

# 000 001 002 003 004 005 006 007 008 009 010 011 012 013 014 015 016 017 018 019 020 021 022 023 024 025 026 027 028 029 030 031 032 033 034 035 036 037 038 039 040 041 042 043 044 045 046 047 048 049 050 051 052 053 COSA: CONTEXT-AWARE OUTPUT-SPACE ADAPTER FOR TEST-TIME ADAPTATION IN TIME SERIES FORE- CASTING

Anonymous authors

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## ABSTRACT

Deployed time-series forecasters suffer performance degradation under non-stationarity and distribution shifts. Test-time adaptation (TTA) for time-series forecasting differs from vision TTA because ground truth becomes observable shortly after prediction. Existing time-series TTA methods typically employ dual input/output adapters that indirectly modify data distributions, making their effect on the frozen model difficult to analyze. We introduce the *Context-aware Output-Space Adapter* (COSA), a minimal, plug-and-play adapter that directly corrects predictions of a frozen base model. COSA performs residual correction modulated by gating, utilizing the original prediction and a lightweight context vector that summarizes statistics from recently observed ground truth. At test time, only the adapter parameters (linear layer and gating) are updated under a leakage-free protocol, using observed ground truth with an adaptive learning rate schedule for faster adaptation. Across diverse scenarios, COSA demonstrates substantial performance gains versus baselines without TTA (13.91~17.03%) and SOTA TTA methods (10.48~13.05%), with particularly large improvements at long horizons, while adding a reasonable level of parameters and negligible computational overhead. The simplicity of COSA makes it architecture-agnostic and deployment-friendly. Source code: <https://anonymous.4open.science/r/linear-adapter-A720>

## 1 INTRODUCTION

Time-series forecasting serves as the foundation for critical decision-making across diverse domains, including finance (Chen et al., 2023), supply chain management (Aamer et al., 2020), energy grids (Di Piazza et al., 2021), and predictive maintenance (Makridis et al., 2020). Modern forecasting models, including Transformer-based architectures (Zhou et al., 2021; Liu et al., 2023; 2022), typically achieve high accuracy. However, they suffer performance degradation in real deployment settings due to non-stationarity and distribution shifts (Du et al., 2021; Chen et al., 2024a). Time series exhibit inherent non-stationarity, with changing temporal patterns and statistical characteristics over time, resulting in distributions at training that typically differ from those encountered after deployment.

To address this challenge, various approaches have been proposed, including online learning, continual learning, and domain adaptation. Online and continual learning methods adapt by updating model parameters directly to streaming data (Du et al., 2021; Zhang et al., 2024; Kirkpatrick et al., 2017; Rolnick et al., 2019; Giannini et al., 2023; Pham et al., 2022), but these approaches incur additional computational costs, memory requirements, catastrophic forgetting issues, and plasticity. Furthermore, these methods typically require labeled data or explicit knowledge of task boundaries, making them unsuitable for scenarios where only unlabeled streaming data is available during deployment. Domain adaptation methods learn robust representations by reducing source-target distribution differences (Wilson et al., 2020; Jin et al., 2022), but they rely on explicit target domain data and boundary definitions.

Test-time adaptation (TTA) offers an alternative approach that adapts to distribution changes by updating only lightweight modules using unlabeled test streams after deployment. TTA methods have

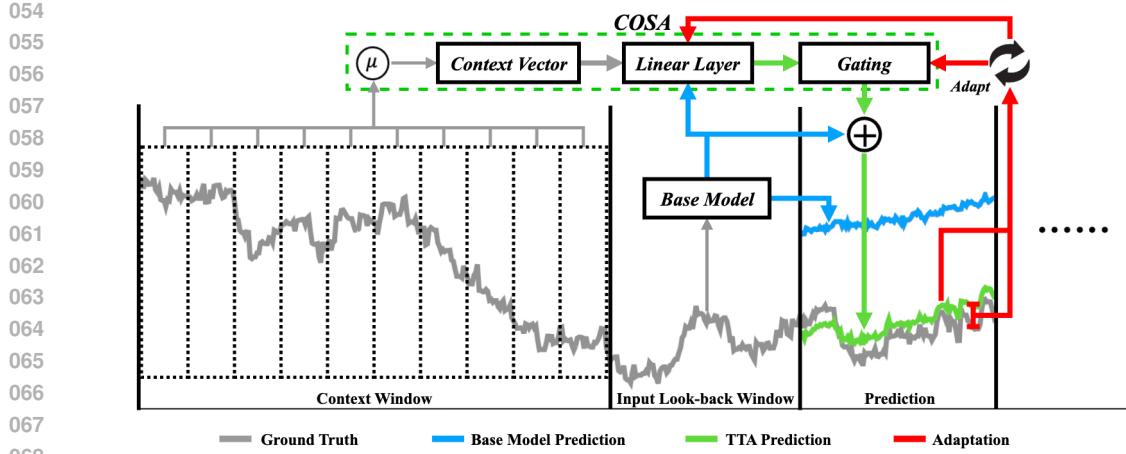


Figure 1: Overview of COSA operation showing the context-aware gated linear adapter architecture with input processing, linear transformation, gating mechanism, and output correction for test-time adaptation.

evolved mainly in the vision domain through batch normalization coefficient optimization and entropy minimization (Wang et al., 2020), self-supervised/contrastive learning combined with pseudo-labeling (Liang et al., 2021; Chen et al., 2022; Gong et al., 2025), single-sample multi-augmentation-based adaptation (Zhang et al., 2022), and long-term adaptation stabilization (Wang et al., 2022).

Unlike vision tasks, time-series forecasting has unique characteristics that distinguish it from vision tasks: 1) it employs normalization methods different from vision tasks to preserve periodicity and level information, and 2) ground truth becomes sequentially observable after prediction with short delays, enabling the use of direct losses such as Mean Squared Error (MSE).

Time-series forecasting TTA is a recently evolving topic; to the best of our knowledge, only few methods (Kim et al., 2025; Medeiros et al., 2025; Grover & Etemad, 2025) have been proposed. All of them adopted dual-adapter architectures that place calibration modules at both input and output ends of the base model. They map inputs to domains that the base model can handle more easily and restore outputs to the original domain, controlling adaptation intensity through gating. However, these indirect distribution calibration methods involve design complexity and create uncertainty about the impact of input transformations on internal model representations.

To this end, we propose Context-aware Output-Space Adapter (COSA), which offers a direct output-space correction approach that operates with minimal computational overhead. Figure 1 presents the overview of COSA. COSA takes the predictions from a frozen base model and a lightweight context vector, summarizes recent observation statistics as input, computes residuals through linear correction, and controls correction strength using gating. At deployment, we freeze the base forecaster and update only a lightweight output adapter (i.e., linear correction with a learnable gate) under a leakage-free streaming protocol: after each prediction, adaptation uses only previously revealed ground truth, never current or future labels. COSA is architecture-agnostic and demonstrates consistent performance improvements over existing state-of-the-art time-series forecasting TTA methods across various predictors and horizons.

The main contributions of this study are summarized as follows:

1. **Architecture-agnostic output adapter.** Unlike existing time-series TTA methods that adopt dual input-output adapters, COSA consists of a single output adapter. COSA operates independently in the output space, correcting predictions from any base model without changes to training pipelines or internal parameters. COSA also shows compatibility with SOTA normalizers, consistently reducing prediction error.
2. **Context-aware linear residual with gating.** A linear correction uses the base prediction and a lightweight context vector that summarizes statistics of recent observed ground truth, and a learnable gate modulates correction strength.

108 3. **Consistent accuracy gains.** Across six benchmarks, four horizons, and six baseline  
 109 architectures, COSA improves test MSE over baselines (13.91~17.03%) and SOTA TTA  
 110 methods (10.48~13.05%), in particular, with the largest gains at longer horizons.  
 111

112 4. **Fast, efficient TTA.** Adaptive learning rate enables faster convergence of COSA, leading to  
 113 higher accuracy within a few adaptation steps. Specifically, COSA enables 88.59~90.10%  
 114 faster inference time against prior SOTA TTA methods.  
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116

## 117 2 RELATED WORK

118

### 120 2.1 TIME-SERIES FORECASTING

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122 To handle non-stationarity in time-series forecasting, existing methods typically employ 1) on-  
 123 line learning, 2) continual learning, and 3) domain adaptation. Representative online learning,  
 124 D3A (Zhang et al., 2024) narrows source–target gaps through z-score monitoring of loss distribu-  
 125 tions and Gaussian noise injection, whereas Adarnn (Du et al., 2021) reduces temporal distribution  
 126 shifts using temporal distribution characterization and distribution matching. In continual learning,  
 127 cPNM (Giannini et al., 2023) grows temporal columns and transfers knowledge via lateral connec-  
 128 tions, and FSNet (Pham et al., 2022) separates per-layer adapters for rapid adaptation from asso-  
 129 ciative memory for long-term retention to balance plasticity and stability. For domain adaptation,  
 130 CoDATS (Wilson et al., 2020) learns domain-invariant features adversarially, and DAF (Jin et al.,  
 131 2022) shares attention with domain-invariant queries/keys and domain-specific values. These fami-  
 132 lies generally update the base model during training or online operation, differing from TTA, which  
 133 adapts lightweight modules on unlabeled test streams while keeping the base model frozen.  
 134

### 135 2.2 TEST-TIME ADAPTATION

136

137 Tent (Wang et al., 2020) optimizes only batch-normalization affine parameters under entropy mini-  
 138 mization, and SHOT (Liang et al., 2021) combines information maximization with self-supervised  
 139 objectives to transfer source hypotheses to the target. AdaContrast (Chen et al., 2022) constructs  
 140 pseudo-labels via contrastive learning with a dynamic memory bank for gradual adaptation, while  
 141 MEMO (Zhang et al., 2022) applies multi-augmentation to a single test example to minimize  
 142 marginal output entropy, updating all weights. CoTTA (Wang et al., 2022) limits error accumulation  
 143 via weight and stochastic restoration, and ACCUP (Gong et al., 2025) integrates adaptive clustering  
 144 with pseudo-labeling. However, they are proposed for vision tasks. TTA for time-series forecasting  
 145 requires different approaches from those for vision tasks due to its own characteristics.  
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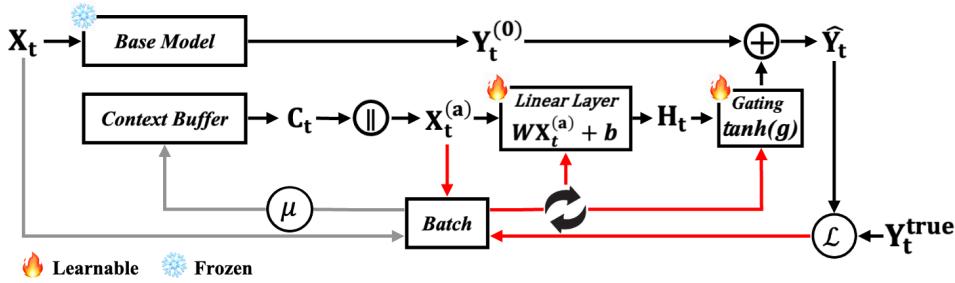
### 147 2.3 TEST-TIME ADAPTATION FOR TIME-SERIES FORECASTING

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149 Time-series forecasting TTA methods typically employ dual adapters that calibrate distributions at  
 150 both input and output. TAFAS (Kim et al., 2025) couples a calibration module to map inputs to a  
 151 model-friendly domain and restores outputs to the original domain. It uses gating to modulate the  
 152 calibration strength and utilizes Periodicity-Aware Adaptive Scheduling (PAAS) to adjust adaptation  
 153 frequency using frequency patterns based on inputs. PETSA (Medeiros et al., 2025) factorizes the  
 154 calibration module with a low-rank structure and adopts a combined loss for stable adaptation with  
 155 fewer parameters. DynaTTA (Grover & Etemad, 2025) adjusts the dynamic learning rate, based on  
 156 local distribution shift, global distribution shift, loss z-score. Existing time-series forecasting TTA  
 157 methods employ an indirect approach that bidirectionally calibrates distributions at the input and  
 158 output sides of the base model. They entailed design complexity due to indirect calibration and  
 159 difficulty in predicting the impact of input transformations on internal representations. In contrast,  
 160 we aim to utilize a single output-space adapter that directly corrects predictions without requiring  
 161 input calibration or bidirectional transformation, resulting in a simpler design and more predictable  
 adaptation behavior.

162 Table 1: Adapter-specific notation. Basic sizes/indices are defined as  $(W, L, K, B; t, i, k)$ .  
163

Symbol	Meaning (shape)
$\mathbf{Y}_t^{(0)}$	Base (frozen) $L$ -step prediction at time $t$ ( $\mathbb{R}^L$ ).
$\mathbf{Y}_t^{\text{true}}$	True $L$ -step target revealed after $t$ ( $\mathbb{R}^L$ ).
$\mathbf{C}_t$	Context vector from revealed batch statistics $[\mu_t - K, \dots, \mu_t - 1]^\top$ ( $\mathbb{R}^K$ ).
$\mathbf{X}_t$	Input look-back window ( $\mathbb{R}^W$ ).
$\mathbf{X}_t^{(a)}$	Adapter input $[\mathbf{Y}_t^{(0)} \parallel \mathbf{C}_t]$ ( $\mathbb{R}^{L+K}$ ).
$\mathbf{H}_t$	Linear residual $\mathbf{W} \mathbf{X}_t^{(a)} + \mathbf{b}$ ( $\mathbb{R}^L$ ).
$\hat{\mathbf{Y}}_t$	Corrected output $\mathbf{Y}_t^{(0)} + \alpha \mathbf{H}_t$ with $\alpha = \tanh(g) \in [-1, 1]$ ( $\mathbb{R}^L$ ).
$\mathbf{W}, \mathbf{b}, g$	Adapter weights ( $\mathbb{R}^L \times (L + K)$ ), bias ( $\mathbb{R}^L$ ), and gate parameter ( $\mathbb{R}$ ).
<i>Operators:</i> concatenation $[\mathbf{a} \parallel \mathbf{b}]$ ; $\ \cdot\ _2$ vector norm; $\ \cdot\ _F$ Frobenius.	

177 Figure 2: Detailed architecture of COSA illustrating the linear correction layer (weight matrix  $\mathbf{W}$   
178 and bias  $\mathbf{b}$ ), learnable gating parameter ( $g$ ), and context vector ( $\mathbf{C}$ ) integration for output-space  
179 correction.  
180181 

### 3 COSA: CONTEXT-AWARE OUTPUT-SPACE ADAPTER

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#### 3.1 NOTATION AND PROBLEM FORMULATION

183 Table 1 shows the symbols necessary for COSA and their meanings.

184 This study targets univariate time-series forecasting, following the existing SOTA time-series fore-  
185 casting TTA methods (Kim et al., 2025; Medeiros et al., 2025; Grover & Etemad, 2025). For mul-  
186 tivariate time-series inputs, we decompose them into per-variable univariate forecasting tasks and  
187 perform the task iteratively for each variable. At time  $t$ , base model generates  $L$ -step original pre-  
188 dictions  $\mathbf{Y}_t^{(0)} \in \mathbb{R}^L$  from input  $\mathbf{X}_t \in \mathbb{R}^W$ , where  $W$  denotes the input look-back window length.  
189 COSA generates corrected predictions  $\hat{\mathbf{Y}}_t \in \mathbb{R}^L$  from input  $\mathbf{X}_t^{(a)} \in \mathbb{R}^{L+K}$ , where  $K$  denotes the  
190 length of the context vector. After making predictions, the ground truth for that interval becomes se-  
191 quentially observable following a short delay. Like other TTA approaches, we keep the base model  
192 completely frozen and perform only adapter adaptation at test time. Adaptation is performed by col-  
193 lecting the most recent  $B$  prediction, ground truth pairs (batch index  $i \in \{1, \dots, B\}$  and context  
194 index  $k \in \{1, \dots, K\}$ ).195 

#### 3.2 OVERALL ARCHITECTURE

196 Figure 2 illustrates the overall operation of COSA. COSA consists of a single output adapter that  
197 directly corrects the predictions. The key components are: 1) a linear layer composed of weight  
198 matrix  $\mathbf{W}$  and bias variable  $\mathbf{b}$  that computes correction values  $\mathbf{H}$ , 2) learnable gating  $g$  that controls  
199 correction strength, and 3) a context vector  $\mathbf{C}$  that summarizes and stores recent trend information.  
200201 We choose a single linear layer for two key reasons: 1) **Efficiency**: Linear operations provide lower  
202 latency and higher throughput compared to nonlinear modules, making them suitable for fast adap-  
203 tation. We confirmed that a single-layer adapter shows 34.95% faster wall-clock time on average than  
204 a 2-layer MLP adapter. 2) **Simplicity-Performance balance**: As reported in LTSF-Linear (Zeng  
205 et al., 2025), a single linear layer achieves comparable performance to a 2-layer MLP adapter but with  
206 significantly lower complexity.

et al., 2023), a linear layer sufficiently performs well in time-series forecasting, despite its simplicity. We also verified that a single linear layer adapter showed 5.71% even better performance on average against a 2-layer MLP adapter. These characteristics make the linear layer beneficial for TTA. Detailed results are provided in Appendix G.3.

The streaming protocol for leakage prevention is as follows (let the last adaptation was performed in  $t-1$ ):

1. **Prediction:** At time  $t$ , base model generates prediction  $\mathbf{Y}_t^{(0)}$  from input  $\mathbf{X}_t$ .
2. **Correction:** Feed  $\mathbf{Y}_t^{(0)}$  and context  $C_t$  into COSA to generate the corrected prediction  $\hat{\mathbf{Y}}_t$ .
3. **Observation:** After delay  $\Delta \geq 0$ , values of ground truth of the prediction horizon  $\mathbf{Y}_t^{true}$  are sequentially observed.
4. **Adaptation:** Collect the most recent  $B$  prediction, ground truth pairs  $\{\hat{\mathbf{Y}}_{t+i-1}, \mathbf{Y}_{t+i-1}^{true}\}$ , and perform adaptation that updates COSA parameters  $\{\mathbf{W}, \mathbf{b}, \mathbf{g}\}$ .

### 3.3 OUTPUT-SPACE RESIDUAL CORRECTION

For time  $t$ , we concatenate the original prediction of base model and context vector to create the adapter input:

$$\mathbf{X}_t^{(a)} = [\mathbf{Y}_t^{(0)} \parallel \mathbf{C}_t].$$

The residual is computed using a linear transformation:

$$\mathbf{H}_t = \mathbf{W} \mathbf{X}_t^{(a)} + \mathbf{b}.$$

The correction magnitude is controlled through gating to compose the final output:

$$\hat{\mathbf{Y}}_t = \mathbf{Y}_t^{(0)} + \tanh(\mathbf{g}) \mathbf{H}_t.$$

The  $\tanh$  activation stabilizes the correction magnitude.

### 3.4 CONTEXT CONSTRUCTION

To prevent information leakage, the context summarizes previously observed ground truth information. For time  $t$ , we compute batch-wise aggregation as:

$$\mu_t = \text{agg}\{y_{t-(kB)+i}^{true} : 1 \leq i \leq B\}, \quad 1 \leq k \leq K.$$

where the aggregation function  $\text{agg}$  can use statistics such as mean, median, etc. We construct the context vector by stacking the most recent  $K$  aggregated values:

$$\mathbf{C}_t = [\mu_1, \mu_2, \dots, \mu_K]^\top.$$

This context vector summarizes level/scale changes and gradual drift patterns to help interpret the relative magnitude of the base prediction  $\mathbf{Y}_t^{(0)}$  (reducing to single time-series values when  $B=1$ ).

### 3.5 ADAPTATION OBJECTIVE AND SCHEDULING

Because targets arrive with a delay, we employ a direct objective with weight decay:

$$\mathcal{L} = \sum_{i=1}^B \|(\hat{\mathbf{Y}}_{t-i-1} - \mathbf{Y}_{t-i-1}^{true})\|_2^2 + \lambda (\|\mathbf{W}\|_F^2 + \|\mathbf{b}\|_2^2 + \|\mathbf{g}\|_2^2). \quad (1)$$

When  $B$  forecast-target pairs have been enqueued, we run  $S$  gradient steps on the adapter parameters using a cosine-adaptive learning-rate schedule, simply *CALR*. We apply cosine annealing within the  $S$  steps,

$$\eta^{(s+1)} = \eta_{\min} + \frac{1}{2}(\eta^{(s)} - \eta_{\min}) \left(1 + \cos \frac{s\pi}{S}\right). \quad (2)$$

and then adjust  $\eta$  online, based on short-horizon loss trends to encourage fast but stable convergence (decrease  $\eta$  on loss upticks; mildly increase on plateaus). [When a new batch arrives, it is always](#)

270 initialized with the same learning rate, and thereafter the learning rate for the next step within the  
 271 batch is determined through Equation 2 according to the loss. Early stopping and gradient clipping  
 272 are also implemented. The threshold values for learning rate adjustment are stability-induced  
 273 by balancing adaptation speed against stability. Conservative thresholds ensure convergence while  
 274 aggressive values enable faster response to distribution shifts. Full pseudocode and thresholds are  
 275 given in Algorithm 1 in Appendix A.

## 276 4 EXPERIMENTS

### 277 4.1 EXPERIMENTAL SETTINGS

278 We evaluate COSA on six benchmark datasets (ETTh1/2, ETTm1/2, Exchange Rate, and Weather)  
 279 with a fixed look-back window ( $W = 96$ ) and four prediction horizons ( $L \in \{96, 192, 336, 720\}$ ).  
 280 We used six representative base models spanning different architectures: Transformer-based (iTrans-  
 281 former (Liu et al., 2023), PatchTST (Nie et al., 2023)), linear-based (DLinear (Zeng et al., 2023),  
 282 OLS (Toner & Darlow, 2024)), and MLP-based (FrTS (Yi et al., 2023), MICN (Wang et al., 2023)).  
 283 By default, all input time series are treated as variable-wise univariate forecasting tasks, standard  
 284 normalization is applied, and MSE serves as the performance comparison metric.

285 We compare *COSA* (our method) with *Baseline* (without TTA), *TAFAS* (Kim et al., 2025), and  
 286 *PETSA* (Medeiros et al., 2025). All experiments were conducted according to the official bench-  
 287 mark library (Wang et al., 2024)<sup>1</sup>. The train:valdiation:test ratio is 7:1:2 for all datasets.

288 Unless otherwise noted, we fix the adapter hyperparameters to  $K=10$  and  $S=3$ , enabled *CALR*. We  
 289 utilize the average as *agg*. Ablation studies for the variations of *agg* are provided in Appendix G.1.

290 We report two variants for COSA: COSA-F, which uses a fixed  $B=48$  (half of the look-back), and  
 291 COSA-P, which sets  $B$  online following the PAAS in TAFAS (Kim et al., 2025). Hyperparameters  
 292 for comparative methods follow the settings reported in the original papers or official code defaults.  
 293 In tables, the best score is shown in bold and the second best is underlined.

294 We utilize Xavier uniform initializer (Glorot & Bengio, 2010) with gain = 0.1 for parameters of the  
 295 weight matrix  $W$ . The bias  $b$  and gating  $g$  are initialized to 0, and Adam optimizer is utilized.

296 All experiments were conducted on a machine with an Intel i7-7800X CPU and NVIDIA GeForce  
 297 RTX 3080 10GB.

### 303 4.2 MAIN RESULTS

#### 305 4.2.1 COMPARISON WITH SOTA TIME-SERIES TTA METHODS

307 The proposed COSA achieves best performance in all scenarios, as shown in Table 2<sup>2</sup>. The results  
 308 reveal two key performance patterns:

- 310 1. **Architecture-agnostic benefits:** Consistent improvements across all base models demon-  
 311 strate that effectiveness of COSA is not dependent on specific model architectures. The  
 312 average improvement ranges from 10.48% to 13.05%.
- 313 2. **Effectiveness in long-term forecasting:** The largest performance improvements were ob-  
 314 served at the 720 horizon, where COSA-F and COSA-P showed performance improve-  
 315 ments of 32.24% and 26.33% compared to baseline, respectively, and 28.21% and 21.96%  
 316 compared to other methods. This trend suggests that COSA becomes increasingly valuable  
 317 for longer prediction horizons.

318 These findings demonstrate that the COSA, which performs residual correction directly in the output  
 319 space, proves more effective than existing indirect dual-adapter approaches.

321 <sup>1</sup>In the case of *DynatTA* (Grover & Etemad, 2025), there were reproducibility issues when we used the  
 322 officially released source code. Therefore, we report the comparison results with them in the Appendix F.4 with  
 323 the used detailed hyperparameters.

324 <sup>2</sup>All reported results are averaged over 10 runs with different random seeds to ensure statistical reliability.

324 Table 2: Prediction accuracy comparison. Standard deviations less than 0.001 are omitted.  
325

	Transformer-based												Linear-based												MLP-based																			
	iTTransformer						DLinear						FreTS																															
	Baseline TAFAS			PETSA			COSA-F			COSA-P			Baseline TAFAS			PETSA			COSA-F			COSA-P			Baseline TAFAS			PETSA			COSA-F			COSA-P										
329	ETTh1	96	.4507	.4411	.4393	.4368	<b>.4363</b>	.4695	.4618	.4594	.4574	<b>.4482</b>	.4462	.4403	.4387	.4384	<b>.4371</b>																											
		192	.5078	.4928	.4949	.4961	<b>.4919</b>	.5213	.5117	.5118	.5066	<b>.5050</b>	.5022	.4954	.4942	.4951	<b>.4940</b>																											
		336	.5658	.5629	.5640	.5651	<b>.5300</b>	.5659	.5604	.5617	.5528	<b>.5456</b>	.5544	.5521	.5527	<b>.5467</b>	.5351																											
		720	.7038	.6612	.6596	.5958	<b>.5638</b>	.7117	.6820	.6743	.6107	<b>.5896</b>	.7182	.6852	.6846	.6259	<b>.5959</b>																											
330	ETTh2	96	.2577	.2549	.2551	.2504	<b>.2493</b>	.2323	.2303	.2306	.2300	<b>.2281</b>	.2384	.2367	.2364	.2367	<b>.2350</b>																											
		192	.3161	.3010	.3006	.2983	<b>.2947</b>	.2862	.2842	.2876	.2827	<b>.2819</b>	.2866	.2824	.2832	<b>.2816</b>	.2824																											
		336	.3545	.3352	.3348	.3241	<b>.3339</b>	.3252	.3185	.3184	.3050	.3083	.3317	.3229	.3233	.3031	.3153																											
		720	.4276	.4023	.4043	<b>.3487</b>	.3591	.4087	.3873	.3853	<b>.3062</b>	.3477	.4119	.3857	.3860	<b>.3169</b>	.3399																											
331	ETTm1	96	.3823	.3558	.3570	<b>.3447</b>	.3455	.3715	.3497	.3524	<b>.3456</b>	.3475	.3675	.3582	.3583	<b>.3520</b>	.3525																											
		192	.4423	.4146	.4142	<b>.4124</b>	.4140	.4438	.4166	.4178	<b>.4113</b>	.4122	.4325	.4212	.4198	<b>.4150</b>	.4212																											
		336	.5093	.4754	.4751	<b>.4569</b>	.4643	.5183	.4799	.4803	<b>.4753</b>	.4858	.5005	.4827	.4789	<b>.4661</b>	.4775																											
		720	.6065	.5562	.5553	<b>.4773</b>	.5102	.5929	.5488	.5532	<b>.4774</b>	.4991	.5704	.5486	.5476	<b>.4718</b>	.4982																											
332	ETTm2	96	.1647	.1634	.1637	<b>.1627</b>	.1632	.1598	.1584	.1584	<b>.1583</b>	.1586	.1581	.1572	.1572	<b>.1568</b>	.1569																											
		192	.2209	.2183	.2173	<b>.2171</b>	.2173	.1930	.1913	.1913	<b>.1904</b>	.1905	.1923	.1909	.1909	<b>.1908</b>	.1908																											
		336	.2727	.2630	.2592	<b>.2435</b>	.2535	.2324	.2289	.2292	<b>.2083</b>	.2242	.2320	.2288	.2289	<b>.2098</b>	.2211																											
		720	.3451	.3305	.3332	<b>.2477</b>	.2606	.3062	.2968	.2963	<b>.2215</b>	.2316	.3012	.2916	.2926	<b>.2158</b>	.2314																											
333	Exchange Rate	96	.0882	.0876	.0885	<b>.0818</b>	.0837	.0913	.0885	.0878	<b>.0812</b>	.0834	.0828	.0799	.0803	<b>.0744</b>	.0766																											
		192	.1811	.1686	.1740	<b>.1403</b>	.1479	.1827	.1760	.1730	<b>.1459</b>	.1519	.1734	.1665	.1648	<b>.1366</b>	.1499																											
		336	.3428	.3079	.3097	<b>.2089</b>	.2624	.3277	.2941	.2920	<b>.2039</b>	.2480	.3240	.2930	.2923	<b>.2053</b>	.2461																											
		720	.8540	.8322	.8004	<b>.3421</b>	.4460	.8873	.8762	.8781	<b>.3494</b>	.4481	.8368	.8273	.8067	<b>.3352</b>	.4458																											
334	Weather	96	.1755	.1664	.1674	<b>.1597</b>	.1617	.1954	.1796	.1823	<b>.1773</b>	.1793	.1856	.1759	.1765	<b>.1724</b>	.1737																											
		192	.2232	.2101	.2128	<b>.2067</b>	.2088	.2403	.2244	.2254	<b>.2216</b>	.2217	.2310	.2165	.2192	<b>.2135</b>	.2189																											
		336	.2800	.2614	.2665	<b>.2503</b>	.2515	.2918	.2709	.2740	<b>.2567</b>	.2626	.2843	.2653	.2681	<b>.2561</b>	.2587																											
		720	.3571	.3458	.3459	<b>.2480</b>	.2730	.3643	.3500	.3497	<b>.2581</b>	.2708	.3599	.3490	.3488	<b>.2573</b>	.2692																											
335	PatchTST	96	.4312	.4262	.4269	<b>.4242</b>	.4238	.4511	.4409	.4391	<b>.4390</b>	.4372	.5103	.4901	.4898	.4693	<b>.4684</b>																											
		192	.4955	.4865	.4854	<b>.4830</b>	.4805	.5046	.4934	.4937	<b>.4915</b>	.4906	.5954	.5617	.5620	.5372	<b>.5328</b>																											
		336	.5559	.5478	.5475	<b>.5438</b>	.5320	.5510	.5440	.5465	<b>.5385</b>	.5320	.6615	.6387	.6420	.5950	<b>.5878</b>																											
		720	.7117	.6860	.6822	<b>.6113</b>	.5997	.6630	.6431	.5969	<b>.5733</b>	.5733	.9233	.8142	.8375	.7001	<b>.6504</b>																											
336	ETTm2	96	.2362	.2351	.2362	<b>.2349</b>	.2343	.2306	.2288	.2288	<b>.2232</b>	.2265	.2582	.2551	.2552</td																													

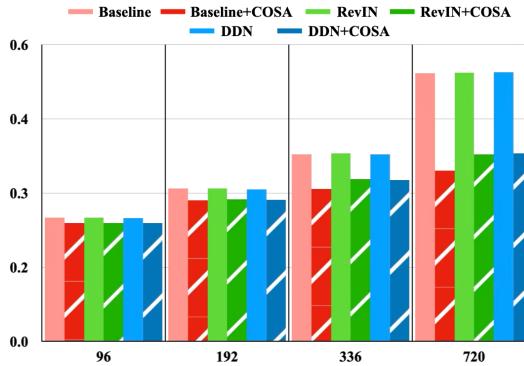


Figure 3: Prediction accuracy comparison with normalization methods.

COSA directly optimizes MSE on revealed targets and uses the context vector to encode recent level/scale, so the linear layer learns scale and level corrections from the error signal itself. Further analysis is provided in Appendix G.7.

#### 4.3 SENSITIVITY AND ABLATIONS

We probe the following four key design choices: 1) adaptation steps  $S$ , 2) context length  $K$ , 3) batch size  $B$ , and 4) adaptive learning rate  $CALR$ .

We evaluated performance by varying each hyperparameter individually while keeping others fixed at the default settings. Figure 4 shows MSE and wall-clock time according to each hyperparameter. Figure 4a shows changes according to the number of iterative learning steps  $S$ . COSA shows a pattern where test MSE decreases as  $S$  increases. However, while wall-clock time also increases with increasing  $S$ , even at the highest  $S = 4$  setting, it showed time levels similar to PETSA.

Figure 4b examines the effect of context length  $K$ , which controls how much past information the adapter uses. Accuracy improves consistently with larger  $K$ , while wall-clock time remains unchanged. Since the adapter input concatenates base model’s prediction with the context vector (dimensionality  $L + K$ ), and  $L$  typically dominates, increasing  $K$  has negligible runtime impact. The context provides incremental but reliable gains by supplementing the level/scale information.

Figure 4c shows performance changes with batch size  $B$ . As described in Section 3.5,  $B$  determines the frequency of adaptation, collecting  $B$  {prediction, ground truth} pairs before each update. Even with  $B = 96$ , COSA outperforms the baseline, with accuracy improving as  $B$  decreases due to more frequent adaptation. This explains the superior performance of COSA-P over COSA-F on ETTh1: the average  $B$  determined by PAAS for ETTh1 is 24.55, while for other datasets the values are over 80. Detailed analysis is provided in Appendix C. However, smaller  $B$  increases wall-clock time due to both more adaptation calls and the computational cost of adaptation steps  $S$ .

Figure 4d shows performance with and without  $CALR$  (Section 3.5).  $CALR$  achieves up to 12.13% accuracy improvement as the window length increases and a 21.34% reduction in wall-clock time. This confirms that aggressive dynamic learning rate scheduling enhances performance within limited adaptation steps  $S$  while enabling early-stopping for computational efficiency.

Results for additional ablations (context aggregation methods and correction layer architecture) are provided in Appendix G.

#### 4.4 COMPUTATIONAL OVERHEAD

Table 3: Computational overhead comparison of adapter methods.

Method	# Params ↓	Peak mem (MB) ↓	Samples/sec ↑	Adaptation time/batch (ms) ↓	Inference time/batch (ms) ↓
TAFAS	1,252,958	<b>17.59</b>	<b>1,413.23 ± 92.28</b>	<b>73.23 ± 8.74</b>	$10.96 \pm 0.64$
PETSA	<b>58,334</b>	36.09	$987.91 \pm 78.67$	88.46 ± 7.08	$12.63 \pm 0.37$
COSA (Ours)	1,211,287	27.07	1080.70 ± 80.66	80.12 ± 5.93	<b>1.25 ± 0.06</b>

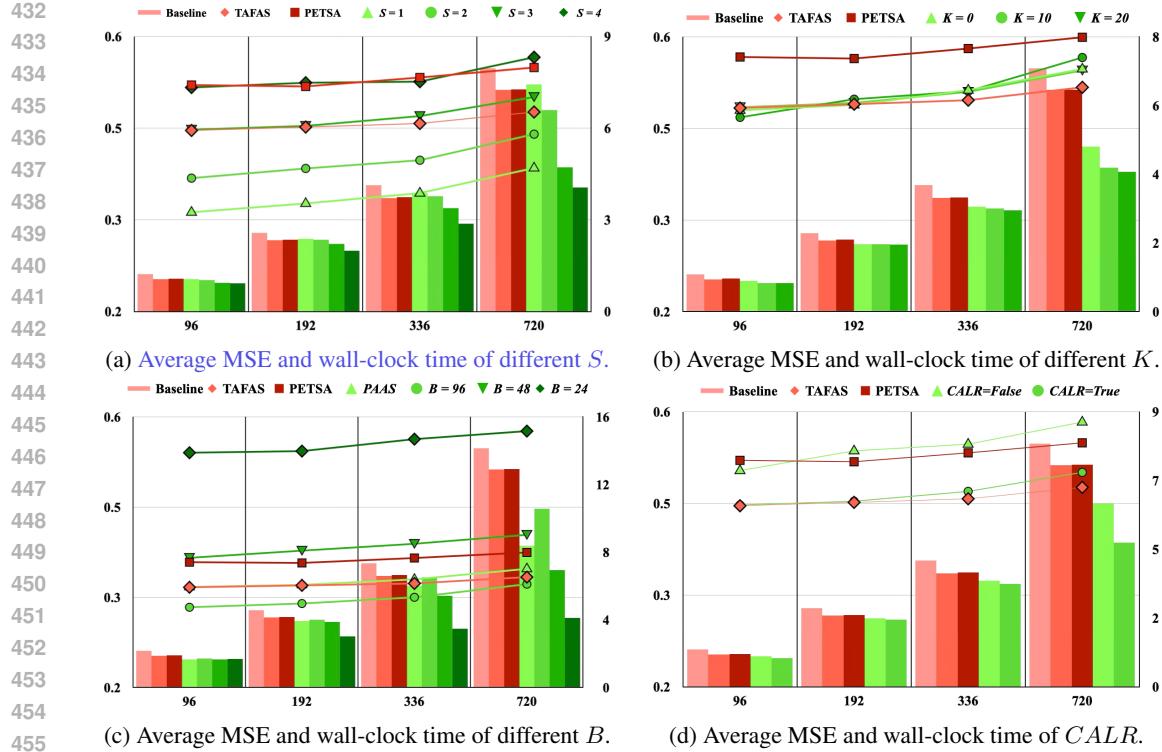


Figure 4: Hyperparameter analysis showing the trade-off between performance and efficiency. Charts display average test MSE (bars, left axis) and wall-clock time (lines, right axis, in seconds) across different parameter settings.

We report 1) observed additional parameters, 2) peak memory utilization, 3) throughput (samples per second), 4) wall-clock time per batch, and 5) inference time per batch.

All hyperparameters remain at default values. Table 3 summarizes the average overhead across all datasets, base model, and horizons. COSA shows moderate overhead, falling between TAFAS and PETSA, while achieving the significantly fastest inference time. COSA performs adaptation repeatedly for  $S$  steps, meaning that the throughput and adaptation time are dependent on  $S$ . However, the single adapter structure and simplicity of COSA alleviate the overhead and improve the inference time, which is not affected by  $S$ . The computational complexity is  $\mathcal{O}(L \cdot (L + K))$  for the linear transformation plus  $\mathcal{O}(L)$  for the gating operation, resulting in quadratic scaling with respect to prediction horizon  $L$ . Further theoretical calculations are included in Appendix B.

## 5 CONCLUSION AND LIMITATIONS

We introduced COSA, an architecture-agnostic TTA module that directly corrects the prediction of base model with a single linear layer guided by short-term context and a stabilizing gate. Across six benchmarks and diverse base models, COSA improves accuracy by 13.91% to 17.03% over baselines and by 10.48% to 13.05% over prior state-of-the-art TTA methods. These gains arise from the synergy of trend-aware context, residual correction, and gated modulation.

While COSA shows strong empirical results, several areas offer room for refinement. The current adaptation relies on full ground truth, though extending to partial observations would enable real-time deployment. Performance varies with batch size  $B$ , and the fixed context length  $K$  may not be optimal for all temporal patterns. Additionally, linear corrections, while effective for many cases, could be enhanced for complex nonlinear shifts.

Future work will explore masked updates for real-time adaptation with partial targets, adaptive selection of  $K$  and  $B$  based on detected periodicity, and hybrid linear/nonlinear adapters for more complex distribution shifts. These extensions will broaden the applicability of the proposed method while maintaining its computational efficiency.

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648 A ADAPTATION ALGORITHM OF COSA  
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650 This section details the core adaptation algorithm of COSA. This algorithm extends the optimizer  
651 mentioned in Equation 2, combining short-term loss trends, cosine annealing, and adaptive gradient  
652 clipping, batch-wise learning rate reset. We apply widely used values for the coefficients of *CALR*  
653 and the threshold value of early stopping. The base model remains frozen, operating only on adapter  
654 parameters  $\varphi = \{\mathbf{W}, \mathbf{b}, \mathbf{g}\}$ .

655 **Purpose:** Performs rapid adaptation of linear adapters using direct loss, adaptive learning rate  
656 scheduling, and gradient clipping to improve prediction accuracy within a few adaptation step  $S$ .  
657

658 **Algorithm 1** COSA adaptation.  
659

660 **Require:** Stream of batches  $(\hat{\mathbf{Y}}, \mathbf{Y}^{\text{true}})$  with length  $B$ , context vector  $\mathbf{C}$ , steps  $S$ ,  $\eta_{\min}, \eta_{\max}$ , weight decay  $\lambda$ ,  
661 clip base  $c$   
662 **Ensure:** adapted predictions with improved accuracy over the base model  
663 1: **for** each batch  $(\hat{\mathbf{Y}}, \mathbf{Y}^{\text{true}})$  in Data Stream **do** ▷ Loop over new batches  
664 2:   **Initialize:**  $\eta \leftarrow \eta_{\max}$ , loss history  $\mathcal{H} \leftarrow []$  ▷ Reset LR for new batch  
665 3:   **for**  $s = 1$  to  $S$  **do** ▷ Main adaptation loop  
666 4:     **Forward pass:** form  $\mathbf{X}^{(a)} = [\mathbf{Y}^{(0)} \parallel \mathbf{C}]$ , then  $\mathbf{H} = (\mathbf{W} \mathbf{X}^{(a)\top} + \mathbf{b})^\top$   
667 5:     **Gating:**  $\hat{\mathbf{Y}} \leftarrow \mathbf{Y}^{(0)} + \tanh(\mathbf{g}) \odot \mathbf{H}$   
668 6:     **MSE loss:**  $\mathcal{L} \leftarrow \|(\hat{\mathbf{Y}} - \mathbf{Y}^{\text{true}})\|_F^2 + \lambda \|\varphi\|_2^2$   
669 7:     **Learning rate adaptation:**  
670 8:       **if**  $|\mathcal{H}| \geq 2$  **then** ▷ Recent loss change  
671 9:          $\Delta \leftarrow \mathcal{L} - \mathcal{H}[-1]$  ▷ Loss increased - reduce LR  
672 10:        **if**  $\Delta > 0$  **then**  
673 11:            $\eta \leftarrow \max(0.5 \eta, \eta_{\min})$  ▷ Converged - increase LR for next batch  
674 12:        **else if**  $|\Delta| < 10^{-6}$  **then**  
675 13:            $\eta \leftarrow \min(1.1 \eta, \eta_{\max})$   
676 14:        **end if**  
677 15:       **end if**  
678 16:       **Cosine annealing:**  $\eta \leftarrow \eta_{\min} + \frac{1}{2}(\eta - \eta_{\min})(1 + \cos(\frac{s\pi}{S}))$   
679 17:       **Gradient computation:**  $g_\varphi \leftarrow \nabla_{\varphi} \mathcal{L}$   
680 18:       **Adaptive clipping:**  $\|g_\varphi\| \leftarrow \min(\|g_\varphi\|, \max(c, \mathcal{L}))$   
681 19:       **Parameter update:**  $\varphi \leftarrow \varphi - \eta g_\varphi$   
682 20:       **Early stopping:**  
683 21:       **if**  $s > 2$  and  $|\mathcal{H}[-1] - \mathcal{H}[-2]| < 10^{-6}$  **then**  
684 22:           **break**  
685 23:       **end if**  
686 24:     **end for**  
687 25: **end for**  
688

689 COSA targets TSF-TTA under non-stationary environments in which the distribution of time-series  
690 data changes over time. In such environments, the classical notion of convergence toward a fixed  
691 optimal point is not well-defined. Instead, stable learning within each adaptation window is critical.  
692 *CALR* guarantees uniformly bounded step-wise updates through the following four mechanisms,  
693 which structurally prevent error amplification and thus ensure stability during adaptation.

- 694 1. **Upper-bounded learning rate:** The learning rate is constrained by  $\eta \leq \eta_{\max}$ , limiting the  
695 maximum magnitude of a single-step update.
- 696 2. **Gradient clipping:** At Line 18 of Algorithm 1, the gradient norm is adaptively bounded as  
697  $\|g_\varphi\| \leftarrow \min(\|g_\varphi\|, \max(c, \mathcal{L}))$ .
- 698 3. **L2 regularization:** The weight-decay term in Equation 1,  $\lambda(\|\mathbf{W}\|_F^2 + \|\mathbf{b}\|_2^2 + \|g\|_2^2)$ , con-  
699 strains parameter magnitude.
- 700 4. **Bounded gating:** Because  $\alpha = \tanh(\mathbf{g}) \in [-1, 1]$ , the correction magnitude is structurally  
701 limited.

702 For every new batch, the learning rate is reinitialized to  $\eta_{\max}$  (Line 2 of Algorithm 1), giving  
703 each batch an equal opportunity for adaptation. The learning rate is then adapted according to the  
704 batch's loss behavior. When the loss spikes, we reduce the learning rate as  $\eta \leftarrow \max(0.5\eta, \eta_{\min})$ ,

702  
703  
704 Table 4: Average  $B$  of each dataset determined by PAAS.  
705  
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707

Dataset	ETTh1	ETTh2	ETTm1	ETTm2	Exchange Rate	Weather
Average $B$	24.55	38.41	92.73	83.41	92.80	80.38

708 temporarily lowering update intensity. When the loss decreases stably, we increase it as  $\eta \leftarrow$   
709  $\min(1.1\eta, \eta_{\max})$ , strengthening adaptation. This enables stable learning even when short-term per-  
710 turbations or anomalies appear in the input data, allowing rapid recovery.

711  
712 

## B COMPUTATIONAL COST

713  
714 In this section, we report theoretical calculations of parameters, FLOPs, and memory footprint.

715 For univariate time series, the number of parameters is as follows:

716  
717 **Parameter count.**

718  
719 
$$\underbrace{L(L+K)}_W + \underbrace{L}_b + \underbrace{1}_g \Rightarrow \# \text{params} = (L(L+K) + L + 1).$$
  
720

721 **FLOPs per adaptation step (batch of size  $B$ ).** The dominant cost is the linear transform and  
722 residual composition:

723  
724 
$$\mathcal{O}(B L(L+K)) \text{ for } \mathbf{W} \mathbf{X}^{(a)}, \text{ plus } \mathcal{O}(BL) \text{ for gating \& residual add.}$$

725 **Memory footprint.** Additional activations are modest: the linear residual  $\mathbf{H} \in \mathbb{R}^{B \times L}$  and the  
726 context vector  $\mathbf{C} \in \mathbb{R}^K$ . The total adaptation cost scales linearly with the number of adaptation  
727 steps  $S$  and variables  $V$ .728  
729 

## C BATCH SIZE ANALYSIS OF PAAS

730  
731 **Adaptive vs. Fixed Batch Strategy:** While COSA-F shows the best performance in most cases,  
732 COSA-P generally performs better on the ETTh1 and ETTh2 datasets, revealing important insights  
733 about temporal adaptation strategies. The reason for this trend is that the size of  $B$  determined  
734 by PAAS is often smaller than 48 for these datasets, as shown in Table 4, enabling more frequent  
735 adaptation that better captures the higher-frequency patterns characteristic of these hourly datasets.736  
737 This differential performance validates the importance of dataset-specific adaptation scheduling:  
738 datasets with more complex temporal dynamics benefit from more frequent adaptation (smaller  $B$ ),  
739 while datasets with smoother patterns can effectively use larger batch sizes for computational effi-  
740 ciency.741  
742 

## D BEHAVIOR ANALYSIS OF COSA

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744 

### D.1 ANALYSIS BETWEEN GATING AND LINEAR RESIDUAL LAYER

745  
746 In COSA, the gating is defined as  $\text{gating} = \tanh(g) \in [-1, 1]$ , where  $g$  is a learnable parameter,  
747 and this bounded scalar modulates the correction strength by multiplying the output of the linear  
748 residual layer. If we were to use  $g$  directly instead of  $\tanh(g)$ , small variations in  $g$  could induce  
749 disproportionately large and unstable changes in the correction, making the adapter overly sensitive to  
750 noisy points. The  $\tanh$  transform keeps the gating bounded, ensuring that changes in  $g$  are reflected  
751 smoothly and gradually. When the residual magnitude spikes, the gate moves toward 0, as shown in  
752 Figure 5, thereby attenuating the residual correction and stabilizing the adaptation process.753  
754 

### D.2 ANALYSIS BETWEEN LEARNING RATE AND MSE

755 Figure 6 visualizes the trajectory of pre-adaptation loss and learning rate for the iTransformer-  
ETTm1,  $L = 96$  case. As shown in Figure 6, when a short-term loss spike occurs, CALR immedi-

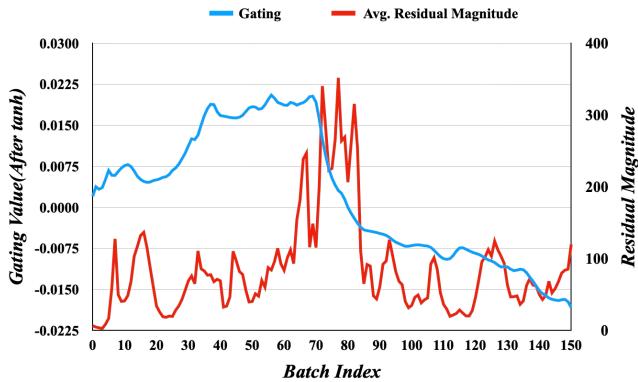


Figure 5: Trajectory of average gating and average residual magnitude of batches over time.

ately decreases the learning rate to minimize the impact of the perturbation, and once the loss enters a stable decreasing phase, CALR increases the learning rate again to promote rapid re-adaptation. This control mechanism suppresses excessive parameter drift without requiring roll-back, enabling COSA to recover its correction performance instantly after a perturbation. The interaction between the learning rate and loss shows that, in non-stationary environments with short-term perturbations, COSA can respond and recover performance stably.

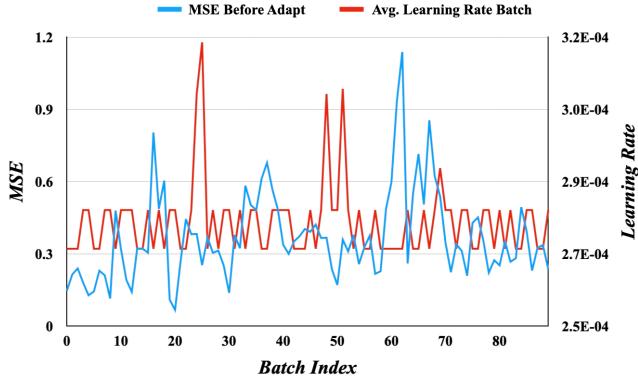


Figure 6: Trajectory of initial MSE and average learning rate of batches over time.

## E QUALITY OF TTA

To evaluate TTA quality, we measured Explained Residual Variance (ERV) and Negative Adaptation Rate (NAR) metrics across all datasets, base models, and forecasting horizons. ERV is defined as in Equation 3, where  $\hat{R}$  represents residuals for TTA-applied predictions and  $R^{(0)}$  represents residuals for base model predictions. Specifically, ERV quantifies the extent to which TTA reduces the residual variance of the base model’s predictions. Higher ERV values indicate greater residual variance reduction and correspondingly improved prediction performance through TTA.

$$\text{ERV} = 1 - \frac{\text{Var}(\hat{R})}{\text{Var}(R^{(0)})}. \quad (3)$$

NAR is the ratio of prediction windows where the MSE worsened when TTA was applied, with smaller values indicating better performance.

$$\text{NAR} = \frac{1}{N} \sum_{t=1}^N I[MSE(\hat{Y}_t) > MSE(Y_t^{(0)})], \quad \text{where } \begin{cases} I[\text{con}] = 1 & \text{if con = True} \\ I[\text{con}] = 0 & \text{otherwise} \end{cases} \quad (4)$$

810 Table 5: Average ERV and NAR across all benchmark datasets and base models.  
811

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	TAFAS	PETSA	COSA
ERV $\uparrow$	.0100	.0160	<b>.0768</b>
NAR $\downarrow$	34.94%	36.34%	<b>20.25%</b>

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812  
813 As shown in Table 5, COSA shows the highest ERV and the lowest NAR. This indicates that COSA  
814 provides effective TTA while decreasing the residual and improving accuracy on average.  
815816 

## F FURTHER EXPERIMENTS

  
817818 

### F.1 COMPARISON ON A LARGER DATASET

  
819820 To demonstrate that COSA can achieve stable and substantial performance gains even in larger-scale  
821 environments, we additionally conducted experiments on the Electricity dataset Lai et al. (2018);  
822 Godahewa et al. (2021). We followed the same experimental setup as in Section 4.1, and used three  
823 representative base models, iTransformer, DLinear, and FrTS. Table 6 is consistent with the findings  
824 in Section 4.2, COSA achieves either the best or second-best performance across all forecasting  
825 horizons  $L$ , and unlike other methods, which exhibit performance degradation compared to baselines  
826 in some cases, COSA improves their performances in every case. These results indicate that COSA  
827 remains robust and effective even in large-scale environments.  
828829 Table 6: Prediction accuracy comparison on Electricity dataset.  
830

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	iTransformer				DLinear				FrTS							
	No TTA	TAFAS	PETSA	COSA-F	COSA-P	No TTA	TAFAS	PETSA	COSA-F	COSA-P	No TTA	TAFAS	PETSA	COSA-F	COSA-P	
96	.1663	<b>.1568</b>	.1596	.1571	<b>.1570</b>	.2235	<b>.2224</b>	.2242	.2232	<b>.2228</b>	.1824	<b>.1781</b>	.1802	.1801	.1799	
192	.1794	<b>.1635</b>	.1644	<b>.1631</b>	<b>.1631</b>	.2242	.2153	.2152	<b>.2146</b>	<b>.2143</b>	.1794	.1894	.1781	<b>.1780</b>	<b>.1779</b>	
336	.1952	.1743	.1741	<b>.1730</b>	<b>.1727</b>	.2383	.2247	<b>.2233</b>	<b>.2226</b>	<b>.2223</b>	.1905	.1885	.1885	<b>.1881</b>	<b>.1879</b>	
720	.2567	.2316	.2301	<b>.2251</b>	<b>.2239</b>	.2792	.2629	.2615	<b>.2557</b>	<b>.2541</b>	.2304	.2299	.2287	<b>.2236</b>	<b>.2221</b>	

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831 

### F.2 COMPARISON WITH VARYING INPUT/PREDICTION LENGTH

  
832833 To further verify the performance of COSA across diverse scenarios, we conducted experiments by  
834 varying both the input window  $W$  and the prediction horizon  $L$ . To examine short-term forecasting  
835 rather than long-term forecasting, we added the setting  $W = 96$ ,  $L \in \{24, 48\}$ . To evaluate performance  
836 under longer input windows, we additionally tested  $W = 192$  with  $L \in \{192, 336, 720\}$  and  
837  $W = 336$  with  $L \in \{336, 720\}$ . Table 7 summarizes the results across these different combinations  
838 of  $W$  and  $L$ . Consistent with Section 4.2, COSA achieves the best or second-best performance in  
839 most cases, demonstrating its ability to maintain high predictive accuracy across a wide range of  
840 settings. Unlike other methods, which show performance degradation relative to baselines in several  
841 cases, COSA improves prediction accuracy over baselines in every case. In contrast, TAFAS and  
842 PETSA, which adopt dual-adapter architectures that modify both the input and output of base model  
843 incur substantial additional complexity as  $W$  increases, which likely contributes to their degraded  
844 performance. Since COSA operates solely in the output space of base model, it delivers consistent  
845 performance gains regardless of  $W$ .  
846847 

### F.3 COMPARISON WITH SOLID

  
848849 SOLID (Chen et al., 2024b) is a fine-tuning method of the prediction layer of the base model by  
850 detecting context drift. Its reconditioner estimates context drift based on the mutual information be-  
851 tween the model’s residual and the input context. When drift is detected, SOLID selectively chooses  
852 samples and fine-tunes the model’s prediction layer at the sample level. Like COSA, SOLID oper-  
853 ates in the output space of base model. However, unlike COSA, which keeps base model frozen and  
854 performs corrections through a lightweight adapter, SOLID directly updates the prediction layer of  
855 base model.  
856

864 Table 7: Prediction accuracy comparison with different input/prediction sequence length.  
865

		iTransformer						DLinear						FrTS					
		Input	Pred	No TTA	TAFAS	PETSA	COSA-F	COSA-P	No TTA	TAFAS	PETSA	COSA-F	COSA-P	No TTA	TAFAS	PETSA	COSA-F	COSA-P	
867	ETTh1	96	24	.3269	.3254	.3299	.3105	<b>.3098</b>	.3437	.3751	.3766	.3431	<b>.3429</b>	.2953	.3243	.3239	.2946	<b>.2943</b>	
		96	48	.3732	.3768	.3776	.3539	<b>.3527</b>	.3838	.4177	.4166	.3826	<b>.3820</b>	.3424	.3770	.3754	.3416	<b>.3413</b>	
		192	192	.4459	.5015	.4893	.4175	<b>.4120</b>	.4172	.4967	.4834	.4157	<b>.4141</b>	.4235	.4991	.4835	.4207	<b>.4186</b>	
		192	336	.4729	.5709	.5422	.4486	<b>.4456</b>	.4537	.5558	.5362	.4528	<b>.4489</b>	.4596	.5677	.5398	.4577	<b>.4535</b>	
		192	720	.5885	.6529	.6687	.5619	<b>.5477</b>	.5828	.6504	.6526	.5734	<b>.5660</b>	.6484	.6627	.6728	.6351	<b>.6190</b>	
		336	336	.5354	.6139	.5686	.5209	<b>.5059</b>	.4392	.5652	.5174	.4368	<b>.4289</b>	.4837	.6114	.5444	.4783	<b>.4674</b>	
872	ETTh2	336	720	.6512	.6873	.6635	.6115	<b>.5780</b>	.5748	.6344	.6443	.5589	<b>.5198</b>	.7265	.6905	.6738	.6960	<b>.6295</b>	
		96	24	<b>.0837</b>	.1277	.1266	<b>.0812</b>	<b>.0862</b>	.1217	.1218	<b>.0861</b>	<b>.0862</b>	.0812	.1180	.1178	<b>.0806</b>	.0807		
		96	48	.1047	.1518	.1520	<b>.1007</b>	.1008	.1031	.1444	.1452	<b>.1028</b>	.1030	.1004	.1452	.1447	<b>.0996</b>	<b>.0996</b>	
		192	192	.1633	.2272	.2280	<b>.1546</b>	.1563	.1344	.2155	.2096	<b>.1334</b>	.1338	.1437	.2218	.2184	<b>.1412</b>	.1420	
		192	336	.1658	.2541	.2487	<b>.1551</b>	.1573	.1474	.2445	.2394	<b>.1460</b>	.1468	.1556	.2494	.2460	<b>.1519</b>	.1536	
		192	720	.2197	.3453	.3192	<b>.2110</b>	.2158	.1782	.3152	.2962	<b>.1762</b>	.1778	.1943	.3261	.3086	<b>.1892</b>	.1925	
876	ETTh1	336	336	.2070	.2986	.3005	<b>.2021</b>	.2108	.1469	.2366	.2375	<b>.1447</b>	.1468	.1722	.2579	.2604	<b>.1645</b>	.1695	
		336	720	<b>.3334</b>	.4253	.4355	<b>.3255</b>	.3334	.1807	.3101	.3004	<b>.1776</b>	.1798	.1969	.3130	.3124	<b>.1920</b>	.1949	
		96	24	.2543	<b>.2359</b>	.2429	<b>.2405</b>	.2450	.2578	.2616	.2599	<b>.2523</b>	.2569	.2494	.2503	.2471	<b>.2449</b>	.2492	
		96	48	.3305	<b>.3099</b>	.3135	<b>.3115</b>	.3133	.3105	.3167	.3151	<b>.3035</b>	.3064	.3191	.3269	.3222	<b>.3171</b>	.3177	
		192	192	.3800	.4006	.3961	<b>.3591</b>	.3603	.3694	.4029	.3942	<b>.3643</b>	.3648	.3551	.3863	.3815	<b>.3524</b>	.3528	
		192	336	.4336	.4499	.4401	<b>.4149</b>	.4150	.4239	.4620	.4436	<b>.4162</b>	.4169	.4036	.4371	.4290	<b>.3985</b>	.3987	
878	ETTh2	192	720	.4992	.5385	.5090	<b>.4716</b>	.4718	.4797	.5376	.5101	<b>.4671</b>	.4681	.4631	.5152	.4941	<b>.4550</b>	.4560	
		336	336	.4820	.4913	<b>.4441</b>	.4490	.4592	.3981	.4444	.4244	<b>.3968</b>	.3977	.4011	.4380	.4275	<b>.3975</b>	.4006	
		336	720	.5202	.5432	.5169	<b>.4678</b>	.4904	.4437	.5053	.4852	<b>.4256</b>	.4423	.4407	.5046	.4877	<b>.4261</b>	.4397	
		96	24	.0542	.0800	.0744	<b>.0530</b>	.0531	.0601	.0782	.0777	<b>.0598</b>	.0599	<b>.0562</b>	.0748	.0741	<b>.0561</b>	<b>.0561</b>	
		96	48	.0735	.1044	.0988	<b>.0731</b>	.0732	.0767	.1027	.1015	<b>.0761</b>	.0762	.0736	.0992	.0987	<b>.0734</b>	<b>.0733</b>	
		192	192	.1035	.1647	.1601	<b>.1023</b>	<b>.1022</b>	.0990	.1451	.1429	<b>.0984</b>	.0985	.0998	.1480	.1456	<b>.0982</b>	.0984	
882	ETTh1	192	336	.1343	.2191	.1970	<b>.1339</b>	.1201	.1791	.1741	<b>.1190</b>	.1195	.1210	.1863	.1781	<b>.1200</b>	<b>.1192</b>		
		192	720	.1628	.2511	.2377	<b>.1564</b>	.1589	.1518	.2291	.2247	<b>.1473</b>	.1498	.1476	.2337	.2232	<b>.1436</b>	.1446	
		336	336	.1354	.2280	.1987	<b>.1328</b>	.1347	.1176	.1782	.1704	<b>.1167</b>	.1174	.1198	.1815	.1760	<b>.1172</b>	.1188	
		336	720	.1645	.2785	.2517	<b>.1455</b>	.1604	.1456	.2338	.2218	<b>.1317</b>	.1446	.1490	.2309	.2255	<b>.1289</b>	.1453	
		96	24	.0318	<b>.0292</b>	<b>.0273</b>	.0306	.0306	.0434	<b>.0397</b>	<b>.0393</b>	.0434	.0434	.0283	<b>.0254</b>	<b>.0241</b>	.0283	.0283	
		96	48	.0526	.0542	<b>.0479</b>	<b>.0516</b>	.0516	.0606	<b>.0590</b>	<b>.0579</b>	.0606	.0606	.0481	<b>.0438</b>	<b>.0418</b>	.0480	.0481	
886	ETTh2	192	192	.2045	<b>.1999</b>	.2189	<b>.2040</b>	.2040	.1715	.1819	.2024	<b>.1714</b>	.1715	<b>.1655</b>	.1728	.1809	<b>.1655</b>	<b>.1655</b>	
		192	336	.2963	.3221	.3511	<b>.2919</b>	.2933	.2878	.3316	.3484	<b>.2850</b>	.2875	.2804	.3129	.3318	<b>.2780</b>	.2802	
		192	720	.8546	.7713	.7828	.8316	.8320	.9037	.9393	.9488	<b>.9016</b>	.9016	<b>.4506</b>	.8200	.8315	<b>.4501</b>	<b>.4501</b>	
		336	336	.4088	<b>.3790</b>	.4204	<b>.4036</b>	.4036	.2753	.3036	.3323	<b>.2700</b>	.2751	.3246	<b>.3219</b>	.3589	<b>.3182</b>	.3245	
		336	720	1.7882	<b>.10041</b>	<b>.10775</b>	.15829	.15828	.5274	.8620	.8816	<b>.5269</b>	.5269	.4266	.9353	.9175	<b>.4263</b>	<b>.4263</b>	
		96	24	.1095	<b>.1026</b>	<b>.1016</b>	.1077	.1207	<b>.1151</b>	<b>.1151</b>	.1200	<b>.1199</b>	.1193	<b>.1085</b>	<b>.1111</b>	.1183	.1183		
893	ETTh1	96	48	.1380	<b>.1292</b>	<b>.1310</b>	.1362	.1363	.1581	.1499	<b>.1475</b>	.1559	.1560	.1530	<b>.1435</b>	.1452	.1508	.1510	
		192	192	.2165	.2102	<b>.2051</b>	<b>.2075</b>	.2099	.2393	<b>.2225</b>	<b>.2214</b>	.2332	.2354	.2131	<b>.2058</b>	.2086	.2108		
		192	336	.2747	.2588	<b>.2549</b>	.2611	.2653	.2904	.2709	<b>.2691</b>	.2791	.2829	.2694	<b>.2547</b>	<b>.2531</b>	.2604	.2637	
		192	720	.3321	.3316	.3390	<b>.3151</b>	.3211	.3426	.3363	.3446	<b>.3276</b>	.3339	.3290	.3360	<b>.3158</b>	.3205		
		336	336	.2988	<b>.2705</b>	<b>.2708</b>	.2778	.2978	.2722	.2633	<b>.2619</b>	.2627	.2707	.2526	.2520	<b>.2474</b>	.2504		
		336	720	.3381	.3423	.3557	<b>.2885</b>	.3340	.3245	.3247	.3316	<b>.2742</b>	.3207	.3129	.3203	.3229	<b>.2648</b>	.3088	
894	ETTh2	96	24	.1026	<b>.1016</b>	<b>.1016</b>	.1077	.1207	<b>.1151</b>	<b>.1151</b>	.1200	<b>.1199</b>	.1193	<b>.1085</b>	<b>.1111</b>	.1183	.1183		
		96	48	.1310	<b>.1292</b>	<b>.1310</b>	.1362	.1363	.1581	.1499	<b>.1475</b>	.1559	.1560	.1530	<b>.1435</b>	.1452	.1508	.1510	
		192	192	.2102	<b>.2051</b>	<b>.2075</b>	.2099	.2393	<b>.2225</b>	<b>.2214</b>	.2332	.2354	.2131	<b>.2058</b>	.2086	.2108			
		192	336	.2747	.2588	<b>.2549</b>	.2611	.2653	.2904	.2709	<b>.2691</b>	.2791	.2829	.2694	<b>.2547</b>	<b>.2531</b>	.2604	.2637	
		192	720	.3321	.3316	.3390	<b>.3151</b>	.3211	.3426	.3363	.3446	<b>.3276</b>	.3339	.3290	.3360	<b>.3158</b>	.3205		
		336	336	.2988	<b>.2705</b>	<b>.2708</b>	.2778	.2978	.2722	.2633	<b>.2619</b>	.2627	.2707	.2526	.2520	<b>.2474</b>	.2504		
895	ETTh1	96	24	.1026	<b>.1016</b>	<b>.1016</b>	.1077	.1207	<b>.1151</b>	<b>.1151</b>	.1200	<b>.1199</b>	.1193	<b>.1085</b>	<b>.1111</b>	.1183	.1183		
		96	48	.1310	<b>.1292</b>	<b>.1310</b>	.1362	.1363	.1581	.1499	<b>.1475</b>	.1559	.1560	.1530	<b>.1435</b>	.1452	.1508	.1510	
		192	192	.2102	<b>.2051</b>	<b>.2075</b>	.2099	.2393	<b>.2225</b>	<b>.2214</b>	.2332	.2354	.2131	<b>.2058</b>	.2086	.2108			
		192	336	.2747	.2588	<b>.2549</b>	.2611	.2653	.2904	.2709	<b>.2691</b>	.2791	.2829	.2694	<b>.2547</b>	<b>.2531</b>	.2604	.2637	
		192	720	.3321	.3316	.3390	<b>.3151</b>	.3211	.3426	.3363	.3446	<b>.3276</b>	.3339	.3290	.3360	<b>.3158</b>	.3205		
		336	336	.2988	<b>.2705</b>	<b>.2708</b>	.2778	.2978	.2722	.2633	<b>.2619</b>	.2627	.2707	.2526	.2520	<b>.2474</b>	.2504		
896	ETTh2	96	24	.1026	<b>.1016</b>	<b>.1016</b>	.1077	.1207	<b>.1151</b>	<b>.1151</b>	.1200	<b>.1199</b>	.1193	<b>.1085</b>	<b>.1111</b>	.1183	.1183		
		96	48	.1310	<b>.1292</b>	<b>.1310</b>	.1362	.1363	.1581	.1499	<b>.1475</b>	.1559	.1560	.1530	<b>.1435</b>	.1452	.1508	.1510	
		192	192	.2102	<b>.</b>														

Table 8: Comparison with SOLID

	iTransformer		DLinear		FreTS	
	SOLID		COSA-P		SOLID	
	COSA-P		SOLID		COSA-P	
ETTh1	96	.4404	<b>.4363</b>	.4595	<b>.4574</b>	<b>.4093</b>
	192	.4935	<b>.4919</b>	.5063	<b>.5066</b>	<b>.4701</b>
	336	.5420	<b>.5300</b>	.5602	<b>.5528</b>	<b>.5254</b>
	720	<b>.6523</b>	.5638	.7107	<b>.6107</b>	.6980
ETTh2	96	<b>.2480</b>	.2493	.2315	<b>.2281</b>	.2354
	192	.3061	<b>.2947</b>	.2824	<b>.2819</b>	.2830
	336	<b>.3339</b>	<b>.3339</b>	.3103	<b>.3083</b>	.3248
	720	.3701	<b>.3591</b>	<b>.3136</b>	.3477	<b>.3167</b>
ETTm1	96	<b>.3353</b>	.3455	.3634	<b>.3456</b>	<b>.3121</b>
	192	.4266	<b>.4140</b>	.4336	<b>.4222</b>	.4299
	336	.5019	<b>.4643</b>	.5071	<b>.4858</b>	.4915
	720	.5986	<b>.5102</b>	.5821	<b>.4991</b>	.5612
ETTm2	96	.1641	<b>.1632</b>	.1590	<b>.1583</b>	.1574
	192	.2291	<b>.2173</b>	.1910	<b>.1943</b>	.1933
	336	<b>.2525</b>	.2535	<b>.2138</b>	.2242	.2328
	720	.2704	<b>.2606</b>	.2419	<b>.2316</b>	.2377
Exchange Rate	96	.0873	<b>.0837</b>	.0913	<b>.0834</b>	.0822
	192	.1783	<b>.1479</b>	.1826	<b>.1519</b>	.1723
	336	.3294	<b>.2624</b>	.3276	<b>.2480</b>	.3218
	720	.7531	<b>.4460</b>	.8872	<b>.4481</b>	.8325
Weather	96	.1753	<b>.1617</b>	.1954	<b>.1793</b>	.1849
	192	.2231	<b>.2088</b>	.2403	<b>.2217</b>	.2309
	336	.2801	<b>.2515</b>	.2918	<b>.2626</b>	.2843
	720	.3450	<b>.2730</b>	.3643	<b>.2708</b>	.3561

Table 9: Prediction accuracy comparison with DynaTTA Grover &amp; Etemad (2025).

	Transformer-based				Linear-based				MLP-based			
	iTransformer		PatchTST		DLinear		OLS		FreTS		MICN	
	DynaTTA	COSA-F	DynaTTA	COSA-P	DynaTTA	COSA-F	DynaTTA	COSA-P	DynaTTA	COSA-F	DynaTTA	COSA-P
ETTh1	96	.4523	<b>.4368</b>	<b>.4363</b>	.8371	<b>.4242</b>	<b>.4238</b>	.4708	<b>.4574</b>	<b>.4482</b>	.4486	<b>.4390</b>
	192	.5175	<b>.4961</b>	<b>.4919</b>	.8006	<b>.4830</b>	<b>.4805</b>	.5321	<b>.5066</b>	<b>.5050</b>	.5096	<b>.4915</b>
	336	.5874	<b>.5651</b>	<b>.5300</b>	.8097	<b>.5438</b>	<b>.5320</b>	.5792	<b>.5528</b>	<b>.5456</b>	.5626	<b>.5385</b>
	720	.7123	<b>.5958</b>	<b>.5638</b>	1.0887	<b>.6113</b>	<b>.5822</b>	.7112	<b>.6107</b>	<b>.5896</b>	.6933	<b>.5969</b>
ETTh2	96	.2630	<b>.2504</b>	<b>.2493</b>	.4154	<b>.2349</b>	<b>.2343</b>	.2338	<b>.2300</b>	<b>.2281</b>	.2326	<b>.2232</b>
	192	.3210	<b>.2983</b>	<b>.2947</b>	.4154	<b>.2665</b>	<b>.2608</b>	.2888	<b>.2827</b>	<b>.2819</b>	.2911	<b>.2796</b>
	336	.3677	<b>.3241</b>	<b>.3339</b>	.4386	<b>.2971</b>	<b>.2978</b>	.3380	<b>.3050</b>	<b>.3083</b>	.3430	<b>.3003</b>
	720	.4646	<b>.3487</b>	<b>.3591</b>	.4991	<b>.3233</b>	<b>.3428</b>	.4325	<b>.3062</b>	<b>.3477</b>	.4270	<b>.3177</b>
ETTm1	96	.3753	<b>.3447</b>	<b>.3455</b>	.7205	<b>.3625</b>	<b>.3626</b>	.3814	<b>.3456</b>	<b>.3475</b>	.3830	<b>.3454</b>
	192	.4835	<b>.4124</b>	<b>.4124</b>	.6898	<b>.4250</b>	<b>.4258</b>	.4809	<b>.4113</b>	<b>.4122</b>	.4827	<b>.4115</b>
	336	.5843	<b>.4569</b>	<b>.4643</b>	.8073	<b>.4568</b>	<b>.4697</b>	.5711	<b>.4753</b>	<b>.4858</b>	.5719	<b>.4748</b>
	720	.7243	<b>.4773</b>	<b>.5102</b>	.9292	<b>.4681</b>	<b>.4882</b>	.6569	<b>.4774</b>	<b>.4991</b>	.6884	<b>.4763</b>
ETTm2	96	.1832	<b>.1627</b>	<b>.1632</b>	.2508	<b>.1558</b>	<b>.1562</b>	.1640	<b>.1583</b>	<b>.1586</b>	.1684	<b>.1582</b>
	192	.2897	<b>.2171</b>	<b>.2173</b>	.2744	<b>.2007</b>	<b>.2022</b>	.2040	<b>.1904</b>	<b>.1905</b>	.2115	<b>.1906</b>
	336	.3246	<b>.2435</b>	<b>.2535</b>	.3434	<b>.2258</b>	<b>.2352</b>	.2908	<b>.2083</b>	<b>.2242</b>	.2917	<b>.2131</b>
	720	.5344	<b>.2477</b>	<b>.2606</b>	.4447	<b>.2446</b>	<b>.2645</b>	.3765	<b>.2215</b>	<b>.2316</b>	.4571	<b>.2171</b>
Exchange Rate	96	.0983	<b>.0818</b>	<b>.0837</b>	.1217	<b>.0765</b>	<b>.0788</b>	.0948	<b>.0812</b>	<b>.0834</b>	.0918	<b>.0756</b>
	192	.1970	<b>.1403</b>	<b>.1479</b>	.2517	<b>.1464</b>	<b>.1570</b>	.1975	<b>.1459</b>	<b>.1519</b>	.1749	<b>.1393</b>
	336	.3251	<b>.2089</b>	<b>.2624</b>	.3728	<b>.1983</b>	<b>.2445</b>	.3001	<b>.2039</b>	<b>.2480</b>	.3024	<b>.2020</b>
	720	.8790	<b>.3421</b>	<b>.4460</b>	.9999	<b>.3543</b>	<b>.4662</b>	.8812	<b>.3494</b>	<b>.4481</b>	.8300	<b>.3444</b>
Weather	96	.1823	<b>.1597</b>	<b>.1617</b>	.2317	<b>.1624</b>	<b>.1634</b>	.1950	<b>.1773</b>	<b>.1793</b>	.1985	<b>.1772</b>
	192	.2678	<b>.2067</b>	<b>.2088</b>	.2611	<b>.2106</b>	<b>.2108</b>	.3311	<b>.2216</b>	<b>.2217</b>	.3074	<b>.2223</b>
	336	.3894	<b>.2503</b>	<b>.2515</b>	.3329	<b>.2451</b>	<b>.2488</b>	.4103	<b>.2567</b>	<b>.2626</b>	.5953	<b>.2551</b>
	720	.4996	<b>.2480</b>	<b>.2730</b>	.4067	<b>.2590</b>	<b>.2713</b>	.4915	<b>.2581</b>	<b>.2708</b>	.4974	<b>.2579</b>

## F.5 COMPARISON WITH VARIOUS BATCH SIZES

Table 10a and Table 10b summarize the prediction accuracy and efficiency overhead under different batch sizes  $B$ . Thanks to CALR’s stability-induced design, COSA adapts reliably even with very small batches, and the resulting increase in update frequency often leads to improved forecasting accuracy. Notably, even in extremely small settings such as  $B = 8$ , COSA maintains higher accuracy than existing TTA methods, demonstrating resilience against over-correction and short-term perturbations. On the other hand, smaller  $B$  inevitably increases the number of adaptation steps, leading

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Table 10: Performance comparison with different batch sizes  $B$ .

(a) Prediction accuracy.

	No TTA	TAFAS	PETSA	PAAS	8	16	24	48	96
<b>96</b>	0.2545	0.2471	0.2480	0.2409	<b>0.1908</b>	<u>0.2202</u>	0.2330	0.2398	0.2411
<b>192</b>	0.3144	0.3038	0.3046	0.2887	<b>0.1900</b>	<u>0.2295</u>	0.2524	0.2848	0.2946
<b>336</b>	0.3839	0.3653	0.3664	0.3280	<b>0.1837</b>	<u>0.2292</u>	0.2526	0.3013	0.3483
<b>720</b>	0.5539	0.5226	0.5232	0.3804	<b>0.1811</b>	<u>0.2384</u>	0.2672	0.3286	0.4158

(b) Wall-clock time (Seconds).

	TAFAS	PETSA	PAAS	8	16	24	48	96
<b>96</b>	<u>5.9271</u>	7.4129	7.0642	47.3922	25.6158	17.2297	9.6333	<b>5.1258</b>
<b>192</b>	<u>6.0383</u>	7.3675	7.1419	49.4422	25.1222	18.0969	9.4344	<b>5.5133</b>
<b>336</b>	<u>6.1554</u>	7.6588	7.4131	49.2211	25.1119	17.2906	9.5644	<b>5.8081</b>
<b>720</b>	<b>6.5300</b>	7.9867	8.1578	46.3711	24.4683	17.6253	10.3036	<u>6.5397</u>

to higher adaptation time and a clear computation–accuracy trade-off. Considering this trade-off, we adopt  $B = 48$  for COSA-F in our main experiments, which provides a balanced choice between accuracy gains and computational efficiency.

## G ADDITIONAL ABLATIONS

This section provides additional ablation studies on various design choices of COSA. Each experiment was conducted to understand the impact of specific components and determine optimal hyperparameters. The default setting uses mean-based context aggregation with  $K = 10$  and  $S = 3$ .

### G.1 CONTEXT BUILDING METHODS COMPARISON

#### G.1.1 STATISTICAL METHODS

This experiment was conducted to evaluate the impact of different context construction methods on adapter performance. We compared three methods, i.e., Mean, Median, and Weighted Average (WA), to find the optimal context construction strategy. The weight of WA was designed to assign greater weight to recent values using exponential decay weighting. Table 11 presents a comprehensive performance comparison of the three context construction methods.

Mean-based context construction demonstrated superior performance compared to median and weighted average approaches across most experimental configurations. While median-based aggregation provided robustness against outliers, it resulted in lower overall accuracy. The weighted average approach showed marginal improvements relative to its implementation complexity. These findings support the adoption of simple statistical aggregation for effective context summarization in COSA.

#### G.1.2 CONTEXT SELECTION STRATEGY

COSA aims not to model long-term time-series structure, but to perform fast and stable local residual correction for output bias observed in the current window. In non-stationary environments, the input distribution shifts continuously over time; thus, information from distant past windows may become misaligned with the current drift direction and deteriorate correction quality. For this reason, the default COSA employs a lightweight context vector constructed solely from the most recently observed batches.

To examine the effects of longer-range temporal patterns, we additionally implemented a Selective Context mechanism. This approach stores all past context values in a buffer and computes importance scores via attention between the current window and past contexts, selecting the top- $K$  values

Table 11: Prediction accuracy comparison of diverse aggregation functions.

	Transformer-based						Linear-based						MLP-based						
	iTransformer			PatchTST			DLinear			OLS			FreTS			MICN			
	Mean	Median	WA	Mean	Median	WA	Mean	Median	WA	Mean	Median	WA	Mean	Median	WA	Mean	Median	WA	
ETTh1	96	<b>.4327</b>	.4472	<b>.4472</b>	<b>.4092</b>	.4274	.4275	<b>.4615</b>	.4660	.4657	<b>.4359</b>	.4463	.4462	<b>.4362</b>	.4439	.4440	<b>.4704</b>	.4934	.4926
	192	<b>.4491</b>	.4850	.4870	<b>.4422</b>	.4778	.4770	<b>.4869</b>	.5090	.5111	<b>.4932</b>	.4897	.4894	<b>.4671</b>	.4893	.4954	<b>.4769</b>	.5567	.5568
	336	<b>.4476</b>	.5301	.5317	<b>.4550</b>	.5199	.5285	<b>.4632</b>	.5379	.5378	<b>.5188</b>	.5208	.5209	<b>.4411</b>	.5273	.5245	<b>.4814</b>	.5889	.5904
	720	<b>.4592</b>	.6237	.6251	<b>.4788</b>	.6329	.6335	.4777	.6358	.6376	<b>.5616</b>	.6243	.6242	<b>.4755</b>	.6439	.6428	<b>.5230</b>	.7196	.7181
ETTh2	96	<b>.2489</b>	.2532	.2536	<b>.2336</b>	.2346	.2358	<b>.2303</b>	.2352	.2324	<b>.2283</b>	.2300	.2299	<b>.2359</b>	.2379	.2382	<b>.2468</b>	.2566	.2568
	192	<b>.3003</b>	.3012	.3013	<b>.2708</b>	.2886	.2894	<b>.2682</b>	.2846	.2863	<b>.2762</b>	.2954	.2893	<b>.2766</b>	.2846	.2917	<b>.2906</b>	.3190	.3145
	336	<b>.3277</b>	.3671	.3685	<b>.2688</b>	.3190	.3202	<b>.2860</b>	.3283	.3285	<b>.2937</b>	.3030	.3025	<b>.2889</b>	.3214	.3205	<b>.3088</b>	.3429	.3426
	720	<b>.3311</b>	.4013	.4023	<b>.3091</b>	.3737	.3737	<b>.3006</b>	.3358	.3358	<b>.2992</b>	.3415	.3415	<b>.2979</b>	.3588	.3564	<b>.3454</b>	.4172	.4185
ETTm1	96	<b>.3428</b>	.3687	.3685	<b>.3604</b>	.3918	.3921	<b>.3453</b>	.3575	.3574	<b>.3440</b>	.3573	.3572	<b>.3522</b>	.3633	.3633	<b>.3804</b>	.4252	.4248
	192	<b>.4076</b>	.4307	.4304	<b>.4171</b>	.4398	.4398	<b>.4158</b>	.4266	.4265	<b>.4125</b>	.4265	.4263	<b>.4173</b>	.4257	.4266	<b>.4402</b>	.4742	.4740
	336	<b>.4663</b>	.4930	.4949	<b>.4662</b>	.4942	.4944	<b>.4784</b>	.5009	.5005	<b>.4700</b>	.4995	.5006	<b>.4771</b>	.4898	.4886	<b>.4937</b>	.5381	.5381
	720	<b>.4940</b>	.5614	.5615	<b>.4776</b>	.5359	.5316	<b>.4928</b>	.5640	.5603	<b>.4693</b>	.5638	.5653	<b>.4863</b>	.5414	.5419	<b>.5083</b>	.5830	.5838
ETTm2	96	<b>.1616</b>	.1672	.1653	<b>.1552</b>	.1591	.1595	<b>.1578</b>	.1594	.1596	<b>.1583</b>	.1596	.1600	<b>.1556</b>	.1592	.1594	<b>.1710</b>	.1712	.1723
	192	<b>.2172</b>	.2194	.2240	<b>.1989</b>	.2087	.2121	<b>.1900</b>	.1959	.1957	<b>.1919</b>	.1970	.1995	<b>.1908</b>	.1935	.1933	<b>.2102</b>	.2131	.2132
	336	<b>.2402</b>	.2700	.2762	<b>.2279</b>	.2821	.2543	<b>.2135</b>	.2448	.2561	<b>.2066</b>	.2499	.2477	<b>.2158</b>	.2353	.2420	<b>.2354</b>	.2523	.2546
	720	<b>.2550</b>	.3461	.3463	<b>.2397</b>	.3011	.3222	<b>.2357</b>	.2985	.2833	<b>.2104</b>	.3179	.2821	<b>.2360</b>	.2732	.2753	<b>.2510</b>	.3020	.3084
Exchange Rate	96	<b>.0843</b>	.0852	.0852	<b>.0803</b>	.0814	.0815	<b>.0843</b>	.0884	.0885	<b>.0728</b>	.0787	.0787	<b>.0790</b>	.0785	.0785	<b>.0980</b>	.1065	.1068
	192	<b>.1540</b>	.1606	.1607	<b>.1480</b>	.1544	.1546	<b>.1599</b>	.1653	.1654	<b>.1335</b>	.1507	.1509	<b>.1390</b>	.1500	.1502	<b>.1827</b>	.1870	.1872
	336	<b>.2588</b>	.2754	.2756	<b>.2611</b>	.2787	.2789	<b>.2565</b>	.2918	.2920	<b>.1833</b>	.2736	.2738	<b>.2511</b>	.2683	.2684	<b>.2660</b>	.3040	.3043
	720	<b>.5039</b>	.5113	.5115	<b>.4937</b>	.5076	.5078	<b>.5001</b>	.5267	.5270	<b>.3349</b>	.4983	.4986	<b>.4789</b>	.4977	.4980	<b>.4815</b>	.5806	.5809
Weather	96	<b>.1636</b>	.1726	.1726	<b>.1655</b>	.1731	.1735	<b>.1738</b>	.1931	.1931	<b>.1748</b>	.1934	.1934	<b>.1758</b>	.1831	.1835	<b>.1666</b>	.1739	.1738
	192	<b>.2073</b>	.2268	.2265	<b>.2052</b>	.2162	.2162	<b>.2217</b>	.2500	.2520	<b>.2144</b>	.2496	.2490	<b>.2151</b>	.2346	.2347	<b>.2060</b>	.2208	.2205
	336	<b>.2474</b>	.2707	.2707	<b>.2443</b>	.2668	.2660	<b>.2622</b>	.2891	.2885	<b>.2428</b>	.2911	.2897	<b>.2630</b>	.2736	.2735	<b>.2735</b>	.2650	.2648
	720	<b>.2907</b>	.3118	.3119	<b>.2682</b>	.3088	.3090	<b>.2713</b>	.3310	.3325	<b>.2487</b>	.3327	.3331	<b>.2583</b>	.3268	.3247	<b>.2670</b>	.3140	.3094
Average		<b>.3121</b>	.3450	.3458	<b>.3032</b>	.3364	.3366	<b>.3097</b>	.3423	.3422	<b>.2990</b>	.3371	.3354	<b>.3046</b>	.3334	.3340	<b>.3284</b>	.3669	.3670

to form the context vector. Such a mechanism can leverage repeated phases or cycles in datasets with strong periodicity.

Table 12a compares COSA (the standard recent-context construction) with the dynamic context selection method. While the dynamic context selection method achieves clear improvements on datasets such as ETT, where the periodic structure is strong and easily detectable, the overall performance of the original COSA remains superior. Selective Context also introduces non-trivial overhead, since computing importance scores increases both adaptation time and inference time. Moreover, in fully non-stationary settings where distributional characteristics change continuously, older contexts may become outdated and destabilize the correction process. Nonetheless, the observed gains on datasets with pronounced periodicity show the potential of Selective Context. We provide a more detailed discussion of these observations in Section H.

### G.1.3 COMPARISON WITH ENCODER-BASED CONTEXT

To compare with encoder-based context construction, we implemented an alternative approach that replaces the original statistics-based method in COSA with a temporal encoder that directly consumes the previously observed ground-truth sequence from the past 720 steps (the longest  $L$ ). We added RNN-, LSTM-, and Attention-based encoders, each taking the past sequence in the form of  $[720, 1]$  as input and producing a  $[K, 1]$  context vector. The resulting context vector is concatenated with the base model’s prediction output, just as in the original design, and then fed into the linear correction layer. The encoder is seamlessly integrated at the front of COSA, modifying only the context-generation stage while keeping the remaining components unchanged.

Table 13 shows that, except for a few isolated cases, the original statistics-based context (0.3240) performs better than encoder-based alternatives (0.3254, 0.3260, 0.3278). Furthermore, the added architectural complexity increases both adaptation and inference overhead. In non-stationary TTA settings, where the input distribution shifts rapidly and adaptation steps are short, it is difficult for an encoder to learn stable temporal representations. Consequently, the generated embeddings may become misaligned with the current drift direction or overfit to outdated historical patterns, ultimately degrading correction performance.

Table 12: Prediction accuracy and overhead of selective context.

(a) Prediction accuracy.

	Transformer-based		Linear-based			MLP-based		
	iTransformer	PatchTST	DLinear	OLS	FrTS	MICN		
	Recent	Selective	Recent	Selective	Recent	Selective	Recent	Selective
ETTh1	96	.4363	<b>.4362</b>	.4238	<b>.4234</b>	<b>.4482</b>	.4562	.4372
	192	<b>.4919</b>	.4927	<b>.4805</b>	.4848	<b>.5050</b>	.5088	<b>.4906</b>
	336	<b>.5300</b>	.5367	.5320	<b>.5310</b>	<b>.5456</b>	.5541	.5320
	720	<b>.5638</b>	.5671	<b>.5822</b>	.5881	<b>.5896</b>	.6180	<b>.5733</b>
ETTh2	96	<b>.2493</b>	.2494	<b>.2343</b>	.2349	.2281	<b>.2258</b>	.2265
	192	.2947	<b>.2942</b>	<b>.2608</b>	.2661	.2819	<b>.2813</b>	<b>.2791</b>
	336	<b>.3339</b>	.3367	.2978	<b>.2949</b>	.3083	<b>.3064</b>	.3043
	720	<b>.3591</b>	.3603	<b>.3428</b>	.3453	.3477	<b>.3462</b>	<b>.3453</b>
ETTm1	96	.3455	<b>.3440</b>	<b>.3626</b>	.3627	<b>.3475</b>	<b>.3456</b>	.3475
	192	.4140	<b>.4128</b>	<b>.4258</b>	.4278	.4122	<b>.4221</b>	<b>.4119</b>
	336	<b>.4643</b>	.4718	.4697	<b>.4693</b>	.4858	<b>.4857</b>	<b>.4749</b>
	720	<b>.5102</b>	.5246	.4882	<b>.4868</b>	<b>.4991</b>	.5065	.5007
ETTm2	96	.1632	<b>.1631</b>	.1562	<b>.1560</b>	.1586	<b>.1582</b>	.1586
	192	.2173	<b>.2165</b>	.2022	<b>.2011</b>	.1905	<b>.1930</b>	.1907
	336	<b>.2535</b>	.2551	.2352	<b>.2331</b>	<b>.2242</b>	.2245	.2226
	720	.2606	<b>.2578</b>	.2645	<b>.2633</b>	<b>.2316</b>	.2427	<b>.2349</b>
Exchange Rate	96	.0837	<b>.0835</b>	<b>.0788</b>	.0789	<b>.0834</b>	<b>.0773</b>	.0773
	192	<b>.1479</b>	.1516	.1570	<b>.1554</b>	<b>.1519</b>	.1543	<b>.1457</b>
	336	<b>.2624</b>	.2633	<b>.2445</b>	.2478	<b>.2480</b>	.2481	<b>.2323</b>
	720	<b>.4460</b>	.4749	<b>.4662</b>	.4983	<b>.4481</b>	.4984	<b>.4541</b>
Weather	96	.1617	<b>.1616</b>	.1634	<b>.1631</b>	.1793	<b>.1790</b>	.1803
	192	.2088	<b>.2056</b>	<b>.2108</b>	.2109	.2217	<b>.2181</b>	.2237
	336	<b>.2515</b>	.2524	<b>.2488</b>	.2554	<b>.2626</b>	.2665	<b>.2642</b>
	720	<b>.2730</b>	.2798	<b>.2713</b>	.2798	<b>.2708</b>	.2729	<b>.2708</b>

(b) Overhead analysis.

Method	# Params ↓	Adaptation time/batch (ms) ↓	Inference time/batch (ms) ↓	Average MSE ↓
Recent	<b>1,211,287</b>	<b>80.12 ± 13.58</b>	<b>1.25 ± .0984</b>	<b>.3240</b>
Selective	1,212,217	83.64 ± 15.71	1.26 ± .1039	.3287

These findings confirm that the statistics-based context remains the most robust and stable choice for non-stationary adaptation, while encoder-based context generation still demonstrates potential. We discuss these observations in greater detail in Section H.

## G.2 INPUT CALIBRATION EFFECTS

COSA performs residual correction directly in the output space, and we demonstrated that output-only correction is often sufficient. However, in certain time series, we observe that input-level spikes or local noise degrade the base model’s predictions first, and this degradation subsequently propagates to the residual correction stage. To examine how such input perturbations influence the overall correction process, we conducted experiments combining COSA with the input-side GCM module from TAFAS. Table 14 reports the results.

In most cases, output-only correction achieves higher predictive accuracy. However, for datasets such as ETTh1, ETTh2, and ETTm2, where significant input noise is present, the combination with GCM produces improved results. In these cases, input GCM smooths the noisy input patterns, allowing the base model to generate more stable predictions, which in turn enhances the effectiveness of COSA.

Nevertheless, because GCM operates via distribution-shift normalization, it risks oversmoothing or removing meaningful drift signals when the input exhibits rapid or irregular changes. This behavior explains why, on average (in terms of MSE), output-only correction remains more stable across diverse non-stationary scenarios. Overall, when input disturbances are not the primary source of prediction error, output-only correction is the most robust and reliable option.

Table 13: Prediction accuracy and overhead comparison with encoder-based context.

1134	1135	1136	1137	(a) Prediction accuracy.																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																			
				Transformer-based					Linear-based					MLP-based																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																									
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				CALR	Cosine	Exp	Fixed	Plateau	Step	CALR	Cosine	Exp	Fixed	Plateau	Step	CALR	Cosine	Exp	Fixed	Plateau	Step																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																		
1139	1140	1141	1142	1143	1144	1145	1146	1147	1148	1149	1150	1151	1152	1153	1154	1155	1156	1157	1158	1159	1160	1161	1162	1163	1164	1165	1166	1167	1168	1169	1170	1171	1172	1173	1174	1175	1176	1177	1178	1179	1180	1181	1182	1183	1184	1185	1186	1187	1188	1189	1190	1191	1192	1193	1194	1195	1196	1197	1198	1199	1200	1201	1202	1203	1204	1205	1206	1207	1208	1209	1210	1211	1212	1213	1214	1215	1216	1217	1218	1219	1220	1221	1222	1223	1224	1225	1226	1227	1228	1229	1230	1231	1232	1233	1234	1235	1236	1237	1238	1239	1240	1241	1242	1243	1244	1245	1246	1247	1248	1249	1250	1251	1252	1253	1254	1255	1256	1257	1258	1259	1260	1261	1262	1263	1264	1265	1266	1267	1268	1269	1270	1271	1272	1273	1274	1275	1276	1277	1278	1279	1280	1281	1282	1283	1284	1285	1286	1287	1288	1289	1290	1291	1292	1293	1294	1295	1296	1297	1298	1299	1300	1301	1302	1303	1304	1305	1306	1307	1308	1309	1310	1311	1312	1313	1314	1315	1316	1317	1318	1319	1320	1321	1322	1323	1324	1325	1326	1327	1328	1329	1330	1331	1332	1333	1334	1335	1336	1337	1338	1339	1340	1341	1342	1343	1344	1345	1346	1347	1348	1349	1350	1351	1352	1353	1354	1355	1356	1357	1358	1359	1360	1361	1362	1363	1364	1365	1366	1367	1368	1369	1370	1371	1372	1373	1374	1375	1376	1377	1378	1379	1380	1381	1382	1383	1384	1385	1386	1387	1388	1389	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1390	1391	1392	1393	1394

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Table 15: Prediction accuracy comparison of single linear adapter and 2-layer MLP adapter.

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	Transformer-based		Linear-based		MLP-based			Transformer-based		Linear-based		MLP-based												
	iTransformer	PatchTST	DLinear	OLS	FrTS	MICN		iTransformer	PatchTST	DLinear	OLS	FrTS	MICN											
	Linear	MLP	Linear	MLP	Linear	MLP	Linear	MLP	Linear	MLP	Linear	MLP	MLP											
ETTh1	96.4363	4376	4238	4267	4482	.4644	.4372	.4460	.4371	.4412	.4684	.4841	2.35	3.79	2.35	3.83	2.24	3.45	2.15	3.10	2.14	3.49	2.38	3.84
	192.4919	.4968	.4805	.4857	.5050	.5135	.4906	.4980	.4940	.4967	.5282	.5496	2.39	3.73	2.44	3.83	2.23	3.49	2.21	3.42	2.16	3.47	2.59	3.83
	336.5300	.5471	.5320	.5294	.5456	.5501	.5320	.5282	.5351	.5346	.5878	.6067	2.40	3.68	2.43	3.77	2.22	3.52	2.18	3.45	2.32	3.40	2.51	3.91
	720.5638	.6167	.5822	.6350	.5896	.6498	.5733	.6351	.5959	.6558	.6504	.7325	2.39	3.46	2.25	3.49	2.23	3.22	2.24	3.11	2.36	4.57		
ETTh2	96.2493	.2517	.2343	.2339	.2281	.2299	.2265	.2350	.2350	.2485	.2517	.2517	2.38	3.76	2.36	3.63	2.19	3.49	2.19	3.43	1.54	3.47	2.37	3.81
	192.2947	.2981	.2608	.2825	.2819	.2828	.2791	.2781	.2824	.2767	.3017	.3094	2.40	3.74	2.44	3.80	2.28	3.51	2.20	3.41	2.24	3.43	2.66	3.85
	336.3339	.3306	.2978	.3127	.3083	.3106	.3043	.3113	.3153	.3168	.3310	.3484	2.48	3.71	2.45	3.77	2.25	3.49	2.17	3.38	2.30	3.47	2.87	3.95
	720.3591	.3931	.3428	.3837	.3477	.3689	.3453	.3750	.3399	.3660	.3885	.4170	2.34	3.40	2.35	3.48	2.21	3.33	2.18	3.24	2.19	3.19	3.72	4.62
ETTm1	96.3455	.3522	.3626	.3680	.3475	.3505	.3475	.3489	.3525	.3577	.3831	.3914	8.49	14.08	8.56	14.24	8.14	11.50	8.17	13.16	8.22	13.22	8.33	14.38
	192.4140	.4103	.4248	.4246	.4122	.4147	.4119	.4137	.4212	.4168	.4514	.4470	8.72	14.41	8.67	14.31	8.35	13.25	5.68	13.38	8.57	13.68	9.27	14.39
	336.4643	.4625	.4697	.4709	.4858	.4678	.4749	.4680	.4775	.4708	.5054	.4784	9.07	14.62	9.03	12.04	8.72	13.59	8.86	13.31	8.87	14.17	10.86	15.26
	720.5102	.4927	.4882	.4651	.4991	.4763	.5007	.4774	.4982	.4814	.5225	.4888	9.64	15.32	8.72	12.74	9.32	14.00	9.36	14.31	9.60	14.62	16.05	20.23
ETTm2	96.1632	.1632	.1562	.1569	.1586	.1582	.1587	.1569	.1571	.1704	.1703	.8.51	11.73	8.72	14.41	8.34	13.23	8.06	13.04	8.45	9.13	8.25	14.35	
	192.2173	.2140	.2022	.1978	.1905	.1880	.1907	.1884	.1908	.1850	.2120	.2039	8.75	14.35	8.77	14.38	8.32	13.31	5.27	13.28	8.51	13.65	9.32	14.42
	336.2535	.2412	.2352	.2283	.2242	.2103	.2226	.2142	.2211	.2092	.2351	.2331	8.10	14.64	9.10	14.56	8.84	13.50	8.89	13.57	8.86	13.64	10.80	15.24
	720.2606	.2759	.2645	.2711	.2316	.2532	.2349	.2551	.2314	.2477	.2643	.2709	7.74	15.14	9.51	15.04	9.29	13.86	9.32	14.26	9.50	14.48	16.04	20.21
Exchange	96.0837	.0869	.0788	.0838	.0834	.0890	.0773	.0789	.0766	.0803	.1008	.1106	1.38	2.01	1.38	1.99	1.22	1.79	1.20	1.77	1.26	1.81	1.39	2.00
	192.1479	.1730	.1570	.1696	.1519	.1761	.1457	.1570	.1499	.1603	.1722	.1956	1.31	1.89	1.36	1.88	1.17	1.68	1.15	1.69	1.17	1.70	1.42	1.96
	336.2624	.3103	.2445	.2941	.2480	.2872	.2323	.2856	.2461	.2910	.2660	.3399	1.26	1.70	1.32	1.81	1.09	1.57	1.10	1.58	1.10	1.62	1.48	1.60
	720.4460	.4099	.4662	.2828	.4481	.8373	.4541	.7980	.4458	.7983	.4815	.9665	1.09	1.47	1.09	1.43	.91	1.24	.90	1.26	.93	1.27	1.46	1.76
Average	.3218	.3438	.3166	.3383	.3196	.3425	.3158	.3368	.3176	.3369	.3421	.3696	6.16	9.60	6.60	10.21	6.04	9.28	5.79	9.28	6.09	9.35	7.36	10.75

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whether more complex architectures necessarily guarantee better performance. Table 15 provides a comprehensive performance and efficiency comparison between linear and MLP adapters.

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The comparative analysis reveals that single linear adapters achieve performance comparable to or superior to 2-layer MLP adapters while requiring significantly reduced computational resources. Although MLP adapters occasionally demonstrated slight performance improvements, the  $1.5 \sim 2 \times$  computational overhead renders them impractical for real-time adaptation scenarios. These results validate the architectural design principle of COSA that emphasizes simplicity without compromising effectiveness.

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#### G.4 COMPARISON WITH VARIOUS LEARNING-RATE SCHEDULERS

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To validate the effectiveness of CALR, we compared it against several official PyTorch learning-rate schedulers: CosineAnnealingLR, ExponentialLR, ReduceLROnPlateau, StepLR, and a fixed learning rate. All schedulers were configured with the same base learning rate of 0.005 for a fair comparison. One-Cycle, although widely used, was excluded because it requires a predefined learning-rate schedule; in a streaming TTA scenario where samples arrive continuously and the batch size changes dynamically under PAAS, such predefinition is not feasible.

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As summarized in Table 16, each scheduler achieves improvements in some individual cases. However, when results are averaged across all datasets and prediction lengths, the proposed CALR achieves the best or second-best accuracy in the vast majority of settings. These findings support CALR’s stability-induced design and its suitability for non-stationary TTA environments.

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**G.5 EXTENTION TO MULTIVARIATE TIME-SERIES FORECASTING**

COSA is originally introduced as an output-space residual correction module, treating each variable as an independent univariate forecasting task, for fair comparison with existing SOTA methods that assume univariate forecasting. However, in real multivariate time-series settings, correlations among variables may influence drift patterns, suggesting that modeling cross-variable interactions could potentially benefit COSA. Basically, can be extended to multivariate forecasting; to examine this possibility, we implemented it.

We first incorporate *Cross-Variable Context Attention*, allowing the context of each variable to reference information from other variables and thereby capture correlation-driven contextual interactions. Additionally, we introduce a mixed structure composed of a low-rank shared component and variable-specific components: the shared component captures drift patterns common across variables

Table 16: Prediction accuracy comparison with various learning rate schedulers.

	Transformer-based				Linear-based				MLP-based										
	iTransformer		DLinear		FreTS														
	CALR	Cosine	Exp	Fixed	Plateau	Step	CALR	Cosine	Exp	Fixed	Plateau	Step							
ETTh1	96	<b>.4363</b>	.4858	.4961	<b>.4848</b>	.4848	<b>.4885</b>	<b>.4482</b>	.4498	.4556	.4513	.4513	<b>.4537</b>	<b>.4371</b>	.4400	.4441	.4398	.4398	.4405
	192	<b>.4919</b>	.5405	.5613	.5413	.5413	.5426	<b>.5050</b>	.5069	.5183	.5090	.5090	.5110	.4940	<b>.4914</b>	.5002	<b>.4915</b>	.4915	.4931
	336	<b>.5300</b>	.5741	.5952	.5751	.5751	.5826	<b>.5456</b>	.5560	.5714	.5586	.5586	.5642	<b>.5351</b>	.5429	.5570	.5442	.5442	.5494
	720	<b>.5638</b>	.6216	.6835	.6163	.6163	.6336	<b>.5896</b>	.6033	.6511	.5953	.5953	.6166	<b>.5959</b>	.6116	.6593	<b>.6041</b>	.6041	.6200
ETTh2	96	<b>.2493</b>	.2984	.3021	<b>.2984</b>	.2984	.2987	<b>.2281</b>	.2308	<b>.2287</b>	.2321	.2321	.2333	<b>.2350</b>	.2378	<b>.2359</b>	.2376	.2376	.2372
	192	<b>.2947</b>	.3386	.3520	.3399	.3400	.3394	<b>.2819</b>	.2823	<b>.2811</b>	.2836	.2836	.2845	<b>.2824</b>	.2837	<b>.2827</b>	.2834	.2834	.2831
	336	<b>.3339</b>	.3823	.3992	.3856	.3856	.3802	<b>.3083</b>	<b>.3078</b>	.3093	.3104	.3105	.3081	.3153	<b>.3115</b>	.3151	.3131	.3131	<b>.3087</b>
	720	<b>.3591</b>	.4094	.4278	.4113	.4113	<b>.4070</b>	.3477	.3490	.3562	<b>.3462</b>	<b>.3463</b>	.3488	.3399	.3421	.3524	.3391	.3389	<b>.3387</b>
ETTm1	96	<b>.3455</b>	.4006	.4087	<b>.3978</b>	.3978	.4048	<b>.3475</b>	.3501	.3610	<b>.3497</b>	.3497	.3569	<b>.3525</b>	.3548	.3567	<b>.3539</b>	.3539	.3555
	192	<b>.4140</b>	.4650	.4772	<b>.4630</b>	.4630	.4683	<b>.4122</b>	.4140	.4283	.4146	.4146	.4191	<b>.4212</b>	.4236	.4279	.4231	.4230	.4246
	336	<b>.4643</b>	.5110	.5286	<b>.5100</b>	.5100	.5160	.4858	<b>.4828</b>	.5028	.4838	.4838	.4875	.4775	<b>.4740</b>	.4821	<b>.4740</b>	.4740	.4750
	720	<b>.5102</b>	.5321	.5732	.5350	.5349	.5392	.4991	<b>.4861</b>	.5153	<b>.4889</b>	.4889	.4915	.4982	<b>.4923</b>	.5073	.4950	.4950	.4951
ETTm2	96	<b>.1632</b>	.2138	.2140	.2139	.2139	<b>.2136</b>	<b>.1586</b>	.1621	<b>.1591</b>	.1629	.1629	.1646	<b>.1569</b>	.1611	<b>.1572</b>	.1604	.1604	.1606
	192	<b>.2173</b>	.2697	.2705	.2692	.2693	.2704	<b>.1905</b>	.1948	.1916	.1955	.1956	.1973	<b>.1908</b>	.1958	.1921	.1951	.1951	.1955
	336	<b>.2535</b>	.3028	.3125	.3047	.3045	.3065	<b>.2242</b>	.2305	<b>.2268</b>	.2310	.2310	.2324	<b>.2211</b>	.2285	<b>.2247</b>	.2276	.2276	.2278
	720	<b>.2606</b>	.3000	.3159	.2987	.2986	<b>.2966</b>	<b>.2316</b>	.2369	.2383	.2405	.2405	<b>.2348</b>	<b>.2314</b>	.2388	.2397	.2405	.2403	<b>.2334</b>
Exchange Rate	96	<b>.0837</b>	.1335	.1344	.1335	.1335	.1334	<b>.0834</b>	.0865	.0848	.0873	.0873	.0886	<b>.0766</b>	.0800	<b>.0775</b>	.0794	.0794	.0792
	192	<b>.1479</b>	.1961	.2025	.1960	.1960	.1952	<b>.1519</b>	.1523	.1552	.1533	.1533	.1542	<b>.1499</b>	.1518	.1545	.1513	.1513	<b>.1505</b>
	336	<b>.2624</b>	.3120	.3495	.3116	.3117	<b>.3102</b>	<b>.2480</b>	.2521	.2710	.2528	.2527	.2535	<b>.2461</b>	.2501	.2735	.2491	.2492	<b>.2484</b>
	720	<b>.4460</b>	.4481	.6222	.4498	<b>.4460</b>	<b>.4448</b>	.4481	.4185	.5919	<b>.4164</b>	<b>.4162</b>	.4179	.4458	.4128	.5679	.4072	<b>.4063</b>	.4068
Weather	96	<b>.1617</b>	.2118	.2151	.2115	.2115	.2123	<b>.1793</b>	.1824	.1827	.1827	.1827	.1858	<b>.1737</b>	.1770	.1767	<b>.1761</b>	.1761	.1776
	192	<b>.2088</b>	.2514	.2592	.2517	.2517	.2517	<b>.2217</b>	.2226	.2270	.2232	.2232	.2259	<b>.2189</b>	.2201	.2235	<b>.2191</b>	.2192	.2204
	336	<b>.2515</b>	.2916	.3063	.2949	.2948	.2920	.2626	<b>.2510</b>	.2622	<b>.2532</b>	.2532	.2541	.2587	.2497	.2606	.2505	.2505	<b>.2496</b>
	720	<b>.2730</b>	.3230	.3460	.3225	.3225	.3267	<b>.2708</b>	.2774	.2965	.2802	.2802	.2810	<b>.2692</b>	.2726	.2921	.2755	.2755	.2725
PatchTST																			
PatchTST				OLS				MICN											
	CALR	Cosine	Exp	Fixed	Plateau	Step	CALR	Cosine	Exp	Fixed	Plateau	Step							
ETTh1	96	<b>.4238</b>	.4723	.4294	.5723	.4923	<b>.4232</b>	<b>.4372</b>	.4375	.4448	.4401	.4401	.4413	<b>.4684</b>	.4739	.4904	<b>.4708</b>	.4708	.4769
	192	<b>.4805</b>	.5307	.4958	.6301	.5501	<b>.4838</b>	<b>.4906</b>	.4912	.5041	.4944	.4944	.4951	.5328	.5320	.5709	<b>.5297</b>	.5298	.5390
	336	<b>.5320</b>	.5851	.5535	.6826	.6026	<b>.5396</b>	<b>.5320</b>	.5344	.5515	.5384	.5384	.5424	.5878	.5864	.6417	<b>.5861</b>	.5861	.5974
	720	<b>.5822</b>	.6412	.6553	.7330	.6533	<b>.6031</b>	<b>.5733</b>	.5872	.6371	<b>.5808</b>	.5808	.5987	<b>.6504</b>	.6726	.8268	<b>.6506</b>	.6506	.6977
ETTh2	96	<b>.2343</b>	.2840	.2352	.3839	.3039	<b>.2345</b>	<b>.2265</b>	.2275	<b>.2268</b>	.2301	.2300	.2296	<b>.2485</b>	.2499	.2499	.2521	<b>.2466</b>	
	192	<b>.2608</b>	.3114	.2641	.4092	.3292	<b>.2617</b>	<b>.2791</b>	.2804	.2804	.2828	.2828	.2823	.3017	<b>.2990</b>	.3077	.3025	.3026	<b>.2960</b>
	336	<b>.2978</b>	.3514	.3086	.4543	.3743	<b>.2993</b>	.3043	.3030	.3064	.3063	.3063	<b>.3029</b>	.3310	.3303	.3399	.3388	.3388	<b>.3243</b>
	720	<b>.3428</b>	.3913	.3663	.4951	.4151	<b>.3485</b>	<b>.3453</b>	.3487	.3589	.3473	.3472	.3476	<b>.3885</b>	.3965	.4019	.3929	.3929	<b>.3884</b>
ETTm1	96	<b>.3626</b>	.4104	.3741	.5183	.4383	<b>.3655</b>	<b>.3475</b>	.3487	.3608	.3495	.3495	.3552	<b>.3831</b>	.3912	.3982	<b>.3900</b>	.3900	.3913
	192	<b>.4258</b>	.4747	.4427	.5764	.4964	<b>.4315</b>	<b>.4119</b>	.4125	.4283	.4142	.4142	.4174	<b>.4514</b>	.4533	.4641	<b>.4524</b>	.4524	.4541
	336	<b>.4697</b>	.5149	.4825	.6203	.5403	<b>.4700</b>	<b>.4749</b>	.4706	.4920	.4728	.4728	.4751	.5054	<b>.5053</b>	.5249	<b>.5048</b>	.5048	.5079
	720	<b>.4882</b>	.5349	.5077	.6391	.5550	<b>.4877</b>	<b>.5007</b>	.4831	.5136	<b>.4873</b>	.4873	.4882	.5225	<b>.5152</b>	.5443	.5188	.5188	<b>.5185</b>
ETTm2	96	<b>.1562</b>	.2065	<b>.1566</b>	.3064	.2265	<b>.1566</b>	<b>.1586</b>	.1608	<b>.1590</b>	.1627	.1627	.1630	<b>.1704</b>	.1742	<b>.1709</b>	.1762	.1763	<b>.1709</b>
	192	<b>.2022</b>	.2527	.2056	.3532	.2732	<b>.2034</b>	<b>.1907</b>	.1933	<b>.1914</b>	.1954	.1953	.1956	<b>.2120</b>	.2154	.2138	.2180	.2180	<b>.2122</b>
	336	<b>.2352</b>	.2863	.2367	.3863	.3063	<b>.2363</b>	<b>.2226</b>	.2278	<b>.2256</b>	.2298	.2298	.2298	<b>.2351</b>	.2383	.2365	.2408	.2408	<b>.2354</b>
	720	<b>.2645</b>	.3145	.2692	.4114	.3314	<b>.2619</b>	<b>.2349</b>	.2390	.2417	.2445	.2445	.2367	.2643	<b>.2628</b>	.2672	.2647	.2647	<b>.2565</b>
Exchange Rate	96	.0788	.1278	.0802	.2278	.1478	<b>.0776</b>	<b>.0773</b>	.0789	.0780	.0809	.0809	.0808	<b>.1008</b>	.1031	.1027	.1051	.1051	<b>.0994</b>
	192	<b>.1570</b>	.2051	.1642	.3052	.2251	<b>.1544</b>	<b>.1457</b>	.1452	.1490	.1474	.1473	.1466	.1722	<b>.1715</b>	.1779	.1735	.1735	<b>.1670</b>
	336	<b>.2445</b>	.2966	.2780	.3962	.3164	<b>.2448</b>	<b>.2323</b>	.2331	.2578	.2349	.2348	.2334	<b>.2660</b>	.2730	.3114	.2745	.2745	.2675
	720	<b>.4662</b>	.4743	.5963	.5724	.4923	<b>.4218</b>	.4541	.4224	.5806	.4190	.4190	<b>.4189</b>	.4815	.4515	.6597	.4488	.4511	<b>.4460</b>
Weather	96	<b>.1634</b>	.2124	.1651	.3124	.2324	<b>.1629</b>	<b>.1803</b>	.1822	.1840	.1838	.1838	.1855	<b>.1651</b>	.1678	.1669	.1695	.1695	<b>.1644</b>
	192	<b>.2108</b>	.2564	.2122	.3569	.2769	<b>.2065</b>	<b>.2237</b>	.2232	.2290	.2250	.2250	.2263	.2120	<b>.2096</b>	.2105	.2109	.2109	<b>.2050</b>
	336	<b>.2488</b>	.2924	.2540	.3950	.3150	<b>.2419</b>	<b>.2642</b>	.2618	.2743	.2651	.2651	.2647	.2737	.2545	.2599	.2556	.2556	<b>.2499</b>
	720	<b>.2713</b>	.3230	.2913	.4275	.3475	<b>.2737</b>	<b>.2708</b>	.2783	.2987	.2824	.2824	.2817	<b>.2855</b>	.2864	.3035	.2959	.2959	.2906

in an efficient low-dimensional form, while the specific components model idiosyncratic behavior unique to each variable. These two components are combined through a learnable mixing coefficient that automatically balances global and variable-specific contributions.

Table 17a presents the comparison results. For datasets where meaningful cross-variable dependencies exist, the multivariate structure achieves higher predictive accuracy than the univariate version of COSA. However, for datasets with weak inter-variable correlations, such as the Exchange Rate, the univariate structure remains more stable. In such cases, the shared component struggles to learn useful common patterns, which can lead to performance degradation. Moreover, as shown in Table 17b, the additional complexity leads to increased adaptation time and inference latency.

1296 These results indicate that multivariate-based correlation modeling can indeed provide accuracy  
 1297 gains, but further design improvements are required for effective deployment under TTA constraints.  
 1298 We discuss these limitations and potential future directions in Section H.  
 1299

1300 Table 17: Prediction accuracy and overhead of multivariate consideration.  
 13011302 (a) Prediction accuracy.  
 1303

	Transformer-based				Linear-based				MLP-based				
	iTransformer		PatchTST		DLinear		OLS		FreTS		MICN		
	Indiv.	Corr.	Indiv.	Corr.	Indiv.	Corr.	Indiv.	Corr.	Indiv.	Corr.	Indiv.	Corr.	
ETTh1	96	.4363	<b>.4351</b>	.4238	<b>.4157</b>	.4482	<b>.4202</b>	<b>.4372</b>	.4388	<b>.4371</b>	.4408	.4684	<b>.4533</b>
	192	.4919	<b>.4762</b>	.4805	<b>.4589</b>	.5050	<b>.4646</b>	.4906	<b>.4806</b>	.4940	<b>.4769</b>	.5328	<b>.5039</b>
	336	.5300	<b>.4759</b>	.5320	<b>.4798</b>	.5456	<b>.4823</b>	.5320	<b>.4884</b>	.5351	<b>.4987</b>	.5878	<b>.5105</b>
	720	.5638	<b>.4371</b>	.5822	<b>.5244</b>	.5896	<b>.4695</b>	.5733	<b>.4660</b>	.5959	<b>.4954</b>	.6504	<b>.5314</b>
ETTh2	96	.2493	<b>.2453</b>	.2343	<b>.1836</b>	<b>.2281</b>	.2342	.2265	<b>.2249</b>	.2350	<b>.2311</b>	.2485	<b>.2411</b>
	192	.2947	<b>.2871</b>	.2608	<b>.2172</b>	.2819	<b>.2578</b>	.2791	<b>.2770</b>	.2824	<b>.2922</b>	.3017	<b>.2923</b>
	336	<b>.3339</b>	.3341	.2978	<b>.2361</b>	.3083	<b>.2866</b>	.3043	<b>.2911</b>	.3153	<b>.2971</b>	.3310	<b>.3122</b>
	720	.3591	<b>.3306</b>	.3428	<b>.2638</b>	.3477	<b>.3094</b>	.3453	<b>.3083</b>	.3399	<b>.2979</b>	.3885	<b>.3441</b>
ETTm1	96	.3455	<b>.3186</b>	.3626	<b>.3595</b>	.3475	<b>.3335</b>	.3475	<b>.3330</b>	.3525	<b>.3381</b>	.3831	<b>.3385</b>
	192	.4140	<b>.3988</b>	.4258	<b>.4159</b>	.4122	<b>.4058</b>	.4119	<b>.4125</b>	.4212	<b>.4153</b>	.4514	<b>.4188</b>
	336	.4643	<b>.4491</b>	.4697	.4739	.4858	<b>.4561</b>	.4749	<b>.4648</b>	.4775	<b>.4618</b>	.5054	<b>.4628</b>
	720	.5102	<b>.4372</b>	.4882	.4892	.4991	<b>.4406</b>	.5007	<b>.4323</b>	.4982	<b>.4533</b>	.5225	<b>.4496</b>
ETTm2	96	<b>.1632</b>	.1633	.1562	<b>.1195</b>	.1586	<b>.1557</b>	.1586	<b>.1574</b>	.1569	<b>.1560</b>	.1704	<b>.1697</b>
	192	.2173	<b>.2141</b>	.2022	<b>.1526</b>	<b>.1905</b>	.2005	.1907	<b>.1935</b>	.1908	<b>.1921</b>	.2120	<b>.2097</b>
	336	.2535	<b>.2347</b>	.2352	<b>.1783</b>	.2242	<b>.2235</b>	.2226	<b>.2145</b>	.2211	<b>.2149</b>	.2351	<b>.2429</b>
	720	.2606	<b>.2110</b>	.2645	<b>.2162</b>	.2316	<b>.2295</b>	.2349	<b>.2006</b>	.2314	<b>.2022</b>	.2643	<b>.2265</b>
Exchange Rate	96	<b>.0837</b>	.0840	<b>.0788</b>	.0851	.0834	<b>.0791</b>	<b>.0773</b>	.0773	.0766	<b>.0765</b>	.1008	<b>.0995</b>
	192	<b>.1479</b>	.1493	<b>.1570</b>	.1828	<b>.1519</b>	.1609	<b>.1457</b>	<b>.1457</b>	<b>.1499</b>	.1516	<b>.1722</b>	.1726
	336	<b>.2624</b>	.2838	<b>.2445</b>	.3162	<b>.2480</b>	.2599	<b>.2323</b>	.2456	<b>.2461</b>	.2627	<b>.2660</b>	.2955
	720	<b>.4460</b>	.5221	<b>.4662</b>	.7731	<b>.4481</b>	.5280	<b>.4541</b>	.5184	<b>.4458</b>	.5079	<b>.4815</b>	.5711
Weather	96	.1617	<b>.1547</b>	<b>.1634</b>	.1656	.1793	<b>.1566</b>	.1803	<b>.1731</b>	.1737	<b>.1673</b>	.1651	<b>.1591</b>
	192	.2088	<b>.1938</b>	.2108	<b>.2073</b>	.2217	<b>.2003</b>	.2237	<b>.2158</b>	.2189	<b>.2095</b>	.2120	<b>.1979</b>
	336	.2515	<b>.2300</b>	<b>.2488</b>	.2539	.2626	<b>.2321</b>	.2642	<b>.2461</b>	.2587	<b>.2331</b>	.2737	<b>.2565</b>
	720	.2730	<b>.2236</b>	<b>.2713</b>	.2868	.2708	<b>.2254</b>	.2708	<b>.2172</b>	.2692	<b>.2165</b>	.2855	<b>.2420</b>

(b) Overhead analysis.

Method	# Params ↓	Adaptation time/batch (ms) ↓	Inference time/batch (ms) ↓	Average MSE ↓
Univariate	<b>1,211,287</b>	<b>80.12 ± 13.58</b>	<b>1.25 ± .0984</b>	.3240
Multivariate	1,214,851	186.28 ± 15.36	6.35 ± .2452	<b>.3071</b>

1333 G.6 EXTENSION TO VECTOR GATING  
 1334

1335 To evaluate whether finer-grained control over correction strength could provide additional benefits,  
 1336 we implemented an element-wise gating vector as an extension of the scalar gating mechanism in  
 1337 COSA. This vector shares the same dimensionality as the prediction length, allowing each time step  
 1338 within the prediction window to modulate its correction intensity independently. Such a design is  
 1339 intended to handle scenarios where drift occurs in only a specific portion of the horizon.

1340 However, as shown in Table 18a, vector gating yields degraded overall accuracy compared to the  
 1341 original scalar gating, and also exhibits reduced stability. We attribute this performance degradation  
 1342 to the propagation of local noise: a noise spike at a particular horizon position can influence the  
 1343 entire gating vector over successive adaptation steps, causing cumulative negative impact throughout  
 1344 the correction process. In contrast, scalar gating provides consistent batch-level modulation that  
 1345 effectively bounds the influence of noise and maintains stable behavior across adaptation windows.  
 1346

1347 G.7 VISUALIZATION OF NORMALIZATION  
 1348

1349 Figure 7 visualizes the learned weights of the linear layer in COSA with and without representative  
 time-series normalization modules (RevIN (Kim et al., 2021) and DDN (Dai et al., 2024)).

Table 18: Prediction accuracy and overhead of vector gating.

(a) Performance comparison.						
		iTransformer	DLinear	FrTS		
		Scalar	Vector	Scalar	Vector	Scalar
ETTh1	96	.4363	<b>.4336</b>	.4574	<b>.4436</b>	.4371
	192	.4919	<b>.4875</b>	.5066	<b>.4985</b>	.4940
	336	<b>.5300</b>	.5430	.5528	<b>.5466</b>	.5467
	720	<b>.5638</b>	.6013	<b>.6107</b>	.6178	.6259
ETTh2	96	.2493	<b>.1990</b>	.2281	<b>.1798</b>	.2350
	192	.2947	<b>.2318</b>	.2819	<b>.2198</b>	.2972
	336	.3339	<b>.2604</b>	.3083	<b>.2472</b>	.3153
	720	.3591	<b>.3035</b>	.3477	<b>.2893</b>	.3399
ETTm1	96	<b>.3455</b>	.3611	.3456	<b>.3425</b>	<b>.3525</b>
	192	.4140	<b>.4119</b>	.4222	<b>.4068</b>	.4212
	336	<b>.4643</b>	.4720	.4858	<b>.4706</b>	.4775
	720	<b>.5102</b>	.5484	<b>.4991</b>	.5370	<b>.4982</b>
ETTm2	96	.1632	<b>.1245</b>	.1583	<b>.1215</b>	.1569
	192	.2173	<b>.1683</b>	.1943	<b>.1487</b>	.1934
	336	.2535	<b>.2010</b>	.2242	<b>.1798</b>	.2211
	720	.2606	<b>.2488</b>	<b>.2316</b>	.2319	.2314
Exchange Rate	96	<b>.0837</b>	.0875	<b>.0834</b>	.0903	<b>.0766</b>
	192	<b>.1479</b>	.1774	<b>.1519</b>	.1790	<b>.1499</b>
	336	<b>.2624</b>	.3258	<b>.2480</b>	.3134	<b>.2461</b>
	720	<b>.4460</b>	.7649	<b>.4481</b>	.7904	<b>.4458</b>
Weather	96	<b>.1617</b>	.1718	<b>.1793</b>	.1908	<b>.1737</b>
	192	<b>.2088</b>	.2176	<b>.2217</b>	.2326	<b>.2189</b>
	336	<b>.2515</b>	.2706	<b>.2626</b>	.2808	<b>.2587</b>
	720	<b>.2730</b>	.3359	<b>.2708</b>	.3418	<b>.2692</b>

(b) Overhead analysis.

Method	# Params ↓	Adaptation time/batch (ms) ↓	Inference time/batch (ms) ↓	Average MSE ↓
Scalar	<b>1,211,287</b>	<b>80.12 ± 13.58</b>	<b>1.25 ± .0984</b>	<b>.3240</b>
Vector	1,212,446	96.34 ± 12.48	1.89 ± .0745	.3287

RevIN performs standard normalization on each input time series and then applies a corresponding denormalization step on the output. This procedure mitigates train–test distribution mismatch while restoring the information removed during normalization at the prediction stage, preventing degradation in forecasting performance.

DDN, in contrast, operates jointly in the time and frequency domains. It decomposes the input into low-frequency and high-frequency components and computes local statistics from each domain to remove non-stationarity. DDN then reconstructs non-stationary patterns in the predicted outputs using distribution statistics estimated from the model’s predictions, enabling dynamic tracking of distribution drift.

Each heatmap entry  $(i, j)$  shows the weight connecting the  $j$ -th input to the  $i$ -th output; columns  $1:L$  correspond to the original prediction of base model  $\mathbf{Y}^{(0)}$  and columns  $L+1:L+K$  to the context vector  $\mathbf{C}$ . The example is taken from a single variable of ETTh1 with look-back  $W=96$  and horizon  $L=96$ . Notably, the rightmost block (context columns) is strongly attenuated when RevIN or DDN is applied, whereas without a normalizer, the same block exhibits structured, non-negligible weights. This pattern indicates that explicit normalization reduces the marginal utility of the context (level/scale cues are already standardized), while in the non-normalized COSA leverages  $\mathbf{C}$  to perform level-shift correction directly in the output space—supporting our claim that the adapter can subsume normalization effects when needed and remain compatible with them when present.

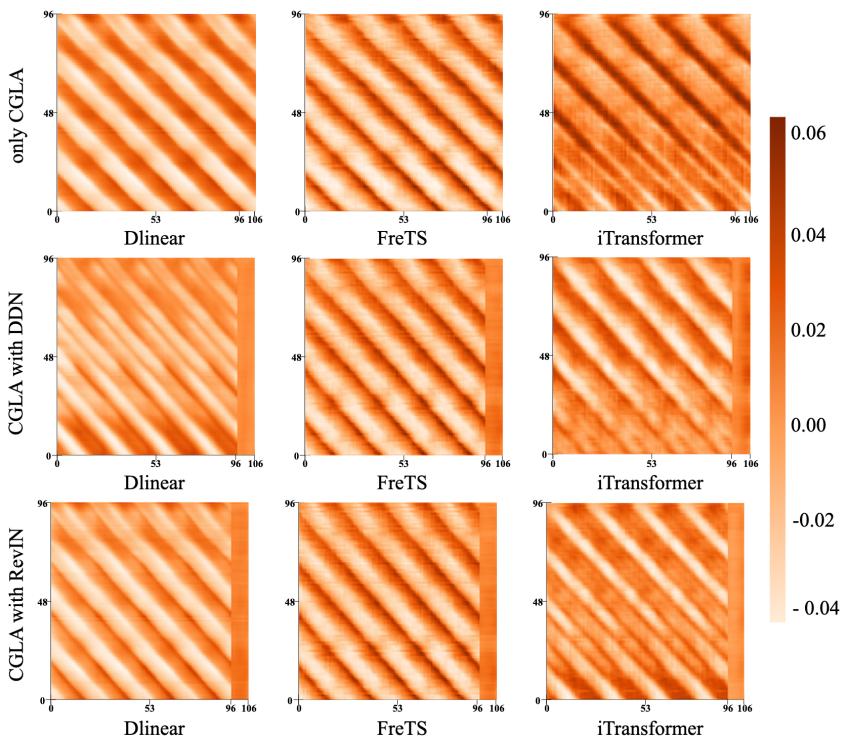


Figure 7: Weight heatmaps of the COSA linear layer for one ETTh1 variable ( $W=96$ ,  $L=96$ ). Columns  $1:L$  are base-prediction inputs  $\mathbf{Y}^{(0)}$ ; columns  $L+1:L+K$  are context inputs  $\mathbf{C}$ . Each cell shows the weight from input  $j$  to output  $i$ . Color scales are kept identical across panels to allow magnitude comparison.

## H DISCUSSION

Although COSA is built around a simple output-space linear adapter, the extended experiments in the Appendix examined multiple alternative design choices. While low-rank adaptation, input-side calibration, vector gating, selective/encoder-based context, and multivariate extensions each provide potential benefits in specific scenarios, our overall findings show that, considering average accuracy, stability, and latency, the architecture adopted in this paper remains the most consistent and robust choice for TSF-TTA.

The key observations are summarized below:

- **Low-rank factorization.** Despite its parameter-efficiency appeal, reducing representational capacity can lead to unstable adaptation. A joint adapter that integrates low-rank structure without compromising stability is a meaningful direction for future work.
- **Input-side calibration (GCM).** Combining COSA with input GCM improves performance on datasets with strong input noise (e.g., ETTh1/h2/m2) by smoothing perturbations before prediction. However, for fast-drifting or irregular series, GCM may oversmooth important variations and degrade performance, reaffirming that output-only correction is a reasonable and stable default.
- **Gating and its variants.** Although vector gating was expected to modulate drift at a finer temporal resolution, local noise propagated across the gating vector and reduced stability compared to scalar gating. Scalar gating’s batch-level modulation limits the influence of noise and achieves more reliable behavior.
- **Context construction.** Selective context (phase-aligned retrieval) and encoder-based context (RNN/LSTM/Attention) showed improvements in certain periodic datasets, but both suffered from outdated information, overfitting, or latency overhead in non-stationary set-

1458       tings. These results highlight that additional complexity does not guarantee better TTA per-  
 1459       formance unless paired with drift-aware representations and online update strategies. Fu-  
 1460       ture directions include sub-sequence vector gating, structure-aware context that explicitly  
 1461       encodes trend and seasonality, and lightweight encoders capable of tracking drift without  
 1462       incurring high overhead.

1463       • **Multivariate residual correction.** While multivariate modeling with cross-variable at-  
 1464       tention and shared components improved performance in most datasets, it degraded both accu-  
 1465       racy and efficiency in datasets with weak inter-variable correlations (e.g., Exchange Rate).  
 1466       This suggests the need for selective correlation modeling or structural sparsity to suppress  
 1467       unnecessary cross-variable interactions.

1468       Taken together, the extended Appendix experiments reinforce that the proposed simple architecture  
 1469       is particularly well-suited for TSF-TTA. They also indicate substantial room for generalizing COSA  
 1470       through carefully integrated low-rank structures, input calibration modules, selective or encoder-  
 1471       based context modeling, and vector gating, while preserving the efficiency and stability crucial for  
 1472       non-stationary test-time adaptation.

## 1474       I CONFIDENCE INTERVAL OF MAIN RESULTS

1475       Table 19 reports the 95% confidence intervals of the main accuracy comparison results over 10  
 1476       independent runs for each method–dataset–horizon combination. Overall, the intervals are narrow,  
 1477       indicating that the run-to-run variability of all methods is small, and COSA-F/P consistently retain  
 1478       their advantage over baselines even when accounting for this uncertainty.

## 1481       THE USE OF LARGE LANGUAGE MODELS

1482       **Tool & Version:** Claude Sonnet 4 (Anthropic, 2025-09)

1483       **Research Stage:** Not used.

1484       **Writing Stage:** Language editing of author-drafted text for clarity and conciseness.

1485       **Human Oversight:** All outputs reviewed/edited by the authors; authors accept full responsibility  
 1486       for the content.

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Table 19: 95% confidence interval of main accuracy comparison results

Transformer	Transformer-based												MLP-based											
	PatchTST						Linear-based						FreTS						MICN					
	TAFAS	PETSA	COSA-F	COSA-P	TAFAS	PETSA	COSA-F	COSA-P	TAFAS	PETSA	COSA-F	COSA-P	TAFAS	PETSA	COSA-F	COSA-P	TAFAS	PETSA	COSA-F	COSA-P	TAFAS	PETSA	COSA-F	COSA-P
ETTm1	96	4409	4390	4366	4361	4243	4247	4226	4616	4592	4571	4405	4385	4367	4377	4345	4890	4886	4683	4682	4683	4682	4682	4682
ETTm1	96	-4413	-4396	-4370	-4365	-4281	-4254	-4258	-4620	-4596	-4577	-4413	-4397	-4377	-4391	-4357	-4910	-4910	-4703	-4704	-4704	-4704	-4704	-4704
ETTm1	192	-4916	-4937	-4948	-4948	-4830	-4825	-4805	-5088	-5079	-5052	-4920	-4901	-4892	-4892	-4892	-5615	-5619	-5570	-5570	-5570	-5570	-5570	-5570
ETTm1	192	-4940	-4961	-4974	-4974	-4900	-4883	-4855	-5157	-5103	-5100	-4948	-4953	-4950	-4979	-4974	-5619	-5621	-5374	-5374	-5374	-5374	-5374	-5374
ETTm1	336	5380	5386	5348	5348	5441	5399	5288	5601	5508	5511	5420	5444	5367	5505	5448	6332	6332	5890	5890	5890	5890	5890	5890
ETTm1	336	-5678	-5694	-5698	-5698	-5612	-5605	-5609	-5612	-5603	-5603	-5621	-5621	-5621	-5621	-5621	-6128	-6128	-6010	-6010	-6010	-6010	-6010	-6010
ETTm1	720	-6581	-6622	-6643	-6643	-5936	-5612	-6805	-6712	-6654	-6602	-6928	-6832	-6884	-6884	-6884	-6919	-6919	-6823	-6823	-6823	-6823	-6823	-6823
ETTm2	96	-2552	-2554	-2502	-2490	-2345	-2358	-2345	-2347	-2366	-2353	-2308	-2317	-2287	-2282	-2247	-2356	-2356	-2354	-2354	-2354	-2354	-2354	-2354
ETTm2	192	-2997	-2990	-2970	-2934	-2734	-2747	-2747	-2634	-2629	-2625	-2864	-2807	-2827	-2775	-2769	-2956	-2956	-2949	-2949	-2949	-2949	-2949	-2949
ETTm2	336	-3384	-3388	-3267	-3370	-3159	-3166	-3002	-2940	-2940	-2940	-2888	-2888	-2888	-2888	-2888	-3167	-3167	-3167	-3167	-3167	-3167	-3167	-3167
ETTm2	720	-4051	-4062	-3514	-3514	-3567	-3567	-3562	-3562	-3562	-3562	-3562	-3562	-3562	-3562	-3562	-3562	-3562	-3562	-3562	-3562	-3562	-3562	-3562
ETTm1	96	3556	3568	3445	3445	3883	3927	3616	3616	3496	3523	3455	3455	3505	3535	3453	3581	3581	3519	3519	3519	3519	3519	3519
ETTm1	192	-4139	-4136	-4118	-4118	-4134	-4135	-3572	-3572	-3572	-3572	-3572	-3572	-3572	-3572	-3572	-3572	-3572	-3572	-3572	-3572	-3572	-3572	-3572
ETTm1	336	-4153	-4148	-4148	-4148	-4146	-4146	-4146	-4146	-4146	-4146	-4146	-4146	-4146	-4146	-4146	-4147	-4147	-4147	-4147	-4147	-4147	-4147	-4147
ETTm1	720	-5664	-5680	-4062	-4062	-3515	-3515	-3515	-3515	-3515	-3515	-3515	-3515	-3515	-3515	-3515	-3515	-3515	-3515	-3515	-3515	-3515	-3515	-3515
ETTm2	96	-1630	-1633	-1623	-1623	-1577	-1579	-1557	-1557	-1559	-1559	-1588	-1588	-1577	-1577	-1580	-1580	-1587	-1587	-1587	-1587	-1587	-1587	-1587
ETTm2	192	-2177	-2167	-2165	-2165	-2036	-2027	-1998	-1998	-1998	-1998	-1998	-1998	-1998	-1998	-1998	-1995	-1995	-1995	-1995	-1995	-1995	-1995	-1995
ETTm2	336	-2616	-2576	-2447	-2447	-2248	-2248	-2046	-2046	-2046	-2046	-1917	-1917	-1907	-1907	-1907	-1917	-1917	-1917	-1917	-1917	-1917	-1917	-1917
ETTm2	720	-3165	-3165	-2455	-2455	-2455	-2455	-2455	-2455	-2455	-2455	-2455	-2455	-2455	-2455	-2455	-2455	-2455	-2455	-2455	-2455	-2455	-2455	-2455
ETTm1	96	-0873	-0883	-0883	-0883	-0855	-0855	-0855	-0855	-0855	-0855	-0848	-0848	-0848	-0848	-0848	-0847	-0847	-0847	-0847	-0847	-0847	-0847	-0847
ETTm1	192	-1645	-1706	-1363	-1363	-1440	-1711	-1742	-1394	-1443	-1518	-1899	-1922	-1534	-1534	-1534	-1408	-1408	-1408	-1408	-1408	-1408	-1408	-1408
ETTm1	336	-2995	-3029	-2098	-2098	-2546	-3186	-3225	-1886	-1886	-1886	-2647	-2647	-2647	-2647	-2647	-1783	-1783	-1783	-1783	-1783	-1783	-1783	-1783
ETTm1	720	-8077	-7758	-3085	-3085	-4155	-8348	-8348	-8348	-8348	-8348	-8427	-8427	-8427	-8427	-8427	-1721	-1721	-1721	-1721	-1721	-1721	-1721	-1721
ETTm2	96	-0879	-0887	-0887	-0887	-0851	-0851	-0851	-0851	-0851	-0851	-0848	-0848	-0848	-0848	-0848	-0837	-0837	-0837	-0837	-0837	-0837	-0837	-0837
ETTm2	192	-1727	-1774	-1443	-1443	-2179	-2179	-2179	-1645	-1645	-1645	-1487	-1487	-1487	-1487	-1487	-1620	-1620	-1620	-1620	-1620	-1620	-1620	-1620
ETTm2	336	-3163	-3165	-2170	-2170	-2702	-3364	-3375	-2080	-2080	-2080	-2647	-2647	-2647	-2647	-2647	-2194	-2194	-2194	-2194	-2194	-2194	-2194	-2194
ETTm2	720	-3325	-3352	-2501	-2501	-2627	-3261	-3261	-2433	-2433	-2433	-3085	-3085	-3085	-3085	-3085	-2732	-2732	-2732	-2732	-2732	-2732	-2732	-2732
ETTm1	96	-1663	-1673	-1596	-1596	-1616	-1721	-1721	-1631	-1631	-1631	-1729	-1729	-1729	-1729	-1729	-1803	-1803	-1803	-1803	-1803	-1803	-1803	-1803
ETTm1	192	-1665	-1675	-1598	-1598	-1618	-1727	-1727	-1627	-1627	-1627	-1825	-1825	-1825	-1825	-1825	-1800	-1800	-1800	-1800	-1800	-1800	-1800	-1800
ETTm1	336	-2644	-2644	-2149	-2149	-2089	-2089	-2089	-2149	-2149	-2149	-2154	-2154	-2154	-2154	-2154	-2104	-2104	-2104	-2104	-2104	-2104	-2104	-2104
ETTm1	720	-3404	-3405	-2415	-2415	-2673	-3307	-3307	-2496	-2496	-2496	-3477	-3477	-3477	-3477	-3477	-2626	-2626	-2626	-2626	-2626	-2626	-2626	-2626
ETTm2	96	-0879	-0883	-0883	-0883	-0851	-0851	-0851	-0851	-0851	-0851	-0848	-0848	-0848	-0848	-0848	-0837	-0837	-0837	-0837	-0837	-0837	-0837	-0837
ETTm2	192	-1645	-1706	-1363	-1363	-1440	-1711	-1742	-1394	-1443	-1518	-1899	-1922	-1534	-1534	-1534	-1487	-1487	-1487	-1487	-1487	-1487	-1487	-1487
ETTm2	336	-2644	-2644	-2149	-2149	-2089	-2089	-2089	-2149	-2149	-2149	-2154	-2154	-2154	-2154	-2154	-2104	-2104	-2104	-2104	-2104	-2104	-2104	-2104
ETTm2	720	-3404	-3405	-2415	-2415	-2673	-3307	-3307	-2496	-2496	-2496	-3477	-3477	-3477	-3477	-3477	-2626	-2626	-2626	-2626	-2626	-2626	-2626	-2626