on Intelligent Systems and Technology*, 14(6):1–50, 2023.
 - Deboleena Roy, Indranil Chakraborty, and Kaushik Roy. Scaling deep spiking neural networks with binary stochastic activations. In *2019 IEEE International Conference on Cognitive Computing (ICCC)*, pp. 50–58. IEEE, 2019a.
 - Kaushik Roy, Akhilesh Jaiswal, and Priyadarshini Panda. Towards spike-based machine intelligence with neuromorphic computing. *Nature*, 575(7784):607–617, 2019b.
 - Rowayda A Sadek. Svd based image processing applications: state of the art, contributions and research challenges. *arXiv preprint arXiv:1211.7102*, 2012.
 - Xinyu Shi, Jianhao Ding, Zecheng Hao, and Zhaofei Yu. Towards energy efficient spiking neural networks: An unstructured pruning framework. In *The Twelfth International Conference on Learning Representations*, 2024.
 - Martino Sorbaro, Qian Liu, Massimo Bortone, and Sadique Sheik. Optimizing the energy consumption of spiking neural networks for neuromorphic applications. *Frontiers in neuroscience*, 14: 516916, 2020.
 - Sunil Vadera and Salem Ameen. Methods for pruning deep neural networks. *IEEE Access*, 10: 63280–63300, 2022.

- Yixuan Wang, Yang Xu, Rui Yan, and Huajin Tang. Deep spiking neural networks with binary weights for object recognition. *IEEE Transactions on Cognitive and Developmental Systems*, 13 (3):514–523, 2020.
- Yuanyuan Wang, Chao Wang, Hong Zhang, Yingbo Dong, and Sisi Wei. A sar dataset of ship detection for deep learning under complex backgrounds. *remote sensing*, 11(7):765, 2019.
- Wenjie Wei, Yu Liang, Ammar Belatreche, Yichen Xiao, Honglin Cao, Zhenbang Ren, Guoqing Wang, Malu Zhang, and Yang Yang. Q-snns: Quantized spiking neural networks. *arXiv* preprint *arXiv*:2406.13672, 2024.
- Yujie Wu, Lei Deng, Guoqi Li, Jun Zhu, and Luping Shi. Spatio-temporal backpropagation for training high-performance spiking neural networks. *Frontiers in neuroscience*, 12:331, 2018.
- Sheng Xu, Anran Huang, Lei Chen, and Baochang Zhang. Convolutional neural network pruning: A survey. In 2020 39th Chinese Control Conference (CCC), pp. 7458–7463. IEEE, 2020.
- Jiaqi Yan, Qianhui Liu, Malu Zhang, Lang Feng, De Ma, Haizhou Li, and Gang Pan. Efficient spiking neural network design via neural architecture search. *Neural Networks*, 173:106172, 2024.
- Man Yao, Jiakui Hu, Tianxiang Hu, Yifan Xu, Zhaokun Zhou, Yonghong Tian, Bo Xu, and Guoqi Li. Spike-driven transformer v2: Meta spiking neural network architecture inspiring the design of next-generation neuromorphic chips. *arXiv preprint arXiv:2404.03663*, 2024a.
- Man Yao, Jiakui Hu, Zhaokun Zhou, Li Yuan, Yonghong Tian, Bo Xu, and Guoqi Li. Spike-driven transformer. *Advances in neural information processing systems*, 36, 2024b.
- Hang Yin, John Boaz Lee, Xiangnan Kong, Thomas Hartvigsen, and Sihong Xie. Energy-efficient models for high-dimensional spike train classification using sparse spiking neural networks. In *Proceedings of the 27th ACM SIGKDD conference on knowledge discovery & data mining*, pp. 2017–2025, 2021.
- Ruokai Yin, Yuhang Li, Abhishek Moitra, and Priyadarshini Panda. Mint: Multiplier-less integer quantization for energy efficient spiking neural networks. In 2024 29th Asia and South Pacific Design Automation Conference (ASP-DAC), pp. 830–835. IEEE, 2024a.
- Yujia Yin, Xinyi Chen, Chenxiang Ma, Jibin Wu, and Kay Chen Tan. Efficient online learning for networks of two-compartment spiking neurons. *arXiv* preprint arXiv:2402.15969, 2024b.
- Shimin Zhang, Qu Yang, Chenxiang Ma, Jibin Wu, Haizhou Li, and Kay Chen Tan. Tc-lif: A two-compartment spiking neuron model for long-term sequential modelling. In *Proceedings of the AAAI Conference on Artificial Intelligence*, volume 38, pp. 16838–16847, 2024.
- Xiangguo Zhang, Haotong Qin, Yifu Ding, Ruihao Gong, Qinghua Yan, Renshuai Tao, Yuhang Li, Fengwei Yu, and Xianglong Liu. Diversifying sample generation for accurate data-free quantization. In *Proceedings of the IEEE/CVF conference on computer vision and pattern recognition*, pp. 15658–15667, 2021.
- Yichi Zhang, Zhiru Zhang, and Lukasz Lew. Pokebnn: A binary pursuit of lightweight accuracy. In *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pp. 12475–12485, 2022.
- Hanle Zheng, Yujie Wu, Lei Deng, Yifan Hu, and Guoqi Li. Going deeper with directly-trained larger spiking neural networks. In *Proceedings of the AAAI conference on artificial intelligence*, volume 35, pp. 11062–11070, 2021.
- Chenlin Zhou, Liutao Yu, Zhaokun Zhou, Zhengyu Ma, Han Zhang, Huihui Zhou, and Yonghong Tian. Spikingformer: Spike-driven residual learning for transformer-based spiking neural network. *arXiv preprint arXiv:2304.11954*, 2023.
- Chenzhuo Zhu, Song Han, Huizi Mao, and William J Dally. Trained ternary quantization. *arXiv* preprint arXiv:1612.01064, 2016.

A ANALYSIS ON THE ORDER OF QUANTIZATION AND PRUNING

When two or more model lightweight techniques are employed, compatibility issues often arise, such as the order of applying these techniques and the training strategies involved. In this paper, we adpot the 'quantize first, then prune' strategy based on the following two considerations. **First**, this strategy can better guarantee the effect of pruning technique. Specifically, if pruning is applied before quantization, important convolutional kernels identified in the full-precision parameter domain may become misaligned after quantization, as the quantization reintroduces additional errors. In contrast, by quantizing first and then pruning, redundant convolutional kernels are identified directly in the target low-precision parameter domain. This order allows for more accurate identification and preservation of critical kernels. **Second**, this strategy significantly reduces training overhead. Pruning before quantization requires three weight updates: 'full-precision SNN training—) pruning with fine-tuning —) quantization with fine-tuning,' while 'quantize first, then prune' only requires two adjustments: 'quatized SNN training—) pruning with fine-tuning.'

In addition to the theoretical analysis, we have also conducted experiments by reversing the order of quantization and pruning, termed PQ-SNN, to validate the effectiveness of QP-SNN. Experiments are performed on the CIFAR-100 with ResNet20 under the bit-width of 4. We summarize the experimental results in Table 3, from which two conclusions can be obtained. **First**, the proposed ReScaW and SVS can improve both performance, regardless of the order in which they are applied, leading to a 1.83% improvement in PQ-SNN and a 4.46% improvement in QP-SNN. This proves the effectiveness of our ReScaW and SVS methods. **Second**, QP-SNN achieves the highest performance (surpassing PQ-SNN by 1.39%), demonstrating that 'quantize first, then prune' is more effective.

Table 3: Ablation study on the order of quantization and pruning.

Method 1	PQ-SNN baseline	PQ-SNN	QP-SNN baseline	QP-SNN
Accuracy	71.51%	73.34% _(baseline+1.83%)	70.27%	74.73% _(baseline+4.46%)

B SCALABILITY OF QP-SNN TO COMPLEX ARCHITECTURES AND TASKS

QP-SNN can be extended to complex architectures like Transformer and complex tasks like object detection. The reason we choose the ResNet and simple classification tasks is to facilitate a comprehensive comparison with advanced compression methods in SNNs (Li et al. (2024); Shi et al. (2024)). In this section, we have conducted two additional experiments: (1) using the Spikingformer (Zhou et al. (2023)) architecture, and (2) applying our method to an object detection task, to prove the scalability of QP-SNN to complex architectures and tasks.

Experiments with the Spikingformer architecture. We select the Spikingformer-4-384 structure and validate it on the CIFAR-10 dataset. The training setups are consistent with the original paper (Zhou et al. (2023)). Experimental results are shown in Table 4, where our method achieves a 87.93% reduction in model size, a 55.48% decrease in SOPs, and a 55.64% reduction in power consumption, while maintaining an excellent performance of 76.94%. These results fully validate the effectiveness of QP-SNN for complex Spiking Transformer architecture.

Table 4: Performance on the Spikingformer architecture.

Architecture Method	Connection	Bit	Model size (MB)	SOPs (M)	Power (mJ)	Accuracy
Spikingformer-4-384 Full-precis		16	18.64	292.14	0.266	79.09%
Spikingformer-4-384 QP-SNN		4	2.25	130.05	0.118	76.94%

Object detection validation. We conduct object detection experiments on the remote sensing dataset SSDD (Wang et al. (2019)), which focuses on ship detection imagery acquired through synthetic aperture radar. In our experiments, we adopt the YOLO-v3 detection architecture with ResNet10 as the backbone. During training, we perform the pruning operation on the backbone and

 employ the SGD optimizer with a polynomial decay learning rate schedule, initializing the learning rate at 1e-2 and training for 300 epochs. Results are shown in Table 5, where our method achieves a mAP@0.5 of 97.10% with an 88.85% reduction in the model size of the backbone model. This fully validates the effectiveness of QP-SNN for complex tasks.

Table 5: Object detection results on SSDD (Wang et al. (2019)).

Architecture	Method	Bit	Model size (MB)	mAP@0.5
YOLO-v3 (ResNet10	Full-precision	32	19.29	96.80%
as the backbone)	QP-SNN	4	2.15	97.10%

C EFFICIENCY VALIDATION OF QP-SNN

Model compression aims to optimize efficiency during the inference phase, facilitating efficient deployment on resource-constrained devices. Therefore, we present the key efficiency metrics of QP-SNN during inference, including model size, SOPs, power consumption, and accuracy, to verify the efficiency advantage of QP-SNN.

We first present a comparison of our model with the full-precision uncompressed SNN counterparts. The results are summarized in Table 7. We acknowledge that our method exhibits accuracy loss compared to uncompressed SNNs. However, this performance degradation is a common challenge in the field of model compression. Fortunately, QP-SNN demonstrates satisfactory performance under extreme compression ratios. For example, on the CIFAR-10 dataset, under the extreme connection ratio of 9.61%, QP-SNN reduces the model size by 98.74%, SOPs by 78.69%, and power consumption by 77.45%, while the accuracy decreases by only 2.44%. This trade-off between performance degradation and resource efficiency is highly advantageous in edge computing scenarios.

Table 6: Efficiency metrics comparison of QP-SNN with full-precision uncompressed SNN.

	Architecture	Connection	Bit	Model size (MB)	SOPs (M)	Power (mJ)	Accuracy
CIFAR-10	VGG-16	100%	32	58.88	54.60	0.204	93.63%
	VGG-16	9.61%	4	0.74	11.63	0.046	91.19%
CIFAR-100	ResNet20	100%	32	68.4	415.64	0.756	79.49%
	ResNet20	22.69%	4	2.17	131.53	0.126	74.73%

We then add a comparison of our method with related studies on CIFAR-10. Experimental results are shown in Table 7. It can be seen that QP-SNN exhibits competitive SOPs compared to compression work in the SNN domain, and exhibits extremely low model size due to quantization. Moreover, it is worth noting that the advanced works (Deng et al. (2021); Shi et al. (2024)) focus on unstructured pruning, which typically achieves higher sparsity and performance but requires specialized hardware support. In contrast, our work adopts uniform quantization and structured pruning, balancing the advantages of sparsity, performance, and hardware compatibility.

Table 7: Efficiency metrics comparison of QP-SNN with related studies on the CIFAR-10 dataset.

Method	Architecture	Time step	HardF	Model size (MB)	SOPs (M)
Deng et al. (2021) [TNNLS21]	7Conv2FC	8	X	62.16	107.97
Shi et al. (2024) [ICLR24]	6Conv2FC	8	X	33.76	11.98
Li et al. (2024) [ICML24]	VGG-16	4	\checkmark	5.68	-
QP-SNN	VGG-16	4	\checkmark	0.74	11.63

D LEARNING ALGORITHM FOR QP-SNN

In this section, we introduce the learning algorithm for the QP-SNN. We use the spatio-temporal backpropagation (STBP) (Wu et al. (2018)) and the straight-through estimator (STE) (Bengio et al. (2013)) methods to solve the non-differentiability of the spike generation function and quantization.

Training QP-SNNs requires calculating the gradient of the loss function with respect to the synaptic weight. In this work, we use the STBP learning algorithm, which performs gradient propagation in both spatial and temporal dimensions. By applying the chain rule, STBP computes the derivative of the loss function $\mathcal L$ with respect to synaptic weights $\mathbf W^l$ through the following equation,

$$\frac{\partial \mathcal{L}}{\partial \mathbf{W}^{l}} = \sum_{t=1}^{T} \frac{\partial \mathcal{L}}{\partial \mathbf{S}^{l+1}[t]} \frac{\partial \mathbf{S}^{l+1}[t]}{\partial \mathbf{U}^{l+1}[t]} \left(\frac{\partial \mathbf{U}^{l+1}[t]}{\partial \mathbf{W}^{l}} + \sum_{\tau < t} \prod_{i=t-1}^{\tau} \left(\frac{\partial \mathbf{U}^{l+1}[i+1]}{\partial \mathbf{U}^{l+1}[i]} + \frac{\partial \mathbf{U}^{l+1}[i+1]}{\partial \mathbf{S}^{l+1}[i]} \frac{\partial \mathbf{S}^{l+1}[i]}{\partial \mathbf{U}^{l+1}[i]} \right) \frac{\partial \mathbf{U}^{l+1}[\tau]}{\partial \mathbf{W}^{l}} \right), \tag{14}$$

where the derivative of the loss function with respect to the spike $\frac{\partial \mathcal{L}}{\partial \mathbf{S}^{l+1}[t]}$ is obtained in an iterative manner. The terms of $\frac{\partial \mathbf{U}^{l+1}[t]}{\partial \mathbf{W}^l}$, $\frac{\partial \mathbf{U}^{l+1}[i+1]}{\partial \mathbf{U}^{l+1}[i]}$ and $\frac{\partial \mathbf{U}^{l+1}[i+1]}{\partial \mathbf{S}^{l+1}[i]}$ can be computed from Eq.(1). Unfortunately, the direct training of SNNs faces a distinct challenge due to the non-differentiable nature of the spiking (i.e. firing) mechanism. Specifically, the term of $\frac{\partial \mathbf{S}^{l+1}[t]}{\partial \mathbf{U}^{l+1}[t]}$ represents the gradient of the spike generation function (described in Eq. (2)). This function evaluates to infinity at the moment of spike emission and to zero elsewhere, making it incompatible with the traditional error backpropagation used in ANN training. STBP addresses this non-differentiability problem by employing surrogate gradients to approximate the true gradient Wu et al. (2018). In this paper, we use the triangular surrogate function (Deng et al. (2022)), described as

$$\frac{\partial \mathbf{S}^{l+1}[t]}{\partial \mathbf{U}^{l+1}[t]} = \frac{1}{a} \max \left(a - |\mathbf{U}^{l+1}[t] - \theta|, 0 \right),\tag{15}$$

where a is the coefficient that controls the width of the gradient window. In this paper, we use the cross-entropy loss function to access the difference between the predicted probability distribution and the true label, given by,

$$\mathcal{L} = -\sum_{i=1}^{N_L} y_i \log \left(\frac{exp(\frac{1}{T} \sum_{t=1}^T \tilde{\mathbf{U}}_i^L[t])}{\sum_i exp(\frac{1}{T} \sum_{t=1}^T \tilde{\mathbf{U}}_i^L[t])} \right), \tag{16}$$

where N_L is the number of classes, and $y_i \in \{0, 1\}$ is the label for the *i*-th neuron in the last layer. Moreover, to solve the non-differentiability of quantization, we use the STE method (Hinton et al. (2012); Bengio et al. (2013)), expressed as,

$$\frac{\partial \mathbf{W}^l}{\partial \mathbf{W}_{int}^l} = 1_{|\mathbf{W}^l| \le 1}.$$
(17)

By using the surrogate gradient function and STE, the proposed QP-SNN can be trained directly with gradient backpropagation.

E COMPLETE WEIGHT DISTRIBUTION COMPARISON

E.1 VANILLA UNIFORM QUANTIZATION

We present the weight distributions of models utilizing vanilla uniform quantization across multiple datasets and architectures, such as ResNet20 on CIFAR100, VGG-16 on TinyImageNet, and VG-GSNN on DVS-CIFAR10. In addition to the weight distribution, we also label the 1st and 99th percentiles of each layer's weights in the figure to determine the value of a. Based on the value of a and the utilization rate equation $\frac{s(b)\cdot a+1}{s(b)+1}$ in Sec. 4.1, we calculate the bit-width utilization for each model. In these calculations, we consider an 8-bit weight configuration, i.e., s(b) = 256.

The weight distribution of ResNet20 on the CIFAR-100 dataset is presented in Figure 6. It can be seen from this figure that only the weight distribution of the first layer is relatively wide, with an a value of 0.7, which corresponds to a bit-width utilization rate of 70.12%. In contrast, the a value for the subsequent layers are predominantly around 0.2, resulting in a significantly lower bit-width utilization rate of approximately 20.31%.

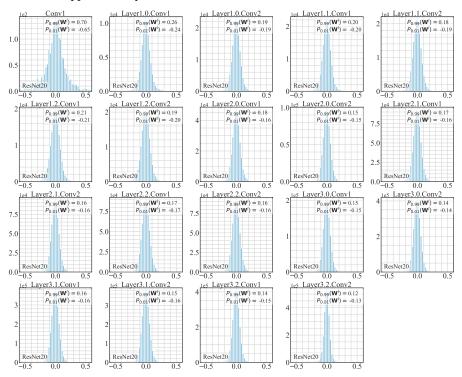


Figure 6: Weight distribution: vanilla uniform quantization, ResNet20, CIFAR-100.

The weight distribution of VGG-16 on TinyImagenet is illustrated in Figure 7. From this figure, it can be revealed that the weight distribution of each layer is broader than ResNet20 on CIFAR-100. However, the maximum *a* value is 0.64, which corresponds to a bit-width utilization rate of approximately 64.14%. This result indicates it is still quite far from full utilization.

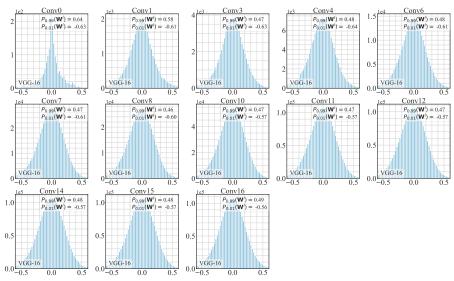


Figure 7: Weight distribution: vanilla quantization, VGG-16, TinyImageNet.

 The weight distribution of VGGSNN on DVS-CIFAR10 is displayed in Figure 8. As can be seen from the figure, the maximum a value is 0.44 (Conv1), corresponding to a bit width utilization rate of 44.22%. Moreover, the a value of subsequent layers is mainly around 0.3, resulting in a significantly lower bit width utilization rate of about 30.27%.

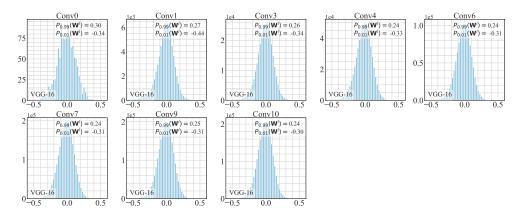


Figure 8: Weight distribution: vanilla quantization, VGGSNN, DVS-CIFAR10.

Clearly, these weight distributions prove the inefficient bit-width utilization of vanilla uniform quantization. This inefficiency leads to a substantial number of floating-point weights being discretized on the same integer grid during the quantization process, thus reducing the discrimination of the quantized weights. Consequently, this reduction adversely impacts the network's representational capacity and overall performance.

E.2 RESCAW-BASED UNIFORM QUANTIZATION

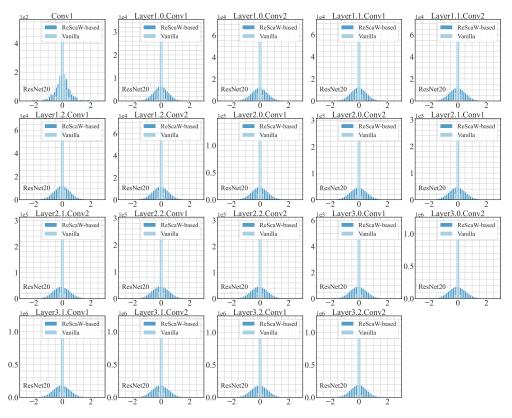


Figure 9: Weight distribution: ReScaW-based uniform quantization, ResNet20, CIFAR-100.

We also present a comparison of weight distributions between vanilla uniform quantization and ReScaW-based uniform quantization across multiple datasets and architectures. The weight distribution of ResNet20 on CIFAR-100 is presented in Figure 9, VGG-16 on TinyImageNet is illustrated in Figure 10, and VGG-SNN on DVS-CIFAR10 is displayed in Figure 11. These three figures clearly demonstrate that the weight distribution using ReScaW-based quantization is broader than that of vanilla uniform quantization, indicating the more efficient bit-width utilization of our ReScaW.

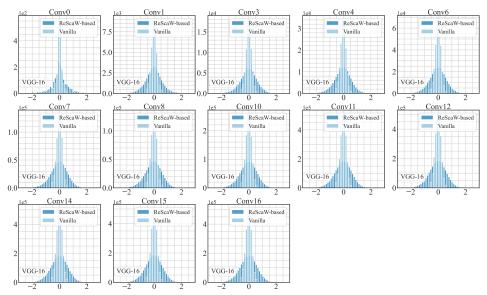


Figure 10: Weight distribution: ReScaW-based uniform quantization, VGG-16, TinyImageNet.

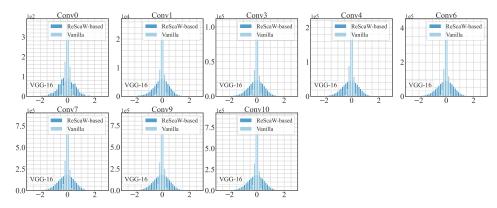


Figure 11: Weight distribution: ReScaW-based uniform quantization, VGGSNN, DVS-CIFAR10.

F COMPLETE IMPORTANCE SCORE COMPARISON

F.1 SCA-BASED PRUNING CRITERION

We present the convolutional kernel scores of models using the SCA criterion across different architectures and datasets, including ResNet20 on CIFAR100, VGG-16 on TinyImageNet, and VGGSNN on DVS-CIFAR10. Note that we only display the layers that perform pruning operations, and the colors in these figures represent the value of the importance score. Moreover, to intuitively reflect the robustness of the pruning criterion to input samples, we compute the average cosine similarity of kernel scores between pairs of input batches for each layer in every model. The calculation for the average cosine similarity of *l*-th layer is outlined as,

$$AvgCosS_{l} = \frac{2}{N_{B}(N_{B} - 1)} \sum_{i < j} \frac{\sum_{f} Score_{i}(\mathbf{W}^{l,f}) \cdot Score_{j}(\mathbf{W}^{l,f})}{\sqrt{\sum_{f} Score_{i}(\mathbf{W}^{l,f})^{2}} \cdot \sqrt{\sum_{f} Score_{j}(\mathbf{W}^{l,f})^{2}}}$$
(18)

where N_B is the number of input batches and $Score_i$ is the kernel score for input batch i.

The kernel scores for ResNet20 on CIFAR-100 are presented in Figure 12. It can be seen from this figure that the SCA-based pruning criterion yields varying scores for the same kernel when processing different input samples. Furthermore, we calculated AvgCosS_l for each layer in ResNet20, and the $\min_l \text{AvgCosS}_l$ is 0.870. This indicates that the SCA criterion is not robust enough to inputs.

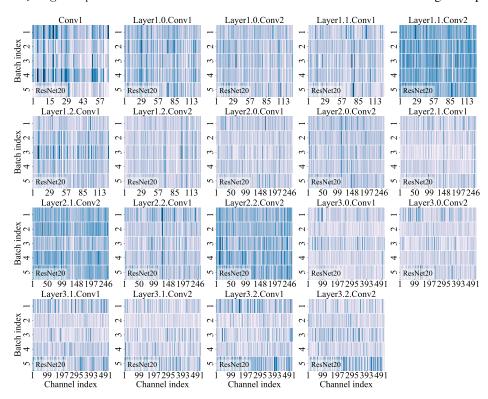


Figure 12: Kernel scores: SCA-based pruning criterion, ResNet20, CIFAR-100.

The kernel scores for VGG-16 on TinyImagenet are illustrated in Figure 13. We calculate $AvgCosS_l$ for each layer in VGG-16, and obtain the $min_l AvgCosS_l$ is 0.879. In this structure, the kernel scores' fluctuation with inputs is slightly better compared to ResNet20, but still not negligible.

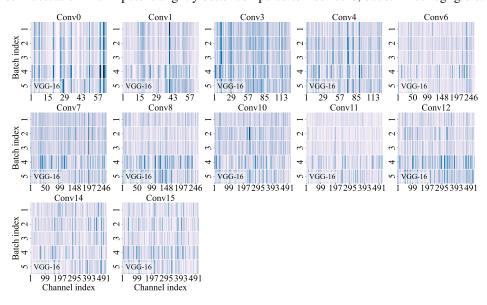


Figure 13: Kernel scores: SCA-based pruning criterion, VGG-16, TinyImageNet.

 The kernel scores for VGGSNN on DVS-CIFAR-10 are displayed in Figure 14. As can be seen from the figure, The kernel score's fluctuation with input data is better compared to both ResNet and VGG-16, but in deeper layers, the fluctuation is higher. We also calculate AvgCosS_l for each layer in VGGSNN, and the $\min_l \text{AvgCosS}_l$ is 0.952.

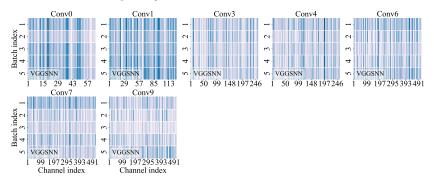


Figure 14: Kernel scores: SCA-based pruning criterion, VGGSNN, DVS-CIFAR10.

These results demonstrate that the SCA-based pruning criterion yields varying scores for the same kernel when processing different input sample, demonstrating low robustness to input samples. This sensitivity to inputs suggests that the criterion may fail to accurately identify critical convolutional kernels within SNNs, potentially impacting the reliability of the pruning process.

F.2 SVS-BASED PRUNING CRITERION

We also depict kernel scores using the SVS pruning criterion. The kernel score for ResNet20 on CIFAR-100 in Figure 15, VGG-16 on TinyImagenet in Figure 16, and VGGSNN on DVS-CIFAR10 in Figure 17. We still only display the layers that perform pruning operation. In VGG-16, ResNet20, and VGGSNN, the $\min_l \mathrm{AvgCosS}_l$ values are 0.997, 0.993, and 1.000 respectively, which exceed the corresponding $\min_l \mathrm{AvgCosS}_l$ when using the SCA-Based pruning criterion by 13.4%, 14.1%, and 5.0%, respectively. The results demonstrate that the SVS-based pruning criterion yields consistent evaluations, with only minor variations between different input samples. This high robustness to input samples enables QP-SNN to effectively identify and eliminate redundant kernels.

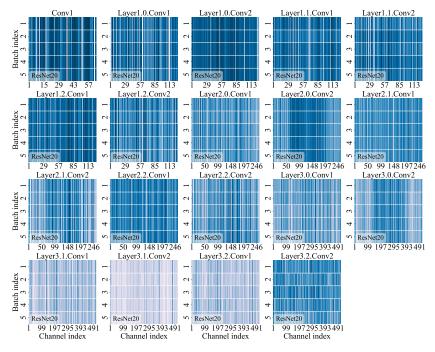


Figure 15: Kernel scores: SVS-based pruning criterion, ResNet20, CIFAR-100.

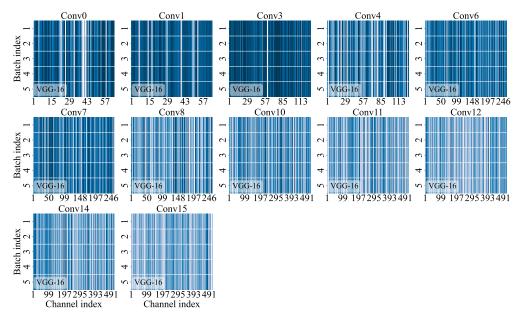


Figure 16: Kernel scores: SVS-based pruning criterion, VGG-16, TinyImageNet.

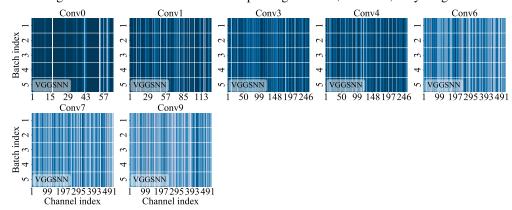


Figure 17: Kernel scores: SVS-based pruning criterion, VGGSNN, DVS-CIFAR10.

G EXPERIMENT

Datasets We evaluate our method on image classification datasets, including static datasets CIFAR-10 (Krizhevsky et al. (2009)), CIFAR-100 (Krizhevsky et al. (2009)), TinyImageNet (Deng et al. (2009)), ImageNet-1k (Deng et al. (2009)), and the neuromorphic dataset DVS-CIFAR10 Li et al. (2017). Before introducing the experiment setups, we briefly outline each dataset. The CIFAR-10 and CIFAR-100 are color image datasets, with each dataset containing 50,000 training images and 10,000 testing images. Each image features 3 color channels and a spatial resolution of 32×32 pixels. CIFAR-10 is composed of 10 categories, whereas CIFAR-100 comprises 100 categories. During the preprocessing process of CIFAR datasets, we apply the commonly used data augmentation techniques (Cubuk et al. (2018); DeVries (2017)). The TinyImageNet dataset is a subset of the ImageNet dataset, consisting of 200 categories, with each category containing 500 training images and 50 test images. Each image has 3 color channels and a spatial resolution of 64×64 pixels. The ImageNet-1K dataset is a large-scale dataset commonly used for computer vision tasks. It spans 1000 classes and contains around 1.3 million training images and 50,000 validation images. The DVS-CIFAR10 is a neuromorphic dataset captured using Dynamic Vision Sensor (DVS) event cameras. It is the most challenging neuromorphic dataset, featuring 9,000 training samples and 1,000 testing samples, featuring a spatial resolution of 128×128 . During the preprocessing process of the DVS-CIFAR10 dataset, we apply the data augmentation technique proposed in (Li et al. (2022)).

Experimental Setups We summarize the training hyperparameters for each dataset in Table 8, including time step, image resolution, optimizer, and other factors. Additionally, we present the network architectures and the corresponding pruning rates for each module in Table ($9\sim11$). In our experiments, we directly utilize the classification head after completing the convolution operations. Therefore, we do not prune the output channels of the last convolutional layer to preserve the integrity of the classification head. Note that the pruning rates used in our experiments are manually selected, without rigorous design or the application of parameter search methods.

Table 8: Experimental setups.

CIFAR-10/100	TinyImageNet	ImageNet	DVS-CIFAR10
2, 4	4	4	10
32×32	64×64	224×224	48×48
256	256	256	64
300 / 150	300 / 150	320 / 200	300 / 150
SGD / Adam	SGD / Adam	SGD / SGD	SGD / Adam
0.1 / 0.001	0.1 / 0.001	0.1 / 0.05	0.1 / 0.001
Cosine	Cosine	Cosine	Cosine
	2, 4 32×32 256 300 / 150 SGD / Adam 0.1 / 0.001	2, 4 4 32×32 64×64 256 256 300 / 150 300 / 150 SGD / Adam 0.1 / 0.001 0.1 / 0.001	2, 4 4 4 4 32×32 64×64 224×224 256 256 256 300 / 150 300 / 150 320 / 200 SGD / Adam SGD / Adam SGD / SGD 0.1 / 0.001 0.1 / 0.005

Table 9: Detailed network architecture and the channel pruning ratio for VGG-16.

	Table 9. Deta	ineu netwo	TK architect	Channel Pruning Ratio Channel Pruning Ratio							
T	Danalosti : ::	Chana 1	Marshall	CIEA					N		
Layer	Resolution	Channel	Module		R-10		R-100		ageNet		
				4.25M	1.42M	2.31M	1.68M	4.65M	3.43M		
1	H imes W	64	Conv -BN-LIF	0.45	0.49	0.45	0.45	0.45	0.45		
2	$H \times W$	64	QConv -BN-LIF	0.45	0.49	0.45	0.45	0.45	0.45		
3	-		MaxPool				_				
4	$\frac{H}{2} \times \frac{W}{2}$	128	QConv -BN-LIF	0.45	0.49	0.45	0.45	0.45	0.45		
5	$\frac{H}{2} \times \frac{W}{2}$	128	QConv -BN-LIF	0.45	0.49	0.45	0.45	0.45	0.45		
6	-		MaxPool			-	-				
7	$\frac{H}{4} \times \frac{W}{4}$	256	QConv -BN-LIF	0.45	0.49	0.45	0.45	0.45	0.45		
8	$\frac{H}{4} \times \frac{W}{4}$	256	QConv -BN-LIF	0.45	0.49	0.45	0.45	0.45	0.45		
9	$\frac{H}{4} \times \frac{W}{4}$	256	QConv -BN-LIF	0.45	0.49	0.45	0.45	0.45	0.45		
10	-		MaxPool	-							
11	$\frac{H}{8} \times \frac{W}{8}$	512	QConv -BN-LIF	0.51	0.8	0.7	0.78	0.51	0.62		
12	$\frac{H}{8} \times \frac{W}{8}$	512	QConv -BN-LIF	0.51	0.8	0.7	0.78	0.51	0.62		
13	$\frac{H}{8} \times \frac{W}{8}$	512	QConv -BN-LIF	0.51	0.8	0.7	0.78	0.51	0.62		
14	-		MaxPool				-				
15	$\frac{H}{16} \times \frac{W}{16}$	512	QConv -BN-LIF	0.51	0.8	0.7	0.78	0.51	0.62		
16	$\frac{H}{16} \times \frac{W}{16}$	512	QConv -BN-LIF	0.51	0.8	0.7	0.78	0.51	0.62		
17	$\frac{H}{16} \times \frac{W}{16}$	512	QConv -BN-LIF	-	-	-	-	-	-		

Table 10: Detailed network architecture and the channel pruning ratio for ResNet20.

Layer	Resolution	Channel	Module	CIFAR-	10 / 100	
				O.1	3.87M / 3.92M	
conv0	$H \times W$	64	Conv-BN-LIF	0.1	0.1	
Layer1.0	$H \times W$	128	QConv-BN-LIF	0.3	0.35	
Layer1.0	11 × VV	120	QConv-BN-LIF	0.3	0.35	
Layer1.1	$H \times W$	128	QConv-BN-LIF	0.6	0.75	
Layer1.1	11 ~ **	120	QConv-BN-LIF	onv-BN-LIF 0.3 onv-BN-LIF 0.3 onv-BN-LIF 0.6 onv-BN-LIF 0.3 onv-BN-LIF 0.6 onv-BN-LIF 0.6	0.35	
Layer1.2	$H \times W$	128	QConv-BN-LIF	0.6	0.75	
Layer1.2		120	QConv-BN-LIF	0.3	0.35	
Layer2.0	$\frac{H}{2} imes \frac{W}{2}$	256	QConv-BN-LIF	0.6	0.75	
Layer2.0		$\frac{2}{2} \wedge \frac{2}{2}$	QConv-BN-LIF	0.6	0.75	
Layer2.1	$\frac{H}{2} \times \frac{W}{2}$	256	QConv-BN-LIF	0.6	0.75	
LayC12.1	$\frac{1}{2}$ \wedge $\frac{1}{2}$	230	QConv-BN-LIF	0.6	0.75	
Layer2.2	$\frac{H}{2} \times \frac{W}{2}$	256	QConv-BN-LIF	0.6	0.75	
Layci2.2	$\frac{1}{2}$ \wedge $\frac{1}{2}$	250	QConv-BN-LIF	0.6	0.75	
Layer3.0	$\frac{H}{4} \times \frac{W}{4}$	512	QConv-BN-LIF	0.6	0.75	
Layers.0	$\frac{1}{4}$ $\stackrel{\wedge}{4}$	312	QConv-BN-LIF	-	-	
Layer3.1	$\frac{H}{4} \times \frac{W}{4}$	512	QConv-BN-LIF	0.6	0.75	
Layers.1	$\frac{1}{4} \times \frac{1}{4}$	$\frac{1}{4} \times \frac{1}{4}$ 312	QConv-BN-LIF	-	-	
Layer3.2	$\frac{H}{4} \times \frac{W}{4}$	512	QConv-BN-LIF	0.6	0.75	
LayCI3.2	$\frac{1}{4} \times \frac{1}{4}$	$\frac{1}{4} \times \frac{1}{4}$	$1 \times \frac{1}{4}$ 312	QConv-BN-LIF	-	-

Table 11: Detailed network architecture and the channel pruning ratio for VGGSNN.

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			Channel Pruning Ratio				
Layer	Resolution	Channel	Module	DVS-CIFAR10			
				1.46M	0.9M	0.25M	
1	$H \times W$	64	Conv-BN-LIF	0.5	0.5	0.82	
2	$H \times W$	128	QConv-BN-LIF	0.5	0.5	0.82	
3	-		MaxPool	-			
4	$\frac{H}{2} \times \frac{W}{2}$	256	QConv-BN-LIF	0.5	0.5	0.82	
5	$\frac{\bar{H}}{2} imes \frac{\bar{W}}{2}$	256	QConv-BN-LIF	0.7	0.8	0.93	
6	-		MaxPool		-		
7	$\frac{H}{4} \times \frac{W}{4}$	512	QConv-BN-LIF	0.7	0.8	0.93	
8	$\frac{\dot{H}}{4} \times \frac{\dot{W}}{4}$	512	QConv-BN-LIF	0.7	0.8	0.93	
9	-		MaxPool		-		
10	$\frac{H}{8} \times \frac{W}{8}$	512	QConv-BN-LIF	0.7	0.8	0.93	
11	$\frac{\tilde{H}}{8} imes \frac{\tilde{W}}{8}$	512	QConv-BN-LIF	-	-	-	

Model size calculation The model size is computed by aggregating the storage requirements of both quantized and full precision parameters, as expressed by the following equation (Qin et al. (2022); Zhang et al. (2022)),

$$M = \text{Params} \times \text{Bitwidth} = \sum P_q \times B_q + \sum P_{fp} \times B_{fp}, \tag{19}$$

where P_q and P_{fp} denote the quantized parameters and full precision parameters, respectively, while B_q and B_{fp} represent their corresponding bit widths. It is important to note that, in our experiments, full-precision weights are employed in both the initial convolutional layer and the final fully connected layer to ensure optimal performance (Zhang et al. (2021); Ding et al. (2022)). We also take this configuration into account when calculating our model size.