# IMPROVED DENSITY RATIO ESTIMATION FOR EVALUATING SYNTHETIC DATA QUALITY

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#### ABSTRACT

High-quality synthetic data is essential for accurate downstream analysis. Density Ratio Estimation (DRE) has emerged as a powerful tool for evaluating synthetic data quality. However, existing DRE methods are highly sensitive to hyperparameter selection, where suboptimal choices lead to poor convergence rates and degraded empirical performance. To mitigate this, we propose a novel model aggregation algorithm for DRE that trains multiple models with diverse hyperparameter configurations and combines their outputs. Our approach achieves fast convergence without requiring prior knowledge of the unknown density ratio smoothness and is minimax optimal for the squared loss. We demonstrate that our method enhances the performance of established DRE techniques across benchmark datasets, achieving state-of-the-art results on MiniDomainNet and Amazon Reviews.

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#### 1 INTRODUCTION

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In the field of synthetic data evaluation, three primary categories of utility measures have been iden-027 tified by Drechsler & Haensch (2024): Fit-for-purpose measures, analysis-specific utility measures, 028 and global utility measures. Fit-for-purpose measures primarily assess the univariate distributions 029 of observed and synthetic data, often employing visualization techniques or goodness-of-fit tests. While these measures offer an initial assessment of the synthesis model's performance, their scope 031 is inherently limited, as they typically examine only one or two variables at a time. To capture more complex relationships, analysis-specific utility measures evaluate whether analyses conducted on 033 synthetic data yield results comparable to those obtained from the original data. For instance, these measures can assess the similarity of regression model coefficients (Karr et al., 2006) or compare the predictive performance of models trained on synthetic versus observed data based on relevant evaluation metrics. However, a key limitation of analysis-specific utility measures is their lack of generalizability, strong utility for one analysis does not necessarily imply high utility for another. 037

038 Global utility measures offer a potential solution to the limitations of previous approaches by assessing the divergence between the entire multivariate distributions of the observed and synthetic data. 040 Consequently, they represent one of the most promising classes of utility measures, as the closer the multivariate distributions of the observed and synthetic data, the more similar the results of any 041 subsequent analyses are expected to be. Global utility is typically quantified using divergence met-042 rics, such as the Kullback-Leibler divergence, or by determining whether a classification model can 043 effectively distinguish between observed and synthetic data, a method known as propensity score 044 mean squared error (pMSE) (Snoke et al., 2018). Despite their advantages, global utility measures are often criticized for being overly general (Drechsler, 2022). Their outputs can be difficult to in-046 terpret and provide limited insight into specific regions where the synthetic data fail to accurately 047 capture the characteristics of the true data. 048

To address the limitations associated with conventional global utility measures, Volker et al. (2024) recently proposed density ratio estimation (DRE) as an alternative approach for utility assessment. Let  $\{x_m\}_{m=1}^M$  and  $\{x_n\}_{n=1}^N$ ,  $M, N \in \mathbb{N}$  be two samples that are independently and identically distributed (i.i.d.) according to two probability density functions p and q, respectively. Then the objective of DRE is to learn the density ratio  $\beta(x) := \frac{p(x)}{q(x)}$  from the samples, see Figure 1 (Left) for an illustration. Conceptually, when two datasets exhibit similar multivariate distributions, the



Figure 1: Left: Density ratio  $\beta = \frac{p}{q}$  between Normal distribution  $p = \mathcal{N}(0, 0.5)$  and  $q = \mathcal{N}(0, 1)$ . Right: Procedures for selecting a single Model 1–3 (dashed) cannot approximate  $\beta$  well. In contrast, our aggregation strategy (solid) achieves a good approximation.

density ratio remains approximately equal to 1 across the data range. Conversely, if the distributions of the observed and synthetic data diverge significantly, the density ratio deviates substantially from 1 in regions where discrepancies between the distributions are most pronounced.

However, the performance of DRE methods is highly sensitive to the choice of hyperparameters, and poorly chosen hyperparameters often result in suboptimal convergence rates and degraded empirical performance, see Figure 1 (Right) for a simplified example. In this work, we therefore study the problem of resolving hyperparameter choice issues for DRE methods.

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## 2 RELATED WORK

Global utility measures are commonly used to quantify the degree of distributional similarity between observed and synthetic data samples. One effective approach for assessing this similarity involves evaluating whether a classification model can reliably differentiate between samples from the two distributions. If a classification model achieves high accuracy in distinguishing between observed and synthetic data, it indicates a low level of distributional similarity, thereby implying reduced global utility. The propensity score mean squared error (pMSE) introduced by Woo et al. (2009) provides a formalized metric for capturing this relationship. Let  $\{x_m\}_{m=1}^M, \{x_n\}_{n=1}^N$  be a real and synthetic dataset respectively, and  $s(x_i)$  the predicted probability of a classifier that a datapoint  $x_i$  is synthetic. Then

$$pMSE = \frac{1}{M+N} \sum_{i=1}^{M+N} \left( s(x_i) - \frac{N}{M+N} \right).$$

094 Snoke et al. (2018) extended this approach by comparing the pMSE value with its expected value un-095 der the null hypothesis that the real and synthetic data are indistinguishable. In addition to the pMSE, 096 various alternative measures can be derived from the estimated propensity scores. These include the percentage of correctly classified records (Raab et al., 2021) and the Kolmogorov-Smirnov statis-098 tic (Bowen et al., 2021), both of which exhibit a strong correlation with the pMSE. Drechsler (2022) 099 demonstrated that the utility score is highly sensitive to the choice of the propensity score model, emphasizing that substantial improvements in synthetic data generation models may not always be 100 reflected in the pMSE. Furthermore, selecting an appropriate propensity score model presents chal-101 lenges, as common issues in model selection, such as the bias-variance trade-off, remain relevant. 102

An alternative approach to quantifying distributional similarity is by utilizing the Kullback-Leibler
 (KL) divergence which is approximated by density estimation techniques (Karr et al., 2006; Wang et al., 2009). However, density estimation is one of the most challenging tasks in statistical learning, inherently introducing estimation errors, particularly in high-dimensional settings (Sugiyama et al., 2012a). These errors become further exacerbated when computing the ratio of estimated densities, as inaccuracies in both density estimates magnify during the division process. Direct DRE mitigates

this issue by modeling and estimating the density ratio directly, without the need for separate density estimations.

Recognizing this advantage, Volker et al. (2024) proposed the use of DRE for assessing data utility. Thereby, they can evaluate global utility by calculating some f-divergence between the real and synthetic data distributions. Moreover, using a density ratio estimator also allows for evaluating local utility by using point evaluations  $\beta(x_i) := \frac{p(x_i)}{q(x_i)}$ . It was first observed by Sugiyama et al. (2012b) that a broad class of methods for DRE use the objective

$$f_{\mathcal{H}} := \operatorname*{arg\,min}_{f \in \mathcal{H}} B_F(\beta, g(f)) \tag{1}$$

and derive the desired density ratio estimator by  $\beta_{\mathcal{H}} := g(f_{\mathcal{H}})$ , where  $g : \mathbb{R} \to \mathbb{R}$  is a strictly increasing function and

$$B_F\left(\beta,\widehat{\beta}\right) := \mathbb{E}_{x \sim Q}[F(\beta(x)) - F(\widehat{\beta}(x)) - F'(\widehat{\beta}(x))[\beta(x) - \widehat{\beta}(x)]]$$

denotes the Bregman divergence with prescribed generator  $F : \mathbb{R} \to \mathbb{R}$ , and  $\mathcal{H}$  a given model class. Consider the following example (cf. Sugiyama et al. (2012b); Menon & Ong (2016); Zellinger et al. (2023)):

#### 127 Example 1.

- 1. As shown in Kanamori et al. (2012b) the kernel unconstrained least squares importance fitting procedure (KuLSIF) (Kanamori et al., 2009) is realized by using  $F(x) = (x-1)^2/2$  and g(x) = x in equation (1) such that  $B_F(\beta, g(f)) = \frac{1}{2} ||\beta g(f)||_{L^2(Q)}$ .
- 2. Menon & Ong (2016) use  $F(x) = x^{3/2}$  and  $g(x) = e^{2x}$  in equation (1) to obtain the exponential function approach (Exp) as applied for AdaBoost (Freund et al., 1996).
  - 3. The square loss approach (SQ) in Menon & Ong (2016) uses  $F(x) = \frac{1}{2x+2}$  and  $g(x) = \frac{-1+2x}{2x+2}$ .

4. To realize the logistic regression (Nelder & Wedderburn, 1972) (LR) approach as used in Bickel et al. (2009)  $F(x) = x \log(x) - (1+x) \log(1+x)$  and  $g(x) = e^x$  are set in equation 1.

All these methods share hyperparameter choice issues which we approach by model aggregation as explained in the next section in more detail.

#### 3 Method

#### Algorithm 1 DRE Aggregation

**Input:** *K* different hyperparameter setups, dataset  $\{(x_n, y_n)\}_{n=1}^{M+N} \stackrel{\text{iid}}{\sim} \rho$ . **Output:** Aggregation  $\hat{\beta}(x) = g\left(\sum_{k=1}^{K} \hat{\alpha}_k f_k(x)\right)$  with optimal coefficients  $\hat{\alpha} := (\hat{\alpha}_1, \dots, \hat{\alpha}_K) \in \mathbb{R}^K$ . **Step 1:** Train one model  $\{\beta_k\}_{k=1}^K$  for each hyperparameter setup (e.g., by a method in Example 1) and denote by  $f_k = g^{-1}(\beta_k)$  the associated binary classifiers. **Step 2:** Compute aggregation weights  $\hat{\alpha} = \hat{\mathbf{G}}^{-1}\hat{\mathbf{r}}$  with empirical Gram matrix  $\hat{\mathbf{G}}$  and inner product vector  $\hat{\mathbf{r}}$  by  $\hat{\mathbf{G}} = \left(\frac{1}{M+N}\sum_{n=1}^{M+N} h(x_n, y_n)f_k(x_n)f_j(x_n)\right)_{k,j=1}^K \hat{\mathbf{r}} = \left(\frac{1}{M+N}\sum_{n=1}^{M+N} h(x_n, y_n)f_n(x_n)y_n\right)_{k=1}^K$  with Hessian h(x, y) depending on the chosen binary loss, see Appendix B for the example of LR. **Return:** Aggregation  $\hat{\beta}(x) = g\left(\sum_{k=1}^K \hat{\alpha}_k f_k(x)\right)$ .

162 **Notation** Following Menon & Ong (2016) the optimization problem (1) can be equivalently for-163 mulated as binary classification with loss function  $\ell: \mathcal{Y} \times \mathbb{R} \to \mathbb{R}$  and  $\mathcal{Y} := \{-1, 1\}$ , such that 164  $\ell(1, f(x))$  and  $\ell(-1, f(x))$  measure the error of a classifier f(x) predicting whether x is originating from P or Q. For this, we only need the assumption that the combined sample  $\{x_m\}_{m=1}^M \cup \{x_n\}_{n=1}^N$ 165 is an i.i.d. sample from the distribution  $\rho$  constructed as follows (Zellinger et al., 2023): it is defined 166 as a probability measure on  $\mathcal{X} \times \mathcal{Y}$  with conditionals  $\rho(x|y=1) := p(x), \rho(x|y=-1) := q(x),$ 167 and, marginal  $\rho_{\mathcal{V}}$  defined as Bernoulli measure such that the probability for both events y = 1, y =168 -1 is  $\frac{1}{2}$ . Then the optimization problem (1) is equivalent to the minimization (Menon & Ong, 2016) 169 170

$$f_{\mathcal{H}} := \operatorname*{arg\,min}_{f \in \mathcal{H}} \mathcal{R}(f) \tag{2}$$

with expected risk

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$$\mathcal{R}(f) := \int_{\mathcal{X} \times \mathcal{Y}} \ell(y, f(x)) d\rho(x, y)$$

and the density ratio estimator  $\beta_{\mathcal{H}} := g(f_{\mathcal{H}})$  can be recovered from the classifier  $f_{\mathcal{H}}$ . For instance, all the methods discussed in Example 1 can be optimized through risk minimization (2) by using the corresponding loss functions.

**Problem** Given a finite number  $\beta_1, \ldots, \beta_K : \mathcal{X} \to \mathbb{R}$  of density ratio models, each trained with a different hyperparameter setting, the goal is to find a model  $\hat{\beta} : \mathcal{X} \to \mathbb{R}$  with minimal error  $B_F(\beta, \hat{\beta})$ .

**Approach** We approach the problem by a linear aggregation of models

$$\widehat{\beta} := g\left(\sum_{k=1}^{K} \alpha_k f_k\right) \tag{3}$$

with  $f_k := g^{-1}(\beta_k)$  being the binary classifier associated to the density ratio estimator  $\beta_k$  and the aggregation weights  $\alpha_1, \ldots, \alpha_K$  which we compute as follows.

First, we follow Menon & Ong (2016) and Marteau-Ferey et al. (2019) to bound the Bregman divergence in equation 1 by a norm (cf. Zellinger et al. (2023) for this strategy)

$$B_F(\beta,\widehat{\beta}) - B_F(\beta,g(f_{\mathcal{H}})) = 2(\mathcal{R}(f) - \mathcal{R}(f_{\mathcal{H}})) \le 2 \cdot \left\|g^{-1}(\widehat{\beta}) - f_{\mathcal{H}}\right\|^2$$

with some norm  $\|.\|$  that depends on the choices F and g, see Appendix B for its derivations. Our approach is to choose the aggregation weights  $\alpha_1, \ldots, \alpha_k$  that minimize this upper bound

$$\min_{\alpha_1,\dots,\alpha_K \in \mathbb{R}} \left\| \sum_{k=1}^K \alpha_k f_k - f_{\mathcal{H}} \right\|^2$$
(4)

which has two advantages: (a) an analytic solution by functional least-squares and (b) fast provableconvergence rate for estimators.

Functional least squares aggregation A necessary optimality condition for equation 4 leads to
 the solution (Chen et al., 2015; Dinu et al., 2023)

$$L(\alpha) := \left\| \sum_{k=1}^{K} \alpha_k f_k - f_{\mathcal{H}} \right\|^2 = \left\langle \sum_{k=1}^{K} \alpha_k f_k - f_{\mathcal{H}}, \sum_{k=1}^{K} \alpha_k f_k - f_{\mathcal{H}} \right\rangle$$

$$=\sum_{k,j=1}^{\infty}\alpha_k\alpha_j\,\langle f_k,f_j\rangle-2\sum_{k=1}^{\infty}\alpha_k\,\langle f_k,f_{\mathcal{H}}\rangle+\langle f_{\mathcal{H}},f_{\mathcal{H}}\rangle$$

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$$\frac{\partial L(\alpha)}{\partial \alpha_k} = 2\left(\sum_{k=1}^{K} \alpha_k \langle f_k, f_j \rangle - \langle f_k, f_{\mathcal{H}} \rangle\right) = 0$$

 $\alpha = \mathbf{G}^{-1}\mathbf{r}$ 

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with  $\mathbf{G} = (\langle f_k, f_j \rangle)_{k,j=1}^K$ ,  $\mathbf{r} = (\langle f_k, f_H \rangle)_{i=1}^K$ . After discretization, we arrive at Algorithm 1.

**Relation to model selection methods** In the continuous case (i.e., with access to p, q), our aggregation strategy is at least as good as model selection:

$$\min_{\alpha_{1},...,\alpha_{K}\in\mathbb{R}}\left\|\sum_{k=1}^{K}\alpha_{k}f_{k}-f_{\mathcal{H}}\right\|^{2} \leq \min_{\alpha_{1},...,\alpha_{k}\in\{0,1\}}\left\|\sum_{k=1}^{K}\alpha_{k}f_{k}-f_{\mathcal{H}}\right\|^{2} \leq \min_{k\in\{1,...,K\}}\left\|f_{k}-f_{\mathcal{H}}\right\|^{2}.$$
(5)

Our next result shows that this also holds in the practical case where we only use finite samples from p, q.

**Theorem 1.** Let assumptions 1–4 and technical assumptions from Appendix A be satisfied. Consider K > 1,  $\delta > 0$ ,  $\{\lambda_k\}_{k=1}^K$  as defined in Appendix A and associated  $\widehat{f}^{\lambda_k}$  as in Equation 10. Then we have that for  $\widehat{\beta}$  of Algorithm 1 applied with  $\beta_k := g(\widehat{f}^{\lambda_k})$ :

$$B_F\left(\beta,\widehat{\beta}\right) - B_F(\beta,g(f_{\mathcal{H}})) \le C(M+N)^{-\frac{2r\alpha+\alpha}{2r\alpha+\alpha+1}},\tag{6}$$

with probability at least  $1 - (9 + 2K)\delta$  for sufficiently large M + N and C > 0 independent of M, N.

**Remark 1.** To the best of our knowledge Theorem 1 provides the first provable principled way of achieving minimax optimal convergence rates for a parameter choice procedure in DRE, a full proof can be found in Appendix A.

In the following, we go beyond theoretical convergence results and conduct a comprehensive empirical evaluation of our algorithm across multiple benchmark datasets.

#### 4 EXPERIMENTS

We investigate the performance of our aggregation approach for resolving parameter choice issues within the following areas of application. For all experiments, the real and synthetic data distribution are represented by p and q respectively.

**Datasets with known density ratios** Building upon Kanamori et al. (2012b) we create ten distinct datasets using Gaussian Mixture distributions in a 50-dimensional space. Each, real and synthetic data distribution gets assigned a Gaussian Mixture distribution, see Appendix C for more details.

**Domain Aaptation datasets** To evaluate the effect of our algorithm in large-scale real-world scenarios we conduct experiments involving importance weighting for domain adaptation. Given a source dataset  $\{x'_n\}_{n=1}^{N} \stackrel{\text{iid}}{\sim} Q$  with labels  $\{y_n\}_{n=1}^{N}$  (which represents synthetic data) and a target dataset  $\{x_i\}_{i=1}^{M} \stackrel{\text{iid}}{\sim} P$  without labels (which represents real data), the goal is to learn a model f' with low expected risk  $\mathcal{R}(f') := \mathbb{E}_{(x,y)\sim P}[\ell(y, f'(x))]$  on the target domain without having sampled labels from the target domain. Motivated by Sugiyama et al. (2007) this task can be approached by approximating the density ratio  $\frac{p}{q}$  with estimator  $\hat{\beta}$  and empirical risk minimization such that

$$f' = \operatorname*{arg\,min}_{f \in \mathcal{H}} \frac{1}{N} \sum_{n=1}^{N} \widehat{\beta}(x_n) \ell(y_n, f(x_n)).$$

We evaluate on image, text, and time series datasets, see Appendix C for more details.

Methods To test our aggregation approach we pick four popular representatives of the large class
 of widely used DRE methods that can be modeled as Bregman divergences as in equation (1). For
 this we use the DRE methods presented in Example 1 with cross-validation as hyperparameter selection procedure as a baseline and compare this for each of the four methods against our aggregation
 approach. In the domain adaptation task we evaluate this for 11 different domain adaption methods. We refer to Appendix C for more details.

**Empirical Results** Our proposed aggregation approach consistently outperforms all evaluated DRE methods in experiments involving geometric datasets with known density ratios (Table 1 and benchmark domain adaptation scenarios(Table 2 and Table 4). Notably, model aggregation consis-tently yields superior results compared to non-aggregated baselines, both on geometric datasets and in domain adaptation tasks, when performance is averaged across multiple domain adaptation scenarios. More detailed results, including the performance of individual DRE methods across specific domain adaptation scenarios, are presented in Tables 5-37. Furthermore, our approach achieves new state-of-the-art performance in deep domain adaptation, as demonstrated on the MiniDomainNet and Amazon Reviews benchmarks. We additionally conduct three ablation studies. One shows that our algorithm assigns higher weights to more accurate models (Figure 2), one shows that our algorithm can also be used in a heuristic setting where not all assumption of Theorem 1 hold (Table 3). The final one shows that our algorithm is better than model averaging (Table 3). 

		Geometric Figures										
		Cross-Validation fo	or Binary Classifie	r	Aggregation							
Dataset	KuLSIF	Exp	LR	SQ	KuLSIF	Exp	LR	SQ				
c3,d1.70	$8.616(\pm 0.011)$	$8.322(\pm 0.009)$	$8.840(\pm 0.021)$	$9.170(\pm 0.011)$	8.320(±0.004)	$8.151(\pm 0.011)$	$8.572(\pm 0.016)$	$8.831(\pm 0.011)$				
c2,d1.72	$13.031(\pm 0.005)$	$12.994(\pm 0.015)$	$13.255(\pm 0.013)$	$13.537(\pm 0.027)$	$12.854(\pm 0.007)$	$12.365(\pm 0.011)$	$13.250(\pm 0.009)$	$13.102(\pm 0.019)$				
c2,d1.59	$12.625(\pm 0.005)$	$19.748(\pm 0.037)$	$12.829(\pm 0.014)$	$13.056(\pm 0.015)$	$12.422(\pm 0.010)$	$12.441(\pm 0.042)$	$12.719(\pm 0.012)$	$12.615(\pm 0.011)$				
c1,d1.55	$11.813(\pm 0.007)$	$14.477(\pm 0.103)$	$12.001(\pm 0.023)$	$12.179(\pm 0.013)$	$11.625(\pm 0.004)$	$11.324(\pm 0.018)$	$12.001(\pm 0.015)$	$11.458(\pm 0.010)$				
c2,d1.78	$9.632(\pm 0.003)$	$18.008(\pm 0.069)$	$9.802(\pm 0.035)$	$9.990(\pm 0.006)$	$9.425(\pm 0.013)$	$17.043(\pm 0.015)$	$9.702(\pm 0.023)$	$9.625(\pm 0.007)$				
c2,d1.55	$10.371(\pm 0.007)$	$9.774(\pm 0.019)$	$10.555(\pm 0.059)$	$10.757(\pm 0.023)$	$10.001(\pm 0.002)$	$9.523(\pm 0.010)$	$10.415(\pm 0.039)$	$10.317(\pm 0.019)$				
c3,d1.57	$12.014(\pm 0.003)$	$18.995(\pm 0.126)$	$12.214(\pm 0.037)$	$14.048(\pm 0.029)$	$12.003(\pm 0.007)$	$12.021(\pm 0.008)$	$11.238(\pm 0.013)$	$12.940(\pm 0.018)$				
c2,d1.61	$11.614(\pm 0.004)$	$11.282(\pm 0.034)$	$11.800(\pm 0.008)$	$12.242(\pm 0.007)$	$11.365(\pm 0.003)$	$10.787(\pm 0.013)$	$10.920(\pm 0.008)$	$11.891(\pm 0.007)$				
c3,d1.46	$12.803(\pm 0.009)$	$12.616(\pm 0.008)$	$12.971(\pm 0.007)$	$13.159(\pm 0.006)$	$9.421(\pm 0.003)$	$12.025(\pm 0.010)$	$12.132(\pm 0.004)$	$12.970(\pm 0.004)$				
c1,d1.63	$9.527(\pm 0.006)$	$9.704(\pm 0.009)$	$9.732(\pm 0.014)$	$9.965(\pm 0.015)$	$9.397(\pm 0.008)$	$9.611(\pm 0.011)$	$9.071(\pm 0.007)$	$9.729(\pm 0.009)$				
Avg	$11.205(\pm 0.006)$	$13.392(\pm 0.097)$	$11.400(\pm 0.023)$	$11.810(\pm 0.015)$	$10.683(\pm 0.006)$	$11.529(\pm 0.015)$	$11.002(\pm 0.014)$	$11.348(\pm 0.012)$				

Table 1: Mean and standard deviation (after  $\pm$ ) of twice the Bregman divergence error on the geometrically constructed datasets following Kanamori et al. (2012b) over ten different sample draws from P and Q.

			Doma	in Adaptation: M	liniDomainNet			
	С	ross-Validation fo	or Binary Classifi	er		Aggre	gation	
DA-Method	KuLSIF	Exp	LR	SQ	KuLSIF	Exp	LR	SQ
MMDA	$0.527(\pm 0.009)$	$0.528(\pm 0.011)$	$0.528(\pm 0.012)$	$0.518(\pm 0.010)$	0.536(±0.007)	$0.539(\pm 0.011)$	$0.536(\pm 0.006)$	$0.535(\pm 0.009)$
CoDATS	$0.536(\pm 0.012)$	$0.532(\pm 0.015)$	$0.530(\pm 0.020)$	$0.517(\pm 0.018)$	$0.542(\pm 0.010)$	$0.543(\pm 0.014)$	$0.540(\pm 0.014)$	$0.533(\pm 0.017)$
DANN	$0.531(\pm 0.009)$	$0.522(\pm 0.012)$	$0.520(\pm 0.019)$	$0.506(\pm 0.016)$	$0.536(\pm 0.007)$	$0.535(\pm 0.011)$	$0.526(\pm 0.013)$	$0.519(\pm 0.015)$
CDAN	$0.531(\pm 0.012)$	$0.531(\pm 0.017)$	$0.524(\pm 0.023)$	$0.512(\pm 0.021)$	$0.537(\pm 0.009)$	$0.544(\pm 0.017)$	$0.535(\pm 0.017)$	$0.526(\pm 0.020)$
DSAN	$0.539(\pm 0.011)$	$0.532(\pm 0.015)$	$0.527(\pm 0.015)$	$0.513(\pm 0.013)$	$0.544(\pm 0.009)$	$0.546(\pm 0.014)$	$0.535(\pm 0.009)$	$0.525(\pm 0.012)$
DIRT	$0.517(\pm 0.026)$	$0.386(\pm 0.177)$	$0.520(\pm 0.023)$	$0.509(\pm 0.021)$	$0.523(\pm 0.025)$	$0.395(\pm 0.175)$	$0.526(\pm 0.017)$	$0.525(\pm 0.020)$
AdvSKM	$0.516(\pm 0.006)$	$0.515(\pm 0.009)$	$0.512(\pm 0.012)$	$0.500(\pm 0.010)$	$0.522(\pm 0.005)$	$0.529(\pm 0.008)$	$0.521(\pm 0.006)$	$0.517(\pm 0.008)$
HoMM	$0.531(\pm 0.008)$	$0.529(\pm 0.012)$	$0.521(\pm 0.015)$	$0.505(\pm 0.013)$	$0.539(\pm 0.007)$	$0.544(\pm 0.011)$	$0.529(\pm 0.009)$	$0.528(\pm 0.012)$
DDC	$0.517(\pm 0.010)$	$0.517(\pm 0.013)$	$0.514(\pm 0.012)$	$0.500(\pm 0.010)$	$0.527(\pm 0.008)$	$0.529(\pm 0.012)$	$0.524(\pm 0.008)$	$0.515(\pm 0.009)$
DeepCoral	$0.535(\pm 0.012)$	$0.528(\pm 0.013)$	$0.530(\pm 0.012)$	$0.514(\pm 0.011)$	$0.543(\pm 0.010)$	$0.540(\pm 0.012)$	$0.536(\pm 0.007)$	$0.527(\pm 0.009)$
CMD	$0.529(\pm 0.010)$	$0.524(\pm 0.021)$	$0.521(\pm 0.021)$	$0.510(\pm 0.019)$	$0.536(\pm 0.008)$	$0.538(\pm 0.020)$	$0.527(\pm 0.015)$	$0.521(\pm 0.018)$
Avg.	$0.528(\pm 0.011)$	$0.513(\pm 0.029)$	$0.523(\pm 0.017)$	$0.510(\pm 0.015)$	$0.535(\pm 0.010)$	$0.526(\pm 0.028)$	$0.530 (\pm 0.011)$	$0.525 (\pm 0.014)$

Table 2: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on MiniDomainNet datasets over three different random initialization of model weights and several domain adaptation tasks.

## 5 CONCLUSION

In this work, we proposed an algorithm to resolve hyperparameter choice issues in DRE to improve the evaluation of synthetic data quality. We approach these issues by introducing a novel model aggregation algorithm to DRE that first trains a sequence of models with distinct hyperparameter settings. Subsequently, the respective model outputs are aggregated via a linear combination where the coefficients are optimized such that the algorithm achieves fast convergence rates without requir-ing prior knowledge of the unknown density ratio smoothness and is optimal for square loss. We supported this theoretical result by a comprehensive empirical evaluation on both, benchmarks for DRE and large-scale deep domain adaptation. All experimental results confirm that our algorithm clearly outperforms established DRE methods. Furthermore, on domain adaptation benchmarks, we achieved new state-of-the-art performance on the MiniDomainNet and Amazon Reviews datasets.

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#### THEORETICAL ANALYSIS А

In the following we show that our aggregation approach (3) achieves fast convergence rates when (1) is optimized in some RKHS  $\mathcal{H}$  with norm  $\|.\|_{\mathcal{H}}$  and Tikhonov penalty  $\|f\|_{\mathcal{H}}^2$  as follows

$$f^{\lambda} := \underset{f \in \mathcal{H}}{\operatorname{arg\,min}} \left[ B_F(\beta, g(f)) + \frac{\lambda}{2} \left\| f \right\|_{\mathcal{H}}^2 \right],\tag{7}$$

where  $\lambda > 0$  is the regularization parameter which we aim to choose. All DRE methods in Example 1 fit into the optimization problem (7), see (Zellinger et al., 2023; Gruber et al., 2024). We fix a sequence  $(\lambda_k)_{k=1}^K$  of regularization parameters and refine our aggregation (3) by

$$\widehat{\beta} := g\left(\sum_{k=1}^{K} \alpha_k f^{\lambda_k}\right)$$

511 To prove that our Algorithm 1 achieves fast convergence rates, we introduce a set of assumptions 512 typical in learning theory, such as assumptions on data, the regularity of the underlying problem and 513 the previously introduced loss function  $\ell$ .

514 **Assumption 1.** The loss function  $\ell : \mathcal{Y} \times \mathbb{R} \to \mathbb{R}$  which is used for separating  $\{(x_m, 1)\}_{m=1}^M$  from 515  $\{(x'_n, -1)\}_{n=1}^N$  has an associated link function  $\psi : [0, 1] \to \mathbb{R}$  with the following properties: 516

- $\psi$  is invertible and the associated conditional Bayes risk  $G(u) := u\ell(1, \psi(u)) + (1 \psi(u))$  $u)\ell(-1,\psi(u))$  is twice differentiable,
- the minimizer  $f_{\mathcal{H}}$  satisfies  $f_{\mathcal{H}}(x) = \psi(\rho(y=1|x))$ .

Assumption 2 (source condition). There exist some  $r \in (0, \frac{1}{2}]$ ,  $v \in \mathcal{H}$  satisfying  $f_{\mathcal{H}} = \mathbf{H}(f_{\mathcal{H}})^r v$ 520 for the expected Hessian  $\mathbf{H}(f) := \mathbb{E}_{(x,y) \sim \rho} [\nabla^2 \ell(y, f(x))].$ 521

**Assumption 3** (capacity condition). There exist  $\alpha \geq 1$  and S > 0 such that  $df_{\lambda} \leq S\lambda^{-\frac{1}{\alpha}}$  with the degrees of freedom

$$\mathrm{df}_{\lambda} := \mathbb{E}_{(x,y)\sim\rho} \left[ \left\| \mathbf{H}_{\lambda}(f_{\mathcal{H}})^{-\frac{1}{2}} \nabla \ell(y, f_{\mathcal{H}}(x)) \right\|_{\mathcal{H}}^{2} \right]$$

and  $\mathbf{H}_{\lambda}(f) := \mathbf{H}(f) + \lambda I$ .

529 Both, source and capacity condition, are typically used in learning theory (Caponnetto & De Vito, 530 2007; Bauer et al., 2007; Marteau-Ferey et al., 2019) to encode the regularity of the underlying 531 problem. We also need the following self-concordance assumption (Bach, 2010; Ostrovskii & 532 Bach, 2021) on our loss function, which is known to be satisfied for the examples we discussed 533 (cf. Zellinger et al. (2023)).

534 **Assumption 4** (Pseudo self-concordance). For any  $y \in \mathcal{Y}$ , the function  $\ell_y : \mathbb{R} \to \mathbb{R}$  defined by 535  $\ell_{y}(\eta) := \ell(y, \eta)$  is convex, three times differentiable and satisfies 536

$$\left|\ell_{u}^{\prime\prime\prime}(\eta)\right| \leq \ell_{u}^{\prime\prime}(\eta). \tag{8}$$

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> Note that by Lemma 3 in Gruber et al. (2024), Assumption 4 implies generalized self concordance, which is e.g. commonly employed in Marteau-Ferey et al. (2019); Zellinger et al. (2023). As a next

step we discuss the specific norms that occur in (4) and (5) in more detail, see Appendix B for an example. From Menon & Ong (2016); Marteau-Ferey et al. (2019) we know that

$$B_F(\beta,\widehat{\beta}) - B_F(\beta,g(f_{\mathcal{H}})) \le 2 \left\|\widehat{\beta} - f_{\mathcal{H}}\right\|_{\mathbf{H}_{\lambda}(f_{\mathcal{H}})}^2$$

for  $f_{\mathcal{H}}$ ,  $\mathbf{H}_{\lambda}(f_{\mathcal{H}})$  as in Assumption 2, and

$$\|f\|_{\mathbf{H}_{\lambda}(f_{\mathcal{H}})} := \left\| \mathbf{H}_{\lambda}(f_{\mathcal{H}})^{1/2} f \right\|_{\mathcal{H}}.$$
(9)

However, the norm values  $\|\cdot\|_{\mathbf{H}_{\lambda}(f_{\mathcal{H}})}$  are not directly accessible, as we have only observation from the measure  $\rho$ . That is, we have to estimate the norm to find an approximate solution to the optimization problem (4).

In the following, consider some small regularization parameter value  $\lambda > 0$  (as precisely specified in Section A) and the empirical risk minimizer and empirical Hessian

$$\widehat{\mathbf{H}}_{\lambda}(f) := \frac{1}{M+N} \sum_{n=1}^{M+N} \nabla^{2} \ell(y_{n}, f(x_{n})) + \lambda I,$$

$$\widehat{f}^{\lambda} := \underset{f \in \mathcal{H}}{\operatorname{arg\,min}} \frac{1}{M+N} \sum_{n=1}^{M+N} \ell(y_{n}, f(x_{n})) + \frac{\lambda}{2} \|f\|_{\mathcal{H}}^{2}.$$
(10)

To prove our main theorem, we will need to recall several concentration bounds on weighted norms, which were to a large extend established by Marteau-Ferey et al. (2019). We will need the following technical assumption:

Assumption 5 (technical assumption).

• The kernel k is continuous and bounded  $\sup_{x \in \mathcal{X}} \|k(x, \cdot)\|_{\mathcal{H}} \leq R$ .

• Let  $z = (x, y) \in \mathcal{X} \times \mathcal{Y}$  and denote  $\ell_z(f) = \ell(y, f(x))$ . Then the quantities  $|\ell_z(0)|, \|\nabla \ell_z(0)\|_{\mathcal{H}}, \operatorname{Tr}(\nabla^2 \ell_z(0))$  are almost surely (wrt.  $\rho$ ) bounded.

The first estimate deals with estimates for empirical risk minimizers  $\widehat{f}^{\lambda}$  in weighted norms.

**Lemma 1** (Marteau-Ferey et al. (2019), Theorem 38). Let Assumptions 1–5 be satisfied,  $\delta \in (0, \frac{1}{2}]$ , and define  $B_1^*$ ,  $B_2^*$  and L by

$$B_1^* := \sup_{z \in \operatorname{supp}(\rho)} \operatorname{Tr}(\nabla \ell_z(f_{\mathcal{H}})), \quad B_2^* := \sup_{z \in \operatorname{supp}(\rho)} \operatorname{Tr}(\nabla^2 \ell_z(f_{\mathcal{H}})), \quad L := \|f_{\mathcal{H}}\|_{\mathbf{H}^{-2r}(f_{\mathcal{H}})}.$$

Whenever  $0 < \lambda \leq \min\{B_2^*, (2LR \log \frac{2}{\delta})^{-1/r}, S^{2\alpha}(B_2^*)^{\alpha}(B_1^*)^{-2\alpha}\}$  with S as in Assumption 3 and M + N is larger than

$$\max\left\{5184\frac{B_2^*}{\lambda}\log\left(\frac{8\cdot414^2B_2^*}{\lambda\delta}\right),\frac{1296S^2}{L^2\lambda^{1+2r+1/\alpha}}\right\},$$

then a minimizer  $\widehat{f}^{\lambda}$  of Equation 10 satisfies, with probability at least  $1-2\delta$ ,

$$\mathcal{R}(\hat{f}^{\lambda}) - \mathcal{R}(f_{\mathcal{H}}) \leq \left\| \hat{f}^{\lambda} - f_{\mathcal{H}} \right\|_{\mathbf{H}(f_{\mathcal{H}})}^{2} \leq \left\| \hat{f}^{\lambda} - f_{\mathcal{H}} \right\|_{\mathbf{H}_{\lambda}(f_{\mathcal{H}})}^{2}$$

$$\leq 414 \frac{S^{2}}{(M+N)\lambda^{1/\alpha}} \log\left(\frac{2}{\delta}\right) + 414L^{2}\lambda^{1+2r} =: S(M+N,\delta,\lambda) + A(\lambda).$$
(11)

Next we use similar arguments as in Zellinger et al. (2023) to construct an admissible sequence of
regularization parameters and associated regularized estimators, which we want to aggregate in the
end. The same reasoning as used in the well known Lepskii balancing principle (Lepskii, 1991;
Goldenshluger & Pereverzev, 2000; Birgé, 2001; Mathé, 2006; De Vito et al., 2010; Mücke, 2018;
Blanchard et al., 2019; Lu et al., 2020; Zellinger et al., 2021) will give us, that the minimal (over all admissible values for λ) risk difference to the target even achieves the optimal rate:

**Lemma 2.** Let Assumptions 1–5 be satisfied and let 

$$\lambda_k := \lambda_0 \cdot \xi^k, k \in \{1, \dots, K\}$$

with  $\xi > 1$ ,  $\lambda_0 \leq \xi^{-K} \min \left\{ B_2^*, \left( 2LR \log \frac{2}{\delta} \right)^{-\frac{1}{r}}, S^{2\alpha}(B_2^*)^{\alpha}(B_1^*)^{-2\alpha} \right\}$ ,  $K < \frac{e^{1296}}{4} - 2$  and  $\delta \in [\frac{2}{e^{1296}}, \frac{1}{4+2K}]$ . Moreover, let  $\eta = 1296 \log^{-1}(\frac{2}{\delta})$  and  $\lambda^*$  be the solution of  $\eta S(M+N, \delta, \lambda^*) = 0$  $A(\lambda^*)$ . Then  $\lambda_1, ..., \lambda_K$  and  $\lambda^*$  satisfy the assumptions of the previous Lemma 1 and we have for k = 1, ..., K:

$$\left\|\widehat{f}^{\lambda_k} - f_{\mathcal{H}}\right\|_{\mathbf{H}_{\lambda_k}(f_{\mathcal{H}})}^2 \le S(M+N,\delta,\lambda_k) + A(\lambda_k).$$
(12)

and even more:

$$\min_{1 \le k \le K} \left\| \widehat{f}^{\lambda_k} - f_{\mathcal{H}} \right\|_{\mathbf{H}_{\lambda_k}(f_{\mathcal{H}})}^2 \le C^*(S(M+N,\delta,\lambda^*) + A(\lambda^*)) = C^*(M+N)^{-\frac{2r\alpha+\alpha}{2r\alpha+\alpha+1}}.$$
(13)

with probability at least  $1 - (4 + 2K)\delta$ , for large enough sample size M + N greater than

$$\max\left\{5184\frac{B_2^*}{\lambda_0}\log\left(\frac{8\cdot414^2B_2^*}{\lambda_0\delta}\right), \frac{1296S^2}{L^2\lambda_0^{1+2r+1/\alpha}}\right\}$$
(14)

equation 14 and  $C^* := 16560\xi^{\max(1+2r,1/\alpha)}L^2 \left(\frac{1296S^2}{L^2}\right)^{\frac{\alpha+2r\alpha}{1+2\alpha r+\alpha}}$ .

*Proof.* It has been shown in the proof of Zellinger et al. (2023, Theorem 1) that under the given conditions,  $\lambda_k$  for i = 1, ..., K as well as  $\lambda^*$  are admissible according to Lemma 1, which establishes equation 11. Let us now show equation 13. First note that S is a decreasing and A an increasing function with respect to  $\lambda$ , so that  $\lambda^*$  is a minimizer of S + A. Due to the structure of S + A, it is also clear that there is an index  $1 \le j \le K$  with  $\lambda_j \le \lambda^* \le \lambda_{j+1}$  so that 

$$\lambda_{\dagger} := \operatorname*{arg\,min}_{\lambda \in \{\lambda_1, \dots, \lambda_K\}} S(M + N, \delta, \lambda) + A(\lambda) \in \{\lambda_j, \lambda_{j+1}\}.$$

We now distinguish two cases: Let us first consider  $\lambda_{\dagger} = \lambda_j$ . Then  $\lambda_{\dagger} \ge \lambda^* \frac{1}{\xi}$  which on the other hand implies  $S(\lambda_{\dagger}) = \frac{B(\delta)}{\lambda_{\dagger}^{1/\alpha}(M+N)} \le B(\delta)(\lambda^*)^{-1/\alpha}\xi^{1/\alpha}(M+N)^{-1} = \xi^{1/\alpha}S(\lambda^*)$  (for  $B(\delta) = 414S^2 \log\left(\frac{2}{\delta}\right)$  and  $A(\lambda_{\dagger}) \leq A(\lambda^*) \leq \xi^{1/\alpha} A(\lambda^*)$ . 

In the second case we assume  $\lambda_{\dagger} = \lambda_{j+1}$ , which yields  $\lambda_{\dagger} \leq \lambda^* \xi$  and therefore  $A(\lambda_{\dagger}) \leq A(\xi \lambda^*) = A(\lambda^*)\xi^{1+2r}$  and also  $S(\lambda_{\dagger}) \leq S(\lambda^*) \leq \xi^{1+2r}S(\lambda^*)$ . Thus in both cases:  $S(\lambda_{\dagger}) + A(\lambda_{\dagger}) \leq S(\lambda^*) = A(\lambda_{\dagger})\xi^{1+2r}$ .  $\xi^{\max(1+2r,1/\alpha)}(S(\lambda^*) + A(\lambda^*))$ , implying equation 13. 

As a next step, let us state some concentration bounds on weighted norms, that relate on the one hand the Hessian norms  $\mathbf{H}_{\lambda}(f)$  evaluated for different  $f \in \mathcal{H}$ , where on the other hand, the connections between empirical and non-empirical Hessian norms are explored. To do so, we will also need to introduce further notation: we write  $\mathbf{B} \preccurlyeq \mathbf{A}$  iff  $\mathbf{A} - \mathbf{B}$  is positive semi-definite. Moreover, we define  $\mathbf{t}(f) := \sup_{(x,y) \in \operatorname{supp}(\rho)} \sup_{g \in \{yk(x,\cdot)\}} |f \cdot g|.$ 

**Lemma 3** (Marteau-Ferey et al. (2019), Proposition 15). Let Assumptions 1–5 be satisfied,  $\lambda \ge 0$ and  $f_1, f_2 \in \mathcal{H}$ . Then, we have 

$$\mathbf{H}_{\lambda}(f_1) \preccurlyeq e^{\mathbf{t}(f_1 - f_2)} \mathbf{H}_{\lambda}(f_2).$$
(15)

Lemma 4 (Marteau-Ferey et al. (2019); Zellinger et al. (2023)). Under the conditions of Lemma 1, we have, with probability at least  $1 - 2\delta$ ,

$$\mathbf{t}(f_{\mathcal{H}} - f^{\lambda}) \le \log(2), \quad \mathbf{t}(f^{\lambda} - \hat{f}^{\lambda}) \le \log(2) \quad \mathbf{t}(f_{\mathcal{H}} - \hat{f}^{\lambda}) \le 2\log(2).$$
(16)

Lemma 5 (Marteau-Ferey et al. (2019), Rudi & Rosasco (2017)). Let the conditions of Lemma 1 be satisfied. Then, it holds, with probability at least  $1 - \delta$ , 

$$\mathbf{H}_{\lambda}(f) \preccurlyeq 2\hat{\mathbf{H}}_{\lambda}(f). \tag{17}$$

If, in addition,  $0 < ||\mathbf{H}(f)||_{\mathcal{H}}$ , then it holds, for all

$$M + N \ge \frac{16B_2^*}{\|\mathbf{H}(f)\|_{\mathcal{H}}} \log\left(\frac{2}{\delta}\right),\tag{18}$$

with probability at least  $1 - \delta$ ,

 $\widehat{\mathbf{H}}_{\lambda}(f) \preccurlyeq \frac{3}{2}\mathbf{H}_{\lambda}(f).$ (19)

We will need another technical assumption in order to apply equation 19 to a sequence of models:

**Assumption 6.** For the sequence  $(\lambda_k)_{k=1}^K$  there exists  $b^*$ 0 with  $b^*$ > $\leq$  $\min_{k \in \{1,\dots,K\}} \left\| \mathbf{H}(\widehat{f}^{\lambda_k}) \right\|_{\mathcal{H}}$ 

We are now in the position to formulate and prove a detailed version of our finite sample bounds for aggregation of empirical DR-estimators:

**Theorem 2.** Let assumptions 1-6 be fulfilled. Consider K > 1 and a sequence  $\lambda_k$  of regularization parameters and associated empirical risk minimizers  $f^{\lambda_k}$  for  $0 \le k \le K$ , as defined in Lemma 2. Let moreover  $\delta \in \left[\frac{2}{e^{1296}}, \frac{1}{9+2K}\right]$ . Then we have that for  $\widehat{\beta}$  of Algorithm equation 1 applied with  $\beta_k := g(\widehat{f}^{\lambda_k}):$ 

$$B_F\left(\beta,\widehat{\beta}\right) - B_F(\beta,g(f_{\mathcal{H}})) \le C(M+N)^{-\frac{2r\alpha+\alpha}{2r\alpha+\alpha+1}},\tag{20}$$

with probability at least  $1 - (9 + 2K)\delta$  for M + N larger than equation 23 and C given by equa-tion 22. 

*Proof.* If the inequalities that we are going to state hold with high probability (under conditions mentioned in the theorem), we will write  $\leq_{\rho}$ . Let us start by following Menon & Ong (2016):

$$B_F\left(\beta, g\left(\sum_{k=1}^K \widehat{\alpha_k} \widehat{f}^{\lambda_k}\right)\right) - B_F(\beta, g(f_{\mathcal{H}})) = 2\left(\mathcal{R}\left(\sum_{k=1}^K \widehat{\alpha_k} \widehat{f}^{\lambda_k}\right) - \mathcal{R}\left(f_{\mathcal{H}}\right)\right).$$

Next we apply equation 11, combine it with equation 15 and equation 16 to obtain:

$$B_F\left(\beta, g\left(\sum_{k=1}^K \widehat{\alpha_k} \widehat{f}^{\lambda_k}\right)\right) - B_F(\beta, g(f_{\mathcal{H}})) \underbrace{\leq_{\rho}}_{(A)} 2 \left\|\sum_{k=1}^K \widehat{\alpha_k} \widehat{f}^{\lambda_k} - f_{\mathcal{H}}\right\|_{\mathbf{H}_{\lambda_0}(f_{\mathcal{H}})}^2 \underbrace{\leq_{\rho}}_{(B)} 8 \left\|\sum_{k=1}^K \widehat{\alpha_k} \widehat{f}^{\lambda_k} - f_{\mathcal{H}}\right\|_{\mathbf{H}_{\lambda_0}(\widehat{f}^{\lambda_0})}^2$$

An application of equation 17 then yields

$$8 \left\| \sum_{k=1}^{K} \widehat{\alpha_{k}} \widehat{f}^{\lambda_{k}} - f_{\mathcal{H}} \right\|_{\mathbf{H}_{\lambda_{0}}(\widehat{f}^{\lambda_{0}})}^{2} \underbrace{\leq_{\rho}}_{(C)} 16 \left\| \sum_{k=1}^{K} \widehat{\alpha_{k}} \widehat{f}^{\lambda_{k}} - f_{\mathcal{H}} \right\|_{\widehat{\mathbf{H}}_{\lambda_{0}}(\widehat{f}^{\lambda_{0}})}^{2}$$
$$= 16 \min_{\alpha_{1}, \dots, \alpha_{K} \in \mathbb{R}} \left\| \sum_{k=1}^{K} \alpha_{k} \widehat{f}^{\lambda_{k}} - f_{\mathcal{H}} \right\|_{\widehat{\mathbf{H}}_{\lambda_{0}}(\widehat{f}^{\lambda_{0}})}^{2}$$
$$\leq 16 \min_{k \in \{1, \dots, K\}} \left\| \widehat{f}^{\lambda_{k}} - f_{\mathcal{H}} \right\|_{\widehat{\mathbf{H}}_{\lambda_{0}}(\widehat{f}^{\lambda_{0}})}^{2}, \qquad (21)$$

where the last inequality follows from equation 5. Next we use that  $\lambda_0 < \lambda_k$  to upper-bound equation 21 by:

$$\min_{k \in \{1,\dots,K\}} \left\| \widehat{f}^{\lambda_k} - f_{\mathcal{H}} \right\|_{\widehat{\mathbf{H}}_{\lambda_0}(\widehat{f}^{\lambda_0})}^2 \le \min_{k \in \{1,\dots,K\}} \left\| \widehat{f}^{\lambda_k} - f_{\mathcal{H}} \right\|_{\widehat{\mathbf{H}}_{\lambda_k}(\widehat{f}^{\lambda_0})}^2.$$

We can further apply equation 19, which is valid due to assumption 6, and moreover, we use equa-tion 15 and equation 16, so that we end up with: 

$$\begin{array}{cccc}
 & 16 \min_{k \in \{1,...,K\}} \left\| \widehat{f}^{\lambda_{k}} - f_{\mathcal{H}} \right\|_{\widehat{\mathbf{H}}_{\lambda_{k}}(\widehat{f}^{\lambda_{0}})}^{2} \underbrace{\leq_{\rho}}_{(D)} 24 \min_{k \in \{1,...,K\}} \left\| \widehat{f}^{\lambda_{k}} - f_{\mathcal{H}} \right\|_{\mathbf{H}_{\lambda_{k}}(\widehat{f}^{\lambda_{0}})}^{2} \underbrace{\leq_{\rho}}_{(E)} 96 \min_{k \in \{1,...,K\}} \left\| \widehat{f}^{\lambda_{k}} - f_{\mathcal{H}} \right\|_{\mathbf{H}_{\lambda_{k}}(f_{\mathcal{H}})}^{2} \underbrace{\leq_{\rho}}_{(F)} C(M + N)^{-\frac{2r\alpha + \alpha}{2r\alpha + \alpha + 1}},
\end{array}$$

 where (F) follows from invoking equation 13 and the constant is given by

$$C := 96C^* = 96 \cdot 16560\xi^{\max(1+2r,1/\alpha)} L^2 \left(\frac{1296S^2}{L^2}\right)^{\frac{\alpha+2r\alpha}{1+2\alpha r+\alpha}},$$
(22)

so that equation 20 is established. Note that by Lemma 5, (F) holds with probability  $1 - (4 + 2K)\delta$ and (A)-(E) all hold with probability  $1-\delta$ , so that equation 20 is valid with probability  $1-(9+2K)\delta$ , yielding the mentioned admissible range for  $\delta$ . Moreover, taking into account the requirements equation 14 and equation 18, we obtain that M + N needs to be at least as large as

$$\max\left\{5184\frac{B_{2}^{*}}{\lambda_{0}}\log\left(\frac{8\cdot414^{2}B_{2}^{*}}{\lambda_{0}\delta}\right), \frac{1296S^{2}}{L^{2}\lambda_{0}^{1+2r+1/\alpha}}, \frac{16B_{2}^{*}}{b^{*}}\log\left(\frac{2}{\delta}\right)\right\}.$$
 (23)

#### DERIVATION OF LOSS AND HESSIAN FOR LR В

Starting with F, g of LR from Example 1 we have

$$F(x) := x \log(x) - (1+x) \log(1+x)$$
$$g(x) := e^x$$

From Theorem 1 from Zellinger (2025) we have

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$$\gamma\left(\psi^{-1}(x)\right) = -F\left(e^{x}\right)\left(1-\psi^{-1}(x)\right) = \frac{x}{1+e^{x}} + \log\left(1+e^{x}\right) - x$$
$$\gamma'(\eta) = \frac{\partial}{\partial\eta}\left(-\left(\frac{\eta}{1-\eta}\log\left(\frac{\eta}{1-\eta}\right) - \left(1+\frac{\eta}{1-\eta}\right)\log\left(1+\frac{\eta}{1-\eta}\right)\right)\left(1-\eta\right)\right)$$
$$= -\log\left(\frac{\eta}{1-\eta}\right)$$

Taking the result for loss function  $\ell(y, x)$  from Zellinger (2025) gives us further after simplifying

$$\ell(-1,x) = \gamma(\psi^{-1}(x)) - \psi^{-1}(x)\gamma'(\psi^{-1}(x))$$

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752 
$$= \frac{x}{1+e^x} + \log(1+e^x) - x - \frac{e^x}{1+e^x}(-x) = \log(1+e^x)$$

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$$\ell(1,x) = \gamma(\psi^{-1}(x)) + (1-\psi^{-1}(x))\gamma'(\psi^{-1}(x))$$

755 
$$= \frac{x}{1+e^x} + \log(1+e^x) - x + \left(1 - \frac{e^x}{1+e^x}\right)(-x) = \log(1+e^{-x})$$

which is the loss function for LR. In the next step we derive the Hessian term h(x, y) used in Algorithm 1. Again, now using model  $\hat{f}^{\lambda_0}$  we get after simplification

$l'(-1, \hat{f}^{\lambda_0}(x)) = \frac{e^{\hat{f}^{\lambda_0}(x)}}{1 + e^{\hat{f}^{\lambda_0}(x)}},$
$l''(-1, \hat{f}^{\lambda_0}(x)) = \frac{e^{\hat{f}^{\lambda_0}(x)}}{(1 + e^{\hat{f}^{\lambda_0}(x)})^2},$
$l'(1, \hat{f}^{\lambda_0}(x)) = -\frac{1}{1 + e\hat{f}^{\lambda_0}(x)},$
$l''(1, \hat{f}^{\lambda_0}(x)) = \frac{e\hat{f}^{\lambda_0}(x)}{(1 + e\hat{f}^{\lambda_0}(x))^2}.$

with the second order derivatives being h(x, y). Other loss functions with respective Hessians can be derived analogously.

## C DETAILS ON EXPERIMENTS

#### C.1 DETAILS ON DATASET WITH KNOWN DENSITY RATIOS

777 To evaluate the accuracy of our aggregation algorithm, we build upon the methodologies proposed 778 by Kanamori et al. (2012b); Nguyen et al. (2010). Specifically, we construct high-dimensional 779 data with precisely known density ratios, enabling a systematic analysis of the estimation accuracy. Our approach extends and generalizes the settings used in prior studies. For instance, widely used datasets such as Ringnorm and Twonorm (Breiman, 1996) represent specific cases of Gaus-781 sian mixture models, where the mean and covariance parameters are set to predefined values for 782 each mixture component. Similarly, the experiments described in Nguyen et al. (2010) can also be 783 framed within a Gaussian mixture model structure. To introduce greater complexity, we generate 784 distributions by randomly sampling the number, weights, and covariances of the mixture compo-785 nents from 50-dimensional space, which exceeds the dimensionality considered in existing studies. 786 More concretely, the means are sampled uniformly from  $[0, 0.5]^{50}$ , while the weights of the mixture 787 components are sampled from [0,1] and subsequently normalized to sum to 1. Each distribution 788 (source and target) is assigned a distinct Gaussian Mixture distribution. In each experiment, the 789 maximum number of mixture components is restricted to four. The number of components for the 790 source distribution, n, is randomly selected from  $\{1, 2, 3\}$ , while the target distribution gets assigned 791 4 - n components, ensuring variability across datasets.

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793 C.2 DETAILS ON DOMAIN ADAPTATION DATASETS

**Image data for domain adaptation.** The DomainNet-2019 dataset (Peng et al., 2019) includes the 795 six distinct image domains "Real", "Clipart", "Quickdraw", "Sketch", "Painting", and "Infograph". 796 Following the approach of Zellinger et al. (2017) we utilize a simplified version of this dataset 797 known as MiniDomainNet. This reduced version narrows the focus to the five largest classes in the 798 training set across all six domains. To optimize computational efficiency we use a ResNet-18 (He 799 et al., 2016) trained on ImageNet (Krizhevsky et al., 2012). This pre-trained backbone is assumed 800 to have already learned low-level filters effective for the "Real" image domain requiring adaptation 801 only for the remaining five domains resulting in five domain adaptation tasks. 802

Time-series (sensory) data for domain adaptation. The Heterogeneity Activity Recognition
 dataset (Stisen et al., 2015) explores the variations specific to sensors, devices, and workloads for
 human activity recording. It utilizes data collected from 36 different smartphones and smartwatches
 comprising 13 different device models from four manufacturers. Our experimental setup incorpo rates all five domain adaptation scenarios analyzed in (Ragab et al., 2023).

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- **Text data for domain adaptation.** The Amazon Reviews dataset (Blitzer et al., 2006) contains bag-of-words representations of textual reviews across four categories: books, DVDs, kitchen, and

electronics with binary labels indicating the class of review. Each category represents a different domain from which a total of twelve domain adaptation tasks are constructed by pairing each domain as a source domain with every other domain as a target domain.

814 C.3 DETAILS ON EXPERIMENTAL SETUP 815

### 816 C.3.1 METHODS

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To test our aggregation approach we pick four popular representatives of the large class of widely 818 used DRE methods that can be modeled as Bregman divergences as in equation (1). For this we 819 use the methods presented in Example 1: KuLSIF (Kanamori et al., 2009), Exp (Menon & Ong, 820 2016), SQ (Menon & Ong, 2016), and LR (Bickel et al., 2009) with cross-validation as hyperpa-821 rameter selection procedure as a baseline and compare this for each of the four methods against 822 our aggregation approach. For KuLSIF, which offers a closed-form solution, no numerical opti-823 mization is required. For the other methods, we utilize the CG algorithm from Python's SciPY 824 library (Virtanen et al., 2020), employing the Polak-Ribière line search strategy (Hager & Zhang, 825 2006). In our domain adaptation experiments, we adhere to the evaluation protocol established by Dinu et al. (2023); Gruber et al. (2024). Specifically, we calculate an ensemble of various deep 826 neural networks using the importance-weighted functional regression approach. We use the density 827 ratio estimates from the aggregated and non-aggregated versions of KuLSIF, Exp, SQ, and LR as 828 importance weights. To comprehensively assess the impact on different domain adaptation tech-829 niques, we generate ensemble model candidates for 11 domain adaptation methods. These include 830 Minimum Discrepancy Estimation for Deep Domain Adaptation (MMDA) (Rahman et al., 2020), 831 the Convolutional deep Domanin Adaptation model for Time-Series data (CoDATS) (Wilson et al., 832 2020), Domain-Adversarial Neural Networks (DANN) (Ganin et al., 2016), Conditional Adversar-833 ial Domain Adaptation (CDAN) (Long et al., 2018), Deep Subdomain Adaptation (DSAN) (Zhou 834 et al., 2021), the DIRT-T approach to Unsupervised Domain Adaptation (DIRT) (Shu et al., 2018), 835 Adversarial Spectral Kernel Matching (AdvSKM) (Liu & Xue, 2021), Higher-order Moment Match-836 ing (HoMM) (Chen et al., 2020), Deep Domain Confusion (DDC) (Tzeng et al., 2014), Correlation 837 Alignment via Deep Neural Networks (Deep Coral) (Sun et al., 2017), and Central Moment Discrepancy (CMD) (Zellinger et al., 2017). Altogether, this benchmark involved training over 9,000 838 deep neural network models and evaluating the complete ensembling benchmark proposed by Dinu 839 et al. (2023) for Amazon Reviews, MiniDomainNet, and HHAR. The experiments on these datasets 840 were conducted to compare 8 DRE methods (with and without aggregation). 841

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#### C.3.2 KNOWN DENSITY RATIOS

844 Building upon Kanamori et al. (2012b) we create ten distinct datasets using Gaussian Mixture dis-845 tributions in a 50-dimensional space. These distributions feature a varying number of mixture com-846 ponents in  $\{1, 2, 3\}$  for either distributions P and Q. Each component gets assigned a unique mean within  $[0, 0.5]^{50}$  with corresponding covariance matrix. For all datasets the exact density ratio  $\frac{p}{q}$  is 847 848 known as it is fully determined by the ratio of the Gaussian Mixtures. For each Gaussian mixture 849 dataset 5,000 samples are drawn from the underlying distributions. The selection and evaluation of the baseline DRE methods are conducted using a standard train/validation/test split approach with 850 split ratios 64/16/20 respectively. The corresponding aggregated DRE methods are trained and eval-851 uated on the same splits while the aggregation weights are computed on the respective validation 852 sets. The regularization parameter  $\lambda$  is selected from the range  $\{10^{-6}, 10^{-5}, \dots, 10^4\}$ , and each 853 experiment is repeated 10 times to ensure statistical robustness. Consistent with Kanamori et al. 854 (2012a), a Gaussian kernel is employed for all density ratio estimation methods, with the kernel 855 width determined using the median heuristic (Schölkopf & Smola, 2002). 856

# C.3.3 ABLATION STUDIES

We additionally add an ablation study as proof of concept that our aggregation algorithm can also be
used in a heuristic setting for which we can't prove fast convergence rates as in Theorem 1. For this
we train several deep neural networks based logistic regression models (DeepLR) with different hyperparameter settings and optimize objective (4) as done for the other DRE methods. In Table 3 we
can see that even in the absence of theoretical guarantees our aggregation approach improves experimental results on all datasets compared to its baseline model that was selected by cross-validation.

$\begin{array}{c} c2d1.59 & c1d1.55 \\ .001(\pm 0.008) & 9.963(\pm 0.01733(\pm 0.009)) & 9.631(\pm 0.00733(\pm 0.009)) \\ \end{array}$	$\begin{array}{c} c2d1.78\\ \hline 12) & 9.857(\pm 0.013)\\ \textbf{14}) & \textbf{9.569}(\pm \textbf{0.014}) \end{array}$	$\begin{array}{c} c2d1.55\\ 10.992(\pm0.009)\\ \textbf{10.428}(\pm0.008)\end{array}$	$\begin{array}{c} c3d1.57\\ 13.421(\pm0.010)\\ \textbf{12.733}(\pm\textbf{0.011})\end{array}$	$\begin{array}{c} c2d1.61\\ 11.892(\pm0.011)\\ \textbf{11.229}(\pm0.010)\end{array}$	$\begin{array}{c} c3d1.46\\ 9.573(\pm0.006)\\ \textbf{8.954}(\pm0.005)\end{array}$
$\begin{array}{ccc} .001(\pm 0.008) & 9.963(\pm 0.01) \\ \textbf{733}(\pm 0.009) & \textbf{9.631}(\pm 0.02) \\ \end{array}$	$\begin{array}{llllllllllllllllllllllllllllllllllll$	$\begin{array}{c} 10.992 (\pm 0.009) \\ \textbf{10.428} (\pm \textbf{0.008}) \end{array}$	$\substack{13.421(\pm 0.010)\\ \textbf{12.733}(\pm \textbf{0.011})}$	$\begin{array}{c} 11.892 (\pm 0.011) \\ 11.229 (\pm 0.010) \end{array}$	$\begin{array}{c} 9.573 (\pm 0.006) \\ 8.954 (\pm 0.005) \end{array}$
Abla	ation 2: Averaging				
c2d1.59 c1d1.55	c2d1.78	c2d1.55	c3d1.57	c2d1.61	c3d1.46
$.597(\pm 0.007)$ 11.803( $\pm 0.0$	(11) 9.533(±0.010)	$10.292(\pm 0.009)$	$12.011(\pm 0.005)$	$11.524(\pm 0.003)$	$10.357(\pm 0.006)$
	c2d1.59 c1d1.55 597(±0.007) 11.803(±0.0	$\begin{array}{ccc} c2d1.59 & c1d1.55 & c2d1.78 \\ \hline 597(\pm 0.007) & 11.803(\pm 0.011) & 9.533(\pm 0.010) \end{array}$	$\begin{array}{cccc} c2d1.59 & c1d1.55 & c2d1.78 & c2d1.55 \\ \hline 597(\pm 0.007) & 11.803(\pm 0.011) & 9.533(\pm 0.010) & 10.292(\pm 0.009) \\ \end{array}$	c2d1.59         c1d1.55         c2d1.78         c2d1.55         c3d1.57           597(±0.007)         11.803(±0.011)         9.533(±0.010)         10.292(±0.009)         12.011(±0.005)	$\begin{array}{cccccccccccccccccccccccccccccccccccc$

Table 3: Mean and standard deviation (after  $\pm$ ) of twice the Bregman divergence error on the geo-872 metrically constructed datasets following Kanamori et al. (2012b) over ten different sample draws 873 from P and Q. 874



Figure 2: Plot of the value of the aggregation weights against twice the Bregman divergence error on the geometrically constructed dataset "c3,d1.70". More accurate models get assigned higher weights.

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In the second ablation study we compare our method to a naive aggregation approach where model 892 outputs are averaged. Results in Table 3 suggest that averaging model outputs cannot compete with 893 our aggregation algorithm. For the first ablation study we use a deep neural network based logis-894 tic regression model trained with binary cross-entropy loss and different regularization parameters 895 in  $\{10^{-6}, 10^{-5}, \dots, 10^4\}$ . The model is optimized by gradient descent for 125 epochs. We eval-896 uate this model on geometrically-constructed datasets by using the exact same data splits as for 897 the other DRE methods. In the second ablation study we compare our aggregation algorithm to a model averaging approach. We use the exact same experimental setup as for our algorithm and replace aggregation by averaging model outputs on geometrically-constructed datasets. In Figure 2 899 we illustrate the value of the weights assigned to KuLSIF estimators with different regularization 900 parameter settings evaluated on dataset "c3,d1.70". It can be seen that more accurate models get 901 assigned higher weight values. 902

#### C.3.4 DOMAIN ADAPTATION 904

905 The results of the domain adaptation benchmark experiment were computed using gradient-based 906 training across a total of 9,174 models. The implementation of certain components is based on the 907 codebase by Dinu et al. (2023); Gruber et al. (2024). The specifics of the experimental setup are as 908 follows:

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• MiniDomainNet (image data): 11 methods  $\times$  8 parameters  $\times$  5 domain adaptation tasks  $\times$  3 seeds = 1320 trained models

- 912 • AmazonReviews (text data): 11 methods  $\times$  14 parameters  $\times$  12 domain adaptation tasks  $\times$  3 seeds = 5544 trained models 913
  - HHAR (sensory data): 11 methods  $\times$  14 parameters  $\times$  5 domain adaptation tasks  $\times$  3 seeds = 2310 trained models
- 915 916

- Consistent with Dinu et al. (2023), we utilized 11 domain adaptation methods from the AdaTime 917 benchmark (Ragab et al., 2023). For each method and domain adaptation modality (text, image,

sensory), we evaluated all 8 density ratio estimation approaches across 22 domain adaptation sce-narios. The model implementation for domain adaptation methods and experimental configurations also followed Dinu et al. (2023). Specifically, fully connected networks were used for Amazon Re-views, while a pretrained ResNet-18 backbone was employed for MiniDomainNet. For training and selecting/aggregating the density ratio estimation methods within this pipeline we perform an additional train/val split of 80/20 on the datasets that are used for training the domain adaption methods. For the regularization parameter  $\lambda$  we use  $\{10^{-6}, 10^{-5}, \dots, 10^4\}$  as hyperparameter space. Fol-lowing Kanamori et al. (2012a), we use a Gaussian kernel with kernel width set according to the median heuristic (Schölkopf & Smola, 2002) for all DRE methods. In the results tables, we report the classification accuracy on the respective test sets of the target distribution for all compared DRE methods. 

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932			Domain Adaptation: Amazon Reviews											
002		С	ross-Validation f	or Binary Classifi	er	Aggregation								
933	DA-Method	KuLSIF	Exp	LR	SQ	KuLSIF	Exp	LR	SQ					
934	MMDA	$0.786(\pm 0.010)$	$0.771(\pm 0.009)$	$0.784(\pm 0.010)$	$0.780(\pm 0.008)$	$0.794(\pm 0.008)$	$0.782(\pm 0.008)$	$0.790(\pm 0.010)$	$0.789(\pm 0.006)$					
935	CoDATS	$0.795(\pm 0.012)$	$0.777(\pm 0.011)$	$0.794(\pm 0.012)$	$0.788(\pm 0.009)$	0.803(±0.010)	$0.790(\pm 0.010)$	$0.797(\pm 0.012)$	$0.793(\pm 0.008)$					
036	DANN	$0.794(\pm 0.011)$	$0.779(\pm 0.011)$	$0.793(\pm 0.012)$	$0.790(\pm 0.010)$	0.804(±0.009)	$0.792(\pm 0.010)$	$0.800(\pm 0.012)$	$0.799(\pm 0.008)$					
550	CDAN	$0.787(\pm 0.012)$	$0.772(\pm 0.010)$	$0.787(\pm 0.010)$	$0.785(\pm 0.009)$	$0.792(\pm 0.010)$	$0.783(\pm 0.009)$	$0.790(\pm 0.010)$	$0.792(\pm 0.007)$					
937	DSAN	$0.794(\pm 0.011)$	$0.778(\pm 0.012)$	$0.793(\pm 0.013)$	$0.790(\pm 0.011)$	0.803(±0.009)	$0.790(\pm 0.011)$	$0.798(\pm 0.013)$	$0.798(\pm 0.009)$					
020	DIRT	$0.787(\pm 0.011)$	$0.776(\pm 0.011)$	$0.788(\pm 0.012)$	$0.784(\pm 0.010)$	$0.797(\pm 0.009)$	$0.787(\pm 0.010)$	$0.790(\pm 0.012)$	$0.794(\pm 0.008)$					
930	AdvSKM	$0.779(\pm 0.011)$	$0.761(\pm 0.009)$	$0.777(\pm 0.010)$	$0.772(\pm 0.008)$	$0.784(\pm 0.009)$	$0.774(\pm 0.008)$	$0.781(\pm 0.010)$	$0.782(\pm 0.006)$					
939	HoMM	$0.777(\pm 0.009)$	$0.760(\pm 0.010)$	$0.774(\pm 0.011)$	$0.770(\pm 0.009)$	0.786(±0.007)	$0.772(\pm 0.009)$	$0.779(\pm 0.011)$	$0.779(\pm 0.008)$					
0.40	DDC	$0.780(\pm 0.011)$	$0.764(\pm 0.011)$	$0.778(\pm 0.012)$	$0.774(\pm 0.010)$	$0.787(\pm 0.009)$	$0.777(\pm 0.010)$	$0.782(\pm 0.012)$	$0.783(\pm 0.008)$					
940	DeepCoral	$0.784(\pm 0.010)$	$0.767(\pm 0.010)$	$0.781(\pm 0.011)$	$0.776(\pm 0.009)$	$0.794(\pm 0.008)$	$0.779(\pm 0.009)$	$0.785(\pm 0.011)$	$0.784(\pm 0.007)$					
941	CMD	$0.790(\pm 0.013)$	$0.773(\pm 0.011)$	$0.786(\pm 0.012)$	$0.781(\pm 0.011)$	$0.797(\pm 0.011)$	$0.783(\pm 0.011)$	$0.790(\pm 0.012)$	$0.787 (\pm 0.008)$					
942	Avg.	$0.787(\pm 0.011)$	$0.771(\pm 0.010)$	$0.785(\pm 0.011)$	$0.781(\pm 0.009)$	$0.795(\pm 0.009)$	$0.783 (\pm 0.009)$	$0.789 (\pm 0.011)$	$0.789 (\pm 0.007)$					

	Domain Adaptation: HHAR								
	C	ross-Validation fo	or Binary Classifi	er	Aggregation				
DA-Method	KuLSIF	Exp	LR	SQ	KuLSIF	Exp	LR	SQ	
MMDA	$0.780(\pm 0.008)$	$0.670(\pm 0.098)$	$0.773(\pm 0.013)$	$0.736(\pm 0.006)$	0.826(±0.023)	$0.711(\pm 0.085)$	$0.786(\pm 0.007)$	0.763(±0.005	
CoDATS	$0.723(\pm 0.130)$	$0.776(\pm 0.021)$	$0.779(\pm 0.021)$	$0.741(\pm 0.011)$	0.765(±0.120)	$0.818(\pm 0.016)$	$0.793(\pm 0.015)$	$0.767(\pm 0.010)$	
DANN	$0.697(\pm 0.179)$	$0.785(\pm 0.024)$	$0.795(\pm 0.021)$	$0.757(\pm 0.011)$	$0.738(\pm 0.170)$	$0.828(\pm 0.015)$	$0.807(\pm 0.015)$	$0.780(\pm 0.010)$	
CDAN	$0.792(\pm 0.029)$	$0.706(\pm 0.166)$	$0.788(\pm 0.029)$	$0.751(\pm 0.022)$	0.834(±0.031)	$0.750(\pm 0.144)$	$0.804(\pm 0.024)$	$0.775(\pm 0.021)$	
DSAN	$0.754(\pm 0.128)$	$0.528(\pm 0.228)$	$0.792(\pm 0.015)$	$0.754(\pm 0.014)$	$0.794(\pm 0.133)$	$0.572(\pm 0.219)$	$0.805(\pm 0.013)$	$0.775(\pm 0.013)$	
DIRT	$0.731(\pm 0.084)$	$0.790(\pm 0.040)$	$0.790(\pm 0.023)$	$0.753(\pm 0.014)$	0.774(±0.086)	$0.828(\pm 0.023)$	$0.801(\pm 0.017)$	$0.779(\pm 0.013)$	
AdvSKM	$0.752(\pm 0.007)$	$0.746(\pm 0.013)$	$0.746(\pm 0.018)$	$0.708(\pm 0.008)$	$0.793(\pm 0.024)$	$0.790(\pm 0.019)$	$0.759(\pm 0.012)$	$0.735(\pm 0.006)$	
HoMM	$0.759(\pm 0.009)$	$0.662(\pm 0.096)$	$0.754(\pm 0.021)$	$0.716(\pm 0.011)$	0.803(±0.022)	$0.707(\pm 0.083)$	$0.768(\pm 0.016)$	$0.749(\pm 0.010)$	
DDC	$0.748(\pm 0.017)$	$0.454(\pm 0.215)$	$0.744(\pm 0.019)$	$0.706(\pm 0.009)$	$0.794(\pm 0.018)$	$0.496(\pm 0.196)$	$0.759(\pm 0.013)$	$0.732(\pm 0.009)$	
DeepCoral	$0.701(\pm 0.115)$	$0.749(\pm 0.021)$	$0.758(\pm 0.015)$	$0.720(\pm 0.006)$	$0.745(\pm 0.118)$	$0.791(\pm 0.013)$	$0.769(\pm 0.011)$	$0.743(\pm 0.005)$	
CMD	$0.671(\pm 0.170)$	$0.770(\pm 0.015)$	$0.770(\pm 0.016)$	$0.732(\pm 0.008)$	$0.714(\pm 0.164)$	$0.814(\pm 0.017)$	$0.780(\pm 0.010)$	$0.754(\pm 0.007)$	
Avg.	$0.737(\pm 0.080)$	$0.694(\pm 0.085)$	$0.772(\pm 0.019)$	$0.734(\pm 0.011)$	0.780(±0.082)	$0.737(\pm 0.075)$	$0.785(\pm 0.014)$	$0.759(\pm 0.010)$	

Table 4: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on MiniDomainNet, Amazon Reviews and HHAR datasets over three different random initialization of model weights and several domain adaptation tasks.

	(	Cross-Validation f	or Binary Classifie	er	Aggregation				
Scenario	KuLSIF	Exp	LR	SQ	KuLSIF	Exp	LR	SQ	
R  ightarrow C	$0.585(\pm 0.013)$	$0.590(\pm 0.016)$	$0.589(\pm 0.024)$	$0.578(\pm 0.022)$	$0.595(\pm 0.011)$	$0.598(\pm 0.015)$	$0.596(\pm 0.017)$	$0.592(\pm 0.021)$	
$R \to I$	$0.377(\pm 0.009)$	$0.372(\pm 0.008)$	$0.378(\pm 0.007)$	$0.365(\pm 0.005)$	$0.393(\pm 0.007)$	$0.385(\pm 0.008)$	$0.394(\pm 0.001)$	$0.384(\pm 0.004)$	
$\mathbf{R} \to \mathbf{P}$	$0.722(\pm 0.004)$	$0.729(\pm 0.006)$	$0.725(\pm 0.006)$	$0.723(\pm 0.004)$	$0.730(\pm 0.002)$	$0.743(\pm 0.006)$	$0.721(\pm 0.000)$	$0.728(\pm 0.003)$	
$\mathbf{R}  ightarrow \mathbf{Q}$	$0.354(\pm 0.008)$	$0.348(\pm 0.016)$	$0.349(\pm 0.014)$	$0.328(\pm 0.013)$	$0.356(\pm 0.006)$	$0.356(\pm 0.016)$	$0.358(\pm 0.008)$	$0.351(\pm 0.012)$	
$R \to S$	$0.596(\pm 0.009)$	$0.599(\pm 0.010)$	$0.600(\pm 0.009)$	$0.596(\pm 0.007)$	$0.606(\pm 0.007)$	$0.611(\pm 0.009)$	$0.610(\pm 0.002)$	$0.618 (\pm 0.006)$	
Avg.	$0.527(\pm 0.009)$	$0.528(\pm 0.011)$	$0.528(\pm 0.012)$	$0.518(\pm 0.010)$	$0.536(\pm 0.007)$	$0.539 (\pm 0.011)$	$0.536 (\pm 0.006)$	$0.535 (\pm 0.009)$	

Table 5: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on MiniDomainNet computed with domain adaptation method MMDA.

	C	ross-Validation fo	r Binary Classifie	r	Aggregation				
Scenario	KuLSIF	Exp	LR	SQ	KuLSIF	Exp	LR	SQ	
$R \rightarrow C$	$0.597(\pm 0.011)$	$0.577(\pm 0.010)$	$0.594(\pm 0.010)$	$0.576(\pm 0.008)$	0.602(±0.009)	$0.587(\pm 0.008)$	$0.601(\pm 0.005)$	$0.593(\pm 0.006)$	
$R \rightarrow I$	$0.366(\pm 0.012)$	$0.368(\pm 0.023)$	$0.349(\pm 0.038)$	$0.338(\pm 0.036)$	$0.373(\pm 0.011)$	$0.385(\pm 0.023)$	$0.357(\pm 0.031)$	$0.356(\pm 0.035)$	
$R \rightarrow P$	$0.739(\pm 0.015)$	$0.733(\pm 0.018)$	$0.737(\pm 0.017)$	$0.726(\pm 0.015)$	$0.747(\pm 0.014)$	$0.745(\pm 0.017)$	$0.750(\pm 0.011)$	$0.742(\pm 0.014)$	
$R \rightarrow Q$	$0.361(\pm 0.013)$	$0.364(\pm 0.014)$	$0.355(\pm 0.027)$	$0.342(\pm 0.025)$	$0.370(\pm 0.010)$	$0.377(\pm 0.013)$	$0.369(\pm 0.021)$	$0.364(\pm 0.023)$	
$R \rightarrow S$	$0.619(\pm 0.008)$	$0.616(\pm 0.008)$	$0.616(\pm 0.009)$	$0.601(\pm 0.008)$	$0.617(\pm 0.006)$	$0.624(\pm 0.008)$	$0.622(\pm 0.002)$	$0.607(\pm 0.008)$	
Avg.	$0.536(\pm 0.012)$	$0.532(\pm 0.015)$	$0.530(\pm 0.020)$	$0.517(\pm 0.018)$	$0.542(\pm 0.010)$	$0.543 (\pm 0.014)$	$0.540 (\pm 0.014)$	$0.533(\pm 0.017)$	

Table 6: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on MiniDomainNet computed with domain adaptation method CoDATS.

-	C	cross-Validation f	or Binary Classifi	er	Aggregation				
Scenario	KuLSIF	Exp	ĹR	SQ	KuLSIF	Exp	LR	SQ	
R  ightarrow C	$  0.591(\pm 0.015)$	$0.576(\pm 0.013)$	$0.579(\pm 0.012)$	$0.560(\pm 0.009)$	0.597(±0.013)	$0.583(\pm 0.011)$	$0.587(\pm 0.005)$	$0.568(\pm 0.007)$	
R  ightarrow I	$0.374(\pm 0.009)$	$0.372(\pm 0.011)$	$0.369(\pm 0.026)$	$0.354(\pm 0.024)$	$0.379(\pm 0.007)$	$0.387(\pm 0.009)$	$0.375(\pm 0.021)$	$0.368(\pm 0.022)$	
$\mathbf{R} \to \mathbf{P}$	$0.720(\pm 0.007)$	$0.716(\pm 0.008)$	$0.699(\pm 0.032)$	$0.692(\pm 0.030)$	$0.724(\pm 0.006)$	$0.727(\pm 0.008)$	$0.702(\pm 0.026)$	$0.699(\pm 0.029)$	
$\mathbf{R}  ightarrow \mathbf{Q}$	$0.357(\pm 0.009)$	$0.340(\pm 0.016)$	$0.337(\pm 0.016)$	$0.322(\pm 0.014)$	$0.362(\pm 0.005)$	$0.355(\pm 0.015)$	$0.348(\pm 0.009)$	$0.326(\pm 0.013)$	
$R \rightarrow S$	$0.613(\pm 0.007)$	$0.607(\pm 0.010)$	$0.614(\pm 0.007)$	$0.602(\pm 0.005)$	0.619(±0.005)	$0.624(\pm 0.010)$	$0.621(\pm 0.001)$	$0.632(\pm 0.004)$	
Avg.	$0.531(\pm 0.009)$	$0.522(\pm 0.012)$	$0.520(\pm 0.019)$	$0.506(\pm 0.016)$	0.536(±0.007)	$0.535(\pm 0.011)$	$0.526(\pm 0.013)$	$0.519(\pm 0.015)$	

Table 7: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on MiniDomainNet computed with domain adaptation method DANN.

	C	ross-Validation fo	or Binary Classifi	er	Aggregation			
Scenario	KuLSIF	Exp	ĹR	SQ	KuLSIF	Exp	LR	SQ
$R \to C$	$  0.592(\pm 0.018)$	$0.595(\pm 0.029)$	$0.594(\pm 0.023)$	$0.578(\pm 0.021)$	$0.594(\pm 0.015)$	$0.616(\pm 0.028)$	$0.608(\pm 0.017)$	$0.598(\pm 0.019)$
$R \to I$	$0.372(\pm 0.013)$	$0.381(\pm 0.012)$	$0.337(\pm 0.056)$	$0.324(\pm 0.053)$	$0.384(\pm 0.011)$	$0.384(\pm 0.011)$	$0.346(\pm 0.050)$	$0.343(\pm 0.052)$
$R \to P$	$0.729(\pm 0.004)$	$0.720(\pm 0.015)$	$0.725(\pm 0.011)$	$0.713(\pm 0.009)$	$0.735(\pm 0.001)$	$0.734(\pm 0.014)$	$0.731(\pm 0.005)$	$0.722(\pm 0.008)$
$\mathbf{R}  ightarrow \mathbf{Q}$	$0.353(\pm 0.018)$	$0.352(\pm 0.020)$	$0.354(\pm 0.017)$	$0.351(\pm 0.014)$	$0.354(\pm 0.014)$	$0.369(\pm 0.020)$	$0.364(\pm 0.011)$	$0.363(\pm 0.012)$
$R \to S$	$0.609(\pm 0.008)$	$0.607(\pm 0.012)$	$0.611(\pm 0.009)$	$0.594(\pm 0.007)$	$0.618(\pm 0.005)$	$0.618(\pm 0.010)$	$0.623(\pm 0.003)$	$0.603(\pm 0.006)$
Avg.	$0.531(\pm 0.012)$	$0.531(\pm 0.017)$	$0.524(\pm 0.023)$	$0.512(\pm 0.021)$	0.537(±0.009)	$0.544(\pm 0.017)$	$0.535(\pm 0.017)$	$0.526(\pm 0.020)$

Table 8: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on MiniDomainNet computed with domain adaptation method CDAN.

	Cı	Cross-Validation for Binary Classifier				Aggregation			
Scenario	KuLSIF	Exp	LR	SQ	KuLSIF	Exp	LR	SQ	
$R \rightarrow C$	$0.623(\pm 0.015)$	$0.603(\pm 0.026)$	$0.596(\pm 0.019)$	$0.589(\pm 0.017)$	$0.622(\pm 0.013)$	$0.614(\pm 0.026)$	$0.606(\pm 0.013)$	$0.597(\pm 0.016)$	
$R \to I$	$0.374(\pm 0.010)$	$0.367(\pm 0.008)$	$0.350(\pm 0.014)$	$0.339(\pm 0.012)$	$0.383(\pm 0.008)$	$0.391(\pm 0.006)$	$0.363(\pm 0.010)$	$0.344(\pm 0.011)$	
$R \rightarrow P$	$0.720(\pm 0.007)$	$0.724(\pm 0.008)$	$0.720(\pm 0.008)$	$0.708(\pm 0.005)$	$0.726(\pm 0.004)$	$0.738(\pm 0.007)$	$0.729(\pm 0.001)$	$0.723(\pm 0.004)$	
$R \rightarrow Q$	$0.364(\pm 0.012)$	$0.355(\pm 0.018)$	$0.354(\pm 0.018)$	$0.334(\pm 0.016)$	$0.366(\pm 0.010)$	$0.364(\pm 0.016)$	$0.359(\pm 0.012)$	$0.347(\pm 0.015)$	
$R \to S$	$0.616(\pm 0.012)$	$0.609(\pm 0.015)$	$0.615(\pm 0.016)$	$0.598(\pm 0.014)$	$0.621(\pm 0.011)$	$0.622(\pm 0.014)$	$0.618(\pm 0.010)$	$0.612(\pm 0.013)$	
Avg.	$0.539(\pm 0.011)$	$0.532(\pm 0.015)$	$0.527(\pm 0.015)$	$0.513(\pm 0.013)$	$0.544(\pm 0.009)$	$0.546 (\pm 0.014)$	$0.535 (\pm 0.009)$	$0.525 (\pm 0.012)$	

Table 9: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on MiniDomainNet computed with domain adaptation method DSAN.

		Cross-Validation f	or Binary Classifie	er	Aggregation			
Scenari	KuLSIF	Exp	LR	SQ	KuLSIF	Exp	LR	SQ
$R \rightarrow C$	$0.572(\pm 0.021)$	$0.474(\pm 0.176)$	$0.566(\pm 0.022)$	$0.555(\pm 0.020)$	$0.580(\pm 0.019)$	$0.478(\pm 0.175)$	$0.582(\pm 0.016)$	$0.575(\pm 0.0$
$R \to I$	$0.376(\pm 0.047)$	$0.236(\pm 0.135)$	$0.406(\pm 0.025)$	$0.391(\pm 0.022)$	0.387(±0.045)	$0.246(\pm 0.133)$	$0.407(\pm 0.018)$	$0.402(\pm 0.0$
$R \to P$	$0.714(\pm 0.026)$	$0.542(\pm 0.271)$	$0.713(\pm 0.025)$	$0.700(\pm 0.024)$	$0.718(\pm 0.024)$	$0.550(\pm 0.270)$	$0.711(\pm 0.020)$	$0.724(\pm 0.0)$
$\mathbf{R}  ightarrow \mathbf{Q}$	$0.336(\pm 0.018)$	$0.248(\pm 0.055)$	$0.329(\pm 0.021)$	$0.315(\pm 0.019)$	$0.340(\pm 0.016)$	$0.258(\pm 0.054)$	$0.338(\pm 0.016)$	$0.325(\pm 0.0)$
$R \to S$	$0.586(\pm 0.020)$	$0.431(\pm 0.245)$	$0.587(\pm 0.021)$	$0.585(\pm 0.019)$	$0.591(\pm 0.019)$	$0.441(\pm 0.244)$	$0.595(\pm 0.015)$	$0.598(\pm 0.5)$
Avg.	$0.517(\pm 0.026)$	$0.386(\pm 0.177)$	$0.520(\pm 0.023)$	$0.509(\pm 0.021)$	0.523(±0.025)	$0.395(\pm 0.175)$	$0.526(\pm 0.017)$	$0.525(\pm 0.525)$

Table 10: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on MiniDomainNet computed with domain adaptation method DIRT.

1027		C	ross-Validation fo	or Binary Classifie	r	Aggregation				
1022	Scenario	KuLSIF	Exp	ĹR	SQ	KuLSIF	Exp	LR	SQ	
1020	$R \rightarrow C$	$0.568(\pm 0.008)$	$0.561(\pm 0.013)$	$0.552(\pm 0.006)$	$0.535(\pm 0.004)$	0.580(±0.006)	$0.573(\pm 0.012)$	$0.564(\pm 0.000)$	$0.548(\pm 0.003)$	
1029	$R \to I$	$0.382(\pm 0.010)$	$0.389(\pm 0.007)$	$0.385(\pm 0.026)$	$0.369(\pm 0.024)$	$0.381(\pm 0.008)$	$0.415(\pm 0.006)$	$0.384(\pm 0.019)$	$0.384(\pm 0.023)$	
1030	$R \to P$	$0.717(\pm 0.005)$	$0.712(\pm 0.014)$	$0.712(\pm 0.010)$	$0.705(\pm 0.008)$	$0.717(\pm 0.004)$	$0.725(\pm 0.013)$	$0.724(\pm 0.004)$	$0.723(\pm 0.006)$	
1000	$R \to Q$	$0.332(\pm 0.005)$	$0.325(\pm 0.007)$	$0.324(\pm 0.011)$	$0.315(\pm 0.008)$	$0.342(\pm 0.003)$	$0.329(\pm 0.006)$	$0.331(\pm 0.004)$	$0.332(\pm 0.007)$	
1031	$R \to S$	$0.584(\pm 0.004)$	$0.586(\pm 0.003)$	$0.588(\pm 0.005)$	$0.575(\pm 0.004)$	$0.587(\pm 0.003)$	$0.602 (\pm 0.002)$	$0.602 (\pm 0.001)$	$0.598(\pm 0.002)$	
1032	Avg.	$0.516(\pm 0.006)$	$0.515(\pm 0.009)$	$0.512(\pm 0.012)$	$0.500(\pm 0.010)$	$0.522(\pm 0.005)$	$0.529 (\pm 0.008)$	$0.521 (\pm 0.006)$	$0.517(\pm 0.008)$	

Table 11: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on MiniDomainNet computed with domain adaptation method AdvSKM.

	C	ross-Validation fo	or Binary Classifi	er	Aggregation				
Scenario	KuLSIF	Exp	ĹR	SQ	KuLSIF	Exp	LR	SQ	
$R \to C$	$0.590(\pm 0.020)$	$0.588(\pm 0.020)$	$0.577(\pm 0.020)$	$0.567(\pm 0.018)$	0.604(±0.018)	$0.604(\pm 0.019)$	$0.589(\pm 0.013)$	$0.591(\pm 0.017)$	
$R \to I$	$0.399(\pm 0.006)$	$0.407(\pm 0.009)$	$0.378(\pm 0.025)$	$0.365(\pm 0.024)$	$0.400(\pm 0.004)$	$0.419(\pm 0.008)$	$0.386(\pm 0.018)$	$0.385(\pm 0.023)$	
$R \to P$	$0.729(\pm 0.002)$	$0.726(\pm 0.009)$	$0.726(\pm 0.010)$	$0.704(\pm 0.008)$	0.736(±0.000)	$0.744(\pm 0.008)$	$0.737(\pm 0.004)$	$0.725(\pm 0.007)$	
$\mathbf{R}  ightarrow \mathbf{Q}$	$0.351(\pm 0.005)$	$0.333(\pm 0.013)$	$0.333(\pm 0.013)$	$0.318(\pm 0.012)$	$0.356(\pm 0.003)$	$0.345(\pm 0.011)$	$0.341(\pm 0.008)$	$0.345(\pm 0.011)$	
$R \to S$	$0.588(\pm 0.008)$	$0.593(\pm 0.011)$	$0.592(\pm 0.008)$	$0.572(\pm 0.005)$	0.599(±0.007)	$0.610(\pm 0.009)$	$0.594(\pm 0.002)$	$0.595(\pm 0.003)$	
Avg.	$0.531(\pm 0.008)$	$0.529(\pm 0.012)$	$0.521(\pm 0.015)$	$0.505(\pm 0.013)$	0.539(±0.007)	$0.544(\pm 0.011)$	$0.529(\pm 0.009)$	$0.528(\pm 0.012)$	

Table 12: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on MiniDomainNet computed with domain adaptation method HoMM. 

	C	Cross-Validation for Binary Classifier				Aggregation				
Scenario	KuLSIF	Exp	ĹR	SQ	KuLSIF	Exp	LR	SQ		
$R \to C$	$0.569(\pm 0.027)$	$0.571(\pm 0.029)$	$0.563(\pm 0.028)$	$0.555(\pm 0.027)$	$0.584(\pm 0.025)$	$0.590(\pm 0.029)$	$0.577(\pm 0.023)$	$0.573(\pm 0.027)$		
$R \to I$	$0.389(\pm 0.011)$	$0.391(\pm 0.016)$	$0.390(\pm 0.011)$	$0.369(\pm 0.010)$	0.394(±0.009)	$0.399(\pm 0.015)$	$0.398(\pm 0.006)$	0.388(±0.009)		
$R \to P$	$0.717(\pm 0.002)$	$0.721(\pm 0.003)$	$0.715(\pm 0.002)$	$0.701(\pm 0.000)$	$0.727(\pm 0.000)$	$0.726(\pm 0.002)$	$0.723(\pm 0.003)$	$0.711(\pm 0.000)$		
$R \rightarrow Q$	$0.333(\pm 0.004)$	$0.323(\pm 0.013)$	$0.324(\pm 0.013)$	$0.313(\pm 0.010)$	$0.337(\pm 0.002)$	$0.335(\pm 0.012)$	$0.336(\pm 0.006)$	$0.331(\pm 0.009)$		
$R \to S$	$0.580(\pm 0.005)$	$0.578(\pm 0.005)$	$0.579(\pm 0.004)$	$0.562(\pm 0.003)$	$0.594(\pm 0.003)$	$0.595(\pm 0.004)$	$0.586(\pm 0.002)$	$0.574(\pm 0.002)$		
Avg.	$0.517(\pm 0.010)$	$0.517(\pm 0.013)$	$0.514(\pm 0.012)$	$0.500(\pm 0.010)$	0.527(±0.008)	$0.529 (\pm 0.012)$	$0.524(\pm 0.008)$	$0.515 (\pm 0.009)$		

Table 13: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on MiniDomainNet computed with domain adaptation method DDC. 

	(	Cross-Validation f	or Binary Classifie	er	Aggregation			
Scenario	KuLSIF	Exp	ĹR	SQ	KuLSIF	Exp	LR	SQ
$R \to C$	$0.588(\pm 0.021)$	$0.569(\pm 0.016)$	$0.567(\pm 0.012)$	$0.543(\pm 0.010)$	$0.593(\pm 0.020)$	$0.578(\pm 0.015)$	$0.578(\pm 0.006)$	$0.548(\pm 0.009)$
$R \to I$	$0.369(\pm 0.012)$	$0.372(\pm 0.008)$	$0.381(\pm 0.018)$	$0.370(\pm 0.017)$	$0.371(\pm 0.010)$	$0.387(\pm 0.008)$	$0.380(\pm 0.013)$	$0.379(\pm 0.016)$
$R \to P$	$0.735(\pm 0.011)$	$0.737(\pm 0.010)$	$0.734(\pm 0.005)$	$0.722(\pm 0.004)$	$0.749(\pm 0.010)$	$0.749(\pm 0.010)$	$0.737(\pm 0.001)$	$0.732(\pm 0.003)$
$R \to Q$	$0.363(\pm 0.011)$	$0.348(\pm 0.021)$	$0.349(\pm 0.016)$	$0.334(\pm 0.014)$	$0.363(\pm 0.008)$	$0.359(\pm 0.020)$	$0.365(\pm 0.011)$	$0.355(\pm 0.013)$
$R \to S$	$0.621(\pm 0.006)$	$0.616(\pm 0.009)$	$0.617(\pm 0.009)$	$0.604(\pm 0.008)$	$0.637(\pm 0.003)$	$0.629(\pm 0.008)$	$0.619(\pm 0.003)$	$0.620(\pm 0.006)$
Avg.	$0.535(\pm 0.012)$	$0.528(\pm 0.013)$	$0.530(\pm 0.012)$	$0.514(\pm 0.011)$	$0.543(\pm 0.010)$	$0.540 (\pm 0.012)$	$0.536(\pm 0.007)$	$0.527(\pm 0.009)$

Table 14: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on MiniDomainNet computed with domain adaptation method DeepCoral. 

	C	ross-Validation fo	r Binary Classifie	er	Aggregation			
Scenario	KuLSIF	Exp	LR	SQ	KuLSIF	Exp	LR	SQ
$R \to C$	$0.576(\pm 0.015)$	$0.560(\pm 0.026)$	$0.552(\pm 0.017)$	$0.538(\pm 0.015)$	$0.585(\pm 0.013)$	$0.574(\pm 0.025)$	$0.560(\pm 0.011)$	$0.541(\pm 0.01)$
$R \rightarrow I$	$0.383(\pm 0.009)$	$0.391(\pm 0.021)$	$0.381(\pm 0.033)$	$0.375(\pm 0.032)$	0.386(±0.008)	$0.400(\pm 0.019)$	$0.384(\pm 0.026)$	0.397(±0.03
$R \to P$	$0.739(\pm 0.008)$	$0.739(\pm 0.016)$	$0.742(\pm 0.011)$	$0.723(\pm 0.008)$	$0.753(\pm 0.006)$	$0.747(\pm 0.016)$	$0.747(\pm 0.005)$	$0.732(\pm 0.00)$
$R \rightarrow Q$	$0.354(\pm 0.013)$	$0.336(\pm 0.030)$	$0.335(\pm 0.028)$	$0.321(\pm 0.026)$	$0.362(\pm 0.011)$	$0.352(\pm 0.029)$	$0.341(\pm 0.022)$	0.333(±0.02
$R \to S$	$0.595(\pm 0.005)$	$0.594(\pm 0.010)$	$0.597(\pm 0.014)$	$0.590(\pm 0.013)$	$0.594(\pm 0.004)$	$0.617(\pm 0.010)$	$0.603(\pm 0.009)$	$0.605(\pm 0.01)$
Avg.	$0.529(\pm 0.010)$	$0.524(\pm 0.021)$	$0.521(\pm 0.021)$	$0.510(\pm 0.019)$	0.536(±0.008)	$0.538(\pm 0.020)$	$0.527(\pm 0.015)$	$0.521(\pm 0.01)$

Table 15: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on MiniDomainNet computed with domain adaptation method CMD. 

1081									
1082		(	Cross-Validation fo	r Binary Classifier			Aggre	gation	
1083	Scenario	KuLSIF	Exp	LR	SQ	KuLSIF	Exp	LR	SQ
1084	$B \to D$	$0.795(\pm 0.003)$	$0.784(\pm 0.002)$	$0.796(\pm 0.003)$	$0.792(\pm 0.001)$	$0.799(\pm 0.001)$	$0.794(\pm 0.002)$	$0.802(\pm 0.003)$	$0.796(\pm 0.000)$
	$B \to E$	$0.776(\pm 0.018)$	$0.752(\pm 0.015)$	$0.766(\pm 0.016)$	$0.762(\pm 0.014)$	$0.784(\pm 0.016)$	$0.764(\pm 0.015)$	$0.770(\pm 0.016)$	$0.773(\pm 0.012)$
1085	$B \to K$	$0.793(\pm 0.019)$	$0.791(\pm 0.020)$	$0.794(\pm 0.021)$	$0.792(\pm 0.019)$	$0.806(\pm 0.017)$	$0.797(\pm 0.018)$	$0.804(\pm 0.021)$	$0.800(\pm 0.017)$
1086	$\mathbf{D}\to\mathbf{B}$	$0.799(\pm 0.007)$	$0.770(\pm 0.005)$	$0.793(\pm 0.006)$	$0.794(\pm 0.004)$	$0.805(\pm 0.004)$	$0.790(\pm 0.004)$	$0.788(\pm 0.006)$	$0.805(\pm 0.001)$
1000	$\mathbf{D}  ightarrow \mathbf{E}$	$0.791(\pm 0.008)$	$0.785(\pm 0.010)$	$0.790(\pm 0.011)$	$0.792(\pm 0.010)$	$0.797(\pm 0.007)$	$0.783(\pm 0.010)$	$0.800(\pm 0.011)$	$0.805(\pm 0.008)$
1087	$D \to K$	$0.802(\pm 0.010)$	$0.791(\pm 0.008)$	$0.801(\pm 0.009)$	$0.797(\pm 0.007)$	$0.810(\pm 0.008)$	$0.803(\pm 0.007)$	$0.808(\pm 0.009)$	$0.812(\pm 0.005)$
1099	${\rm E}  ightarrow {\rm B}$	$0.709(\pm 0.015)$	$0.693(\pm 0.010)$	$0.709(\pm 0.011)$	$0.705(\pm 0.010)$	$0.720(\pm 0.014)$	$0.708(\pm 0.009)$	$0.708(\pm 0.011)$	$0.718(\pm 0.007)$
1000	$\mathrm{E}  ightarrow \mathrm{D}$	$0.746(\pm 0.003)$	$0.729(\pm 0.008)$	$0.737(\pm 0.009)$	$0.727(\pm 0.006)$	$0.761(\pm 0.002)$	$0.731(\pm 0.007)$	$0.744(\pm 0.009)$	$0.731(\pm 0.004)$
1089	$E \to K$	$0.878(\pm 0.009)$	$0.867(\pm 0.008)$	$0.876(\pm 0.008)$	$0.881(\pm 0.005)$	$0.883(\pm 0.006)$	$0.878(\pm 0.007)$	$0.879(\pm 0.008)$	$0.896(\pm 0.004)$
1000	$\mathbf{K}  ightarrow \mathbf{B}$	$0.729(\pm 0.005)$	$0.723(\pm 0.005)$	$0.732(\pm 0.006)$	$0.727(\pm 0.004)$	$0.740(\pm 0.003)$	$0.734(\pm 0.003)$	$0.742(\pm 0.006)$	$0.727(\pm 0.002)$
1090	$\mathbf{K} \to \mathbf{D}$	$0.757(\pm 0.015)$	$0.740(\pm 0.011)$	$0.756(\pm 0.012)$	$0.750(\pm 0.010)$	$0.767(\pm 0.013)$	$0.756(\pm 0.011)$	$0.766(\pm 0.012)$	$0.758(\pm 0.008)$
1091	$K \to E$	$0.857(\pm 0.008)$	$0.832(\pm 0.007)$	$0.858(\pm 0.007)$	$0.848(\pm 0.005)$	$0.855(\pm 0.005)^{'}$	$0.850(\pm 0.005)$	$0.865(\pm 0.007)$	$0.854(\pm 0.004)$
1092	Avg.	$0.786(\pm 0.010)$	$0.771(\pm 0.009)$	$0.784(\pm 0.010)$	$0.780(\pm 0.008)$	$0.794(\pm 0.008)$	$0.782 (\pm 0.008)$	$0.790 (\pm 0.010)$	$0.789(\pm 0.006)$

Table 16: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on Amazon Reviews computed with domain adaptation method MMDA. 

		Cross-Validation f	for Binary Classifie	er		Aggre	gation	
Scenario	KuLSIF	Exp	LR	SQ	KuLSIF	Exp	LR	SQ
$B \to D$	$  0.804(\pm 0.008)$	$0.778(\pm 0.006)$	$0.806(\pm 0.007)$	$0.796(\pm 0.004)$	0.807(±0.006)	$0.787(\pm 0.004)$	$0.804(\pm 0.007)$	$0.803(\pm 0.002)$
$B \to E$	$0.785(\pm 0.012)$	$0.763(\pm 0.009)$	$0.782(\pm 0.010)$	$0.773(\pm 0.008)$	$0.789(\pm 0.011)$	$0.777(\pm 0.007)$	$0.777(\pm 0.010)$	$0.777(\pm 0.005)$
$B \to K$	$0.807(\pm 0.009)$	$0.784(\pm 0.005)$	$0.807(\pm 0.007)$	$0.797(\pm 0.005)$	0.809(±0.006)	$0.799(\pm 0.004)$	$0.811(\pm 0.007)$	0.806(±0.003
$D \to B$	$0.801(\pm 0.005)$	$0.790(\pm 0.004)$	$0.802(\pm 0.005)$	$0.807(\pm 0.003)$	$0.817(\pm 0.003)$	$0.798(\pm 0.003)$	$0.806(\pm 0.005)$	$0.812(\pm 0.001$
$D \rightarrow E$	$0.806(\pm 0.011)$	$0.787(\pm 0.015)$	$0.804(\pm 0.015)$	$0.797(\pm 0.013)$	0.815(±0.009)	$0.797(\pm 0.014)$	$0.808(\pm 0.015)$	$0.805(\pm 0.010)$
$D \to K$	$0.819(\pm 0.012)$	$0.801(\pm 0.014)$	$0.819(\pm 0.016)$	$0.810(\pm 0.013)$	$0.830(\pm 0.010)$	$0.824(\pm 0.013)$	$0.826(\pm 0.016)$	$0.812(\pm 0.012)$
$\mathrm{E}  ightarrow \mathrm{B}$	$0.719(\pm 0.025)$	$0.704(\pm 0.031)$	$0.721(\pm 0.031)$	$0.717(\pm 0.030)$	$0.732(\pm 0.024)$	$0.716(\pm 0.030)$	$0.723(\pm 0.031)$	$0.718(\pm 0.029)$
$\mathrm{E} \to \mathrm{D}$	$0.748(\pm 0.024)$	$0.729(\pm 0.017)$	$0.743(\pm 0.017)$	$0.743(\pm 0.015)$	$0.755(\pm 0.022)$	$0.737(\pm 0.016)$	$0.750(\pm 0.017)$	$0.748(\pm 0.013)$
$E \to K$	$0.883(\pm 0.012)$	$0.868(\pm 0.008)$	$0.881(\pm 0.009)$	$0.874(\pm 0.007)$	$0.885(\pm 0.010)$	$0.880(\pm 0.008)$	$0.888(\pm 0.009)$	$0.877(\pm 0.005)$
$K \to B$	$0.741(\pm 0.008)$	$0.730(\pm 0.007)$	$0.734(\pm 0.008)$	$0.730(\pm 0.006)$	$0.747(\pm 0.007)$	$0.735(\pm 0.005)$	$0.737(\pm 0.008)$	$0.736(\pm 0.004)$
$K \to D$	$0.766(\pm 0.007)$	$0.745(\pm 0.006)$	$0.762(\pm 0.007)$	$0.760(\pm 0.004)$	$0.773(\pm 0.005)$	$0.762(\pm 0.006)$	$0.765(\pm 0.007)$	$0.766(\pm 0.002)$
$K \to E$	$0.866(\pm 0.008)$	$0.849(\pm 0.006)$	$0.865(\pm 0.007)$	$0.855(\pm 0.005)$	0.881(±0.006)	$0.863(\pm 0.005)$	$0.873(\pm 0.007)$	$0.862(\pm 0.004)$
Avg.	$  0.795(\pm 0.012)$	$0.777(\pm 0.011)$	$0.794(\pm 0.012)$	$0.788(\pm 0.009)$	0.803(±0.010)	$0.790(\pm 0.010)$	$0.797(\pm 0.012)$	$0.793(\pm 0.008)$

Table 17: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on Amazon Re-views computed with domain adaptation method CoDATS.


1	1	1	8
1	1	1	9
1	1	2	0

1119		(	Cross-Validation f	for Binary Classifie	r		Aggre	gation	
1100	Scenario	KuLSIF	Exp	LR	SQ	KuLSIF	Exp	LR	SQ
1120	$B \rightarrow D$	$0.802(\pm 0.006)$	$0.793(\pm 0.008)$	$0.802(\pm 0.010)$	$0.805(\pm 0.007)$	$0.814(\pm 0.004)$	$0.812(\pm 0.007)$	$0.800(\pm 0.010)$	$0.818(\pm 0.005)$
1121	$B \to E$	$0.784(\pm 0.012)$	$0.743(\pm 0.011)$	$0.763(\pm 0.013)$	$0.755(\pm 0.010)$	$0.793(\pm 0.010)$	$0.749(\pm 0.010)$	$0.770(\pm 0.013)$	$0.762(\pm 0.009)$
1122	$B \to K$	$0.801(\pm 0.009)$	$0.783(\pm 0.007)$	$0.803(\pm 0.008)$	$0.802(\pm 0.005)$	$0.812(\pm 0.007)$	$0.795(\pm 0.006)$	$0.813(\pm 0.008)$	$0.818(\pm 0.004)$
1122	$D \rightarrow B$	$0.804(\pm 0.003)$	$0.788(\pm 0.002)$	$0.799(\pm 0.003)$	$0.798(\pm 0.001)$	$0.812(\pm 0.001)$	$0.797(\pm 0.001)$	$0.802(\pm 0.003)$	$0.805(\pm 0.001)$
1123	D  ightarrow E	$0.808(\pm 0.007)$	$0.787(\pm 0.008)$	$0.811(\pm 0.009)$	$0.807(\pm 0.007)$	$0.814(\pm 0.004)$	$0.801(\pm 0.007)$	$0.810(\pm 0.009)$	$0.819(\pm 0.005)$
110/	$D \rightarrow K$	$0.814(\pm 0.013)$	$0.806(\pm 0.017)$	$0.814(\pm 0.018)$	$0.813(\pm 0.015)$	$0.822(\pm 0.011)$	$0.818(\pm 0.016)$	$0.822(\pm 0.018)$	$0.818(\pm 0.013)$
1124	${\rm E}  ightarrow {\rm B}$	$0.713(\pm 0.017)$	$0.706(\pm 0.014)$	$0.717(\pm 0.014)$	$0.710(\pm 0.012)$	$0.724(\pm 0.015)$	$0.722(\pm 0.012)$	$0.727(\pm 0.014)$	$0.725(\pm 0.010)$
1125	$E \rightarrow D$	$0.748(\pm 0.009)$	$0.733(\pm 0.005)$	$0.748(\pm 0.006)$	$0.751(\pm 0.005)$	$0.758(\pm 0.007)$	$0.752(\pm 0.003)$	$0.758(\pm 0.006)$	$0.758(\pm 0.003)$
1106	$E \to K$	$0.878(\pm 0.015)$	$0.866(\pm 0.013)$	$0.874(\pm 0.015)$	$0.871(\pm 0.012)$	$0.894(\pm 0.013)$	$0.877(\pm 0.012)$	$0.884(\pm 0.015)$	$0.882(\pm 0.010)$
1120	$K \rightarrow B$	$0.739(\pm 0.014)$	$0.739(\pm 0.003)$	$0.750(\pm 0.003)$	$0.740(\pm 0.002)$	$0.749(\pm 0.012)$	$0.745(\pm 0.002)$	$0.760(\pm 0.003)$	$0.747(\pm 0.001)$
1127	$K \rightarrow D$	$0.770(\pm 0.020)$	$0.752(\pm 0.037)$	$0.766(\pm 0.039)$	$0.760(\pm 0.036)$	$0.782(\pm 0.019)$	$0.767(\pm 0.036)$	$0.776(\pm 0.039)$	$0.764(\pm 0.033)$
1100	$K \to E$	$0.863(\pm 0.011)$	$0.853(\pm 0.007)$	$0.865(\pm 0.007)$	$0.870(\pm 0.005)$	$0.879(\pm 0.008)$	$0.864(\pm 0.006)$	$0.874(\pm 0.007)$	$0.878 (\pm 0.003)$
1120	Avg.	$0.794(\pm 0.011)$	$0.779(\pm 0.011)$	$0.793(\pm 0.012)$	$0.790(\pm 0.010)$	$0.804(\pm 0.009)$	$0.792 (\pm 0.010)$	$0.800 (\pm 0.012)$	$0.799 (\pm 0.008)$
1129									

Table 18: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on Amazon Re-views computed with domain adaptation method DANN. 

135 136									
		C	ross-Validation fo	or Binary Classifie	r		Aggre	gation	
137	Scenario	KuLSIF	Exp	LR	SQ	KuLSIF	Exp	LR	SQ
38	$B \to D$	$0.802(\pm 0.009)$	$0.786(\pm 0.010)$	$0.800(\pm 0.011)$	$0.800(\pm 0.008)$	0.813(±0.007)	$0.793(\pm 0.009)$	$0.808(\pm 0.011)$	$0.805(\pm 0.007)$
	$B \rightarrow E$	$0.779(\pm 0.009)$	$0.759(\pm 0.007)$	$0.777(\pm 0.007)$	$0.777(\pm 0.004)$	$0.778(\pm 0.006)$	$0.770(\pm 0.006)$	$0.779(\pm 0.007)$	$0.784(\pm 0.001)$
39	$B \to K$	$0.797(\pm 0.007)$	$0.776(\pm 0.017)$	$0.789(\pm 0.018)$	$0.785(\pm 0.016)$	$0.800(\pm 0.005)$	$0.783(\pm 0.016)$	$0.794(\pm 0.018)$	$0.791(\pm 0.014)$
10	$\mathbf{D} \to \mathbf{B}$	$0.797(\pm 0.008)$	$0.787(\pm 0.006)$	$0.796(\pm 0.007)$	$0.797(\pm 0.004)$	$0.813(\pm 0.006)$	$0.809(\pm 0.006)$	$0.796(\pm 0.007)$	$0.814(\pm 0.003)$
	$D \rightarrow E$	$0.798(\pm 0.008)$	$0.791(\pm 0.004)$	$0.800(\pm 0.005)$	$0.798(\pm 0.003)$	$0.799(\pm 0.006)$	$0.801(\pm 0.003)$	$0.802(\pm 0.005)$	$0.804(\pm 0.002)$
1	$D \to K$	$0.804(\pm 0.015)$	$0.794(\pm 0.015)$	$0.802(\pm 0.016)$	$0.803(\pm 0.014)$	$0.813(\pm 0.013)$	$0.796(\pm 0.014)$	$0.806(\pm 0.016)$	$0.805(\pm 0.012)$
2	${\rm E}  ightarrow {\rm B}$	$0.707(\pm 0.020)$	$0.681(\pm 0.014)$	$0.705(\pm 0.016)$	$0.695(\pm 0.014)$	$0.711(\pm 0.018)$	$0.695(\pm 0.014)$	$0.708(\pm 0.016)$	$0.705(\pm 0.012)$
~	$\mathrm{E} \to \mathrm{D}$	$0.738(\pm 0.011)$	$0.724(\pm 0.012)$	$0.737(\pm 0.013)$	$0.740(\pm 0.010)$	$0.744(\pm 0.008)$	$0.732(\pm 0.010)$	$0.744(\pm 0.013)$	$0.740(\pm 0.009)$
3	$E \to K$	$0.879(\pm 0.011)$	$0.859(\pm 0.012)$	$0.875(\pm 0.013)$	$0.865(\pm 0.011)$	$0.880(\pm 0.009)$	$0.877(\pm 0.010)$	$0.885(\pm 0.013)$	$0.877(\pm 0.009)$
14	$K \to B$	$0.727(\pm 0.014)$	$0.717(\pm 0.006)$	$0.735(\pm 0.007)$	$0.733(\pm 0.006)$	$0.741(\pm 0.013)$	$0.730(\pm 0.005)$	$0.737(\pm 0.007)$	$0.744(\pm 0.004)$
+4	$K \to D$	$0.754(\pm 0.026)$	$0.755(\pm 0.008)$	$0.765(\pm 0.009)$	$0.765(\pm 0.007)$	$0.752(\pm 0.023)$	$0.758(\pm 0.006)$	$0.769(\pm 0.009)$	$0.770(\pm 0.005)$
15	$K \to E$	$0.859(\pm 0.005)$	$0.841(\pm 0.004)$	$0.858(\pm 0.005)$	$0.859(\pm 0.003)$	$0.862(\pm 0.003)$	$0.850(\pm 0.004)$	$0.854(\pm 0.005)$	$0.865(\pm 0.000)$
46	Avg.	$0.787(\pm 0.012)$	$0.772(\pm 0.010)$	$0.787(\pm 0.010)$	$0.785(\pm 0.009)$	$0.792(\pm 0.010)$	$0.783(\pm 0.009)$	$0.790 (\pm 0.010)$	$0.792(\pm 0.007)$

Table 19: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on Amazon Reviews computed with domain adaptation method CDAN.

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		(	Cross-Validation f	or Binary Classifie	er		Aggre	gation	
00	Scenario	KuLSIF	Exp	LR	SQ	KuLSIF	Exp	LR	SQ
6	$B \rightarrow D$	$0.803(\pm 0.015)$	$0.790(\pm 0.011)$	$0.803(\pm 0.011)$	$0.795(\pm 0.009)$	$0.816(\pm 0.013)$	$0.798(\pm 0.009)$	$0.813(\pm 0.011)$	$0.804(\pm 0.007)$
7	$B \rightarrow E$	$0.788(\pm 0.004)$	$0.772(\pm 0.015)$	$0.786(\pm 0.016)$	$0.782(\pm 0.014)$	$0.794(\pm 0.003)$	$0.792(\pm 0.014)$	$0.793(\pm 0.016)$	$0.796(\pm 0.012)$
	$B \to K$	$0.804(\pm 0.012)$	$0.797(\pm 0.014)$	$0.807(\pm 0.015)$	$0.803(\pm 0.013)$	$0.812(\pm 0.009)$	$0.812(\pm 0.013)$	$0.809(\pm 0.015)$	$0.805(\pm 0.011)$
8	D  ightarrow B	$0.801(\pm 0.005)$	$0.783(\pm 0.003)$	$0.802(\pm 0.005)$	$0.805(\pm 0.003)$	$0.813(\pm 0.003)$	$0.794(\pm 0.002)$	$0.810(\pm 0.005)$	$0.820(\pm 0.001)$
0	$D \rightarrow E$	$0.803(\pm 0.008)$	$0.786(\pm 0.008)$	$0.801(\pm 0.009)$	$0.804(\pm 0.007)$	$0.815(\pm 0.006)$	$0.791(\pm 0.007)$	$0.805(\pm 0.009)$	$0.821(\pm 0.005)$
)5	$D \rightarrow K$	$0.803(\pm 0.029)$	$0.793(\pm 0.015)$	$0.805(\pm 0.017)$	$0.810(\pm 0.014)$	$0.813(\pm 0.028)$	$0.809(\pm 0.014)$	$0.807(\pm 0.017)$	$0.812(\pm 0.014)$
50	$E \rightarrow B$	$0.719(\pm 0.021)$	$0.704(\pm 0.021)$	$0.719(\pm 0.022)$	$0.714(\pm 0.020)$	$0.733(\pm 0.020)$	$0.717(\pm 0.020)$	$0.725(\pm 0.022)$	$0.724(\pm 0.018)$
-1	$E \rightarrow D$	$0.749(\pm 0.004)$	$0.735(\pm 0.008)$	$0.746(\pm 0.009)$	$0.738(\pm 0.007)$	$0.764(\pm 0.002)$	$0.754(\pm 0.008)$	$0.753(\pm 0.009)$	$0.740(\pm 0.005)$
	$E \rightarrow K$	$0.883(\pm 0.010)$	$0.854(\pm 0.007)$	$0.881(\pm 0.008)$	$0.873(\pm 0.007)$	$0.898(\pm 0.008)$	$0.862(\pm 0.007)$	$0.890(\pm 0.008)$	$0.871(\pm 0.004)$
2	$K \rightarrow B$	$0.739(\pm 0.010)$	$0.720(\pm 0.017)$	$0.732(\pm 0.018)$	$0.727(\pm 0.016)$	$0.738(\pm 0.008)$	$0.731(\pm 0.016)$	$0.732(\pm 0.018)$	$0.732(\pm 0.014)$
0	$K \rightarrow D$	$0.767(\pm 0.008)$	$0.753(\pm 0.014)$	$0.770(\pm 0.015)$	$0.770(\pm 0.012)$	$0.773(\pm 0.005)$	$0.764(\pm 0.013)$	$0.766(\pm 0.015)$	$0.782(\pm 0.010)$
03	$K \rightarrow E$	$0.864(\pm 0.006)$	$0.847(\pm 0.006)$	$0.863(\pm 0.007)$	$0.858(\pm 0.004)$	$0.870(\pm 0.004)$	$0.858(\pm 0.005)$	$0.870(\pm 0.007)$	$0.870(\pm 0.002)$
64	Avg.	$0.794(\pm 0.011)$	$0.778(\pm 0.012)$	$0.793(\pm 0.013)$	$0.790(\pm 0.011)$	$0.803(\pm 0.009)$	$0.790 (\pm 0.011)$	$0.798 (\pm 0.013)$	$0.798 (\pm 0.009)$
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Table 20: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on Amazon Reviews computed with domain adaptation method DSAN.

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1173		(	Cross-Validation f	or Binary Classifie	r		Aggre	gation	
117/	Scenario	KuLSIF	Exp	ĹR	SQ	KuLSIF	Exp	LR	SQ
11/4	$B \rightarrow D$	$0.812(\pm 0.004)$	$0.795(\pm 0.004)$	$0.811(\pm 0.005)$	$0.804(\pm 0.003)$	0.825(±0.003)	$0.804(\pm 0.003)$	$0.810(\pm 0.005)$	$0.817(\pm 0.000)$
1175	$B \to E$	$0.786(\pm 0.007)$	$0.769(\pm 0.008)$	$0.779(\pm 0.008)$	$0.771(\pm 0.005)$	$0.795(\pm 0.005)$	$0.784(\pm 0.007)$	$0.786(\pm 0.008)$	$0.784(\pm 0.003)$
1176	$B \to K$	$0.809(\pm 0.006)$	$0.793(\pm 0.006)$	$0.797(\pm 0.007)$	$0.794(\pm 0.005)$	$0.816(\pm 0.004)$	$0.801(\pm 0.004)$	$0.797(\pm 0.007)$	$0.805(\pm 0.002)$
1170	D  ightarrow B	$0.806(\pm 0.009)$	$0.801(\pm 0.008)$	$0.811(\pm 0.009)$	$0.807(\pm 0.007)$	$0.809(\pm 0.007)$	$0.812(\pm 0.008)$	$0.809(\pm 0.009)$	$0.812(\pm 0.005)$
1177	$D \rightarrow E$	$0.804(\pm 0.012)$	$0.789(\pm 0.021)$	$0.802(\pm 0.022)$	$0.800(\pm 0.021)$	$0.810(\pm 0.011)$	$0.813(\pm 0.020)$	$0.806(\pm 0.022)$	$0.805(\pm 0.020)$
1170	$D \rightarrow K$	$0.830(\pm 0.012)$	$0.809(\pm 0.017)$	$0.823(\pm 0.018)$	$0.817(\pm 0.016)$	$0.844(\pm 0.010)$	$0.826(\pm 0.017)$	$0.832(\pm 0.018)$	$0.829(\pm 0.014)$
1170	$E \rightarrow B$	$0.686(\pm 0.016)$	$0.675(\pm 0.018)$	$0.685(\pm 0.019)$	$0.680(\pm 0.017)$	$0.696(\pm 0.013)$	$0.687(\pm 0.017)$	$0.689(\pm 0.019)$	$0.684(\pm 0.016)$
1179	$E \rightarrow D$	$0.711(\pm 0.017)$	$0.706(\pm 0.016)$	$0.715(\pm 0.016)$	$0.708(\pm 0.015)$	$0.727(\pm 0.016)$	$0.711(\pm 0.015)$	$0.715(\pm 0.016)$	$0.726(\pm 0.013)$
1100	$E \rightarrow K$	$0.885(\pm 0.009)$	$0.868(\pm 0.006)$	$0.880(\pm 0.008)$	$0.876(\pm 0.005)$	$0.898(\pm 0.008)$	$0.878(\pm 0.005)$	$0.886(\pm 0.008)$	$0.885(\pm 0.002)$
1180	K  ightarrow B	$0.720(\pm 0.011)$	$0.717(\pm 0.010)$	$0.731(\pm 0.011)$	$0.732(\pm 0.009)$	$0.730(\pm 0.010)$	$0.722(\pm 0.008)$	$0.729(\pm 0.011)$	$0.737(\pm 0.007)$
1181	$K \rightarrow D$	$0.729(\pm 0.013)$	$0.732(\pm 0.009)$	$0.748(\pm 0.010)$	$0.750(\pm 0.009)$	$0.742(\pm 0.011)$	$0.733(\pm 0.008)$	$0.746(\pm 0.010)$	$0.764(\pm 0.007)$
1100	$K \to E$	$0.863(\pm 0.013)$	$0.857(\pm 0.008)$	$0.870(\pm 0.009)$	$0.867(\pm 0.008)$	$0.872(\pm 0.011)$	$0.872(\pm 0.008)$	$0.880(\pm 0.009)$	$0.876(\pm 0.005)$
1102	Avg.	$0.787(\pm 0.011)$	$0.776(\pm 0.011)$	$0.788(\pm 0.012)$	$0.784(\pm 0.010)$	$0.797(\pm 0.009)$	$0.787 (\pm 0.010)$	$0.790 (\pm 0.012)$	$0.794 (\pm 0.008)$
1183									

Table 21: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on Amazon Reviews computed with domain adaptation method DIRT.

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1190		C	ross-Validation fo	r Binary Classifie	er		Aggre	gation	
1191	Scenario	KuLSIF	Exp	ĹR	SQ	KuLSIF	Exp	LR	SQ
1192	$B \to D$	$0.794(\pm 0.005)$	$0.770(\pm 0.005)$	$0.786(\pm 0.006)$	$0.778(\pm 0.004)$	$0.801(\pm 0.003)$	$0.787(\pm 0.003)$	$0.793(\pm 0.006)$	$0.784(\pm 0.002)$
	$B \to E$	$0.760(\pm 0.012)$	$0.744(\pm 0.010)$	$0.756(\pm 0.011)$	$0.755(\pm 0.009)$	$0.764(\pm 0.010)$	$0.750(\pm 0.010)$	$0.761(\pm 0.011)$	$0.762(\pm 0.007)$
1193	$B \to K$	$0.782(\pm 0.018)$	$0.765(\pm 0.015)$	$0.781(\pm 0.017)$	$0.776(\pm 0.014)$	$0.784(\pm 0.015)$	$0.778(\pm 0.015)$	$0.786(\pm 0.017)$	$0.785(\pm 0.012)$
1194	$\mathbf{D}\to\mathbf{B}$	$0.794(\pm 0.010)$	$0.780(\pm 0.004)$	$0.794(\pm 0.005)$	$0.785(\pm 0.003)$	$0.798(\pm 0.008)$	$0.787(\pm 0.004)$	$0.795(\pm 0.005)$	$0.795(\pm 0.001)$
1104	$D \to E$	$0.783(\pm 0.006)$	$0.768(\pm 0.004)$	$0.776(\pm 0.005)$	$0.776(\pm 0.004)$	$0.790(\pm 0.004)$	$0.791(\pm 0.004)$	$0.779(\pm 0.005)$	$0.792(\pm 0.002)$
1195	$D \to K$	$0.789(\pm 0.013)$	$0.771(\pm 0.011)$	$0.789(\pm 0.011)$	$0.779(\pm 0.009)$	$0.786(\pm 0.011)$	$0.780(\pm 0.010)$	$0.796(\pm 0.011)$	$0.785(\pm 0.007)$
1106	${\rm E}  ightarrow {\rm B}$	$0.711(\pm 0.021)$	$0.694(\pm 0.017)$	$0.706(\pm 0.018)$	$0.702(\pm 0.016)$	$0.721(\pm 0.019)$	$0.709(\pm 0.016)$	$0.706(\pm 0.018)$	$0.717(\pm 0.014)$
1190	$\mathrm{E} \to \mathrm{D}$	$0.732(\pm 0.007)$	$0.722(\pm 0.007)$	$0.731(\pm 0.007)$	$0.726(\pm 0.005)$	$0.746(\pm 0.004)$	$0.729(\pm 0.007)$	$0.734(\pm 0.007)$	$0.728(\pm 0.003)$
1197	$E \to K$	$0.875(\pm 0.011)$	$0.861(\pm 0.010)$	$0.874(\pm 0.012)$	$0.870(\pm 0.010)$	$0.882(\pm 0.008)$	$0.885(\pm 0.009)$	$0.880(\pm 0.012)$	$0.876(\pm 0.008)$
1100	$K \to B$	$0.723(\pm 0.007)$	$0.701(\pm 0.004)$	$0.723(\pm 0.005)$	$0.725(\pm 0.003)$	$0.726(\pm 0.005)$	$0.706(\pm 0.003)$	$0.729(\pm 0.005)$	$0.742(\pm 0.001)$
1190	$K \to D$	$0.748(\pm 0.014)$	$0.726(\pm 0.014)$	$0.750(\pm 0.014)$	$0.743(\pm 0.012)$	$0.748(\pm 0.013)$	$0.740(\pm 0.013)$	$0.757(\pm 0.014)$	$0.754(\pm 0.010)$
1199	$K \to E$	$0.858(\pm 0.008)$	$0.833(\pm 0.006)$	$0.854(\pm 0.007)$	$0.849(\pm 0.005)$	$0.867(\pm 0.006)$	$0.838(\pm 0.005)$	$0.858(\pm 0.007)$	$0.858(\pm 0.003)$
1200	Avg.	$0.779(\pm 0.011)$	$0.761(\pm 0.009)$	$0.777(\pm 0.010)$	$0.772(\pm 0.008)$	$0.784(\pm 0.009)$	$0.774 (\pm 0.008)$	$0.781 (\pm 0.010)$	$0.782(\pm 0.006)$

Table 22: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on Amazon Reviews computed with domain adaptation method AdvSKM.

		Cross-Validation f	for Binary Classifie	er		Aggre	gation	
Scenario	KuLSIF	Exp	LR	SQ	KuLSIF	Exp	LR	SQ
$B \to D$	$  0.794(\pm 0.007)$	$0.777(\pm 0.008)$	$0.792(\pm 0.010)$	$0.782(\pm 0.008)$	$0.794(\pm 0.006)$	$0.788(\pm 0.007)$	$0.798(\pm 0.010)$	$0.794(\pm 0.0$
$B \to E$	$0.761(\pm 0.012)$	$0.746(\pm 0.018)$	$0.756(\pm 0.018)$	$0.755(\pm 0.017)$	$0.770(\pm 0.010)$	$0.766(\pm 0.017)$	$0.756(\pm 0.018)$	$0.773(\pm 0.1)$
$B \to K$	$0.781(\pm 0.017)$	$0.764(\pm 0.021)$	$0.776(\pm 0.022)$	$0.776(\pm 0.020)$	$0.792(\pm 0.015)$	$0.781(\pm 0.020)$	$0.781(\pm 0.022)$	0.787(±0.
$D \to B$	$0.790(\pm 0.002)$	$0.776(\pm 0.002)$	$0.789(\pm 0.003)$	$0.783(\pm 0.001)$	$0.795(\pm 0.000)$	$0.792(\pm 0.002)$	$0.790(\pm 0.003)$	$0.795(\pm 0.5)$
$D \to E$	$0.781(\pm 0.004)$	$0.756(\pm 0.003)$	$0.772(\pm 0.004)$	$0.777(\pm 0.002)$	$0.790(\pm 0.002)$	$0.767(\pm 0.002)$	$0.778(\pm 0.004)$	$0.783(\pm 0.00)$
$D \to K$	$0.789(\pm 0.015)$	$0.770(\pm 0.014)$	$0.788(\pm 0.015)$	$0.785(\pm 0.014)$	$0.800(\pm 0.013)$	$0.783(\pm 0.013)$	$0.798(\pm 0.015)$	$0.792(\pm 0$
$E \to B$	$0.699(\pm 0.012)$	$0.679(\pm 0.013)$	$0.693(\pm 0.014)$	$0.689(\pm 0.013)$	$0.710(\pm 0.011)$	$0.698(\pm 0.012)$	$0.701(\pm 0.014)$	0.699(±0
$E \to D$	$0.735(\pm 0.011)$	$0.722(\pm 0.009)$	$0.732(\pm 0.010)$	$0.722(\pm 0.009)$	$0.744(\pm 0.008)$	$0.724(\pm 0.008)$	$0.734(\pm 0.010)$	$0.727(\pm 0$
$E \to K$	$0.873(\pm 0.009)$	$0.857(\pm 0.007)$	$0.872(\pm 0.008)$	$0.862(\pm 0.006)$	$0.884(\pm 0.007)$	$0.865(\pm 0.007)$	$0.881(\pm 0.008)$	0.863(±0
$K \to B$	$0.722(\pm 0.006)$	$0.703(\pm 0.012)$	$0.717(\pm 0.013)$	$0.711(\pm 0.011)$	$0.723(\pm 0.003)$	$0.709(\pm 0.011)$	$0.713(\pm 0.013)$	$0.724(\pm 0$
$K \to D$	$0.748(\pm 0.008)$	$0.734(\pm 0.008)$	$0.752(\pm 0.009)$	$0.753(\pm 0.006)$	0.760(±0.006)	$0.742(\pm 0.006)$	$0.762(\pm 0.009)$	$0.759(\pm 0$
$K \to E$	$0.856(\pm 0.006)$	$0.834(\pm 0.007)$	$0.854(\pm 0.007)$	$0.847(\pm 0.006)$	0.864(±0.004)	$0.849(\pm 0.006)$	$0.860(\pm 0.007)$	$0.857(\pm 0$
Avg.	$0.777(\pm 0.009)$	$0.760(\pm 0.010)$	$0.774(\pm 0.011)$	$0.770(\pm 0.009)$	0.786(±0.007)	$0.772(\pm 0.009)$	$0.779(\pm 0.011)$	$0.779(\pm 0$

Table 23: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on Amazon Reviews computed with domain adaptation method HoMM.

		(	Cross-Validation f	or Binary Classifie	er		Aggre	gation	
	Scenario	KuLSIF	Exp	ĹR	SQ	KuLSIF	Exp	LR	SQ
-	$B \rightarrow D$	$0.790(\pm 0.009)$	$0.775(\pm 0.006)$	$0.790(\pm 0.008)$	$0.783(\pm 0.006)$	$0.794(\pm 0.007)$	$0.797(\pm 0.005)$	$0.796(\pm 0.008)$	$0.789(\pm 0.004)$
	$B \rightarrow E$	$0.763(\pm 0.014)$	$0.749(\pm 0.015)$	$0.760(\pm 0.016)$	$0.750(\pm 0.014)$	$0.774(\pm 0.012)$	$0.759(\pm 0.013)$	$0.763(\pm 0.016)$	$0.752(\pm 0.012)$
	$B \rightarrow K$	$0.783(\pm 0.014)$	$0.774(\pm 0.022)$	$0.779(\pm 0.022)$	$0.772(\pm 0.020)$	$0.793(\pm 0.012)$	$0.787(\pm 0.021)$	$0.786(\pm 0.022)$	$0.780(\pm 0.018)$
	$D \rightarrow B$	$0.795(\pm 0.006)$	$0.780(\pm 0.007)$	$0.791(\pm 0.008)$	$0.783(\pm 0.006)$	$0.796(\pm 0.004)$	$0.799(\pm 0.006)$	$0.793(\pm 0.008)$	$0.790(\pm 0.005)$
	$D \rightarrow E$	$0.784(\pm 0.004)$	$0.757(\pm 0.007)$	$0.778(\pm 0.008)$	$0.782(\pm 0.005)$	0.790(±0.001)	$0.776(\pm 0.007)$	$0.784(\pm 0.008)$	$0.792(\pm 0.004)$
	$D \rightarrow K$	$0.789(\pm 0.021)$	$0.780(\pm 0.014)$	$0.790(\pm 0.015)$	$0.781(\pm 0.014)$	$0.796(\pm 0.018)$	$0.787(\pm 0.014)$	$0.792(\pm 0.015)$	$0.789(\pm 0.011)$
	$E \rightarrow B$	$0.705(\pm 0.024)$	$0.680(\pm 0.022)$	$0.699(\pm 0.024)$	$0.702(\pm 0.022)$	$0.713(\pm 0.022)$	$0.692(\pm 0.021)$	$0.700(\pm 0.024)$	$0.713(\pm 0.020)$
	$E \rightarrow D$	$0.736(\pm 0.007)$	$0.727(\pm 0.007)$	$0.740(\pm 0.007)$	$0.739(\pm 0.005)$	$0.746(\pm 0.005)$	$0.744(\pm 0.005)$	$0.737(\pm 0.007)$	$0.742(\pm 0.003)$
	$E \rightarrow K$	$0.877(\pm 0.011)$	$0.862(\pm 0.007)$	$0.874(\pm 0.009)$	$0.879(\pm 0.007)$	$0.885(\pm 0.009)$	$0.880(\pm 0.006)$	$0.884(\pm 0.009)$	$0.890(\pm 0.004)$
	$K \rightarrow B$	$0.726(\pm 0.003)$	$0.714(\pm 0.006)$	$0.722(\pm 0.007)$	$0.719(\pm 0.005)$	$0.734(\pm 0.001)$	$0.721(\pm 0.006)$	$0.731(\pm 0.007)$	$0.737(\pm 0.004)$
	$K \rightarrow D$	$0.751(\pm 0.013)$	$0.736(\pm 0.007)$	$0.752(\pm 0.009)$	$0.750(\pm 0.006)$	$0.756(\pm 0.011)$	$0.750(\pm 0.007)$	$0.760(\pm 0.009)$	$0.759(\pm 0.004)$
	$K \rightarrow E$	$0.856(\pm 0.008)$	$0.837(\pm 0.006)$	$0.856(\pm 0.007)$	$0.852(\pm 0.005)$	$0.862(\pm 0.005)$	$0.837(\pm 0.004)$	$0.865(\pm 0.007)$	$0.864(\pm 0.003)$
-	Avg.	$0.780(\pm 0.011)$	$0.764(\pm 0.011)$	$0.778(\pm 0.012)$	$0.774(\pm 0.010)$	0.787(±0.009)	$0.777(\pm 0.010)$	$0.782(\pm 0.012)$	$0.783(\pm 0.008)$

Table 24: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on Amazon Reviews computed with domain adaptation method DDC.

1243 **Cross-Validation for Binary Classifier** Aggregation KuLSIF KuLSIF Scenario Exp SO Exp LR SO LR 1244  $0.795(\pm 0.009)$  $0.799(\pm 0.011)$  $0.790(\pm 0.009)$  $0.801(\pm 0.006)$  $B \to D$  $0.801(\pm 0.010)$  $0.814(\pm 0.008)$  $0.812(\pm 0.008)$  $\mathbf{0.804} (\pm \mathbf{0.011})$ 1245  $0.753(\pm 0.012)$  $0.756(\pm 0.010)$  $B \to E$  $0.773(\pm 0.008)$  $0.763(\pm 0.012)$  $0.781(\pm 0.006)$  $0.762(\pm 0.011)$  $0.772(\pm 0.012)$  $0.765(\pm 0.008)$  $B \to K$  $0.785(\pm 0.017)$  $0.765(\pm 0.017)$  $0.781(\pm 0.018)$  $0.773(\pm 0.016)$  $0.797(\pm 0.016)$ 1246  $0.782(\pm 0.017)$  $0.789(\pm 0.018)$  $0.779(\pm 0.013)$  $D \to B$  $0.797(\pm 0.004)$  $0.783(\pm 0.002)$  $0.794(\pm 0.003)$  $0.789(\pm 0.001)$  $0.803(\pm 0.002)$  $0.794(\pm 0.000)$  $0.804(\pm 0.003)$  $0.803(\pm 0.000)$ 1247  $D \to E$  $0.785(\pm 0.003)$  $0.769(\pm 0.009)$  $0.779(\pm 0.011)$  $0.769(\pm 0.009)$  $0.793(\pm 0.002)$ 0.778(±0.008)  $0.777(\pm 0.011)$  $0.775(\pm 0.007)$  $D \to K$  $0.792(\pm 0.014)$  $0.774(\pm 0.016)$  $0.791(\pm 0.016)$  $0.785(\pm 0.013)$  $0.799(\pm 0.012)$  $0.787(\pm 0.015)$  $0.792(\pm 0.016)$  $0.785(\pm 0.010)$ 1248  $E \to B$  $0.710(\pm 0.024)$  $0.695(\pm 0.022)$  $0.709(\pm 0.024)$  $0.706(\pm 0.022)$  $0.713(\pm 0.022)$  $0.704(\pm 0.022)$  $0.717(\pm 0.024)$  $0.709(\pm 0.020)$ 1249  $E \to D$  $0.739(\pm 0.004)$  $0.724(\pm 0.002)$  $0.739(\pm 0.003)$  $0.729(\pm 0.000)$  $0.747(\pm 0.002)$  $0.731(\pm 0.002)$  $0.748(\pm 0.003)$  $0.738(\pm 0.001)$  $E \to K$  $0.878(\pm 0.007)$  $0.863(\pm 0.007)$  $0.876(\pm 0.009)$  $0.875(\pm 0.007)$  $0.894(\pm 0.005)$  $0.882(\pm 0.006)$  $0.878(\pm 0.009)$  $0.886(\pm 0.005)$ 1250 0.735(+0.008) $K \to B$  $0.739(\pm 0.009)$  $0.720(\pm 0.007)$  $0.738(\pm 0.005)$  $0.754(\pm 0.007)$  $0.735(\pm 0.007)$  $0.733(\pm 0.008)$  $0.756(\pm 0.003)$ 1251  $K \to D$  $0.755(\pm 0.015)$  $0.733(\pm 0.016)$  $0.749(\pm 0.017)$  $0.746(\pm 0.014)$  $0.770(\pm 0.013)$  $0.743(\pm 0.015)$  $0.754(\pm 0.017)$  $0.753(\pm 0.011)$  $K \rightarrow E$  $0.857(\pm 0.010)$  $0.830(\pm 0.004)$  $0.855(\pm 0.005)$  $0.851(\pm 0.004)$  $0.864(\pm 0.008)$  $0.842(\pm 0.003)$  $0.850(\pm 0.005)$  $0.863(\pm 0.002)$ 1252  $0.784(\pm 0.010)$  $0.767(\pm 0.010)$  $0.781(\pm 0.011)$  $0.776(\pm 0.009)$  $0.794(\pm 0.008)$  $0.779(\pm 0.009)$  $0.785(\pm 0.011)$  $0.784(\pm 0.007)$ Avg. 1253

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Table 25: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on Amazon Reviews computed with domain adaptation method DeepCoral.

	(	Cross-Validation f	or Binary Classifie	er		Aggre	gation	
Scenario	KuLSIF	Exp	ĹR	SQ	KuLSIF	Exp	LR	SQ
$B \rightarrow D$	$  0.799(\pm 0.005)$	$0.785(\pm 0.007)$	$0.794(\pm 0.009)$	$0.792(\pm 0.007)$	$0.809(\pm 0.002)$	$0.796(\pm 0.007)$	$0.803(\pm 0.009)$	$0.790(\pm 0.004)$
$3 \rightarrow E$	$0.779(\pm 0.014)$	$0.747(\pm 0.020)$	$0.761(\pm 0.021)$	$0.756(\pm 0.019)$	$0.787(\pm 0.012)$	$0.759(\pm 0.018)$	$0.756(\pm 0.021)$	$0.758(\pm 0.017)$
$B \rightarrow K$	$0.781(\pm 0.029)$	$0.782(\pm 0.010)$	$0.793(\pm 0.011)$	$0.783(\pm 0.009)$	$0.788(\pm 0.026)$	$0.791(\pm 0.009)$	$0.799(\pm 0.011)$	$0.791(\pm 0.007)$
$D \to B$	$0.798(\pm 0.012)$	$0.791(\pm 0.006)$	$0.802(\pm 0.007)$	$0.792(\pm 0.005)$	$0.799(\pm 0.010)$	$0.796(\pm 0.005)$	$0.806(\pm 0.007)$	$0.798(\pm 0.003)$
D  ightarrow E	$0.795(\pm 0.009)$	$0.777(\pm 0.009)$	$0.802(\pm 0.010)$	$0.792(\pm 0.008)$	$0.811(\pm 0.007)$	$0.795(\pm 0.008)$	$0.812(\pm 0.010)$	$0.800(\pm 0.006)$
$D \to K$	$0.799(\pm 0.018)$	$0.786(\pm 0.013)$	$0.804(\pm 0.015)$	$0.796(\pm 0.013)$	$0.812(\pm 0.016)$	$0.797(\pm 0.013)$	$0.803(\pm 0.015)$	$0.804(\pm 0.011)$
$E \rightarrow B$	$0.719(\pm 0.014)$	$0.714(\pm 0.016)$	$0.721(\pm 0.017)$	$0.726(\pm 0.016)$	$0.732(\pm 0.012)$	$0.727(\pm 0.015)$	$0.727(\pm 0.017)$	$0.732(\pm 0.013)$
$\mathrm{E}  ightarrow \mathrm{D}$	0.750(±0.009)	$0.730(\pm 0.007)$	$0.744(\pm 0.008)$	$0.742(\pm 0.007)$	$0.746(\pm 0.007)$	$0.738(\pm 0.006)$	$0.752(\pm 0.008)$	$0.752(\pm 0.005)$
$E \to K$	$0.875(\pm 0.015)$	$0.857(\pm 0.009)$	$0.875(\pm 0.010)$	$0.867(\pm 0.007)$	$0.879(\pm 0.013)$	$0.875(\pm 0.008)$	$0.872(\pm 0.010)$	$0.880(\pm 0.004)$
$K \to B$	$0.745(\pm 0.004)$	$0.719(\pm 0.004)$	$0.731(\pm 0.004)$	$0.731(\pm 0.003)$	$0.748(\pm 0.003)$	$0.727(\pm 0.003)$	$0.733(\pm 0.004)$	$0.732(\pm 0.001)$
$K \to D$	$0.775(\pm 0.019)$	$0.723(\pm 0.030)$	$0.740(\pm 0.031)$	$0.730(\pm 0.029)$	$0.783(\pm 0.018)$	$0.732(\pm 0.030)$	$0.749(\pm 0.031)$	$0.740(\pm 0.027)$
$K \to E$	$0.864(\pm 0.010)$	$0.859(\pm 0.005)$	$0.867(\pm 0.006)$	$0.865(\pm 0.004)$	$0.868(\pm 0.008)$	$0.866(\pm 0.004)$	$0.870(\pm 0.006)$	$0.866(\pm 0.002)$
Avg.	$0.790(\pm 0.013)$	$0.773(\pm 0.011)$	$0.786(\pm 0.012)$	$0.781(\pm 0.011)$	$0.797(\pm 0.011)$	$0.783(\pm 0.011)$	$0.790(\pm 0.012)$	0.787(±0.008)

Table 26: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on Amazon Reviews computed with domain adaptation method CMD.

	C	ross-Validation fo	or Binary Classifi	er		Aggre	gation	
Scenario	KuLSIF	Exp	ĹR	SQ	KuLSIF	Exp	LR	SQ
0  ightarrow 6	$0.746(\pm 0.008)$	$0.701(\pm 0.031)$	$0.716(\pm 0.026)$	$0.678(\pm 0.012)$	0.793(±0.022)	$0.740(\pm 0.001)$	$0.728(\pm 0.019)$	$0.702(\pm 0.011)$
$1 \rightarrow 6$	$0.897(\pm 0.002)$	$0.864(\pm 0.009)$	$0.867(\pm 0.006)$	$0.829(\pm 0.008)$	$0.953(\pm 0.029)$	$0.906(\pm 0.022)$	$0.891(\pm 0.000)$	$0.858(\pm 0.007)$
$2 \rightarrow 7$	$0.488(\pm 0.010)$	$0.484(\pm 0.009)$	$0.493(\pm 0.009)$	$0.460(\pm 0.005)$	$0.532(\pm 0.021)$	$0.528(\pm 0.022)$	$0.494(\pm 0.003)$	$0.475(\pm 0.004)$
$3 \rightarrow 8$	$0.839(\pm 0.012)$	$0.845(\pm 0.032)$	$0.864(\pm 0.012)$	$0.826(\pm 0.002)$	$0.877(\pm 0.019)$	$0.883(\pm 0.000)$	$0.877(\pm 0.006)$	$0.859(\pm 0.001)$
$4 \rightarrow 5$	$0.928(\pm 0.006)$	$0.456(\pm 0.410)$	$0.923(\pm 0.012)$	$0.888(\pm 0.002)$	0.975(±0.025)	$0.497(\pm 0.379)$	$0.938(\pm 0.006)$	$0.920(\pm 0.001)$
Avg.	$0.780(\pm 0.008)$	$0.670(\pm 0.098)$	$0.773(\pm 0.013)$	$0.736(\pm 0.006)$	0.826(±0.023)	$0.711(\pm 0.085)$	$0.786(\pm 0.007)$	$0.763(\pm 0.005)$

Table 27: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on HHAR computed with domain adaptation method MMDA.

	C	ross-Validation fo	or Binary Classifi	er	Aggregation					
Scenario	KuLSIF	Exp	ĹR	SQ	KuLSIF	Exp	LR	SQ		
$0 \rightarrow 6$	$0.596(\pm 0.048)$	$0.634(\pm 0.045)$	$0.631(\pm 0.043)$	$0.593(\pm 0.029)$	$0.638(\pm 0.017)$	$0.674(\pm 0.012)$	$0.643(\pm 0.038)$	$0.620(\pm 0.028)$		
$1 \rightarrow 6$	$0.939(\pm 0.006)$	$0.908(\pm 0.011)$	$0.906(\pm 0.013)$	$0.868(\pm 0.001)$	$0.982(\pm 0.024)$	$0.955(\pm 0.019)$	$0.919(\pm 0.006)$	$0.896(\pm 0.000)$		
$2 \rightarrow 7$	$0.472(\pm 0.005)$	$0.470(\pm 0.008)$	$0.476(\pm 0.008)$	$0.438(\pm 0.006)$	$0.516(\pm 0.025)$	$0.511(\pm 0.024)$	$0.493(\pm 0.002)$	$0.464(\pm 0.005)$		
$3 \rightarrow 8$	$0.960(\pm 0.030)$	$0.921(\pm 0.028)$	$0.934(\pm 0.030)$	$0.896(\pm 0.016)$	$1.005(\pm 0.002)$	$0.964(\pm 0.005)$	$0.954(\pm 0.024)$	$0.928(\pm 0.014)$		
4  ightarrow 5	$0.648(\pm 0.562)$	$0.947(\pm 0.013)$	$0.947(\pm 0.012)$	$0.909(\pm 0.002)$	0.682(±0.530)	$0.984(\pm 0.018)$	$0.958(\pm 0.006)$	$0.925(\pm 0.002)$		
Avg.	$0.723(\pm 0.130)$	$0.776(\pm 0.021)$	$0.779(\pm 0.021)$	$0.741(\pm 0.011)$	0.765(±0.120)	$0.818(\pm 0.016)$	$0.793(\pm 0.015)$	$0.767(\pm 0.010)$		

Table 28: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on HHAR com-1294 puted with domain adaptation method CoDATS. 1295

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	C	ross-Validation fo	or Binary Classifi	Aggregation				
Scenario	KuLSIF	Exp	LR	SQ	KuLSIF	Exp	LR	SQ
$0 \rightarrow 6$	$0.604(\pm 0.036)$	$0.652(\pm 0.043)$	$0.657(\pm 0.027)$	$0.619(\pm 0.013)$	0.647(±0.006)	$0.690(\pm 0.010)$	$0.669(\pm 0.021)$	$0.637(\pm 0.012)$
$1 \rightarrow 6$	$0.936(\pm 0.002)$	$0.890(\pm 0.038)$	$0.906(\pm 0.010)$	$0.868(\pm 0.004)$	$0.977(\pm 0.028)$	$0.935(\pm 0.006)$	$0.916(\pm 0.004)$	$0.891(\pm 0.002)$
$2 \rightarrow 7$	$0.327(\pm 0.284)$	$0.511(\pm 0.026)$	$0.533(\pm 0.045)$	$0.495(\pm 0.031)$	$0.367(\pm 0.253)$	$0.552(\pm 0.006)$	$0.541(\pm 0.038)$	$0.513(\pm 0.030)$
$3 \rightarrow 8$	$0.964(\pm 0.006)$	$0.919(\pm 0.007)$	$0.923(\pm 0.015)$	$0.885(\pm 0.001)$	$1.005(\pm 0.026)$	$0.964(\pm 0.026)$	$0.939(\pm 0.008)$	$0.900(\pm 0.001)$
$4 \rightarrow 5$	$0.654(\pm 0.566)$	$0.951(\pm 0.005)$	$0.957(\pm 0.010)$	$0.919(\pm 0.004)$	0.696(±0.536)	$0.998(\pm 0.026)$	$0.969(\pm 0.004)$	$0.960(\pm 0.003)$
Avg.	$0.697(\pm 0.179)$	$0.785(\pm 0.024)$	$0.795(\pm 0.021)$	$0.757(\pm 0.011)$	0.738(±0.170)	$0.828(\pm 0.015)$	$0.807(\pm 0.015)$	$0.780(\pm 0.010)$

Table 29: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on HHAR computed with domain adaptation method DANN.

	C	ross-Validation fo	or Binary Classifi	er	Aggregation					
Scenario	KuLSIF	Exp	ĹR	SQ	KuLSIF	Exp	LR	SQ		
$0 \rightarrow 6$	$0.622(\pm 0.009)$	$0.507(\pm 0.281)$	$0.666(\pm 0.014)$	$0.628(\pm 0.000)$	0.660(±0.022)	$0.558(\pm 0.249)$	$0.685(\pm 0.008)$	$0.658(\pm 0.002)$		
$1 \rightarrow 6$	$0.933(\pm 0.000)$	$0.906(\pm 0.008)$	$0.908(\pm 0.006)$	$0.870(\pm 0.008)$	$0.982(\pm 0.031)$	$0.940(\pm 0.025)$	$0.922(\pm 0.001)$	$0.899(\pm 0.007)$		
$2 \rightarrow 7$	$0.550(\pm 0.061)$	$0.547(\pm 0.061)$	$0.552(\pm 0.066)$	$0.514(\pm 0.052)$	$0.592(\pm 0.030)$	$0.592(\pm 0.029)$	$0.562(\pm 0.060)$	$0.533(\pm 0.050)$		
$3 \rightarrow 8$	$0.874(\pm 0.076)$	$0.863(\pm 0.059)$	$0.862(\pm 0.056)$	$0.829(\pm 0.042)$	$0.911(\pm 0.043)$	$0.910(\pm 0.028)$	$0.878(\pm 0.050)$	$0.850(\pm 0.041)$		
$4 \rightarrow 5$	$0.980(\pm 0.000)$	$0.707(\pm 0.423)$	$0.954(\pm 0.006)$	$0.916(\pm 0.008)$	$1.025(\pm 0.031)$	$0.749(\pm 0.391)$	$0.972(\pm 0.001)$	$0.935(\pm 0.007)$		
Avg.	$0.792(\pm 0.029)$	$0.706(\pm 0.166)$	$0.788(\pm 0.029)$	$0.751(\pm 0.022)$	0.834(±0.031)	$0.750(\pm 0.144)$	$0.804(\pm 0.024)$	$0.775(\pm 0.021)$		

Table 30: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on HHAR computed with domain adaptation method CDAN.

	C	ross-Validation fo	or Binary Classifi	er	Aggregation						
Scenario	KuLSIF	Exp	ĹR	SQ	KuLSIF	Exp	LR	SQ			
$0 \rightarrow 6$	$0.719(\pm 0.070)$	$0.350(\pm 0.289)$	$0.705(\pm 0.043)$	$0.667(\pm 0.029)$	0.753(±0.039)	$0.391(\pm 0.257)$	$0.720(\pm 0.038)$	$0.686(\pm 0.028)$			
$1 \rightarrow 6$	$0.929(\pm 0.000)$	$0.410(\pm 0.429)$	$0.893(\pm 0.023)$	$0.855(\pm 0.009)$	$0.975(\pm 0.031)$	$0.464(\pm 0.396)$	$0.911(\pm 0.018)$	$0.870(\pm 0.008)$			
$2 \rightarrow 7$	$0.496(\pm 0.000)$	$0.495(\pm 0.002)$	$0.495(\pm 0.001)$	$0.457(\pm 0.013)$	$0.538(\pm 0.031)$	$0.538(\pm 0.030)$	$0.509(\pm 0.006)$	$0.482(\pm 0.012)$			
$3 \rightarrow 8$	$0.971(\pm 0.005)$	$0.926(\pm 0.005)$	$0.927(\pm 0.005)$	$0.889(\pm 0.009)$	$1.009(\pm 0.027)$	$0.965(\pm 0.028)$	$0.937(\pm 0.001)$	$0.913(\pm 0.008)$			
$4 \rightarrow 5$	$0.654(\pm 0.566)$	$0.460(\pm 0.417)$	$0.939(\pm 0.005)$	$0.901(\pm 0.009)$	0.694(±0.535)	$0.503(\pm 0.385)$	$0.947(\pm 0.001)$	$0.925(\pm 0.008)$			
Avg.	$0.754(\pm 0.128)$	$0.528(\pm 0.228)$	$0.792(\pm 0.015)$	$0.754(\pm 0.014)$	0.794(±0.133)	$0.572(\pm 0.219)$	$0.805(\pm 0.013)$	$0.775(\pm 0.013)$			

Table 31: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on HHAR computed with domain adaptation method DSAN.

	C	ross-Validation fo	or Binary Classifi	er	Aggregation					
Scenario	KuLSIF	Exp	ĹR	SQ	KuLSIF	Exp	LR	SQ		
$0 \rightarrow 6$	$0.693(\pm 0.072)$	$0.694(\pm 0.050)$	$0.709(\pm 0.043)$	$0.671(\pm 0.029)$	0.737(±0.041)	$0.729(\pm 0.018)$	$0.729(\pm 0.037)$	$0.701(\pm 0.027)$		
$1 \rightarrow 6$	$0.938(\pm 0.000)$	$0.884(\pm 0.029)$	$0.904(\pm 0.010)$	$0.866(\pm 0.004)$	$0.985(\pm 0.031)$	$0.923(\pm 0.004)$	$0.909(\pm 0.004)$	$0.887(\pm 0.004)$		
$2 \rightarrow 7$	$0.194(\pm 0.336)$	$0.582(\pm 0.090)$	$0.545(\pm 0.041)$	$0.507(\pm 0.027)$	$0.234(\pm 0.306)$	$0.620(\pm 0.058)$	$0.548(\pm 0.036)$	$0.541(\pm 0.026)$		
$3 \rightarrow 8$	$0.848(\pm 0.007)$	$0.839(\pm 0.022)$	$0.842(\pm 0.011)$	$0.804(\pm 0.003)$	$0.887(\pm 0.024)$	$0.879(\pm 0.011)$	$0.856(\pm 0.006)$	$0.823(\pm 0.002)$		
$4 \rightarrow 5$	$0.984(\pm 0.004)$	$0.949(\pm 0.008)$	$0.951(\pm 0.009)$	$0.919(\pm 0.005)$	$1.026(\pm 0.026)$	$0.989(\pm 0.024)$	$0.964(\pm 0.002)$	$0.941(\pm 0.004)$		
Avg.	$0.731(\pm 0.084)$	$0.790(\pm 0.040)$	$0.790(\pm 0.023)$	$0.753(\pm 0.014)$	$0.774(\pm 0.086)$	$0.828(\pm 0.023)$	$0.801(\pm 0.017)$	$0.779(\pm 0.013)$		

Table 32: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on HHAR computed with domain adaptation method DIRT.

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12/11		0	ross-Validation fo	or Binary Classifi	er	Aggregation				
1341	Scenario	KuLSIF	Exp	ĹR	SQ	KuLSIF	Exp	LR	SQ	
1342	$0 \rightarrow 6$	$0.718(\pm 0.009)$	$0.714(\pm 0.010)$	$0.705(\pm 0.020)$	$0.667(\pm 0.006)$	0.766(±0.022)	$0.755(\pm 0.022)$	$0.721(\pm 0.014)$	$0.690(\pm 0.005)$	
1343	$1 \rightarrow 6$	$0.857(\pm 0.006)$	$0.835(\pm 0.026)$	$0.836(\pm 0.025)$	$0.798(\pm 0.011)$	0.893(±0.025)	$0.894(\pm 0.007)$	$0.840(\pm 0.019)$	$0.823(\pm 0.010)$	
19//	$2 \rightarrow 7$	$0.490(\pm 0.014)$	$0.497(\pm 0.010)$	$0.502(\pm 0.024)$	$0.464(\pm 0.010)$	$0.526(\pm 0.017)$	$0.541(\pm 0.022)$	$0.519(\pm 0.018)$	$0.492(\pm 0.008)$	
1344	$3 \rightarrow 8$	$0.810(\pm 0.002)$	$0.806(\pm 0.005)$	$0.807(\pm 0.005)$	$0.769(\pm 0.009)$	$0.856(\pm 0.029)$	$0.840(\pm 0.027)$	$0.819(\pm 0.001)$	$0.796(\pm 0.008)$	
1345	$4 \rightarrow 5$	$0.884(\pm 0.005)$	$0.875(\pm 0.014)$	$0.878(\pm 0.017)$	$0.840(\pm 0.003)$	$0.924(\pm 0.026)$	$0.921(\pm 0.019)$	$0.897(\pm 0.011)$	$0.874(\pm 0.002)$	
1346	Avg.	$0.752(\pm 0.007)$	$0.746(\pm 0.013)$	$0.746(\pm 0.018)$	$0.708(\pm 0.008)$	$0.793(\pm 0.024)$	$0.790 (\pm 0.019)$	$0.759 (\pm 0.012)$	$0.735 (\pm 0.006)$	
1347										

Table 33: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on HHAR com-puted with domain adaptation method AdvSKM.

352		C	ross-Validation fo	or Binary Classifi	Aggregation				
353	Scenario	KuLSIF	Exp	ĹR	SQ	KuLSIF	Exp	LR	SQ
54	$0 \rightarrow 6$	$0.732(\pm 0.010)$	$0.719(\pm 0.025)$	$0.725(\pm 0.024)$	$0.687(\pm 0.010)$	$0.782(\pm 0.021)$	$0.764(\pm 0.007)$	$0.742(\pm 0.018)$	$0.721(\pm 0.008)$
	$1 \rightarrow 6$	$0.879(\pm 0.011)$	$0.856(\pm 0.019)$	$0.853(\pm 0.024)$	$0.815(\pm 0.010)$	$0.917(\pm 0.020)$	$0.899(\pm 0.013)$	$0.866(\pm 0.017)$	$0.845(\pm 0.009)$
55	$2 \rightarrow 7$	$0.455(\pm 0.015)$	$0.466(\pm 0.029)$	$0.474(\pm 0.024)$	$0.436(\pm 0.010)$	$0.499(\pm 0.016)$	$0.515(\pm 0.002)$	$0.491(\pm 0.018)$	$0.466(\pm 0.009)$
56	$3 \rightarrow 8$	$0.818(\pm 0.005)$	$0.820(\pm 0.008)$	$0.822(\pm 0.004)$	$0.784(\pm 0.010)$	$0.859(\pm 0.026)$	$0.863(\pm 0.024)$	$0.835(\pm 0.002)$	$0.820(\pm 0.009)$
50	$4 \rightarrow 5$	$0.911(\pm 0.005)$	$0.449(\pm 0.399)$	$0.899(\pm 0.031)$	$0.861(\pm 0.017)$	$0.958(\pm 0.026)$	$0.496(\pm 0.366)$	$0.905(\pm 0.025)$	$0.894(\pm 0.016)$
10	Avg.	$0.759(\pm 0.009)$	$0.662(\pm 0.096)$	$0.754(\pm 0.021)$	$0.716(\pm 0.011)$	0.803(±0.022)	$0.707(\pm 0.083)$	$0.768(\pm 0.016)$	$0.749(\pm 0.010)$

Table 34: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on HHAR computed with domain adaptation method HoMM.

	C	ross-Validation fo	or Binary Classifi	er	Aggregation				
Scenario	KuLSIF	Exp	LR	SQ	KuLSIF	Exp	LR	SQ	
$0 \rightarrow 6$	$0.697(\pm 0.013)$	$0.349(\pm 0.286)$	$0.690(\pm 0.011)$	$0.652(\pm 0.003)$	$0.748(\pm 0.018)$	$0.397(\pm 0.255)$	$0.709(\pm 0.005)$	$0.680(\pm 0.003)$	
$1 \rightarrow 6$	$0.882(\pm 0.017)$	$0.639(\pm 0.413)$	$0.873(\pm 0.014)$	$0.835(\pm 0.000)$	$0.924(\pm 0.014)$	$0.677(\pm 0.381)$	$0.886(\pm 0.009)$	$0.864(\pm 0.001)$	
$2 \rightarrow 7$	$0.439(\pm 0.041)$	$0.440(\pm 0.036)$	$0.439(\pm 0.037)$	$0.401(\pm 0.023)$	$0.486(\pm 0.010)$	$0.476(\pm 0.004)$	$0.452(\pm 0.032)$	$0.422(\pm 0.023)$	
$3 \rightarrow 8$	$0.818(\pm 0.008)$	$0.621(\pm 0.342)$	$0.823(\pm 0.006)$	$0.785(\pm 0.008)$	$0.858(\pm 0.022)$	$0.663(\pm 0.310)$	$0.840(\pm 0.001)$	$0.813(\pm 0.007)$	
$4 \rightarrow 5$	$0.905(\pm 0.008)$	$0.219(\pm 0.000)$	$0.895(\pm 0.025)$	$0.857(\pm 0.011)$	0.955(±0.023)	$0.266(\pm 0.032)$	$0.908(\pm 0.019)$	$0.879(\pm 0.010)$	
Avg.	$0.748(\pm 0.017)$	$0.454(\pm 0.215)$	$0.744(\pm 0.019)$	$0.706(\pm 0.009)$	$0.794(\pm 0.018)$	$0.496 (\pm 0.196)$	$0.759 (\pm 0.013)$	$0.732 (\pm 0.009)$	

Table 35: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on HHAR computed with domain adaptation method DDC.

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		C	ross-Validation fo	or Binary Classifi	er	Aggregation				
	Scenario	KuLSIF	Exp	ĹR	SQ	KuLSIF	Exp	LR	SQ	
	$0 \rightarrow 6$	$0.728(\pm 0.019)$	$0.700(\pm 0.032)$	$0.717(\pm 0.025)$	$0.679(\pm 0.011)$	$0.768(\pm 0.012)$	$0.739(\pm 0.001)$	$0.733(\pm 0.019)$	$0.694(\pm 0.010)$	
	$1 \rightarrow 6$	$0.886(\pm 0.009)$	$0.845(\pm 0.039)$	$0.861(\pm 0.014)$	$0.823(\pm 0.000)$	$0.924(\pm 0.022)$	$0.890(\pm 0.008)$	$0.865(\pm 0.009)$	$0.842(\pm 0.001)$	
	$2 \rightarrow 7$	$0.460(\pm 0.012)$	$0.470(\pm 0.014)$	$0.480(\pm 0.020)$	$0.442(\pm 0.006)$	$0.509(\pm 0.019)$	$0.512(\pm 0.017)$	$0.488(\pm 0.015)$	$0.462(\pm 0.005)$	
	$3 \rightarrow 8$	$0.812(\pm 0.000)$	$0.810(\pm 0.003)$	$0.811(\pm 0.001)$	$0.773(\pm 0.013)$	$0.849(\pm 0.031)$	$0.852(\pm 0.029)$	$0.832(\pm 0.004)$	$0.804(\pm 0.011)$	
	$4 \rightarrow 5$	$0.618(\pm 0.536)$	$0.919(\pm 0.020)$	$0.923(\pm 0.016)$	$0.885(\pm 0.002)$	$0.672(\pm 0.504)$	$0.963(\pm 0.012)$	$0.929(\pm 0.009)$	$0.911(\pm 0.000)$	
	Avg.	$0.701(\pm 0.115)$	$0.749(\pm 0.021)$	$0.758(\pm 0.015)$	$0.720(\pm 0.006)$	$0.745(\pm 0.118)$	$0.791(\pm 0.013)$	$0.769 (\pm 0.011)$	$0.743 (\pm 0.005)$	

SQ

 $0.655(\pm 0.004)$ 

 $0.859(\pm 0.006)$ 

 $0.475(\pm 0.026)$ 

 $0.775(\pm 0.003)$ 

 $0.896(\pm 0.001)$ 

 $0.732(\pm 0.008)$ 

KuLSIF

 $0.739(\pm 0.019)$ 

 $0.947(\pm 0.024)$ 

 $0.370(\pm 0.247)$ 

 $0.856(\pm 0.019)$ 

 $0.660(\pm 0.511)$ 

 $\mathbf{0.714}(\pm \mathbf{0.164})$ 

Aggregation

LR

 $0.706(\pm 0.004)$ 

 $0.904(\pm 0.001)$ 

0.523(±0.035)

 $0.825(\pm 0.005)$ 

 $0.945(\pm 0.007)$ 

 $0.780(\pm 0.010)$ 

SQ

 $\mathbf{0.667} (\pm 0.002)$ 

 $0.891(\pm 0.005)$ 

 $0.493(\pm 0.024)$ 

 $0.797(\pm 0.002)$ 

 $0.921(\pm 0.001)$ 

 $0.754(\pm 0.007)$ 

Exp

 $0.757(\pm 0.020)$ 

 $0.924(\pm 0.015)$ 

 $0.542(\pm 0.003)$ 

 $0.860(\pm 0.023)$ 

 $0.989(\pm 0.021)$ 

 $0.814(\pm 0.017)$ 

Table 36: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on HHAR computed with domain adaptation method Deep Coral.

**Cross-Validation for Binary Classifier** 

ĹR

 $0.693(\pm 0.010)$ 

 $0.896(\pm 0.008)$ 

 $0.513(\pm 0.040)$ 

 $0.813(\pm 0.011)$ 

 $0.934(\pm 0.013)$ 

 $0.770(\pm 0.016)$ 

Exp

 $0.713(\pm 0.012)$ 

 $0.885(\pm 0.018)$ 

 $0.503(\pm 0.027)$ 

 $0.813(\pm 0.009)$ 

 $0.937(\pm 0.011)$ 

 $0.770(\pm 0.015)$ 

1394

Scenario

0 
ightarrow 6

 $1 \rightarrow 6$ 

2 
ightarrow 7

 $\mathbf{3} \to \mathbf{8}$ 

4 
ightarrow 5

Avg.

KuLSIF

 $0.693(\pm 0.012)$ 

 $0.907(\pm 0.006)$ 

 $0.320(\pm 0.277)$ 

 $0.811(\pm 0.011)$ 

 $0.625(\pm 0.541)$ 

 $0.671(\pm 0.170)$ 

1400 Table 37: Mean and standard deviation (after  $\pm$ ) of target classification accuracy on HHAR com-1401 puted with domain adaptation method CMD. 1402

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