

MULTI-SYNAPTIC COOPERATION: A BIO-INSPIRED FRAMEWORK FOR ROBUST AND SCALABLE CONTINUAL LEARNING

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ABSTRACT

013 Continual learning aims to acquire new knowledge incrementally while retaining prior information, with catastrophic forgetting (CF) being a central challenge. 014 Existing methods can mitigate CF to some extent but are constrained by limited 015 capacity, which often requires dynamic expansion for long task sequences and 016 makes performance sensitive to task order. Inspired by the richness and plasticity of 017 synaptic connections in biological nervous systems, we propose the Multi-Synaptic 018 Cooperation Network (MSCN), a generalized framework that models cooperative 019 interactions among multiple synapses through multi-synaptic connections mod- 020 ulated by local synaptic activity. This design enhances model representational 021 capacity and enables task-adaptive plasticity by means of multi-synaptic coop- 022 eration, providing a new avenue for expanding model capacity while improving 023 robustness to task order. During learning, our MSCN dynamically activates task- 024 relevant synapses while suppressing irrelevant ones, enabling targeted retrieval and 025 minimizing interference. Extensive experiments across four benchmark datasets, 026 involving both spiking and non-spiking neural networks, demonstrate that our 027 method consistently outperforms state-of-the-art continual learning methods with 028 significantly improved robustness to task-order variation. Furthermore, our analy- 029 sis reveals an optimal trade-off between synaptic richness and learning efficiency, 030 where excessive connectivity can impair circuit performance. These findings high- 031 light the importance of the multi-synaptic cooperation mechanism for achieving 032 efficient continual learning and provide new insights into biologically inspired, 033 robust, and scalable continual learning.

1 INTRODUCTION

037 Continual learning aims to develop models capable of acquiring and retaining knowledge from a 038 sequence of tasks or data distributions, thereby mimicking the human ability to learn progressively 039 over time. This approach is also known as lifelong learning or incremental learning Thrun (1994) and 040 holds promise for building adaptive and efficient systems in dynamic environments. A core challenge 041 in continual learning is catastrophic forgetting McCloskey & Cohen (1989)—a phenomenon where 042 the model’s performance on previously acquired tasks degrades significantly when updated with new 043 data De Lange et al. (2022); Parisi et al. (2019); Masana et al. (2023).

044 Recently, various approaches have been proposed to mitigate catastrophic forgetting Bonicelli et al. 045 (2022); Tong et al. (2023); Qiao et al. (2024); Li et al. (2024a). These approaches can be broadly 046 categorized into three primary types Masana et al. (2023): *Rehearsal-based* methods Lopez-Paz & 047 Ranzato (2017); Bang et al. (2021); Van De Ven et al. (2020); Hayes et al. (2020), *Regularization- 048 based* methods Kirkpatrick et al. (2017); Wołczyk et al. (2022); Schwarz et al. (2018); Li et al. 049 (2024b), and *Architecture-based* methods Yoon et al. (2018); Zhou et al. (2022b); Li et al. (2019); 050 Wang et al. (2023); Serra et al. (2018); Hung et al. (2019b); Kang et al. (2022). Among these three 051 types, *Architecture-based* methods are particularly notable for the ability to dynamically adjust 052 the network structure to accommodate new tasks. They primarily rely on two strategies: network 053 expansion and pruning. Expansion strategies Hung et al. (2019b); Li et al. (2019); Yoon et al. (2018) 054 start with a small model and dynamically expand the network to mitigate forgetting. In contrast, 055 pruning strategies Mallya et al. (2018); Wang et al. (2022a); Kang et al. (2022) assign a sub-network

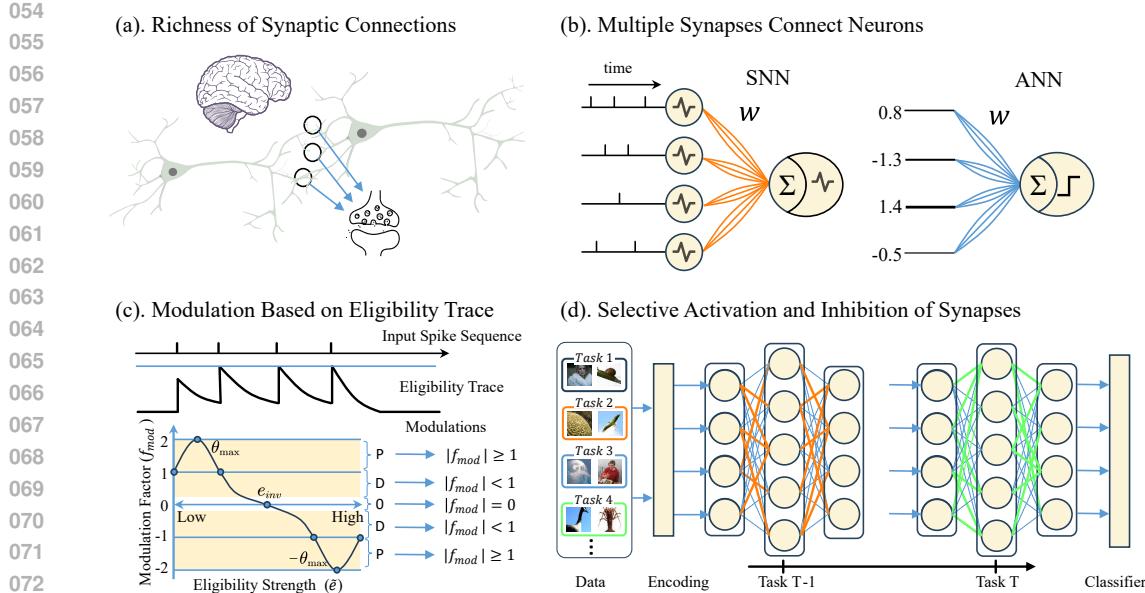


Figure 1: Overview of the MSCN framework. (a) The phenomenon of multi-synaptic connections in biological neurons. (b) Modeling of neurons with multiple synaptic connections in both SNNs and ANNs. (c) Local synaptic activity plasticity based on eligibility traces. Depending on the eligibility trace, synapses undergo potentiation (P), depression (D), or remain unchanged (O), reflecting the modulation’s strength and direction. (d) The process of selectively activating task-relevant synapses and inhibiting irrelevant ones.

to each old task. These sub-networks are pruned from a pre-allocated dense model. Further training is restricted to the unpruned parameters only. While these strategies offer several advantages, including performance and the potential for forget-free learning in some cases, they still face notable challenges: (i) Dynamic expansion requires continuous network growth to accommodate new tasks, which makes it hardware-unfriendly; (ii) Both expansion and pruning methods are often sensitive to the task order, leading to significant performance variation depending on the sequence of tasks.

Remarkably, the brain achieves continual learning without suffering from dynamic structural growth Rasch & Born (2007); Joseph & Gu (2021), highlighting the potential of biologically inspired mechanisms as significant alternatives to artificial network expansion. Among these, multi-synaptic connectivity is believed to be a key factor in supporting continual learning Shi et al. (2025); Wu & Mel (2009); Ko et al. (2011), as its diverse synaptic architecture enhances the information representation capacity of neural circuits. Meanwhile, *Three-factor* learning rules Frémaux & Gerstner (2016); Gerstner et al. (2018) have been widely studied as biologically plausible models of synaptic plasticity, in which synaptic changes are not only modulated by global neuromodulatory signals but also depend on the local synaptic activity. Inspired by this, we propose MSCN, a novel framework that enhances representational flexibility and robustness by employing the multi-synaptic cooperation mechanism, rather than increasing network depth, width, or dynamically expanding the architecture, as illustrated in Fig. 1. Our framework consists of two components: the multi-synapse connectivity structure that augments the model’s representational capacity within a fixed network architecture, and the synaptic plasticity modulation mechanism based on local synaptic activity. Such local synaptic activity is integrated via eligibility traces, which serve as modulatory signals to synaptic weight updates. During learning, task-relevant synapses are dynamically selected, while irrelevant ones are suppressed, thereby effectively minimizing interference across tasks.

Our contributions are as follows:

- We propose MSCN, the first continual learning framework that explicitly leverages the multi-synaptic cooperation mechanism, providing a biologically inspired and capacity-efficient solution. By maximally harnessing synaptic resources, MSCN unlocks the potential

108 of fixed-capacity networks and substantially boosts the scalability of continual learning
 109 systems.
 110

- 111 • We design a modulatory mechanism based on local synaptic activities that modulates
 112 synaptic plasticity through eligibility traces, enabling precise, activity-dependent modulation
 113 at the synaptic level. This modulation significantly strengthens the robustness of continual
 114 learning models to task order variations, ensuring stable performance even under highly
 115 dynamic and unpredictable training sequences.
- 116 • Extensive experiments on four benchmark datasets across both spiking and non-spiking
 117 architectures demonstrate that MSCN consistently outperforms state-of-the-art continual
 118 learning methods in terms of accuracy, forgetting mitigation, and robustness to task order,
 119 while also exhibiting competitive computational efficiency.

120 **2 RELATED WORK**

123 **Continual Learning** methods are roughly divided into three categories: *Rehearsal-based* methods
 124 store past experiences in memory to mitigate forgetting. Some works Rebuffi et al. (2017); Tiwari et al.
 125 (2022); Zhou et al. (2022c); Jeeveswaran et al. (2023) design sampling strategies to allocate a limited
 126 memory budget, while others Lin et al. (2022); Rolnick et al. (2019); Sun et al. (2023) build special
 127 subspace of old tasks as the memory. *Regularization-based* methods aim to consolidate previous
 128 knowledge by adding extra regularization terms to the loss function. Some works Li & Hoiem
 129 (2017); Kirkpatrick et al. (2017); Cha et al. (2020) constrain important weights in the parameter
 130 space Akyürek et al. (2021); Rudner et al. (2022); Kim et al. (2023), feature representations Gao
 131 et al. (2022); Jeeveswaran et al. (2023), or output logits Li & Hoiem (2017); Oh et al. (2022) to
 132 remain close to those of the old model. *Architecture-based* methods dedicate different incremental
 133 model structures towards each task to minimize forgetting Zhou et al. (2022a); Lu et al. (2024); Kang
 134 et al. (2022). Some works Serra et al. (2018); Yoon et al. (2019); Hu et al. (2023) adopt modular
 135 architectures by dynamically expanding additional components Yan et al. (2021); Zhu et al. (2022),
 136 or freeze subsets of parameters Abati et al. (2020); Liu et al. (2021) to overcome forgetting. In this
 137 work, to better investigate the capacity efficiency and robustness of our method, we implement our
 138 multi-synaptic cooperation mechanism based on the architecture-based methods without dynamically
 139 expanding the network.

140 **Neural Network Dynamics** in continual learning describe how internal representations and connec-
 141 tivity patterns evolve as new tasks are learned sequentially Márton et al. (2022). These dynamics
 142 manifest across multiple levels, including synaptic updates, activation trajectories, and parameter
 143 plasticity under task transitions Vyas et al. (2020). Recent works have begun to explicitly model
 144 neural dynamics in continual learning by introducing mechanisms such as synaptic trajectories,
 145 context-dependent modulation, and task-driven weight routing Li & Wang (2017); Li et al. (2024c);
 146 Xu et al. (2024). These studies highlight the importance of capturing temporal evolution in network
 147 parameters to support adaptive behavior over extended task sequences. Additional research explores
 148 dynamic mechanisms such as gating, masking, and sparsity-inducing priors to modulate parameter
 149 updates and isolate task-specific pathways Abati et al. (2020); Wang et al. (2022b); Yan et al. (2022).
 150 Recently, multi-synaptic (redundant) connections between neuron pairs have been shown to enhance
 151 computational capacity Zenke & Laborie (2024); Hofmann et al. (2025). Nevertheless, the coopera-
 152 tive interactions among multiple synapses and their implications for continual learning remain largely
 153 underexplored. In contrast, our method introduces multi-synaptic dynamics within each connection
 154 and the modulation based on local synapse activity, enabling representational diversity and adaptive
 155 modulation of synaptic plasticity. This novel design does not require increasing network depth/width
 156 or dynamically expanding the network; instead, it increases capacity and enhances robustness through
 157 a multi-synaptic cooperation mechanism.

158 **3 METHOD**

159 **3.1 MODELING MULTI-SYNAPTIC SPIKING NEURON**

160 Biological systems achieve continual learning without relying on architectural growth Song et al.
 161 (2024); Shi et al. (2025). A key neurobiological observation is the presence of multiple synaptic

162 contacts between the same axon–dendrite pair, providing redundancy and adaptability Trachtenberg
 163 et al. (2002); Yang et al. (2014). Since our design operates at the synaptic level, the proposed method
 164 can be applied to both ANN and SNN Maass (1997); Gütig & Sompolinsky (2006) architectures.
 165 To better capture biological principles, we first model the multi-synaptic cooperation mechanism
 166 in SNNs, which are more consistent with biological processes and offer event-driven, temporally
 167 sparse, and energy-efficient computation Gütig & Sompolinsky (2006). As a concrete instantiation,
 168 we adopt the leaky integrate-and-fire (LIF) neuron Lapique (1907), a widely used model balancing
 169 biological plausibility and computational simplicity Shiu et al. (2024); Brand & Petruccione (2024).
 170 The membrane potential $V(t)$ evolves over continuous time as follows:

$$\tau_m \frac{dV(t)}{dt} = -(V(t) - V_{\text{rest}}) + I(t) \quad (1)$$

174 where τ_m is the membrane time constant, V_{rest} is the resting potential, and $I(t)$ denotes the total
 175 synaptic input current. This formulation captures leakage and current integration but assumes a
 176 single synapse per connection, limiting diversity. To address this, we generalize the neuron model
 177 by introducing $P \geq 1$ parallel synapses for each synaptic connection. Consider a neuron with N
 178 presynaptic neurons, each forming P distinct synaptic pathways to it. Therefore, in continuous time,
 179 the membrane potential of the postsynaptic neuron is given by:

$$V(t) = \sum_{i=1}^N \sum_{p=1}^P w_{ip} \text{PSP}_{ip}(t) - \vartheta \sum_j e^{-\frac{t-t_s^j}{\tau_m}} \quad (2)$$

180 where w_{ip} denotes the synaptic weight of the p -th parallel synapse associated with the i -th presynaptic
 181 neuron, PSP_{ip} represents the postsynaptic potential of this synapse and ϑ denotes the firing threshold.
 182 To preserve synaptic heterogeneity Deng et al. (2025) and enable independent optimization, we
 183 introduce distinct decay time constants across parallel synapses. Accordingly, for the p -th synapse of
 184 presynaptic neuron i , the spike arrival times are denoted by t_{ip}^f , and PSP_{ip} is defined as:
 185

$$\text{PSP}_{ip}(t) = \sum_f K_{ip}(t - t_{ip}^f) \quad (3)$$

$$K_{ip}(t) = e^{-\frac{t}{\tau_{s_{ip}}}} \quad (4)$$

186 where $K_{ip}(t)$ denotes the kernel function of the p -th parallel synapse, and $\tau_{s_{ip}}$ represents its decay
 187 time constant, which is initialized to different values (non-trainable). This design allows multiple
 188 temporal and weighted channels to influence the synaptic plasticity, thereby enhancing the diversity of
 189 spatiotemporal representations. On this basis, modeling in the ANN architecture can be more readily
 190 formulated. Given space limitations, the corresponding implementation is presented in Appendix A.1.

201 3.2 PLASTICITY MODULATION BASED ON ELIGIBILITY TRACES

202 Building on multi-synaptic connections, we introduce a modulation mechanism of synaptic plasticity
 203 based on local synaptic activity. Specifically, we propose the eligibility trace as the basis for
 204 modulating local synaptic plasticity. We begin by formulating the modulation signal in continuous
 205 time as a cumulative sum of synaptic spike events. For a connection between two neurons, P parallel
 206 synapses share a common eligibility trace, which is defined as:

$$\frac{d\tilde{e}}{dt} = -\frac{\tilde{e}}{\tau} + \sum_f \delta(t - t^f) \quad (5)$$

207 where τ is the decay time constant, $\delta(\cdot)$ denotes the Dirac delta function. For practical implementation,
 208 we adopt a discrete-time formulation, and the dynamics of \tilde{e} are updated as follows:

$$\tilde{e}[t+1] = \tilde{e}[t] - \frac{\tilde{e}[t]}{\tau} + S[t+1] \quad (6)$$

216 where $S[t + 1] \in \{0, 1\}$ indicates whether a spike occurred at time step $t + 1$. This design captures
 217 recent spiking accumulation while allowing the eligibility trace to decay in the absence of input,
 218 enabling the eligibility trace to track local synaptic activity over time.

219 The effect of the modulation factor on synaptic plasticity is governed by a nonlinear function $f_{\text{mod}}(\tilde{e})$,
 220 which determines how strongly and in what direction the synapse should change in response to local
 221 synaptic activity signals. Following Zhang et al. (2023), we adopt a piecewise quadratic form for
 222 f_{mod} , which adjusts the strength and direction (potentiation or depression) of synaptic plasticity
 223 depending on the eligibility trace. In practice, \tilde{e} is normalized over all model synapses to $[-1, 1]$ to
 224 reflect the relative strength of local synaptic activity. The modulation function is defined as:
 225

$$226 \quad f_{\text{mod}}(\tilde{e}) = \begin{cases} 1 + (\theta_{\text{max}} - 1) \left(\frac{|\tilde{e}|}{e_1} \right)^2, & 0 \leq |\tilde{e}| \leq e_1, \\ 227 \quad \theta_{\text{max}} \left[1 - \left(\frac{|\tilde{e}| - e_1}{e_{\text{inv}} - e_1} \right)^2 \right], & e_1 \leq |\tilde{e}| \leq e_{\text{inv}}, \\ 228 \quad -f_{\text{mod}}(2e_{\text{inv}} - |\tilde{e}|), & e_{\text{inv}} \leq |\tilde{e}| \leq 2e_{\text{inv}}, \\ 229 \quad 0, & \text{otherwise} \end{cases} \quad (7)$$

230 where $e_1 = 0.5e_{\text{inv}}$ sets the low-moderate boundary, θ_{max} controls the maximum modulation
 231 strength, and e_{inv} marks the zero point of f_{mod} . (Fig. 1c). This function modulates plasticity based on
 232 local synaptic activity: potentiation occurs when $|f_{\text{mod}}| \geq 1$, depression arises when $0 < |f_{\text{mod}}| < 1$,
 233 and complete depression is observed when $f_{\text{mod}} = 0$. The final modulated synaptic weight change is
 234 computed as:
 235

$$236 \quad \Delta w = -\eta \cdot |f_{\text{mod}}(\tilde{e})| \cdot \frac{\partial \mathcal{L}}{\partial w} \quad (8)$$

237 where η is the learning rate and $\partial \mathcal{L} / \partial w$ is the gradient. The modulation function f_{mod} adjusts the
 238 size and direction of the synaptic weight update. By dynamically adjusting synaptic updates in
 239 response to recent local activity, this design mimics the biological mechanism of robust learning
 240 through activity-dependent modulation Wu et al. (2021); Wu & Maass (2025), thereby enabling the
 241 network to adapt to changing task demands and maintain stable performance.

242 3.3 GENERALIZING TO CLASSIC ARCHITECTURE-BASED METHODS

243 In this section, we integrate our method into the *Architecture-based* setting, adopting the same setup
 244 as in Kang et al. (2023); Serra et al. (2018); Wortsman et al. (2020). Consider a standard supervised
 245 continual learning setting with T tasks presented sequentially. For each task j , the model receives
 246 a dataset $\mathcal{D}_j = \{(\mathbf{x}_{i,j}, y_{i,j})\}_{i=1}^{n_j}$ consisting of n_j labeled samples. A fixed-topology deep neural
 247 network $\mathcal{F}(\cdot; \boldsymbol{\theta})$, parameterized by model parameters $\boldsymbol{\theta}$, is employed. The objective at each step is to
 248 optimize the model for the current task j :

$$249 \quad \boldsymbol{\theta}^* = \underset{\boldsymbol{\theta}}{\text{minimize}} \frac{1}{n_j} \sum_{i=1}^{n_j} \mathcal{L}(\mathcal{F}(\mathbf{x}_{i,j}; \boldsymbol{\theta}), y_{i,j}) \quad (9)$$

250 Following Gao et al. (2023); Wortsman et al. (2020), task identities are assumed to be available during
 251 both training and inference, under a multi-head setting in which each task is assigned a distinct output
 252 head. For each task j , a binary mask \mathbf{m}_j^* is learned to activate the relevant synapses. The training
 253 objective is formulated as:

$$254 \quad \boldsymbol{\theta}^*, \mathbf{m}_j^* = \underset{\boldsymbol{\theta}, \mathbf{m}_j}{\text{minimize}} \frac{1}{n_j} \sum_{i=1}^{n_j} [\mathcal{L}(\mathcal{F}(\mathbf{x}_{i,j}; \boldsymbol{\theta} \odot \mathbf{m}_j), y_{i,j}) - \mathcal{L}(\mathcal{F}(\mathbf{x}_{i,j}; \boldsymbol{\theta}), y_{i,j})] \quad (10)$$

255 where \odot denotes element-wise multiplication. A shared learnable relevance score \mathbf{r} is maintained
 256 across tasks, with each entry corresponding to a synapse Kang et al. (2023). Trained jointly with

270 the network parameters, \mathbf{r} enables the model to identify task-relevant connections. For task j ,
 271 the subnetwork $\hat{\theta}_j$ is formed by selecting the top $c\%$ of weights ranked by relevance, where c is
 272 the layerwise capacity ratio Wortsman et al. (2020). The selected weights are indicated by the
 273 binary mask \mathbf{m}_j , in which a value of 1 signifies that the corresponding weight is active during the
 274 forward pass, and 0 indicates it is deactivated. To preserve past knowledge, an accumulated mask
 275 $\mathbf{M}_{j-1} = \bigvee_{i=1}^{j-1} \mathbf{m}_i$ (with \bigvee as logical OR) is applied when learning task j . The parameters θ are
 276 updated as:

$$\theta \leftarrow \theta - \Delta\theta \odot (1 - \mathbf{M}_{j-1}) \quad (11)$$

280 where $\Delta\theta$ denotes the gradient step, and the term $(1 - \mathbf{M}_{j-1})$ ensures that only unallocated synapses
 281 remain trainable, thereby preserving the stability of parameters from previously learned tasks.

283 4 EXPERIMENTS

285 4.1 EXPERIMENTAL SETUP

287 We conduct comprehensive experiments under diverse training configurations, input domains, datasets,
 288 and network architectures, and evaluate continual learning performance using two widely adopted
 289 metrics Kang et al. (2022); Konishi et al. (2023): *Average Accuracy (ACC)* and *Backward Transfer*
 290 (*BWT*). ACC measures the model’s average accuracy over all tasks after learning task T , reflecting
 291 its overall generalization ability. BWT measures the impact of new tasks on prior ones, with higher
 292 values better and 0 indicating no forgetting. Unless otherwise stated, we set the synapse count to
 293 $P = 3$ in all main experiments, ablation studies, and computational cost analyses. Implementation
 294 and hardware details are provided in Appendix A.2.

295 Table 1: Performance comparison on four datasets, evaluating performance under both SNN and
 296 ANN frameworks. We report the results across 5 independent runs with different random seeds under
 297 the same experimental setup. Table 5 in Appendix A.2 shows the standard deviations.

299 Network	300 Method	PMNIST		10-split CIFAR-100		TinyImageNet		5-Datasets	
		301 ACC (%) ↑	302 BWT (%) ↑	303 ACC (%) ↑	304 BWT (%) ↑	305 ACC (%) ↑	306 BWT (%) ↑	307 ACC (%) ↑	308 BWT (%) ↑
301 SNN	302 <i>MTL</i>	303 96.52	304 /	305 79.83	306 /	307 79.24	308 /	309 89.93	310 /
	303 EWC ^{PNAS} Kirkpatrick et al. (2017)	304 91.45	305 -3.20	306 73.75	307 -4.89	308 60.29	309 -25.47	310 57.06	311 -44.55
	304 HAT ^{CML} Serra et al. (2018)	305 93.25	306 -2.07	307 73.67	308 -0.13	309 62.18	310 -8.51	311 72.72	312 -22.90
	305 GPM ^{ICLR} Saha et al. (2021)	306 94.80	307 -1.62	308 77.48	309 -1.37	310 70.07	311 -2.92	312 79.70	313 -15.52
	306 HLOP ^{ICLR} Xiao et al. (2024)	307 95.15	308 -1.30	309 78.58	310 -0.26	311 71.40	312 -0.52	313 88.65	314 -3.71
305 ANN	306 MSCN	307 96.34	308 0.0	309 79.54	310 0.0	311 73.22	312 0.0	313 88.84	314 0.0
	307 EWC ^{PNAS} Kirkpatrick et al. (2017)	308 92.01	309 -0.03	310 72.77	311 -3.59	312 64.51	313 -0.04	314 88.64	315 -0.04
	308 GPM ^{ICLR} Saha et al. (2021)	309 94.96	310 -0.02	311 73.18	312 -1.17	313 67.39	314 1.45	315 91.22	316 -0.01
	309 PackNet ^{CVPR} Mallya et al. (2018)	310 96.37	311 0.0	312 72.39	313 0.0	314 55.46	315 0.0	316 92.81	317 0.0
	310 SupSup ^{NeurIPS} Wortsman et al. (2020)	311 96.31	312 0.0	313 75.47	314 0.0	315 59.60	316 0.0	317 93.28	318 0.0
	311 WSN ^{CML} Kang et al. (2022)	312 96.41	313 0.0	314 76.38	315 0.0	316 71.96	317 0.0	318 93.41	319 0.0
	312 TAMiL ^{ICLR} Bhat et al. (2023)	313 96.87	314 -3.15	315 76.73	316 -3.47	317 72.55	318 -3.02	319 93.47	320 -4.72
	313 SPG ^{CML} Konishi et al. (2023)	314 96.35	315 -	316 74.82	317 -	318 73.26	319 -	320 93.32	321 -
	314 DFGP ^{ICCV} Yang et al. (2023)	315 94.64	316 -0.01	317 74.59	318 0.0	319 -	320 -	321 92.09	322 -0.01
	315 Bayesian ^{CML} Thapa & Li (2024)	316 96.74	317 -	318 75.57	319 -	320 73.93	321 -	322 93.36	323 -
	316 MSCN	317 97.53	318 0.0	319 77.37	320 0.0	321 75.03	322 0.0	323 93.69	324 0.0

313 4.2 COMPARISON TO THE STATE-OF-THE-ART METHODS

314 We first conduct a comprehensive evaluation of MSCN in a multi-head task-incremental learning
 315 scenario, using four widely used benchmark datasets and employing both SNNs and ANNs. As
 316 summarized in Table 1, where the dataset complexity roughly increases from left to right, the
 317 results consistently demonstrate the strength and reliability of MSCN across diverse datasets and
 318 architectures. Notably, on TinyImageNet with ANN, MSCN achieves an accuracy that exceeds the
 319 second-best method, Bayesian Thapa & Li (2024), by 1.10%. Although several approaches, such as
 320 WSN Kang et al. (2022), SupSup Wortsman et al. (2020), and PackNet Mallya et al. (2018), achieve
 321 zero backward transfer, they do not match the overall accuracy of MSCN. These findings indicate
 322 that multi-synaptic connectivity is an effective and scalable design for continual learning. Moreover,
 323 Fig. 2 shows that MSCN attains superior per-task performance on most tasks, further validating
 324 its representational strength. Since most existing works on continual learning are based on ANN

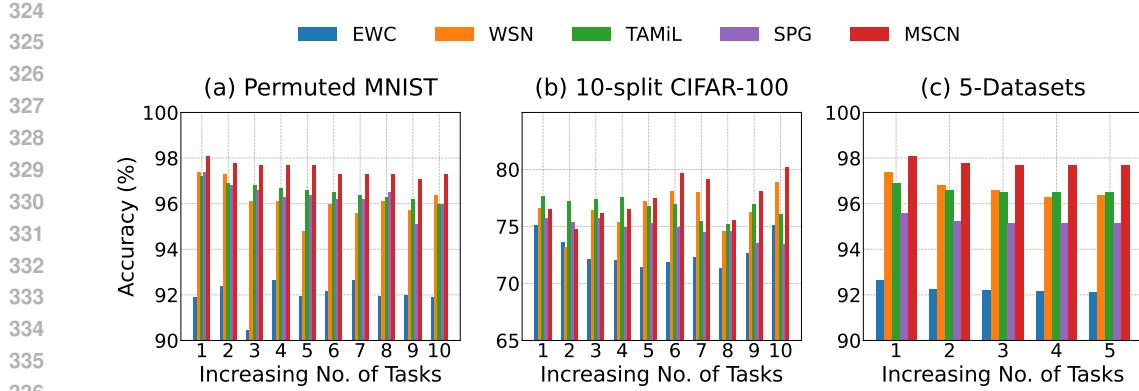


Figure 2: Per-task accuracy across the entire incremental learning.

architectures, we investigate our method extensively within the same framework in the following sections to ensure fairness while highlighting its strengths.

4.3 ROBUSTNESS TO TASK ORDER PERMUTATIONS

We evaluate order robustness by training on multiple CIFAR-100 Split permutations and measuring per-task accuracy variation over three task orders. As illustrated in Fig. 3d, we observe that EWC Kirkpatrick et al. (2017) and GPM Saha et al. (2021) display large fluctuations across task sequences, highlighting their strong sensitivity to order. WSN Kang et al. (2022) performs competitively with EWC but shows a tendency to overfit to particular task orders (Fig. 3a–b). In contrast, MSCN achieves stable accuracy across all tasks and permutations, with only minimal variation (Fig. 3c). This consistency indicates that MSCN can flexibly adapt to new tasks while mitigating interference and preserving prior knowledge, highlighting the important role of local activity-dependent synaptic modulation as a foundational mechanism for building scalable continual learning systems. Additional experiments on five task orders are reported in Fig. 10 of the Appendix A.3.4.

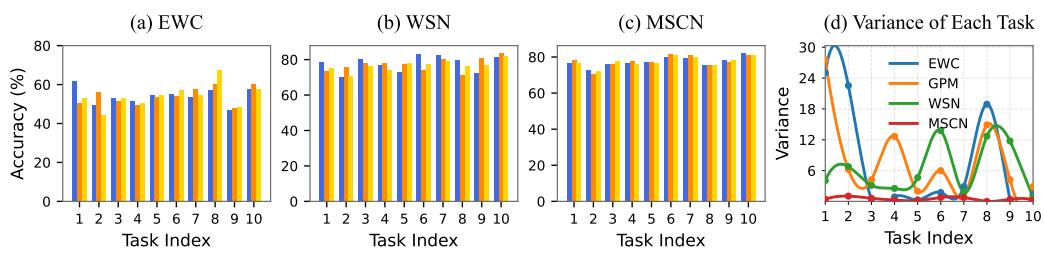


Figure 3: Task order robustness comparison on CIFAR-100 Split. Bar plots in (a), (b), and (c) show per-task accuracy under three different task sequences. Specifically, (a) corresponds to the EWC method, (b) to the WSN method, and (c) to our MSCN method. (d) shows the standard deviation of the accuracy for each task across different task sequences.

4.4 ABLATION STUDY

To better understand the individual contributions of the key components in MSCN, we perform an ablation study by selectively removing the multi-synaptic connectivity structure and the neuromodulatory mechanism. The results across four benchmark datasets are summarized in Table 2. The full MSCN model, with both components enabled, consistently achieves the highest accuracy across all datasets. Disabling the neuromodulatory mechanism results in a noticeable performance drop, particularly on TinyImageNet and PMNIST. Conversely, removing the multi-synaptic structure also results in performance degradation, particularly on CIFAR-100 and 5-Datasets. We observe that when both components are ablated, performance drops further across all datasets, confirming that

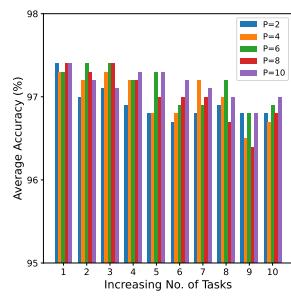
378 the two mechanisms act cooperatively and that their interaction is essential for MSCN’s ability to
 379 achieve robust and scalable continual learning.
 380

381
 382 Table 2: An ablation study of MSCN on ACC. ✓ indicates that the component is included, while
 383 ✗ indicates that it is excluded.

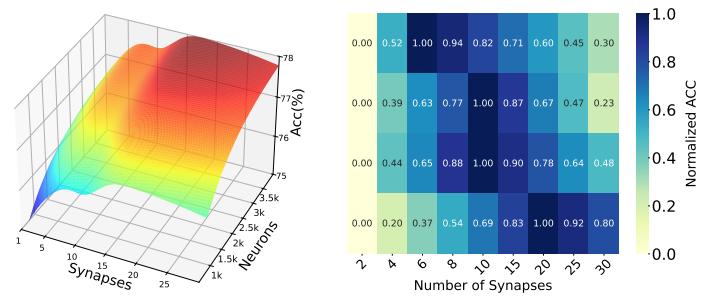
384	385	Multi-synapse	Modulation	PMNIST	CIFAR-100	TinyImageNet	5-Datasets
386		✓	✓	97.53 (± 0.19)	77.37 (± 0.23)	75.03 (± 0.27)	93.69 (± 0.21)
387		✗	✓	96.79 (± 0.20)	77.03 (± 0.22)	73.81 (± 0.26)	93.47 (± 0.24)
388		✓	✗	96.53 (± 0.21)	76.81 (± 0.25)	73.78 (± 0.29)	93.51 (± 0.22)
389		✗	✗	96.34 (± 0.22)	76.34 (± 0.24)	72.59 (± 0.31)	93.32 (± 0.25)

393 4.5 EFFECT OF SYNAPSE COUNT

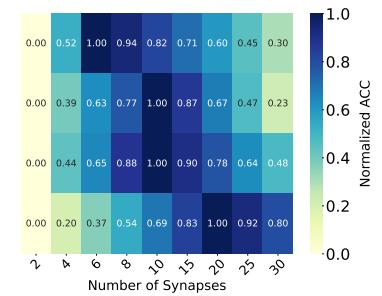
394 To probe the role of multi-synaptic connectivity, we vary synapse and neuron counts and measure
 395 performance across tasks. On CIFAR-100 Split (Fig. 4), increasing synapses per connection consis-
 396 tently raises per-task accuracy as the number of tasks grows. Jointly scaling synapses and neurons
 397 (Fig. 5) reveals a saturation regime: accuracy improves with capacity but plateaus once model
 398 capacity exceeds task complexity. Fig. 6 summarizes four benchmarks; rows (top→bottom) are
 399 PMNIST, CIFAR-100, TinyImageNet, and 5-Datasets, reflecting increasing complexity. We observe
 400 that, although the optimal number of synapses varies with task difficulty, it generally stabilizes once a
 401 certain threshold is exceeded. Interestingly, the observed performance trend happens to mirror how
 402 synaptic counts are distributed in the brain—typically confined to a limited but effective range Toni
 403 et al. (1999); Watson et al. (2025). Additional experimental results are provided in Appendix A.3.3.



415 Figure 4: Per-task accuracy
 416 under different synapse
 417 counts on CIFAR-100 Split.



415 Figure 5: Accuracy under
 416 different synapse and neuron
 417 counts on CIFAR-100 Split.



415 Figure 6: Accuracy changes across
 416 four datasets under varying num-
 417 bers of synapses.

421 4.6 CAPACITY ANALYSIS

422 To evaluate the capacity efficiency of MSCN, we adopt the commonly used metric CAP Kang et al.
 423 (2022); Wortsman et al. (2020) (defined in Appendix A.2.2) and compare it with baseline approaches,
 424 where lower CAP values indicate better capacity utilization. Fig. 7 shows the relationship between
 425 accuracy and total capacity usage across four benchmark datasets. The results demonstrate that MSCN
 426 consistently achieves the highest accuracy with significantly lower capacity overhead. On Permutated
 427 MNIST and TinyImageNet (Fig. 7a,c), MSCN outperforms all baselines while requiring substantially
 428 fewer resources. Similar trends are observed on CIFAR-100 and the 5-Datasets benchmark (Fig. 7b,d),
 429 where methods such as PackNet Mallya et al. (2018) and SupSup Wortsman et al. (2020) consume
 430 much more capacity but yield lower or comparable performance. These results indicate that the
 431 multi-synaptic cooperation mechanism enables more effective knowledge storage and reuse across
 432 tasks.

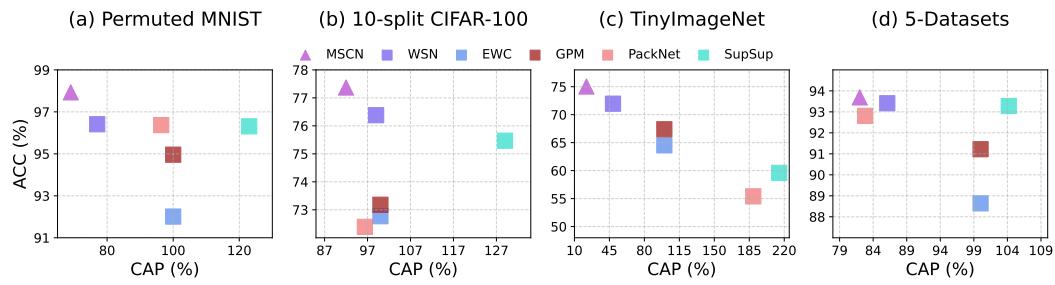


Figure 7: Accuracy over CAP (%) across four benchmarks.

445 4.7 COMPUTATIONAL EFFICIENCY

446 Since multi-synaptic connections inevitably increase the parameter count, we conducted experiments
 447 under the same parameter budget as the baselines to fairly evaluate computational efficiency. We
 448 further evaluated robustness under five task orders using AOPD (where lower values indicate stronger
 449 robustness; see Appendix A.2.2 for details). As shown in Table 3, although reducing the parameter
 450 count leads to a drop in MSCN’s accuracy, our method consistently achieves the best efficiency and
 451 robustness while maintaining competitive accuracy. These results demonstrate that the proposed
 452 multi-synaptic cooperation mechanism achieves high computational efficiency and establishes the
 453 foundation for robust and scalable continual learning.

Table 3: Computational efficiency under the same parameter budget (Training time in hours).

Method	PMNIST			10-split CIFAR-100		
	Training Time ↓	ACC (%) ↑	AOPD (%) ↓	Training Time ↓	ACC (%) ↑	AOPD (%) ↓
PackNet	0.59 (± 0.15)	96.43 (± 0.18)	2.23	1.13 (± 0.10)	72.45 (± 0.20)	5.36
SupSup	0.53 (± 0.12)	96.36 (± 0.22)	1.27	0.87 (± 0.08)	75.54 (± 0.17)	3.81
WSN	0.38 (± 0.05)	96.49 (± 0.13)	0.29	0.78 (± 0.06)	76.47 (± 0.34)	2.59
MSCN	0.33 (± 0.11)	96.89 (± 0.19)	0.23	0.65 (± 0.04)	76.40 (± 0.14)	2.41

Method	TinyImageNet			5-Datasets		
	Training Time ↓	ACC (%) ↑	AOPD (%) ↓	Training Time ↓	ACC (%) ↑	AOPD (%) ↓
PackNet	1.45 (± 0.12)	55.51 (± 0.25)	6.51	3.45 (± 0.08)	92.89 (± 0.12)	4.37
SupSup	0.97 (± 0.07)	59.65 (± 0.24)	6.94	3.26 (± 0.10)	93.31 (± 0.16)	2.83
WSN	0.92 (± 0.04)	72.03 (± 0.41)	4.98	3.05 (± 0.08)	93.50 (± 0.13)	1.37
MSCN	0.75 (± 0.03)	74.04 (± 0.21)	4.73	2.82 (± 0.09)	93.33 (± 0.09)	1.26

474 5 CONCLUSION

475 In this paper, we propose MSCN, the first continual learning framework that explicitly models multi-
 476 synaptic cooperation. By equipping each connection with multiple plastic synapses and employing
 477 local synaptic activity-based modulation, MSCN achieves effective knowledge retention and adapt-
 478 ability within a fixed architecture. Extensive evaluations across diverse datasets and architectures
 479 demonstrate that our approach consistently outperforms state-of-the-art baselines in terms of compu-
 480 tational efficiency and task order robustness. These findings highlight that the synergistic interplay
 481 between multi-synaptic connectivity and localized plasticity modulation substantially enhances the
 482 network’s representational capacity, providing new insights for robust and scalable continual learning.
 483 In addition, the similarity between our model’s synapse counts and those found in biological systems
 484 further supports the plausibility of our design. Future work will explore allocating different numbers
 485 of synapses across neuron connections to further optimize synaptic resource utilization.

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795 A APPENDIX

796 A.1 MULTI-SYNAPTIC COOPERATION NETWORK IN ANNS

797 A.1.1 MODELING MULTI-SYNAPTIC NEURON

798 In biological neurons, a single axon can establish multiple synaptic contacts with the same dendritic
 799 branch, enabling the signal to influence the target neuron through parallel pathways Turegano-Lopez
 800 et al. (2024); Callan et al. (2021). To simulate this structure in artificial neural networks, we represent
 801 each inter-neuronal connection not by a single weight but by a vector of parallel synaptic weights.
 802 Each element in this vector is trained independently, and their combined effect determines the
 803 connection strength. This design remains compatible with existing network architectures, supports
 804 standard gradient-based learning, and naturally extends plasticity rules developed for spiking neural
 805 networks.

806 To model multi-synaptic connections in ANNs, we first associate each connection (i, j) with a column
 807 vector of synaptic weights \mathbf{w}_{ij} :

$$808 \mathbf{w}_{ij} = [w_{ij}^1, \dots, w_{ij}^P]^\top \quad (12)$$

809 where P is a hyperparameter representing the number of synaptic connections between each pair of
 810 neurons. To preserve synaptic diversity and enable distinct optimization of parallel synapses, we

810 assign different activation functions to different parallel synapses. The input to postsynaptic neuron j
 811 from presynaptic neuron i is then defined as:
 812

$$813 \quad 814 \quad 815 \quad g_{ij}(x_i) = \sum_{p=1}^P \sigma_p(w_{ij}^p x_i) \quad 816$$

817 where σ_p denotes the activation function specific to the p -th synapse. When an input vector \mathbf{x} is given
 818 to a fully connected layer, the input to neuron j is computed as
 819

$$820 \quad 821 \quad 822 \quad z_j = \sum_{i=1}^N g_{ij}(x_i) = \sum_{i=1}^N \sum_{p=1}^P \sigma_p(w_{ij}^p x_i) \quad 823$$

824 where N is the number of input neurons in the layer. The value z_j is then passed through a ReLU
 825 activation function resulting in the output $y_j = \max(0, z_j)$. Similarly, in convolutional layers, the
 826 additional synaptic dimension is incorporated into each filter. As a result, the summation in Eq. (14)
 827 also spans spatial locations and input channels.
 828

829 For local synaptic plasticity modulation, we associate the local activity of each neuron with its output
 830 value. The eligibility trace is defined as follows:
 831

$$830 \quad 831 \quad \tilde{e}[t+1] = \tilde{e}[t] - \frac{\tilde{e}[t]}{\tau} + z_j \quad 832$$

833 where τ is a decay time constant. Each synaptic weight is updated using the following learning rule:
 834

$$835 \quad 836 \quad \Delta w_{ij}^p = -\eta \cdot |f_{\text{mod}}(\tilde{e}_{ij})| \cdot \frac{\partial \mathcal{L}}{\partial w_{ij}^p} \quad 837$$

838 where η is the learning rate. The eligibility trace \tilde{e}_{ij} keeps track of local synaptic activity. The
 839 function f_{mod} uses this information to smoothly adjust the synaptic strength—potentiation or de-
 840 pression—similar to how synaptic plasticity is modulated in spiking neural models. When $P = 1$,
 841 Eq. (12)–Eq. (16) become the same as in standard ANNs, so this method remains fully compatible
 842 with existing implementations.
 843

844 A.2 IMPLEMENTATION DETAILS

845 A.2.1 DATASETS.

846 The datasets used in our experiments are summarized in Table 4. We evaluate our approach on four
 847 standard continual learning benchmarks: Permuted MNIST (PMNIST), CIFAR-100, TinyImageNet,
 848 and 5-Datasets, which are presented in roughly increasing order of dataset complexity.
 849

850 **PMNIST** is a variant of the original MNIST dataset consisting of 28×28 grayscale images of
 851 handwritten digits. Each task applies a fixed but unique random permutation to the pixel positions,
 852 making it a widely adopted benchmark for evaluating robustness in task-incremental learning. For
 853 PMNIST, we assign each task 60,000 training and 10,000 testing samples to increase the challenge.
 854

855 **CIFAR-100**. CIFAR-100 is an object recognition dataset with 100 natural image classes. Following
 856 the protocol in Rebuffi et al. (2017), we partition the dataset into 10 tasks, each comprising 10 disjoint
 857 classes with their corresponding images.
 858

859 **TinyImageNet** contains 100,000 64×64 color images across 200 classes. We construct 40 sequential
 860 tasks by splitting the dataset into 5-way classification problems. For fair comparison, we randomly
 861 sample a subset of the original dataset and align the test set with the training set as in Serra et al.
 862 (2018).
 863

864 **5-Datasets** combines tasks from five diverse datasets: MNIST, SVHN, Fashion-MNIST, CIFAR-10,
 865 and NotMNIST, each treated as an independent task. This setting evaluates the model’s generalizabil-
 866 ity under distribution shift and cross-domain learning.
 867

864 For CIFAR-100 and TinyImageNet, we follow standard settings with 500 training and 100/50 test
 865 images per class, respectively.
 866

867 Table 4: Dataset statistics
 868

869 Dataset	870 PMNIST	871 CIFAR-100	872 TinyImageNet	873 5-Datasets
870 Tasks	871 10	872 10	873 40	874 5
870 Classes	871 10	872 100	873 200	874 /
870 Training Samples	871 60,000	872 50,000	873 100,000	874 /
870 Test Samples	871 10,000	872 10,000	873 10,000	874 /

875 **A.2.2 EVALUATION METRICS**
 876

877 Following Kang et al. (2022); Wortsman et al. (2020); Mallya et al. (2018), we evaluate all methods
 878 based on the following metrics:

879 **Accuracy (ACC)** measures the average of the final classification accuracy on all tasks:
 880

$$881 \text{ACC} = \frac{1}{T} \sum_{i=1}^T acc_{T,i} \quad (17)$$

883 where $acc_{T,i}$ is the test accuracy for task i after training on task T .
 884

885 **Backward Transfer (BWT)** measures the influence of learning new tasks on the performance of
 886 previously learned ones. A negative BWT indicates forgetting, whereas a positive BWT suggests that
 887 learning later tasks improved the performance of earlier ones. BWT is computed as:
 888

$$889 \text{BWT} = \frac{1}{T-1} \sum_{i=1}^{T-1} (acc_{T,i} - acc_{i,i}) \quad (18)$$

891 where $acc_{i,i}$ denotes the accuracy of task i immediately after it is learned. A BWT close to zero
 892 implies stability, while highly negative values indicate catastrophic forgetting.
 893

894 **Capacity (CAP)** measures the amount of network capacity used under each parameter pruning
 895 method Kang et al. (2022). It accounts for both the proportion of trainable parameters and the
 896 efficiency of binary encoding. The CAP metric is defined as:
 897

$$898 \text{CAP} = (1 - C) + \frac{(1 - \alpha)N}{32} \quad (19)$$

899 where α is the average mask compression rate ($\alpha=0.78$), N is the number of tasks, and C is the
 900 percentage of non-fixed parameters. A smaller CAP value indicates higher effective network capacity.
 901

902 **Average Order-normalized Performance Disparity (AOPD)** measures the robustness of these al-
 903 gorithms under different task orders. Following the protocol of Yoon et al. (2019), we assessed
 904 the task order robustness with the Order-normalized Performance Disparity (OPD) metric, which
 905 is computed as the disparity between the performance \bar{A}_t of task t on R different task orders:
 906 $OPD_t \triangleq \max\{\bar{A}_t^1, \dots, \bar{A}_t^R\} - \min\{\bar{A}_t^1, \dots, \bar{A}_t^R\}$. The average OPD (AOPD) is defined by
 907

$$908 \text{AOPD} \triangleq \frac{1}{T} \sum_{t=0}^{T-1} OPD_t \quad (20)$$

909 **A.2.3 EXPERIMENT SETTINGS**
 910

911 All experiments were conducted on a Linux server equipped with an Intel Xeon Gold 5220 (2.20 GHz)
 912 CPU and two NVIDIA Tesla V100-SXM2 GPUs (32 GB each, driver 535.129.03). Following Kang
 913 et al. (2022); Wortsman et al. (2020); Mallya et al. (2018), we use a two-layered MLP with 100
 914 neurons per layer for PMNIST and use a modified version of AlexNet for the CIFAR-100 Split dataset
 915 and a reduced ResNet-18 Chaudhry et al. (2019); Saha et al. (2021) for 5-Datasets. For TinyImageNet,
 916 we also use the same network architecture Gupta et al. (2020a); Deng et al. (2021), which consists of
 917 4 Conv layers and 3 fully connected layers. **For a fair comparison, we follow the experimental setting**
 918 **in Kang et al. (2022); Thapa & Li (2024), and all methods are evaluated under the same multi-head**
 919 **setting with known task labels.** The hyperparameter settings are presented in Table 7.

918 Table 5: Performance deviations of the proposed method and baselines on four datasets.
919920 (a) PMNIST and 10-split CIFAR-100
921

922 Network	923 Method	924 PMNIST		925 10-split CIFAR-100	
		926 ACC (%)	927 BWT (%)	928 ACC (%)	929 BWT (%)
930 SNN	931 MTL	932 0.12	933 /	934 0.31	935 /
	936 EWCKirkpatrick et al. (2017)	937 0.51	938 0.42	939 0.63	940 0.57
	941 HAT Serra et al. (2018)	942 0.24	943 0.0	944 0.37	945 0.19
	946 GPM Saha et al. (2021)	947 0.43	948 0.34	949 0.41	950 0.38
	951 HLOP Xiao et al. (2024)	952 0.39	953 0.21	954 0.35	955 0.18
	956 MSCN	957 0.22	958 0.0	959 0.25	960 0.0
961 ANN	962 MTL	963 0.14	964 /	965 0.21	966 /
	967 EWCKirkpatrick et al. (2017)	968 0.56	969 0.01	970 0.57	971 0.49
	972 GPM Saha et al. (2021)	973 0.07	974 0.01	975 0.48	976 0.39
	977 PackNet Mallya et al. (2018)	978 0.04	979 0.0	980 0.41	981 0.0
	982 SupSup Wortsman et al. (2020)	983 0.09	984 0.0	985 0.32	986 0.0
	987 WSN Kang et al. (2022)	988 0.07	989 0.0	990 0.29	991 0.0
	992 TAMiL Bhat et al. (2023)	993 0.17	994 0.04	995 0.36	996 0.49
	997 MSCN	998 0.19	999 0.0	1000 0.23	1001 0.0

922 (b) TinyImageNet and 5-Datasets
923

924 Network	925 Method	926 TinyImageNet		927 5-Datasets	
		928 ACC (%)	929 BWT (%)	930 ACC (%)	931 BWT (%)
932 SNN	933 MTL	934 0.29	935 /	936 0.26	937 /
	938 EWCKirkpatrick et al. (2017)	939 0.59	940 0.72	941 0.48	942 0.65
	943 HAT Serra et al. (2018)	944 0.61	945 0.44	946 0.33	947 0.51
	948 GPM Saha et al. (2021)	949 0.46	950 0.29	951 0.36	952 0.42
	953 HLOP Xiao et al. (2024)	954 0.41	955 0.23	956 0.30	957 0.25
	958 MSCN	959 0.31	960 0.0	961 0.29	962 0.0
963 ANN	964 MTL	965 0.33	966 /	967 0.27	968 /
	969 EWCKirkpatrick et al. (2017)	970 0.44	971 0.03	972 0.26	973 0.02
	974 GPM Saha et al. (2021)	975 0.42	976 0.31	977 0.20	978 0.01
	979 PackNet Mallya et al. (2018)	980 0.35	981 0.0	982 0.12	983 0.0
	984 SupSup Wortsman et al. (2020)	985 0.40	986 0.0	987 0.21	988 0.0
	989 WSN Kang et al. (2022)	990 0.34	991 0.0	992 0.13	993 0.0
	994 TAMiL Bhat et al. (2023)	995 0.31	996 0.13	997 0.22	998 0.08
	999 MSCN	1000 0.27	1001 0.0	1002 0.21	1003 0.0

964 A.2.4 ARCHITECTURAL DETAILS

965 **Two-layered MLP:** In conducting the PMNIST experiments, we are following the exact setup as
966 denoted by Saha et al. (2021) fully-connected network with two hidden layers of 100 neurons Lopez-
967 Paz & Ranzato (2017).968 **Modified AlexNet:** For the split CIFAR-100 dataset, we use a modified version of AlexNet similar
969 to Gupta et al. (2020b); Saha et al. (2021).

972 Table 7: Experiment settings and hyperparameter configurations for different datasets
973

974 Dataset	975 PMNIST	976 10-split CIFAR-100	977 TinyImageNet	978 5-Datasets
979 learning rate	1×10^{-3}	1×10^{-3}	1×10^{-3}	1×10^{-3}
980 dropout rate	0.2	0.2	0.5	0.2
981 epochs	5	200	10	100
982 batch size	10	64	10	64
983 warmup ratio	0.05	0.05	0.05	0.05
984 optimizer	AdamW	AdamW	AdamW	AdamW
985 weight decay	1×10^{-2}	1×10^{-2}	1×10^{-2}	1×10^{-2}
986 architecture	Two-layered MLP	Modified AlexNet	4 Conv layers and 3 Fully connected layers	Reduced ResNet18

983 **4 Conv layers and 3 Fully connected layers:** For TinyImageNet, we use the same network architecture as Gupta et al. (2020b); Deng et al. (2021).

984 **Reduced ResNet18:** In conducting the 5-Dataset experiments, we use a smaller version of ResNet18 with three times fewer feature maps across all layers as denoted by Lopez-Paz & Ranzato (2017).

985 A.2.5 LIST OF MAIN NOTATIONS

986 In Table 8, we list the main notations used in this paper, together with brief explanations, enabling
987 quick reference to the meaning of each symbol.

988 Table 8: List of main notations

989 Notation	990 Description
991 m_j	992 Binary mask selecting active synapses for task j
993 M_{j-1}	994 Accumulated mask of all previous tasks up to $j - 1$
995 r	996 Learnable relevance score for each synapse
997 c	998 Layer-wise capacity ratio for subnet selection
999 P	1000 Number of parallel synapses in each connection (synapse count)
1001 w_{ip}	1002 Weight of the p -th synapse from presynaptic neuron i
1003 N	1004 Number of presynaptic neurons
1005 $V(t)$	1006 Membrane potential of a spiking neuron at time t
1007 τ_m	1008 Membrane time constant in LIF neurons
1009 V_{rest}	1010 Resting potential of the spiking neuron
1011 $I(t)$	1012 Total synaptic input current at time t
1013 $\text{PSP}_{ip}(t)$	1014 Postsynaptic potential from synapse p of neuron i
1015 $\tau_{s,ip}$	1016 Decay constant of the p -th parallel synapse of neuron i
1017 $K_{ip}(t)$	1018 Synaptic kernel of the p -th synapse of neuron i
1019 t_{ip}^f	1020 Arrival time of the f -th spike at synapse (i, p)
1021 \tilde{e}	1022 Eligibility trace representing local synaptic activity
1023 τ	1024 Decay time constant of the eligibility trace
1025 $f_{\text{mod}}(\tilde{e})$	1026 Modulation function for \tilde{e}

1017 A.3 EXTRA EXPERIMENTS

1018 A.3.1 INTEGRATION WITH DIFFERENT TYPES OF METHODS

1019 To further evaluate the applicability of our MSCN, we integrated it with different types of methods
1020 and conducted additional experiments on both 10-split CIFAR-100 and TinyImageNet under the same
1021 parameter budget. As shown in Table 9, integrating MSCN into regularization-based and replay-
1022 based methods consistently improves BWT. Notably, combining MSCN with ER on TinyImageNet
1023 improves BWT by 53.8% (an absolute decrease of 10.69). The observed BWT improvements are
1024 attributed to the high capacity efficiency of MSCN, which arises from the independent optimization of
1025

Table 9: Integration with different types of methods.

Type	Method	10-split CIFAR-100		TinyImageNet	
		ACC (%) \uparrow	BWT (%) \uparrow	ACC (%) \uparrow	BWT (%) \uparrow
regularization-based	EWC	72.77 (± 0.57)	-3.59 (± 0.49)	64.51 (± 0.44)	-0.04 (± 0.03)
	EWC+MSCN	73.26 (± 0.66)	-2.78 (± 0.19)	64.98 (± 0.54)	-0.03 (± 0.01)
replay-based	ER	70.07 (± 0.73)	-7.70 (± 0.59)	48.32 (± 0.91)	-19.86 (± 0.70)
	ER+MSCN	71.13 (± 0.62)	-5.24 (± 0.51)	49.26 (± 0.84)	-9.17 (± 0.55)
architecture-based	Bayesian	75.57 (± 0.38)	0.00 (± 0.00)	73.93 (± 0.36)	0.00 (± 0.00)
	Bayesian+MSCN	76.48 (± 0.34)	0.00 (± 0.00)	74.56 (± 0.33)	0.00 (± 0.00)

multiple parallel synapses, as demonstrated in Fig. 7. Such higher capacity efficiency has been shown to reduce catastrophic forgetting Hung et al. (2019a); Mirzadeh et al. (2022); Farajtabar et al. (2020). Meanwhile, the modulation mechanism further enhances this property by depressing the effect of noisy samples and strengthening learning on clean ones. In contrast, for architecture-based methods, BWT remains zero because the weights of past tasks are frozen, which is exactly as expected. At the same time, when our MSCN is incorporated, all three types of methods achieve improved accuracy. These additional experiments further highlight the robustness of our MSCN.

A.3.2 LAYER-WISE CAPACITY ANALYSIS

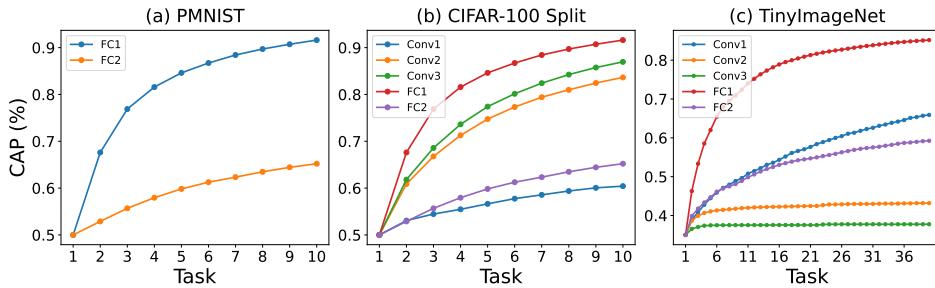


Figure 8: Synaptic capacity usage as the number of tasks increases on three benchmarks. Each curve shows the percentage of active synapses per layer as tasks are incrementally introduced.

As shown in Fig. 8, we analyze the synaptic capacity usage across three benchmarks: PMNIST, CIFAR-100 Split, and TinyImageNet. For each dataset, we measure the percentage of utilized synapses in each layer as tasks are incrementally learned. Across all three datasets, we observe a consistent pattern: capacity usage increases rapidly during the initial tasks, then gradually slows down as more tasks are introduced. This effect is particularly pronounced in the fully connected layers, such as FC1, which tend to accumulate more synaptic updates compared to early convolutional layers. The underlying reason is that the model needs to allocate new synaptic resources to encode novel task-specific features at the beginning. However, as training progresses, many new tasks can be handled by reusing synapses that represent similar features, reducing the need for additional capacity. This confirms the model’s ability to reuse past representations more effectively as it acquires more knowledge, leading to a slower growth in capacity usage over time.

A.3.3 ANALYSIS OF SYNAPSE COUNT

Fig. 9 illustrates the relationship between synapse count (denoted as P) and average accuracy as the number of tasks increases, evaluated on PMNIST and CIFAR-100 Split. We vary the number of synapses per connection across five settings ($P=2, 4, 6, 8, 10$) and track model performance throughout the incremental learning process. We observe that on PMNIST, accuracy remains high across all configurations; however, larger synapse counts (e.g., $P=8, 10$) tend to deliver more stable performance over multiple tasks. On CIFAR-100 Split, the benefits of increased synaptic capacity become more evident: higher P values consistently result in better average accuracy, particularly as

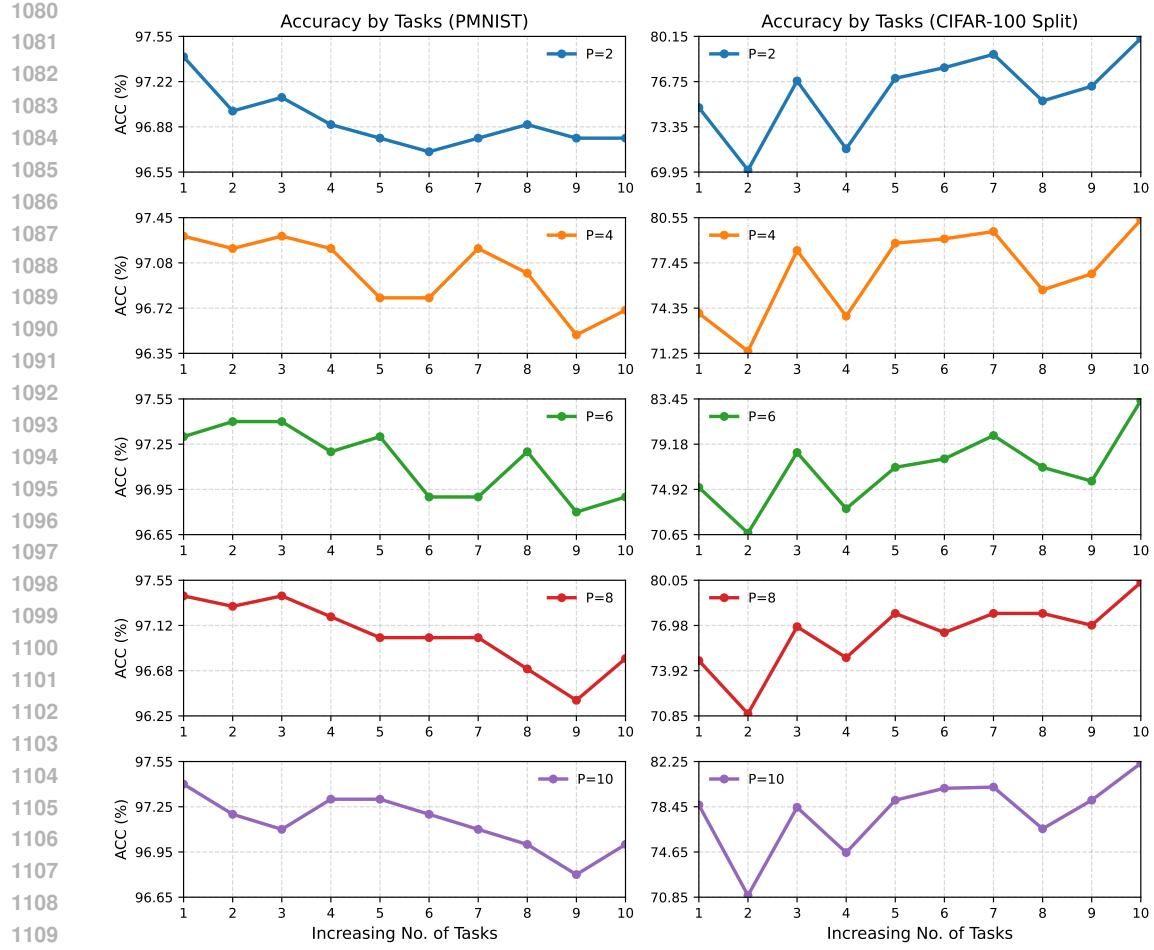


Figure 9: Average accuracy with increasing number of tasks under different synapse counts.

the number of tasks grows. These results confirm that synaptic multiplicity enhances the model’s ability to retain knowledge and generalize over longer task sequences.

A.3.4 ORDER ROBUSTNESS ANALYSIS

To further investigate the robustness of our method to task permutations, we conduct additional experiments on the CIFAR-100 Split benchmark using five randomly shuffled task orders. Fig. 10 presents the per-task accuracy across all 10 tasks for three representative baselines—EWC Kirkpatrick et al. (2017), GPM Saha et al. (2021), and WSN Kang et al. (2022)—alongside our proposed MSCN. We observe that EWC (Fig. 10a) and GPM (Fig. 10b) are highly sensitive to task order, exhibiting considerable variance in accuracy for the same task index across different permutations. In contrast, WSN (Fig. 10c) achieves more stable performance, though moderate fluctuations persist, particularly on later tasks. Notably, our method, MSCN (Fig. 10d), maintains consistently high accuracy across all permutations and task indices, with significantly reduced inter-order variance. These results show that MSCN is robust to task order, ensuring stability in dynamic environments.

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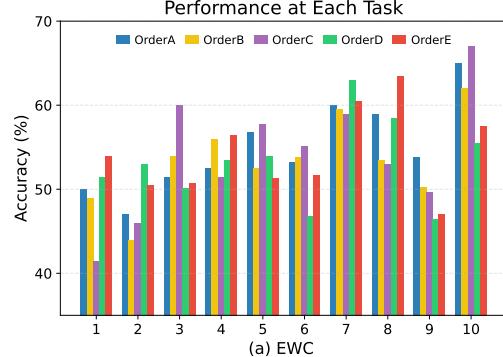
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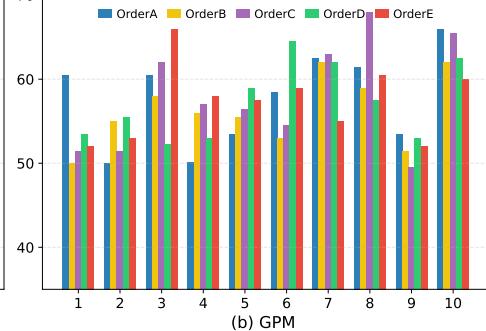
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1148 Performance at Each Task



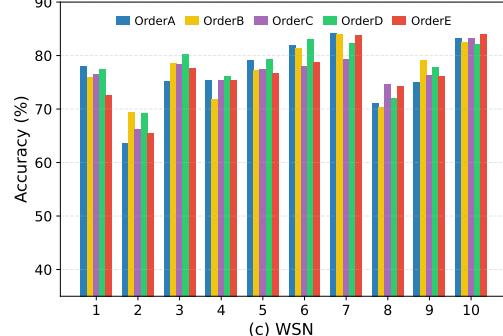
(a) EWC

1149 Performance at Each Task



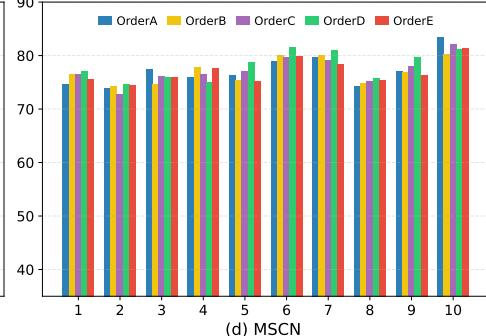
(b) GPM

1150 Performance at Each Task



(c) WSN

1151 Performance at Each Task



(d) MSCN

1152 Figure 10: Task order robustness comparison on CIFAR-100 Split. Bar plots show per-task accuracy under five different task sequences.

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