QBB: Quantization with Binary Bases for LLMs

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Abstract

Current post-training quantization methods for LLMs compress the weights down to 4-bits, with moderate to low degradation in accuracy. However, further reducing the number of bits or accelerating the network while avoiding large accuracy drops, especially for smaller, sub 7B models, remains an actively researched and open problem. To address this, in this work, we introduce Quantization with Binary Bases (QBB), a new approach for low-bit quantization that effectively removes (nearly) all multiplications, reducing the implementation to summations. Our novel approach works by decomposing the original weights into a set of binary (1-bit) matrices using an iterative process. For a given layer, starting from a weight matrix, we first construct an initial approximation using an analytical solution, where each new binary matrix, paired with a scaling vector, approximates the residual error of the previous estimation. Secondly, using gradient descent and a progressive learning curriculum, we find the optimal set of binary matrices and scaling vectors that minimize the ℓ_2 distance between the produced approximation and original weights. Thirdly, as previous steps are input agnostic, we holistically optimize the scaling vectors alone, calibrating them in student-teacher fashion, with the teacher providing both the data, by autoregressive generation starting from a random token, and the target logits. When evaluated across multiple LLM families, our approach matches and outperforms all prior works, setting a new state-of-the-art result using a summation-only based approach.

1 Introduction

Large Language Models (LLMs) demonstrated proficiency in natural language understanding and generation across multiple domains, exhibiting strong in-context learning abilities [3; 52; 53]. This remarkable performance can be in part attributed to the ever-increasing model and dataset sizes [25; 9], with the current generation of models being trained on Trillion-sized (tokens) datasets [53], using Billions of parameters [53; 24; 29]. This, in turn, made deploying such models, even on consumer-grade GPUs, problematic. A promising and flexible direction that disentangles the training and the deployment process, while being hardware friendly, is given by post-training and/or datafree quantization [16; 32; 48]. Within this area, current methods have successfully achieved $4 \times$ compression (i.e. 4-bit quantization) with small drops in accuracy [16; 7; 32], especially for larger (7B+) models. However, compressing the model further and/or applying said methods to smaller models yields unsatisfactory results [16; 32]. Importantly, on the inference side, this class of PTQ approaches replaces 16b multiplications with mixed-precision (i.e., 16b-4b) ones, which have limited hardware support and rely on software-based solutions. Our aim is to alleviate these limitations, enabling higher compression rates while removing (nearly) all multiplications.

To this end, departing from prior work, we focus on the most extreme case of quantization, that of binarization (which, as we will show, enables us to remove costly multiplications). As binarizing the weights directly, without retraining, results in unsatisfactory performance, we propose to approximate the weights W using a set of binary matrices $\mathbf{B}_i, i \in \{1, ..., N\}$ with corresponding fp16 scaling vectors α_i . The main case of interest studied is that of N = 4. We note that binarising the weights

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is a particularly interesting case as the matrix multiplications can be implemented using masked selection/data loading and summations, removing all the multiplications, but 1, that with the scaling vector.

As binarising the weights directly is suboptimal (see Sec. 4), we introduce a new iterative approach for estimating the optimal binary matrices \mathbf{B}_i and scaling vectors $\boldsymbol{\alpha}_i$: Firstly, for a given weight \mathbf{W} belonging to the *l*-th layer, we construct an initial approximation using an analytical solution, whereby each new additional binary matrix approximates the residual error of the previous estimation(s). Secondly, using gradient descent, we iteratively adjust the binary weights and scaling vectors one by one by minimizing the ℓ_2 norm between the target weights and the produced estimation. As until now the process is agnostic to the input distribution of the data, we plug the approximated weights back into the model, optimizing in the interest of speed and generalizability the scaling vectors only. This step uses a teacher-student approach and does not require any training dataset. Instead, we generate synthetic data starting from random tokens by adapting [38] to be more sample efficient. Note that this bypasses the need for any real data. Our approach matches and outperforms prior 4-bit quantization methods across a wide variety of LLMs models (e.g: LLaMA-2, Phi-2, etc.) while removing all multiplication (except the final one with the scaling vector), being fast to calibrate and being amenable, in certain conditions to higher compression rates (see Sec. 4.6), setting a new state-of-the-art result.

2 Related work

LLMs quantization is a particular application of network quantization [18; 8; 22; 42; 56] to LLMs. As for the former, broadly speaking, these methods can be split into two categories: Quantization-Aware Training (QAT) - which requires retraining or training in quantized form, and Post-Training Quantization (PTQ), which can be applied directly, without additional retraining. As retraining such models, especially without losing generality, is challenging, most of the work focused on PTQ [16; 49; 32; 30], although a recent line of work tackles the latter too using data-free strategies [38] or parameters efficient fine-tuning [14]. One of the most prominent recent lines of work was the introduction of GPTQ [16] that proposes a one-shot low-bit weight quantization method based on approximate second-order information. Follow-up work improves upon it by considering the outliers [27; 13], the effect of the activations on the weight quantization performance [32; 30], by training the quantization parameters [48] or by grouping and reordering the parameters [62]. Methodologically, our approach stands in between PQT and QAT, as we support both layer-wise input agnostic binarization and fast data-free recalibration. In either case, our approach doesn't require a training corpus.

Binarization also known as 1-bit quantization, represents the most extreme case of quantization. In this instance, when both operands are binary, the multiplications can be replaced with bitwise operations, while when one is binary and the other real, the multiplications become summations. These desirable properties make binarization a particularly interesting case of quantization. The current base formulation can be traced to [10; 11], which proposes to binarize the values using the sign function, whose gradient is estimated using a straight-through estimator [2]. Subsequent works primarily focus on training-aware solutions for vision models [46; 33; 34; 5; 4; 15; 58; 64; 63; 26; 6; 40; 35; 61; 45]. For example, Rastegari et al. [46] introduces analytically computed scaling vectors for both the input and the weights, while [4] building on top, proposes to learn them holistically, via backpropagation instead. Liu et al. [34] argues for the use of real-valued down-sampling layers and the use of double skip connections, while [5] replaces ReLU with PReLUs and makes use of two-staged optimization.

Many works have also studied network binarization in the context of transformers [1; 44; 36; 37], focusing on either full retraining or fine-tuning on labeled datasets using mostly smaller models (e.g., BERT, BART). More relevant to our work are the recent attempts to adapt and apply binarization to LLMs [55; 39; 47; 60]. BitNet [55] swaps all linear layers with BitLinear, their 1-bit weight's replacement, which are then trained from scratch. PB-LLM [47] explores the partial binarization of LLMs, in which the salient weights are stored in higher bits, and the rest are binarized, with a fine-tuning step (i.e., a QAT step) to recover the original LLM performance. BitNet b1.58 [39] encodes every weight using three states $\{-1, 0, 1\}$ instead of two, which are then trained from scratch similar to BitNet [55]. Finally, OneBit [60] proposes a 1-bit QAT method that decomposes the weights into 1-bit weights and two full-precision scaling vectors, which are then fine-tuned with a



Figure 1: **Binary weights initialization phase**: starting from the target weight **W**, we construct N binary matrices \mathbf{B}_i and scaling vectors $\boldsymbol{\alpha}_i$ analytically. The 1st binary weight and scaling vector are obtained using Eq. 2 while the subsequent ones use Eq. 3.



Figure 2: Iterative weights binarization: Starting from the weights initialized as shown in Fig. 1, we update the binary weights one-by-one, where at each step $i \in \{1 \dots N\}$, only \mathbf{B}_i is updated by minimizing the loss function in eq. (4), while the rest are frozen. Note that all of the scaling vectors α_i are updated at every step.

distillation loss for a better approximation. However, all these approaches require full retraining or fine-tuning on labeled datasets with a large training overhead. In contrast, our approach is applicable post-training, doesn't require any labeled (nor unlabeled) datasets, is fast to optimize, makes use of multiple binary bases, and scales well to billion-sized models.

3 Method

3.1 Layer-wise input-agnostic weights binarization

Given a linear layer, represented as $f(\mathbf{X}, \mathbf{W}, \mathbf{b}) = \mathbf{X} \cdot \mathbf{W} + \mathbf{b}$, with $\mathbf{X} \in \mathbb{R}^{n \times c_{in}}$ the input tensor, $\mathbf{W} \in \mathbb{R}^{c_{in} \times c_{out}}$ the weight matrix and, optionally, $\mathbf{b} \in \mathbb{R}^{c_{out}}$ the bias term. *n* represents the number of tokens, c_{in} and c_{out} the number of input, and respectively output channels. Note that we are considering the batch size to be 1 and the bias 0 for brevity, as the formulations are independent of them. Our goal is to then quantize the elements of \mathbf{W} with \mathbf{W} such that $\mathbf{X} \cdot \mathbf{W} \approx \mathbf{X} \cdot \mathbf{W}$. Unlike prior works [16; 32] that focus primarily on 3 and 4-bit quantization, herein, we focus on compressing the weights using a set of binary bases, without comprising the model's accuracy and importantly, without requiring any training or calibration dataset(s), enabling in the process a potential implementation based (nearly) solely on summations.

For our purposes, let us consider the most extreme case of quantization, that of binarization, whereby the values are represented using 1-bit. In this instance, the real-valued weights \mathbf{W} can be approximated as $\mathbf{W} \approx \widetilde{\mathbf{W}} = \alpha \mathbf{B}$, where $\mathbf{B} = \mathtt{sign}(\mathbf{W})$ is a binary matrix and $\alpha \in \mathbb{R}^{c_{out}}_+$ a scaling vector. Given a set of real-valued weights that are binarized, following Rastegari et al. [46], the optimal value for α can be computed analytically as $\alpha = \frac{1}{c_{out}} \|\mathbf{W}\|_{\ell_1, \mathrm{col}}$ with $\|\mathbf{W}\|_{\ell_1, \mathrm{col}}$ as the ℓ_1 -norm computed over the columns of \mathbf{W} . Note, that in order to avoid spurious states (i.e. states at which the function

is ill-defined - 0), the sign function used is defined as: $\mathtt{sign}(x) = \begin{cases} -1, & x < 0 \\ 1, & x \geq 0 \end{cases}$

In essence, this relation tells us that we can find the optimal values for **B** and α by solely looking at **W**, i.e. without requiring any training data. The downside is that the quantization errors are very high due to reduced representation power, which completely degrades the model's performance. This is perhaps not surprising, as the number of representable states for one given value drops from 2¹⁶ for 16-bits to 2⁴ for 4 bits and, finally, 2¹ for the binary case. This discrepancy is even more noticeable when considering the total number of unique permutations representable on such a weight matrix.

To address this, we propose to represent $\widetilde{\mathbf{W}}$ with a linear combination of N binary matrices:

$$\widetilde{\mathbf{W}} = \sum_{i=1}^{N} \alpha_i \mathbf{B}_i \tag{1}$$

In this case, finding the optimal values for α_i , \mathbf{B}_i , $i \in \{1, ..., N\}$ can no longer be achieved using the analytical solution of Rastegari et al. [46]. As such, we propose a new iterative optimization approach in which the weights and the scaling vectors are iteratively learned via gradient descent. The exact optimization process requires, however, careful considerations. The gradients of sign(.) are 0 almost everywhere, taking the form of the Dirac Delta function. Hence, to make training possible, in practice they are approximated using a straight-through estimator [2] taking the form of a clipped identity function [46; 11]. These gradients are however noisy with the training prone to oscillations and instabilities: for a value infinitesimally close to 0, there exists a full state transition to either of the extremes, i.e. -1 or +1, for any non-zero gradient, hence any noise, even a machine representation error, can result in large swings. To alleviate this, we study (i) how to initialize the weights and the scales, and (ii) how to stabilize the optimization process.

Weights and scale initialization: Given an initial estimation $\alpha_1 B_1$ computed analytically by directly approximating the weight matrix W as:

$$\mathbf{B}_{1} = \operatorname{sign}(\mathbf{W}), \boldsymbol{\alpha}_{1} = \frac{1}{c_{out}} \left\| \boldsymbol{W} \right\|_{\ell_{1}, \operatorname{col}},$$
(2)

we then initialize the subsequent $\alpha_i, \mathbf{B}_i, i \in \{2...N\}$ values by approximating the residual error Δ_i at step *i*:

$$\mathbf{B}_{i} = \operatorname{sign}(\mathbf{\Delta}_{i}), \boldsymbol{\alpha}_{i} = \frac{1}{c_{out}} \left\| \mathbf{\Delta}_{i} \right\|_{\ell_{1}, \operatorname{col}}, \quad \mathbf{\Delta}_{i} = \mathbf{W} - \sum_{j=1}^{i-1} \boldsymbol{\alpha}_{j} \mathbf{B}_{j}.$$
(3)

This sets the underlying distribution behind each \mathbf{B}_i matrix to the direction that would minimize the overall quantization error. See Fig. 1 for an illustration.

Iterative weights and scales optimization: Starting from the above initialization, we aim to minimize the following loss function:

$$\mathcal{L}_2 = \|\mathbf{W} - \sum_{i=1}^N \boldsymbol{\alpha}_i \mathbf{B}_i\|_2^2, \tag{4}$$

where both α_i and \mathbf{B}_i are trainable parameters, with \mathbf{B}_i maintained in the binary state using the sign function. However, the direct, *naïve* approach of optimizing all parameters jointly leads to training instability. To alleviate this, we devise an iterative training procedure, akin to block coordinate descent, in which the weights are trained one-by-one. Specifically, and as shown in Fig. 2, for Nbinary matrices, we have N training steps. During each training step, only one binary weight is updated, while the rest stay frozen. We note, however, that the scales are trained in all cases. This approach prevents us from concomitantly changing too many binary weights, effectively simplifying the problem at each step to learning a binary correction factor to an existing approximation.

Progressive weights quantization: To further simplify the approximation of full-precision weights using binary bases, we follow previous binarization approaches [5; 40] and progressively reduce the gap between full-precision and binary weights. Specifically, instead of directly approximating full-precision weights, we first quantize them to a lower precision using an off-the-shelf method (e.g., 4-bit using GPTQ). Then, we apply the proposed method with these quantized weights as a starting point (i.e. initialization followed by iterative optimization).

3.2 Data-free holistic binarization

Until now, our binarization process was input-agnostic, considering only the to-be-binarized weights W on a per-layer basis. However, this does not factor two important aspects: (1) the effect of cumulative errors resulted from imperfect approximations of the previous layer's weights and (2) the effect on the overall model's output objectives, given that a local approximation isn't necessarily the optimal global solution under quantization induced errors.

To maintain the generalization properties of the target LLM, instead of making use of downstream datasets, we generate synthetic data using the (full-precision) model itself, following Liu et al. [38]. Specifically, the 1st token is randomly selected, with the model generating the subsequent ones up to a certain length or until the EOS token is encountered. Note that the next token is selected stochastically to increase the diversity of the output sequences.

Once the data is generated, we can directly use it to train the model with the standard next-token CE loss. However, as the synthetic data is noisy, forcing these labels into the quantized model is suboptimal. Instead, we directly use the produced logits p^{T} as soft ground truth, effectively performing Knowledge Distillation [20]. In practice, we use the MSE loss between the student (quantized model) and teacher (full precision model) logits, which is analogous to a cross-entropy based distillation at high-temperature [20]. The loss is defined as:

$$\mathcal{L}_{\text{MSE}} = \sum_{v=1}^{V} \sum_{i=1}^{n} \| p_{i,v}^{\mathcal{T}} - p_{i,v}^{\mathcal{S}} \|_{2}^{2},$$
(5)

where V represents the size of the vocabulary and n the number of tokens.

By inspecting the per-layer quantization (Sec. 3.1), we notice that different layers within different regions of the model have different quantization errors that are sometimes different by up to an order of magnitude. Hence, training them only with a signal applied at the very end of the model is suboptimal. Thus, we also apply a layer-wise MSE loss between the corresponding features of the teacher and student and the end of every transformer block:

$$\mathcal{L}_{\text{feat}} = \sum_{l=1}^{L} \sum_{i=1}^{n} \|f_{i,l}^{\mathcal{T}} - f_{i,l}^{\mathcal{S}}\|_{2}^{2}, \tag{6}$$

where $f_{i,l}^{\mathcal{T}}$ and $f_{i,l}^{\mathcal{S}}$ are the features after the *l*-th transformer module of the *i*-th token produced by the teacher, and respectively student (quantized) model.

The overall loss is then computed as:

$$\mathcal{L}_{\text{distill}} = s_1 \mathcal{L}_{\text{MSE}} + s_2 \mathcal{L}_{\text{feat}},\tag{7}$$

with s_1 and s_2 scaling factors for balancing the two loss terms.

It's generally accepted that higher accuracy gaps between the student-teacher pair hinder the learning process, as the student has a difficult job of matching the teacher's output. To alleviate this, herein, we randomly swap parts of the teacher model with blocks from the student model. Effectively, this creates an instant family of models, with a performance situated between that of student and teacher models. The sampling is varied, with increasing difficulty (i.e. fewer blocks swapped) as the training progresses.

Efficient Calibration: To improve the efficiency of our calibration process, firstly, we only fine-tune the scaling vectors α_i making the training process compute and time efficient, keeping everything else, including the binary weights \mathbf{B}_i , frozen. Secondly, to speed up the training further and make it more sample-efficient, we propose a simple filtering step of the generated training data. Specifically, we only train on self-generated sequences where the quantized student and full-precision teacher differ the most, instead of directly using all the generated samples as in Liu et al. [38]. This is done by first scoring the generated sequences using Eq. 5, then keeping the top-*K* samples with the highest student-teacher discrepancy. This reduces the training time without any impact on the final results.

4 Ablation studies and analysis

4.1 Impact of the proposed components

Method	Phi-2 (2.7B)	LLaMA-2 (7B)
without Sec. 3.1 & 3.2	N/A	N/A
+ Sec. 3.1	12.32	5.37
+ Sec. 3.2	10.48	5.21

Table 1: **Impact of the main components** measured for a Phi-2 (2.7B) and LLaMA-2 (7B) model in terms of perplexity on WikiText2. N/A - indicates failure (> 10^5 perplexity).

In this section, we showcase the importance of each proposed component, focusing in particular on what it takes to make the binarization stable. For a breakdown of the KD subcomponents, see Sec. 4.3. As the results from Tab. 1 show, both proposed components, i.e. Layer-wise input agnostic weights binarization (Sec. 3.1) and Data-free holistic distillation (Sec. 3.2) improve the model's accuracy and are critical for achieving convergence. Notably, the data-free calibration is particularly important for smaller models, which are generally harder to quantize.

Moreover, to validate that binarization is inherently unstable, we first ablate the initialization step. In Fig. 3 we plot, on a layer-by-layer basis, the ℓ_2 quantization error for different weight initialization strategies: random initialization - the



Figure 3: Per-layer reconstruction error for a Phi-2 model when varying the initialization used: random, without the cascaded (residual) init, and with.

weights are sampled from a normal distribution; w/o cascaded initialization - all weights attempt to minimize the global error at initialization; with cascaded initialization - each weight approximates the remaining residual error (Eqs. 2 and 3). We can immediately observe that random initialization results in errors that are an order of magnitude higher. Furthermore, the proposed cascaded initialization results in reconstruction errors that are on average $2 \times$ smaller than the direct alternative, that minimizes the global error instead of the residual one, as proposed in our work. Interestingly, there are a few layers (the ones harder to quantize) for which the two are behaving similarly. Such layers tend to have more outliers, which makes the finding of the optimal solution (that minimizes the average reconstruction error), more prone to local minimums.

4.2 Binary weights and process analysis

To offer some insights on the binarization process, in Fig. 4 we show the proportion of the weights that change state between initialization and the end of the iterative training process, on a per-layer basis, for each binary base. Interestingly, the first and last binary matrix undergo minimal changes, with typically only 0.01 - 0.2% of the weights transitioning to a different state. In comparison, the second, and particularly the third base change approximately 40% and respectively 50% of their bases. Moreover, we can observe that for layer IDs 6 and 8, while the proportion of transitions decreases for the second one, the amount increases for the third, which appears to compensate in order to maintain the same overall proportion of bit flips when aggregated across all bases. These phenomena can be tied to how the initialization is performed: the first binary matrix directly approximates the



Figure 4: Proportion of binary weights that changed their state (bit flips) after applying the proposed iterative training process, shown for the first 20 layers of a Phi-2 model for all 4 bases.

full precision weights \mathbf{W} , hence it is already close to its optimal solution while the last one has to approximates a relatively small residual error, as 3 bases give relative similar results (see Fig. 6).

4.3 Effect of distillation

Knowledge Distillation [20] was shown to improve the performance of smaller models by the virtue of providing guidance either at the feature level [19] or at the output space, by providing (soft) pseudo-labels. Herein, we ablate various design choices, summarizing the results in Tab. 2. In particular, we consider the following options: (1) CE - using directly the synthetic data as hard labels and then calibrating the model using the standard next token prediction Cross-Entropy Loss; (2) KD - Using the soft probabilities provided by the teacher, this is identical to standard Knowledge Distillation [20]; (3) KD-MSE - Compute a ℓ_2 (MSE) loss between the logits of the student and teacher; (4) KD-MSE with swap - gradually vary the strength of teacher, from weaker to stronger, by randomly swapping some block in the teacher model with ones from the student and then apply the KD-MSE loss. Note that the per-layer feature loss (eq. 6) is used for all cases except (1) CE, i.e. when the teacher model is not utilised. As the results show, the KD-MSE with swap outperforms all other variants. Moreover, for this use case, the KD-MSE variant outperforms the vanilla KD loss.

Table 2: Effect of different Knowledge Distillation strategies measured using a Phi-2 (2.7B) model in terms of perplexity on WikiText2.

CE	KD	KD-MSE	KD-MSE with swap
11.82	10.61	10.48	10.40

4.4 Effect of data filtering

During the calibration step, in order to make the training more sample efficient, we proposed to filter the randomly self-generated data and only keep the sequences with the highest teacherstudent discrepancy as measured by the MSE between their output logits (i.e. Eq. 5). As shown in Fig. 5, this simple filtering step results in faster convergence for the same amount of training samples (i.e. lower perplexity) compared to directly training on the randomly generated sequences.

4.5 How many binary bases should we use?

Throughout this work, we mainly focus on the N = 4 case as it provides an optimal balance between accuracy, compute cost and storage. For clarity and completeness, herein, we explore how the performance varies for different values of N. As a study case, we take the Phi-2 (2.7B)model and plot the initial reconstruction errors, after applying the method described in Sec. 3.1. We do so on a layer-by-layer basis, as this will also reveal wherever certain layers are harder to quantize. Looking at the results shown in Fig. 6we can make the following observations: (1) There is a notable performance drop and phase transition for $N \leq 2$; (2) Perhaps unsurprisingly, not all layers are made equal, with different layers having different approximation errors, and hence exhibiting variable difficulty levels from



Figure 5: The PPL on WikiText-2 with Phi-2 (2.7b) trained on a variable number of training samples. Here, we compare the performance when using the generated data directly, or when filtering is applied.



Figure 6: Per-layer reconstruction error after the initial layer-by-layer optimization for a Phi-2 model. Notice that the performance is generally stable for $N \ge 3$.

a quantization point of view; This could be indicative for future quantization efforts; (3) For the layers located in the middle, a pattern emerges, with every block being (nearly) equally hard/easy to quantize. This aligns well with the idea that transformers learn a similar representation across most of their layers, unlike, let's say, a convolutional model; (4) For N = 5, we can observe improvements, especially for the most difficult layers, while the easier one has a similar value as for N = 4.

4.5.1 Effect of iterative optimisation

Herein, we measure the impact of the proposed iterative training strategy presented in Sec. 3.1. As the results from Fig. 7 updating all weights jointly leads to significantly worse results, leading to an average error that is one order of magnitude higher.

4.5.2 Effect of progressive weights quantization

In line with prior work on binarization [40], we aim to gradually increase the quantization level, as this simplifies the problem by reducing the apparent difficulty of the target. To this end, in Tab. 3 we measure the impact of progressive quantization and showcase that our approach is amenable to different quantization targets. On one hand, we can observe that attempting to directly quantize the fp16 weights results in de-



Figure 7: Per-layer reconstruction error after the initial layer-by-layer optimization for a Phi-2 model. Notice that the performance is generally stable for $N \ge 3$.

graded performance, on the other, our approach works with target weights produced by different approaches, in this case: QPTQ and OmniQuant. Moreover, we can observe that better int4 weights also translate in better binary bases, with our method incorporating the improved scale and outlier handling from OmniQuant for example.

Table 3: Effect of progressive weight quantization strategies measured using a LLama-2 (7B) model in terms of perplexity on WikiText2.

	FP16	GPTQ	OmniQuant
Starting perf:	5.12	5.61	5.58
Ours:	7.10	5.49	5.21

4.6 Discussion on efficiency

Current low-bit post-training quantization methods result in implementations that replace the full/half precision multiplications present within a linear layer with ones performed using operators represented on fewer bits, most frequently 16b-4b (activation-weights). When the number of bits for at least one of the operands drops to the most extreme case, i.e., 1-bit, all these multiplications are removed. Depending on the implementation, they become either a masked selection $\{0, 1\}$ or a conditional sign set $(\{-1,1\})$. Herein, we opt in for the former, as depending on the target hardware, it is possible to reduce the number of summations too, by implementing a masked load, given that the binary matrices generally have a sparsity level between 50-80%. Getting back to the core message, by removing all the multiplications inside the linear layer, except for the final one with the scaling vector, the power consumption could be reduced, and on custom hardware, it could translate into a smaller die size and faster execution [51; 50; 31; 57], as in principle an adder circuit can be implemented using a flip-flop. While different implementation and technological nodes will result in some variations, taking as an example [21], on a 45nm node, and depending on the bit-width of the activation, an adder consumes $4 - 8 \times$ less energy compared with a multiplier. While left for future studies, further decreasing the activations too to 1-bit can enable even faster implementations based solely on bit-wise operations [4; 10]. Memory-wise, as we learn a sum of binary bases, certain implementations, although not trivial to construct, can exploit either a left-most significant bit alignment to compress

the weights to $\log_2(N + 1)$ bits, as a sum of N binary matrices results in N + 1 states, or can make use of codebooks given the cross-matrix similarities and sparsity levels. All in all, we highlight that such representation, which removes (nearly) all the multiplications, opens the door to important energy savings, which are especially important in a world where the total energy consumption of AI models is expected to reach 85-135 TWh by 2027 [12] (if current trends follow) - this equates to the entire power consumption of the Netherlands.

5 Results

We compare our approach with the current state-of-the-art for low-bit quantization in terms of perplexity score on the main benchmark for quantization - WikiText2 [41], focusing mainly on the LLaMA-2 [53] {7, 13, 70}B family of models. However, we also include results for LLaMA [52] {7, 13, 30, 65}B and Phi-2 [23] 2.7B models. This allows us to effectively cover a wide range of model architectures and sizes, from the "smaller", and hence harder to quantize, Phi-2 (2.7B parameters) model to the large 70B LLaMA-2 model.

Training details. We implement our method using PyTorch [43], sourcing the pretrained models from Hugging Face [59] repo, as provided by their respective authors. The evaluation code is based on [17]. During the input-agnostic quantization part, presented in Sec. 3.1 and using a single A100 GPU, we optimize each set of binary matrices and scaling vectors, layer by layer, using the following hyperparameters: Adam optimizer [28], 15000 iterations, no weight decay, an initial learning rate of 1e - 4 decayed to 0 using a cosine scheduler. For the data-free distillation step, presented in Sec. 3.2, we fine-tune the scaling vectors only for 2 epochs using an Adam optimizer, a cosine learning rate scheduler, no weights decay, and an initial learning rate set to 2.5e - 4. For added stability, we clip the gradients with a norm higher than 1.

Baselines. For weight-only quantization, we compare with the primary baseline which is the vanilla Round-to-nearest (RTN) quantization, in addition to current state-of-the-art methods for both W4A16 (i.e. weights in 4-bits and activations in 16-bits) and W3A16 quantization. Specifically, we consider GPTQ [16], SpQR [13], QuIP# [54], and OmniQuant [48]. Here, we report the results for both per-channel weight quantization and group-wise weight quantization with a group size of 128 (i.e. denoted as g128).

Outcome. As the results from Tab. 4 show, our approach matches or outperforms prior PTQ approaches across all model sizes.

Broader impact and limitations

As our work removes nearly all multiplications, it could improve the energy efficiency of the current generation of AI models, reducing costs while being more environmentally friendly.

In terms of limitations, our work builds on top of existing pre-trained LLMs, some trained on closed datasets, hence any potential biases present in the original data, affecting the original models would likely propagate to the quantized models too. Therefore, we recommend caution before deploying such models. Moreover, the benefits and gains mentioned are theoretical, as no custom implementation was constructed. Additional effort may be required to translate the theoretical gains into practice.

6 Conclusions

In this work, we introduced Quantization with Binary Bases (QBB), a new approach for low-bit quantization that effectively removes (nearly) all multiplications, reducing the implementation to summations. Our new approach decomposes the original weights into a set of binary matrices and scaling vector(s) using an iterative process, whereby starting from an initial approximation obtained using an analytical solution, each new binary matrix and scaling vector is optimized in a progressive manner using gradient descent by minimizing the ℓ_2 distance between the produced approximation and the original weights. Finally, as the previous steps were input agnostic, the scaling factors are optimized holistically, calibrating them in student-teacher fashion, with the teacher providing both the data, by autoregressive generation starting from a random token, and the target logits. When

Method	Quantization	LLAMA			LLAMA-2			
		7B	13B	30B	70B	7B	13B	70B
FP16	-	5.68	5.09	4.10	3.53	5.12	4.57	3.12
RTN		6.43	5.55	4.57	3.87	6.11	5.20	3.67
GPTQ [16]		6.13	5.40	4.48	3.83	5.83	5.13	3.58
AWQ [32]	W4A16	6.08	5.34	4.39	3.76	6.15	5.12	-
OmniQuant [48]		5.86	5.21	4.25	3.71	5.74	5.02	3.47
QuIP# [54]		5.76	5.17	4.18	3.60	5.56	4.95	3.38
RTN	W4A16g128	5.96	5.25	4.23	3.67	5.72	4.98	3.46
GPTQ [16]		5.85	5.20	4.23	3.65	5.61	4.98	3.42
AWQ [32]		5.81	5.20	4.21	3.62	5.62	4.97	-
OmniQuant [48]		5.77	5.17	4.19	3.62	5.58	4.95	3.40
RTN	W3A16	25.73	11.39	14.95	10.68	539.48	10.68	7.52
GPTQ [16]		8.06	6.76	5.84	5.06	8.37	6.44	4.82
AWQ [32]		11.88	7.45	10.07	5.21	24.00	10.45	-
OmniQuant [48]		6.49	5.68	4.74	4.04	6.58	5.58	3.92
QuIP# [54]		5.98	5.31	4.36	3.78	5.79	5.10	3.56
RTN	W3A16g128	7.01	5.88	4.87	4.24	6.66	5.51	3.97
GPTQ [16]		6.55	5.62	4.80	4.17	6.29	5.42	3.85
AWQ [32]		6.46	5.51	4.63	3.99	6.24	5.32	-
OmniQuant [48]		6.15	5.44	4.56	3.94	6.03	5.28	3.78
QBB (Ours)	W(4x1)A16g128	5.69	5.14	4.19	3.64	5.21	4.63	3.20

Table 4: Weights only quantization results of LLaMA and LLaMA-2 models in terms of perplexity on WikiText2.

evaluated across multiple LLM families, our approach matches and outperforms all prior works, setting a new state-of-the-art result using a summation-only based approach.

References

- Haoli Bai, Wei Zhang, Lu Hou, Lifeng Shang, Jing Jin, Xin Jiang, Qun Liu, Michael Lyu, and Irwin King. Binarybert: Pushing the limit of bert quantization. *arXiv preprint arXiv:2012.15701*, 2020. 2
- [2] Yoshua Bengio, Nicholas Léonard, and Aaron Courville. Estimating or propagating gradients through stochastic neurons for conditional computation. *arXiv preprint arXiv:1308.3432*, 2013.
 2, 4
- [3] Tom Brown, Benjamin Mann, Nick Ryder, Melanie Subbiah, Jared D Kaplan, Prafulla Dhariwal, Arvind Neelakantan, Pranav Shyam, Girish Sastry, Amanda Askell, et al. Language models are few-shot learners. Advances in neural information processing systems, 33:1877–1901, 2020. 1
- [4] Adrian Bulat and Georgios Tzimiropoulos. XNOR-Net++: Improved binary neural networks. In *BMVC*, 2019. 2, 8
- [5] Adrian Bulat, Georgios Tzimiropoulos, Jean Kossaifi, and Maja Pantic. Improved training of binary networks for human pose estimation and image recognition. *arXiv preprint arXiv:1904.05868*, 2019. 2, 4
- [6] Adrian Bulat, Brais Martinez, and Georgios Tzimiropoulos. BATS: Binary ArchitecTure search. ECCV, 2020. 2
- [7] Jerry Chee, Yaohui Cai, Volodymyr Kuleshov, and Christopher M De Sa. Quip: 2-bit quantization of large language models with guarantees. Advances in Neural Information Processing Systems, 36, 2024. 1
- [8] Yoojin Choi, Mostafa El-Khamy, and Jungwon Lee. Towards the limit of network quantization. *arXiv preprint arXiv:1612.01543*, 2016. 2
- [9] Aakanksha Chowdhery, Sharan Narang, Jacob Devlin, Maarten Bosma, Gaurav Mishra, Adam Roberts, Paul Barham, Hyung Won Chung, Charles Sutton, Sebastian Gehrmann, et al. Palm: Scaling language modeling with pathways. *Journal of Machine Learning Research*, 24(240): 1–113, 2023. 1
- [10] Matthieu Courbariaux, Yoshua Bengio, and Jean-Pierre David. BinaryConnect: Training deep neural networks with binary weights during propagations. In *NeurIPS*, pages 3123–3131, 2015.
 2, 8
- [11] Matthieu Courbariaux, Itay Hubara, Daniel Soudry, Ran El-Yaniv, and Yoshua Bengio. Binarized neural networks: Training deep neural networks with weights and activations constrained to+ 1 or-1. arXiv preprint arXiv:1602.02830, 2016. 2, 4
- [12] Alex de Vries. The growing energy footprint of artificial intelligence. *Joule*, 7(10):2191–2194, 2023. 9
- [13] Tim Dettmers, Ruslan Svirschevski, Vage Egiazarian, Denis Kuznedelev, Elias Frantar, Saleh Ashkboos, Alexander Borzunov, Torsten Hoefler, and Dan Alistarh. Spqr: A sparse-quantized representation for near-lossless llm weight compression. arXiv preprint arXiv:2306.03078, 2023. 2, 9
- [14] Tim Dettmers, Artidoro Pagnoni, Ari Holtzman, and Luke Zettlemoyer. Qlora: Efficient finetuning of quantized llms. Advances in Neural Information Processing Systems, 36, 2024. 2
- [15] Ruizhou Ding, Ting-Wu Chin, Zeye Liu, and Diana Marculescu. Regularizing activation distribution for training binarized deep networks. In CVPR, 2019. 2
- [16] Elias Frantar, Saleh Ashkboos, Torsten Hoefler, and Dan Alistarh. Gptq: Accurate post-training quantization for generative pre-trained transformers. *arXiv preprint arXiv:2210.17323*, 2022. 1, 2, 3, 9, 10

- [17] Leo Gao, Jonathan Tow, Baber Abbasi, Stella Biderman, Sid Black, Anthony DiPofi, Charles Foster, Laurence Golding, Jeffrey Hsu, Alain Le Noac'h, Haonan Li, Kyle McDonell, Niklas Muennighoff, Chris Ociepa, Jason Phang, Laria Reynolds, Hailey Schoelkopf, Aviya Skowron, Lintang Sutawika, Eric Tang, Anish Thite, Ben Wang, Kevin Wang, and Andy Zou. A framework for few-shot language model evaluation, 12 2023. URL https://zenodo.org/records/ 10256836. 9
- [18] Yunchao Gong, Liu Liu, Ming Yang, and Lubomir Bourdev. Compressing deep convolutional networks using vector quantization. arXiv preprint arXiv:1412.6115, 2014. 2
- [19] Byeongho Heo, Jeesoo Kim, Sangdoo Yun, Hyojin Park, Nojun Kwak, and Jin Young Choi. A comprehensive overhaul of feature distillation. In *Proceedings of the IEEE/CVF International Conference on Computer Vision*, pages 1921–1930, 2019. 7
- [20] Geoffrey Hinton, Oriol Vinyals, and Jeff Dean. Distilling the knowledge in a neural network. arXiv preprint arXiv:1503.02531, 2015. 5, 7
- [21] Mark Horowitz. 1.1 computing's energy problem (and what we can do about it). In 2014 IEEE international solid-state circuits conference digest of technical papers (ISSCC), pages 10–14. IEEE, 2014. 8
- [22] Benoit Jacob, Skirmantas Kligys, Bo Chen, Menglong Zhu, Matthew Tang, Andrew Howard, Hartwig Adam, and Dmitry Kalenichenko. Quantization and training of neural networks for efficient integer-arithmetic-only inference. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pages 2704–2713, 2018. 2
- [23] Mojan Javaheripi, Sébastien Bubeck, Marah Abdin, Jyoti Aneja, Sebastien Bubeck, Caio César Teodoro Mendes, Weizhu Chen, Allie Del Giorno, Ronen Eldan, Sivakanth Gopi, et al. Phi-2: The surprising power of small language models. *Microsoft Research Blog*, 2023. 9
- [24] Albert Q Jiang, Alexandre Sablayrolles, Arthur Mensch, Chris Bamford, Devendra Singh Chaplot, Diego de las Casas, Florian Bressand, Gianna Lengyel, Guillaume Lample, Lucile Saulnier, et al. Mistral 7b. arXiv preprint arXiv:2310.06825, 2023. 1
- [25] Jared Kaplan, Sam McCandlish, Tom Henighan, Tom B Brown, Benjamin Chess, Rewon Child, Scott Gray, Alec Radford, Jeffrey Wu, and Dario Amodei. Scaling laws for neural language models. arXiv preprint arXiv:2001.08361, 2020. 1
- [26] Dahyun Kim, Kunal Pratap Singh, and Jonghyun Choi. Learning architectures for binary networks. In ECCV, 2020. 2
- [27] Sehoon Kim, Coleman Hooper, Amir Gholami, Zhen Dong, Xiuyu Li, Sheng Shen, Michael W Mahoney, and Kurt Keutzer. Squeezellm: Dense-and-sparse quantization. arXiv preprint arXiv:2306.07629, 2023. 2
- [28] Diederik P Kingma and Jimmy Ba. Adam: A method for stochastic optimization. arXiv preprint arXiv:1412.6980, 2014. 9
- [29] Teven Le Scao, Angela Fan, Christopher Akiki, Ellie Pavlick, Suzana Ilić, Daniel Hesslow, Roman Castagné, Alexandra Sasha Luccioni, François Yvon, Matthias Gallé, et al. Bloom: A 176b-parameter open-access multilingual language model. 2023. 1
- [30] Changhun Lee, Jungyu Jin, Taesu Kim, Hyungjun Kim, and Eunhyeok Park. Owq: Lessons learned from activation outliers for weight quantization in large language models. arXiv preprint arXiv:2306.02272, 2023. 2
- [31] Wenshuo Li, Xinghao Chen, Jinyu Bai, Xuefei Ning, and Yunhe Wang. Searching for energyefficient hybrid adder-convolution neural networks. In *Proceedings of the IEEE/CVF conference* on computer vision and pattern recognition, pages 1943–1952, 2022. 8
- [32] Ji Lin, Jiaming Tang, Haotian Tang, Shang Yang, Xingyu Dang, and Song Han. Awq: Activation-aware weight quantization for llm compression and acceleration. *arXiv preprint arXiv:2306.00978*, 2023. 1, 2, 3, 10

- [33] Xiaofan Lin, Cong Zhao, and Wei Pan. Towards accurate binary convolutional neural network. In *NeurIPS*, pages 345–353, 2017. 2
- [34] Zechun Liu, Baoyuan Wu, Wenhan Luo, Xin Yang, Wei Liu, and Kwang-Ting Cheng. Bi-Real Net: Enhancing the performance of 1-bit CNNs with improved representational capability and advanced training algorithm. In ECCV, pages 747–763, 2018. 2
- [35] Zechun Liu, Zhiqiang Shen, Marios Savvides, and Kwang-Ting Cheng. Reactnet: Towards precise binary neural network with generalized activation functions. In *Computer Vision–ECCV* 2020: 16th European Conference, Glasgow, UK, August 23–28, 2020, Proceedings, Part XIV 16, pages 143–159. Springer, 2020. 2
- [36] Zechun Liu, Barlas Oguz, Aasish Pappu, Lin Xiao, Scott Yih, Meng Li, Raghuraman Krishnamoorthi, and Yashar Mehdad. Bit: Robustly binarized multi-distilled transformer. Advances in neural information processing systems, 35:14303–14316, 2022. 2
- [37] Zechun Liu, Barlas Oguz, Aasish Pappu, Yangyang Shi, and Raghuraman Krishnamoorthi. Binary and ternary natural language generation. *arXiv preprint arXiv:2306.01841*, 2023. 2
- [38] Zechun Liu, Barlas Oguz, Changsheng Zhao, Ernie Chang, Pierre Stock, Yashar Mehdad, Yangyang Shi, Raghuraman Krishnamoorthi, and Vikas Chandra. Llm-qat: Data-free quantization aware training for large language models. *arXiv preprint arXiv:2305.17888*, 2023. 2, 5
- [39] Shuming Ma, Hongyu Wang, Lingxiao Ma, Lei Wang, Wenhui Wang, Shaohan Huang, Li Dong, Ruiping Wang, Jilong Xue, and Furu Wei. The era of 1-bit llms: All large language models are in 1.58 bits. arXiv preprint arXiv:2402.17764, 2024. 2
- [40] Brais Martinez, Jing Yang, Adrian Bulat, and Georgios Tzimiropoulos. Training binary neural networks with real-to-binary convolutions. *ICLR*, 2020. 2, 4, 8
- [41] Stephen Merity, Caiming Xiong, James Bradbury, and Richard Socher. Pointer sentinel mixture models. arXiv preprint arXiv:1609.07843, 2016. 9
- [42] Markus Nagel, Mart van Baalen, Tijmen Blankevoort, and Max Welling. Data-free quantization through weight equalization and bias correction. In *Proceedings of the IEEE/CVF International Conference on Computer Vision*, pages 1325–1334, 2019. 2
- [43] Adam Paszke, Sam Gross, Soumith Chintala, Gregory Chanan, Edward Yang, Zachary DeVito, Zeming Lin, Alban Desmaison, Luca Antiga, and Adam Lerer. Automatic differentiation in pytorch. 2017. 9
- [44] Haotong Qin, Yifu Ding, Mingyuan Zhang, Qinghua Yan, Aishan Liu, Qingqing Dang, Ziwei Liu, and Xianglong Liu. Bibert: Accurate fully binarized bert. arXiv preprint arXiv:2203.06390, 2022. 2
- [45] Haotong Qin, Mingyuan Zhang, Yifu Ding, Aoyu Li, Zhongang Cai, Ziwei Liu, Fisher Yu, and Xianglong Liu. Bibench: Benchmarking and analyzing network binarization. In *International Conference on Machine Learning*, pages 28351–28388. PMLR, 2023. 2
- [46] Mohammad Rastegari, Vicente Ordonez, Joseph Redmon, and Ali Farhadi. Xnor-net: Imagenet classification using binary convolutional neural networks. In *European conference on computer* vision, pages 525–542. Springer, 2016. 2, 3, 4
- [47] Yuzhang Shang, Zhihang Yuan, Qiang Wu, and Zhen Dong. Pb-llm: Partially binarized large language models. arXiv preprint arXiv:2310.00034, 2023. 2
- [48] Wenqi Shao, Mengzhao Chen, Zhaoyang Zhang, Peng Xu, Lirui Zhao, Zhiqian Li, Kaipeng Zhang, Peng Gao, Yu Qiao, and Ping Luo. Omniquant: Omnidirectionally calibrated quantization for large language models. arXiv preprint arXiv:2308.13137, 2023. 1, 2, 9, 10
- [49] Ying Sheng, Lianmin Zheng, Binhang Yuan, Zhuohan Li, Max Ryabinin, Beidi Chen, Percy Liang, Christopher Ré, Ion Stoica, and Ce Zhang. Flexgen: High-throughput generative inference of large language models with a single gpu. In *International Conference on Machine Learning*, pages 31094–31116. PMLR, 2023. 2

- [50] Han Shu, Jiahao Wang, Hanting Chen, Lin Li, Yujiu Yang, and Yunhe Wang. Adder attention for vision transformer. Advances in Neural Information Processing Systems, 34:19899–19909, 2021. 8
- [51] Dehua Song, Yunhe Wang, Hanting Chen, Chang Xu, Chunjing Xu, and DaCheng Tao. Addersr: Towards energy efficient image super-resolution. In *Proceedings of the IEEE/CVF Conference* on Computer Vision and Pattern Recognition, pages 15648–15657, 2021. 8
- [52] Hugo Touvron, Thibaut Lavril, Gautier Izacard, Xavier Martinet, Marie-Anne Lachaux, Timothée Lacroix, Baptiste Rozière, Naman Goyal, Eric Hambro, Faisal Azhar, et al. Llama: Open and efficient foundation language models. *arXiv preprint arXiv:2302.13971*, 2023. 1, 9
- [53] Hugo Touvron, Louis Martin, Kevin Stone, Peter Albert, Amjad Almahairi, Yasmine Babaei, Nikolay Bashlykov, Soumya Batra, Prajjwal Bhargava, Shruti Bhosale, et al. Llama 2: Open foundation and fine-tuned chat models. arXiv preprint arXiv:2307.09288, 2023. 1, 9
- [54] Albert Tseng, Jerry Chee, Qingyao Sun, Volodymyr Kuleshov, and Christopher De Sa. Quip#: Even better llm quantization with hadamard incoherence and lattice codebooks. *arXiv preprint arXiv:2402.04396*, 2024. 9, 10
- [55] Hongyu Wang, Shuming Ma, Li Dong, Shaohan Huang, Huaijie Wang, Lingxiao Ma, Fan Yang, Ruiping Wang, Yi Wu, and Furu Wei. Bitnet: Scaling 1-bit transformers for large language models. arXiv preprint arXiv:2310.11453, 2023. 2
- [56] Kuan Wang, Zhijian Liu, Yujun Lin, Ji Lin, and Song Han. Haq: Hardware-aware automated quantization with mixed precision. In *Proceedings of the IEEE/CVF conference on computer* vision and pattern recognition, pages 8612–8620, 2019. 2
- [57] Yunhe Wang, Mingqiang Huang, Kai Han, Hanting Chen, Wei Zhang, Chunjing Xu, and Dacheng Tao. Addernet and its minimalist hardware design for energy-efficient artificial intelligence. arXiv preprint arXiv:2101.10015, 2021.
- [58] Ziwei Wang, Jiwen Lu, Chenxin Tao, Jie Zhou, and Qi Tian. Learning channel-wise interactions for binary convolutional neural networks. In CVPR, pages 568–577, 2019. 2
- [59] Thomas Wolf, Lysandre Debut, Victor Sanh, Julien Chaumond, Clement Delangue, Anthony Moi, Pierric Cistac, Tim Rault, Rémi Louf, Morgan Funtowicz, et al. Huggingface's transformers: State-of-the-art natural language processing. arXiv preprint arXiv:1910.03771, 2019. 9
- [60] Yuzhuang Xu, Xu Han, Zonghan Yang, Shuo Wang, Qingfu Zhu, Zhiyuan Liu, Weidong Liu, and Wanxiang Che. Onebit: Towards extremely low-bit large language models. arXiv preprint arXiv:2402.11295, 2024. 2
- [61] Chunyu Yuan and Sos S Agaian. A comprehensive review of binary neural network. Artificial Intelligence Review, 56(11):12949–13013, 2023. 2
- [62] Zhihang Yuan, Lin Niu, Jiawei Liu, Wenyu Liu, Xinggang Wang, Yuzhang Shang, Guangyu Sun, Qiang Wu, Jiaxiang Wu, and Bingzhe Wu. Rptq: Reorder-based post-training quantization for large language models. arXiv preprint arXiv:2304.01089, 2023. 2
- [63] Shilin Zhu, Xin Dong, and Hao Su. Binary ensemble neural network: More bits per network or more networks per bit? In CVPR, pages 4923–4932, 2019. 2
- [64] Bohan Zhuang, Chunhua Shen, Mingkui Tan, Lingqiao Liu, and Ian Reid. Structured binary neural networks for accurate image classification and semantic segmentation. In CVPR, pages 413–422, 2019. 2

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