

COSA: CONTEXT-AWARE OUTPUT-SPACE ADAPTER FOR TEST-TIME ADAPTATION IN TIME SERIES FORECASTING

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Paper under double-blind review

ABSTRACT

Deployed time-series forecasters suffer performance degradation under non-stationarity and distribution shifts. Test-time adaptation (TTA) for time-series forecasting differs from vision TTA because ground truth becomes observable shortly after prediction. Existing time-series TTA methods typically employ dual input/output adapters that indirectly modify data distributions, making their effect on the frozen model difficult to analyze. We introduce the *Context-aware Output-Space Adapter* (COSA), a minimal, plug-and-play adapter that directly corrects predictions of a frozen base model. COSA performs residual correction modulated by gating, utilizing the original prediction and a lightweight context vector that summarizes statistics from recently observed ground truth. At test time, only the adapter parameters (linear layer and gating) are updated under a leakage-free protocol, using observed ground truth with an adaptive learning rate schedule for faster adaptation. Across diverse scenarios, COSA demonstrates substantial performance gains versus baselines without TTA (13.91~17.03%) and SOTA TTA methods (10.48~13.05%), with particularly large improvements at long horizons, while adding a reasonable level of parameters and negligible computational overhead. The simplicity of COSA makes it architecture-agnostic and deployment-friendly. Source code: <https://anonymous.4open.science/r/linear-adapter-A720>

1 INTRODUCTION

Time-series forecasting serves as the foundation for critical decision-making across diverse domains, including finance (Chen et al., 2023), supply chain management (Aamer et al., 2020), energy grids (Di Piazza et al., 2021), and predictive maintenance (Makridis et al., 2020). Modern forecasting models, including Transformer-based architectures (Zhou et al., 2021; Liu et al., 2023; 2022), typically achieve high accuracy. However, they suffer performance degradation in real deployment settings due to non-stationarity and distribution shifts (Du et al., 2021; Chen et al., 2024a). Time series exhibit inherent non-stationarity, with changing temporal patterns and statistical characteristics over time, resulting in distributions at training that typically differ from those encountered after deployment.

To address this challenge, various approaches have been proposed, including online learning, continual learning, and domain adaptation. Online and continual learning methods adapt by updating model parameters directly to streaming data (Du et al., 2021; Zhang et al., 2024; Kirkpatrick et al., 2017; Rolnick et al., 2019; Giannini et al., 2023; Pham et al., 2022), but these approaches incur additional computational costs, memory requirements, catastrophic forgetting issues, and plasticity. Furthermore, these methods typically require labeled data or explicit knowledge of task boundaries, making them unsuitable for scenarios where only unlabeled streaming data is available during deployment. Domain adaptation methods learn robust representations by reducing source-target distribution differences (Wilson et al., 2020; Jin et al., 2022), but they rely on explicit target domain data and boundary definitions.

Test-time adaptation (TTA) offers an alternative approach that adapts to distribution changes by updating only lightweight modules using unlabeled test streams after deployment. TTA methods have

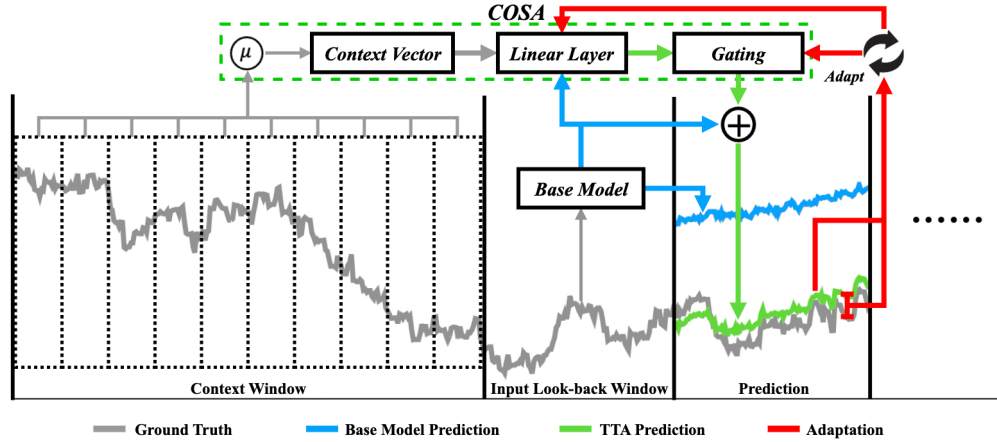


Figure 1: Overview of COSA operation showing the context-aware gated linear adapter architecture with input processing, linear transformation, gating mechanism, and output correction for test-time adaptation.

evolved mainly in the vision domain through batch normalization coefficient optimization and entropy minimization (Wang et al., 2020), self-supervised/contrastive learning combined with pseudo-labeling (Liang et al., 2021; Chen et al., 2022; Gong et al., 2025), single-sample multi-augmentation-based adaptation (Zhang et al., 2022), and long-term adaptation stabilization (Wang et al., 2022).

Unlike vision tasks, time-series forecasting has unique characteristics that distinguish it from vision tasks: 1) it employs normalization methods different from vision tasks to preserve periodicity and level information, and 2) ground truth becomes sequentially observable after prediction with short delays, enabling the use of direct losses such as Mean Squared Error (MSE).

Time-series forecasting TTA is a recently evolving topic; to the best of our knowledge, only few methods (Kim et al., 2025; Medeiros et al., 2025; Grover & Etemad, 2025) have been proposed. All of them adopted dual-adapter architectures that place calibration modules at both input and output ends of the base model. They map inputs to domains that the base model can handle more easily and restore outputs to the original domain, controlling adaptation intensity through gating. However, these indirect distribution calibration methods involve design complexity and create uncertainty about the impact of input transformations on internal model representations.

To this end, we propose Context-aware Output-Space Adapter (COSA), which offers a direct output-space correction approach that operates with minimal computational overhead. Figure 1 presents the overview of COSA. COSA takes the predictions from a frozen base model and a lightweight context vector, summarizes recent observation statistics as input, computes residuals through linear correction, and controls correction strength using gating. At deployment, we freeze the base forecaster and update only a lightweight output adapter (i.e., linear correction with a learnable gate) under a leakage-free streaming protocol: after each prediction, adaptation uses only previously revealed ground truth, never current or future labels. COSA is architecture-agnostic and demonstrates consistent performance improvements over existing state-of-the-art time-series forecasting TTA methods across various predictors and horizons.

The main contributions of this study are summarized as follows:

1. **Architecture-agnostic output adapter.** Unlike existing time-series TTA methods that adopt dual input-output adapters, COSA consists of a single output adapter. COSA operates independently in the output space, correcting predictions from any base model without changes to training pipelines or internal parameters. COSA also shows compatibility with SOTA normalizers, consistently reducing prediction error.
2. **Context-aware linear residual with gating.** A linear correction uses the base prediction and a lightweight context vector that summarizes statistics of recent observed ground truth, and a learnable gate modulates correction strength.

3. **Consistent accuracy gains.** Across six benchmarks, four horizons, and six baseline architectures, COSA improves test MSE over baselines (13.91~17.03%) and SOTA TTA methods (10.48~13.05%), in particular, with the largest gains at longer horizons.
4. **Fast, efficient TTA.** Adaptive learning rate enables faster convergence of COSA, leading to higher accuracy within a few adaptation steps. Specifically, COSA enables 88.59~90.10% faster inference time against prior SOTA TTA methods.

2 RELATED WORK

2.1 TIME-SERIES FORECASTING

To handle non-stationarity in time-series forecasting, existing methods typically employ 1) on-line learning, 2) continual learning, and 3) domain adaptation. Representative online learning, D3A (Zhang et al., 2024) narrows source–target gaps through z-score monitoring of loss distributions and Gaussian noise injection, whereas Adarnn (Du et al., 2021) reduces temporal distribution shifts using temporal distribution characterization and distribution matching. In continual learning, cPNN (Giannini et al., 2023) grows temporal columns and transfers knowledge via lateral connections, and FSNet (Pham et al., 2022) separates per-layer adapters for rapid adaptation from associative memory for long-term retention to balance plasticity and stability. For domain adaptation, CoDATS (Wilson et al., 2020) learns domain-invariant features adversarially, and DAF (Jin et al., 2022) shares attention with domain-invariant queries/keys and domain-specific values. These families generally update the base model during training or online operation, differing from TTA, which adapts lightweight modules on unlabeled test streams while keeping the base model frozen.

2.2 TEST-TIME ADAPTATION

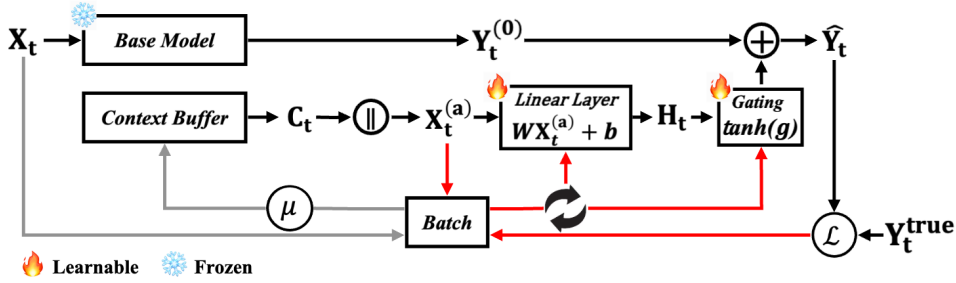
Tent (Wang et al., 2020) optimizes only batch-normalization affine parameters under entropy minimization, and SHOT (Liang et al., 2021) combines information maximization with self-supervised objectives to transfer source hypotheses to the target. AdaContrast (Chen et al., 2022) constructs pseudo-labels via contrastive learning with a dynamic memory bank for gradual adaptation, while MEMO (Zhang et al., 2022) applies multi-augmentation to a single test example to minimize marginal output entropy, updating all weights. CoTTA (Wang et al., 2022) limits error accumulation via weight and stochastic restoration, and ACCUP (Gong et al., 2025) integrates adaptive clustering with pseudo-labeling. However, they are proposed for vision tasks. TTA for time-series forecasting requires different approaches from those for vision tasks due to its own characteristics.

2.3 TEST-TIME ADAPTATION FOR TIME-SERIES FORECASTING

Time-series forecasting TTA methods typically employ dual adapters that calibrate distributions at both input and output. TAFAS (Kim et al., 2025) couples a calibration module to map inputs to a model-friendly domain and restores outputs to the original domain. It uses gating to modulate the calibration strength and utilizes Periodicity-Aware Adaptive Scheduling (PAAS) to adjust adaptation frequency using frequency patterns based on inputs. PETSA (Medeiros et al., 2025) factorizes the calibration module with a low-rank structure and adopts a combined loss for stable adaptation with fewer parameters. DynaTTA (Grover & Etemad, 2025) adjusts the dynamic learning rate, based on local distribution shift, global distribution shift, loss z-score. Existing time-series forecasting TTA methods employ an indirect approach that bidirectionally calibrates distributions at the input and output sides of the base model. They entailed design complexity due to indirect calibration and difficulty in predicting the impact of input transformations on internal representations. In contrast, we aim to utilize a single output-space adapter that directly corrects predictions without requiring input calibration or bidirectional transformation, resulting in a simpler design and more predictable adaptation behavior.

Table 1: Adapter-specific notation. Basic sizes/indices are defined as $(W, L, K, B; t, i, k)$.

Symbol	Meaning (shape)
$\mathbf{Y}_t^{(0)}$	Base (frozen) L -step prediction at time t (\mathbb{R}^L).
$\mathbf{Y}_t^{\text{true}}$	True L -step target revealed after t (\mathbb{R}^L).
\mathbf{C}_t	Context vector from revealed batch statistics $[\mu_t - K, \dots, \mu_t - 1]^\top$ (\mathbb{R}^K).
\mathbf{X}_t	Input look-back window (\mathbb{R}^W).
$\mathbf{X}_t^{(a)}$	Adapter input $[\mathbf{Y}_t^{(0)} \parallel \mathbf{C}_t]$ (\mathbb{R}^{L+K}).
\mathbf{H}_t	Linear residual $\mathbf{W} \mathbf{X}_t^{(a)} + \mathbf{b}$ (\mathbb{R}^L).
$\hat{\mathbf{Y}}_t$	Corrected output $\mathbf{Y}_t^{(0)} + \alpha \mathbf{H}_t$ with $\alpha = \tanh(g) \in [-1, 1]$ (\mathbb{R}^L).
$\mathbf{W}, \mathbf{b}, g$	Adapter weights ($\mathbb{R}^L \times (L + K)$), bias (\mathbb{R}^L), and gate parameter (\mathbb{R}).
<i>Operators:</i> concatenation $[\mathbf{a} \parallel \mathbf{b}]$; $\ \cdot\ _2$ vector norm; $\ \cdot\ _F$ Frobenius.	

Figure 2: Detailed architecture of COSA illustrating the linear correction layer (weight matrix \mathbf{W} and bias \mathbf{b}), learnable gating parameter (g), and context vector (\mathbf{C}) integration for output-space correction.

3 COSA:CONTEXT-AWARE OUTPUT-SPACE ADAPTER

3.1 NOTATION AND PROBLEM FORMULATION

Table 1 shows the symbols necessary for COSA and their meanings.

This study targets univariate time-series forecasting, following the existing SOTA time-series forecasting TTA methods (Kim et al., 2025; Medeiros et al., 2025; Grover & Etemad, 2025). For multivariate time-series inputs, we decompose them into per-variable univariate forecasting tasks and perform the task iteratively for each variable. At time t , base model generates L -step original predictions $\mathbf{Y}_t^{(0)} \in \mathbb{R}^L$ from input $\mathbf{X}_t \in \mathbb{R}^W$, where W denotes the input look-back window length. COSA generates corrected predictions $\hat{\mathbf{Y}}_t \in \mathbb{R}^L$ from input $\mathbf{X}_t^{(a)} \in \mathbb{R}^{L+K}$, where K denotes the length of the context vector. After making predictions, the ground truth for that interval becomes sequentially observable following a short delay. Like other TTA approaches, we keep the base model completely frozen and perform only adapter adaptation at test time. Adaptation is performed by collecting the most recent B prediction, ground truth pairs (batch index $i \in \{1, \dots, B\}$ and context index $k \in \{1, \dots, K\}$).

3.2 OVERALL ARCHITECTURE

Figure 2 illustrates the overall operation of COSA. COSA consists of a single output adapter that directly corrects the predictions. The key components are: 1) a linear layer composed of weight matrix \mathbf{W} and bias variable \mathbf{b} that computes correction values \mathbf{H} , 2) learnable gating g that controls correction strength, and 3) a context vector \mathbf{C} that summarizes and stores recent trend information.

We choose a single linear layer for two key reasons: 1) **Efficiency**: Linear operations provide lower latency and higher throughput compared to nonlinear modules, making them suitable for fast adaptation. We confirmed that a single-layer adapter shows 34.95% faster wall-clock time on average than a 2-layer MLP adapter. 2) **Simplicity-Performance balance**: As reported in LTSF-Linear (Zeng

et al., 2023), a linear layer sufficiently performs well in time-series forecasting, despite its simplicity. We also verified that a single linear layer adapter showed 5.71% even better performance on average against a 2-layer MLP adapter. These characteristics make the linear layer beneficial for TTA. Detailed results are provided in Appendix G.3.

The streaming protocol for leakage prevention is as follows (let the last adaptation was performed in $t-1$):

1. **Prediction:** At time t , base model generates prediction $\mathbf{Y}_t^{(0)}$ from input \mathbf{X}_t .
2. **Correction:** Feed $\mathbf{Y}_t^{(0)}$ and context \mathbf{C}_t into COSA to generate the corrected prediction $\hat{\mathbf{Y}}_t$.
3. **Observation:** After delay $\Delta \geq 0$, values of ground truth of the prediction horizon \mathbf{Y}_t^{true} are sequentially observed.
4. **Adaptation:** Collect the most recent B prediction, ground truth pairs $\{\hat{\mathbf{Y}}_{t+i-1}, \mathbf{Y}_{t+i-1}^{true}\}$, and perform adaptation that updates COSA parameters $\{\mathbf{W}, \mathbf{b}, \mathbf{g}\}$.

3.3 OUTPUT-SPACE RESIDUAL CORRECTION

For time t , we concatenate the original prediction of base model and context vector to create the adapter input:

$$\mathbf{X}_t^{(a)} = [\mathbf{Y}_t^{(0)} \parallel \mathbf{C}_t].$$

The residual is computed using a linear transformation:

$$\mathbf{H}_t = \mathbf{W} \mathbf{X}_t^{(a)} + \mathbf{b}.$$

The correction magnitude is controlled through gating to compose the final output:

$$\hat{\mathbf{Y}}_t = \mathbf{Y}_t^{(0)} + \tanh(\mathbf{g}) \mathbf{H}_t.$$

The tanh activation stabilizes the correction magnitude.

3.4 CONTEXT CONSTRUCTION

To prevent information leakage, the context summarizes previously observed ground truth information. For time t , we compute batch-wise aggregation as:

$$\mu_t = \text{agg}\{y_{t-(kB)+i}^{true} : 1 \leq i \leq B\}, \quad 1 \leq k \leq K.$$

where the aggregation function **agg** can use statistics such as mean, median, etc. We construct the context vector by stacking the most recent K aggregated values:

$$\mathbf{C}_t = [\mu_1, \mu_2, \dots, \mu_K]^\top.$$

This context vector summarizes level/scale changes and gradual drift patterns to help interpret the relative magnitude of the base prediction $\mathbf{Y}_t^{(0)}$ (reducing to single time-series values when $B=1$).

3.5 ADAPTATION OBJECTIVE AND SCHEDULING

Because targets arrive with a delay, we employ a direct objective with weight decay:

$$\mathcal{L} = \sum_{i=1}^B \|\hat{\mathbf{Y}}_{t-i-1} - \mathbf{Y}_{t-i-1}^{true}\|_2^2 + \lambda(\|\mathbf{W}\|_F^2 + \|\mathbf{b}\|_2^2 + \|\mathbf{g}\|_2^2). \quad (1)$$

When B forecast–target pairs have been enqueued, we run S gradient steps on the adapter parameters using a cosine–adaptive learning-rate schedule, simply *CALR*. We apply cosine annealing within the S steps,

$$\eta^{(s+1)} = \eta_{\min} + \frac{1}{2}(\eta^{(s)} - \eta_{\min}) \left(1 + \cos \frac{s\pi}{S}\right). \quad (2)$$

and then adjust η online, based on short-horizon loss trends to encourage fast but stable convergence (decrease η on loss upticks; mildly increase on plateaus). [When a new batch arrives, it is always](#)

initialized with the same learning rate, and thereafter the learning rate for the next step within the batch is determined through Equation 2 according to the loss. Early stopping and gradient clipping are also implemented. The threshold values for learning rate adjustment are stability-induced by balancing adaptation speed against stability. Conservative thresholds ensure convergence while aggressive values enable faster response to distribution shifts. Full pseudocode and thresholds are given in Algorithm 1 in Appendix A.

4 EXPERIMENTS

4.1 EXPERIMENTAL SETTINGS

We evaluate COSA on six benchmark datasets (ETTh1/2, ETTm1/2, Exchange Rate, and Weather) with a fixed look-back window ($W = 96$) and four prediction horizons ($L \in \{96, 192, 336, 720\}$). We used six representative base models spanning different architectures: Transformer-based (iTransformer (Liu et al., 2023), PatchTST (Nie et al., 2023)), linear-based (DLinear (Zeng et al., 2023), OLS (Toner & Darlow, 2024)), and MLP-based (FreTS (Yi et al., 2023), MICN (Wang et al., 2023)). By default, all input time series are treated as variable-wise univariate forecasting tasks, standard normalization is applied, and MSE serves as the performance comparison metric.

We compare *COSA* (our method) with *Baseline* (without TTA), *TAFAS* (Kim et al., 2025), and *PETSA* (Medeiros et al., 2025). All experiments were conducted according to the official benchmark library (Wang et al., 2024)¹. The train:validation:test ratio is 7:1:2 for all datasets.

Unless otherwise noted, we fix the adapter hyperparameters to $K=10$ and $S=3$, enabled *CALR*. We utilize the average as *agg*. Ablation studies for the variations of *agg* are provided in Appendix G.1.

We report two variants for COSA: COSA-F, which uses a fixed $B=48$ (half of the look-back), and COSA-P, which sets B online following the PAAS in TAFAS (Kim et al., 2025). Hyperparameters for comparative methods follow the settings reported in the original papers or official code defaults. In tables, the best score is shown in bold and the second best is underlined.

We utilize Xavier uniform initializer (Glorot & Bengio, 2010) with gain = 0.1 for parameters of the weight matrix W . The bias b and gating g are initialized to 0, and Adam optimizer is utilized.

All experiments were conducted on a machine with an Intel i7-7800X CPU and NVIDIA GeForce RTX 3080 10GB.

4.2 MAIN RESULTS

4.2.1 COMPARISON WITH SOTA TIME-SERIES TTA METHODS

The proposed COSA achieves best performance in all scenarios, as shown in Table 2². The results reveal two key performance patterns:

1. **Architecture-agnostic benefits:** Consistent improvements across all base models demonstrate that effectiveness of COSA is not dependent on specific model architectures. The average improvement ranges from 10.48% to 13.05%.
2. **Effectiveness in long-term forecasting:** The largest performance improvements were observed at the 720 horizon, where COSA-F and COSA-P showed performance improvements of 32.24% and 26.33% compared to baseline, respectively, and 28.21% and 21.96% compared to other methods. This trend suggests that COSA becomes increasingly valuable for longer prediction horizons.

These findings demonstrate that the COSA, which performs residual correction directly in the output space, proves more effective than existing indirect dual-adapter approaches.

¹In the case of *DynaTTA* (Grover & Etemad, 2025), there were reproducibility issues when we used the officially released source code. Therefore, we report the comparison results with them in the Appendix F.4 with the used detailed hyperparameters.

²All reported results are averaged over 10 runs with different random seeds to ensure statistical reliability.

Table 2: Prediction accuracy comparison. Standard deviations less than 0.001 are omitted.

		Transformer-based					Linear-based					MLP-based				
		iTransformer					DLinear					FreTS				
		Baseline	TAFAS	PETSA	COSA-F	COSA-P	Baseline	TAFAS	PETSA	COSA-F	COSA-P	Baseline	TAFAS	PETSA	COSA-F	COSA-P
ETTh1	96	.4507	.4411	.4393	<u>.4368</u>	.4363	.4695	.4618	.4594	<u>.4574</u>	.4482	.4462	.4403	.4387	<u>.4384</u>	.4371
	192	.5078	.4928	.4949	<u>.4961</u>	.4919	.5213	.5117	.5118	<u>.5066</u>	.5050	.5022	.4954	<u>.4942</u>	.4951	.4940
	336	.5658	.5629	.5640	<u>.5651</u>	.5300	.5659	.5604	.5617	<u>.5528</u>	.5456	.5544	.5521	.5527	.5467	<u>.5351</u>
	720	.7038	.6612	.6596	<u>.5958</u>	.5638	.7117	.6820	.6743	<u>.6107</u>	.5896	.7182	.6852	.6846	<u>.6259</u>	.5959
ETTh2	96	.2577	.2549	.2551	<u>.2504</u>	.2493	.2323	.2303	.2306	<u>.2300</u>	.2281	.2384	.2367	<u>.2364</u>	.2367	.2350
	192	.3161	.3010	.3006	<u>.2983</u>	.2947	.2862	.2842	.2876	<u>.2827</u>	.2819	.2866	.2824	.2832	.2816	<u>.2824</u>
	336	.3545	.3352	.3348	<u>.3241</u>	.3339	.3252	.3185	.3184	.3050	<u>.3083</u>	.3317	.3229	.3233	.3031	<u>.3153</u>
	720	.4276	.4023	.4043	.3487	<u>.3591</u>	.4087	.3873	.3853	.3062	<u>.3477</u>	.4119	.3857	.3860	.3169	<u>.3399</u>
ETTm1	96	.3823	.3558	.3570	.3447	<u>.3455</u>	.3715	.3497	.3524	.3456	<u>.3475</u>	.3675	.3582	.3583	.3520	<u>.3525</u>
	192	.4423	.4146	.4142	.4124	<u>.4140</u>	.4438	.4166	.4178	.4113	<u>.4122</u>	.4325	.4212	<u>.4198</u>	.4150	.4212
	336	.5093	.4754	.4751	.4569	<u>.4643</u>	.5183	.4799	.4803	.4753	<u>.4858</u>	.5005	.4827	.4789	.4661	<u>.4775</u>
	720	.6065	.5562	.5553	.4773	<u>.5102</u>	.5929	.5488	.5532	.4774	<u>.4991</u>	.5704	.5486	.5476	.4718	<u>.4982</u>
ETTm2	96	.1647	.1634	.1637	.1627	<u>.1632</u>	.1598	.1584	.1584	.1583	<u>.1586</u>	.1581	.1572	.1572	.1568	<u>.1569</u>
	192	.2209	.2183	.2173	.2171	<u>.2173</u>	.1930	.1913	.1913	.1904	<u>.1905</u>	.1923	.1909	.1908	.1905	<u>.1908</u>
	336	.2727	.2630	.2592	.2435	<u>.2535</u>	.2324	.2289	.2292	.2083	<u>.2242</u>	.2320	.2288	.2289	.2098	<u>.2211</u>
	720	.3451	.3305	.3332	.2477	<u>.2606</u>	.3062	.2968	.2963	.2215	<u>.2316</u>	.3012	.2916	.2926	.2158	<u>.2314</u>
Exchange Rate	96	.0882	.0876	.0885	.0818	<u>.0837</u>	.0913	.0885	.0878	.0812	<u>.0834</u>	.0828	.0799	.0803	.0744	<u>.0766</u>
	192	.1811	.1686	.1740	.1403	<u>.1479</u>	.1827	.1760	.1730	.1459	<u>.1519</u>	.1734	.1665	.1648	.1366	<u>.1499</u>
	336	.3428	.3079	.3097	.2089	<u>.2624</u>	.3277	.2941	.2920	.2039	<u>.2480</u>	.3240	.2930	.2923	.2053	<u>.2461</u>
	720	.8540	.8322	.8004	.3421	<u>.4460</u>	.8873	.8762	.8781	.3494	<u>.4481</u>	.8368	.8273	.8067	.3352	<u>.4458</u>
Weather	96	.1755	.1664	.1674	.1597	<u>.1617</u>	.1954	.1796	.1823	.1773	<u>.1793</u>	.1856	.1759	.1765	.1724	<u>.1737</u>
	192	.2232	.2101	.2128	.2067	<u>.2088</u>	.2403	.2244	.2254	.2216	<u>.2217</u>	.2310	.2165	.2192	.2135	<u>.2189</u>
	336	.2800	.2614	.2665	.2503	<u>.2515</u>	.2918	.2709	.2740	.2567	<u>.2626</u>	.2843	.2653	.2681	.2561	<u>.2587</u>
	720	.3571	.3458	.3459	.2480	<u>.2730</u>	.3643	.3500	.3497	.2581	<u>.2708</u>	.3599	.3490	.3488	.2573	<u>.2692</u>
		PatchTST					OLS					MICN				
		Baseline					Baseline					Baseline				
		TAFAS	PETSA	COSA-F	COSA-P		TAFAS	PETSA	COSA-F	COSA-P		TAFAS	PETSA	COSA-F	COSA-P	
ETTh1	96	.4312	.4262	.4269	<u>.4242</u>	.4238	.4511	.4409	.4391	<u>.4390</u>	.4372	.5103	.4901	.4898	<u>.4693</u>	.4684
	192	.4955	.4865	.4854	<u>.4830</u>	.4805	.5046	.4934	.4937	<u>.4915</u>	.4906	.5954	.5617	.5620	<u>.5372</u>	.5328
	336	.5559	.5478	.5475	<u>.5438</u>	.5320	.5510	.5440	.5465	<u>.5385</u>	.5320	.6615	.6387	.6420	<u>.5950</u>	.5878
	720	.7117	.6860	.6822	<u>.6113</u>	.5822	.6997	.6630	.6431	<u>.5969</u>	.5733	.9233	.8142	.8375	<u>.7001</u>	.6504
ETTh2	96	.2362	.2351	.2362	<u>.2349</u>	.2343	.2306	.2285	.2288	.2232	<u>.2265</u>	.2582	.2551	.2552	<u>.2492</u>	.2485
	192	.2826	.2758	.2773	<u>.2665</u>	.2608	.2839	.2824	.2848	<u>.2796</u>	.2791	.3282	.3179	.3258	<u>.3049</u>	.3017
	336	.3199	.3125	.3132	<u>.2971</u>	.2978	.3258	.3182	.3189	.3003	<u>.3043</u>	.3732	.3482	.3497	<u>.3241</u>	.3310
	720	.4264	.4005	.4012	.3233	<u>.3428</u>	.4162	.3908	.3884	.3177	<u>.3453</u>	.4617	.4474	.4473	.3650	<u>.3885</u>
ETTm1	96	.4024	.3894	.3937	.3625	<u>.3626</u>	.3710	.3506	.3536	.3454	<u>.3475</u>	.4354	.3951	.3951	<u>.3837</u>	.3831
	192	.4512	.4372	.4413	.4250	<u>.4258</u>	.4439	.4160	.4184	.4115	<u>.4119</u>	.4855	.4566	.4574	.4476	<u>.4514</u>
	336	.5081	.4905	.4946	.4568	<u>.4697</u>	.5182	.4787	.4792	.4748	<u>.4749</u>	.5556	.5108	.5082	.4832	<u>.5054</u>
	720	.5629	.5427	.5462	.4681	<u>.4882</u>	.5922	.5478	.5522	.4763	<u>.5007</u>	.6212	.5756	.5778	.5029	<u>.5225</u>
ETTm2	96	.1584	.1581	.1583	.1558	<u>.1562</u>	.1602	.1590	.1589	.1582	<u>.1586</u>	.1710	.1711	.1730	.1702	<u>.1704</u>
	192	.2059	.2036	.2037	.2007	<u>.2022</u>	.1936	.1921	.1919	.1906	<u>.1907</u>	.2121	.2102	.2126	.2102	<u>.2120</u>
	336	.2458	.2451	.2452	.2258	<u>.2352</u>	.2331	.2299	.2302	.2131	<u>.2226</u>	.2530	.2501	.2520	.2337	<u>.2351</u>
	720	.3268	.3268	.3256	.2446	<u>.2645</u>	.3066	.2986	.2971	.2171	<u>.2349</u>	.3327	.3220	.3131	.2477	<u>.2643</u>
Exchange Rate	96	.0867	.0843	.0837	.0765	<u>.0788</u>	.0814	.0792	.0798	.0756	<u>.0773</u>	.1151	.1087	.1146	.0955	<u>.1008</u>
	192	.1877	.1805	.1832	.1464	<u>.1570</u>	.1727	.1658	.1653	.1393	<u>.1457</u>	.2150	.2198	.1999	.1663	<u>.1722</u>
	336	.3389	.3275	.3300	.1983	<u>.2445</u>	.3226	.2877	.2898	.2020	<u>.2323</u>	.3950	.3047	.3100	.2119	<u>.2660</u>
	720	.8648	.8659	.8643	.3543	<u>.4662</u>	.8366	.8138	.8149	.3444	<u>.4541</u>	1.0259	.7191	.7805	.3871	<u>.4815</u>
Weather	96	.1742	.1724	.1743	.1624	<u>.1634</u>	.1957	.1807	.1795	.1772	<u>.1803</u>	.1757	.1853	.1970	.1636	<u>.1651</u>
	192	.2195	.2147	.2167	.2006	<u>.2108</u>	.2404	.2244	.2274	.2223	<u>.2237</u>	.2237	.2161	.2265	.2082	<u>.2120</u>
	336	.2766	.2666	.2701	.2451	<u>.2488</u>	.2921	.2714	.2748	.2551	<u>.2642</u>	.2812	.2746	.2788	.2729	<u>.2737</u>
	720	.3544	.3383	.3442	.2590	<u>.2713</u>	.3644	.3466	.3493	.2579	<u>.2708</u>	.3508	.3573	.3681	.2582	<u>.2855</u>

4.2.2 COMPARISON WITH NORMALIZATION METHODS

In this section, we analyze whether COSA serves as an alternative or complementary role to existing normalizations, and demonstrate that COSA can work independently of normalizations and is compatible with normalization mechanisms. Figure 3 shows performance comparison of COSA against two representative time-series normalizers, RevIN (Kim et al., 2021) and DDN (Dai et al., 2024). The results support two claims:

1. COSA on its own generally outperforms explicit normalization, as demonstrated by the comparative analysis showing that using COSA with basic normalization achieves the lowest mean MSE across all experimental settings.
2. COSA is compatible with normalization and consistently improves accuracy within the same normalizer settings, with the addition of COSA reducing MSE by approximately 16.8~16.9%.

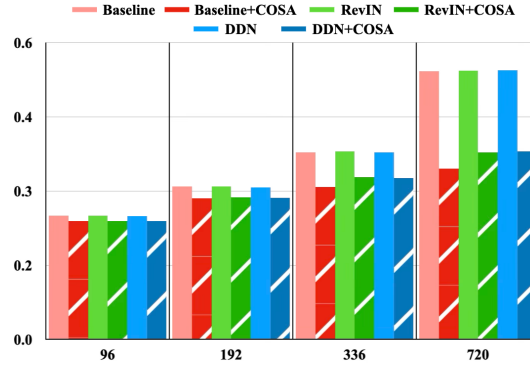


Figure 3: Prediction accuracy comparison with normalization methods.

COSA directly optimizes MSE on revealed targets and uses the context vector to encode recent level/scale, so the linear layer learns scale and level corrections from the error signal itself. Further analysis is provided in Appendix G.7.

4.3 SENSITIVITY AND ABLATIONS

We probe the following four key design choices: 1) adaptation steps S , 2) context length K , 3) batch size B , and 4) adaptive learning rate $CALR$.

We evaluated performance by varying each hyperparameter individually while keeping others fixed at the default settings. Figure 4 shows MSE and wall-clock time according to each hyperparameter. Figure 4a shows changes according to the number of iterative learning steps S . COSA shows a pattern where test MSE decreases as S increases. However, while wall-clock time also increases with increasing S , even at the highest $S = 4$ setting, it showed time levels similar to PETSA.

Figure 4b examines the effect of context length K , which controls how much past information the adapter uses. Accuracy improves consistently with larger K , while wall-clock time remains unchanged. Since the adapter input concatenates base model’s prediction with the context vector (dimensionality $L + K$), and L typically dominates, increasing K has negligible runtime impact. The context provides incremental but reliable gains by supplementing the level/scale information.

Figure 4c shows performance changes with batch size B . As described in Section 3.5, B determines the frequency of adaptation, collecting B {prediction, ground truth} pairs before each update. Even with $B = 96$, COSA outperforms the baseline, with accuracy improving as B decreases due to more frequent adaptation. This explains the superior performance of COSA-P over COSA-F on ETTh1: the average B determined by PAAS for ETTh1 is 24.55, while for other datasets the values are over 80. Detailed analysis is provided in Appendix C. However, smaller B increases wall-clock time due to both more adaptation calls and the computational cost of adaptation steps S .

Figure 4d shows performance with and without $CALR$ (Section 3.5). $CALR$ achieves up to 12.13% accuracy improvement as the window length increases and a 21.34% reduction in wall-clock time. This confirms that aggressive dynamic learning rate scheduling enhances performance within limited adaptation steps S while enabling early-stopping for computational efficiency.

Results for additional ablations (context aggregation methods and correction layer architecture) are provided in Appendix G.

4.4 COMPUTATIONAL OVERHEAD

Table 3: Computational overhead comparison of adapter methods.

Method	# Params ↓	Peak mem (MB) ↓	Samples/sec ↑	Adaptation time/batch (ms) ↓	Inference time/batch (ms) ↓
TAFAS	1,252,958	17.59	1,413.23 ± 92.28	73.23 ± 8.74	10.96 ± 0.64
PETSA	58,334	36.09	987.91 ± 78.67	88.46 ± 7.08	12.63 ± 0.37
COSA (Ours)	1,211,287	27.07	1080.70 ± 80.66	80.12 ± 5.93	1.25 ± 0.06

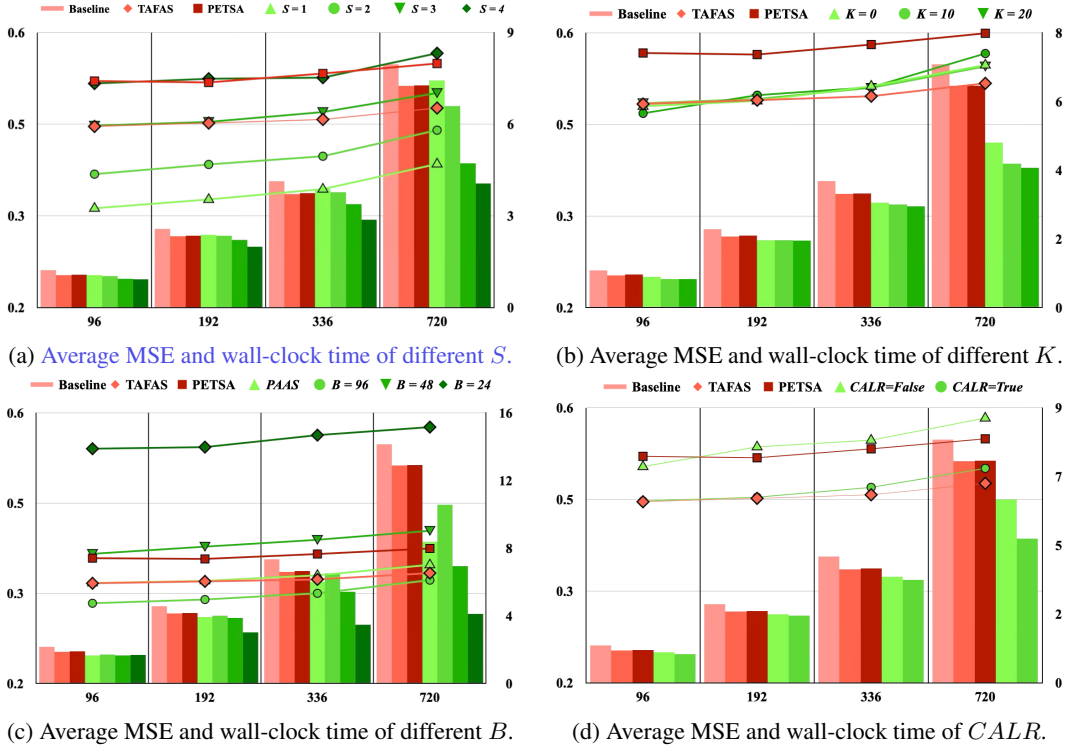


Figure 4: Hyperparameter analysis showing the trade-off between performance and efficiency. Charts display average test MSE (bars, left axis) and wall-clock time (lines, right axis, in seconds) across different parameter settings.

We report 1) observed additional parameters, 2) peak memory utilization, 3) throughput (samples per second), 4) wall-clock time per batch, and 5) inference time per batch.

All hyperparameters remain at default values. Table 3 summarizes the average overhead across all datasets, base model, and horizons. COSA shows moderate overhead, falling between TAFAS and PETSA, while achieving the significantly fastest inference time. COSA performs adaptation repeatedly for S steps, meaning that the throughput and adaptation time are dependent on S . However, the single adapter structure and simplicity of COSA alleviate the overhead and improve the inference time, which is not affected by S . The computational complexity is $\mathcal{O}(L \cdot (L + K))$ for the linear transformation plus $\mathcal{O}(L)$ for the gating operation, resulting in quadratic scaling with respect to prediction horizon L . Further theoretical calculations are included in Appendix B.

5 CONCLUSION AND LIMITATIONS

We introduced COSA, an architecture-agnostic TTA module that directly corrects the prediction of base model with a single linear layer guided by short-term context and a stabilizing gate. Across six benchmarks and diverse base models, COSA improves accuracy by 13.91% to 17.03% over baselines and by 10.48% to 13.05% over prior state-of-the-art TTA methods. These gains arise from the synergy of trend-aware context, residual correction, and gated modulation.

While COSA shows strong empirical results, several areas offer room for refinement. The current adaptation relies on full ground truth, though extending to partial observations would enable real-time deployment. Performance varies with batch size B , and the fixed context length K may not be optimal for all temporal patterns. Additionally, linear corrections, while effective for many cases, could be enhanced for complex nonlinear shifts.

Future work will explore masked updates for real-time adaptation with partial targets, adaptive selection of K and B based on detected periodicity, and hybrid linear/nonlinear adapters for more complex distribution shifts. These extensions will broaden the applicability of the proposed method while maintaining its computational efficiency.

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A ADAPTATION ALGORITHM OF COSA

This section details the core adaptation algorithm of COSA. This algorithm extends the optimizer mentioned in Equation 2, combining short-term loss trends, cosine annealing, and adaptive gradient clipping, batch-wise learning rate reset. We apply widely used values for the coefficients of *CALR* and the threshold value of early stopping. The base model remains frozen, operating only on adapter parameters $\varphi = \{\mathbf{W}, \mathbf{b}, \mathbf{g}\}$.

Purpose: Performs rapid adaptation of linear adapters using direct loss, adaptive learning rate scheduling, and gradient clipping to improve prediction accuracy within a few adaptation step S .

Algorithm 1 COSA adaptation.

Require: Stream of batches $(\hat{\mathbf{Y}}, \mathbf{Y}^{\text{true}})$ with length B , context vector \mathbf{C} , steps S , η_{\min}, η_{\max} , weight decay λ , clip base c

Ensure: adapted predictions with improved accuracy over the base model

```

1: for each batch  $(\hat{\mathbf{Y}}, \mathbf{Y}^{\text{true}})$  in Data Stream do                                ▷ Loop over new batches
2:   Initialize:  $\eta \leftarrow \eta_{\max}$ , loss history  $\mathcal{H} \leftarrow []$                     ▷ Reset LR for new batch
3:   for  $s = 1$  to  $S$  do                                                            ▷ Main adaptation loop
4:     Forward pass: form  $\mathbf{X}^{(a)} = [\mathbf{Y}^{(0)} \parallel \mathbf{C}]$ , then  $\mathbf{H} = (\mathbf{W} \mathbf{X}^{(a)\top} + \mathbf{b})^\top$ 
5:     Gating:  $\hat{\mathbf{Y}} \leftarrow \mathbf{Y}^{(0)} + \tanh(\mathbf{g}) \odot \mathbf{H}$ 
6:     MSE loss:  $\mathcal{L} \leftarrow \|\hat{\mathbf{Y}} - \mathbf{Y}^{\text{true}}\|_F^2 + \lambda \|\varphi\|_2^2$ 
7:     Learning rate adaptation:
8:     if  $|\mathcal{H}| \geq 2$  then
9:        $\Delta \leftarrow \mathcal{L} - \mathcal{H}[-1]$                                                     ▷ Recent loss change
10:      if  $\Delta > 0$  then                                                            ▷ Loss increased - reduce LR
11:         $\eta \leftarrow \max(0.5\eta, \eta_{\min})$ 
12:      else if  $|\Delta| < 10^{-6}$  then                                              ▷ Converged - increase LR for next batch
13:         $\eta \leftarrow \min(1.1\eta, \eta_{\max})$ 
14:      end if
15:    end if
16:    Cosine annealing:  $\eta \leftarrow \eta_{\min} + \frac{1}{2}(\eta - \eta_{\min})(1 + \cos(\frac{s\pi}{S}))$ 
17:    Gradient computation:  $\mathbf{g}_\varphi \leftarrow \nabla_\varphi \mathcal{L}$ 
18:    Adaptive clipping:  $\|\mathbf{g}_\varphi\| \leftarrow \min(\|\mathbf{g}_\varphi\|, \max(c, \mathcal{L}))$ 
19:    Parameter update:  $\varphi \leftarrow \varphi - \eta \mathbf{g}_\varphi$ 
20:    Early stopping:
21:    if  $s > 2$  and  $|\mathcal{H}[-1] - \mathcal{H}[-2]| < 10^{-6}$  then
22:      break
23:    end if
24:  end for
25: end for

```

COSA targets TSF-TTA under non-stationary environments in which the distribution of time-series data changes over time. In such environments, the classical notion of convergence toward a fixed optimal point is not well-defined. Instead, stable learning within each adaptation window is critical. CALR guarantees uniformly bounded step-wise updates through the following four mechanisms, which structurally prevent error amplification and thus ensure stability during adaptation.

1. **Upper-bounded learning rate:** The learning rate is constrained by $\eta \leq \eta_{\max}$, limiting the maximum magnitude of a single-step update.
2. **Gradient clipping:** At Line 18 of Algorithm 1, the gradient norm is adaptively bounded as $\|\mathbf{g}_\varphi\| \leftarrow \min(\|\mathbf{g}_\varphi\|, \max(c, \mathcal{L}))$.
3. **L2 regularization:** The weight-decay term in Equation 1, $\lambda(\|\mathbf{W}\|_F^2 + \|\mathbf{b}\|_2^2 + \|\mathbf{g}\|_2^2)$, constrains parameter magnitude.
4. **Bounded gating:** Because $\alpha = \tanh(g) \in [-1, 1]$, the correction magnitude is structurally limited.

For every new batch, the learning rate is reinitialized to η_{\max} (Line 2 of Algorithm 1), giving each batch an equal opportunity for adaptation. The learning rate is then adapted according to the batch's loss behavior. When the loss spikes, we reduce the learning rate as $\eta \leftarrow \max(0.5\eta, \eta_{\min})$,

Table 4: Average B of each dataset determined by PAAS.

Dataset	ETTh1	ETTh2	ETTm1	ETTm2	Exchange Rate	Weather
Average B	24.55	38.41	92.73	83.41	92.80	80.38

temporarily lowering update intensity. When the loss decreases stably, we increase it as $\eta \leftarrow \min(1.1\eta, \eta_{\max})$, strengthening adaptation. This enables stable learning even when short-term perturbations or anomalies appear in the input data, allowing rapid recovery.

B COMPUTATIONAL COST

In this section, we report theoretical calculations of parameters, FLOPs, and memory footprint.

For univariate time series, the number of parameters is as follows:

Parameter count.

$$\underbrace{L(L+K)}_w + \underbrace{L}_b + \underbrace{1}_g \Rightarrow \#params = (L(L+K) + L + 1).$$

FLOPs per adaptation step (batch of size B). The dominant cost is the linear transform and residual composition:

$$\mathcal{O}(BL(L+K)) \text{ for } \mathbf{W}\mathbf{X}^{(a)}, \quad \text{plus } \mathcal{O}(BL) \text{ for gating \& residual add.}$$

Memory footprint. Additional activations are modest: the linear residual $\mathbf{H} \in \mathbb{R}^{B \times L}$ and the context vector $\mathbf{C} \in \mathbb{R}^K$. The total adaptation cost scales linearly with the number of adaptation steps S and variables V .

C BATCH SIZE ANALYSIS OF PAAS

Adaptive vs. Fixed Batch Strategy: While COSA-F shows the best performance in most cases, COSA-P generally performs better on the ETTh1 and ETTh2 datasets, revealing important insights about temporal adaptation strategies. The reason for this trend is that the size of B determined by PAAS is often smaller than 48 for these datasets, as shown in Table 4, enabling more frequent adaptation that better captures the higher-frequency patterns characteristic of these hourly datasets.

This differential performance validates the importance of dataset-specific adaptation scheduling: datasets with more complex temporal dynamics benefit from more frequent adaptation (smaller B), while datasets with smoother patterns can effectively use larger batch sizes for computational efficiency.

D BEHAVIOR ANALYSIS OF COSA

D.1 ANALYSIS BETWEEN GATING AND LINEAR RESIDUAL LAYER

In COSA, the gating is defined as $gating = \tanh(g) \in [-1, 1]$, where g is a learnable parameter, and this bounded scalar modulates the correction strength by multiplying the output of the linear residual layer. If we were to use g directly instead of $\tanh(g)$, small variations in g could induce disproportionately large and unstable changes in the correction, making the adapter overly sensitive to noisy points. The \tanh transform keeps the gating bounded, ensuring that changes in g are reflected smoothly and gradually. When the residual magnitude spikes, the gate moves toward 0, as shown in Figure 5, thereby attenuating the residual correction and stabilizing the adaptation process.

D.2 ANALYSIS BETWEEN LEARNING RATE AND MSE

Figure 6 visualizes the trajectory of pre-adaptation loss and learning rate for the iTransformer-ETTm1, $L = 96$ case. As shown in Figure 6, when a short-term loss spike occurs, CALR immedi-

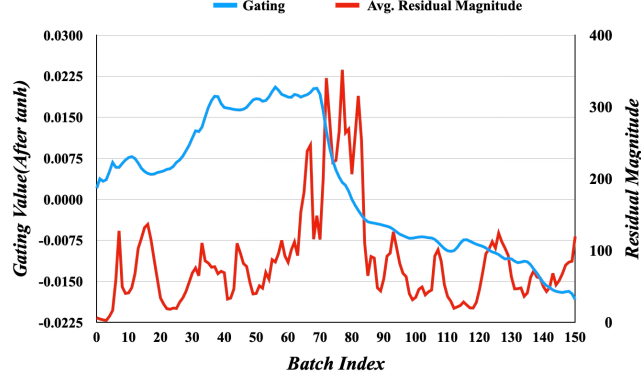


Figure 5: Trajectory of average gating and average residual magnitude of batches over time.

ately decreases the learning rate to minimize the impact of the perturbation, and once the loss enters a stable decreasing phase, CALR increases the learning rate again to promote rapid re-adaptation. This control mechanism suppresses excessive parameter drift without requiring roll-back, enabling COSA to recover its correction performance instantly after a perturbation. The interaction between the learning rate and loss shows that, in non-stationary environments with short-term perturbations, COSA can respond and recover performance stably.

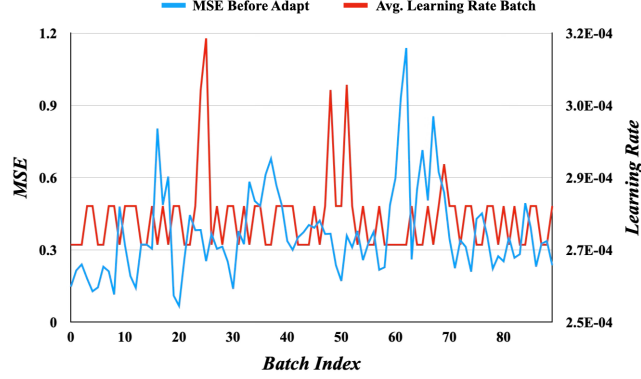


Figure 6: Trajectory of initial MSE and average learning rate of batches over time.

E QUALITY OF TTA

To evaluate TTA quality, we measured Explained Residual Variance (ERV) and Negative Adaptation Rate (NAR) metrics across all datasets, base models, and forecasting horizons. ERV is defined as in Equation 3, where \hat{R} represents residuals for TTA-applied predictions and $R^{(0)}$ represents residuals for base model predictions. Specifically, ERV quantifies the extent to which TTA reduces the residual variance of the base model’s predictions. Higher ERV values indicate greater residual variance reduction and correspondingly improved prediction performance through TTA.

$$\text{ERV} = 1 - \frac{\text{Var}(\hat{R})}{\text{Var}(R^{(0)})}. \quad (3)$$

NAR is the ratio of prediction windows where the MSE worsened when TTA was applied, with smaller values indicating better performance.

$$\text{NAR} = \frac{1}{N} \sum_{t=1}^N I[\text{MSE}(\hat{\mathbf{Y}}_t) > \text{MSE}(\mathbf{Y}_t^{(0)})], \quad \text{where} \begin{cases} I[\text{con}] = 1 & \text{if con} = \text{True} \\ I[\text{con}] = 0 & \text{otherwise} \end{cases} \quad (4)$$

Table 5: Average ERV and NAR across all benchmark datasets and base models.

	TAFAS	PETSA	COSA
ERV \uparrow	.0100	.0160	.0768
NAR \downarrow	34.94%	36.34%	20.25%

As shown in Table 5, COSA shows the highest ERV and the lowest NAR. This indicates that COSA provides effective TTA while decreasing the residual and improving accuracy on average.

F FURTHER EXPERIMENTS

F.1 COMPARISON ON A LARGER DATASET

To demonstrate that COSA can achieve stable and substantial performance gains even in larger-scale environments, we additionally conducted experiments on the Electricity dataset Lai et al. (2018); Godahewa et al. (2021). We followed the same experimental setup as in Section 4.1, and used three representative base models, iTransformer, DLinear, and FreTS. Table 6 is consistent with the findings in Section 4.2, COSA achieves either the best or second-best performance across all forecasting horizons L , and unlike other methods, which exhibit performance degradation compared to baselines in some cases, COSA improves their performances in every case. These results indicate that COSA remains robust and effective even in large-scale environments.

Table 6: Prediction accuracy comparison on Electricity dataset.

	iTransformer					DLinear					FreTS				
	No TTA	TAFAS	PETSA	COSA-F	COSA-P	No TTA	TAFAS	PETSA	COSA-F	COSA-P	No TTA	TAFAS	PETSA	COSA-F	COSA-P
96	.1663	.1568	.1596	.1571	.1570	.2235	.2224	.2242	.2232	.2228	.1824	.1781	.1802	.1801	.1799
192	.1794	.1635	.1644	.1631	.1631	.2242	.2153	.2152	.2146	.2143	.1794	.1894	.1781	.1780	.1779
336	.1952	.1743	.1741	.1730	.1727	.2383	.2247	.2233	.2226	<u>.2223</u>	.1905	.1885	.1885	<u>.1881</u>	.1879
720	.2567	.2316	.2301	<u>.2251</u>	.2239	.2792	.2629	.2615	<u>.2557</u>	.2541	.2304	.2299	.2287	<u>.2236</u>	.2221

F.2 COMPARISON WITH VARYING INPUT/PREDICTION SEQUENCE LENGTH

To further verify the performance of COSA across diverse scenarios, we conducted experiments by varying both the input window W and the prediction horizon L . To examine short-term forecasting rather than long-term forecasting, we added the setting $W = 96$, $L \in \{24, 48\}$. To evaluate performance under longer input windows, we additionally tested $W = 192$ with $L \in \{192, 336, 720\}$ and $W = 336$ with $L \in \{336, 720\}$. Table 7 summarizes the results across these different combinations of W and L . Consistent with Section 4.2, COSA achieves the best or second-best performance in most cases, demonstrating its ability to maintain high predictive accuracy across a wide range of settings. Unlike other methods, which show performance degradation relative to baselines in several cases, COSA improves prediction accuracy over baselines in every case. In contrast, TAFAS and PETSA, which adopt dual-adaptor architectures that modify both the input and output of base model incur substantial additional complexity as W increases, which likely contributes to their degraded performance. Since COSA operates solely in the output space of base model, it delivers consistent performance gains regardless of W .

F.3 COMPARISON WITH SOLID

SOLID (Chen et al., 2024b) is a fine-tuning method of the prediction layer of the base model by detecting context drift. Its reconitioner estimates context drift based on the mutual information between the model’s residual and the input context. When drift is detected, SOLID selectively chooses samples and fine-tunes the model’s prediction layer at the sample level. Like COSA, SOLID operates in the output space of base model. However, unlike COSA, which keeps base model frozen and performs corrections through a lightweight adapter, SOLID directly updates the prediction layer of base model.

Table 7: Prediction accuracy comparison with different input/prediction sequence length.

			iTransformer					DLinear					FreTS					
			Input	Pred	No TTA	TAFAS	PETSA	COSA-F	COSA-P	No TTA	TAFAS	PETSA	COSA-F	COSA-P	No TTA	TAFAS	PETSA	COSA-F
ETH1	96	24	.3269	.3254	.3299	<u>.3105</u>	.3098	.3437	.3751	.3766	<u>.3431</u>	.3429	.2953	.3243	.3239	<u>.2946</u>	.2943	
	96	48	.3732	.3768	.3776	<u>.3539</u>	.3527	.3838	.4177	.4166	<u>.3826</u>	.3820	.3424	.3770	.3754	<u>.3416</u>	.3413	
	192	192	.4459	.5015	.4893	<u>.4175</u>	.4120	.4172	.4967	.4834	<u>.4157</u>	.4141	.4235	.4991	.4835	<u>.4207</u>	.4186	
	192	336	.4729	.5709	.5422	<u>.4486</u>	.4456	.4537	.5558	.5362	<u>.4528</u>	.4489	.4596	.5677	.5398	<u>.4577</u>	.4535	
	192	720	.5885	.6529	.6687	<u>.5619</u>	.5477	.5828	.6504	.6526	<u>.5734</u>	.5660	.6484	.6627	.6728	<u>.6351</u>	.6190	
	336	336	.5354	.6139	.5686	<u>.5209</u>	.5059	.4392	.5652	.5174	<u>.4368</u>	.4289	.3837	.6114	.5444	<u>.4783</u>	.4674	
ETH2	336	720	.6512	.6873	.6635	<u>.6115</u>	.5780	.5748	.6344	.6443	<u>.5589</u>	.5198	.7265	.6905	<u>.6738</u>	.6960	.6295	
	96	24	<u>.0837</u>	.1277	.1266	.0812	<u>.0812</u>	<u>.0862</u>	.1217	.1218	.0861	<u>.0862</u>	.0812	.1180	.1178	.0806	<u>.0807</u>	
	96	48	.1047	.1518	.1520	.1007	<u>.1008</u>	.1031	.1444	.1452	.1028	<u>.1030</u>	<u>.1004</u>	.1452	.1447	.0996	<u>.0996</u>	
	192	192	.1633	.2272	.2280	.1546	<u>.1563</u>	.1344	.2155	.2096	.1334	<u>.1338</u>	.1437	.2218	.2184	.1412	<u>.1420</u>	
	192	336	.1658	.2541	.2487	.1551	<u>.1573</u>	.1474	.2445	.2394	.1460	<u>.1468</u>	.1556	.2494	.2460	.1519	<u>.1536</u>	
	192	720	.2197	.3453	.3192	.2110	<u>.2158</u>	.1782	.3152	.2962	.1762	<u>.1778</u>	.1943	.3261	.3086	.1892	<u>.1925</u>	
ETTh1	336	336	<u>.2070</u>	.2986	.3005	.2021	<u>.2108</u>	.1469	.2366	.2375	.1447	<u>.1468</u>	.1722	.2579	.2604	.1645	<u>.1695</u>	
	336	720	<u>.3334</u>	.4253	.4355	.3255	<u>.3334</u>	.1807	.3101	.3004	.1776	<u>.1798</u>	.1969	.3130	.3124	.1920	<u>.1949</u>	
	96	24	.2543	.2359	.2429	<u>.2405</u>	.2450	.2578	.2616	.2599	.2523	<u>.2569</u>	.2494	.2503	<u>.2471</u>	.2449	<u>.2492</u>	
	96	48	.3305	.3099	.3135	<u>.3115</u>	.3133	.3105	.3167	.3151	.3035	<u>.3064</u>	.3191	.3269	.3222	.3171	<u>.3177</u>	
	192	192	.3800	.4006	.3961	.3591	<u>.3603</u>	.3694	.4029	.3942	.3643	<u>.3648</u>	.3551	.3863	.3815	.3524	<u>.3528</u>	
	192	336	.4336	.4499	.4401	.4149	<u>.4150</u>	.4239	.4620	.4436	.4162	<u>.4169</u>	.4036	.4371	.4290	.3985	<u>.3987</u>	
ETTh2	192	720	.4992	.5385	.5090	.4716	<u>.4718</u>	.4797	.5376	.5101	.4671	<u>.4681</u>	.4631	.5152	.4941	.4550	<u>.4560</u>	
	336	336	.4820	.4913	.4441	<u>.4490</u>	.4592	.3981	.4444	.4244	.3968	<u>.3977</u>	.4011	.4380	.4275	.3975	<u>.4006</u>	
	336	720	.5202	.5432	.5169	.4678	<u>.4904</u>	.4437	.5053	.4852	.4256	<u>.4423</u>	.4407	.5046	.4877	.4261	<u>.4397</u>	
	96	24	.0542	.0800	.0744	.0530	<u>.0531</u>	.0601	.0782	.0777	.0598	<u>.0599</u>	<u>.0562</u>	.0748	.0741	.0561	<u>.0561</u>	
	96	48	.0735	.1044	.0988	.0731	<u>.0732</u>	.0767	.1027	.1015	.0761	<u>.0762</u>	.0736	.0992	.0987	.0734	<u>.0733</u>	
	192	192	.1035	.1647	.1601	.1023	<u>.1022</u>	.0990	.1451	.1429	.0984	<u>.0985</u>	.0998	.1480	.1456	.0982	<u>.0984</u>	
Exchange Rate	192	336	.1343	.2191	.1970	.1339	<u>.1335</u>	.1201	.1791	.1741	.1190	<u>.1195</u>	.1210	.1863	.1781	.1200	<u>.1192</u>	
	192	720	.1628	.2511	.2377	.1564	<u>.1589</u>	.1518	.2291	.2247	.1473	<u>.1498</u>	.1476	.2337	.2232	.1436	<u>.1446</u>	
	336	336	.1354	.2280	.1987	.1328	<u>.1347</u>	.1176	.1782	.1704	.1167	<u>.1174</u>	.1198	.1815	.1760	.1172	<u>.1188</u>	
	336	720	.1645	.2785	.2517	.1455	<u>.1604</u>	.1456	.2338	.2185	.1317	<u>.1446</u>	.1490	.2309	.2255	.1289	<u>.1453</u>	
	96	24	.0318	<u>.0292</u>	.0273	.0306	.0306	.0434	<u>.0397</u>	.0393	.0434	.0283	<u>.0254</u>	.0241	.0283	<u>.0283</u>		
	96	48	.0526	.0542	.0479	<u>.0516</u>	.0606	.0590	.0579	.0606	.0606	.0481	<u>.0438</u>	.0418	.0480	<u>.0481</u>		
Weather	192	192	.2045	.1999	.2189	<u>.2040</u>	<u>.2040</u>	.1715	.1819	.2024	.1714	<u>.1715</u>	.1655	<u>.1728</u>	.1809	.1655	<u>.1655</u>	
	192	336	.2963	.3221	.3511	.2919	<u>.2933</u>	.2878	.3316	.3484	.2850	<u>.2875</u>	.2804	.3129	.3318	.2780	<u>.2802</u>	
	192	720	.8546	.7713	<u>.7828</u>	.8316	.8320	<u>.9037</u>	.9393	.9488	.9016	<u>.9016</u>	.4506	.8200	.8315	.4501	<u>.4501</u>	
	336	336	.4088	.3790	.4204	<u>.4036</u>	<u>.4036</u>	.2753	.3036	.3323	.2700	<u>.2751</u>	.3246	.3219	.3589	.3182	<u>.3245</u>	
	336	720	1.7882	1.0041	<u>1.0775</u>	1.5829	1.5828	<u>.5274</u>	.8620	.8816	.5269	<u>.5269</u>	<u>.4266</u>	.9353	.9175	.4263	<u>.4263</u>	
	96	24	.1095	<u>.1026</u>	.1016	.1077	.1077	.1207	.1151	.1151	.1200	<u>.1199</u>	.1193	.1085	<u>.1111</u>	.1183	<u>.1183</u>	
Weather	96	48	.1380	.1292	<u>.1310</u>	.1362	.1363	.1581	<u>.1499</u>	.1475	.1559	.1560	.1530	.1435	<u>.1452</u>	.1508	<u>.1510</u>	
	192	192	.2165	.2102	.2051	<u>.2075</u>	.2099	.2393	<u>.2225</u>	.2214	.2332	.2354	.2131	<u>.2058</u>	.2021	.2086	<u>.2108</u>	
	192	336	.2747	.2588	.2549	.2611	.2653	.2904	<u>.2709</u>	.2691	.2791	.2829	.2694	<u>.2547</u>	.2531	.2604	<u>.2637</u>	
	192	720	.3321	.3316	.3390	.3151	<u>.3211</u>	.3426	.3363	.3446	.3276	<u>.3339</u>	.3290	.3286	.3360	.3158	<u>.3205</u>	
	336	336	.2988	.2705	<u>.2708</u>	.2778	.2978	.2722	.2633	.2619	<u>.2627</u>	.2707	.2526	.2520	<u>.2474</u>	.2444	<u>.2504</u>	
	336	720	.3381	.3423	.3557	.2885	<u>.3340</u>	.3245	.3247	.3316	.2742	<u>.3207</u>	.3129	.3203	<u>.3229</u>	.2648	<u>.3088</u>	

Using the publicly available source codes, we evaluated SOLID on three base forecasting models: DLinear, FreTS, and iTransformer. The results are summarized in Table 8. Across all settings, COSA achieves higher predictive accuracy compared to SOLID.

Moreover, COSA is significantly more efficient: it requires only 7.44 ± 0.0488 seconds of wall-clock time on average, whereas SOLID incurs a much larger overhead with 306.55 ± 2.6183 seconds. The substantial cost of SOLID arises from computing context drift and repeatedly updating the prediction layer of the base model, processes that are far heavier than COSA’s lightweight updates. Because COSA freezes base model and updates only a compact output-space adapter, it offers a dramatically faster execution while maintaining higher accuracy.

F.4 COMPARISON WITH DYNATTA

This section presents complete baseline results of prediction accuracy comparison with various existing methods. DynaTTA requires setting a total of 15 hyperparameters, and due to this complexity, we report its performance using the best settings from our trials. The used hyperparameters of DynaTTA are as follows:

- HIDDEN_DIM=64, GATING_INIT=0.01, BASE_LR= 0.005, MSE_BUFFER_SIZE=100, RTAB_SIZE=50, RDB_SIZE=30, METRIC_HISTORY_SIZE=20, ALPHA_MIN=0.0001, ALPHA_MAX=0.01, KAPPA=2.0, ETA=0.1, EPS=1e-8, WARMUP_FACTOR=2, UPDATE_BUFFERS_INTERVAL=5, UPDATE_METRICS_INTERVAL=3

Table 8: Comparison with SOLID

		iTransformer		DLinear		FreTS	
		SOLID COSA-P		SOLID COSA-P		SOLID COSA-P	
ETTh1	96	.4404	.4363	.4595	.4574	.4093	.4371
	192	.4935	.4919	.5063	.5066	.4701	.4940
	336	.5420	.5300	.5602	.5528	.5254	.5467
	720	.6523	.5638	.7107	.6107	.6980	.6259
ETTh2	96	.2480	.2493	.2315	.2281	.2354	.2350
	192	.3061	.2947	.2824	.2819	.2830	.2972
	336	.3339	.3339	.3103	.3083	.3248	.3153
	720	.3701	.3591	.3136	.3477	.3167	.3399
ETTm1	96	.3353	.3455	.3634	.3456	.3121	.3525
	192	.4266	.4140	.4336	.4222	.4299	.4212
	336	.5019	.4643	.5071	.4858	.4915	.4775
	720	.5986	.5102	.5821	.4991	.5612	.4982
ETTm2	96	.1641	.1632	.1590	.1583	.1574	.1569
	192	.2291	.2173	.1910	.1943	.1933	.1934
	336	.2525	.2535	.2138	.2242	.2328	.2211
	720	.2704	.2606	.2419	.2316	.2377	.2314
Exchange Rate	96	.0873	.0837	.0913	.0834	.0822	.0766
	192	.1783	.1479	.1826	.1519	.1723	.1499
	336	.3294	.2624	.3276	.2480	.3218	.2461
	720	.7531	.4460	.8872	.4481	.8325	.4458
Weather	96	.1753	.1617	.1954	.1793	.1849	.1737
	192	.2231	.2088	.2403	.2217	.2309	.2189
	336	.2801	.2515	.2918	.2626	.2843	.2587
	720	.3450	.2730	.3643	.2708	.3561	.2692

Table 9: Prediction accuracy comparison with DynaTTA Grover & Etemad (2025).

		Transformer-based				Linear-based				MLP-based									
		iTransformer		PatchTST		DLinear		OLS		FreTS		MICN							
		DynaTTA	COSA-F	COSA-P	DynaTTA	COSA-F	COSA-P	DynaTTA	COSA-F	COSA-P	DynaTTA	COSA-F	COSA-P	DynaTTA	COSA-F	COSA-P			
ETTh1	96	4523	4368	4363	8371	4242	4238	4708	4574	4482	4486	4390	4372	4508	4384	4371	5063	4693	4684
	192	5175	4961	4919	8006	4830	4805	5321	5066	5050	5096	4915	4906	5139	4951	4940	5745	5372	5328
	336	5874	5651	5300	8097	5438	5320	5792	5528	5456	5626	5385	5320	5840	5467	5351	6594	5950	5878
	720	7123	5958	5638	10887	6113	5822	7112	6107	5896	6933	5969	5733	7095	6259	5959	8262	7001	6504
ETTh2	96	2630	2504	2493	4154	2349	2343	2338	2300	2281	2326	2232	2265	2395	2367	2350	2661	2492	2485
	192	3210	2983	2947	4315	2665	2608	2888	2827	2819	2911	2796	2791	2916	2816	2824	3417	3049	3017
	336	3677	3241	3339	4386	2971	2978	3380	3050	3083	3430	3003	3043	3474	3031	3153	3777	3241	3310
	720	4646	3487	3591	4991	3233	3428	4325	3062	3477	4270	3177	3453	4297	3169	3399	5229	3650	3885
ETTm1	96	3753	3447	3455	7205	3625	3626	3814	3456	3475	3830	3454	3475	3723	3520	3525	4095	3837	3831
	192	4835	4124	4140	6898	4250	4258	4809	4113	4122	4827	4115	4119	4811	4150	4212	5331	4476	4514
	336	5843	4569	4643	8073	4568	4697	5711	4753	4858	5719	4748	4749	5739	4661	4775	6418	4832	5054
	720	7243	4773	5102	9292	4681	4882	6569	4774	4991	6884	4763	5007	7152	4718	4982	6932	5029	5225
ETTm2	96	1832	1627	1632	2508	1558	1562	1640	1583	1586	1684	1582	1586	1661	1568	1569	2033	1702	1704
	192	2897	2171	2173	2744	2007	2022	2040	1904	1905	2115	1906	1907	2048	1905	1908	2349	2102	2120
	336	3246	2435	2535	3434	2258	2352	2908	2083	2242	2917	2131	2226	2778	2098	2211	2988	2337	2351
	720	5344	2477	2606	4447	2446	2645	3765	2215	2316	4571	2171	2349	4020	2158	2314	5362	2477	2643
Exchange Rate	96	0983	0818	0837	1217	0765	0788	0948	0812	0834	0918	0756	0773	0906	0744	0766	1210	0955	1008
	192	1970	1403	1479	2517	1464	1570	1975	1459	1519	1749	1393	1457	1871	1366	1499	2227	1663	1722
	336	3251	2089	2624	3728	1983	2445	3001	2039	2480	3024	2020	2323	3111	2053	2461	3536	2119	2660
	720	8790	3421	4460	9999	3543	4662	8812	3494	4481	8300	3444	4541	8348	3352	4458	8570	3871	4815
Weather	96	1823	1597	1617	2317	1624	1634	1950	1773	1793	1985	1772	1803	1937	1724	1737	2303	1636	1651
	192	2678	2067	2088	2611	2006	2108	3311	2216	2217	3074	2223	2237	2850	2135	2189	3839	2082	2120
	336	3894	2503	2515	3329	2451	2488	4103	2567	2626	9593	2851	2642	3970	2561	2587	5355	2729	2737
	720	4996	2480	2730	4067	2590	2713	4915	2581	2708	4974	2579	2708	5251	2573	2692	5772	2582	2855

F.5 COMPARISON WITH VARIOUS BATCH SIZES

Table 10a and Table 10b summarize the prediction accuracy and efficiency overhead under different batch sizes B . Thanks to CALR’s stability-induced design, COSA adapts reliably even with very small batches, and the resulting increase in update frequency often leads to improved forecasting accuracy. Notably, even in extremely small settings such as $B = 8$, COSA maintains higher accuracy than existing TTA methods, demonstrating resilience against over-correction and short-term perturbations. On the other hand, smaller B inevitably increases the number of adaptation steps, leading

Table 10: Performance comparison with different batch sizes B .

(a) Prediction accuracy.

	No TTA	TAFAS	PETSA	PAAS	8	16	24	48	96
96	0.2545	0.2471	0.2480	0.2409	0.1908	<u>0.2202</u>	0.2330	0.2398	0.2411
192	0.3144	0.3038	0.3046	0.2887	0.1900	<u>0.2295</u>	0.2524	0.2848	0.2946
336	0.3839	0.3653	0.3664	0.3280	0.1837	<u>0.2292</u>	0.2526	0.3013	0.3483
720	0.5539	0.5226	0.5232	0.3804	0.1811	<u>0.2384</u>	0.2672	0.3286	0.4158

(b) Wall-clock time (Seconds).

	TAFAS	PETSA	PAAS	8	16	24	48	96
96	<u>5.9271</u>	7.4129	7.0642	47.3922	25.6158	17.2297	9.6333	5.1258
192	<u>6.0383</u>	7.3675	7.1419	49.4422	25.1222	18.0969	9.4344	5.5133
336	<u>6.1554</u>	7.6588	7.4131	49.2211	25.1119	17.2906	9.5644	5.8081
720	6.5300	7.9867	8.1578	46.3711	24.4683	17.6253	10.3036	<u>6.5397</u>

to higher adaptation time and a clear computation–accuracy trade-off. Considering this trade-off, we adopt $B = 48$ for COSA-F in our main experiments, which provides a balanced choice between accuracy gains and computational efficiency.

G ADDITIONAL ABLATIONS

This section provides additional ablation studies on various design choices of COSA. Each experiment was conducted to understand the impact of specific components and determine optimal hyperparameters. The default setting uses mean-based context aggregation with $K = 10$ and $S = 3$.

G.1 CONTEXT BUILDING METHODS COMPARISON

G.1.1 STATISTICAL METHODS

This experiment was conducted to evaluate the impact of different context construction methods on adapter performance. We compared three methods, i.e., Mean, Median, and Weighted Average (WA), to find the optimal context construction strategy. The weight of WA was designed to assign greater weight to recent values using exponential decay weighting. Table 11 presents a comprehensive performance comparison of the three context construction methods.

Mean-based context construction demonstrated superior performance compared to median and weighted average approaches across most experimental configurations. While median-based aggregation provided robustness against outliers, it resulted in lower overall accuracy. The weighted average approach showed marginal improvements relative to its implementation complexity. These findings support the adoption of simple statistical aggregation for effective context summarization in COSA.

G.1.2 CONTEXT SELECTION STRATEGY

COSA aims not to model long-term time-series structure, but to perform fast and stable local residual correction for output bias observed in the current window. In non-stationary environments, the input distribution shifts continuously over time; thus, information from distant past windows may become misaligned with the current drift direction and deteriorate correction quality. For this reason, the default COSA employs a lightweight context vector constructed solely from the most recently observed batches.

To examine the effects of longer-range temporal patterns, we additionally implemented a Selective Context mechanism. This approach stores all past context values in a buffer and computes importance scores via attention between the current window and past contexts, selecting the top- K values

Table 11: Prediction accuracy comparison of diverse aggregation functions.

		Transformer-based						Linear-based						MLP-based					
		iTransformer			PatchTST			DLinear			OLS			FreTS			MICN		
		Mean	Median	WA	Mean	Median	WA	Mean	Median	WA	Mean	Median	WA	Mean	Median	WA	Mean	Median	WA
ETTh1	96	.4327	.4472	.4472	.4092	.4274	.4275	.4615	.4660	.4657	.4359	.4463	.4462	.4362	.4439	.4440	.4704	.4934	.4926
	192	.4491	.4850	.4870	.4422	.4778	.4770	.4869	.5090	.5111	.4932	.4897	.4894	.4671	.4893	.4954	.4769	.5567	.5568
	336	.4476	.5301	.5317	.4550	.5199	.5285	.4632	.5379	.5378	.5188	.5208	.5209	.4411	.5273	.5245	.4814	.5889	.5904
	720	.4592	.6237	.6251	.4788	.6329	.6335	.4777	.6358	.6376	.5616	.6243	.6242	.4755	.6439	.6428	.5230	.7196	.7181
ETTh2	96	.2489	.2532	.2536	.2336	.2346	.2358	.2303	.2352	.2324	.2283	.2300	.2299	.2359	.2379	.2382	.2468	.2566	.2568
	192	.3003	.3012	.3013	.2708	.2886	.2894	.2682	.2846	.2863	.2762	.2954	.2893	.2766	.2846	.2917	.2906	.3190	.3145
	336	.3277	.3671	.3685	.2688	.3190	.3202	.2860	.3283	.3285	.2937	.3030	.3025	.2889	.3214	.3205	.3088	.3429	.3426
	720	.3311	.4013	.4023	.3091	.3737	.3737	.3006	.3358	.3358	.2992	.3415	.3415	.2979	.3588	.3564	.3454	.4172	.4185
ETTm1	96	.3428	.3687	.3685	.3604	.3918	.3921	.3453	.3575	.3574	.3440	.3573	.3572	.3522	.3633	.3633	.3804	.4252	.4248
	192	.4076	.4307	.4304	.4171	.4398	.4398	.4158	.4266	.4265	.4125	.4265	.4263	.4173	.4257	.4266	.4402	.4742	.4740
	336	.4663	.4930	.4949	.4662	.4942	.4944	.4784	.5009	.5005	.4700	.4995	.5006	.4771	.4898	.4886	.4937	.5381	.5381
	720	.4940	.5614	.5615	.4776	.5359	.5316	.4928	.5640	.5603	.4693	.5638	.5653	.4863	.5414	.5419	.5083	.5830	.5838
ETTm2	96	.1616	.1672	.1653	.1552	.1591	.1595	.1578	.1594	.1596	.1583	.1596	.1600	.1556	.1592	.1594	.1710	.1712	.1723
	192	.2172	.2194	.2240	.1989	.2087	.2121	.1900	.1959	.1957	.1919	.1970	.1995	.1908	.1935	.1933	.2102	.2131	.2132
	336	.2402	.2700	.2762	.2279	.2821	.2543	.2135	.2448	.2561	.2066	.2499	.2477	.2158	.2353	.2420	.2354	.2523	.2546
	720	.2550	.3461	.3463	.2397	.3011	.3222	.2357	.2985	.2833	.2104	.3179	.2821	.2360	.2732	.2753	.2510	.3020	.3084
Exchange Rate	96	.0843	.0852	.0852	.0803	.0814	.0815	.0843	.0884	.0885	.0728	.0787	.0787	.0790	.0785	.0785	.0980	.1065	.1068
	192	.1540	.1606	.1607	.1480	.1544	.1546	.1599	.1653	.1654	.1335	.1507	.1509	.1390	.1500	.1502	.1827	.1870	.1872
	336	.2588	.2754	.2756	.2611	.2787	.2789	.2565	.2918	.2920	.1833	.2736	.2738	.2511	.2683	.2684	.2660	.3040	.3043
	720	.5039	.5113	.5115	.4937	.5076	.5078	.5001	.5267	.5270	.3349	.4983	.4986	.4789	.4977	.4980	.4815	.5806	.5809
Weather	96	.1636	.1726	.1726	.1655	.1731	.1735	.1738	.1931	.1931	.1748	.1934	.1934	.1758	.1831	.1835	.1666	.1739	.1738
	192	.2073	.2268	.2265	.2052	.2162	.2162	.2217	.2500	.2520	.2144	.2496	.2490	.2151	.2346	.2347	.2060	.2208	.2205
	336	.2474	.2707	.2707	.2443	.2668	.2660	.2622	.2891	.2885	.2428	.2911	.2897	.2630	.2736	.2735	.2735	.2650	.2648
	720	.2907	.3118	.3119	.2682	.3088	.3090	.2713	.3310	.3325	.2487	.3327	.3331	.2583	.3268	.3247	.2670	.3140	.3094
Average		.3121	.3450	.3458	.3032	.3364	.3366	.3097	.3423	.3422	.2990	.3371	.3354	.3046	.3334	.3340	.3284	.3669	.3670

to form the context vector. Such a mechanism can leverage repeated phases or cycles in datasets with strong periodicity.

Table 12a compares COSA (the standard recent-context construction) with the dynamic context selection method. While the dynamic context selection method achieves clear improvements on datasets such as ETT, where the periodic structure is strong and easily detectable, the overall performance of the original COSA remains superior. Selective Context also introduces non-trivial overhead, since computing importance scores increases both adaptation time and inference time. Moreover, in fully non-stationary settings where distributional characteristics change continuously, older contexts may become outdated and destabilize the correction process. Nonetheless, the observed gains on datasets with pronounced periodicity show the potential of Selective Context. We provide a more detailed discussion of these observations in Section H.

G.1.3 COMPARISON WITH ENCODER-BASED CONTEXT

To compare with encoder-based context construction, we implemented an alternative approach that replaces the original statistics-based method in COSA with a temporal encoder that directly consumes the previously observed ground-truth sequence from the past 720 steps (the longest L). We added RNN-, LSTM-, and Attention-based encoders, each taking the past sequence in the form of $[720, 1]$ as input and producing a $[K, 1]$ context vector. The resulting context vector is concatenated with the base model’s prediction output, just as in the original design, and then fed into the linear correction layer. The encoder is seamlessly integrated at the front of COSA, modifying only the context-generation stage while keeping the remaining components unchanged.

Table 13 shows that, except for a few isolated cases, the original statistics-based context (0.3240) performs better than encoder-based alternatives (0.3254, 0.3260, 0.3278). Furthermore, the added architectural complexity increases both adaptation and inference overhead. In non-stationary TTA settings, where the input distribution shifts rapidly and adaptation steps are short, it is difficult for an encoder to learn stable temporal representations. Consequently, the generated embeddings may become misaligned with the current drift direction or overfit to outdated historical patterns, ultimately degrading correction performance.

Table 12: Prediction accuracy and overhead of selective context.

(a) Prediction accuracy.

		Transformer-based				Linear-based				MLP-based			
		iTransformer		PatchTST		DLinear		OLS		FreTS		MICN	
		Recent	Selective	Recent	Selective	Recent	Selective	Recent	Selective	Recent	Selective	Recent	Selective
ETTh1	96	.4363	.4362	.4238	.4234	.4482	.4562	.4372	.4359	.4371	.4361	.4684	.4673
	192	.4919	.4927	.4805	.4848	.5050	.5088	.4906	.4933	.4940	.4965	.5328	.5368
	336	.5300	.5367	.5320	.5310	.5456	.5541	.5320	.5368	.5351	.5505	.5878	.5966
	720	.5638	.5671	.5822	.5881	.5896	.6180	.5733	.6093	.5959	.6430	.6504	.7137
ETTh2	96	.2493	.2494	.2343	.2349	.2281	.2258	.2265	.2262	.2350	.2346	.2485	.2486
	192	.2947	.2942	.2608	.2661	.2819	.2813	.2791	.2825	.2824	.2945	.3017	.3027
	336	.3339	.3367	.2978	.2949	.3083	.3064	.3043	.3027	.3153	.3175	.3310	.3328
	720	.3591	.3603	.3428	.3453	.3477	.3462	.3453	.3619	.3399	.3509	.3885	.3906
ETTm1	96	.3455	.3440	.3626	.3627	.3475	.3456	.3475	.3454	.3525	.3522	.3831	.3815
	192	.4140	.4128	.4258	.4278	.4122	.4221	.4119	.4219	.4212	.4212	.4514	.4533
	336	.4643	.4718	.4697	.4693	.4858	.4857	.4749	.4854	.4775	.4805	.5054	.5060
	720	.5102	.5246	.4882	.4868	.4991	.5065	.5007	.5005	.4982	.4970	.5225	.5256
ETTm2	96	.1632	.1631	.1562	.1560	.1586	.1582	.1586	.1581	.1569	.1570	.1704	.1705
	192	.2173	.2165	.2022	.2011	.1905	.1930	.1907	.1952	.1908	.1929	.2120	.2125
	336	.2535	.2551	.2352	.2331	.2242	.2245	.2226	.2212	.2211	.2185	.2351	.2555
	720	.2606	.2578	.2645	.2633	.2316	.2427	.2349	.2368	.2314	.2373	.2643	.2764
Exchange Rate	96	.0837	.0835	.0788	.0789	.0834	.0834	.0773	.0773	.0766	.0763	.1008	.1007
	192	.1479	.1516	.1570	.1554	.1519	.1543	.1457	.1462	.1499	.1514	.1722	.1770
	336	.2624	.2633	.2445	.2478	.2480	.2481	.2323	.2361	.2461	.2541	.2660	.2732
	720	.4460	.4749	.4662	.4983	.4481	.4984	.4541	.4835	.4458	.4914	.4815	.5255
Weather	96	.1617	.1616	.1634	.1631	.1793	.1790	.1803	.1799	.1737	.1731	.1651	.1654
	192	.2088	.2056	.2108	.2109	.2217	.2181	.2237	.2222	.2189	.2187	.2120	.2134
	336	.2515	.2524	.2488	.2554	.2626	.2665	.2642	.2659	.2587	.2603	.2737	.2813
	720	.2730	.2798	.2713	.2798	.2708	.2729	.2708	.2721	.2692	.2732	.2855	.2970

(b) Overhead analysis.

Method	# Params ↓	Adaptation time/batch (ms) ↓	Inference time/batch (ms) ↓	Average MSE ↓
Recent	1,211,287	80.12 ± 13.58	1.25 ± .0984	.3240
Selective	1,212,217	83.64 ± 15.71	1.26 ± .1039	.3287

These findings confirm that the statistics-based context remains the most robust and stable choice for non-stationary adaptation, while encoder-based context generation still demonstrates potential. We discuss these observations in greater detail in Section H.

G.2 INPUT CALIBRATION EFFECTS

COSA performs residual correction directly in the output space, and we demonstrated that output-only correction is often sufficient. However, in certain time series, we observe that input-level spikes or local noise degrade the base model’s predictions first, and this degradation subsequently propagates to the residual correction stage. To examine how such input perturbations influence the overall correction process, we conducted experiments combining COSA with the input-side GCM module from TAFAS. Table 14 reports the results.

In most cases, output-only correction achieves higher predictive accuracy. However, for datasets such as ETTh1, ETTh2, and ETTh2, where significant input noise is present, the combination with GCM produces improved results. In these cases, input GCM smooths the noisy input patterns, allowing the base model to generate more stable predictions, which in turn enhances the effectiveness of COSA.

Nevertheless, because GCM operates via distribution-shift normalization, it risks oversmoothing or removing meaningful drift signals when the input exhibits rapid or irregular changes. This behavior explains why, on average (in terms of MSE), output-only correction remains more stable across diverse non-stationary scenarios. Overall, when input disturbances are not the primary source of prediction error, output-only correction is the most robust and reliable option.

Table 13: Prediction accuracy and overhead comparison with encoder-based context.

(a) Prediction accuracy.

		Transformer-based						Linear-based						MLP-based					
		iTransformer						DLinear						FreTS					
		CALR	Cosine	Exp	Fixed	Plateau	Step	CALR	Cosine	Exp	Fixed	Plateau	Step	CALR	Cosine	Exp	Fixed	Plateau	Step
ETTh1	96	.4363	.4858	.4961	.4848	.4848	.4885	.4482	.4498	.4556	.4513	.4513	.4537	.4371	.4400	.4441	.4398	.4398	.4405
	192	.4919	.5405	.5613	.5413	.5413	.5426	.5050	.5069	.5183	.5090	.5090	.5110	.4914	.5002	.4915	.4915	.4915	.4931
	336	.5300	.5741	.5952	.5751	.5751	.5826	.5456	.5560	.5714	.5586	.5586	.5642	.5351	.5429	.5570	.5442	.5442	.5494
	720	.5638	.6216	.6835	.6163	.6163	.6336	.5896	.6033	.6511	.5953	.5953	.6166	.5959	.6116	.6593	.6041	.6041	.6200
ETTh2	96	.2493	.2984	.3021	.2984	.2984	.2987	.2281	.2308	.2287	.2321	.2321	.2333	.2350	.2378	.2359	.2376	.2376	.2372
	192	.2947	.3386	.3520	.3399	.3400	.3394	.2819	.2823	.2811	.2836	.2836	.2845	.2824	.2837	.2827	.2834	.2834	.2831
	336	.3339	.3823	.3992	.3856	.3856	.3802	.3083	.3078	.3093	.3104	.3105	.3081	.3153	.3115	.3151	.3131	.3131	.3087
	720	.3591	.4094	.4278	.4113	.4113	.4070	.3477	.3490	.3562	.3462	.3463	.3488	.3399	.3421	.3524	.3391	.3389	.3387
ETTm1	96	.3455	.4006	.4087	.3978	.3978	.4048	.3475	.3501	.3610	.3497	.3497	.3569	.3525	.3548	.3567	.3539	.3539	.3555
	192	.4140	.4650	.4772	.4630	.4630	.4683	.4122	.4140	.4283	.4146	.4146	.4191	.4212	.4236	.4279	.4231	.4230	.4246
	336	.4643	.5110	.5286	.5100	.5100	.5160	.4858	.4828	.5028	.4838	.4838	.4875	.4775	.4740	.4821	.4740	.4740	.4750
	720	.5102	.5321	.5732	.5350	.5349	.5392	.4991	.4861	.5153	.4889	.4889	.4915	.4982	.4923	.5073	.4950	.4950	.4951
ETTm2	96	.1632	.2138	.2140	.2139	.2139	.2136	.1586	.1621	.1591	.1629	.1629	.1646	.1569	.1611	.1572	.1604	.1604	.1606
	192	.2173	.2697	.2705	.2692	.2693	.2704	.1905	.1948	.1916	.1955	.1956	.1973	.1908	.1958	.1921	.1951	.1951	.1955
	336	.2535	.3028	.3125	.3047	.3045	.3065	.2242	.2305	.2268	.2310	.2310	.2324	.2211	.2285	.2247	.2276	.2276	.2278
	720	.2606	.3000	.3159	.2987	.2986	.2966	.2316	.2369	.2383	.2405	.2405	.2348	.2314	.2388	.2397	.2405	.2403	.2334
Exchange Rate	96	.0837	.1335	.1344	.1335	.1335	.1334	.0834	.0865	.0848	.0873	.0873	.0886	.0766	.0800	.0775	.0794	.0794	.0792
	192	.1479	.1961	.2025	.1960	.1960	.1952	.1519	.1523	.1552	.1533	.1533	.1542	.1499	.1518	.1545	.1513	.1513	.1505
	336	.2624	.3120	.3495	.3116	.3117	.3102	.2480	.2521	.2710	.2528	.2527	.2535	.2461	.2501	.2735	.2491	.2492	.2484
	720	.4460	.4481	.6222	.4498	.4460	.4448	.4481	.4185	.5919	.4164	.4162	.4179	.4458	.4128	.5679	.4072	.4063	.4068
Weather	96	.1617	.2118	.2151	.2115	.2115	.2123	.1793	.1824	.1827	.1827	.1827	.1858	.1737	.1770	.1767	.1761	.1761	.1776
	192	.2088	.2514	.2592	.2517	.2517	.2517	.2217	.2226	.2270	.2232	.2232	.2259	.2189	.2201	.2235	.2191	.2191	.2192
	336	.2515	.2916	.3063	.2949	.2948	.2920	.2626	.2510	.2622	.2532	.2532	.2541	.2587	.2497	.2606	.2505	.2505	.2496
	720	.2730	.3230	.3460	.3225	.3225	.3267	.2708	.2774	.2965	.2802	.2802	.2810	.2692	.2726	.2921	.2755	.2755	.2725

(b) Overhead analysis.

Method	# Params	↓ Adaptation time/batch (ms)	↓ Inference time/batch (ms)	↓ Average MSE
Recent	1,211,287	80.12 ± 13.58	1.25 ± .0984	.3240
Selective	1,212,217	83.64 ± 15.71	1.26 ± .1039	.3287

Table 14: COSA with input GCM.

		Transformer-based				Linear-based				MLP-based			
		iTransformer		PatchTST		DLinear		OLS		FreTS		MICN	
		COSA	w. Input	COSA	w. Input	COSA	w. Input	COSA	w. Input	COSA	w. Input	COSA	w. Input
ETTh1	96	.4363	.4362	.4238	.4209	.4482	.4460	.4372	.4370	.4371	.4343	.4684	.4852
	192	.4919	.4821	.4805	.4790	.5050	.4995	.4906	.4907	.4940	.4919	.5328	.5530
	336	.5300	.5386	.5320	.5216	.5456	.5359	.5320	.5193	.5351	.5286	.5878	.5953
	720	.5638	.6287	.5822	.6386	.5896	.6513	.5733	.6500	.5959	.6726	.6504	.7509
ETTh2	96	.2493	.2001	.2343	.1845	.2281	.1819	.2265	.1803	.2350	.1849	.2485	.1995
	192	.2947	.2384	.2608	.2287	.2819	.2217	.2791	.2292	.2824	.2241	.3017	.2457
	336	.3339	.2528	.2978	.2405	.3083	.2506	.3043	.2474	.3153	.2539	.3310	.2755
	720	.3591	.3048	.3428	.2913	.3477	.2932	.3453	.2940	.3399	.2954	.3885	.3411
ETTm1	96	.3455	.3676	.3626	.3903	.3475	.3518	.3475	.3516	.3525	.3596	.3831	.4216
	192	.4140	.4273	.4258	.4396	.4122	.4194	.4119	.4192	.4212	.4200	.4514	.4742
	336	.4643	.4963	.4697	.4881	.4858	.4924	.4749	.4926	.4775	.4885	.5054	.5365
	720	.5102	.5869	.4882	.5317	.4991	.5678	.5007	.5598	.4982	.5452	.5225	.5920
ETTm2	96	.1632	.1242	.1562	.1200	.1586	.1217	.1586	.1218	.1569	.1203	.1704	.1288
	192	.2173	.1673	.2022	.1551	.1905	.1502	.1907	.1501	.1908	.1491	.2120	.1618
	336	.2535	.2017	.2352	.1900	.2242	.1813	.2226	.1831	.2211	.1823	.2351	.1975
	720	.2606	.2554	.2645	.2468	.2316	.2465	.2349	.2531	.2314	.2364	.2643	.2635
Exchange Rate	96	.0837	.0859	.0788	.0835	.0834	.0883	.0773	.0789	.0766	.0798	.1008	.1105
	192	.1479	.1706	.1570	.1754	.1519	.1807	.1457	.1644	.1499	.1660	.1722	.2083
	336	.2624	.2974	.2445	.3017	.2480	.2986	.2323	.2937	.2461	.2951	.2660	.3358
	720	.4460	.5884	.4662	.5969	.4481	.6107	.4541	.5837	.4458	.5823	.4815	.6885
Weather	96	.1617	.1723	.1634	.1728	.1793	.1924	.1803	.1927	.1737	.1822	.1651	.1741
	192	.2088	.2214	.2108	.2181	.2217	.2363	.2237	.2367	.2189	.2269	.2120	.2289
	336	.2515	.2752	.2488	.2809	.2626	.2951	.2642	.2946	.2587	.2845	.2737	.2728
	720	.2730	.3274	.2713	.3316	.2708	.3356	.2708	.3361	.2692	.3298	.2855	.3364

G.3 ADAPTER ARCHITECTURE COMPARISON

This experiment was conducted to compare the performance and computational efficiency of single linear adapters versus 2-layer MLP adapters with 64 hidden dimensions. We aimed to determine

Table 15: Prediction accuracy comparison of single linear adapter and 2-layer MLP adapter.

	Transformer-based						Linear-based						MLP-based												
	iTransformer	PatchTST	DLinear	OLS	FreTS	MICN	iTransformer	PatchTST	DLinear	OLS	FreTS	MICN	iTransformer	PatchTST	DLinear	OLS	FreTS	MICN							
	Linear	MLP	Linear	MLP	Linear	MLP	Linear	MLP	Linear	MLP	Linear	MLP	Linear	MLP	Linear	MLP	Linear	MLP							
ETH1	96	.4363	.4376	.4238	.4267	.4482	.4644	.4372	.4460	.4371	.4412	.4684	.4841	2.35	3.79	2.35	3.83	2.24	3.45	2.15	3.10	2.14	3.49	2.38	3.84
	192	.4919	.4968	.4805	.4857	.5050	.5135	.4906	.4980	.4940	.4967	.5328	.5496	2.39	3.73	2.44	3.83	2.23	3.49	2.21	3.42	2.16	3.47	2.59	3.83
	336	.5300	.5471	.5320	.5294	.5456	.5501	.5320	.5282	.5351	.5346	.5878	.6067	2.40	3.68	2.43	3.77	2.22	3.53	2.18	3.45	2.32	3.40	2.51	3.91
	720	.5638	.6167	.5822	.6350	.5896	.6498	.5733	.6351	.5959	.6558	.6504	.7325	2.39	3.46	2.25	3.49	2.17	3.10	2.23	3.22	2.24	3.11	3.69	4.57
ETH2	96	.2493	.2517	.2343	.2339	.2281	.2299	.2265	.2269	.2350	.2350	.2485	.2517	2.38	3.76	2.36	3.63	2.19	3.49	2.19	3.43	1.54	3.47	2.37	3.81
	192	.2947	.2981	.2608	.2825	.2819	.2828	.2791	.2781	.2824	.2767	.3017	.3094	2.40	3.74	2.44	3.80	2.28	3.51	2.20	3.41	2.24	3.43	2.66	3.85
	336	.3339	.3306	.2978	.3127	.3083	.3106	.3043	.3113	.3153	.3168	.3310	.3484	2.48	3.71	2.45	3.77	2.25	3.49	2.17	3.38	2.30	3.47	2.87	3.95
	720	.3591	.3931	.3428	.3837	.3477	.3689	.3453	.3750	.3399	.3660	.3885	.4170	2.34	3.40	2.35	3.48	2.21	3.33	2.18	3.24	2.19	3.19	3.72	4.62
ETTh1	96	.3455	.3522	.3626	.3680	.3475	.3505	.3475	.3489	.3525	.3577	.3831	.3914	8.49	14.08	8.56	14.24	8.14	11.50	8.17	13.16	8.22	13.22	8.33	14.38
	192	.4140	.4103	.4258	.4246	.4122	.4147	.4119	.4137	.4212	.4168	.4514	.4470	8.72	14.41	8.67	14.31	8.35	13.25	5.68	13.38	8.57	13.68	9.27	14.39
	336	.4643	.4625	.4697	.4709	.4858	.4678	.4749	.4680	.4775	.4708	.5054	.4784	9.07	14.62	9.03	12.04	8.72	13.59	8.86	13.31	8.87	14.17	10.86	15.26
	720	.5102	.4927	.4882	.4651	.4991	.4763	.5007	.4774	.4982	.4814	.5225	.4888	9.64	15.32	8.72	12.74	9.32	14.00	9.36	14.31	9.60	14.62	16.05	20.23
ETTh2	96	.1632	.1632	.1562	.1569	.1586	.1582	.1586	.1587	.1569	.1571	.1704	.1703	8.51	11.73	8.72	14.41	8.34	13.23	8.06	13.04	8.45	9.13	8.25	14.35
	192	.2173	.2140	.2022	.1978	.1905	.1880	.1907	.1884	.1908	.1850	.2120	.2039	8.75	14.35	8.77	14.38	8.32	13.31	5.27	13.28	8.51	13.65	9.32	14.42
	336	.2535	.2412	.2352	.2283	.2242	.2103	.2226	.2142	.2211	.2092	.2351	.2331	8.10	14.64	9.10	14.56	8.84	13.50	8.89	13.57	8.86	13.64	10.80	15.24
	720	.2606	.2759	.2645	.2711	.2316	.2532	.2349	.2551	.2314	.2477	.2643	.2709	7.74	15.14	9.51	15.04	9.29	13.86	9.32	14.26	9.50	14.48	16.04	20.21
Exchange Rate	96	.0837	.0869	.0788	.0838	.0834	.0890	.0773	.0789	.0766	.0803	.1008	.1106	1.38	2.01	1.38	1.99	1.22	1.79	1.20	1.77	1.26	1.81	1.39	2.00
	192	.1479	.1730	.1570	.1696	.1519	.1761	.1457	.1570	.1499	.1603	.1722	.1956	1.31	1.89	1.36	1.88	1.17	1.68	1.15	1.69	1.17	1.70	1.42	1.96
	336	.2624	.3103	.2445	.2941	.2480	.2872	.2323	.2856	.2461	.2910	.2660	.3399	1.26	1.70	1.32	1.81	1.09	1.57	1.10	1.58	1.10	1.62	1.48	1.60
	720	.4460	.8099	.4662	.8268	.4481	.8373	.4541	.7980	.4458	.7983	.4815	.9665	1.09	1.47	1.09	1.43	.91	1.24	.90	1.26	.93	1.27	1.46	1.76
Weather	96	.1617	.1691	.1634	.1691	.1793	.1904	.1803	.1904	.1737	.1767	.1651	.1703	13.05	20.86	15.19	23.35	12.81	20.34	12.76	18.41	12.84	20.90	12.88	20.56
	192	.2088	.2045	.2108	.2026	.2217	.2285	.2237	.2224	.2189	.2120	.2120	.2070	13.33	20.79	15.33	23.72	13.10	20.43	12.89	20.55	13.12	20.72	13.92	20.44
	336	.2515	.2390	.2488	.2360	.2626	.2469	.2642	.2499	.2587	.2440	.2737	.2386	13.69	21.12	15.93	24.21	13.49	20.83	13.43	20.98	13.53	20.96	14.31	22.14
	720	.2730	.2752	.2713	.2660	.2708	.2764	.2708	.2785	.2692	.2737	.2855	.2582	14.68	17.06	16.71	25.44	14.05	21.26	14.36	21.61	14.41	21.81	18.09	26.57
Average	.3218	.3438	.3166	.3383	.3196	.3425	.3158	.3368	.3176	.3369	.3421	.3696		6.16	9.60	6.60	10.21	6.04	9.28	5.79	9.28	6.09	9.35	7.36	10.75

whether more complex architectures necessarily guarantee better performance. Table 15 provides a comprehensive performance and efficiency comparison between linear and MLP adapters.

The comparative analysis reveals that single linear adapters achieve performance comparable to or superior to 2-layer MLP adapters while requiring significantly reduced computational resources. Although MLP adapters occasionally demonstrated slight performance improvements, the $1.5\sim 2\times$ computational overhead renders them impractical for real-time adaptation scenarios. These results validate the architectural design principle of COSA that emphasizes simplicity without compromising effectiveness.

G.4 COMPARISON WITH VARIOUS LEARNING-RATE SCHEDULERS

To validate the effectiveness of CALR, we compared it against several official PyTorch learning-rate schedulers: CosineAnnealingLR, ExponentialLR, ReduceLROnPlateau, StepLR, and a fixed learning rate. All schedulers were configured with the same base learning rate of 0.005 for a fair comparison. One-Cycle, although widely used, was excluded because it requires a predefined learning-rate schedule; in a streaming TTA scenario where samples arrive continuously and the batch size changes dynamically under PAAS, such predefinition is not feasible.

As summarized in Table 16, each scheduler achieves improvements in some individual cases. However, when results are averaged across all datasets and prediction lengths, the proposed CALR achieves the best or second-best accuracy in the vast majority of settings. These findings support CALR’s stability-induced design and its suitability for non-stationary TTA environments.

G.5 EXTENTION TO MULTIVARIATE TIME-SERIES FORECASTING

COSA is originally introduced as an output-space residual correction module, treating each variable as an independent univariate forecasting task, for fair comparison with existing SOTA methods that assume univariate forecasting. However, in real multivariate time-series settings, correlations among variables may influence drift patterns, suggesting that modeling cross-variable interactions could potentially benefit COSA. Basically, can be extended to multivariate forecasting; to examine this possibility, we implemented it.

We first incorporate *Cross-Variable Context Attention*, allowing the context of each variable to reference information from other variables and thereby capture correlation-driven contextual interactions. Additionally, we introduce a mixed structure composed of a low-rank shared component and variable-specific components: the shared component captures drift patterns common across variables

Table 16: Prediction accuracy comparison with various learning rate schedulers.

		Transformer-based					Linear-based					MLP-based				
		iTransformer					DLinear					FreTS				
		CALR	Cosine	Exp	Fixed Plateau	Step	CALR	Cosine	Exp	Fixed Plateau	Step	CALR	Cosine	Exp	Fixed Plateau	Step
ETTh1	96	.4363	.4858	.4961	.4848	.4885	.4482	.4498	.4556	.4513	.4537	.4371	.4400	.4441	.4398	.4398
	192	.4919	.5405	.5613	.5413	.5413	.5050	.5069	.5183	.5090	.5090	.4914	.5002	.4915	.4915	.4931
	336	.5300	.5741	.5952	.5751	.5751	.5456	.5560	.5714	.5586	.5586	.5351	.5429	.5570	.5442	.5494
	720	.5638	.6216	.6835	.6163	.6163	.5896	.6033	.6511	.5953	.5953	.5959	.6116	.6593	.6041	.6200
ETTh2	96	.2493	.2984	.3021	.2984	.2984	.2281	.2308	.2287	.2321	.2321	.2350	.2378	.2359	.2376	.2372
	192	.2947	.3386	.3520	.3399	.3400	.2819	.2823	.2811	.2836	.2836	.2824	.2837	.2827	.2834	.2831
	336	.3339	.3823	.3992	.3856	.3856	.3802	.3803	.3078	.3093	.3104	.3105	.3081	.3153	.3115	.3131
	720	.3591	.4094	.4278	.4113	.4113	.4070	.3477	.3490	.3562	.3462	.3463	.3488	.3399	.3421	.3389
ETTm1	96	.3455	.4006	.4087	.3978	.3978	.3475	.3501	.3610	.3497	.3497	.3525	.3548	.3567	.3539	.3539
	192	.4140	.4650	.4772	.4630	.4630	.4283	.4146	.4146	.4146	.4146	.4212	.4236	.4279	.4231	.4246
	336	.4643	.5110	.5286	.5100	.5100	.4858	.4828	.5028	.4838	.4838	.4875	.4775	.4740	.4821	.4740
	720	.5102	.5321	.5732	.5350	.5349	.5392	.4991	.4861	.5153	.4889	.4889	.4915	.4982	.4923	.5073
ETTm2	96	.1632	.2138	.2140	.2139	.2139	.2136	.1586	.1621	.1591	.1629	.1629	.1569	.1611	.1572	.1604
	192	.2147	.2697	.2705	.2692	.2693	.2704	.1905	.1948	.1916	.1955	.1956	.1973	.1908	.1958	.1921
	336	.2535	.3028	.3125	.3047	.3045	.3065	.2242	.2305	.2268	.2310	.2310	.2324	.2211	.2285	.2247
	720	.2606	.3000	.3159	.2987	.2986	.2966	.2316	.2369	.2383	.2405	.2405	.2348	.2314	.2388	.2397
Exchange Rate	96	.0837	.1335	.1344	.1335	.1335	.1334	.0834	.0865	.0848	.0873	.0873	.0886	.0766	.0800	.0775
	192	.1479	.1961	.2025	.1960	.1960	.1952	.1519	.1523	.1552	.1533	.1533	.1542	.1499	.1518	.1545
	336	.2624	.3120	.3495	.3116	.3117	.3102	.2480	.2521	.2710	.2528	.2527	.2535	.2461	.2501	.2735
	720	.4460	.4481	.6222	.4498	.4460	.4448	.4481	.4185	.5919	.4164	.4162	.4179	.4458	.4128	.5679
Weather	96	.1617	.2118	.2151	.2115	.2115	.2123	.1793	.1824	.1827	.1827	.1827	.1858	.1737	.1770	.1767
	192	.2088	.2514	.2592	.2517	.2517	.2217	.1905	.2226	.2270	.2232	.2232	.2259	.2189	.2201	.2235
	336	.2515	.2916	.3063	.2949	.2948	.2920	.2626	.2510	.2622	.2532	.2532	.2541	.2587	.2497	.2606
	720	.2730	.3230	.3460	.3225	.3225	.3267	.2708	.2774	.2965	.2802	.2802	.2810	.2692	.2726	.2921
		PatchTST					OLS					MICN				
		CALR	Cosine	Exp	Fixed Plateau	Step	CALR	Cosine	Exp	Fixed Plateau	Step	CALR	Cosine	Exp	Fixed Plateau	Step
		CALR	Cosine	Exp	Fixed Plateau	Step	CALR	Cosine	Exp	Fixed Plateau	Step	CALR	Cosine	Exp	Fixed Plateau	Step
ETTh1	96	.4238	.4723	.4294	.5723	.4923	.4232	.4372	.4375	.4448	.4401	.4401	.4684	.4739	.4904	.4708
	192	.4805	.5307	.4958	.6301	.5501	.4838	.4906	.4912	.5041	.4944	.4944	.4951	.5328	.5320	.5709
	336	.5320	.5851	.5535	.6826	.6026	.5396	.5320	.5342	.5515	.5384	.5384	.5424	.5878	.5864	.6417
	720	.5822	.6412	.6553	.7330	.6533	.6031	.5733	.5872	.6371	.5808	.5808	.5987	.6504	.6726	.8268
ETTh2	96	.2343	.2840	.2352	.3839	.3039	.2345	.2265	.2275	.2268	.2301	.2300	.2296	.2485	.2499	.2499
	192	.2608	.3114	.2641	.4092	.3292	.2617	.2791	.2804	.2804	.2828	.2828	.2823	.3017	.2990	.3077
	336	.2978	.3514	.3086	.4543	.3743	.2993	.3043	.3030	.3064	.3063	.3063	.3029	.3310	.3303	.3399
	720	.3428	.3913	.3663	.4951	.4151	.3485	.3453	.3487	.3589	.3473	.3472	.3476	.3885	.3965	.4019
ETTm1	96	.3626	.4104	.3741	.5183	.4383	.3655	.3475	.3487	.3608	.3495	.3495	.3552	.3831	.3912	.3982
	192	.4258	.4747	.4427	.5764	.4964	.4315	.4119	.4125	.4283	.4142	.4142	.4174	.4514	.4533	.4641
	336	.4697	.5149	.4825	.6203	.5403	.4700	.4749	.4706	.4920	.4728	.4728	.4751	.5054	.5053	.5249
	720	.4882	.5349	.5077	.6391	.5550	.4877	.5007	.4831	.5136	.4873	.4873	.4882	.5225	.5152	.5443
ETTm2	96	.1562	.2065	.1566	.3064	.2265	.1566	.1586	.1608	.1590	.1627	.1627	.1630	.1704	.1742	.1709
	192	.2022	.2527	.2056	.3532	.2732	.2034	.1907	.1933	.1914	.1954	.1953	.1956	.2120	.2154	.2138
	336	.2352	.2863	.2367	.3863	.3063	.2363	.2226	.2278	.2256	.2298	.2298	.2298	.2351	.2383	.2365
	720	.2645	.3145	.2692	.4114	.3314	.2619	.2349	.2390	.2417	.2445	.2445	.2367	.2643	.2628	.2672
Exchange Rate	96	.0788	.1278	.0802	.2278	.1478	.0776	.0773	.0789	.0780	.0809	.0809	.0808	.1008	.1031	.1027
	192	.1570	.2051	.1642	.3052	.2251	.1544	.1457	.1452	.1490	.1474	.1473	.1466	.1722	.1715	.1779
	336	.2445	.2966	.2780	.3962	.3164	.2448	.2323	.2331	.2578	.2349	.2348	.2334	.2660	.2730	.3114
	720	.4662	.4743	.5963	.5724	.4923	.4218	.4541	.4224	.5806	.4190	.4190	.4189	.4815	.4515	.6597
Weather	96	.1634	.2124	.1651	.3124	.2324	.1629	.1803	.1822	.1840	.1838	.1838	.1855	.1651	.1678	.1669
	192	.2108	.2564	.2122	.3569	.2769	.2065	.2237	.2232	.2290	.2250	.2250	.2263	.2120	.2096	.2105
	336	.2488	.2924	.2540	.3950	.3150	.2419	.2642	.2618	.2743	.2651	.2651	.2647	.2737	.2545	.2599
	720	.2713	.3230	.2913	.4275	.3475	.2737	.2708	.2783	.2987	.2824	.2824	.2817	.2855	.2864	.3035

in an efficient low-dimensional form, while the specific components model idiosyncratic behavior unique to each variable. These two components are combined through a learnable mixing coefficient that automatically balances global and variable-specific contributions.

Table 17a presents the comparison results. For datasets where meaningful cross-variable dependencies exist, the multivariate structure achieves higher predictive accuracy than the univariate version of COSA. However, for datasets with weak inter-variable correlations, such as the Exchange Rate, the univariate structure remains more stable. In such cases, the shared component struggles to learn useful common patterns, which can lead to performance degradation. Moreover, as shown in Table 17b, the additional complexity leads to increased adaptation time and inference latency.

These results indicate that multivariate-based correlation modeling can indeed provide accuracy gains, but further design improvements are required for effective deployment under TTA constraints. We discuss these limitations and potential future directions in Section H.

Table 17: Prediction accuracy and overhead of multivariate consideration.

(a) Prediction accuracy.

		Transformer-based				Linear-based				MLP-based			
		iTransformer		PatchTST		DLinear		OLS		FreTS		MICN	
		Indiv.	Corr.	Indiv.	Corr.	Indiv.	Corr.	Indiv.	Corr.	Indiv.	Corr.	Indiv.	Corr.
ETTh1	96	.4363	.4351	.4238	.4157	.4482	.4202	.4372	.4388	.4371	.4408	.4684	.4533
	192	.4919	.4762	.4805	.4589	.5050	.4646	.4906	.4806	.4940	.4769	.5328	.5039
	336	.5300	.4759	.5320	.4798	.5456	.4823	.5320	.4884	.5351	.4987	.5878	.5105
	720	.5638	.4371	.5822	.5244	.5896	.4695	.5733	.4660	.5959	.4954	.6504	.5314
ETTm2	96	.2493	.2453	.2343	.1836	.2281	.2342	.2265	.2249	.2350	.2311	.2485	.2411
	192	.2947	.2871	.2608	.2172	.2819	.2578	.2791	.2770	.2824	.2922	.3017	.2923
	336	.3339	.3341	.2978	.2361	.3083	.2866	.3043	.2911	.3153	.2971	.3310	.3122
	720	.3591	.3306	.3428	.2638	.3477	.3094	.3453	.3083	.3399	.2979	.3885	.3441
ETTm1	96	.3455	.3186	.3626	.3595	.3475	.3335	.3475	.3330	.3525	.3381	.3831	.3385
	192	.4140	.3988	.4258	.4159	.4122	.4058	.4119	.4125	.4212	.4153	.4514	.4188
	336	.4643	.4491	.4697	.4739	.4858	.4561	.4749	.4648	.4775	.4618	.5054	.4628
	720	.5102	.4372	.4882	.4892	.4991	.4406	.5007	.4323	.4982	.4533	.5225	.4496
ETTm2	96	.1632	.1633	.1562	.1195	.1586	.1557	.1586	.1574	.1569	.1560	.1704	.1697
	192	.2173	.2141	.2022	.1526	.1905	.2005	.1907	.1935	.1908	.1921	.2120	.2097
	336	.2535	.2347	.2352	.1783	.2242	.2235	.2226	.2145	.2211	.2149	.2351	.2429
	720	.2606	.2110	.2645	.2162	.2316	.2295	.2349	.2006	.2314	.2022	.2643	.2265
Exchange Rate	96	.0837	.0840	.0788	.0851	.0834	.0791	.0773	.0773	.0766	.0765	.1008	.0995
	192	.1479	.1493	.1570	.1828	.1519	.1609	.1457	.1457	.1516	.1722	.1726	.1726
	336	.2624	.2838	.2445	.3162	.2480	.2599	.2323	.2456	.2461	.2627	.2660	.2955
	720	.4460	.5221	.4662	.7731	.4481	.5280	.4541	.5184	.4458	.5079	.4815	.5711
Weather	96	.1617	.1547	.1634	.1656	.1793	.1566	.1803	.1731	.1737	.1673	.1651	.1591
	192	.2088	.1938	.2108	.2073	.2217	.2003	.2237	.2158	.2189	.2095	.2120	.1979
	336	.2515	.2300	.2488	.2539	.2626	.2321	.2642	.2461	.2587	.2331	.2737	.2565
	720	.2730	.2236	.2713	.2868	.2708	.2254	.2708	.2172	.2692	.2165	.2855	.2420

(b) Overhead analysis.

Method	# Params ↓	Adaptation time/batch (ms) ↓	Inference time/batch (ms) ↓	Average MSE ↓
Univariate	1,211,287	80.12 ± 13.58	1.25 ± .0984	.3240
Multivariate	1,214,851	186.28 ± 15.36	6.35 ± .2452	.3071

G.6 EXTENSION TO VECTOR GATING

To evaluate whether finer-grained control over correction strength could provide additional benefits, we implemented an element-wise gating vector as an extension of the scalar gating mechanism in COSA. This vector shares the same dimensionality as the prediction length, allowing each time step within the prediction window to modulate its correction intensity independently. Such a design is intended to handle scenarios where drift occurs in only a specific portion of the horizon.

However, as shown in Table 18a, vector gating yields degraded overall accuracy compared to the original scalar gating, and also exhibits reduced stability. We attribute this performance degradation to the propagation of local noise: a noise spike at a particular horizon position can influence the entire gating vector over successive adaptation steps, causing cumulative negative impact throughout the correction process. In contrast, scalar gating provides consistent batch-level modulation that effectively bounds the influence of noise and maintains stable behavior across adaptation windows.

G.7 VISUALIZATION OF NORMALIZATION

Figure 7 visualizes the learned weights of the linear layer in COSA with and without representative time-series normalization modules (RevIN (Kim et al., 2021) and DDN (Dai et al., 2024)).

Table 18: Prediction accuracy and overhead of vector gating.

(a) Performance comparison.

		iTransformer		DLinear		FreTS	
		Scalar	Vector	Scalar	Vector	Scalar	Vector
ETTh1	96	.4363	.4336	.4574	.4436	.4371	.4336
	192	.4919	.4875	.5066	.4985	.4940	.4905
	336	.5300	.5430	.5528	.5466	.5467	.5353
	720	.5638	.6013	.6107	.6178	.6259	.6236
ETTh2	96	.2493	.1990	.2281	.1798	.2350	.1842
	192	.2947	.2318	.2819	.2198	.2972	.2202
	336	.3339	.2604	.3083	.2472	.3153	.2501
	720	.3591	.3035	.3477	.2893	.3399	.2898
ETTm1	96	.3455	.3611	.3456	.3425	.3525	.3551
	192	.4140	.4119	.4222	.4068	.4212	.4137
	336	.4643	.4720	.4858	.4706	.4775	.4767
	720	.5102	.5484	.4991	.5370	.4982	.5405
ETTm2	96	.1632	.1245	.1583	.1215	.1569	.1202
	192	.2173	.1683	.1943	.1487	.1934	.1484
	336	.2535	.2010	.2242	.1798	.2211	.1795
	720	.2606	.2488	.2316	.2319	.2314	.2280
Exchange Rate	96	.0837	.0875	.0834	.0903	.0766	.0818
	192	.1479	.1774	.1519	.1790	.1499	.1698
	336	.2624	.3258	.2480	.3134	.2461	.3094
	720	.4460	.7649	.4481	.7904	.4458	.7500
Weather	96	.1617	.1718	.1793	.1908	.1737	.1825
	192	.2088	.2176	.2217	.2326	.2189	.2250
	336	.2515	.2706	.2626	.2808	.2587	.2745
	720	.2730	.3359	.2708	.3418	.2692	.3378

(b) Overhead analysis.

Method	# Params ↓	Adaptation time/batch (ms) ↓	Inference time/batch (ms) ↓	Average MSE ↓
Scalar	1,211,287	80.12 ± 13.58	1.25 ± .0984	.3240
Vector	1,212,446	96.34 ± 12.48	1.89 ± .0745	.3287

RevIN performs standard normalization on each input time series and then applies a corresponding denormalization step on the output. This procedure mitigates train–test distribution mismatch while restoring the information removed during normalization at the prediction stage, preventing degradation in forecasting performance.

DDN, in contrast, operates jointly in the time and frequency domains. It decomposes the input into low-frequency and high-frequency components and computes local statistics from each domain to remove non-stationarity. DDN then reconstructs non-stationary patterns in the predicted outputs using distribution statistics estimated from the model’s predictions, enabling dynamic tracking of distribution drift.

Each heatmap entry (i, j) shows the weight connecting the j -th input to the i -th output; columns 1: L correspond to the original prediction of base model $\mathbf{Y}^{(0)}$ and columns $L+1:L+K$ to the context vector \mathbf{C} . The example is taken from a single variable of ETTh1 with look-back $W=96$ and horizon $L=96$. Notably, the rightmost block (context columns) is strongly attenuated when RevIN or DDN is applied, whereas without a normalizer, the same block exhibits structured, non-negligible weights. This pattern indicates that explicit normalization reduces the marginal utility of the context (level/scale cues are already standardized), while in the non-normalized COSA leverages \mathbf{C} to perform level-shift correction directly in the output space—supporting our claim that the adapter can subsume normalization effects when needed and remain compatible with them when present.

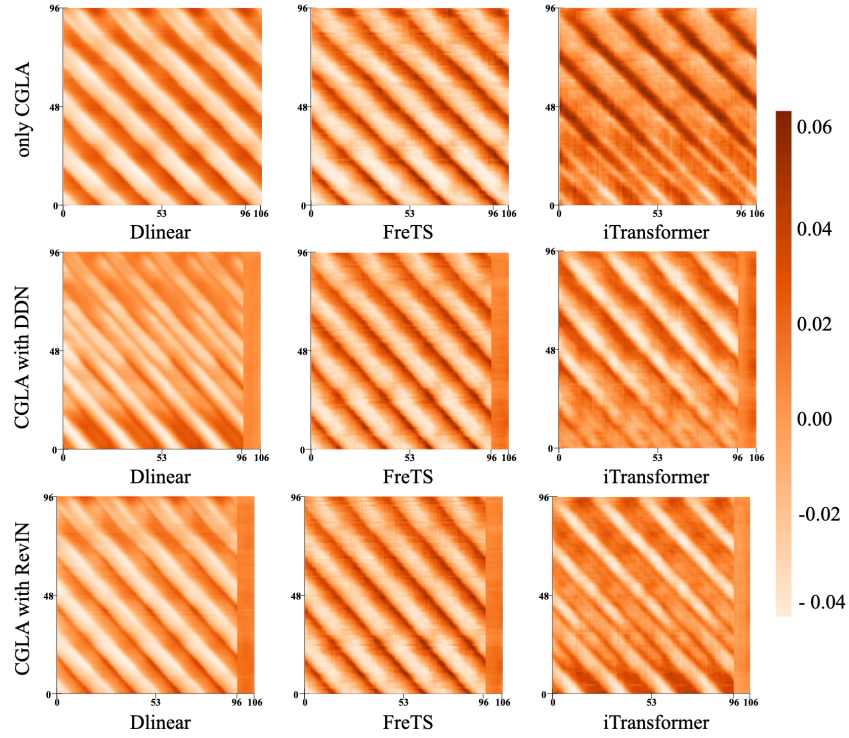


Figure 7: Weight heatmaps of the COSA linear layer for one ETTh1 variable ($W=96$, $L=96$). Columns 1: L are base-prediction inputs $\mathbf{Y}^{(0)}$; columns $L+1:L+K$ are context inputs \mathbf{C} . Each cell shows the weight from input j to output i . Color scales are kept identical across panels to allow magnitude comparison.

H DISCUSSION

Although COSA is built around a simple output-space linear adapter, the extended experiments in the Appendix examined multiple alternative design choices. While low-rank adaptation, input-side calibration, vector gating, selective/encoder-based context, and multivariate extensions each provide potential benefits in specific scenarios, our overall findings show that, considering average accuracy, stability, and latency, the architecture adopted in this paper remains the most consistent and robust choice for TSF-TTA.

The key observations are summarized below:

- **Low-rank factorization.** Despite its parameter-efficiency appeal, reducing representational capacity can lead to unstable adaptation. A joint adapter that integrates low-rank structure without compromising stability is a meaningful direction for future work.
- **Input-side calibration (GCM).** Combining COSA with input GCM improves performance on datasets with strong input noise (e.g., ETTh1/h2/m2) by smoothing perturbations before prediction. However, for fast-drifting or irregular series, GCM may oversmooth important variations and degrade performance, reaffirming that output-only correction is a reasonable and stable default.
- **Gating and its variants.** Although vector gating was expected to modulate drift at a finer temporal resolution, local noise propagated across the gating vector and reduced stability compared to scalar gating. Scalar gating’s batch-level modulation limits the influence of noise and achieves more reliable behavior.
- **Context construction.** Selective context (phase-aligned retrieval) and encoder-based context (RNN/LSTM/Attention) showed improvements in certain periodic datasets, but both suffered from outdated information, overfitting, or latency overhead in non-stationary set-

tings. These results highlight that additional complexity does not guarantee better TTA performance unless paired with drift-aware representations and online update strategies. Future directions include sub-sequence vector gating, structure-aware context that explicitly encodes trend and seasonality, and lightweight encoders capable of tracking drift without incurring high overhead.

- **Multivariate residual correction.** While multivariate modeling with cross-variable attention and shared components improved performance in most datasets, it degraded both accuracy and efficiency in datasets with weak inter-variable correlations (e.g., Exchange Rate). This suggests the need for selective correlation modeling or structural sparsity to suppress unnecessary cross-variable interactions.

Taken together, the extended Appendix experiments reinforce that the proposed simple architecture is particularly well-suited for TSF-TTA. They also indicate substantial room for generalizing COSA through carefully integrated low-rank structures, input calibration modules, selective or encoder-based context modeling, and vector gating, while preserving the efficiency and stability crucial for non-stationary test-time adaptation.

I CONFIDENCE INTERVAL OF MAIN RESULTS

Table 19 reports the 95% confidence intervals of the main accuracy comparison results over 10 independent runs for each method–dataset–horizon combination. Overall, the intervals are narrow, indicating that the run-to-run variability of all methods is small, and COSA-F/P consistently retain their advantage over baselines even when accounting for this uncertainty.

THE USE OF LARGE LANGUAGE MODELS

Tool & Version: Claude Sonnet 4 (Anthropic, 2025-09)

Research Stage: Not used.

Writing Stage: Language editing of author-drafted text for clarity and conciseness.

Human Oversight: All outputs reviewed/edited by the authors; authors accept full responsibility for the content.

Table 19: 95% confidence interval of main accuracy comparison results

		Transformer-based												Linear-based						MLP-based												
		TTransformer						PatchTST						DLinear			OLS			FeTS			COSA-P			TAFAS			MCN			
		TAFAS	PETSA	COSA-F	COSA-P	TAFAS	PETSA	TAFAS	PETSA	COSA-F	COSA-P	TAFAS	PETSA	COSA-F	COSA-P	TAFAS	PETSA	COSA-F	COSA-P	TAFAS	PETSA	COSA-F	COSA-P	TAFAS	PETSA	COSA-F	COSA-P	TAFAS	PETSA	COSA-F	COSA-P	
ETTh1	96	4409	4390	4366	4361	4243	4247	4226	4222	4222	4616	4592	4571	4571	4405	4385	4385	4385	4377	4377	4377	4365	4890	4886	4890	4886	4683	4683	4890	4886	4683	4683
	192	4916	4937	4938	4908	4830	4825	4805	4775	4835	5146	5157	5103	5108	4948	4953	4929	4929	4920	4920	4920	4906	5615	5619	5621	5619	5370	5370	5619	5619	5370	5370
	336	5580	5586	5604	5604	5444	5441	5399	5288	5288	5878	5878	5878	5878	5601	5508	5508	5508	5508	5508	5508	5508	6332	6332	6332	6332	6010	6010	6332	6332	6010	6010
	720	6581	6570	6596	6596	6805	6762	6802	6802	6802	6802	6712	6654	6603	6603	6513	6322	6322	6322	6322	6322	6322	6099	6099	6099	6099	5822	5822	6099	6099	5822	5822
ETTh2	96	2546	2548	2502	2490	2347	2358	2345	2339	2339	2298	2300	2295	2273	2273	2273	2273	2273	2273	2273	2273	2248	2248	2248	2248	2361	2361	2248	2248	2361	2361	
	192	2997	2990	2970	2934	2734	2747	2634	2579	2579	2828	2864	2813	2813	2807	2807	2827	2827	2827	2827	2827	2827	2827	2827	2827	2827	2827	2827	2827	2827	2827	
	336	3320	3322	3311	3315	3308	3091	3098	2940	2940	3116	3116	3116	3116	3170	3179	2990	2990	3002	3002	3002	3002	3201	3201	3201	3201	3002	3002	3201	3201	3002	3002
	720	3995	4004	3384	3385	3367	3359	3359	3366	3366	3366	3366	3366	3366	3366	3366	3366	3366	3366	3366	3366	3366	3366	3366	3366	3366	3366	3366	3366	3366	3366	3366
ETTh1	96	3556	3568	3445	3453	3383	3927	3616	3616	3616	3496	3523	3455	3455	3505	3535	3535	3535	3535	3535	3535	3535	3535	3535	3535	3535	3535	3535	3535	3535	3535	3535
	192	4139	4136	4118	4134	4351	4393	4433	4234	4241	4153	4164	4164	4164	4153	4185	4185	4185	4185	4185	4185	4185	4185	4185	4185	4185	4185	4185	4185	4185	4185	4185
	336	4715	4717	4522	4603	4901	4942	4564	4693	4693	4792	4794	4745	4745	4850	4773	4780	4735	4838	4838	4838	4838	4838	4838	4838	4838	4838	4838	4838	4838	4838	4838
	720	5460	5426	4633	4977	5416	5452	4672	4871	4871	5415	5459	4692	4923	5424	5464	4699	4699	4944	4944	4944	4944	5442	5442	5442	5442	4944	4944	5442	5442	4944	4944
ETTh2	96	1630	1633	1628	1628	1577	1579	1555	1559	1559	1578	1578	1577	1577	1588	1587	1587	1587	1587	1587	1587	1587	1587	1587	1587	1587	1587	1587	1587	1587	1587	1587
	192	2177	2167	2165	2165	2167	2026	2027	1998	1998	2013	2013	2013	2013	2013	2013	2013	2013	2013	2013	2013	2013	2013	2013	2013	2013	2013	2013	2013	2013	2013	2013
	336	2616	2576	2420	2420	2521	2447	2448	2255	2255	2348	2277	2281	2281	2281	2286	2287	2287	2287	2287	2287	2287	2287	2287	2287	2287	2287	2287	2287	2287	2287	2287
	720	3285	3312	2483	2653	2653	3261	3250	2439	2439	2639	2914	2919	2161	2260	2897	2844	2844	2844	2844	2844	2844	2844	2844	2844	2844	2844	2844	2844	2844	2844	2844
Exchange Rate	96	0873	0883	0816	0835	0835	0828	0756	0756	0756	0881	0874	0809	0831	0789	0795	0795	0795	0795	0795	0795	0795	0795	0795	0795	0795	0795	0795	0795	0795	0795	
	192	1645	1706	1363	1440	1711	1742	1394	1487	1487	1708	1677	1410	1464	1601	1601	1601	1601	1601	1601	1601	1601	1601	1601	1601	1601	1601	1601	1601	1601	1601	1601
	336	2995	3029	2008	2546	3186	3225	1886	2355	2355	2904	2891	2011	2448	2787	2821	2821	2821	2821	2821	2821	2821	2821	2821	2821	2821	2821	2821	2821	2821	2821	2821
	720	8077	7758	3085	4155	8348	8317	3238	3238	3238	8427	8468	3123	4145	7882	7876	7876	7876	7876	7876	7876	7876	7876	7876	7876	7876	7876	7876	7876	7876	7876	7876
Weather	96	1663	1673	1596	1616	1616	1721	1740	1621	1621	1792	1821	1771	1790	1790	1790	1790	1790	1790	1790	1790	1790	1790	1790	1790	1790	1790	1790	1790	1790	1790	1790
	192	2078	2107	2045	2067	2140	2159	1998	2101	2101	2190	2194	2157	2163	2163	2163	2163	2163	2163	2163	2163	2163	2163	2163	2163	2163	2163	2163	2163	2163	2163	2163
	336	2595	2641	2482	2494	2594	2647	2382	2428	2428	2682	2719	2544	2601	2737	2737	2737	2737	2737	2737	2737	2737	2737	2737	2737	2737	2737	2737	2737	2737	2737	2737
	720	3404	3405	2415	2673	3307	3369	2496	2626	2626	3477	3477	2560	2684	3477	3477	3477	3477	3477	3477	3477	3477	3477	3477	3477	3477	3477	3477	3477	3477	3477	3477