Advancing Beyond Identification: Multi-bit Watermark for Large Language Models

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Abstract

We show the viability of tackling misuses of large language models beyond the identification of machine-generated text. While existing methods focus on detection only, some malicious misuses demand tracing the adversary 006 user for counteracting them. To address this, we propose Multi-bit Watermark via Position Allocation, embedding traceable multi-bit information during language model generation. Leveraging the benefits of zero-bit watermarking (Kirchenbauer et al., 2023a), our method enables robust extraction of the watermark without any model access, embedding and extraction of long messages (\geq 32-bit) without finetuning, and maintaining text quality, while al-016 lowing zero-bit detection all at the same time. Moreover, our watermark is relatively robust under strong attacks like interleaving human texts and paraphrasing. We compare with existing works to show the effectiveness of our scheme in terms of robustness and latency.

1 Introduction

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How can we take a step further from merely identifying machine-generated text to proactively tackling misuses of large language models? The emergence of human-like language models and their easily accessible nature via web interface and APIs have garnered unprecedented attention from the public and academia (Hu, 2023). The ability to follow complex instructions has boosted the productivity of various tasks such as programming, creative writing, and more. However, there have been increasing concerns about exploiting such language models to automate malicious activities such as spreading disinformation. This has necessitated the development of various methods to detect machinegenerated texts through techniques such as zeroshot detection, supervised training, watermarking, and more (Mitchell et al., 2023; Wang et al., 2023b; Kirchenbauer et al., 2023a; Krishna et al., 2023). These endeavors focus on the crucial task of *identi*fying machine-generated content, which serves as a pivotal step in mitigating the potential harm caused by such text.

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However, when it comes to more pernicious misuses of large language models, such as the dissemination of misinformation and propaganda on social media platforms, the stakes are considerably higher, potentially leading to the erosion of social trust (Valenzuela et al., 2022). Notable instances that exploited automated bots in the past include manipulating an election campaign (Badawy et al., 2018), spreading disinformation about the Russian invasion of Ukraine (Pierri et al., 2023), and promoting products through fake reviews (Annie, 2023). With the rapid pace at which large language models are currently developed, similar threats will be automated in a much more rapid and delicate manner in the future.

In such circumstances, merely identifying the machine-generated text may not suffice for the language model providers. Instead, the ability to trace back to the adversary user responsible for generating the content becomes pivotal in counteracting such misuses. By doing so, the API providers can take a precursory measure to ban these users from their systems. More importantly, this allows media and social platforms, along with API providers, to collaborate with law enforcement authorities and take more decisive actions. All in all, watermarking the user information (or part thereof) can hold the adversary user accountable for potential harms facilitated through language model APIs without having to store user queries (Krishna et al., 2023), which would be prohibitively expensive and concern ordinary users who value privacy. Additionally, watermarking can enable language model providers to bind meta-data (e.g. model versions) for tracing the provenance of the language model output.

All this can be achieved by embedding multi-

bit information. Our proposed method Multi-bit watermark via Position Allocation (MPAC) first allocates each token pseudo-randomly onto a single position of the message to be embedded. Then the message content at the allocated position decides which subset of tokens to favor following a zero-bit watermarking scheme (Kirchenbauer et al., 2023a) that pseudo-randomly biases certain token subsets for generation. To increase load capacity, we can further partition the vocabulary into multiple "colored" lists instead of a single green list, effectively encoding multiple states for every token. We demonstrate the effectiveness of our method compared to concurrent works in terms of robustness and generation latency, espeically in high bit-width and high corruption settings. Finally, we discuss and analyze the limitations of multi-bit watermarking in Section 5 – namely, the trade-off between watermark detection and bit-width. 100

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101 Since our method works on top of zero-bit watermarking, it leverages most of the advantages: (1) 102 Multi-bit message can be extracted without access 103 to the model parameters or the API, allowing other 104 parties to extract the adversary information (e.g. 105 timestamp, ID) if given access to the extraction 106 algorithm. (2) It can be done on the fly without pre-107 training or finetuning the model and can embed and 108 extract long messages (> 32-bit) with negligible 109 overhead. (3) The watermark is not fragile against 110 realistic corruptions such as interleaving with hu-111 man texts or paraphrasing. This has not been previ-112 ously demonstrated in other post-processing multi-113 bit watermarks (Yoo et al., 2023) or stenography 114 methods (Ziegler et al., 2019; de Witt et al., 2023). 115 (4) Finally, our watermarking framework can dis-116 tinguish between machine and human text and si-117 multaneously embed multi-bit information while 118 maintaining the same text quality as its zero-bit 119 counterpart. Our experiments demonstrate that 8-120 bit messages can be embedded effectively in short 121 text lengths (< 100 words) with over 95% bit ac-122 curacy. We hope this opens up new research direc-123 tions for proactively counteracting malicious use 124 cases of language model APIs.¹ 125

2 **Related Works**

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Watermarking has been studied in various types of multimedia such as image (Potdar et al., 2005), video (Asikuzzaman and Pickering, 2017), au-

dio (Hua et al., 2016), and natural language (Topkara et al., 2005). Following previous works (Zhu et al., 2018; Luo et al., 2020), we use the term watermarking to denote embedding information into natural language in a manner that is robust against possible attacks given a watermarked text - in our case, this is the output generated by a language model given the prompt. This differs from steganography (Cheddad et al., 2010; Fang et al., 2017; Ziegler et al., 2019; de Witt et al., 2023), which focuses more on the undetectability of a secret message that is embedded in the multimedia rather than robustness. For instance, Ziegler et al. (2019) sequentially encodes information via arithmetic coding every token. Naively applying this deterministic encoding scheme makes the watermark extremely fragile to simple corruptions as shown in Appendix Fig. 5.

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Recently, methods relying on neural networks have shown progress in natural language watermarking, outperforming traditional methods that rely on rule-based watermarks (Topkara et al., 2006b,a; Atallah et al., 2001). Abdelnabi and Fritz (2021) proposed an end-to-end framework where a decoder network predicts the encoded message. Yang et al. (2022) improved upon the quality of the watermarked text by using an algorithmic approach. Building upon this, Yoo et al. (2023) focused on robustness and capacity, outperforming previous works on both aspects. However, since the proposed method works at the sentence-level, any addition or removal of a sentence will fail to extract the watermark. Moreover, these works cannot distinguish non-watermarked texts, making them unsuitable for distinguishing between machine text and human text.

Meanwhile, directly watermarking language models in a zero-bit manner during token generation has emerged as a promising approach for distinguishing language model outputs from human text (Kirchenbauer et al., 2023a; Aaronson and Kirchner, 2023) while achieving robustness against realistic attacks (Kirchenbauer et al., 2023b). Several works have improved upon Kirchenbauer et al. (2023a), e.g., in low entropy generation tasks such as code generation (Lee et al., 2023), undetectability of the watermark (Christ et al., 2023), and its robustness (Munyer and Zhong, 2023). We focus on extending the prior work for a more proactive counteraction towards identifying malicious users of language models by embedding any information while maintaining the key advantages.

¹https://github.com/anoymous92874838/multibitwatermark-for-llms

Concurrent to our work, Fernandez et al. (2023a) and Wang et al. (2023a) use the entire message to create a signal unique to each message. Crucially, both works use the entire message content directly during embedding as input to the random seed generator, which leads to key differences in terms of robustness and latency. We further discuss their methodology in comparison with ours in the next section. Aside from this, Wang et al. (2023a) further utilize a proxy language model to enhance text quality.

3 Method

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We outline the multi-bit watermark protocol:

- 1. A user sends a prompt X to the language model provider.
- 2. Using the message encoding function \mathcal{E} , the language model provider generates watermarked text Y embedded with a multibit information. The message contains user-specific meta-data that can aid tracing back to the user (e.g. timestamp, location, ID).
- 3. The user publishes the text \tilde{Y} , which may be edited from the original watermarked text.
- 4. If the published text is deemed unsafe or malicious, the detector inspects \tilde{Y} (i) to determine whether the watermark is present (zero-bit detection) and (ii) decode the multi-bit message to take further measure.

3.1 Zero-bit Watermarking (Kirchenbauer et al., 2023a)

As a preliminary, we briefly review zero-bit watermarking introduced by Kirchenbauer et al. (2023a) and elaborate on extending this method to multibit watermarking. An auto-regressive language model p(y|x) predicts the probability distribution over the next token $\Delta(\mathcal{V})$ given arbitrary length prefix tokens where \mathcal{V} is the vocabulary. A zero-bit watermark is embedded by biasing the language model to output a certain subset of tokens. That is, the message encoding function $\mathcal{E} : \Delta(\mathcal{V}) \rightarrow \Delta(\mathcal{V})$ generates another probability distribution that alters the original distribution of p(y|x).

For Kirchenbauer et al. (2023a), the message encoding function pseudo-randomly chooses a subset of tokens at each token step t to form a green list \mathcal{G}_t . The logit scores $l_t \in \mathbb{R}^{|\mathcal{V}|}$ are modified towards selecting the green-listed tokens in favor of the other tokens by adding a bias term δ to the logits in \mathcal{G}_t . Instead of fixing the greenlist using rule-based heuristics such as spelling or synonym variations (He et al., 2022), the greenlist is selected pseudo-randomly at each time step to minimize a noticeable shift in text distributions. At each time step, a seed s is outputted depending on the previous h tokens using a pseudo-random function $f: \mathbb{N}^h \to \mathbb{N}$, and s is used to sample \mathcal{G}_t from \mathcal{V} .

We dub this message encoding function as Greenlist. Given t-1 prefix tokens $X_{1:t-1}$, and pseudo-random function f, the t^{th} token is generated by

Greenlist

- 1. Compute hash of tokens $s = f(X_{t-h:t-1})$.
- 2. Permute vocabulary V_t using *s* as seed for a random number generator (RNG).
- 3. Let \mathcal{G}_t be the first $\gamma |\mathcal{V}|$ tokens from \mathcal{V}_t
- 4. Add δ to token logits in \mathcal{G}_t .

To determine the presence of the watermark, the detector inspects the ratio of the green-listed token. A watermarked text will ideally have a high ratio of green tokens as shown in Fig. 1 Right.

3.2 MPAC: Extending to Multi-bit Watermark

The objective of multi-bit watermarking is to embed and extract a message $\mathbf{m} \in \Sigma^b$ where Σ denotes the *r*-nary possible strings, or more commonly referred to as the alphabet. For a binary message, $\Sigma = \{0, 1\}$. We let $p \in \{0, \ldots, b-1\}$ denote the position of the message and $\mathbf{m}[p] \in \{0, \ldots, r-1\}$ the message content at position p. Hereafter, we use [a] to denote the integer set $\{0, \ldots, a-1\}$.

Our proposed method Multi-bit watermarking via Position Allocation (MPAC) works by allocating the tokens to message positions. First, notice that zero-bit watermarking can be viewed as watermarking a single bit of information stating the existence of a watermark (m=0). In essence, each token generated by the language model is a signal that reinforces the watermark.

Our message encoding function $\mathcal{E} : \Sigma^b \times \Delta(\mathcal{V}) \to \Delta(\mathcal{V})$ alters the probability distribution dependent on the message. We first assign a position p using a random number generator seeded with s. Then the message content $m = \mathbf{m}[p] \in [r]$ is encoded by permuting \mathcal{V} and favoring the m^{th}

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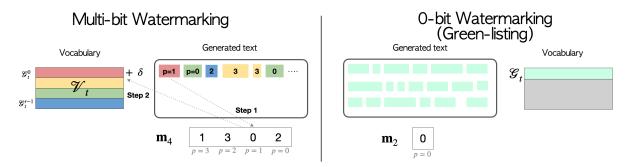


Figure 1: An overview of our method MPAC. The number inside a token (e.g. p = 1) denotes the allocated position, while the color signifies the message content at that position. At Step 1, a position is sampled prior to generating a token. At Step 2, the message at that position determines the token subsets to favor. *Right:* Zero-bit watermarking can be viewed as a special case of multi-bit watermarking.

subset. Our message encoding function is extremely easy to implement over the Greenlist scheme. We highlight the steps in colors that are specific to ours. All other steps are identical to (Kirchenbauer et al., 2023a):

MPAC	
1.	Compute $s = f(X_{t-h:t-1})$.
2.	$p \leftarrow sample([b]) \text{ using } s \text{ as seed.}$
3.	$m \leftarrow \mathbf{m}[p]$
	Permute vocabulary \mathcal{V}_t using s as seed.
5.	Partition $\mathcal{V}_t = [\mathcal{C}_t^0, \cdots, \mathcal{C}_t^{r-1}]$ discarding re-
	mainders if any

6. Add δ to token logits in C_t^m .

Here r is the number of available partitions. The number of vocabulary partitions is determined by the greenlist proportion γ , i.e. $r = \lfloor \frac{1}{\gamma} \rfloor$. When r > 2, we can further increase the load capacity by taking advantage of all the 'colored' lists (hence, the notation C), instead of only using the greenlist. Given a binary message of length b, the message is converted to radix r attaining $\mathbf{m}_r \in [r]^{\tilde{b}}$ where $\tilde{b} = \lceil \frac{b}{\log_2 r} \rceil$. In Figure 1 Left, we illustrate the case of r = 4 and b = 8, where the 8-bit message is converted into radix 4, resulting in an effective message length of 4 $(\tilde{b} = 4)^2$.

At each token generation, the message content at the assigned position p determines which colorlist to add δ to. If the message content is '0', the tokens from the first list (red in Fig. 1) are favored. Note that zero-bit watermarking can be seen as a special case of embedding the same single bit message $(b = 1, \mathbf{m} = 0)$ as shown in Figure 1-Right.

Message Decoding Given a watermarked language model output, we determine the position and which

colorlist each token is from and increment the number of tokens in the colored lists. For instance, for the t^{th} token with message position p = i and the j^{th} colorlist C_t^j , we increment the counter $\mathbf{W}_i[j]$. After computing this on the entire text segment, we predict the message content by taking the colorlist with the most tokens for each position. A more detailed algorithm is shown in Algorithm 1. 297

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3.3 Detecting Machine Text

To distinguish between a watermarked text and a non-watermarked (human-written) text, we count the number of tokens assigned to the predicted message. This corresponds to w in Line 12 of Algorithm 1. We model the number of tokens in the argmax colorlist of position i as a random variable $C_i \stackrel{H_0}{\sim}$ Binomial (T_i, γ) where T_i is the number of tokens assigned to position i. As C_0, \ldots, C_{b-1} are independent for a fixed set of trials (T_i, \ldots, T_{b-1}) and have the same success probability parameter, the sum of these is a binomial random variable as well:

$$C = C_0 + \dots + C_{b-1} \stackrel{H_0}{\sim} \operatorname{Binomial}(T, \gamma) \quad (1)$$

where $T = T_0 + \cdots + T_{b-1}$. This reduces to the same random variable used in zero-bit watermarking and we can compute the z-statistics. More discussions regarding the details of the z-statistic and other possible statistics are outlined in Appendix A.2.

3.4 Comparison to Other Works

The message encoding function of existing works use the entire message **m**. After permuting \mathcal{V}_t , Fernandez et al. (2023a) cyclically shift the vocabulary m_{10} times where m_{10} is the radix-10 form of **m**. This modifies Step 2 of Greenlist. Wang et al. (2023a) hashes **m** to attain a seed s' to permute the

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²Hereafter, we use *b* instead of \tilde{b} to denote the effective message length (dimension of \mathbf{m}_r).

Input: Watermarked text $X_{1:T}$, hash context width h , effective message length \tilde{b} Output: Predicted message $\hat{\mathbf{m}}$, number of colorlisted tokens w							
/* Initialize counter */ 1 $\mathbf{W}_p[m] = 0 \; \forall p, m$ /* Count tokens in colorlists */	/* Predict message */ 9 $\hat{\mathbf{m}}_r =$ " " 10 $w = 0$						
2 for t in $[h + 1, T]$ do 3 $s = f(X_{t-h:t-1})$ 4 $p = \text{sample}([\tilde{b}])$ 5 for m in $[r]$ do 6 Permute \mathcal{V}_t using s as seed 7 lift $X_t \in \mathcal{G}_t^m$ then 8 $\lfloor \mathbf{W}_p[m] += 1$	11 for p in $[\tilde{b}]$ do 12 $w \neq \max(\mathbf{W}_p[m])$ 13 $\hat{m} = \arg\max_m(\mathbf{W}_p[m])$ 14 $\hat{\mathbf{m}}_r \neq \operatorname{str}(\hat{m})$ 15 Get bit message $\hat{\mathbf{m}}$ by converting $\hat{\mathbf{m}}_r$ 16 return $\hat{\mathbf{m}}, w$						

vocabulary along with the seed attained from prefix tokens, modifying Step 1.

Cyclic-Shift

2'. Permute V_t using s as seed. Then, cyclic shift m_{10} times.

Message-Hash

1'. $s' \leftarrow \text{Hash}(s+\text{Hash}(m_{10}))$

Using the entire message leads to two key characteristics that diverge from ours. First, the hamming distance between two messages is not necessarily preserved after applying the encoding function. As an example, consider Message-Hash. Using the final seed s' created from $\mathbf{m} = 0000$ does not guarantee an output from the RNG that is any closer to that of $\mathbf{m} = 0001$ (hamming distance of 1) as it is to $\mathbf{m} = 1111$ (hamming distance of 4). This leads to an all-or-nothing behavior where either the entire message is extracted without error or is a completely random message. In the presence of high corruption, which reflects the real-world case, we show this behavior is not desirable as it lacks enough signal to correctly predict the message.

In addition, the exponential number of messages $(\mathcal{O}(2^b))$ should be considered during message decoding to find the optimal message, which renders decoding of long messages (≥ 32 -bit) computation-heavy³. For Fernandez et al. 2023a, the bit-width affects the *encoding phase* due to the cyclic shift operation, which is more problematic as it affects the end users. MPAC encodes and decodes each bit position of the message independently, which

brings a negligible increase in the computation as the message length is increased.

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The simplicity of our multi-bit watermark scheme via position allocation makes it easy to apply it on top of other methods. For example, using the position allocation scheme, we decompose the multi-bit message into blocks and hierarchically embed them using the message encoding scheme of Fernandez et al. (2023a). Details are in Appendix A.3. In addition, the message encoding function of MPAC can be generalized to other zerobit watermark approaches that uses the exponential minimum sampling approach (Aaronson and Kirchner, 2023; Kuditipudi et al., 2023). The scheme is provided in Appendix A.4.

3.5 Techniques for Practical Use

List decoding is a well-established field in coding theory that decodes a list of messages that are within a certain hamming distance (Elias, 1991; Guruswami and Rudra, 2008; Guruswami, 2004). Inspired by this, we alter our decoding function to output candidate messages sorted by the level of confidence. In practice, list decoding is especially useful because provenance tracing via watermarking is far from finding an exact solution, but narrowing down the possible leakage points for a more detailed inspection that may be costly. For instance, when watermarking the timestamp of activity, it is useful to have a likely set of timestamps for which the practitioners to manually inspect, rather than a single candidate. This technique is not unique to ours and can be applied to other methods as long as the decoding stage is computationally feasible. We detail on how confidence score can be computed in Appendix A.3.

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³See Section 7.5 of Wang et al., 2023a.

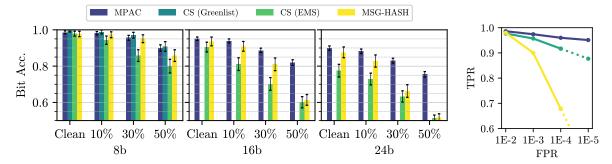


Figure 2: *Left*: Comparison with prior works without corruption (clean) and in the presence of copy-paste attack with p%. On 24-bit, only 100 samples were watermarked for Cyclic-Shift and Message-Hash due to lengthened encoding / decoding time. *Right*: TPR for various FPR thresholds.

4 Experiments

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4.1 Experimental Settings

For our main experiments, we use LLaMA-2-7B (Touvron et al., 2023) to generate sequences using the newslike subset of the Colossal Common Crawl Cleaned corpus (C4) dataset (Raffel et al., 2020) following previous work (Kirchenbauer et al., 2023a). This simulates the scenario of generating fake news given a certain topic. For watermarking and text generation, we follow the configurations used in Kirchenbauer et al. (2023b) unless otherwise denoted: bias $\delta = 2.0$, greenlist ratio $\gamma = 0.25$, which have shown a good trade-off between the detection performance and generation quality. Since $\gamma = 0.25$, the number of colors r is 4. We embed a random b-bit message onto >500 samples and report the mean metrics across samples.

When using the term 'bit' or 'bit-width', this denotes the initial message length and the effective message length is determined by r. When necessary, we also show the three standard error ranges. More details are in Appendix A.5.

Metrics To measure the performance of multi-bit 416 watermarking, we use bit accuracy following previ-417 ous works in the watermarking literature (Zhu et al., 418 2018; Luo et al., 2020; Yang et al., 2022; Yoo et al., 419 2023) to measure how much of the embedded bits 420 can be extracted without error. For zero-bit water-421 mark performance (i.e. machine-text detection), we 422 use area under the ROC curve (AUROC) and the 423 true positive rate (TPR) at various false postive rate 424 thresholds. For text quality, we use the automatic 425 426 metrics used in Kirchenbauer et al. (2023b) such as perplexity (PPL) using a larger oracle model 427 (LLaMA-2-13B) and semantic similarity based on 428 a paraphraser model (Wieting et al., 2022, P-SP). 429 We further discuss the validity of the metrics in 430

Appendix A.6.

Threat Model In the real world, a user often edits the generated text before publishing either to enhance and/or in an attempt to evade the watermark. We study two types of attacks studied in the past work (Kirchenbauer et al., 2023b): *copypaste* mixes the watermarked text and human text and *paraphrasing* uses another language model to paraphrase the watermarked text. For the copypaste attack, we randomly interleave the generated watermarked text into a non-watermarked text, mixing a *p* percentage of non-watermarked texts while maintaining the total length. For paraphrasing, we use GPT-3.5-turbo (the prompt is shown in Table 15). Both attacks do not maintain the start and end tokens of the watermarked text. 431

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4.2 Results

For numerical results, see the tables in Appendix A.10.

Comparison with Other Works. We compare MPAC with Fernandez et al. (2023a, Cyclic-Shift) and Wang et al. (2023a, Message-Hash). We do not compare with other stenography and post-processing works as they are extremely fragile in real-world corruption settings. Please refer to Sec. 2 for details. For Cyclic-Shift, the bit-width is bounded by $\log_2 |\mathcal{V}| \approx 15$ bits, since the cyclic-shift operation is only unique up to the size of the vocabulary. Due to this, we also experiment with extending Cyclic-Shift to another zero-bit watermark method scheme called exponential minimum sampling (Aaronson and Kirchner, 2023, EMS), which does not have a theoretical upperbound. We call this Cyclic-Shift (EMS).

The results in Fig. 2 show the clean and robust multi-bit accuracy in the presence of the copypaste attack. At 8-bit, all methods achieve nearly 100% accuracy and do fairly well even in the pres-

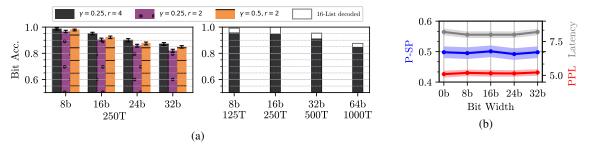


Figure 3: (a) Clean bit accuracy with 3 standard errors for a fixed number of tokens (left) and fixed BPT (right). (b) Text quality (PPL, P-SP) and encoding latency across bit widths. 3 standard errors are shown.

ence of corruption. At higher bit-width, MPAC outperforms others in both clean and robust accuracy. As corruption rate is increased, the other methods show dramatic degradation. In contrast, MPAC can withstand them due to position allocation, which independently encodes each position. In Fig. 2 Right, we compare the watermark detection performance at 8-bit. For Cyclic-Shift and Message-Hash, we use 10,000 negative samples and the TPRs@FPR=1e-5 are linearly interpolated due to the lengthened decoding time. The results demonstrate that MPAC outperforms prior works at low FPR thresholds. Notably, at FPR=1*e*-5, our true positive rate is .951.

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Enlarging the message length comes at the cost of computation for prior works. Increasing the bit-width from 16-bit→24-bit, lengthens the generation time of Cyclic-Shift by roughly 3.6x (14 seconds → 50 seconds) per sample, while MPAC does not have increased latency (Fig. 3b). Message-Hash does not suffer from latency overhead during encoding, but the computation and memory overhead increase exponentially during decoding.

Colorlisting improves multibit performance. Next, we verify the effectiveness of 'colorlisting', which takes advantage of the surplus vocabulary partitions. Fig. 3a demonstrates the gain in the load capacity by using r=4 colorlists as opposed to r=2 given a fixed γ . Besides the 8-bit case, which already achieves high accuracy, the performance of $\gamma = 0.25$, r=4 is statistically significant at p=1e-2 than the second best variant. We further discuss the implications of varying γ , r in Section 5.

Next, we increase the number of tokens (T) and bit width accordingly to demonstrate the feasibility of embedding longer messages. While the performance degrades as we increase the bit-width, the watermark does not entirely break, demonstrating the benefits of decomposing the message by positions. Moreover, the degradation can be partially compensated for by using list decoding. For 32-bit, the best possible message in the list achieves 95% bit acc. by verifying only 16 out of 2^{32} possible messages.

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MPAC can maintain the watermark under various corruptions. The full results of copy-paste attack in Appendix Fig. 10. Even at 32-bit, our watermark is not entirely destroyed as we encode each position of the watermark independently, which shows that it can benefit from error correction codes. We found paraphrasing to be much more challenging than the copy-paste attack and thus, experimented with only 8-bit messages and increasing the token lengths (Fig. 10b). With T=500, the bit accuracy reaches nearly 80% and with 16-list decoding, we are able to attain 90% bit accuracy across all token lengths. More attacks are considered in Appendix A.8.

Detection performance is affected by bit-width. To get a clearer picture of the detection performance, we compute AUC vs. the number of tokens observed in Fig. 4a following Kirchenbauer et al. (2023b). We see that the detection performance decreases as the message bit is increased. This phenomenon is similarly observed in other works as the increase in the number of "hypotheses" required to check leads to an increase in the false positive rate (Fernandez et al., 2023b). We further discuss the reasons behind this in the subsequent section. Note, however, that a watermarked text with 32-bit message reaches AUC over 0.99 once observing 200 tokens (≈ 150 words). The TPR at FPR=1e-3 for $b=\{0, 8, 16, 24, 32\}$ are 0.98, 0.98, 0.95, 0.93, and 0.91, respectively (shown in Table 7).

Text quality is not affected by bit-width. MPAC extends zero-bit watermarking by allocating tokens to message positions and partitioning vocabularies, which would otherwise be allocated to a single position and a single vocabulary partition. Consequently, given the same δ and γ , it only alters

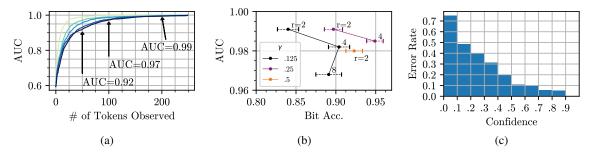


Figure 4: (a) AUC@number of tokens observed for $b=\{0, 8, 16, 24, 32\}$. Darker colors denote larger bit-widths. (b) Zero-bit and multi-bit watermark performance for varying γ and r for 1000 samples at T=100,b=8. (c) Error rate as a function of confidence.

the text distribution to an extent that zero-bit watermarking does regardless of the bit-width. Indeed, our empirical results in Fig. 3b demonstrate that the text quality is statistically indistinguishable across bit-widths. We also show that the encoding latency, which directly experiences user experience, does not increase with bit-width. Three standard error ranges are shown.

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Across Model Scales, Datasets, Hash Schemes. We further experiment with other pretrained models (Jiang et al., 2023; Zhang et al., 2022) and their finetuned versions. Table 6 demonstrates Mistral and OPT also achieve a similar performance, showing that our method is not limited to a specific pretrained model. We also find that the finetuned versions are also capable of watermarking, though the RLHF-tuned LLaMA model show a slight dropoff. The results for larger models (13B, 70B) and other datasets are in Appendix A.9. To summarize, we found that text distributions with low entropy inherently have lower load capacity as observed similarly in prior works. However, our results consistently show that multi-bit watermarking is possible for open-form generation – which resembles disinformation generation – across model types and scales. We also present results for using another hash scheme with a longer context width in Appendix Table 12 and 13, which shows a similar level of performance.

5 Discussions

Load capacity and detection performance tradeoff. As noted above, embedding longer messages degrades the watermark detection performance due to overestimating the statistics of non-watermarked human texts (Fig. 6). This is because computing the statistics involved finding the maximum cell value for each position. One natural solution is to use a better statistic that models the maximum cell value of a multinomial distribution. Empirically, we found that this performed on par or even slightly worse compared to the current approach, which may be due to the approximation error when using a small sample size. We give a more detailed discussion on this in Appendix A.2.

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Radix and Colorlist proportion How do radix and colorlist proportion γ influence multi-bit watermark performance? For γ =.125, the benefits of enlarging r to 8 are saturated and show no statistical significance to r=4. While larger r allows more tokens to be assigned to each position by reducing the effective length of the message, it challenges the problem by increasing the number of possible answers (digits) per position. Additionally, we observed that increasing radix trade-offs zero-bit performance for multi-bit performance. The observations are illustrated in Fig. 4b.

List Decoding Ablation In Fig. 4c, we show a plot of bit error rate stratified by confidence. While not properly calibrated (under-estimation), having higher confidence leads to lower error rate. We also highlight the effectiveness of this technique by comparing it with randomly outputting candidate messages from scratch in Table 2. We also observed that randomly altering a single position provides a good list as the best candidate message is already a good starting point.

6 Conclusion

Our findings demonstrate the viability of embedding any information into the outputs of language models while having the capability to distinguish between machine text and human text. This unveils a novel prospect of counteracting high-stake misuse of large language models via API. One limitation of our approach is the reduced separability of machine and human text when embedding longer messages. Overhauling this limitation can be a major step towards deploying multi-bit watermark in the real world.

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7 Ethics Statement

Watermarking can mitigate malicious use cases by being able to trace back to the malicious user. This will enable holding accountability on adversaries for their malfeasance. However, ordinary users may find the idea discomforting as it may give the sense that the API provider can know what outputs are fed to the individual users. This is not the case unless the content is published to the public by the user, which – in many cases – is already done in an environment where the user can be identified (e.g. social media). All in all, the identification of machine-generated texts and tracing their provenance can enhance the accountability of API access of large language models without breaching individual users' privacy.

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Appendix

Α

11.	Generation	Samples	38	35
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A.1 Decoding Algorithm

Algorithm	2:	Message	Decoding

```
Input: Watermarked text X_{1:T}, hash
              context width h, effective message
             length b
   Output: Predicted message \hat{\mathbf{m}}, number of
                colorlisted tokens w
   /* Initialize counter
1 \mathbf{W}_p[m] = 0 \ \forall p, m
   /* Count tokens in colored lists
                                                            */
2 for t in [h+1,T] do
         s = f(X_{t-h:t-1})
3
        p = \mathsf{sample}([\tilde{b}])
 4
        for m in [r] do
5
              Permute \mathcal{V}_t using s as seed
 6
              if X_t \in \mathcal{G}_t^m then
 7
                   W_{p}[m] += 1
 8
   /* Predict message
                                                            */
9 \hat{\mathbf{m}}_r = "
10 w = 0
11 for p in [b] do
        w += \max(\mathbf{W}_p[m])
12
        \hat{m} = \operatorname{argmax}_m(\mathbf{W}_p[m])
13
        \hat{\mathbf{m}}_r + = \operatorname{str}(\hat{m})
14
15 Get bit message \hat{\mathbf{m}} by converting \hat{\mathbf{m}}_r
```

16 return $\hat{\mathbf{m}}, w$

A.2 Analysis on Watermark Detection

A.2.1 Watermark Detection

The presence of a watermark is determined by counting the number of tokens in the greenlist. For a human-generated text that has no knowledge of the greenlist rule, a token will be from the greenlist with the probability $\gamma \leq 0.5$, the proportion of the greenlist size compared to the entire vocabulary. Without the knowledge of the greenlist (null hypothesis), the number of tokens in the greenlist (g) follows a binomial distribution. (Kirchenbauer et al., 2023a) used the normal approximation to the binomial distribution to compute the z-statistics for a text with T tokens: $z = \frac{g - \gamma T}{\sqrt{\gamma(1-\gamma)T}}$.

Next, we further analyze how bit-width of the message and radix affect detection performance. Our analysis stems from the observation that as we increase the bit-width the detection score for the non-watermarked text increases more rapidly than that of the watermarked text. Consequently,

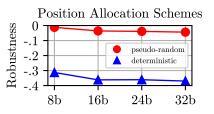


Figure 5: Performance difference between watermark extraction with and without corruption. "Deterministic" denotes sequentially encoding each position of the message as done in Ziegler et al. (2019) in the Greenlist framework. Mixing 20% of non-watermarked text makes the bit accuracy of sequential encoding scheme nearly random.

the difference in the two scores *decreases* as larger bit-width is used, leading to reduced seperability. The results are in Fig. 6. Notice that the difference between the scores of watermarked and nonwatermarked texts decreases for larger bit-width.

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To grasp a hint of what is going on, we do away with the language model and other complexities by modeling this only through statistical distributions. To recap, our detection statistic (Eq. 1) was computed by aggregating the number of tokens in each position of the message. Letting C_i as the number of tokens in the colorlist for the position i, we can write the aggregated form as

$$C = C_0 + \dots + C_{p-1} \stackrel{H_0}{\sim} \operatorname{Binomial}(T, \gamma)$$
 (2)

However, note that during decoding the ground truth message is unknown and thus, is predicted by taking the colorlist that has the max number of tokens. This is problematic when decoding for non-watermarked text as it biases the statistic to be higher when bit-width is increased. We let $W_i = [w_0, \ldots, w_{r-1}]$ be the number of tokens in r colorlists (strength of watermark) for position i. For a non-watermarked text, we can assume that this is a random variable with equal probability for each colorlist

$$W_i \sim \text{Multinomial}(n_i, [\gamma \cdots \gamma])$$
 (3)

where n_i is the number of tokens allocated to position *i*. Our decoding method takes the maximum cell value of this, which makes itself a random variable:

$$W_i^{\max} = \max(W_i) = \max([w_0, \dots, w_{r-1}]).$$
 (4) 93

Our final statistic used for our detection score is

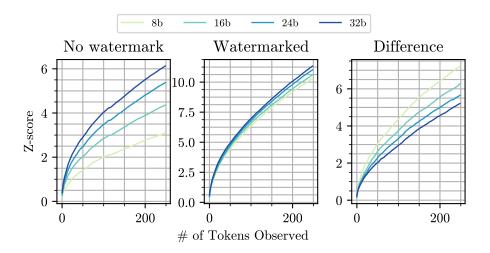


Figure 6: The detection scores of non-watermarked texts, watermarked texts and their difference as a function of number of tokens observed. We see that the difference in the scores decreases as bit-width increases, leading to reduced seperability.

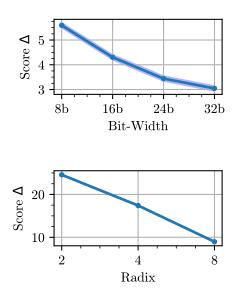


Figure 7: Simulation of the difference between (unormalized) scores for watermarked and non-watermarked multinomial distributions. Higher score signify higher seperability, hence higher detection performance. We use ϵ =0.1. For right, we use γ =.125 to allow more radix.

the sum of this variable over the entire positions:

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$$W^{\max} = \sum_{i}^{p} W_{i}^{\max}$$
 (5)

We see that our statistic is dependent upon the number of candidates when selecting the maximum cell (i.e. radix) through Eq. 4 and the number of positions (i.e. bit-width) through Eq. 5.

To verify the effect of bit-width and radix on the detection score, we compare the difference in the statistics for a uniform multinomial distribution, which signify non-watermarked text, and a multinomial distribution with a slightly modified probability $[\gamma + \epsilon, \gamma, ..., \gamma]$ to signify the added bias term for the watermarked distribution. We sample 1000 samples of W^{max} and compute the difference in the detection scores for the two distributions. The results in Fig. 7 corroborate that an increase in bit-width / radix decreases the separability of the detection scores.

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In an attempt to overhaul this, we tried computing the likelihood of W_i^{rm} before aggregating them using an approximation of (Levin, 1981) (More details in the next section). However, this only led to on par or slightly worse performance. This may be because n_i is small for cases when T is small compared to the length of the message. Other than this, some of the approaches we attempted were:

- Computing test statistic per position or weighting the statistic of each position with n_i before aggregating.
- Computing the p-value of the binomial random variables rather than using the normal approximation, i.e. regularized incomplete beta function.
- Computing the p-value under the null hypothesis that the distribution of the colorlists follows a uniform distribution, i.e. Chi-square Goodness of Fit test

All the approaches either led to on-par or slightly worse results.

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A.2.2 Approximating Max Multinomial Cell Distribution

We used the approximation of (Levin, 1981) for modeling the distribution of the maximum cell frequency. For completeness, we present the steps used for the approximation adapted to our case. For a multinomial distribution with sample size Nand probability vectors $[p_0, \ldots, p_{r-1}]$, Let a be the maximum cell value, then the cumulative distribution function of having a maximum value of a can be approximated for any real number s > 0

$$P(a) = \frac{N!}{s^N e^{-s}} \{ \prod_i^{r-1} P(X_i \le a) \} P(W = N)$$

(6) where $X_i \sim \text{Poisson}(sp_i)$ and $W = \sum_i^{r-1} = Y_i \sim \text{Truncated Poisson}(sp_i)$ with range $0, 1, \dots, a$. Following Example 1 of (Levin, 1981), we set s = N and use Stirling's approximation for N!. We also approximate W using the normal approximation to the Poisson distribution.

A.3 List Decoding and Other Techniques

The decomposition of the message into each bit position bounds the computation during decoding to the number of tokens. This allows MPAC to output a list of most likely messages without exhaustively considering all the possible messages. We alter our decoding function to output candidate messages sorted by the level of confidence. Denoting the predicted message for position *i* by \hat{m} , and the observed number of tokens in the colored list (strength of the watermark) by $w = \mathbf{W}_i[\hat{m}]$, the confidence of \hat{m} should be higher if w deviates from the expected mean under the null hypothesis that all colored lists are equally likely to be sampled. We define confidence at position i as $c_i \propto \Pr(W_i^{\max} \leq w | H_0)$ where W_i^{\max} is the maximum cell value of $W_i \stackrel{H_0}{\sim}$ Multinomial $(T_i, [\gamma \cdots \gamma])$ where T_i is the number of tokens assigned to position *i*. The distribution of W_i^{max} is approximated using techniques from Levin (1981) (See Appendix A.2.2).

Our algorithm can be parameterized by the confidence bound on each position:

- Input: Best prediction $\hat{\mathbf{m}}$ found by majority voting via Alg. 1, confidence bound c_0
- Output: m̂₁, · · · , m̂_{|L|} ∈ L whose predictions are altered on positions with confidence under c₀

Bit Accuracy						
δ	0.5	1	2			
No feedback	.626	.766	.948			
$\tilde{\delta} = \delta + 1$.769	.860	.960			

Table 1: Results for using feedback for adapting bias on T=100,b=8

Accuracy Gained 8b 16b 24b 32b								
c_i -sorted lis Random lis					.6% .3%			
Latency (seconds/250 tokens) 0b 8b 16b 24b 32b								
Encoding (7.9) Decoding (.09)	8.19 .08	7.98 .09	8.01 .09	7.96 .09	8.24 .10			

Table 2: Comparison of absolute improvement in bit accuracy when using confidence-based list decoding and random list.

Empirically, we determine c_0 by constraining $|\mathbb{L}|$. Note that since $\hat{\mathbf{m}}$ is always the most confident message, we comprise \mathbb{L} with the next confident messages. To do this, we greedily alter the positions with the lowest confidence to the colorlist with the second largest number of tokens. Note that this list decoding technique is not unique to ours and can be applied to other methods as long as the decoding stage is computationally feasible.

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A.3.1 Results

We show absolute accuracy gained using confidence-based list decoding (|L|=16) compared with random decoding. We further compare the encoding and decoding latency for sequences with ~ 250 tokens using a single Nvidia A100 when using an additive left hash scheme with context width 1. The results are in Table 2.The latency *does not* proportionally increase with message bit length, making it scalable to long messages. When using an efficient hashing scheme watermarking has a negligible increase in both encoding and decoding compared to vanilla generation, which requires 7.9 seconds and 0.09 seconds, respectively.

A.3.2 Message Correction with Feedback

One key characteristic of our p(y|x) is that we can instantly check whether the message was correctly transmitted by examining whether the sampled token is in the correct colorlist. This property resembles the settings of error correcting codes with feedback, in which the receiver can send feedback to 1054

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the sender after receiving the message(Berlekamp, 1964; Gupta et al., 2023). One can take advantage of this property by adapting the magnitude of the bias during encoding when the majority vote of a given position differs from the actual message.

We provide some preliminary results of taking advantage of feedback during message encoding. One simple scheme is adapting the magnitude of the bias so that when the message is not correctly encoded, we enlarge the bias. Concretely, for $0 \le t \le T$ that is allocated to position p, if the current max colorlist does not match the actual message content, i.e. $\mathbf{m}[p] \ne \operatorname{argmax}_{j} \mathbf{W}[j]$, we use a larger bias $\delta > \delta$. The results in Table 1 show that all lead to an increase in the multi-bit accuracy. However, we observed this came with a degradation in text quality measured by automatic metrics. We leave finding better methodology as a future work.

A.4 Extending MPAC to other methods

Block Allocation Instead of allocating a single position as done in MPAC, we can allocate a block of message, after which techniques of Cyclic-Shift can be used to encode the block message. This ensemble approach enables the prior works to embed longer messages. Deriving it name from Position Allocation, we dub this as Block Allocation.

Block Allocation

1. Compute $s = f(X_{t-h:t-1})$.

2. Chunk message in *n* blocks. $[\mathbf{m}_1, \ldots, \mathbf{m}_n]$ where $\mathbf{m}_n \in \Sigma^{\frac{b}{n}}$

3. $p \leftarrow \mathsf{sample}([n])$ using s as seed.

4. Run Cyclic-Shift with message as \mathbf{m}_p

At decoding, we predict the message for each block and concatenate them. As a preliminary experiment, we use Block Allocation with Cyclic-Shift using n=4 blocks. Block Allocation can embed 24-bit messages with .901 bit accuracy (c.f. Cyclic-Shift achieves .775) and 32-bit with .871 accuracy.

Extension to Other Zero-bit Watermarking Aaronson and Kirchner (2023) is another line of work in zero bit watermarking that modifies the sampling process by generating a secret vector $\mathbf{r} \in [0, 1]^{|\mathcal{V}|}$ based on the random seed *s*. Given the original probability distribution $\mathbf{p}^{|\mathcal{V}|}$, the token with both large p_v and \mathbf{r}_v is favored by choosing

$$x = \operatorname{argmax}_{v \in \mathcal{V}} \mathbf{r}_v^{1/\mathbf{p}_v}.$$
 (7)

We can adapt our position allocation method to this as well by preceding the above step with position allocation. Then, the secret key can be modified depending on the message content by the following rule:

$$\mathbf{r} = \begin{cases} \mathbf{r} & \text{if } \mathbf{m}[p] = 0\\ \mathbf{1} - \mathbf{r} & \text{if } \mathbf{m}[p] = 1 \end{cases}$$
(8)

where 1 is a vector with 1 in all the elements. Analogous to favoring mutually exclusive colorlists, this allows favoring different tokens depending on the message content. At decoding time, we can similarly maintain a counter for each position for the two cases.

A.5 Implementation, Hardware, Code Details

We follow (Kirchenbauer et al., 2023a) in most experimental settings. For the hashing scheme in the main paper, we use LeftHash scheme with context window h = 1. In the appendix, we provide results for the SelfHash scheme. For further discussions regarding the hash scheme see Appendix A.7. To generate sequences with the desired token length T, we generate with the max token set as T. Then we filter out the watermarked and non-watermarked sequences with token lengths under $T_{\text{low}} = T - \tau$. We set $\tau=25$, except for the LFOA dataset, which was set to τ =50 as it has instructions that state to generate answers with 200-300 words. For generation, we use sampling with a temperature of 0.7. For each bit-width, a new set of generations had to be made as the length of the message differed.

For the copy-paste attack, we sample a random non-watermarked text and truncate to have the same length. Then, a position is randomly sampled to insert a p percentage of the watermarked text into the non-watermarked text. We experiment with varying degrees of p (10%~ 50%).

We used float16 for all our models during generation. Our experiment was run on a single NVIDIA A100. For T=250, generating around 500 watermarked and non-watermarked samples took approximately 200 minutes for the left hash scheme. When using the self-hash scheme, this took significantly longer (~ 550 minutes). Our implementation is based on the official codebase of (Kirchenbauer et al., 2023a): https://github. com/jwkirchenbauer/lm-watermarking. We will be releasing our code to reproduce our experiments.

For baselines, we use the official repository of

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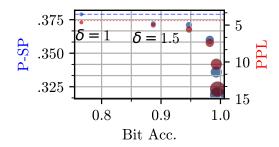


Figure 8: Text quality vs. δ across bias@T=100,b=8

Fernandez et al. $(2023a)^4$ and $(Wang et al., 2023a)^5$. 1145 For Message-Hash, following the same configura-1146 tion presented in their work (GPT-2 as the proxy 1147 model) cannot watermark the outputs of LLaMA-1148 based models due to the difference in the tokeniz-1149 ers. Consequently, we resort to the Vanilla Marking 1150 scheme. This makes all the other factors equiva-1151 lent for the three methods (MPAC, Message-Hash, 1152 Cyclic-Shift) except the message encoding func-1153 tion \mathcal{E} described in §3. Besides, we believe this has 1154 little to no effect on the watermark performance, 1155 since the use of proxy model is intended to enhance 1156 the quality of the text (in terms of perplexity) rather 1157 than the strength of the watermark. 1158

1159 A.6 Metrics: Bit Accuracy, Text Quality

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Text Quality Metrics Using P-SP, we measure the semantic similarity between the human text and watermarked text given the same prompt. While human evaluation is considered to be the golden label, our main purpose is to show that our multi-bit watermarking does not degrade the quality compared to zero-bit watermarking. Moreover, the effect of watermarking on the text quality compared to no watermarking shows promising results in human evaluations when sufficiently large models are used for open-ended generation by Kirchenbauer et al. 2023b (Appendix A.2 and A.9). Additionally, Fernandez et al. (2023a) also demonstrate that watermarking does not lead to noticeable performance degradation even on benchmarks with non-ambiguous answers such as coding and math especially with sufficiently larger models, albeit at a small bias. We further show in Fig. 8 the trade-off curve between bit accuracy and text quality. The size indicates the magnitude of bias ($\{1, \dots, n\}$ 1.52, 3, 4, 5 and horizontal dashed lines indicate

⁵https://github.com/lancopku/ codable-watermarking-for-llm non-watermarked counterparts. Analysis of text quality shows $\delta = 2$ lies at a good trade-off point. Bit Accuracy for Multi-bit Watermark In our experiments, we used bit accuracy (error) as our metric for multi-bit watermark performance. This is a general metric that is independent of the downstream application or the encoding scheme. However, computing the exact match of a message should be done dependent on the context. To illustrate this, we start with some examples. First, consider the case where the encoding scheme to identify users is simply assigning a message to each user. Then, by embedding 4-bit message one can encode 2^4 different users : m='0000' for Bob, m='0001' for Alice, and so on. For such a scenario, one might be interested in computing the exact match of the 4-bit message, also known as the packet error ratio. While this encoding scheme enables tracing back to the exact users at low load capacity, this is extremely inflexible as it cannot handle influx or outflux of users.

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Conversely, one can turn to a more flexible encoding scheme by encoding each character. Using UTF-8, this requires 8 bits per character, which would mean 40 bits is required just for encoding 5 character user ID. For this scenario, one might be more interested in computing the packet error ratio of each character or the entire 40-bit message. A more realistic encoding scheme will be somewhere between the middle, which uses a more efficient representation, e.g. by merging often-used bytes as done in Byte pair encoding (Gage, 1994). Added with error correction codes such as the Reed-Solomon code (Wicker and Bhargava, 1999), this allows a more robust representation. Since focusing on a single type of encoding scheme – and more fundamentally, what information to embed - narrows down the potential applications, we present bit accuracy in our main experiments as done in previous works in the literature (Zhu et al., 2018; Luo et al., 2020; Yang et al., 2022; Yoo et al., 2023; Fernandez et al., 2023b). For T=250, the packet error ratio for the 8-bit message was 7.1%, which is +5.7 % higher than the bit error rate. With 16-list decoding, this is reduced to 2.4%.

Another metric considered in Table III of Fernandez et al. (2023a) was combining the detection scheme and packet error ratio. In this scenario, they assume an encoding scheme of assigning each user to a single message and compute the percentage of finding the exact user given a fixed false positive rate. At FPR= $1e^{-3}$ and using 8-bit message (256

⁴https://github.com/facebookresearch/three_ bricks

Ratio Sampled Position (Sorted)							
LeftHash (<i>h</i> =1) SelfHash (<i>h</i> =4)	0.319	0.251	0.235	0.195			
SelfHash (<i>h</i> =4)	0.264	0.257	0.242	0.238			

Table 3: Ratio of the sampled position for b=8, r=4 (four positions total) for the two hashing schemes for position allocation.

users), we can correctly identify 90.5% cases. Our true positive rate was computed by the setting used in Table 7.

A.7 Discussion on the Hashing Scheme

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The hashing scheme for generating the seed plays a significant role in watermarking. For our MPAC, the hashing scheme is employed once for position allocation and once for permuting the vocabulary list. Here, we discuss some implications of the design choices.

To recap, the function $f(X_{t-h:t-1})$ is used to hash h most recent tokens before generating the tth token. Following the terminology of Kirchenbauer et al. (2023b), LeftHash takes the leftmost token, while SelfHash is determined in a slightly more complex way that is dependent on the tth token (see Algorithm 1 of Kirchenbauer et al. (2023b)). The context width and the hashing scheme determine robustness and quality (diversity) trade-offs. For our experiments, we use the two configurations (LeftHash with h=1 and SelfHash with h=4) proposed in the previous work found to be effective in the two aspects without further fine-tuning.

As expected by the trade-off, the perplexity was slightly higher for LeftHash compared to SelfHash (5.1 vs. 4.9 on average for 250 tokens), while P-SP was at the same level. One clear distinction between the two schemes was the encoding time latency. As SelfHash iteratively searches for tokens, this took significantly longer than the LeftHash scheme, which had nearly no overhead compared to no watermarking (appendix A.5 and Table 2). In addition, we observed that the sampled positions were not uniform for LeftHash with h = 1as shown in Tab. 3 due to the reduced diversity of the tokens in the context width. Despite this, the multi-bit performance was similar for the two schemes (Table 12 and 13). A possible direction for improvement may be using different hashing schemes for position allocation (more robust) and vocabulary partitioning (more quality-focused).

A.8 More on Robustness: Other Attacks, Detection

We also test our watermark against DIPPER (Krishna et al., 2023), which is a specialized paraphrasing model. DIPPER is parameterized by two scalers, which control lexical diversity and token order diversity. We first present the results across bit-width with a lexical diversity of 20 (out of 100). We see that the watermark fares considerably better than using GPT-3 attack in Table 4.

To see the magnitude of semantic drift of the two paraphrasing methods, we compute the P-SP between the original watermarked text and its paraphrased counterpart. We also compute the absolute change in the number of words. Table 5 demonstrates that paraphrasing using GPT-3.5 changes the semantic and the number of words greater than the setting used in Table 4, which may explain why the multi-bit watermark performance is lower for GPT-3.5. When we control the diversity parameters of DIPPER, this is able to degrade the watermark performance as well as GPT-3.5.

Some other forms of possible attacks considered in the literature are word substitution, insertion, and deletion. Word substitution is very similar to the copy-paste attack considered in the main paper. Our watermark scheme is also robust to partial insertion and deletion of words as MPAC relies on the local context to synchronize the positions of the message and the ordering of the vocabulary.

Robustness of zero-bit Watermark Here we provide results for the detection performance under corrptuion. We use the copy-paste attack with the attack percentage ranges of {10%, 20%, 30%, 40%, 50%} and compare the AUC vs. number of tokens observed curve similar to Fig. 9. While the detectability is noticeably affected, the final AUC is recovered to a large degree only after observing 250 tokens. In order of the attack strength, the final AUC's are .992, .987, .980, .971, .942, respectively. For the zero-bit counterpart, all the scores are over .990.

A.9 Ablations on Datasets and Model Sizes

We show additional results on other datasets and
model sizes in Fig. 11. C4 news-like subset1317is the dataset we used for our main experiment.1318"Long-form Question-Answering" (LFQA) is a
dataset curated by Krishna et al. (2023) on the
Reddit's "Explain Like I'm Five" (ELI5) forum.1320The Essays dataset comprises paris of instructions1323

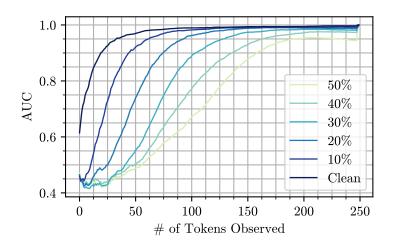


Figure 9: AUC vs. number of tokens observed when corrupted with copy-paste attack for 8-bit message.

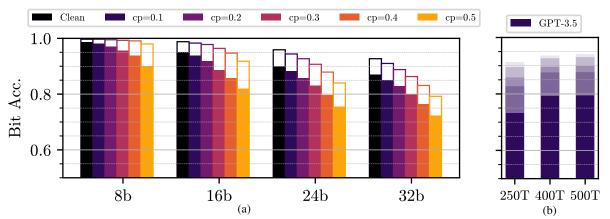


Figure 10: Corrupted bit accuracy for (a) copy-paste attack controlled by the human text percentage at T-250 and (b) paraphrasing attack using GPT-3.5 embedding 8-bit messages at varying token lengths. For (b), we show multiple sizes of list ($|L| \in \{2, 4, 8, 16\}$) by color gradation as 8-bit has relatively small output space.

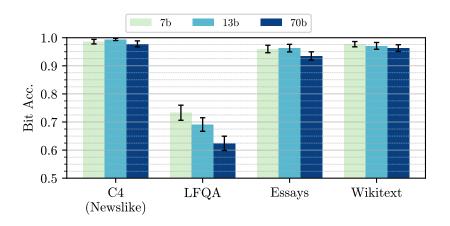


Figure 11: Multi-bit performance across datasets and model sizes.

Bit Acc. after Paraphrasing with DIPPER								
Bit-width	8	16	24	32				
Best Prediction	.922 (.13)	.825 (.12)	.778 (.12)	.736 (.10)				
16-List Decoded	.982 (.05)	.924 (.08)	.864 (.10)	.801 (.09)				

Table 4: Robustness under paraphrasing using DIPPER (Lexical diveristy=20)

		DIPPER			
	GPT-3.5	Lex.=20	Lex.=40	Lex.=60	Lex.=60 Ordering=60
P-SP	.815	.933	.897	.844	.827
Absolute Change in $\#$ of Words	36	13	16	19	20
Bit Acc.	.733	.922	.849	.757	.719

Table 5: Comparison of the two paraphrasing method on text quality.

Model	Bit Acc.
LLaMA-2-7b	.986 (.06)
+ Chat	.922 (.13)
Mistral-7b	.987 (.06)
+ Chat	.977 (.08)
OPT-1.3b	.982 (.07)

Table 6: Performance on other pretrained models and their SFT and RLHF variants (*Llama-2-7b-chat-hf* and *Mistral-7B-Instruct-v0.1*). Results on *b*=8, *T*=250.

and essays (Schuhmann, 2022). Wikitext (Merity et al., 2016) comprises Wikipedia article. We use the 'wikitext-2' subset. For LFQA, we use the finetuned version, LLaMA-2-Chat, specialized for chats as they explicitly have questions or instructions as prompts.

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It is apparent that the watermark performance is affected by the text distribution. When the entropy of the vocabulary distribution is low (low diversity), there is little room for encoding the message with a fixed bias, which has been observed in zero-bit watermarking as well where the watermark performance suffers for low entropy text distributions such as coding (Lee et al., 2023; Kirchenbauer et al., 2023b). For our multi-bit case, this means the load capacity is inherently low for such text distributions. This is especially observed for LFQA, in which the model consistently starts the response by restating the question (e.g. "The reason for [Ques*tion] is* ... "). Across the model scale, the trend is not as apparent although we found that the largest model consistently has a lower performance. This hints that the entropy of the vocabulary distribu-

True Positive Rate								
Bit-width	0	8	16	24	32			
$FPR=1e^{-2}$	0.999	0.986	0.974	0.964	0.958			
$FPR=1e^{-3}$	0.997	0.974	0.956	0.943	0.915			
$FPR=1e^{-4}$	0.997	0.96	0.934	0.905	0.88			
$FPR=1e^{-5}$	0.994	0.951	0.907	0.851	0.793			

Table 7: True positive rate at a fixed false positive rate across bit-widths. We use ~ 500 positive sample and $\sim 100,000$ negative samples. We only count the unique tokens following (Kirchenbauer et al., 2023a; Fernandez et al., 2023a). This has an effect of removing outlier human text samples that have exceptionally high scores.

tion is lower for the largest model, which might explain the higher text quality in general when we increase the model size. Larger models might have the capacity to form high-quality sequences even when the text distribution is altered by increasing the entropy via temperature or explicitly increasing the magnitude of the bias during watermarking. We leave this as a future work.

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A.10 Tabular Results

Here we present the numerical results of the experiments done in the main paper. Numbers in the parenthesis signify the standard deviation.

- Table 8 and 9 ↔ Figure 2 show the comparisons with baseline methods.
- Table 10 ↔ Figure 8 show the relationship between δ vs. text quality and watermark strength.
- Table 11 ↔ Figure 3 left compare the different
 configurations of radix and colorlist proportion.

1367	• Table 12 ↔ Figure 3 left show the multibit wa-
1368	termark performance on a fixed token length.
1369 1370 1371	• Table 13 ↔ Figure 3 right show the multibit watermark performance on a fixed load capacity (bits per token).
1372	• Table 14 ↔ Figure 10a show the multibit wa-
1373	termark performance under copy-paste corrup-
1374	tion.
1375	• Table 15 ↔ Figure 10b show the multibit wa-
1376	termark performance under paraphrasing.
1377	A.11 Generation Samples We show below in Table 16 generated samples.

	B=8,T=250			
Copy-Paste (p)	Clean	cp=10%	cp=30%	cp=50%
Ours	.986 (.06)	.981 (.07)	.956 (.10)	.900 (.13)
FCT+EMS	.979 (.10)	.943 (.17)	.858 (.24)	.800 (.28)
FCT+Greenlist	.995 (.05)	.988 (.08)	.970 (.12)	.908 (.20)
CTWL	.977 (.11)	.973 (.12)	.951(.16)	.858(.24)

Table 8: Comparison of multibit watermark performance with other methods on clean and corrupted settings. For corruption, we use the copy-paste attack. *The load capacity of FCT+Greenlist is limited to 15-bit.

	B=16,T=250			B=24,T=250				
Copy-Paste (p)	Clean	cp=10%	cp=30%	cp=50%	Clean	cp=10%	cp=30%	cp=50%
Ours	.951 (.07)	.939 (.08)	.887 (.09)	.819 (.12)	.899 (.09)	.882 (.09)	.830 (.10)	.755 (.11)
FCT+EMS	.905 (.20)	.811 (.26)	.702 (.26)	.601 (.23)	.775 (.26)	.729 (.24)	.633 (.23)	.513 (.13)
CTWL	936 (.18)	.909 (.20)	.810 (.26)	.614 (.22)	.876 (.22)	.828 (.25)	.663 (.26)	.516 (16)

Table 9: Comparison of multibit watermark performance with other methods on clean and corrupted settings.

δ	0.5	1	1.5	2	3	4	5
Bit Acc.	.626 (.19)	.766 (.18)	.887 (.15)	.947 (.11)	.982 (.08)	.993 (.05	.995 (.05)
P-SP (w/ reference)	.385 (.15)	.379 (.15)	.372 (.15)	.371 (.15	.360 (.14)	.336 (.13)	.319 (.13)
P-SP (w/ non-wm.)	.526 (.18)	.460 (.16)	.433 (.15)	.417 (.15)	.388 (.14)	.349 (.14)	.330 (.13)
PPL	4.41 (1.5)	4.64 (1.8)	5.01 (2.0)	5.6 (2.0)	7.41 (2.7)	10.3 (4.1)	13.67 (5.9)

Table 10: Bit accuracy and text quality on embedding 8 bit-width message on T=250 across various magnitudes of bias δ .

Bit Accuracy @ T=250					
Bit	8	16	24	32	
			.900 (.09)	.871 (0.08)	
$\gamma = .25, r = 2$.966 (.07)	.905 (.08)		0.820 (.08)	
$\gamma = .50, r = 2$.978 (.05)	.922 (.07)	.875 (.08)	0.849 (.07)	

Table 11: Multibit watermark performance measured by bit accuracy for varying configurations of colorlist proportion and radix.

Bit Acc. @ T=250						
Bit	8	16	24	32		
LeftHash(h = 1)	.986 (0.06)	.951 (.07)	.900 (.09)	.871 (0.08)		
SelfHash(h = 4)	.976 (.08)	.905 (.08)	.895 (.09)	.862 (.09)		

Table 12: Bit a	ccuracy for two	o different ha	ash schemes t	for a fixed	token length.

Bit Acc. @ BPT=.064						
Т	63	125	250	500	1000	
Bit	4	8	16	32	64	
LeftHash(h = 1)	.961 (.13)	.958 (.09)	.951 (.07)	.913 (.08)	.846 (.09)	
LeftHash $(h = 1)$ SelfHash $(h = 4)$.952 (.13)	.953 (.10)	.945 (.08)	.911 (.08)	.850 (.08)	

Table 13: Bit accuracy for two different hash schemes for a fixed bits per token.

	Copy-paste Attack						
Attack	Strength	Clean	10%	20%	30%	40%	50%
8-bit	Best	.986 (.06)	.981 (.07)	0.971 (.08)	.956 (.10)	.938 (.12)	.900 (.13)
0-01t	+16-List	.997 (.02)	.997 (.02)	.995 (.03)	.993 (.03)	.991 (.04)	.980 (.05)
16-bit	Best	.951 (.07)	.939 (.08)	.918 (.09)	.887 (.09)	.858 (.11)	.819 (.12)
10-01	+16-List	.988 (0.04)	.983 (.04)	.978 (.05)	.964 (.06)	.947 (.07)	.918 (.08)
24-bit	Best	.899 (.09)	.882 (.09)	.858 (.10)	.830 (.10)	.797 (.11)	.755 (.11)
24-011	+16-List	.959 (.06)	.944 (.06)	.927 (.08)	.907 (.08)	.879 (.09)	.840 (.09)
32-bit	Best	.871 (.08)	.851 (.09)	.828 (.09)	.801 (.09)	.765 (.09)	.723 (.1)
52-0It	+16-List	.927 (.07)	.910 (.08)	.888 (.08)	.863 (.08)	.831 (.09)	.792 (.09)

Table 14: Robustness when certain percentage of human text is mixed into the watermarked text.

GPT-3.5 Paraphrasing					
Token Length 250T 400T 50					
	Best	.733 (.19)	.792 (.19)	.795 (.19)	
	+2-List	.825 (.16)	.874 (.15)	.875 (.15)	
8-bit	+4-List	.856 (.14)	.894 (.13)	.898 (.13)	
	+8-List	.893 (.12)	.924 (.11)	.928 (.11)	
	+16-List	.911 (.10)	.934 (.09)	.939 (.09)	

Prompt

"As an expert copy-editor, please rewrite the following text in your own voice while ensuring that the final output contains the same information as the original text and has roughly the same length. Please paraphrase all sentences and do not omit any crucial details. Additionally, please take care to provide any relevant information about public figures, organizations, or other entities mentioned in the text to avoid any potential misunderstandings or biases."

Table 15: Robustness when paraphrased with GPT-3.5.

Prompt	Non-Watermarked	Watermarked
A blind man in his 60s is searching for the young man who pulled him back from an approaching train and saved his life last Thursday, Nov. 9. Mike Wyatt stood at the stairs to the Peoria train station in Aurora, Colorado, on Monday, looking for the young man who saved his life days earlier	"He told me he was 20 years old and he was going to college," Wyatt told reporters. "He said he was going to be a doctor." Wyatt, who is blind and has been for most of his life, was at the train station ready to catch a train to the airport when he slipped and almost fell in front of an oncoming train.[]	and has given him new life. Inside the station, he spoke to the counter clerk, hoping the clerk might have informa- tion that might lead him to the young man, who jumped at the chance to help Wyatt when he saw he was in danger. But, he said, he found nothing.[]
[] Shortly after the release of the lead single "Life's About to Get Good," it hit number one on the Billboard 200. Of course, fans were simply dying to see how their favourite country icon was doing, so	the album was released on CD, vinyl, and digital. But, Shania took things to the next level and released a deluxe version with added tracks. []	the song was released a few months earlier in June. "OK so I am sooooo proud that my song Life's About to Get Good is now the number one song on Billboard country," she tweeted back in June.[]
[] Amazon's offices will be located within an already-established special tax district where a portion of the prop- erty tax revenue goes toward infrastruc- ture improvements such as parks and wider sidewalks. The incentive agree- ment says that half of any new revenue from that district starting in 202	3 would go to Amazon to help pay for employee benefits and transportation, but the county has said it would not be required to pay those benefits.[]	7 would go to Amazon through a 15- year payment schedule. This amount would grow to more than 60 percent if the company exceeds 10.24 mil- lion square feet of office space. Ama- zon is expected to reach that level in 2027.[]
[] "Below the surface of the Sun a dynamo process is working creating magnetic field," Harra explained in an email interview. "When this becomes buoyant it can rise to the surface of the Sun,	and this is what we call a sunspot." The new research shows that the initial ex- plosion was actually a series of smaller blasts that combined to create the X-7 flare.	and form coronal holes and sunspots. This happens in a fairly homogeneous area on the Sun, so there can be several sunspots with a single magnetic field underneath.
[]The merge listing the most impor- tant changes to Linux 3.8's sound sub- system includes some other changes to audio drivers. The kernel now includes a driver for human interface devices (HIDs) that use I2C (1, 2 and others), using the "HID over I2C" protocol de- signed by Microsoft and implemented in WindowsÂ	7 and later versions of the operat- ing system. The kernel now has a driver for the Samsung Galaxy S III smartphone's touchscreen (1, 2 and others), and the rt2800usb driver, for the RaLink RT2800USB WLAN chip, now supports devices that have Blue- tooth 3.0 (1, 2).[]	7 and Windows Vista. The drivers can read out data from HIDs and set the appropriate commands to them. An ex- ample of such a device is a BT-USB adapter. The sound subsystem now supports two new, high-quality audio codecs (1, 2):[]

Table 16: Randomly sampled examples of watermarked texts on the C4 newslike subset with 100% bit accuracy. Samples are truncated for readability.