

FSM: A Finite State Machine Based Zero-Shot Prompting Paradigm for Multi-Hop Question Answering

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Abstract

Large Language Models (LLMs) with chain-of-thought (COT) prompting have demonstrated impressive abilities on simple natural language inference tasks. However, they tend to perform poorly on Multi-hop Question Answering (MHQA) tasks due to several challenges, including hallucination, error propagation and limited context length. We propose a prompting method, Finite State Machine (FSM) to enhance the reasoning capabilities of LLM for complex tasks in addition to improved effectiveness and trustworthiness. Different from COT methods, FSM addresses MHQA by iteratively decomposing a question into multi-turn sub-questions, and self-correcting in time, improving the accuracy of answers in each step. Specifically, FSM addresses one sub-question at a time and decides on the next step based on its current result and state, in an automaton-like format. Experiments on benchmarks show the effectiveness of our method. Although our method performs on par with the baseline on relatively simpler datasets, it excels on challenging datasets like Musique. Moreover, this approach mitigates the hallucination phenomenon, wherein the correct final answer can be recovered despite errors in intermediate reasoning. Furthermore, our method improves LLMs' ability to follow specified output format requirements, significantly reducing the difficulty of answer interpretation and the need for reformatting.

1 Introduction

Multi-hop Question Answering has intrigued researchers for its complexity and practical implications. Researchers employ two primary strategies to address MHQA using Large Language Models. One effective method is In-Context Learning (ICL) (Wang et al., 2023; Zhou et al., 2022), where models are guided to solve problems based on detailed instructions, often through examples of problem decomposition. However, few-shot methods with

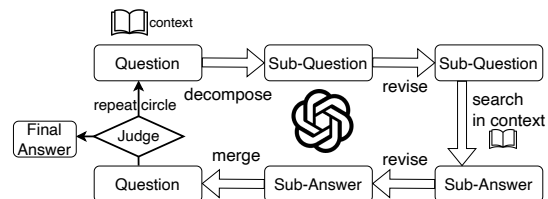


Figure 1: The abstract flow chart of FSM

manual demonstrations are expansive and time-consuming. Another approach involves fine-tuning LLMs with domain-specific data, a complex process (Cao et al., 2023) requiring substantial high-quality data and computational resources. This approach is unable to generalize to unseen datasets and domains without training. Despite advancements in single-hop question answering, MHQA remains challenging due to the need to extract information from lengthy texts and conduct multi-step reasoning without supervision, which poses difficulties for LLMs. LLMs struggle with reading long texts and multi-step reasoning tasks.

Why do LLMs underperform in current MHQA methods? By analyzing errors in existing approaches, we identified four common error types, which will be detailed in Section 4. Specific incorrect examples from common methods are illustrated in Figure 5. We found that LLMs struggle particularly in intermediate reasoning stages, where errors in initial steps can propagate, leading to incorrect conclusions. Additionally, few-shot techniques like REACT (Yao et al., 2022) and SP-COT (Wang et al., 2023) need a minimum of 4-shot displays with long context, surpassing context boundaries.

According to the analysis above, we propose a zero-shot method named Finite State Machine prompting (FSM), simplifying the MHQA task into four sub-tasks: decomposing questions, searching for answers in candidate paragraphs, revising the format, judging whether to continue or summa-

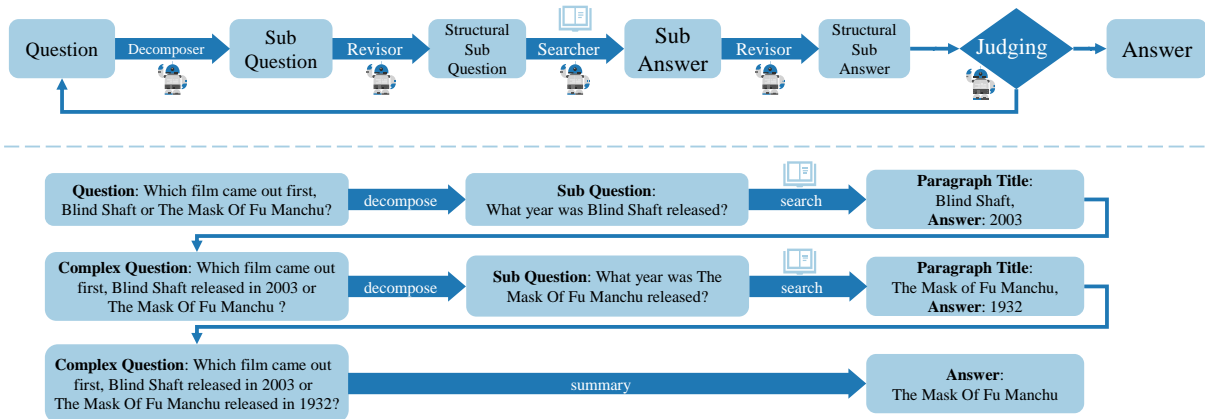


Figure 2: The flow chart of proposed FSM and a simple case in detail. The book icon indicates candidate paragraphs in the search step. The robot denotes LLMs.

075 rizing with all key information. Figure 2 depicts
 076 the process of the FSM. LLMs address one sub-
 077 question per round, deciding the next step based
 078 on the current state, following an automaton-like
 079 process. Clear and explicit sub-tasks, along with
 080 timely revisions, make the reasoning process more
 081 manageable and accurate.

082 Extensive experiments on MHQA benchmarks
 083 (Yang et al., 2018; Trivedi et al., 2022; Ho et al.,
 084 2020) demonstrate that our approach outperforms
 085 GPT and 72B LLM baselines, nearly doubling the
 086 F1 score on Musique (Trivedi et al., 2022). Fur-
 087 thermore, unlike our framework, baselines have a
 088 high frequency of producing outputs in unexpected
 089 formats and type errors that require additional pro-
 090 cessing to extract correct answers.

091 Our contributions are as follows:

092 • To address reasoning challenges in LLMs
 093 for MHQA tasks, we introduce FSM, a zero-shot
 094 prompting paradigm based on finite state machines
 095 to decompose complex questions iteratively. This
 096 approach aims to strengthen control over interme-
 097 diate reasoning and improve overall accuracy.

098 • We investigate the reason for errors in MHQA
 099 and conduct various experiments on the insights.
 100 e.g. hallucination exists in direct answer predic-
 101 tions, and the contextual length is a bottleneck for
 102 reasoning.

103 • Extensive experiments on MHQA benchmarks
 104 in different settings validate FSM’s effectiveness,
 105 especially on challenging datasets. The method can
 106 be adapted to other similar complex tasks.

2 Methodology 107

2.1 Strategies 108

109 The average score of the large model is reported
 110 as only 0.3, which is significantly lower than the
 111 current sota method (Zhang et al., 2023). Through
 112 manual observation of error examples 5, we de-
 113 deduce from the results of baseline methods that the
 114 model struggles with completing complex instruc-
 115 tions in a single step. LLMs tend to forget previous
 116 instructions during reasoning.

117 To address these issues, we propose the follow-
 118 ing strategies:

119 a) **Iterative Decomposition:** Unlike few-shot
 120 reasoning approaches, FSM adopts a multi-turn
 121 process. Each iteration focuses on addressing a
 122 single sub-task, enabling LLMs to understand in-
 123 structions clearly and execute them accurately.

124 b) **Error Checking and Backtracking:** For
 125 each reasoning step, FSM conducts a verification
 126 check to ensure the correctness of response. If an
 127 irregular or incorrect output is identified, the model
 128 is allowed to self-revise the answer or backtrack.

129 c) **Final Review Step:** To minimize distractions
 130 from lengthy contexts, we utilize sub-questions,
 131 corresponding supporting factual paragraphs, evi-
 132 dence, and answers to further verify the consistency
 133 of answers and reasoning, named FSM2.

2.2 Framework 134

135 We present our proposed Finite State Machine
 136 (FSM) in two distinct stages as illustrated in Fig-
 137 ure 2. Initially, we instruct LLMs to address sub-
 138 questions iteratively during the first phase. Subse-
 139 quently, in stage 2, LLMs are tasked with summa-
 140 rizing the responses incorporating key information

141 from each sub-question. The FSM framework is
142 depicted in Figure 2.

143 To elaborate, our approach commences by as-
144 sisting the model in breaking down the primary
145 question into smaller components. Following this,
146 we compare the original question with the sub-
147 questions to ensure semantic equivalence; any dis-
148 parities prompt the model to further decompose
149 the elements. In the third phase, the model scans
150 the context for related paragraphs, retrieving rel-
151 evant information and answers. The fourth step
152 entails revising the complex question with the re-
153 sponse to the sub-question and identifying the re-
154 lationship with updated complex question and sub-
155 question, composition or comparison. Addition-
156 ally, we conduct checks to ascertain whether the
157 answer constitutes a simple or compound sentence,
158 then promptly breaks down compound sentences.
159 This iterative process continues until the revised
160 question reaches a point where no further decom-
161 position is feasible. By meticulously following
162 each step, our methodology enables a more accu-
163 rate evaluation of a model’s true capabilities, dis-
164 tinguishing it from other approaches that tend to
165 overlook crucial intermediate stages, which may
166 yield seemingly correct outcomes despite flawed
167 reasoning processes. We have included prompts
168 for the whole process in the Appendix.

169 3 Experiments

170 3.1 Benchmark and Evaluation

171 We evaluate our model on three high-quality
172 MHQA datasets: HotpotQA (Yang et al., 2018),
173 2WikiMultiHopQA (Ho et al., 2020) and Musique
174 (Trivedi et al., 2022). Learning from the short-
175 cut phenomenon (Min et al., 2019) of single hop
176 questions in HotpotQA, Musique strictly controls
177 the composition of the question, ensuring that it
178 must undergo multiple inferences to find the an-
179 swer. Both HotpotQA and 2Wiki have ten candi-
180 date paragraphs for each question and originally
181 have supporting facts. While Musique has twenty
182 candidate with longer text and no supporting facts.
183 Therefore, Musique is the most standard and diffi-
184 cult MHQA datasets. Following traditions (Wang
185 et al., 2023), We adopt the exact match (EM) and
186 F1 scores as evaluation metrics and conduct experi-
187 ments on subsets of the datasets by randomly select-
188 ing 1000 samples from the test sets. Despite having
189 similar basic instructions and a clearly defined out-
190 put format for all methods, the model’s consistency

191 in following instructions may vary across different
192 methods. This variation can result difficulty for
193 answer extraction during evaluation. To address
194 this issue, we introduce a new metric, format, mea-
195 suring the accuracy of the output format.

196 3.2 Baselines

197 Baseline methods in the experiment:

- 198 • The **Normal** is the basic form, involving only
199 task descriptions and output requirements, without
200 explicit instructions for reasoning.

- 201 • The **COT** (Wei et al., 2022) is widely used
202 in LLMs for inference due to its simplicity and
203 effectiveness. It prompts LLMs to create intermedi-
204 ate step-by-step rationales, aiding in the reasoning
205 process for obtaining answers.

- 206 • The **SP-COT** (Wang et al., 2023) introduces a
207 pipeline for generating high-quality Open-Domain
208 Multi-step Reasoning (ODMR) datasets. It uti-
209 lizes an adaptive sampler for case selection and
210 self-prompted inference via ICL. This technique
211 organizes reasoning chains into six categories, in-
212 spired by the construction of the Musique (Trivedi
213 et al., 2022) dataset.

214 3.3 Setting

215 Our study explores two settings: (1) generating
216 answers directly from the context and question,
217 and (2) building a complete reasoning chain that
218 includes the answer, supporting evidence, and facts
219 to assess the coherence of the reasoning process.
220 Due to the lack of gold evidence for Setting 2 in
221 Musique, our evaluation can not evaluate on it.

222 3.4 Models

223 For MHQA task, we require models with the abil-
224 ity for processing lengthy text. FSM operates in
225 multiple rounds, demanding models capable of han-
226 dling conversational contexts. We selected GPT-
227 3.5-turbo-32k and Qwen72B-chat (Bai et al., 2023)
228 for our study. Additionally, we employed vllm
229 (Kwon et al., 2023) to accelerate the inference pro-
230 cess.

231 3.5 Results

232 The results of setting 1(sole answer) are detailed in
233 Table 2, while the outcomes for setting 2(answer
234 paired with supporting fact) are displayed in Table
235 1. Our approach demonstrates superior results in
236 setting 2, particularly on the most difficult dataset.
237 This is attributed to the increased complexity of in-
238 structions in Setting 2, making it harder for models

		Musique			HotpotQA						2wiki							
		ans			ans		sup		joint		ans		sup		joint			
		EM	F1	Format	EM	F1	EM	F1	EM	F1	Format	EM	F1	EM	F1	EM	F1	Format
Qwen	Normal	18.2	30.9	84.0	31.6	42.8	2.6	26.4	1.3	13.4	90.7	6.7	8.0	1.6	5.5	1.0	2.6	89.8
	COT	1.0	6.6	7.0	3.1	9.7	0.1	0.7	0.1	0.4	4.4	0.6	1.9	0	0.1	0.0	0.0	4.2
	FSM1	26.2	41.2	100.0	22.5	33.3	0.7	9.9	0.4	3.6	100.0	27.6	37.9	4.7	25.8	1.9	9.1	100.0
	FSM2	21.9	37.7	100.0	33.1	46.0	1.8	28.8	1.0	15.7	100.0	36.1	49.3	7.7	38.4	5.1	19.4	100.0
GPT	Normal	16.7	27.8	94.0	34.0	45.9	0.7	15.0	3.0	8.0	94.3	37.3	46.6	1.0	14.1	9.0	7.2	95.8
	COT	4.5	13.6	14.7	12.3	26.0	0.4	4.5	2.0	17.8	16.2	8.2	19.3	0.2	1.3	1.0	4.6	7.0
	FSM1	26.0	38.4	100.0	23.4	32.0	2.4	29.3	2.0	9.8	100.0	30.1	40.0	14.2	47.0	2.0	8.5	100.0
	FSM2	18.6	27.4	100.0	28.4	36.7	2.2	21.4	4.0	26.7	100.0	30.6	37.2	6.9	29.6	7.0	19.8	100.0

Table 1: Results on the MHQA benchmark by the gpt-3.5-turbo-1106 and Qwen-72B with zero-shot in setting 2. Ans means answer. Sup means supporting paragraph index and tile. Joint means evidence triples including relationship with sub-answers. FSM2 means LLMs summary with results of FSM1 again

		Musique		HotpotQA		2Wiki	
		EM	F1	EM	F1	EM	F1
GPT	Normal	19.2	33.3	31.9	43.7	36.0	46.6
	COT	20.6	35.6	32.1	45.5	38.1	53.0
	SP-COT	14.4	28.4	24.8	37.4	23.2	36.0
	FSM1	23.1	40.3	24.5	39.3	27.1	40.6
	FSM2	26.7	40.5	33.3	45.7	39.2	50.1
Qwen	Normal	12.9	19.9	31.0	41.6	31.9	39.1
	COT	14.1	24.0	30.6	42.7	39.9	49.8
	SP-COT	6.0	14.7	14.6	28.6	18.5	31.8
	FSM1	33.2	48.5	28.0	37.4	39.1	47.9
	FSM2	33.2	48.5	32.2	41.3	40.2	50.3

Table 2: Results on the MHQA benchmark by the gpt-3.5-turbo-1106 and Qwen-72B in setting 1.

to follow them accurately. Furthermore, the presence of straightforward single-hop questions in the HotpotQA and 2Wiki datasets (Min et al., 2019) can confuse the LLMs with multi-hop reasoning. While our method’s performance in Setting 1 on less complex datasets like HotpotQA and 2Wiki is moderately satisfactory, it excels in precision with fewer instances of hallucination.

The performance of COT is notably inadequate, falling considerably below the standard few-shot settings. This discrepancy is mainly due to its failure to provide answers in the required format, detailed in Figure 4, a flaw we attribute to its bad instruction following ability. Conversely, the normal method struggles with supporting facts but achieves substantially higher scores on answers. This phenomenon indicates that although LLMs may misinterpret intermediate reasoning steps, they still yield correct answers, hinting at underlying data leakage and speculating. While some errors may stem from misinterpreting instructions, it is evident that there are significant concerns surrounding the authenticity and logical coherence of the models’ reasoning

chains. Additionally, the prospect of dataset leakage during evaluation cannot be disregarded. In conclusion, we posit that our method maintains a competitive edge in this context.

4 Discussion

Figure 5 provides error examples in experiments. We conclude four types of errors. **a) Reasoning Lost Issue:** providing an answer just with the last sub-question, instead of options for the original sentence. **b) Formatting Error:** The output can not be parsed to get answer, which added difficulty to the evaluation. Examples are presented in Figure 4. **c) Sub-question Decomposition Error:** Incorrectly decomposed the sub-questions. **d) Sub-answer Error:** Identified the wrong paragraph but provided a correct answer. **e) Hallucination Response:** Provided an correct answer without locating the relevant paragraph.

5 Conclusion

We have identified issues in traditional methods where LLMs may produce errors in the intermediate reasoning process but still arrive at the correct answer. Additionally, these methods often require few-shot demonstrations, which may surpass the maximum context length of LLMs. Therefore, we propose an easy zero-shot prompt paradigm called the FSM to address MHQA tasks systematically in an automated format. Our framework approaches problem-solving by focusing on one sub-task at a time iteratively, revising each step to ensure precision. By guiding LLMs through problems incrementally, FSM achieves superior results and aids in enhancing the LLMs’ capabilities without resorting to shortcuts.

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Limitations

This multi-turn dialogue process, inherent to our framework, mandates repeated handling of improperly formatted outputs, due to the output before will be the next input, which can be challenging for models with smaller parameter sizes and weaker follow-instruction capabilities. Therefore, models with limited capacity to follow instructions might not benefit from our method as any error in the intermediate steps could lead to an abrupt termination of the process.

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433 to-most prompting enables complex reasoning in 484

434 large language models. 485

435 Appendix 486

436 A Related Work 487

437 **Multi-hop Question Answering** Existing ap- 488

438 proaches to solving the multi-hop QA task can 489

439 be mainly categorized into question decomposi- 490

440 tion (Perez et al., 2020a; Fu et al., 2021; Perez 491

441 et al., 2020b), graph-based method (Tu et al., 2019; 492

442 Thayaparan et al., 2019; Fang et al., 2020), iterative 493

443 method (Qi et al., 2019) and LLMs (Wang et al., 494

444 2023) prompts. These models grapple with compu- 495

445 tational complexity and extensibility, and they lack 496

446 an interpretable reasoning chain, which deviates 497

447 from human cognitive processes. 498

448 **Language model for reasoning.** CoT(Wei et al., 499

449 2022) reveals the ability of large language models 500

450 to formulate their reasoning procedure for problem- 501

451 solving. Several follow-up works have since been 502

452 performed, including the least-to-most prompting 503

453 technique (Zhou et al., 2022) for solving compli- 504

454 cated tasks, zero-shot CoT (Kojima et al.), graph- 505

455 of-thought (GoT) (Besta et al., 2023), and reason-

ing with self-consistency (Wang et al., 2022). Re- 456

Act (Yao et al., 2022) interleaves the generation of 457

reasoning traces with task-specific actions, promot- 458

ing greater synergy. 459

Task decomposition. (Perez et al., 2020a) de- 460

composes a multi-hop question into a number of 461

independent single-hop sub-questions, which are 462

answered by an off-the-shelf question-answering 463

(QA) model. These answers are then aggregated 464

to form the final answer. Both question decom- 465

position and answer aggregation require training 466

models. After the emergence of Large Language 467

Models (LLMs), traditional training methods (Cao 468

et al., 2023) are rarely used due to their expensive 469

nature. Most current research focuses on the few- 470

shot approach. (Zhou et al., 2022) chains the pro- 471

cesses of problem decomposition and sub-problem 472

solving. The original problem and its sub-problems 473

are inherently interrelated, and forcibly breaking 474

them down into unrelated problems would unneces- 475

sarily increase the difficulty. 476

477 B Prompt 478

479 B.1 FSM1 480

Decomposer = Please determine whether the 481

question is simple sentence or compound sen- 482

tence. If it is a simple sentence, return 483

"simple":true,"subquestion":null.Otherwise, sim- 484

ple: false, decompose the question and generate the 485

first answerable simple sentence. reply in the form 486

of "simple":false,"subquestion":xxx. Do not reply 487

any other words and provide answers in JSON for- 488

mat!

Searcher = ""Given the paragraph below, please 489

find out the paragraph that contains the answer of 490

"" Please take a moment to thoroughly understand 491

the content before proceeding to the questions, then 492

carefully read the relevant paragraphs based on the 493

question and provide the most likely answer. Re- 494

turn the title of the paragraph and the answer no 495

more than 5 words in the form of "question":xxx, 496

"paragraph title":xxx, "answer":xxx. Do not re- 497

ply any other words and provide answers in JSON 498

format!"

Judge-if-continue=""Please compare the com- 499

plex question and subquestion, answer whether 500

they are semantically identical in the form of "iden- 501

tical":true or false. Do not reply any other words 502

and provide answers in JSON format!" 503

504	B.2 FSM2		
505	FSM2-post-summary-again="Documents: paragraphs:paragraphs found in FSM1 subquestion and	normal-setting1-w/o-evidence = "Answer the	554
506	answers:subquestion and answers given in FSM1	question according to the context. You must return	555
507	Question:origin question Answer the question rea-	in the form of "explain":"xxxx", "answer":answer.	556
508	soning step-by-step based on the Documents. If it	Do not reply any other words."	557
509	is a general question, please respond with 'Yes'		
510	or 'No'. Finally, you must return the title of	normal-setting2-w-evidence = "Answer the	558
511	the context, the sentence index (start from 0)	question according to the context. Find the para-	559
512	of the paragraph and the concise answer no more	graph that contains the answer of question, and	560
513	than 10 words and explanation in the form of	summarize a triple that contains [subject entity, re-	561
514	"supporting-facts": [[title, sentence id], ...], "evi-	lation, object entity]. Finally, you must return the	562
515	dences": [[subject entity, relation, object entity],...],	title of the context, the sentence index (start from 0)	563
516	"answer":"xxx", "explain":"xxxx". Do not reply any	of the paragraph and the concise answer no more	564
517	other words."	than 10 words in the form of "supporting-facts":	565
518		[[title, sentence id], ...], "evidences": [[subject en-	566
		tity, relation, object entity],...], "answer":answer.	567
		Do not reply any other words."	568
519	B.3 Baseline		
520	SP-COT(Wang et al., 2023)="This is a two-hop	prompt-step = "Answer the question according	569
521	to four-hop reasoning question-answering task that	to the context,Let's think step by step, and explain	570
522	requires decomposing the questions into simple,	your reasoning process. Find the paragraph that	571
523	answerable single-hop questions. The decompo-	contains the answer of question, and summarize a	572
524	sition process involves four types of questions:	triple that contains [subject entity, relation, object	573
525	comparison, inference, compositional, and bridge-	entity]. Finally, you must return the title of the	574
526	comparison. There are six specific decomposi-	context, the sentence index (start from 0) of the	575
527	tion steps in total, denoted by Q* representing the	paragraph and the concise answer no more than 10	576
528	decomposed subproblems. The steps are as fol-	words in the form of "supporting-facts": [[title, sen-	577
529	lows: First, Q1 -> Q2 Second, Q1 -> Q2 -> Q3	tence id], ...], "evidences": [[subject entity, relation,	578
530	Third, Q1 -> Q2 -> Q3 Fourth, (Q1&Q2) -> Q3	object entity],...], "answer":answer. Do not reply	579
531	Fifth, (Q1&Q2) -> Q3; Q3 -> Q4 Sixth, Q1 -> Q2;	any other words."	580
532	(Q2&Q3) -> Q4 The process involves first deter-		
533	mining the type of question and then identifying	React-setting2-w-evidence = ""Solve a question	581
534	the decomposition process type. It's important to	answering task with interleaving Thought, Action,	582
535	note that the decomposition of questions cannot	Observation steps. Thought can reason about the	583
536	be provided all at once; it must be done step by	current situation, and Action can be three types: (1)	584
537	step. Each subproblem needs to be decomposed	Search[entity], which searches the exact entity on	585
538	and answered before moving on to the next one, as	given context and returns the first paragraph if it	586
539	there is interdependence between the subproblems	exists. If not, it will return some similar entities to	587
540	.Finally, you must return the title of the context,	search. (2) Lookup[keyword], which returns the	588
541	the sentence index (start from 0) of the paragraph	next sentence containing keyword in the current	589
542	and the concise answer and explanation in the form	passage. (3) Finish[results], which returns the an-	590
543	of "explain":"xxxx", "supporting-facts": [[title, sen-	swer and finishes the task. You should plan and	591
544	tence id], ...], "evidences": [[subject entity, rela-	reason in the 'Thought', then perform your 'Ac-	592
545	tion, object entity],...], "answer":"no sentence and	tion', lastly, observe the result of action. Loop this	593
546	no more than 10 words ". Do not reply any other	process until the problem was finished. At last, you	594
547	words."	must additional output the title of the paragraphs,	595
548	COT-setting1-w/o-evidence = "Answer the	the sentence index (start from 0) of the paragraph	596
549	question according to the context,Let's think	and the concise answer no more than 10 words	597
550	step by step, and explain your reasoning pro-	and explanation in the form of Thought: reason-	598
551	cess. You must return in the form of "ex-	ing Action: Search[entity] or Lookup[keyword]	599
552	plain":"xxxx", "answer":answer. Do not reply any	or Finish[results] Observation: observe the results	600
553	other words."	of action end with Finish["supporting-facts": [[ti-	601
		tle, sentence id], ...], "evidences": [[subject entity,	602
		relation, object entity],...], "answer":answer] ""	603

B.4 Format Error

Gold-answer
<pre>{"question": "What government position was held by the woman who portrayed Corliss Archer in the film Kiss and Tell?", "answer": "Chief of Protocol", "type": "bridge", "supporting_facts": [{"Kiss and Tell (1945 film)", 0}, {"Shirley Temple", 0}, {"Shirley Temple", 1}], "level": "hard"}</pre>
<pre>{"question": "What science fantasy young adult series, told in first person, has a set of companion books narrating the stories of enslaved worlds and alien species?", "answer": "Animorphs", "type": "bridge", "supporting_facts": [{"The Hork-Bajir Chronicles", 0}, {"The Hork-Bajir Chronicles", 1}, {"The Hork-Bajir Chronicles", 2}, {"Animorphs", 0}, {"Animorphs", 1}], "level": "hard"}</pre>
<pre>{"question": "Are the Laleli Mosque and Esma Sultan Mansion located in the same neighborhood?", "answer": "no", "type": "comparison", "supporting_facts": [{"Laleli Mosque", 0}, {"Esma Sultan Mansion", 0}], "level": "hard"}</pre>
<pre>{"question": "The director of the romantic comedy \"Big Stone Gap\" is based in what New York city?", "answer": "Greenwich Village, New York City", "type": "bridge", "supporting_facts": [{"Big Stone Gap (film)", 0}, {"Adriana Trigiani", 0}], "level": "hard"}</pre>
FSM
<pre>{"answer": "Ambassador to Ghana and Czechoslovakia, Chief of Protocol of the United States.", "supportin_facts": [{"Kiss and Tell (1945 film)", 0}, {"Shirley Temple", "1"}, {"Shirley Temple", "1"}], "evidences": [{"Kiss and Tell (1945 film)", "portrayed", "Shirley Temple"}, {"Shirley Temple Black", "was named", "United States ambassador to Ghana and to Czechoslovakia and also served as Chief of Protocol of the United States"}, {"Shirley Temple Black", "had", "notable achievements outside of her acting career"]]}</pre>
<pre>{"answer": "The Hork-Bajir Chronicles", "supportin_facts": [{"The Hork-Bajir Chronicles", "2"}, {"The Hork-Bajir Chronicles", "0"}], "evidences": [{"Animorphs series", "involves", "enslaved worlds and alien species"}, {"The Hork-Bajir Chronicles", "involving", "enslaved worlds and alien species"]]}</pre>
<pre>{"answer": "Ortaköy neighborhood of Istanbul, Turkey", "supportin_facts": [{"Esma Sultan Mansion", "0"}, {"Esma Sultan Mansion", "0"}], "evidences": [{"Esma Sultan Mansion", "location", "Ortaköy neighborhood of Istanbul, Turkey"]]}</pre>
<pre>{"answer": "Greenwich Village", "supportin_facts": [{"Big Stone Gap (film)", "0"}, {"Adriana Trigiani", "0"}], "evidences": [{"Big Stone Gap", "director", "Adriana Trigiani"}, {"Adriana Trigiani", "based in", "Greenwich Village, New York City"]]}</pre>

Figure 3: The outputs of FSM are standard json format.

COT

```
{"answer": "To answer the question and provide a reasoning process, first, I will search for information related to the woman who portrayed Corliss Archer in the film Kiss and Tell. Then, I will search for the film Kiss and Tell in the given context to find the relevant paragraph. After finding the relevant paragraph, I will summarize a triple that contains [subject entity, relation, object entity] and return the title of the context, the sentence index (start from 0) of the paragraph, and the concise answer.\n\nUpon analyzing the context, I found the relevant paragraph in the section \"Kiss and Tell (1945 film)\". The paragraph contains the information related to the woman who portrayed Corliss Archer, which is Shirley Temple.\n\nTriple: [\"Shirley Temple\", \"portrayed\", \"Corliss Archer\"]\n\nTitle: Meet Corliss Archer\n\nSentence Index: 6\n\nConcise Answer: Shirley Temple portrayed Corliss Archer.\n\nTherefore, the final output is:\n\n```\njson\n{\n  \"supporting_facts\": [[\"Meet Corliss Archer\", 6]],\n  \"evidences\": [[\"Shirley Temple\", \"portrayed\", \"Corliss Archer\"]],\n  \"answer\": \"Shirley Temple portrayed Corliss Archer.\"\n}\n```\", "question": "\"What government position was held by the woman who portrayed Corliss Archer in the film Kiss and Tell?\""}}
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{"answer": "To find the answer, let's first identify the science fantasy young adult series told in first person. The paragraph that contains the relevant information is from the \"Animorphs\" section. The triple containing the solution is [\"Animorphs\", \"is a science fantasy series of young adult books written by\", \"Katherine Applegate and her husband Michael Grant\"]. The title of the context, sentence index, and the concise answer are as follows:\n\nTitle: \"Animorphs\"\n\nSentence Index: 0\n\nAnswer: \"Animorphs\"", "question": "\"What science fantasy young adult series, told in first person, has a set of companion books narrating the stories of enslaved worlds and alien species?\""}}
```

```
{"answer": "To find out if the Laleli Mosque and Esma Sultan Mansion are located in the same neighborhood, first, I need to locate the paragraph that contains the relevant information about the locations of both entities. Then, checking the information from the paragraph, the relation \"located in\" will be identified between \"Laleli Mosque\" and \"Laleli, Fatih\" or \"Esma Sultan Mansion\" and \"Ortak\u00f6y neighborhood\", to conclude if they are in the same neighborhood or not.\n\nThe relevant paragraph is:\n\n[\"Laleli Mosque\", [\"The Laleli Mosque (Turkish: \"Laleli Camii, or Tulip Mosque\" ) is an 18th-century Ottoman imperial mosque located in Laleli, Fatih, Istanbul, Turkey.\"]], [\"Esma Sultan Mansion\", [\"The Esma Sultan Mansion (Turkish: \"Esma Sultan Yal\\u0131s\\u0131\" ), a historical yal\\u0131 (English: waterside mansion ) located at Bosphorus in Ortak\u00f6y neighborhood of Istanbul, Turkey and named after its original owner Esma Sultan, is used today as a cultural center after being redeveloped.\"]],\n\nThe triple that contains the necessary information is: [\"Laleli Mosque\", \"located in\", \"Laleli, Fatih\"]\n\n[\"Esma Sultan Mansion\", \"located at\", \"Bosphorus in Ortak\u00f6y neighborhood\"]\n\nBased on this information, the concise answer is: \"No, they are not located in the same neighborhood.\"\n\nNow, I will use this evidence to provide a summary triple and supporting facts.\n\nThe summary triple is:\n\n{ \"supporting_facts\": [[\"Esma Sultan Mansion\", 6], [\"Laleli Mosque\", 5]], \"evidences\": [[\"Laleli Mosque\", \"located in\", \"Laleli, Fatih\"], [\"Esma Sultan Mansion\", \"located at\", \"Bosphorus in Ortak\u00f6y neighborhood\"]], \"answer\": \"No, they are not located in the same neighborhood.\" }", "question": "\"Are the Laleli Mosque and Esma Sultan Mansion located in the same neighborhood?\""}\n
```

```
{"answer": "To find the answer, let's start by identifying the paragraph containing information about the director of the romantic comedy \"Big Stone Gap.\" Upon examining the paragraphs, we can see that the paragraph about \"Big Stone Gap (film)\" contains the relevant information.\n\nTriple: [\"Adriana Trigiani\", \"is the director of\", \"Big Stone Gap\"]\n\nThen, the concise answer is: \"Adriana Trigiani\"\n\nBased on this, the requested details are as follows:\n\n- Title of the context: \"The director of the romantic comedy \"Big Stone Gap\" is based in what New York city?\"\n\n- Sentence index: 8\n\n- Concise answer: \"Adriana Trigiani\"\n\n- Supporting facts: [[\"Big Stone Gap (film)\", 0]]\n\n- Evidence: [[\"Adriana Trigiani\", \"is the director of\", \"Big Stone Gap\"]]", "question": "\"The director of the romantic comedy \"Big Stone Gap\" is based in what New York city?\""}}
```

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Figure 4: There are some error format examples for COT.



Figure 5: Contrast between baseline and FSM. There are some error examples for baseline.