SCREENER: LEARNING CONDITIONAL DISTRIBUTION OF DENSE SELF-SUPERVISED REPRESENTATIONS FOR UNSUPERVISED PATHOLOGY SEGMENTATION IN 3D MEDICAL IMAGES

Anonymous authors

008

009

010 011 012

013

015

016

017

018

019

021

022

023

024

025

026

027

028

029

031

032

033

Paper under double-blind review

ABSTRACT

Accurate and automated anomaly segmentation is critical for assisting clinicians in detecting and diagnosing pathological conditions, particularly in large-scale medical imaging datasets where manual annotation is not only time- and resourceintensive but also prone to inconsistency. To address these challenges, we propose SCREENER, a fully self-supervised framework for visual anomaly segmentation, leveraging self-supervised representation learning to eliminate the need for manual labels. Additionally, we model the conditional distribution of local image patterns given their global context, enabling the identification of anomalies as patterns with low conditional probabilities and assigning them high anomaly scores. SCREENER comprises three components: a descriptor model that encodes local image patterns into self-supervised representations invariant to local-contentpreserving augmentations; a condition model that captures global contextual information through invariance to image masking; and a density model that estimates the conditional density of descriptors given their global contexts to compute anomaly scores.

We validate SCREENER by training a fully self-supervised model on over 30,000 3D CT images and evaluating its performance on four large-scale test datasets comprising 1,820 3D CT scans across four chest and abdominal pathologies. Our framework consistently outperforms existing unsupervised anomaly segmentation methods. Code and pre-trained models will be made publicly available.



Figure 1: Examples of 2D slices of 3D medical CT images (the first row), the ground truth masks of
 their pathological regions (the second row) and the anomaly maps predicted by fully self-supervised
 SCREENER for pathology segmentation (the third row). Note that, the second image from the left
 contains pneumothorax, missed by ground truth annotation mask, but detected by SCREENER.

054 1 INTRODUCTION

055

098

099

102

103

The accurate and automated segmentation of pathologies in medical computed tomography (CT) images is crucial for assisting clinicians in diagnosing and treating various conditions. However, developing supervised models for pathology segmentation faces significant challenges: labeled datasets are scarce, annotations often cover only a limited range of findings, and manual labelling is not only resource-intensive but also inconsistent. For example, in Figure 1, pneumothorax is present in the second column (black region framed by red box) but is not included in the ground truth mask. Hence, supervised methods for pathology segmentation are often constrained in scope and applicability.

In contrast, large-scale datasets of unlabelled CT images are readily available through public repositories (Team, 2011; Ji et al., 2022; Qu et al., 2024). These datasets remain largely underutilized due to the lack of annotations, despite their potential to enable fully unsupervised learning approaches. Leveraging this abundance of unlabelled data, we aim to develop a model capable of distinguishing pathological regions from normal ones without requiring labeled training data. Our core assumption is that pathological patterns are significantly rarer than healthy patterns in random CT images. This motivates framing pathology segmentation as an unsupervised visual anomaly segmentation (UVAS) problem, where anomalies correspond to pathological regions.

While existing UVAS methods have been explored extensively for natural images, their adaptation to medical imaging remains challenging. A major hurdle is that most CT datasets contain unannotated pathological regions, and there is no automatic way to filter these out to ensure a training set composed entirely of normal (healthy, non-pathological) images — a common requirement for synthetic-based (Zavrtanik et al., 2021; Marimont & Tarroni, 2023) and reconstruction-based (Baur et al., 2021; Schlegl et al., 2019) UVAS methods.

Density-based approaches (Gudovskiy et al., 2022; Zhou et al., 2024), which assume anomalies are rare rather than entirely absent, are better suited for this setting, as they can handle training datasets with unannotated pathological regions. These methods model normal patterns probabilistically and assign higher anomaly scores to deviations. However, they rely on encoders pre-trained on ImageNet (Deng et al., 2009), optimized for natural images and not for the unique structures and textures in medical CT images. This domain shift leads to suboptimal feature representations failing to capture subtle pathological variations, reducing their effectiveness in medical settings.

084 To address these challenges, we propose SCREENER, a framework that enhances density-based 085 UVAS through domain-specific self-supervised learning and learned contextual conditioning. To avoid domain shift issues and labelling requirement, we pre-train self-supervised encoders (O Pinheiro et al., 2020; Wang et al., 2021; Bardes et al., 2022; Goncharov et al., 2023) to produce 087 dense CT-specific feature maps. We further introduce a second self-supervised encoder that gen-880 erates masking-invariant representations, capturing global context without being influenced by local 089 anomalies. Finally, we train a conditional density model to predict the feature maps of one encoder 090 based on the outputs of the other. Anomaly scores are assigned to image regions with high prediction 091 errors, enabling effective segmentation of pathological regions. 092

We demonstrate the effectiveness of SCREENER by training it on over 30,000 3D CT volumes spanning chest and abdominal regions and evaluating its performance on four large-scale test datasets comprising 1,820 scans with diverse pathologies. As shown in Figure 1, our model successfully segments pathological regions across different organs and conditions. We summarize the key contributions of this work:

- Self-Supervised Representations for UVAS: We demonstrate that dense self-supervised representations outperform supervised feature extractors in visual anomaly segmentation, enabling a fully self-supervised framework applicable in domains with limited labeled data.
- Learned Conditioning Variables: We introduce self-supervised condition variables for density-based models, simplifying the estimation of conditional distributions and achieving remarkable segmentation performance using a simple Gaussian density model.
- First Large-Scale Study of UVAS in 3D CT Images: This work presents the first large-scale evaluation of UVAS methods for 3D CT images, showing state-of-the-art performance on unsupervised semantic segmentation of pathologies in diverse anatomical regions, including lung cancer, pneumonia, liver and kidney tumors.

108 2 BACKGROUND & NOTATION

Density-based UVAS methods assign high anomaly scores to image regions with rare patterns using two models, which we call a *descriptor model* and a *density model*. The descriptor model encodes image patterns into vector representations, while the density model learns their distribution and assigns anomaly scores based on the learned density.

In existing methods (Gudovskiy et al., 2022; Zhou et al., 2024), the descriptor model $f_{\theta^{\text{desc}}}$ is a fully-convolutional neural network pre-trained on ImageNet. For a 3D image $\mathbf{x} \in \mathbb{R}^{H \times W \times S}$, it produces feature maps $\mathbf{y} \in \mathbb{R}^{h \times w \times s \times d^{\text{desc}}}$, where each position $p \in P$ corresponds to a descriptor $\mathbf{y}[p] \in \mathbb{R}^{d^{\text{desc}}}$. Here, position set $P = \{p \mid p \in [1, ..., h] \times [1, ..., w] \times [1, ..., s]\}$.

The density model $q_{\theta^{dens}}(y)$ estimates the marginal density $q_Y(y)$ of descriptors. For an abnormal pattern at position p, the descriptor $\mathbf{y}[p]$ is expected to lie in a low-density region, yielding a low $q_{\theta^{dens}}(\mathbf{y}[p])$. Conversely, normal patterns produce high densities. During inference, the negative logdensity values, $-\log q_{\theta^{dens}}(\mathbf{y}[p])$ are used as anomaly segmentation scores. Density models we use in SCREENER are simple Gaussian model and more expressive normalizing flow (see Appendix E).

This framework can be extended using a conditioning mechanism. For each position p, an auxiliary variable $\mathbf{c}[p]$, referred to as a *condition*, is introduced. Let C denote the condition at a random position in a random image. Instead of modelling the complex marginal density $q_Y(y)$, the conditional density $q_{Y|C}(y|c)$ is learned for each condition c. During inference, the negative log-conditional densities, $-\log q_{\theta^{\text{dens}}}(\mathbf{y}[p] | \mathbf{c}[p])$, are used as anomaly scores. State-of-the-art methods (Gudovskiy et al., 2022; Zhou et al., 2024) adopt this conditional framework and use sinusoidal positional encodings as conditions. See detailed descriptions for positional condition alternatives in Appendix D.

131 Self-supervised learning leverages unlabelled data to learn representations invariant to transformations through auxiliary tasks. SSL objectives align embeddings of augmented views $x^{(1)}$, $x^{(2)}$ of the 132 133 same image x while avoiding trivial solutions (mapping all images to the same vector). In vision domain, augmentations typically include color jitter and random crops. Representations are derived by 134 feeding inputs x to an encoder f_{θ} (a neural network), yielding $z = f_{\theta}(x)$. We employ adaptations of 135 SimCLR (Chen et al., 2020) and VICReg (Bardes et al., 2021) to dense feature learning (O Pinheiro 136 et al., 2020; Wang et al., 2021; Bardes et al., 2022; Goncharov et al., 2023) in our approach. For 137 detailed description of these methods, please refer to Appendix C. 138

139

3 Method

140 141

Here we present our method for unsupervised semantic segmentation of pathological regions in
3D medical CT images, illustrated in Figure 2. Our method introduces two key innovations to the
density-based UVAS framework: *self-supervised descriptor model* (Section 3.1), and *self-supervised condition model* (Section 3.2). Section 3.3 describes the training pipeline for density modelling.

146 147

3.1 Descriptor model

The descriptor model $f_{\theta^{\text{desc}}}$ is critical to our method. It must produce descriptors $\mathbf{y}[p]$ that distinguish between pathological and normal positions p, as this differentiation directly determines the anomaly scores in the density-based UVAS framework. Simultaneously, descriptors should minimize irrelevant information; for instance, if they capture noise from CT images, the density model may assign high anomaly scores to healthy regions with extreme noise, leading to false positives.

To pre-train dense descriptors, we use dense joint embedding SSL methods (Section 2 and Appendix C), which allow explicit control over the information content of the representations. Specifically, we penalize descriptors for failing to distinguish between different positions within or across images, ensuring they capture spatially discriminative features. Simultaneously, we enforce invariance to low-level perturbations, such as cropping and color jitter, to eliminate irrelevant information.

The descriptor model training pipeline is illustrated in the upper part of Figure 2. From a random image x, we extract two overlapping 3D crops of random size, resize them to $H \times W \times S$, and apply random augmentations, such as color jitter. The augmented crops, denoted as $\mathbf{x}^{(1)}$ and $\mathbf{x}^{(2)}$, are fed into the descriptor model, producing feature maps $\mathbf{y}^{(1)}$ and $\mathbf{y}^{(2)}$.



Figure 2: Illustration of SCREENER. First, we train a self-supervised descriptor model to produce informative feature maps invariant to image crops and color jitter. Second, we train a self-supervised condition model similarly but also enforce invariance to random block masking, ensuring its feature maps are insensitive to anomalies and reflect only contextually inferable information. Finally, the density model learns the conditional distribution $p_{Y|C}(y \mid c)$ of feature vectors Y = y[p] and C = c[p] from the descriptor and condition models at a given position p. Anomaly score maps are obtained by applying the density model pixel-wise, efficiently implemented by $1 \times 1 \times 1$ convolutions.

207 208 209

201

202

203

204

205

206

From the overlapping region of the two crops, we randomly select *n* positions. For each position *p*, we compute its coordinates $p^{(1)}$ and $p^{(2)}$ relative to the augmented crops and extract descriptors $y^{(1)} = \mathbf{y}^{(1)}[p^{(1)}]$ and $y^{(2)} = \mathbf{y}^{(2)}[p^{(2)}]$. These descriptors form a *positive pair*, as they correspond to the same position in the original image but are predicted from different augmentations.

Repeating this process for m seed images yields a batch of $N = n \cdot m$ positive pairs, denoted as $\{(y_i^{(1)}, y_i^{(2)})\}_{i=1}^N$. This strategy for sampling dense positive pairs follows the approach in (Gon-

charov et al., 2023). Using this batch, we optimize the descriptor model with SSL objectives. In this work, we employ two prominent objectives: InfoNCE (Chen et al., 2020) and VICReg (Bardes et al., 2021), detailed in Appendix C.

219 220

222

221 3.2 CONDITION MODEL

Our self-supervised condition model is inspired by a thought experiment: suppose a region of a CT image is masked, and we attempt to infer its content based on the visible context (as shown in the upper masked crop in Figure 2). In most cases, we would assume the masked region is healthy unless there is explicit evidence to suggest otherwise. This assumption reflects a model of the conditional distribution over possible inpaintings given the context. If the actual content significantly deviates from this expectation –indicating low conditional probability– it is classified as an anomaly.

Building on this intuition, we propose that the condition c[p] in the conditional density-based UVAS framework should capture the *global* context of the image position *p*. *Global* implies that c[p] must be inferable from various masked views of the image. At the same time, conditions may vary across different regions of the image to encode position-specific information, such as anatomical location or tissue type.

To achieve these properties, we learn conditions c[p] through a self-supervised condition model $g_{\theta^{\text{cond}}}$, which has a fully-convolutional architecture similar to the descriptor model. The model generates feature maps $c \in \mathbb{R}^{h \times w \times s \times d^{\text{desc}}}$ that are invariant to image masking, providing a condition for each position in the input image. The training process mirrors that of the VICReg descriptor model (Section 3.1), with the addition of masking as part of the augmentations. An illustration of this approach is shown in the middle part of Figure 2.

The learned conditions c[p] are designed to ignore the presence of pathologies, as such information cannot be consistently inferred from masked views. Instead, the condition model likely encodes patient-level attributes (e.g., age, gender) and position-specific attributes (e.g., anatomical region, tissue type) that are predictable from masked contexts. Conditioning on these variables simplifies density estimation, as conditional distributions are often less complex than marginal distributions.

Moreover, conditioning can improve fairness: for instance, if certain anatomical regions or demographic groups are underrepresented in the training data, an unconditional density model might treat
these as anomalies. In contrast, a model conditioned on gender or anatomical region would handle
such cases more appropriately by treating them within their specific context.

249 250 251

3.3 DENSITY MODELS

To train a conditional density model, $q_{\theta^{\text{dense}}}(y \mid c)$, we sample a batch of m random crops, $\{\mathbf{x}_i\}_{i=1}^m$, each of size $H \times W \times S$, from different CT images. Each crop is passed through the pre-trained descriptor and condition models to produce descriptor maps, $\{\mathbf{y}_i\}_{i=1}^m$, and condition maps, $\{\mathbf{c}_i\}_{i=1}^m$, both of size $h \times w \times s$. We then optimize the conditional negative log-likelihood loss:

257 258

$$\min_{\theta_{\text{dense}}} \quad \frac{1}{m \cdot |P|} \sum_{i=1}^{m} \sum_{p \in P} -\log q_{\theta^{\text{dense}}}(\mathbf{y}_i[p] \mid \mathbf{c}_i[p])$$

260 261

259

262

At inference, an input CT image is divided into M overlapping patches, $\{\mathbf{x}_i\}_{i=1}^M$, each of size $H \times W \times S$. For each patch, we apply the descriptor, condition, and conditional density models to compute the anomaly map, $\{-\log q_{\theta^{dense}}(\mathbf{y}_i[p] \mid \mathbf{c}_i[p])\}_{p \in P}$. These patch-wise anomaly maps are upsampled to $H \times W \times S$ and aggregated into a single anomaly map for the entire CT image by averaging predictions in overlapping regions.

We explore two parameterizations for the marginal and conditional density models: Gaussian distributions as a straightforward baseline and normalizing flows as an expressive generative model enabling tractable density estimation. For further details, please refer to Appendix E.

Dataset	# 3D images	Annotated pathology	# 3D images w/ non-zero pathology mask
NLST (Team, 2011)	25,652	_	_
AMOS (Ji et al., 2022)	2,123	_	_
AbdomenAtlas (Qu et al., 2024)	4,607	-	-
LIDC (Armato III et al., 2011)	1017	lung cancer	603
MIDRC (Tsai et al., 2020)	115	pneumonia	115
KiTS (Heller et al., 2020)	298	kidney tumors	298
LiTS (Bilic et al., 2023)	117	liver tumors	107

Table 1: Summary information on the datasets that we use for training and testing of all models.

4 EXPERIMENTS

4.1 DATASETS

270

285 286

287

298

299

We train all models on three CT datasets: NLST (Team, 2011), AMOS (Ji et al., 2022) and AbdomenAtlas (Qu et al., 2024). Note that we do not use any image annotations during training. Some of
the datasets employed additional criteria for patients to be included in the study, i.e. age, smoking
history, etc. Note that such large scale training datasets include diverse set of patients, implying
presence of various pathologies.

We test all models on four datasets: LIDC (Armato III et al., 2011), MIDRC-RICORD-1a (Tsai et al., 2020), KiTS (Heller et al., 2020) and LiTS (Bilic et al., 2023). Annotations of these datasets include segmentation masks of certain pathologies. Any other pathologies that can be present in these datasets are not labeled. We summarize dataset statistics and pathology information in Table 1.

4.2 EVALUATION METRICS

300 We use standard quality metrics for assessment of visual anomaly segmentation models which are 301 employed in MVTecAD benchmark (Bergmann et al., 2021): pixel-level AUROC and AUPRO cal-302 culated up to 0.3 FPR. We also compute area under the whole pixel-level ROC-curve. Despite, 303 our model can be viewed as semantic segmentation model, we do not report standard segmentation 304 metrics, e.g. Dice score, due to the following reasons. As we mention in Section 4.1, available 305 testing CT datasets contain annotations of only specific types of tumors, while other pathologies 306 may be present in the images but not included in the ground truth masks. It makes impossible to 307 fairly estimate metrics like Dice score or Hausdorff distance, which count our model's true positive 308 predictions of the unannotated pathologies (see second image from the left in the Figure 1 for example) as false positive errors and strictly penalize for them. However, the used pixel-level metrics are 309 not sensitive to this issue, since they are based on sensitivity and specificity. We estimate sensitivity 310 on pixels belonging to the annotated pathologies. To estimate specificity we use random pixels that 311 do not belong to the annotated tumors which are mostly normal, thus yielding a practical estimate. 312

Table 2: Quantitative comparison of our best model and the existing unsupervised visual anomaly segmentation methods on pathology segmentation in 3D medical CT images.

217	0		I	0,	0		-		-	0				
218	Model		AURO	C		А	UROC up t	o FPR0.	3	AUPRO up to FPR0.3				
19		LIDC	MIDRC	KiTS	LiTS	LIDC	MIDRC	KiTS	LiTS	LIDC	MIDRC	KiTS	LiTS	
20	Autoencoder	0.71	0.65	0.66	0.68	0.31	0.21	0.24	0.25	0.59	0.24	0.26	0.37	
20	f-AnoGAN	0.82	0.66	0.67	0.67	0.52	0.21	0.24	0.22	0.46	0.18	0.24	0.22	
21	DRAEM	0.63	0.72	0.82	0.83	0.21	0.31	0.50	0.51	0.17	0.20	0.50	0.57	
22	MOOD-Top1	0.79	0.79	0.77	0.80	0.43	0.43	0.40	0.46	0.32	0.29	0.40	0.32	
	MSFlow	0.70	0.66	0.64	0.64	0.26	0.20	0.18	0.17	0.21	0.14	0.19	0.17	
23	Screener (ours)	0.96	0.89	0.90	0.94	0.89	0.68	0.69	0.80	0.66	0.46	0.68	0.66	

325 326

335 336

337

338 339 340

341

342



Figure 3: Qualitative comparison of baseline UVAS methods and SCREENER anomaly maps on chest and abdomen regions. First column contains CT slices, columns 2 to 6 are baseline methods, column 7 is SCREENER. Last column depicts ground trught annotation mask.

Table 3: Ablation study of the effect of conditional model for the fixed descriptor model (VICReg) and different conditional density models (gaussian and normalizing flow). None in Condtion model column means that results are given for a marginal density model.

Descriptor model	Condition model	Density model	AUROC				AUROC up to FPR0.3				AUPRO up to FPR0.3			
-			LIDC	MIDRC	KiTS	LiTS	LIDC	MIDRC	KiTS	LiTS	LIDC	MIDRC	KiTS	LiTS
${\rm VICReg}, d^{\rm desc}=32$	None Sin and Pos	Gaussian	0.81	0.81	0.61	0.71	0.41	0.47	0.12	0.22	0.46	0.62	0.13	0.28
VICReg, $d^{\text{desc}} = 32$	APE	Gaussian	0.82	0.80	0.74	0.86	0.43	0.42	0.26	0.54	0.40	0.30	0.27	0.52
VICReg, $d^{\text{desc}} = 32$	Masking-equiv.	Gaussian	0.96	0.84	0.87	0.90	0.90	0.58	0.58	0.71	0.64	0.41	0.57	0.48
VICReg, $d^{\text{desc}} = 32$	None	Norm. flow	0.96	0.89	0.88	0.93	0.89	0.68	0.62	0.78	0.67	0.46	0.62	0.65
VICReg, $d^{\text{desc}} = 32$ VICReg $d^{\text{desc}} = 32$	Sin-cos pos.	Norm. flow	0.96	0.89	0.90	$0.94 \\ 0.94$	0.89	0.68	0.69 0.67	0.80	0.66	0.46	0.68	0.66
VICReg, $d^{\text{desc}} = 32$	Masking-equiv.	Norm. flow	0.96	0.87	0.90	0.93	0.88	0.64	0.68	0.80	0.65	0.40	0.67	0.63

350 351 352

353

354

4.3 MAIN RESULTS

355 We compare our best model (VICreg descriptor model, sin-cos positional encodings condition model 356 and conditional normalizing flow density model) with baselines that represent different approaches 357 to visual anomaly segmentation. Specifically, we implement 3D versions of autoencoder (Baur 358 et al., 2021), f-anoGAN (Schlegl et al., 2019) (reconstruction-based methods), DRAEM (Zavrtanik et al., 2021), MOOD-Top1 (Marimont & Tarroni, 2023) (methods based on synthetic anomalies) and 359 MSFlow (density-based method on top of ImageNet features). Quantitative comparison is presented 360 in table 2. Qualitative comparison is shown in Figure 3. 361

362 The analysis of the poor performance of the reconstruction-based methods is given in Appendix B. Synthetic-based models yield many false negatives because during training they were penalized to predict zero scores in the unlabeled real pathological regions which may appear in training images. 364 Meanwhile, MSFlow heavily relies on an ImageNet-pre-trained encoder which produces irrelevant 365 features of 3D medical CT images. Our density-based model with domain-specific self-supervised 366 features outperforms baselines by a large margin. 367

368 369

370

4.4 CONDITION AND DENSITY MODELS' ABLATION

Table 3 demonstrates ablation study of our proposed condition model. We compare our condition 371 model with two baselines: vanila sin-cos positional encodings and anatomical positional embed-372 dings (Goncharov et al., 2024), described in Appendix D. We evaluate condition models in combi-373 nation with different density models, described in Section 3.3. We use the VICReg descriptor with 374 $d^{\text{desc}} = 32$ as it shows slightly better results than contrastive objective as reported in Section 4.5. 375

All conditioning strategies yield results similar to the unconditional model when using expressive 376 normalizing flow density model. However, in experiments with simple gaussian density models, 377 we see that the results significantly improve as the condition model becomes more informative.

Table 4: Ablation study of the effect of descriptor model. In these experiments we do not use condi-379 tioning and use normalizing flow as a marginal density model. We include MSFlow to demonstrate 380 that descriptor model pre-trained on ImageNet is inappropriate for 3D medical CT images. 381

Descriptor m	odel	Condition model	Density model	AUROC			AUROC up to FPR0.3				AUPRO up to FPR0.3				
				LIDC	MIDRC	KiTS	LiTS	LIDC	MIDRC	KiTS	LiTS	LIDC	MIDRC	KiTS	LiTS
ImageNe	t	Sin-cos pos.	MSFlow	0.70	0.66	0.64	0.64	0.26	0.20	0.18	0.17	0.21	0.14	0.19	0.17
SimCLR, d ^{desc}	= 32	None	Norm. flow	0.96	0.87	0.87	0.91	0.90	0.65	0.58	0.71	0.68	0.43	0.58	0.60
VICReg, d ^{desc}	= 32	None	Norm. flow	0.96	0.89	0.88	0.93	0.89	0.68	0.62	0.78	0.67	0.46	0.62	0.65
VICReg, d ^{desc}	= 128	None	Norm. flow	0.96	0.90	0.87	0.93	0.90	0.72	0.60	0.77	0.70	0.52	0.60	0.65

Noticeably, our proposed masking-invariant condition model allows Gaussian model to compete with complex flow-based models and achieve very strong anomaly segmentation results.

4.5 DESCRIPTOR MODELS' ABLATION

We also ablate descriptor models in Table 4. We compare contrastive and VICReg models with $d^{\text{desc}} = 32$. To ablate the effect of the descriptors' dimensionality, we also include VICReg model with $d^{\text{desc}} = 128$. To demonstrate that our domain-specific self-supervised descriptors are better than descriptors pre-trained on general-domain we compare with MSFlow (Zhou et al., 2024).

5 **RELATED WORK**

5.1 VISUAL UNSUPERVISED ANOMALY LOCALIZATION

402 In this section, we review several key approaches, each represented among the top five methods on the localization track of the MVTec AD benchmark (Bergmann et al., 2021), developed to stir 404 progress in visual unsupervised anomaly detection and localization. 405

406 **Synthetic anomalies** In unsupervised settings, real anomalies are typically absent or unlabeled 407 in training images. To simulate anomalies, researchers synthetically corrupt random regions by 408 replacing them with noise, random patterns from a special set (Yang et al., 2023), or parts of other training images (Marimont & Tarroni, 2023). A segmentation model is trained to predict binary 409 masks of corrupted regions, providing well-calibrated anomaly scores for individual pixels. While 410 straightforward to train, these models may overfit to synthetic anomalies and struggle with real ones. 411

412 **Reconstruction-based** Trained solely on normal images, reconstruction-based approaches (Baur 413 et al., 2021; Kingma & Welling, 2013; Schlegl et al., 2019), poorly reconstruct anomalous regions, 414 allowing pixel-wise or feature-wise discrepances to serve as anomaly scores. Later generative ap-415 proaches (Zavrtanik et al., 2021; Zhang et al., 2023; Wang et al.) integrate synthetic anomalies. The 416 limitation stemming from anomaly-free train set assumption still persists—if anomalous images are 417 present, the model may learn to reconstruct anomalies as well as normal regions, undermining the 418 ability to detect anomalies through differences between x and \hat{x} .

419

420 Features pre-trained on ImageNet + density estimation Density-based methods for anomaly 421 detection model the distribution of the training data. Density estimation can be done in a non-422 parametric way by the collection of a memory bank of objects (Roth et al., 2022; Bae et al., 2023). As modeling of the distribution of raw pixel values is infeasible, these methods usually model the 423 distribution of their deep features. 424

425 Unsupervised anomaly detection has seen the rise of flow-based methods (Serrà et al., 2019; Yu 426 et al., 2021), which leverage normalizing flows to assign low likelihoods to anomalies. However, 427 these methods struggle with high-dimensional raw RGB images, often assigning higher likelihoods 428 to anomalies than normal data (Kirichenko et al., 2020). To address this, flow-based methods have 429 been adapted to operate on high-dimensional features extracted from images. Multiscale feature processing, as seen in DifferNet (Rudolph et al., 2021) and CFlow-AD (Gudovskiy et al., 2022), 430 enhances defect detection by handling variations in defect size. However, CFlow-AD's independent 431 estimation of each feature vector lacks contextual awareness, resulting in fragmented and inaccurate

382

389

390 391

392 393

394

395

396

397 398

399 400

401

localization. MSFlow (Zhou et al., 2024) addresses this limitation by concurrently estimating features at all positions, incorporating contextual information through 3x3 convolutions and employing a fusion flow block for information exchange across scales.

Our method is related to FastFlow (Yu et al., 2021), CFlow (Gudovskiy et al., 2022) and MS-Flow (Zhou et al., 2024) methods for anomaly segmentation. Besides some technical differences (e.g. working with 2D natural images), there are several substantial differences: 1) these methods are based on a supervised encoder, pre-trained on ImageNet; 2) we show that density-based anomaly segmentation in medical images can be improved using data-driven condition variables.

From this family, we selected MSFlow as a representative baseline, because it is simpler than PNI, and yields similar top-5 results on the MVTec AD.

443 444

5.2 MEDICAL UNSUPERVISED ANOMALY LOCALIZATION

While there's no standard benchmark for pathology localization on CT images, MOOD (Zimmerer et al., 2021) offers a relevant benchmark with generated anomalies. Unfortunately, this benchmark is currently closed for submissions, preventing us from evaluating our method. We include the top-performing method from MOOD (Marimont & Tarroni, 2023) in our comparison, that relies on synthetic anomalies.

Other recognized methods for anomaly localization in medical images are reconstruction-based: variants of AE/VAE (Baur et al., 2021; Shvetsova et al., 2021), f-AnoGAN Schlegl et al. (2019), and diffusion-based (Pinaya et al., 2022). These approaches highly rely on the fact that the the training set consists of normal images only. However, it is challenging and costly to collect a large dataset of CT images of normal patients. While these methods work acceptable in the domain of 2D medical images and MRI, the capabilities of the methods have not been fully explored in a more complex CT data domain. We have adapted these methods to 3D.

457 458

6 CONCLUSION

459 460

This work explores fully self-supervised approach to anomaly detection and localization in medical 3D images. Previously, methods relied on supervised approaches and anomaly-free training datasets assumption, which hardly holds in typical medical scenarios. We propose SCREENER as a three component model, comprised of (i) self-supervised representation learning descriptor for image features, (ii) density-based anomaly detection model that learns distribution of the features, and (iii) conditioning model containing auxiliary information which boosts simpler density models.

Domain-specific and self-supervised SCREENER is no longer inhibited by limitations of the earlier
 methods and outperforms them by a large margin, which can be seen from empirical results obtained
 on the large-scale collection of computed tomography datasets. As our framework is modular, we
 learned and tested several model choices for each of the component, resulting in a comprehensive
 ablation study.

- 472 **Limitations** We note that this work is largely a proof of concept for SSL in 3D medical imaging 473 as there are still limitations to the proposed approach. Density based anomaly detection poses a 474 limitation in that rare patterns can be flagged as pathological. Since rareness is highly predictive of 475 anomaly, applying to pathology segmentation SCREENER may yield false positive errors on healthy 476 but rare patterns. Another limitation concerns representativeness of the training sample. Our training 477 dataset contains chest and abdominal CTs with much more chest samples. This causes more false 478 positive errors in abdominal region. To work in other anatomical regions, our model needs to be 479 trained on the corresponding images.
- 480

Future work While the performance gains compared to baselines are already significant, we note
 that further improvements might be achieved from increasing descriptors and conditions dimension ality and experiments with multi-scale representations (e.g. by building feature pyramids). Another
 possible avenue for future work is to study scaling laws, i.e. self-supervised models typically scale
 well with increasing pretraining dataset sizes. Distillation of SCREENER into UNet at a pre-training
 stage is also possible and might prove effective for pathology segmentation tasks.

486 REFERENCES 487

494

499

506

- Samuel G Armato III, Geoffrey McLennan, Luc Bidaut, Michael F McNitt-Gray, Charles R Meyer, 488 Anthony P Reeves, Binsheng Zhao, Denise R Aberle, Claudia I Henschke, Eric A Hoffman, 489 et al. The lung image database consortium (lidc) and image database resource initiative (idri): a 490 completed reference database of lung nodules on ct scans. *Medical physics*, 38(2):915–931, 2011. 491
- 492 Jaehyeok Bae, Jae-Han Lee, and Seyun Kim. Pni : Industrial anomaly detection using position and 493 neighborhood information, 2023.
- Adrien Bardes, Jean Ponce, and Yann LeCun. Vicreg: Variance-invariance-covariance regularization 495 for self-supervised learning. arXiv preprint arXiv:2105.04906, 2021. 496
- 497 Adrien Bardes, Jean Ponce, and Yann LeCun. Vicregl: Self-supervised learning of local visual 498 features. Advances in Neural Information Processing Systems, 35:8799–8810, 2022.
- Christoph Baur, Stefan Denner, Benedikt Wiestler, Nassir Navab, and Shadi Albarqouni. Autoen-500 coders for unsupervised anomaly segmentation in brain mr images: a comparative study. Medical 501 Image Analysis, 69:101952, 2021. 502
- Paul Bergmann, Kilian Batzner, Michael Fauser, David Sattlegger, and Carsten Steger. The mvtec 504 anomaly detection dataset: a comprehensive real-world dataset for unsupervised anomaly detec-505 tion. International Journal of Computer Vision, 129(4):1038-1059, 2021.
- Patrick Bilic, Patrick Christ, Hongwei Bran Li, Eugene Vorontsov, Avi Ben-Cohen, Georgios Kaissis, Adi Szeskin, Colin Jacobs, Gabriel Efrain Humpire Mamani, Gabriel Chartrand, et al. 508 The liver tumor segmentation benchmark (lits). Medical Image Analysis, 84:102680, 2023. 509
- 510 Ting Chen, Simon Kornblith, Mohammad Norouzi, and Geoffrey Hinton. A simple framework for 511 contrastive learning of visual representations. In International conference on machine learning, 512 pp. 1597-1607. PMLR, 2020.
- 513 Jia Deng, Wei Dong, Richard Socher, Li-Jia Li, Kai Li, and Li Fei-Fei. Imagenet: A large-scale hi-514 erarchical image database. In 2009 IEEE conference on computer vision and pattern recognition, 515 pp. 248–255. Ieee, 2009. 516
- 517 Mikhail Goncharov, Vera Soboleva, Anvar Kurmukov, Maxim Pisov, and Mikhail Belyaev. vox2vec: A framework for self-supervised contrastive learning of voxel-level representations in medical 518 images. In International Conference on Medical Image Computing and Computer-Assisted Inter-519 vention, pp. 605-614. Springer, 2023. 520
- 521 Mikhail Goncharov, Valentin Samokhin, Eugenia Soboleva, Roman Sokolov, Boris Shirokikh, 522 Mikhail Belyaev, Anvar Kurmukov, and Ivan Oseledets. Anatomical positional embeddings. 523 arXiv preprint arXiv:2409.10291, 2024. 524
- Denis Gudovskiy, Shun Ishizaka, and Kazuki Kozuka. Cflow-ad: Real-time unsupervised anomaly 525 detection with localization via conditional normalizing flows. In Proceedings of the IEEE/CVF 526 winter conference on applications of computer vision, pp. 98–107, 2022. 527
- 528 Nicholas Heller, Niranjan Sathianathen, Arveen Kalapara, Edward Walczak, Keenan Moore, 529 Heather Kaluzniak, Joel Rosenberg, Paul Blake, Zachary Rengel, Makinna Oestreich, Joshua 530 Dean, Michael Tradewell, Aneri Shah, Resha Tejpaul, Zachary Edgerton, Matthew Peterson, 531 Shaneabbas Raza, Subodh Regmi, Nikolaos Papanikolopoulos, and Christopher Weight. The kits19 challenge data: 300 kidney tumor cases with clinical context, ct semantic segmentations, 532 and surgical outcomes, 2020. URL https://arxiv.org/abs/1904.00445.
- 534 Yuanfeng Ji, Haotian Bai, Chongjian Ge, Jie Yang, Ye Zhu, Ruimao Zhang, Zhen Li, Lingyan 535 Zhanng, Wanling Ma, Xiang Wan, et al. Amos: A large-scale abdominal multi-organ benchmark 536 for versatile medical image segmentation. Advances in neural information processing systems, 35:36722-36732, 2022. 538
- Diederik P Kingma and Max Welling. Auto-encoding variational bayes. arXiv preprint arXiv:1312.6114, 2013.

570

571

572

573

577

578

- Durk P Kingma and Prafulla Dhariwal. Glow: Generative flow with invertible 1x1 convolutions.
 Advances in neural information processing systems, 31, 2018.
- Polina Kirichenko, Pavel Izmailov, and Andrew G Wilson. Why normalizing flows fail to detect out-of-distribution data. Advances in neural information processing systems, 33:20578–20589, 2020.
- Sergio Naval Marimont and Giacomo Tarroni. Achieving state-of-the-art performance in the medical out-of-distribution (mood) challenge using plausible synthetic anomalies, 2023.
- Pedro O O Pinheiro, Amjad Almahairi, Ryan Benmalek, Florian Golemo, and Aaron C Courville.
 Unsupervised learning of dense visual representations. *Advances in Neural Information Processing Systems*, 33:4489–4500, 2020.
- Walter HL Pinaya, Mark S Graham, Robert Gray, Pedro F Da Costa, Petru-Daniel Tudosiu, Paul
 Wright, Yee H Mah, Andrew D MacKinnon, James T Teo, Rolf Jager, et al. Fast unsupervised
 brain anomaly detection and segmentation with diffusion models. In *International Conference on Medical Image Computing and Computer-Assisted Intervention*, pp. 705–714. Springer, 2022.
- Chongyu Qu, Tiezheng Zhang, Hualin Qiao, Yucheng Tang, Alan L Yuille, Zongwei Zhou, et al.
 Abdomenatlas-8k: Annotating 8,000 ct volumes for multi-organ segmentation in three weeks.
 Advances in Neural Information Processing Systems, 36, 2024.
- Karsten Roth, Latha Pemula, Joaquin Zepeda, Bernhard Schölkopf, Thomas Brox, and Peter Gehler.
 Towards total recall in industrial anomaly detection. In *Proceedings of the IEEE/CVF Conference* on Computer Vision and Pattern Recognition, pp. 14318–14328, 2022.
- Marco Rudolph, Bastian Wandt, and Bodo Rosenhahn. Same same but differnet: Semi-supervised defect detection with normalizing flows. In *Proceedings of the IEEE/CVF winter conference on applications of computer vision*, pp. 1907–1916, 2021.
- Thomas Schlegl, Philipp Seeböck, Sebastian M Waldstein, Georg Langs, and Ursula Schmidt Erfurth. f-anogan: Fast unsupervised anomaly detection with generative adversarial networks.
 Medical image analysis, 54:30–44, 2019.
 - Joan Serrà, David Álvarez, Vicenç Gómez, Olga Slizovskaia, José F Núñez, and Jordi Luque. Input complexity and out-of-distribution detection with likelihood-based generative models. *arXiv preprint arXiv:1909.11480*, 2019.
- Nina Shvetsova, Bart Bakker, Irina Fedulova, Heinrich Schulz, and Dmitry V Dylov. Anomaly de tection in medical imaging with deep perceptual autoencoders. *IEEE Access*, 9:118571–118583, 2021.
 - National Lung Screening Trial Research Team. The national lung screening trial: overview and study design. *Radiology*, 258(1):243–253, 2011.
- Emily Tsai, Scott Simpson, Matthew P. Lungren, Michelle Hershman, Leonid Roshkovan, Errol Colak, Bradley J. Erickson, George Shih, Anouk Stein, Jayashree Kalpathy-Cramer, Jody Shen, Mona A.F. Hafez, Susan John, Prabhakar Rajiah, Brian P. Pogatchnik, John Thomas Mongan, Emre Altinmakas, Erik Ranschaert, Felipe Campos Kitamura, Laurens Topff, Linda Moy, Jeffrey P. Kanne, and Carol C. Wu. Medical imaging data resource center - rsna international covid radiology database release 1a - chest ct covid+ (midrc-ricord-1a), 2020.
- Shuyuan Wang, Huiyuan Luo, Qi Li, Chengkan Lv, and Zhengtao Zhang. Pouta-produce once, utilize twice for anomaly detection.
- Xinlong Wang, Rufeng Zhang, Chunhua Shen, Tao Kong, and Lei Li. Dense contrastive learning for self-supervised visual pre-training. In *Proceedings of the IEEE/CVF conference on computer vision and pattern recognition*, pp. 3024–3033, 2021.
- 592 Minghui Yang, Peng Wu, and Hui Feng. Memseg: A semi-supervised method for image surface
 593 defect detection using differences and commonalities. *Engineering Applications of Artificial Intelligence*, 119:105835, 2023.

594 595 596	Jiawei Yu, Ye Zheng, Xiang Wang, Wei Li, Yushuang Wu, Rui Zhao, and Liwei Wu. Fast- flow: Unsupervised anomaly detection and localization via 2d normalizing flows. <i>arXiv preprint</i> <i>arXiv:2111.07677</i> , 2021.
597 598 599 600	Vitjan Zavrtanik, Matej Kristan, and Danijel Skočaj. Draem-a discriminatively trained reconstruc- tion embedding for surface anomaly detection. In <i>Proceedings of the IEEE/CVF International</i> <i>Conference on Computer Vision</i> , pp. 8330–8339, 2021.
601 602	Hui Zhang, Zheng Wang, Zuxuan Wu, and Yu-Gang Jiang. Diffusionad: Denoising diffusion for anomaly detection. <i>arXiv preprint arXiv:2303.08730</i> , 2023.
603 604 605 606	Yixuan Zhou, Xing Xu, Jingkuan Song, Fumin Shen, and Heng Tao Shen. Msflow: Multiscale flow- based framework for unsupervised anomaly detection. <i>IEEE Transactions on Neural Networks</i> <i>and Learning Systems</i> , 2024.
607 608 609	David Zimmerer, Jens Petersen, Gregor Köhler, Paul Jäger, Peter Full, Tobias Roß, Tim Adler, Annika Reinke, Lena Maier-Hein, and Klaus Maier-Hein. Medical out-of-distribution analysis challenge 2022. <i>Publisher: Zenodo</i> , 2021.
610 611 612	
613 614	
615 616	
617 618 619	
620 621	
622 623	
624 625 626	
627 628	
629 630	
632 633	
634 635	
636 637 638	
639 640	
641 642	
643 644 645	
646 647	

A ANALYSIS OF RECONSTRUCTION-BASED MODELS



Figure 4: The figure shows 2D slices of CT images (first column) alongside reconstructions and anomaly maps generated by two methods: an Autoencoder (Baur et al., 2021) (second and third columns) and f-AnoGAN (Schlegl et al., 2019) (last two columns). Autoencoder overfits for pixel reconstruction, so it generates pathologies and fails to segment them. Also Autoencoder produces blurry generations, leading to inaccurate reconstructions of fine details and high anomaly scores on these details (e.g., vessels in the lungs). f-AnoGAN, on the other hand, avoids generating patholo-gies, but the generation quality still is insufficient for precise segmentation of only pathological voxels. GANs are known to be unstable and sensitive to hyperparameters, necessitating careful tuning and experimentation to achieve optimal results.

B ANALYSIS OF RECONSTRUCTION-BASED MODELS



Figure 5: The figure shows 2D slices of CT images (first column) alongside reconstructions and anomaly maps generated by two methods: an Autoencoder (Baur et al., 2021) (second and third columns) and f-AnoGAN (Schlegl et al., 2019) (last two columns). Autoencoder overfits for pixel reconstruction, so it generates pathologies and fails to segment them. Also Autoencoder produces blurry generations, leading to inaccurate reconstructions of fine details and high anomaly scores on these details (e.g., vessels in the lungs). f-AnoGAN, on the other hand, avoids generating pathologies, but the generation quality still is insufficient for precise segmentation of only pathological voxels. GANs are known to be unstable and sensitive to hyperparameters, necessitating careful tuning and experimentation to achieve optimal results.

C SELF-SUPERVISED LEARNING

Below, we outline two representative methods: SimCLR and VICReg.

SimCLR In contrastive models, the key objective is to maximize the similarity between embeddings of positive pairs (augmented views of the same input) while minimizing their similarity with negative pairs (views from other inputs). To this end, InfoNCE loss on embeddings is minimized:

$$\min_{\theta} \sum_{i=1}^{N} \sum_{k \in \{1,2\}} -\log \frac{\exp(\langle z_i^{(1)}, z_i^{(2)} \rangle / \tau)}{\exp(\langle z_i^{(1)}, z_i^{(2)} \rangle / \tau) + \sum_{j \neq i} \sum_{l \in \{1,2\}} \exp(\langle z_i^{(k)}, z_j^{(l)} \rangle / \tau)}, \quad (1)$$

where $z_i^{(1)}$ and $z_i^{(2)}$ form a positive pair (i.e. augmentations of the same image x_i).

VICReg Non-contrastive learning avoids explicit negative pairs by structuring the embedding space directly. Specifically, VICReg objective enforces invariance among positive embeddings while constraining covariance matrix of features to be diagonal and variance to be equal to some constant:

$$\min_{\alpha} \quad \alpha \cdot \mathcal{L}^{\text{inv}} + \beta \cdot \mathcal{L}^{\text{var}} + \gamma \cdot \mathcal{L}^{\text{cov}}, \tag{2}$$

The first term $\mathcal{L}^{\text{inv}} = \frac{1}{N \cdot D} \sum_{i=1}^{N} ||z_i^{(1)} - z_i^{(2)}||^2$ penalizes embeddings to be invariant to augmentations. The second term $\mathcal{L}^{\text{var}} = \sum_{k \in \{1,2\}} \frac{1}{D} \sum_{i=1}^{D} \max\left(0, 1 - \sqrt{C_{i,i}^{(k)} + \varepsilon}\right)$ enforces individual embeddings' dimensions to have unit variance. The third term $\mathcal{L}^{\text{cov}} = \sum_{k \in \{1,2\}} \frac{1}{D} \sum_{i \neq j} \left(C_{i,j}^{(k)}\right)^2$

rst becauses animensions to nave and variable. The anita term $\mathcal{L} = \sum_{k \in \{1,2\}} D \sum_{i \neq j} (\mathbb{C}_{i,j})$ encourages different embedding's dimensions to be uncorrelated, increasing the total information content of the embeddings.

⁷⁵⁶ D BASELINE CONDITION MODELS

757 758

Sin-cos positional encodings The existing density-based UVAS methods Gudovskiy et al. (2022); 759 Zhou et al. (2024) for natural images use standard sin-cos positional encodings for conditioning. We 760 also employ them as an option for condition model in our framework. However, let us clarify what 761 we mean by sin-cos positional embeddings in CT images. Note that we never apply descriptor, 762 condition or density models to the whole CT images due to memory constraints. Instead, at all the training stages and at the inference stage of our framework we always apply them to image crops of 763 764 size $H \times W \times S$, as described in Sections 3.1, 3.3. When we say that we apply sin-cos positional embeddings condition model to an image crop, we mean that compute sin-cos encodings of absolute 765 positions of its pixels w.r.t. to the whole CT image. 766

767 768 Anatomical positional embeddings To implement the idea of learning the conditional distribu-769 tion of image patterns at each certain anatomical region, we need a condition model producing 770 conditions c[p] that encode which anatomical region is present in the image at every position p. 771 Supervised model for organs' semantic segmentation would be an ideal condition model for this 772 purpose. However, to our best knowledge, there is no supervised models that are able to segment 773 all organs in CT images. That is why, we decided to try the self-supervised APE Goncharov et al. 773 (2024) model which produces continuous embeddings of anatomical position of CT image pixels.

774 775

776 777

778

779 780

781 782 783

787 788 789

798

803

806 807 808

E DENSITY MODELS

Below, we describe simple Gaussian density model and more expressive learnable Normalizing Flow model.

Gaussian Gaussian marginal density model is written as

$$-\log q_{\theta^{\text{dens}}}(y) = \frac{1}{2} (y - \mu)^{\top} \Sigma^{-1} (y - \mu) + \frac{1}{2} \log \det \Sigma + \text{const},$$
(3)

where the trainable parameters θ^{dens} are mean vector μ and diagonal covariance matrix Σ .

786 Conditional gaussian density model is written as

$$-\log q_{\theta^{\text{dens}}}(y \mid c) = \frac{1}{2} (y - \mu_{\theta^{\text{dens}}}(c))^{\top} (\Sigma_{\theta^{\text{dens}}}(c))^{-1} (y - \mu_{\theta^{\text{dens}}}(c)) + \frac{1}{2} \log \det \Sigma_{\theta^{\text{dens}}}(c) + \text{const},$$
(4)

where $\mu_{\theta^{\text{dens}}}$ and $\Sigma_{\theta^{\text{dens}}}$ are MLP nets which take condition $c \in \mathbb{R}^{d^{\text{cond}}}$ as input and predict a conditional mean vector $\mu_{\theta^{\text{dens}}}(c) \in \mathbb{R}^{d^{\text{desc}}}$ and a vector of conditional variances which is used to construct the diagonal covariance matrix $\Sigma_{\theta^{\text{dens}}}(c) \in \mathbb{R}^{d^{\text{desc}} \times d^{\text{desc}}}$.

As described in Section 3.3, at both training and inference stages, we need to obtain dense negative log-density maps. Dense prediction by MLP nets $\mu_{\theta^{\text{dens}}}(c)$ and $\Sigma_{\theta^{\text{dens}}}(c)$ can be implemented using convolutional layers with kernel size $1 \times 1 \times 1$. In practice, we increase this kernel size to $3 \times 3 \times 3$, which can be equivalently formulated as conditioning on locally aggregated conditions.

Normalizing flow Normalizing flow model of descriptors' marginal distribution is written as:

$$-\log p_{\theta^{\text{dens}}}(y) = \frac{1}{2} \|f_{\theta^{\text{dens}}}(y)\|^2 - \log \left|\det \frac{\partial f_{\theta^{\text{dens}}}(y)}{\partial y}\right| + \text{const},$$
(5)

where neural net f_{θ} must be invertible and has a tractable jacobian determinant.

Conditional normalizing flow model of descriptors' conditional distribution is given by:

$$-\log p_{\theta^{\text{dens}}}(y \mid c) = \frac{1}{2} \|f_{\theta^{\text{dens}}}(y, c)\|^2 - \log \left|\det \frac{\partial f_{\theta^{\text{dens}}}(y, c)}{\partial y}\right| + \text{const}, \tag{6}$$

where neural net $f_{\theta} : \mathbb{R}^{d^{\text{desc}}} \times \mathbb{R}^{d^{\text{cond}}} \to \mathbb{R}^{d^{\text{desc}}}$ must be invertible w.r.t. the first argument, and the second term should be tractable.

We construct f_{θ} by stacking Glow layers Kingma & Dhariwal (2018): act-norms, invertible linear transforms and affine coupling layers. Note that at both training and inference stages we apply f_{θ} to descriptor maps $\mathbf{y} \in \mathbb{R}^{h \times w \times s \times d^{\text{desc}}}$ in a pixel-wise manner to obtain dense negative log-density maps. In conditional model, we apply conditioning in affine coupling layers similar to Gudovskiy et al. (2022) and also in each act-norm layer by predicting maps of rescaling parameters based on condition maps.