Pruning via Merging: Compressing LLMs via Manifold Alignment Based Layer Merging

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Abstract

 While large language models (LLMs) excel in many domains, their complexity and scale challenge deployment in resource-limited en- vironments. Current compression techniques, such as parameter pruning, often fail to effec-006 tively utilize the knowledge from pruned pa- rameters. To address these challenges, we pro- pose Manifold-Based Knowledge Alignment and Layer Merging Compression (MKA), a novel approach that uses manifold learning and the Normalized Pairwise Information Bottle- neck (NPIB) measure to merge similar layers, reducing model size while preserving essen- tial performance. We evaluate MKA on mul- tiple benchmark datasets and various LLMs. Our findings show that MKA not only pre- serves model performance but also achieves substantial compression ratios, outperform- ing traditional pruning methods. Moreover, when coupled with quantization, MKA delivers even greater compression. Specifically, on the MMLU dataset using the Llama3-8B model, MKA achieves a compression ratio of 43.75% with a minimal performance decrease of only 2.82%. The proposed MKA method offers a resource-efficient and performance-preserving model compression technique for LLMs.

028 1 Introduction

 Large Language Models (LLMs), such as GPT-**[4](#page-10-0) [\(OpenAI et al.,](#page-9-0) [2024\)](#page-9-0), Llama-3^{[1](#page-0-0)}, Llama-2 [\(Tou-](#page-10-0)** [vron et al.,](#page-10-0) [2023\)](#page-10-0) and Mistral [\(Jiang et al.,](#page-9-1) [2024\)](#page-9-1), have demonstrated remarkable proficiency in lan- guage understanding and generation. These mod- els, with billions of parameters trained on trillions of tokens, can handle complex tasks and exhibit **[e](#page-8-1)mergent abilities [\(Brown et al.,](#page-8-0) [2020;](#page-8-0) [Chowdhery](#page-8-1)** [et al.,](#page-8-1) [2023\)](#page-8-1). While these models have achieved un- precedented success, their growing complexity and scale have brought to the fore significant challenges

1 <https://github.com/meta-llama/llama3>

in terms of computational resources, memory re- **040** quirements, and energy consumption [\(Bender et al.,](#page-8-2) **041** [2021;](#page-8-2) [Bommasani et al.,](#page-8-3) [2021\)](#page-8-3), raising concerns **042** about their sustainability. **043**

To mitigate these challenges, researchers have **044** developed various model compression techniques **045** in LLM to reduce its parameter size while pre- **046** [s](#page-8-5)erving performance [\(Cheng et al.,](#page-8-4) [2017;](#page-8-4) [Deng](#page-8-5) 047 [et al.,](#page-8-5) [2020;](#page-8-5) [Ganesh et al.,](#page-8-6) [2021;](#page-8-6) [Zhu et al.,](#page-10-1) [2023\)](#page-10-1). **048** These techniques can be roughly categorized into **049** two main mainstreams [\(Men et al.,](#page-9-2) [2024\)](#page-9-2): quan- **050** tization [\(Gholami et al.,](#page-8-7) [2021;](#page-8-7) [Li et al.,](#page-9-3) [2024;](#page-9-3) **051** [Dettmers et al.,](#page-8-8) [2022;](#page-8-8) [Gong et al.,](#page-8-9) [2024;](#page-8-9) [Li et al.,](#page-9-3) **052** [2024\)](#page-9-3) and pruning [\(LeCun et al.,](#page-9-4) [1989;](#page-9-4) [Han et al.,](#page-9-5) **053** [2016;](#page-9-5) [Gupta and Agrawal,](#page-9-6) [2022;](#page-9-6) [Ma et al.,](#page-9-7) [2023a\)](#page-9-7). **054** Quantization based methods aid in the reduction of **055** the memory consumption of weights, activations, **056** and KV caches by using the low-precision values **057** with fewer bits instead of the high-precision values. 058 However, the acceleration benefits of quantization **059** [a](#page-10-2)re seriously dependent on hardware support [\(Tao](#page-10-2) **060** [et al.,](#page-10-2) [2023\)](#page-10-2) and sometimes require additional fine- **061** tuning to maintain performance [\(Dettmers et al.,](#page-8-10) **062** [2023;](#page-8-10) [Men et al.,](#page-9-2) [2024\)](#page-9-2). Compared to quantization, **063** pruning, especially structural pruning [\(Li et al.,](#page-9-8) **064** [2017\)](#page-9-8), eliminates redundant LLM's parameters to **065** decrease the overall parameter count, and can be **066** applied directly to a trained LLM without retrain- **067** ing and is generally more hardware-friendly than **068** quantization approaches. While effective, pruning **069** usually risks losing valuable model structures and **070** determining how to prune the LLM with minimal **071** disruption to the origin remains an unsolved prob- **072** lem [\(Ma et al.,](#page-9-9) [2023b\)](#page-9-9). **073**

To tackle this issue head-on, we delve into the **074** realm of model merging [\(Wortsman et al.,](#page-10-3) [2022\)](#page-10-3), **075** a powerful technique that seamlessly weaves to- **076** gether the strengths and knowledge of multiple **077** models, creating a robust and efficient aggregation. **078** This technique, through averaging the weights of **079** multiple models with the same architecture, can **080**

Figure 1: Manifold-Based Knowledge Alignment and Layer Merging (MKA) framework consists of two main components: (1) The left side illustrates manifold learning for LLM knowledge extraction, where layer activations are transformed into low-dimensional manifolds using the Diffusion Kernel algorithm. (2) The right side depicts the similarity-based layer merging process, employing the NPIB metric to identify layers with aligned knowledge.

 retain essential features without significant addi- tional resources [\(Liu et al.,](#page-9-10) [2024;](#page-9-10) [Wan et al.,](#page-10-4) [2024\)](#page-10-4). Furthermore, by offsetting the biases and errors of individual models, model merging often leads to greatly improved performance [\(Li et al.,](#page-9-11) [2023\)](#page-9-11). Additional, the number of models in the merging process can be gradually and naturally reduced. However, such a useful technology are limited to merging between models currently, and few studies pay attention on merging the same internal struc-tures within a model.

 This raises the question of whether model com- pression could be achieved by reducing the total number of layers through the progressive aggre- gation of knowledge between layers. To answer this question, we introduce Manifold-Based Knowl- edge Alignment and Layer Merging Compression (MKA) in this paper. MKA combines manifold learning and layer merging to preserve essential information while significantly reducing LLM pa- rameter size. As illustrated in Figure [1,](#page-1-0) our method mainly comprises two primary components:

 Manifold Learning for LLM Knowledge: We employ manifold learning techniques to align knowledge across layers by extracting layer ac- tivations from a LLM and applying the Diffusion Kernel algorithm [\(Tenenbaum et al.,](#page-10-5) [2000\)](#page-10-5) to learn low-dimensional manifold representations. This approach captures the nonlinear structure in the activation and achieves dimensionality reduction while preserving important activation features, enabling more effective comparison of knowledge **112** patterns across different layers. **113**

Similarity Alignment Layer Merging: Follow- **114** ing manifold learning, we use the Normalized **115** Pairwise Information Bottleneck (NPIB) measure **116** [\(Tishby et al.,](#page-10-6) [2000\)](#page-10-6) to construct a similarity ma- **117** trix that quantifies the similarity between layers by **118** maximizing their mutual information while con- **119** sidering the entropy of each layer. Based on this **120** similarity matrix, we select the most similar layer 121 pairs for merging. **122**

To rigorously validate the effectiveness of MKA, **123** we conduct extensive empirical evaluations on a di- **124** verse array of benchmark datasets, like MMLU and **125** PIQA, and a wide range of state-of-the-art large **126** language models, including Llama-3 series with **127** 8B and 70B parameters, Llama-2 series with 7B **128** and 13B parameters, and Mixtral-7B. Our exper- **129** imental results indicate that MKA can maintain **130** good performance while achieving a significant **131** compression ratio, outperforming existing pruning **132** methods and achieving even greater compression **133** when combined with quantization. For example, 134 on the MMLU dataset with Llama3-8B, MKA can **135** achieve a compression ratio of 43.75% with only a **136** 2.82% performance drop. **137**

In summary, the main contributions of this paper **138** are as follows: **139**

• We introduce MKA, an innovative model com- **140** pression technique that leverages manifold learn- **141** ing to align and integrate knowledge across lay- **142**

145 • We develop a manifold-based knowledge align-**146** ment approach, utilizing the Diffusion Kernel

147 and Normalized Pairwise Information Bottle-

- **148** neck (NPIB) to effectively capture and align sim-
- **149** ilarities between layers in the parameter space. **150** • We validate the efficacy of MKA through com-
- **151** prehensive experiments on multiple benchmark
- **152** datasets and a variety of large language models, **153** demonstrating its capability to achieve substan-
- **154** tial compression without compromising model **155** performance.
-
-

¹⁵⁶ 2 Manifold-Based Knowledge Alignment **¹⁵⁷** and Layer Merging

143 ers, achieving significant reductions in model

144 size while preserving performance.

 Our MKA method relies on the redundancy present [i](#page-9-12)n the latter layers of post-training LLMs [\(Gromov](#page-9-12) [et al.,](#page-9-12) [2024\)](#page-9-12). By merging layers with high input- output similarity from back to front, we maintain the model's performance while reducing its size. In this section, we first describe the extraction and dimensionality reduction processes for the inter- mediate states, as high-dimensional intermediate states are challenging to analyze. Then, we pro- pose our layer merging method based on similarity alignment, which aims to maintain performance by aligning intermediate states through merging techniques.

171 2.1 Manifold Learning for LLM Knowledge

 To effectively align knowledge across LLM's lay- ers, MKA employs manifold learning techniques that can capture the intricate nonlinear dependen- cies within the LLM's internal structure. This ap- proach allows us to compare and align layer acti- vations in a meaningful way, preserving essential information while reducing model complexity.

 The process begins with the extraction of layer **activations** H^l **from a LLM on the dataset D. These** activations represent the outputs of each layer given a set of input samples, encapsulating the knowledge learned at different stages. To transform these high- dimensional activations into a lower-dimensional space that preserves their essential features and geometric structure, we apply the Diffusion Kernel algorithm [\(Coifman and Lafon,](#page-8-11) [2006\)](#page-8-11). Here are the key steps involved in this process:

189 **Extracting Layer Activations:** For each layer 190 l , we extract the activations H^l given input sam-191 **ples.** These activations H^l are computed using the

following equation: **192**

$$
\mathbf{H}^{l} = \text{LayerNorm}\left(\mathbf{H}^{l-1} + \text{MultiHead}\left(\mathbf{H}^{l-1}\right)\right) \tag{93}
$$

$$
+ \text{ FeedForward}\left(\mathbf{H}^{l-1}\right) \tag{1}
$$

Constructing the Pairwise Distance Matrix: **195** Next, we calculate the pairwise Euclidean distance **196** matrix D for the activations H^l . This matrix cap-
197 tures the distances between all pairs of activations, **198** serving as the basis for the manifold learning pro- **199 cess.** 200

Applying the Diffusion Kernel: We apply the **201** Diffusion Kernel to transform the distance matrix **202** D into low-dimensional manifold representations **203** Φ_i , capturing the intrinsic geometric structure of 204 the data. The kernel function smooths the data, **205** emphasizing the intrinsic geometric structure: **206**

$$
\mathbf{E} = \text{EigVectors}_{d} \left(\text{Diag} \left(\sum_{j} e^{-\left(\frac{\|\mathbf{H}_{i} - \mathbf{H}_{j}\|^{2}}{\sigma K} \right)^{0.5}} \right) \right)
$$

$$
-e^{-\left(\frac{\|\mathbf{H}_i - \mathbf{H}_j\|^2}{\sigma K}\right)} \tag{2}
$$

where σ_K is the kernel bandwidth parameter, and 209 $EigVectors_d$ refers to the eigenvectors correspond- 210 ing to the d smallest eigenvalues of the Laplacian **211** matrix L. This transformation captures the essen- **212** tial features and relationships within the activations, **213** enabling effective comparisons across different lay- **214** ers. **215**

2.2 Similarity-based Layer Merging **216**

Building upon the manifold learning representa- **217** tions, MKA employs a similarity-based layer merg- **218** ing approach to identify and fuse layers with highly **219** aligned knowledge. By quantifying the similarity **220** between layers using the Normalized Pairwise In- **221** formation Bottleneck (NPIB) [\(Tishby et al.,](#page-10-6) [2000\)](#page-10-6) **222** metric, we can determine which layers are most **223** suitable for merging. This process allows us to **224** reduce model size, improve inference speed, and **225** decrease GPU memory consumption. **226**

The layer merging process involves several key **227** steps. First, we construct a similarity matrix using **228** the NPIB metric to compare the knowledge pat- **229** terns across layers. Next, we introduce an adaptive **230** weight allocation function to determine the optimal **231** merging ratio for each pair of layers, ensuring that **232** the merged layer retains the most critical features. **233**

Algorithm 1 Manifold-Based Knowledge Alignment and Layer Merging Compression (MKA) 1: **Input:** LLM M with Layers L_1, L_2, \ldots, L_N , Layer Parameters $\Theta = \theta_1, \theta_2, \ldots, \theta_N$, Dataset \mathcal{D} 2: Output: Compressed Model M[∗] with Aligned Knowledge 3: $\mathcal{H} \leftarrow$ ExtractActivations(\mathcal{M}, \mathcal{D}) \rightarrow Extract activations for each layer on dataset \mathcal{D} 4: $D \leftarrow$ ComputePairwiseDistances(H) \triangleright Compute pairwise Euclidean distance matrix of activations 5: $\mathbf{E} \leftarrow \text{DiffusionKernel}(D, \sigma_K)$ \triangleright Apply diffusion kernel for manifold learning 6: $S \leftarrow$ ComputeNPIB(E) \triangleright Compute NPIB similarity matrix 7: $\Omega \leftarrow$ SortLayersBySimilarity(S) \triangleright Sort layers by similarity for merging 8: while $|\Omega| > 1$ do 9: $(L_i, L_j) \leftarrow$ SelectTopLayerPair(Ω) ⊳ Select top-ranked layer pair based on similarity 10: $\lambda_m \leftarrow$ ComputeFusionRatio(S, L_i, L_j) \triangleright Compute adaptive merging ratio 11: $\theta_m \leftarrow \lambda_m \cdot \theta_i + (1 - \lambda_m) \cdot \theta_j$ \triangleright Fuse layer parameters 12: $L_m \leftarrow$ FuseLayer (L_i, L_i, θ_m) \triangleright Create fused layer using the fused parameters 13: $M \leftarrow \text{ReplaceLayer}(\mathcal{M}, L_i, L_j, L_m)$ \triangleright Update model with fused layer 14: $\Omega \leftarrow \text{UpdateLayerList}(\Omega, L_i, L_j, L_m)$ \triangleright Update layer list with the new fused layer 15: end while 16: return $\mathcal M$

234 Finally, we fuse the parameters of the selected lay-**235** ers using the weighted sum and update the model **236** architecture accordingly.

 Constructing the Similarity Matrix: To iden- tify layers suitable for merging, we first construct a similarity matrix S using the Normalized Pair- wise Information Bottleneck (NPIB) metric. NPIB quantifies the shared information between layers while normalizing their individual entropies, pro- viding an ideal measure for comparing knowledge patterns across layers:

$$
S_{ij} = \text{NPIB}(\mathbf{E}_i, \mathbf{E}_j)
$$

=
$$
\frac{\sum\limits_{x \in \mathbf{E}_i} \sum\limits_{y \in \mathbf{E}_j} p(x, y) \log \frac{p(x, y)}{p(x)p(y)}}{\sqrt{\sum\limits_{x \in \mathbf{E}_i} p(x) \log p(x) \cdot \sum\limits_{y \in \mathbf{E}_j} p(y) \log p(y)}}
$$

²⁴⁵ (3)

246 where $p(x, y)$ denotes the joint probability distri-247 bution of \mathbf{E}_i and \mathbf{E}_j , and $p(x)$ and $p(y)$ represent 248 the marginal probability distributions of \mathbf{E}_i and \mathbf{E}_j , **249** respectively. This similarity matrix helps us deter-**250** mine which layers have the most aligned knowl-**251** edge representations.

 Calculate Weight ratio: To determine the merg-253 ing ratio λ_m for each pair of layers, we introduce the adaptive weight allocation function Ψ. This function dynamically adjusts the merging ratio based on the similarity differences between lay- ers, ensuring that the merged layer retains the most critical features from each original layer:

$$
\lambda_m = \Psi(\bar{s}i, \bar{s}j) = \frac{e^{\mathcal{S}ij}}{\sum k \in \Omega e^{\mathcal{S}_k}} \tag{4}
$$

The adaptive weight allocation function Ψ adjusts **260** the merging weights based on the similarity dif- **261** ference between layers. When the similarity dif- **262** ference between two layers is large, Ψ assigns a **263** higher weight to the layer with higher similarity, 264 reducing the weight of the layer with lower sim- **265** ilarity. This mechanism ensures that the merged **266** layer better preserves the knowledge from the more **267** similar layer. **268**

Merging Layer Parameters: Once the merging **269** ratio λ_m is determined, we fuse the parameters θ_i 270 and θ_i of the selected layers using a weighted sum: **271**

$$
\widetilde{\theta}_m = \lambda_m \theta_i + (1 - \lambda_m) \theta_j \tag{5}
$$

The merged layer L_m is obtained through the func- 273 tion FuseLayer(L_i, L_j, θ_m), which constructs a **274** new layer based on the fused parameters $\hat{\theta}_m$. This 275
new layer integrates the aligned knowledge from 276 new layer integrates the aligned knowledge from **276** the original layers, preserving essential information **277** while reducing redundancy. 278

Finally, we update the model M by replac- 279 ing the original layers L_i and L_j with the 280 newly merged layer L_m , utilizing the function 281 ReplaceLayer(M, L_i, L_j, L_m). This step ensures 282 that the model's architecture is updated to reflect **283** the compression process, maintaining performance **284** while significantly reducing model size. 285

3 Experiments **²⁸⁶**

We conduct a comprehensive set of experiments to 287 evaluate the effectiveness and generalizability of **288** our MKA method across various domains. More- **289**

Figure 2: Comparison of Accuracy (ACC) during merging and pruning on the MMLU dataset. MKA achieves higher compression ratios (approximately 43.5% for Llama3-8B, 45% for Llama3-70B, 40% for Mistral-7B, 31.25% for Llama2-7B, and 57.5% for Llama2-13B) while preserving 90% performance. Please see the appendix [A](#page-11-0) for details.

 over, we aim to compare our approach with prun- ing techniques to assess whether it offers improve- ments and to investigate if it can be combined with quantization methods to achieve even higher com-pression ratios.

295 3.1 Experimental Setup

296 3.1.1 Datasets

 We conduct evaluations using the MKA methods across various benchmark datasets, each specif- ically designed to test various facets of lan- guage comprehension and generation. In detail, MMLU [\(Hendrycks et al.,](#page-9-13) [2020\)](#page-9-13) evaluates broad language understanding across a wide range of do- mains. PIQA [\(Bisk et al.,](#page-8-12) [2020\)](#page-8-12) is designed to test models on commonsense reasoning in the physical world, aiming to assess NLP models' grasp of ev- [e](#page-10-7)ryday physical interactions. HellaSwag [\(Zellers](#page-10-7) [et al.,](#page-10-7) [2019\)](#page-10-7) is a challenge dataset for commonsense natural language inference, consisting of event descriptions with multiple possible continuations, where the task is to select the most plausible one. RACE-H [\(Lai et al.,](#page-9-14) [2017\)](#page-9-14) is a large-scale reading comprehension dataset collected from English ex- ams for Chinese high school students, featuring a high proportion of questions that require reasoning. BoolQ [\(Clark et al.,](#page-8-13) [2019\)](#page-8-13) is a reading comprehen- sion dataset focusing on naturally occurring yes/no questions that often query for complex, non-factoid information and require difficult entailment-like inference to answer correctly.

320 3.1.2 LLMs

 [I](#page-10-0)n our experiments, we employ the Llama-2 [\(Tou-](#page-10-0) [vron et al.,](#page-10-0) [2023\)](#page-10-0), Llama-3, and Mistral-7B [\(Jiang](#page-9-15) [et al.,](#page-9-15) [2023\)](#page-9-15) models, each distinct in their capabili- ties and configurations: Llama-2: Encompassing models from 7 billion to 70 billion parameters, ex- hibits superior performance and safety on diverse benchmarks. Llama-3: Featuring models with 8 billion and 70 billion parameters, Llama3 offers **328** state-of-the-art performance and advanced reason- **329** ing capabilities. Mistral-7B: a 7-billion-parameter **330** model that surpasses Llama-2 and Llama-1 in per- **331** formance and efficiency, leveraging grouped-query **332** and sliding window attention mechanisms for opti- **333** mal inference across lengthy sequences. **334**

3.1.3 Baselines **335**

In this study, we assess the effectiveness of our **336** proposed method, MKA, through two distinct com- **337** parative analyses. Firstly, we evaluate MKA di- **338** rectly against several well-established pruning tech- **339** niques to gauge its standalone efficacy in reducing **340** model size while maintaining performance. Sec- **341** ondly, we extend the comparison to include sce- **342** narios where both the traditional pruning methods **343** and MKA are further enhanced through quantiza- **344** tion. The baseline methods included in our analy- **345** sis are: SparseGPT [\(Frantar and Alistarh,](#page-8-14) [2023\)](#page-8-14): **346** An efficient one-shot pruning method that can in-
 347 duce high sparsity levels in large language models **348** with billions of parameters while preserving ac- 349 curacy, by reducing the pruning problem to a set **350** of large-scale sparse regression instances solved **351** [b](#page-9-2)y a novel approximate solver. ShortGPT [\(Men](#page-9-2) **352** [et al.,](#page-9-2) [2024\)](#page-9-2): A pruning method that removes redun- **353** dant layers from large language models based on a **354** Block Influence metric, which assesses the signifi- **355** cance of each layer. Reverse Pruning: A heuristic **356** approach where the importance of layers is con- **357** sidered inversely proportional to their order in the **358** model, prioritizing the retention of earlier layers. **359** SmoothQuant [\(Xiao et al.,](#page-10-8) [2023\)](#page-10-8): SmoothQuant is **360** a training-free post-training quantization solution **361** that enables efficient 8-bit weight and activation **362** quantization for large language models, offering **363** up to 1.56× speedup and 2× memory reduction **364** with minimal accuracy loss. **GPTQ** [\(Frantar et al.,](#page-8-15) 365 [2022\)](#page-8-15): A one-shot weight quantization method **366** that uses approximate second-order information to maintain high accuracy even with severe weight reduction. AWQ [\(Lin et al.,](#page-9-16) [2023\)](#page-9-16): A novel quan- tization approach that protects salient weights by adjusting per-channel scaling based on activation observations rather than weight Magnitudes.

373 3.2 In what ways does MKA surpass **374** conventional pruning techniques?

 We compare the performance of MKA with base- line compression methods on the MMLU dataset using the Llama3-8B, Llama3-70B, Mistral-7B, Llama2-7B, and Llama2-13B models. The eval- uation metric is Accuracy (ACC) during merging and pruning. The results are presented in Figure [2.](#page-4-0)

 We compare the performance of MKA with base- line compression methods on the MMLU dataset using the Llama3-8B, Llama3-70B, Mistral-7B, Llama2-7B, and Llama2-13B models. The eval- uation metrics include Accuracy (ACC) during merging and pruning. The results are presented in Figure [2.](#page-4-0) We can observe that, across all models, our method improves the compression ratio while maintaining performance. Specifically, the com-**pression ratio^{[2](#page-5-0)}** for Llama3-8B reach 43.5%, for Mistral-7B it reaches 40%, and for Llama2-13B it reaches an impressive 57.5%. Additionally, we ob- serve several phenomena: both methods experience a collapse in model performance, but the model merging method can delay the layer collapse to some extent and stabilize the model's performance very well. Since our strategy is based on Reverse Prune, the scores for the Llama3-8B, Llama2-7B, and Llama2-13B models are very close to the Re- verse Prune. Our hypothesis is that the pruning or merging of these models is similar, but model merging can adjust the merging ratio to surpass the effect of pruning. Moreover, for the Llama3-70B and Mistral-7B models, we noticed that the results do not closely match the Reverse Prune.

406 3.3 How Does MKA Combined with **407** Quantization Perform Compared to **408** Pruning Combined with Quantization?

409 We compare the performance of MKA with the **410** baseline pruning method, ShortGPT [\(Men et al.,](#page-9-2) **411** [2024\)](#page-9-2), on the MMLU dataset using the Llama3-8B,

Model	Method	Retained layers (Compression Ratio)	Acc.			
	Vanilla Model	32 (0.00%)	66.29			
Llama3-8R	ShortGPT+Smooth	18(85.94%)	26.54			
	ShortGPT+GPTO	18(85.94%)	25.98			
	ShortGPT+AWQ	18(85.94%)	26.22			
	MKA (Ours) + Smooth	$18(85.94\%)$	$64.20 (+37.66)$			
	MKA (Ours) + GPTO	$18(85.94\%)$	$62.98 (+37.00)$			
	$MKA (Ours) + AWO$	18(85.94%)	$61.66 (+35.44)$			
	Vanilla Model	32(0.00%)	63.87			
Mistral-7B	ShortGPT+Smooth	20(84.38%)	24.32			
	ShortGPT+GPTO	20(84.38%)	23.16			
	ShortGPT+AWQ	20(84.38%)	23.96			
	MKA (Ours) + Smooth	20(84.38%)	$56.92 (+32.60)$			
	MKA (Ours) + GPTO	20(84.38%)	$56.12 (+32.96)$			
	$MKA (Ours) + AWO$	20(84.38%)	$55.34 (+31.38)$			
	Vanilla Model	32(0.00%)	46.67			
	ShortGPT+Smooth	16(87.50%)	25.67			
	ShortGPT+GPTO	16(87.50%)	25.82			
Llama _{2-7R}	ShortGPT+AWO	$16(87.50\%)$	26.01			
	MKA (Ours) + Smooth	$16(87.50\%)$	$35.66 (+9.99)$			
	MKA (Ours) + GPTO	16(87.50%)	$35.91 (+10.09)$			
	$MKA (Ours) + AWQ$	16(87.50%)	$36.23 (+10.22)$			
	Vanilla Model	40 (0.00%)	55.62			
$Llama2-13B$	ShortGPT+Smooth	20 (87.50%)	25.89			
	ShortGPT+GPTQ	20 (87.50%)	25.35			
	ShortGPT+AWO	20 (87.50%)	23.83			
	MKA (Ours) + Smooth	20 (87.50%)	$46.82 (+20.93)$			
	MKA (Ours) + GPTO	20 (87.50%)	$45.44 (+20.09)$			
	$MKA (Ours) + AWO$	20 (87.50%)	$45.86 (+22.03)$			

Table 1: Performance comparison of MKA and ShortGPT pruning with quantization (SmoothQuant, GPTQ, AWQ) on MMLU using Llama3-8B, Mistral-7B, Llama2-7B, and Llama2-13B. MKA outperforms ShortGPT in accuracy across all models and quantization methods at similar compression ratios with int4. The calculation of the compression ratio only considers the number of hidden layers in the model without considering the embedding layer.

Llama3-70B, Mistral-7B, Llama2-7B, and Llama2- **412** 13B models. The results are shown in Table [1.](#page-5-1) **413**

We can see that the pruned models are able to be 414 further quantized and maintain performance with **415** a higher compression ratio. Notably, at a high **416** compression ratio of around 50%, MKA signif- **417** icantly outperforms ShortGPT. Additionally, we **418** achieve excellent results with various quantization **419** methods. For example, on Llama3-8B, at a com- **420** pression ratio of 43.75%, MKA with SmoothQuant **421** achieves 64.20%, far exceeding ShortGPT with **422** SmoothQuant at 37.66%. Similarly, with the GPTQ **423** quantization method, we achieve 62.98%, sur- **424** passing ShortGPT's 37.00%, and with AWQ, we **425** achieve 61.66%, exceeding ShortGPT's 35.44%. **426**

3.4 MKA vs. Other Pruning Methods on **427** varies benchmarks **428**

We compared the performance of MKA and several **429** other pruning methods on the LLama3-8B model **430** using multiple benchmark datasets at compression **431** ratios of 21.875% and 45.75%. The results are **432** shown in Table [2.](#page-6-0) From the results, we can ob- **433**

²Note that, the compression ratio is calculated as: $\left(L_{\text{total}} - \left(\frac{L_{\text{retained}}}{Q}\right)\right)/L_{\text{total}}$, where L_{total} is the total number of layers before compression, $L_{retained}$ is the number of retained layers, and Q is the quantization factor.

			Compression Ratio = 34.375%			Compression Ratio = 37.5%								
Method	MMLU	PIOA	HellaSwag	RACE-H	BoolO	MMLU	PIOA	HellaSwag	RACE-H	BoolO				
Vanilla Model	66.29	81.12	74.54	66.07	66.79	66.29	81.12	74.54	66.07	66.79				
SparseGPT	44.45	58.77	32.14	35.06	48.29	41.95	56.23	28.63	37.84	52.40				
ShortGPT	42.95	60.99	33.00	41.68	51.96	44.80	61.70	38.69	40.05	57.09				
MKA (Ours)	64.87	67.79	51.32	55.20	63.36	62.05	66.26	50.16	49.49	63.46				

Table 2: Comparison of MKA and pruning methods across MMLU, PIQA, HellaSwag, RACE-H, and BoolQ datasets and on different compression ratios.

Figure 3: Similarity matrices for Llama-3-8B, Llama-3-70B, Mistral-7B, Llama-2-7B, and Llama-2-13B before and after MKA. Later layers show high similarity, supporting layer merging.

 serve that, similar to the previous section, the per- formance of Reverse Pruning and our method are quite similar. However, model fusion can retain per- formance better compared to pruning. Relative to SparseGPT and ShortGPT, our method can achieve better performance retention, with significant im- provements across all datasets. For example, at a compression ratio of 34.375% on the MMLU dataset, our method can outperform ShortGPT by 21.92% and SparseGPT by 20.42%. Similarly, on the HellaSwag dataset, our proposed method can surpass ShortGPT by 18.32% and SparseGPT by **446** 18.32%.

447 3.5 Are Inter-Layer Knowledge Alignment **448** Similarity Matrices Consistent Across **449** Different Large Models?

 We generate layer similarity heatmaps for dif- ferent models before and after applying MKA. These heatmaps visualize the knowledge align- ment and layer merging effects of MKA on var- ious models. Figure [3](#page-6-1) presents the similarity heatmaps for Llama-3-8B, Llama-3-70B, Mistral- 7B, Llama-2-7B, and Llama-2-13B. We observe that the heatmaps for the later layers of each model exhibit high similarity values, indicating that inter- layer similarity is consistently high in the later lay- ers across different models. This observation sup- ports our layer merging approach. Additionally, when merging the earlier layers, we notice a col-lapse of the matrix in the final figure, suggesting

that earlier layers have a significant influence on **464** later layers. Thus, simple merging operations on **465** the earlier layers of the model are not feasible. **466**

4 Discussion 467

4.1 Extension to Multimodal and Specialized **468** Models **469**

Figure 4: The similarity matrix of Mixtral-8x7B and Jamba model.

In addition to its application to large language **470** models, the MKA method shows promising poten- **471** tial for broader adoption across a variety of deep **472** learning architectures. This includes Mixture-of- **473** [E](#page-9-17)xperts (MoE) [\(Jiang et al.,](#page-9-1) [2024\)](#page-9-1), and Mamba [\(Gu](#page-9-17) **474** [and Dao,](#page-9-17) [2023;](#page-9-17) [Lieber et al.,](#page-9-18) [2024\)](#page-9-18) models, which **475** can exhibit similar redundancies in their process- **476** ing layers.The results show in Figure [4.](#page-6-2) Initial **477** experiments conducted on these diverse architec- **478** tures have reinforced the viability of our approach. **479** For instance, the similarity matrices generated on 480 [j](#page-9-1)amba [\(Lieber et al.,](#page-9-18) [2024\)](#page-9-18) and Mixtral-8x7B [\(Jiang](#page-9-1) **481**

[Figure 5: Similarity matrices for various measures in the Llama3-8B model, showing different patterns and](#page-9-1) [effectiveness in capturing layer relationships, with none fully matching the expected merging patterns.](#page-9-1)

 [et al.,](#page-9-1) [2024\)](#page-9-1) applying MKA have shown that Our method can also be generalized to other similar models, but the similarity distributions of jamba and Mixtral-8x7B are slightly different from LLM, and we do not yet know the reason. These exper- iments further validates the effectiveness of our method across different model types.

489 4.2 Analysis of Similarity Measures

 In our evaluation of the Llama3-8B model, we ex- plored several similarity measures: Cosine Simi- larity, Mahalanobis Distance, Euclidean Distance, t-SNE Similarity, and Autoencoder Similarity. The similarity matrices are shown in Figure [5.](#page-7-0) From the results, we observe that Cosine Similarity, Maha- lanobis Distance, and Euclidean Distance display similar distribution patterns with vertical stripes and varied heat values. However, Mahalanobis Distance shows irregular heat values within these stripes, indicating a misalignment with the fused layer data structure. t-SNE Similarity appears ran- dom and lacks consistent patterns. For Autoen- coder Similarity, the high heat values do not corre- spond to suitable merging areas or expected high-similarity regions.

506 4.3 Variations in Accuracy Across Different **507** MMLU Subjects During Layer Merging

Figure 6: Different MMLU dataset subjects ACC change during merging.

508 We examine the impact of model merging on **509** performance across various academic subjects in the MMLU benchmark. Figure [6](#page-7-1) shows the ac- **510** curacy changes across subjects such as College **511** Medicine, College Biology, High School Psychol- **512** ogy, and College Physics during different stages **513** of merging model layers. From our results, we ob- **514** serve that High School Psychology maintained a **515** stable accuracy with only minor fluctuations, sug-
516 gesting a consistent performance and low sensitiv- **517** ity to the merging process. In contrast, College **518** Biology experiences a significant drop in accuracy **519** at the 12.5% merging ratio, followed by a recov- **520** ery. College Physics exhibits frequent fluctuations **521** in accuracy, pointing to a high sensitivity to layer **522** merging. Conversely, College Medicine experi- **523** ences a steady increase in performance with only **524** minor variations. **525**

5 Conclusion **⁵²⁶**

In this paper, we have proposed Manifold-Based **527** Knowledge Alignment and Layer Merging Com- **528** pression (MKA), a novel model compression tech- **529** nique specifically designed to efficiently reduce the **530** size of large language models (LLMs) while main- **531** taining their performance. MKA leverage mani- **532** fold learning techniques to align knowledge across **533** layers and utilizes the Normalized Pairwise Infor- **534** mation Bottleneck (NPIB) measure to identify the **535** most similar layers for merging. By capturing the **536** intricate nonlinear dependencies within LLMs and **537** integrating knowledge from similar layers, MKA **538** achieves remarkable compression ratios without **539** sacrificing model accuracy. We have conducted **540** extensive experiments on a diverse set of bench- **541** mark datasets and various state-of-the-art LLMs to 542 rigorously evaluate the effectiveness of MKA in **543** preserving model performance while significantly **544** reducing model size. Our empirical results demon- **545** strate that MKA consistently outperforms existing **546** pruning methods and can achieve even higher com- **547** pression ratios when combined with quantization **548** techniques. **549**

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⁵⁵⁰ Limitations

 The quality of the manifold learning process in MKA heavily depends on the diversity and repre- sentativeness of the layer activations extracted from the input dataset. In our experiments, we used σ value of 8 and selected the first question from the 57-question MMLU dataset to extract activations. We observed that the number of questions sampled can significantly impact the manifold learning re- sults. Ensuring the Condition Number remains be- low 2000 is crucial for maintaining the integrity of the learned manifold representations. If the dataset used for extracting activations does not adequately cover the model's operational range, the learned manifold representations might fail to capture the true geometric structure of the data.

 The current implementation of MKA has been primarily tested on transformer-based architectures. Although we believe that deep neural networks in- herently contain redundancies, the applicability and effectiveness of MKA on other neural network ar- chitectures, such as convolutional neural networks (CNNs) or recurrent neural networks (RNNs), have not been thoroughly explored. Future research can investigate these architectures to confirm whether MKA can achieve similar compression benefits across different types of neural networks.

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Model	Methods	Ω								$0.03125 \quad 0.0625 \quad 0.09375 \quad 0.125 \quad 0.15625 \quad 0.1875 \quad 0.21875 \quad 0.25 \quad 0.28125 \quad 0.3125 \quad 0.34375 \quad 0.375 \quad 0.40625 \quad 0.4375 \quad 0.46875 \quad 0.51625 \quad 0$	
	Llama3_8b $\left \begin{array}{cccccccccc} \text{ACC (Reverse)} & 66.29 & 66.12 & 66.33 & 66.15 & 66.21 & 65.31 & 64.96 & 62.91 & 64.28 & 65.00 \\ \text{ACC (Ours)} & 66.29 & 65.96 & 66.26 & 66.15 & 58.08 & 62.94 & 64.96 & 62.92 & 64.28 & 65.01 \end{array}\right $									63.99 64.71 62.04 63.52 64.51 30.31 29.07 63.99 64.87 62.05 63.42 64.42 30.29 29.05	
	Llama2_7b ACC (Reverse) 46.67 44.37 46.71 46.09 46.89 46.51 46.79 43.33 45.90 45.22 35.33 Llama2_7b ACC (Ours) 46.67 44.45 46.74 46.07 46.93 46.52 46.84 43.41 45.85 45.09 35.25								40.67 42.40 37.38 39.41	40.58 42.33 37.34 39.26 39.53 35.65 39.45 35.71	

Table 3: ACC during the compression process of Ours and Reverse Prune on Llama3-8b and Llama2-7b models.

Methods		0.025 0.05 0.075 0.1 0.125 0.15 0.175 0.2 0.225 0.25 0.275 0.3 0.325 0.375 0.375 0.4 0.425 0.475 0.5									
ACC (Reverse) 55.62 55.24 55.21 55.12 54.44 54.02 55.63 55.27 53.87 53.66 53.17 51.89 51.56 51.56 51.48 50.75 50.28 48.37 45.18 48.59 46.78											
ACC (Ours)	55.62 55.24 55.21 55.12 54.44 54.02 55.63 55.27 53.87 53.66 53.17 51.89 51.56 51.56 51.49 50.75 50.28 48.37 45.18 48.59 46.78										

Table 4: ACC during the compression process of Ours and Reverse Prune on Llama2-13b model.

861 **A** More Results