

# 000 001 002 003 004 005 006 007 008 009 010 011 012 013 014 015 016 017 018 019 020 021 022 023 024 025 026 027 028 029 030 031 032 033 034 035 036 037 038 039 040 041 042 043 044 045 046 047 048 049 050 051 052 053 PE-DyRA: DYNAMIC RANK ADAPTATION FOR PARAMETER-EFFICIENT FINE-TUNING VIA IMPORTANCE-AWARE PRUNING AND EXPANSION

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## ABSTRACT

As large language models grow in scale, full-parameter fine-tuning for downstream tasks incurs substantial computational and storage costs. Low-Rank Adaptation (LoRA) provides a parameter-efficient paradigm for model adaptation, but its fixed-rank allocation cannot adapt to the heterogeneous importance of different layers or the evolving requirements across training stages, resulting in either redundancy or insufficient capacity. In this paper, we introduce Dynamic Rank Adaptation via Importance-Aware Pruning and Expansion (PE-DyRA), a novel framework that dynamically allocates ranks through importance score-based pruning and expansion. PE-DyRA introduces three key innovations: 1) A parameter importance evaluation measure based on gradient information and input activations to enable more stable ranking; 2) A bidirectional rank adjustment mechanism that dynamically prunes and expands ranks based on importance, enabling flexible allocation and improved parameter utilization; 3) The PE-DyRA framework can be used as a paradigm to achieve better results on benchmark methods such as DoRA, PiSSA, and QLoRA. Extensive experiments demonstrate the effectiveness of PE-DyRA, surpassing baseline methods. Furthermore, theoretical analysis demonstrates that PE-DyRA has better parameter efficiency.

## 1 INTRODUCTION

Large language models (LLMs) (Achiam et al., 2023; Dubey et al., 2024; Guo et al., 2025) have become the core infrastructure of natural language processing, advancing performance from general-purpose inference to domain-specific applications (Ziems et al., 2023; Brown et al., 2020). However, the training and full parameter tuning of these models require huge computing resources and storage overhead (Raffel et al., 2020). Therefore, parameter-efficient fine-tuning methods for large-scale pre-trained models have become a research hotspot (Liu et al., 2022).

Low-Rank Adaptation (LoRA)(Hu et al., 2022) reduces computational cost by decomposing model weights into trainable low-rank matrices. However, its fixed-rank allocation limits adaptability and parameter efficiency (Yang et al., 2024), as different layers contribute unequally to downstream tasks. Kalajdzievski (2023) showed that increasing the rank of LoRA with proper scaling can significantly improve performance. Yet higher ranks incur substantial memory overhead, which has motivated the development of dynamic rank adaptation methods. DyLoRA (Valipour et al., 2023) employs random truncation to enable flexible inference-time rank selection, while IncreLoRA (Zhang et al., 2023a) incrementally allocates more parameters to important modules. AdaLoRA (Zhang et al., 2023b) prunes ranks via importance-based masking. AutoLoRA(Zhang et al., 2024) automates rank selection via meta-learned pruning of redundant singular components. TriAdaptLoRA (Liang et al., 2025) proposes an adaptive rank-growth strategy governed by dynamic thresholds. While the aforementioned methods are effective, they face two key limitations. First, they are restricted to either pruning or expansion. As shown in Figure 1a, pruning alone achieves high utilization but few effective ranks, whereas expansion increases effective ranks but with low utilization. Second, existing approaches primarily rely on weight or gradient magnitudes to assess parameter importance, often neglecting input activations, which play a crucial role in neuron outputs.

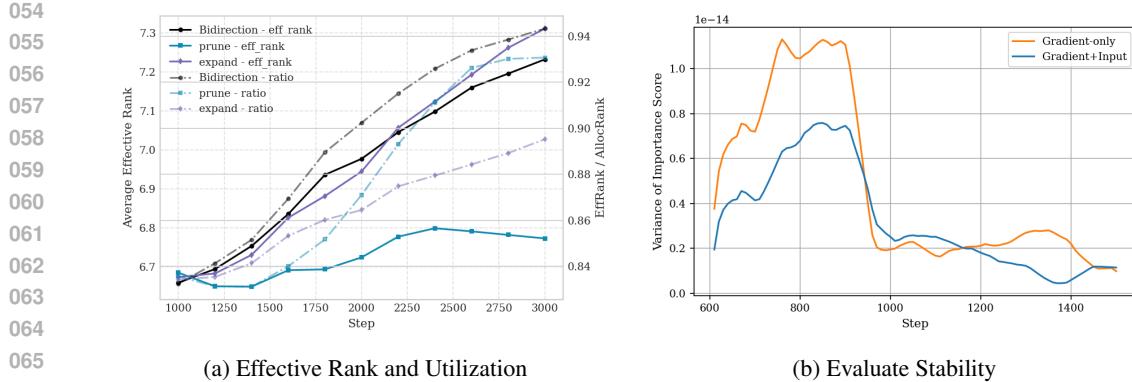


Figure 1: Analysis of importance-guided dynamic rank allocation. (a) Effective rank and utilization ratio across training steps. (b) Stability evaluation of rank adaptation during training.

Table 1: Comparison of dynamic rank adaptation methods.

Method	Importance Basis	Adaptation	Frequency
DyLoRA (Valipour et al., 2023)	Multi-rank joint training	No adjustment	Static
IncreLoRA (Zhang et al., 2023a)	Gradient	Expansion	Periodic
AdaLoRA (Zhang et al., 2023b)	Gradient	Pruning	Periodic
AutoLoRA (Zhang et al., 2024)	Meta-learning	Pruning	Post-optimization
TriAdaptLoRA (Liang et al., 2025)	Frobenius norms	Expansion	Periodic
<b>Ours</b>	<b>Gradient + Input</b>	<b>Bidirectional</b>	<b>Periodic</b>

To address these limitations, we propose a novel dynamic rank assignment strategy that enables more efficient optimization of low-rank adapters through importance-based evaluation and adaptive rank adjustment. At scheduled intervals, parameter efficiency is improved by pruning redundant ranks and expanding those in critical layers. This strategy maintains both high effective rank and utilization during training (Figure 1a), and its bidirectional adjustment surpasses approaches restricted to pruning or expansion. For parameter importance evaluation, we combine gradient information, reflecting parameter sensitivity, with input activations, reflecting data dependence, to obtain a more accurate and fine-grained assessment. See Figure 1b, incorporating the input leads to a more stable evaluation throughout training. Table 1 provides a comparative overview of dynamic rank adaptation methods, demonstrating the advantages of our approach. We evaluate PE-DyRA across diverse tasks and model scales, consistently demonstrating superior performance over existing approaches.

The main contributions of this work are as follows:

- 1) A bidirectional rank adjustment mechanism that dynamically prunes and expands ranks based on importance, enabling flexible allocation and improved parameter utilization.
- 2) We propose an enhanced importance metric that integrates gradient-based parameter sensitivity with input activation information for more stable ranking.
- 3) PE-DyRA framework can be used as a paradigm on benchmark methods such as DoRA, PiSSA, and QLoRA to achieve better results.
- 4) Experimental results across diverse tasks demonstrate the effectiveness of PE-DyRA over baseline methods, while theoretical analysis confirms its superior parameter efficiency.

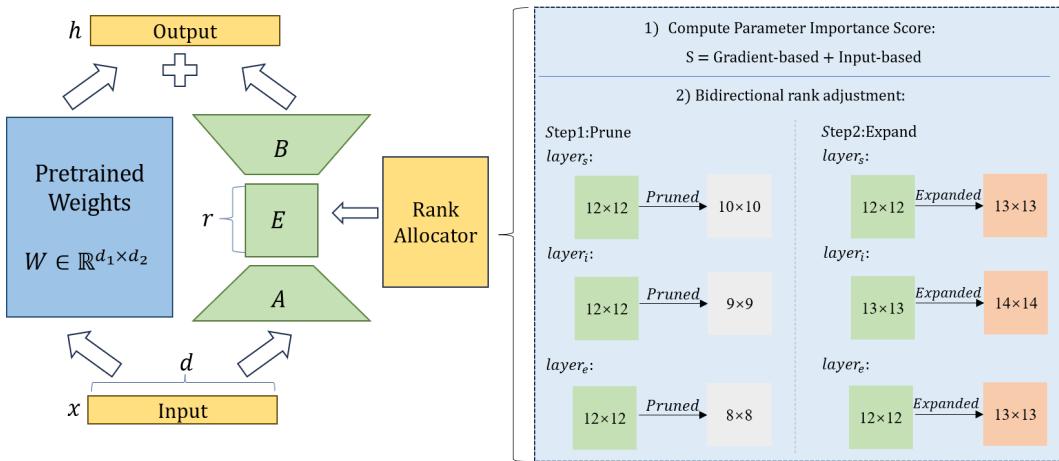
## 2 RELATED WORK

**Low-Rank Adaptation.** PEFT methods have evolved from adapter layers (Houlsby et al., 2019) and prompt tuning (Lester et al., 2021) to LoRA (Hu et al., 2022). The key insight of LoRA is that weight updates during adaptation can be effectively represented using low-rank decompositions.

108 PiSSA (Meng et al., 2024) leverages principal SVD to initialize LoRA by truncating pre-trained  
 109 weights, thereby accelerating fine-tuning convergence. QLoRA (Dettmers et al., 2023) extends  
 110 LoRA with 4-bit quantization and gradient dequantization, enabling efficient fine-tuning of large  
 111 models. DoRA (Liu et al., 2024) decomposes the weight update into two independent components,  
 112 amplitude and direction, and applies LoRA adaptation only to the direction component.

113 **Dynamic Rank Adaptation Methods.** Standard LoRA uses fixed-rank matrices, whereas recent  
 114 work explores dynamic rank adaptation to optimize allocation during training. AdaLoRA (Zhang  
 115 et al., 2023b) adapts ranks via a three-term SVD formulation with importance-based pruning and  
 116 orthogonality regularization, but requires a large initial parameter space. DyLoRA (Valipour et al.,  
 117 2023) enables flexible rank selection during inference by training a unified model across multiple  
 118 candidate ranks simultaneously. IncreLoRA (Zhang et al., 2023a) instead adopts a progressive rank  
 119 expansion strategy, gradually increasing the model capacity. SoRA (Ding et al., 2023) induces sparsity  
 120 within LoRA modules. TriAdaptLoRA (Liang et al., 2025) draws on neuroscience principles to  
 121 introduce an adaptive rank-growth strategy controlled by dynamic thresholds. These methods illustrate  
 122 various strategies for dynamic LoRA rank allocation to balance efficiency and performance.

### 123 3 METHOD



141 Figure 2: Overview of the proposed dynamic rank adjustment framework. (Left) The base architecture  
 142 with rank allocation. (Right) The two-step bidirectional rank adjustment procedure: (1)  
 143 compute parameter importance score  $S$  based on both gradient and input information; (2) prune  
 144 ranks in less important layers and expand them in more critical ones, enabling adaptive allocation of  
 145 model capacity.

146 In this section, we propose PE-DyRA, a novel parameter-efficient fine-tuning method based on a  
 147 dynamic rank adjustment framework that aims to dynamically optimize the assignment of trainable  
 148 parameters. The overall architecture of PE-DyRA is shown in Figure 2. Firstly, the incremental  
 149 weight matrix of LoRA layer is decomposed into SVD form, and the rank allocator performs a bi-  
 150 directional adjustment on the rank size of each layer by calculating the importance score, pruning off  
 151 redundant ranks and then expanding in more critical layers, and finally performing a final warmup.  
 152 To prevent the adaptive capacity from being completely pruned, the minimum rank is set to 1 to  
 153 maintain minimal adaptability.

#### 155 3.1 SVD-FORM ADAPTATION

157 We parameterize the weight increment in the form of singular value decomposition, and represent  
 158 the incremental update of the pre-trained weight matrix as

$$159 \mathbf{W} = \mathbf{W}^{(0)} + \Delta = \mathbf{W}^{(0)} + \mathbf{A} \mathbf{E} \mathbf{B} \quad (1)$$

160 where  $\mathbf{A} \in \mathbb{R}^{d_1 \times r}$  and  $\mathbf{B} \in \mathbb{R}^{r \times d_2}$  are learnable factor matrices,  $\mathbf{E} = \text{diag}(e_1, \dots, e_r)$  is a trainable  
 161 diagonal matrix of singular values.

Similar to the existing work AdaLoRA (Zhang et al., 2023b), we still adopt the concept of triples. For a LoRA layer with rank  $r$ , each rank’s corresponding triple is treated as the fundamental unit for computing importance scores and performing rank adjustments. It can be expressed as  $\mathcal{G}_i = (\mathbf{a}_i, e_i, \mathbf{b}_i)$  for  $i = 1, \dots, r$ , where  $\mathbf{a}_i$  and  $\mathbf{b}_i$  are the  $i$ -th column of  $\mathbf{A}$  and the  $i$ -th row of  $\mathbf{B}$ , respectively.

At step  $t$ , the set of triples is  $\mathcal{G}^{(t)} = \{G_1^{(t)}, G_2^{(t)}, \dots, G_{r^{(t)}}^{(t)}\}$ . We compute an importance score for each triple:  $S_i^{(t)} = f(\mathbf{a}_i^{(t)}, e_i^{(t)}, \mathbf{b}_i^{(t)})$ , where  $f(\cdot)$  integrates gradient-based and input-based sensitivities. Based on  $S_i^{(t)}$ , we update the triple set by pruning and expansion:  $\mathcal{G}^{(t+1)} = (\mathcal{G}^{(t)} \setminus \mathcal{G}_{\text{pruned}}^{(t)}) \cup \mathcal{G}_{\text{expanded}}^{(t)}$ , where  $\mathcal{G}_{\text{pruned}}^{(t)}$  contains the least important triples to be removed, and  $\mathcal{G}_{\text{expanded}}^{(t)}$  introduces new triples initialized for critical directions.

To maintain decomposition stability, we apply spectral regularization (Zhang et al., 2023b):

$$\mathcal{R}_{\text{orth}} = \|\mathbf{A}^\top \mathbf{A} - \mathbf{I}_r\|_F^2 + \|\mathbf{B}^\top \mathbf{B} - \mathbf{I}_r\|_F^2 \quad (2)$$

### 3.2 PARAMETER IMPORTANCE EVALUATION

#### 3.2.1 GRADIENT-BASED PARAMETER IMPORTANCE ESTIMATION

Inspired by AdaLoRA (Zhang et al., 2023b) and Platon (Zhang et al., 2022), we quantify parameter sensitivity using the absolute product of weights and gradients, and apply exponential moving average (EMA) smoothing across training iterations. Due to the high variability and uncertainty, the quantification of uncertainty is also performed. The final importance score is defined as the product of smoothed sensitivity and uncertainty:

$$\begin{cases} \text{Sensitivity: } \bar{I}_{(w_{ij})}^{(t)} = \beta_1 \bar{I}_{(w_{ij})}^{(t-1)} + (1 - \beta_1) \left| w_{ij}^{(t)} \cdot \nabla_{w_{ij}} L^{(t)} \right| \\ \text{Uncertainty: } \bar{U}_{(w_{ij})}^{(t)} = \beta_2 \bar{U}_{(w_{ij})}^{(t-1)} + (1 - \beta_2) \left| \left| w_{ij}^{(t)} \cdot \nabla_{w_{ij}} L^{(t)} \right| - \bar{I}_{(w_{ij})}^{(t)} \right| \\ \text{Importance: } \mathcal{S}_{(w_{ij})}^{(t)} = \bar{I}_{(w_{ij})}^{(t)} \cdot \bar{U}_{(w_{ij})}^{(t)} \end{cases} \quad (3)$$

where  $\beta_1, \beta_2 \in [0, 1]$  are EMA coefficients.

**Gradient-Aware Triple Importance.** During training, we observe that the gradients of the factor matrices  $A$  and  $B$ , which correspond to the left and right singular matrices, are typically smaller by orders of magnitude compared to those of the core matrix  $E$ . This indicates that the update of the core matrix plays a more critical role in the optimization process (see Figure 11 in Appendix I).

Consequently, when evaluating the importance of a triple, we do not rely on a uniform linear combination of its constituent importance scores. Instead, we introduce a **gradient-aware weighting scheme**, where the contribution of each component is scaled according to the relative magnitude of its gradient. Formally, the triple-level importance score at step  $t$  is defined as

$$S_{G_i}^{(t)} = \omega_E^{(t)} \cdot \mathcal{S}(E_i) + \omega_A^{(t)} \cdot \mathcal{S}(A_i) + \omega_B^{(t)} \cdot \mathcal{S}(B_i), \quad (4)$$

where the adaptive weights are computed as

$$\omega_X^{(t)} = \frac{\|\nabla_X L^{(t)}\|_2}{\|\nabla_A L^{(t)}\|_2 + \|\nabla_E L^{(t)}\|_2 + \|\nabla_B L^{(t)}\|_2}, \quad X \in \{A, E, B\}. \quad (5)$$

This formulation ensures that components with stronger optimization impact, particularly the core matrix, receive larger weights in the triple-level importance score. As a result, the aggregated importance evaluation better reflects the actual training dynamics and guides more effective rank allocation during dynamic adjustment.

For detailed empirical results validating the proposed gradient-aware weighting scheme, please refer to Appendix F.

#### 3.2.2 INPUT-BASED PARAMETER IMPORTANCE ESTIMATION

Notably, on datasets with diverse input distributions, the input activations can vary from token to token. So input activations also play an equally critical role in determining the actual output of a

216 neuron. The contribution to the neuron output is determined jointly by magnitude of weight and the  
 217 scale of the corresponding input activation.

218 Motivated by pruning metrics such as Wanda (Sun et al., 2024), we extend the importance estimation  
 219 to the LoRA decomposition. Let  $X$  denote the input activations. Given the input representation  
 220  $X \in \mathbb{R}^{N \times d}$  (where  $N = \text{batch\_size} \times \text{seq\_len}$ , and  $d$  is the hidden dimension), we  
 221 compute the L2 norm along the batch and token dimension for each feature dimension:  $\|X_j\|_2 =$   
 222  $\frac{1}{N} \sum_{i=1}^N x_{ij}^2$ ,  $j = 1, \dots, d$ . This preserves per-feature energy, reflecting the relative contribution  
 223 of each input dimension. Then we apply exponential moving average(EMA) to this. For  $A \in \mathbb{R}^{d_1 \times r}$ ,  
 224 the importance of each element is expressed as  $S_{ij} = |W_{ij}| \cdot \|X_j\|_2$ . The importance score for each  
 225 triplet is defined as

$$227 \quad S_{G_i}^{inp} = |e_i| \cdot \sum_{k=1}^{d_1} S_{ki} \cdot \|\mathbf{B}_{i:}\|_2, \quad i = 1, \dots, r, \quad (6)$$

230 As shown in Algorithm 1 in Appendix I.3, the procedure of computing the overall importance score  
 231 is illustrated.

232 **Layer-level Importance.** For a LoRA layer with  $r$  ranks, corresponding to triples  $\{G_1, G_2, \dots,$   
 233  $G_r\}$ , the layer-level importance score is defined as

$$235 \quad S_{\text{layer}} = \frac{1}{r} \sum_{i=1}^r S(G_i), \quad (7)$$

238 where  $S(G_i)$  denotes the importance score of the  $i$ -th triple at the rank-level.

### 239 3.3 BIDIRECTIONAL RANK ADJUSTMENT STRATEGY

240 **Pruning Phase.** During the pruning phase, we first compute the importance score for each rank-  
 241 level triple  $G = (A, E, B)$ . All triples are sorted according to their importance scores, and the  $k$   
 242 triples with the lowest aggregated scores are selected for removal:  $\mathcal{P} = \operatorname{argmin}_{\mathcal{S}, |\mathcal{S}|=k} \sum_{G \in \mathcal{S}} S(G)$   
 243 , where  $\mathcal{P}$  denotes the set of pruned ranks.

244 **Expansion Phase.** In the expansion phase, we perform layer-level importance evaluation by  
 245 aggregating rank-level scores. Based on these layer-level scores, we execute a global ranking  
 246 across all layers and adopt a strict rank-conservation strategy: the  $k$  rank resources removed  
 247 in the pruning phase are reassigned to the top- $k$  layers with the highest  $S_{\text{layer}}^{(\ell)}$  values:  $\mathcal{E} =$   
 248  $\operatorname{argmax}_{\mathcal{S}, |\mathcal{S}|=k} \sum_{\ell \in \mathcal{S}} S_{\text{layer}}^{(\ell)}$ , where  $\mathcal{E}$  denotes the set of expanded layers.

249 Under the constraint of a fixed total rank budget, the bidirectional adjustment strategy removes  
 250 less important redundant parameters and reallocates them to more critical LoRA layers, thereby  
 251 improving parameter efficiency and enhancing model performance.

252 For detailed bidirectional rank adjustment strategy, please refer to Algorithm 2 in the appendix I.3.

### 253 3.4 PARAMETRIC EFFICIENCY ANALYSIS

254 **Theorem 3.1** (Pareto-Optimal Parameter Efficiency under Rank Allocation Constraints). *Consider*  
 255  $L$  LoRA layers, each assigned a rank  $r_l$ , under a fixed total rank budget  $R_{\text{total}}$ :  $\sum_{l=1}^L r_l = R_{\text{total}}$ .  
 256 Let  $G_l$  denote the importance score of layer  $l$ . The necessary condition for Pareto-optimal parameter  
 257 efficiency is:

$$258 \quad r_l \propto G_l^{2/3} \quad (8)$$

259 That is, layers with higher importance scores should be assigned more ranks.

260 **Inference: Dynamic vs. Static Strategy** A dynamic rank adjustment strategy that updates  $r_l$   
 261 in response to changes in  $G_l$  during training can iteratively approach the Pareto-optimal condition  
 262 equation 8. Static strategies, which fix  $\{r_l\}$  at initialization, cannot adapt to evolving layer impor-  
 263 tance, and thus are generally less efficient in parameter utilization and model performance. See  
 264 Appendix B for the complete derivation.

270 Table 2: Performance comparison of different PEFT methods on GLUE benchmark (rank  $r = 8$ ).  
271

273 <b>Method</b>	<b>SST-2</b>	<b>MNLI</b>	<b>CoLA</b>	<b>QNLI</b>	<b>MRPC</b>	<b>QQP</b>	<b>RTE</b>	<b>STS-B</b>	<b>All</b>
274	Acc.	Acc.	Mcc.	Acc.	Acc.	Acc.	Acc.	Corr.	Avg.
275 LoRA	95.18	89.74	69.33	93.90	89.70	91.99	86.28	91.66	88.473
276 PiSSA	95.53	90.30	71.41	94.07	90.20	91.92	<b>88.09</b>	91.54	89.133
277 LoRA+	95.3	90.28	70.25	94.01	90.93	92.09	86.28	91.54	88.835
278 AdaLoRA	95.53	90.50	69.02	94.42	90.93	92.03	87.00	91.77	88.9
279 DyLoRA	95.18	89.51	69.82	94.29	89.95	91.97	85.92	91.74	88.547
280 IncreLoRA	95.72	90.62	70.20	94.36	90.11	91.91	86.88	91.38	88.898
281 RandLoRA	<b>95.98</b>	89.96	68.22	93.74	90.69	92.06	86.28	91.34	88.534
282 TriAdaptLoRA	95.68	<b>90.64</b>	<b>71.6</b>	94.37	90.77	92.09	87.84	91.79	89.348
283 PE-DyRA	<b>95.98</b>	90.38	71.43	<b>94.53</b>	<b>91.18</b>	<b>92.14</b>	<b>88.09</b>	<b>91.98</b>	<b>89.464</b>

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286 4 EXPERIMENTS  
287288 4.1 MODELS AND DATASETS  
289290 **Natural Language Understanding (NLU).** We adopt **DeBERTa-v3-base** (He et al., 2021) and  
291 fine-tune it on the **GLUE benchmark** (Wang et al., 2019), using eight tasks from the benchmark.292 **Mathematical Reasoning and Code Generation.** We employ **LLaMA-2-7B** (Touvron et al., 2023)  
293 and **LLaMA-3-8B** (Dubey et al., 2024) for evaluation on **mathematical reasoning**, where the mod-  
294 els are fine-tuned on MetaMathQA (Yu et al., 2024) and assessed on GSM8K (Cobbe et al., 2021)  
295 and MATH (Hendrycks et al., 2021). For **code generation**, the models are fine-tuned on CodeFeed-  
296 back (Zheng et al., 2024) and evaluated on HumanEval (Chen et al., 2021) and MBPP (Austin et al.,  
297 2021).298 **Summarization.** We use **BART-large** (Lewis et al., 2019) for summarization on **XSum** (Narayan  
299 et al., 2018), which evaluate the ability to generate concise and faithful summaries.  
300301 4.2 BASELINES  
302303 We compare our method against a broad range of parameter-efficient fine-tuning (PEFT) approaches,  
304 including **LoRA** and its variants, as well as **dynamic rank adaptation methods**:  
305

- 306 • **LoRA-based methods:** LoRA (Hu et al., 2022), LoRA+ (Hayou et al., 2024)  
307 , PiSSA (Meng et al., 2024), DoRA (Liu et al., 2024), RandLoRA (Albert et al., 2025),  
308 QLoRA (Dettmers et al., 2023), RaSA (He et al., 2025).
- 309 • **Dynamic rank methods:** AdaLoRA (Zhang et al., 2023b), IncreLoRA (Zhang et al.,  
310 2023a), DyLoRA (Valipour et al., 2023), TriAdaptLoRA (Liang et al., 2025).

312 4.3 RESULTS  
313314 **Natural Language Understanding.** Table 2 reports the performance of different PEFT methods  
315 on eight tasks from the GLUE benchmark with rank of  $r = 8$ . Overall, our method consistently out-  
316 performs existing baselines, achieving the highest average score (89.464%), demonstrating superior  
317 generalization across both sentence-level and sentence-pair classification tasks. For example, on the  
318 MRPC task, our method achieves 91.18% accuracy, which is 0.25% higher than the best-performing  
319 baseline (AdaLoRA, 90.93%).320 **Mathematical Reasoning and Code Generation.** As shown in Table 3, our method (PE-DyRA)  
321 achieves the best performance on both LLaMA2-7B and LLaMA3-8B. On LLaMA2-7B, the overall  
322 average score of 34.69% surpasses the strongest baseline DoRA (33.99%) by nearly +0.7 points. On  
323 LLaMA3-8B, PE-DyRA also delivers the best average score (65.09%), demonstrating consistent  
advantages in both mathematical reasoning and code generation.

324 Table 3: Performance comparison of different PEFT methods on LLaMA2-7B and LLaMA3-8B.  
325

326 <b>Model</b>	327 <b>Method</b>	328 <b>#Params(%)</b>	329 <b>GSM8K</b>	330 <b>MATH</b>	331 <b>HumanEval</b>	332 <b>MBPP</b>	333 <b>Avg</b>
334 LLaMA2-7B	LoRA	0.15	52.90	7.60	26.0	34.7	30.3
	DoRA	0.17	56.09	9.76	31.7	38.4	33.99
	QLoRA	0.28	50.32	6.12	24.8	32.8	28.51
	RaSA	0.15	<b>56.41</b>	9.72	28.0	36.2	32.58
	AdaLoRA	0.22	52.01	8.26	26.2	35.2	30.42
	PE-DyRA	0.15	56.25	<b>10.12</b>	<b>33.5</b>	<b>38.9</b>	<b>34.69</b>
335 LLaMA3-8B	LoRA	0.13	81.27	39.04	64.0	69.0	63.33
	DoRA	0.15	<b>81.42</b>	37.22	65.2	72.0	63.96
	QLoRA	0.23	81.12	39.58	67.1	70.6	64.6
	RaSA	0.13	80.97	36.18	67.1	69.6	63.46
	AdaLoRA	0.20	81.04	39.62	65.9	72.0	64.64
	PE-DyRA	0.13	80.82	<b>40.24</b>	<b>67.1</b>	<b>72.2</b>	<b>65.09</b>

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342 **Summarization.** Table 4 shows the results on summarization task. Compared with LoRA and  
343 AdaLoRA, our method (PE-DyRA) achieves the best performance across all Rouge metrics while  
344 using the same parameter budget as LoRA (2.06M).

345  
346 Table 4: Performance comparison of different PEFT methods on XSum.  
347

348 <b>Method</b>	349 <b>#Params</b>	350 <b>Rouge-1</b>	351 <b>Rouge-2</b>	352 <b>Rouge-L</b>	353 <b>Rouge-Lsum</b>
LoRA	2.06M	43.6283	20.4566	35.6239	35.6194
AdaLoRA	3.09M	43.9557	20.5627	35.6264	35.6129
PE-DyRA	2.06M	<b>44.0444</b>	<b>20.8523</b>	<b>35.9616</b>	<b>35.9602</b>

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#### 4.4 PE-DYRA AS A GENERAL PARADIGM

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358 To further validate the generality of our proposed method, we integrate PE-DyRA into several rep-  
359 resentative PEFT approaches, including PiSSA, DoRA, and QLoRA, across both natural language  
360 understanding (NLU) and code generation tasks. The results are reported in Table 11 and Table 12  
361 in Appendix I.2.

362 On the DeBERTa-v3-base NLU benchmark, PE-DyRA consistently improves PiSSA, achieving an  
363 average accuracy of 89.29%. For LLaMA models on code generation, PE-DyRA also provides  
364 significant gains. On LLaMA2-7B, PE-DyRA+DoRA improves MBPP by 1.3% over DoRA. On  
365 LLaMA3-8B, PE-DyRA+QLoRA achieves 74.3% on MBPP, outperforming QLoRA by 3.7%.

366 These results suggest that PE-DyRA can be applied as a paradigm to existing PEFT methods, im-  
367 proving their performance across different models and tasks. This highlights its wide applicability  
368 and generalization ability.

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#### 4.5 ANALYSIS

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##### 4.5.1 ABLATION STUDY ON BIDIRECTIONAL STRATEGIES

374  
375 We propose a bidirectional rank adjustment strategy and validate it via an ablation study. From  
376 Table 5, compared with Prune-only or Expand-only variants, our method (PE-DyRA) balances pa-  
377 rameter allocation and model capacity, achieving superior performance without increasing the total  
number of training parameters.

378 Table 5: Performance comparison with different strategies.  
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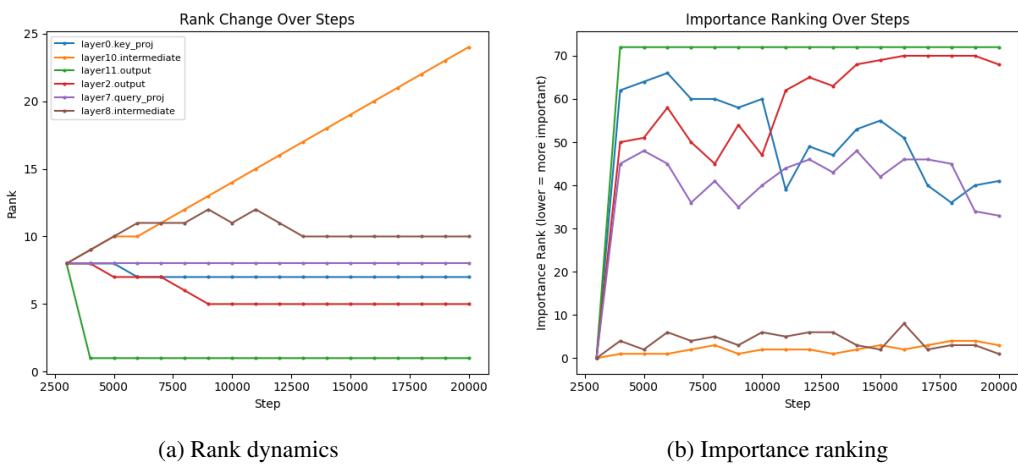
380 <b>Method</b>	381 <b>MRPC</b>	382 <b>STS-B</b>	383 <b>RTE</b>	384 <b>CoLA</b>	385 <b>SST-2</b>	386 <b>QNLI</b>	387 <b>QQP</b>	388 <b>MNLI</b>	389 <b>Avg</b>
390 LoRA	391 89.70	392 91.66	393 86.28	394 69.33	395 95.18	396 93.90	397 91.99	398 89.74	399 88.473
400 +Prune	401 90.20	402 91.80	403 87.36	404 70.19	405 95.53	406 94.34	407 92.13	408 90.37	409 88.99
410 +Expand	411 90.69	412 91.72	413 <b>88.09</b>	414 70.21	415 95.30	416 94.51	417 <b>92.46</b>	418 90.30	419 89.16
420 PE-DyRA	421 <b>91.18</b>	422 <b>91.98</b>	423 <b>88.09</b>	424 <b>71.43</b>	425 <b>95.98</b>	426 <b>94.53</b>	427 92.14	428 <b>90.38</b>	429 <b>89.464</b>

386  
387 4.5.2 ABLATION OF INPUT-BASED IMPORTANCE  
388389 To investigate the effect of input-based importance calculation in PE-DyRA, we conduct an ablation  
390 study on LLaMA2-7B across code generation benchmarks. We conducted experiments on two ways,  
391 without input-based importance and with input-based importance, and analyzed the results.392 Table 6: Ablation study on input-based importance calculation in PE-DyRA.  
393

394 <b>Model</b>	395 <b>Variant</b>	396 <b>Humaneval</b>	397 <b>Humaneval+</b>	398 <b>MBPP</b>	399 <b>MBPP+</b>
400 LLaMA2-7B	401 w/o input-based	402 32.3	403 29.3	404 38.4	405 29.9
406	407 with input-based	408 <b>33.5</b>	409 <b>30.5</b>	410 <b>38.9</b>	411 <b>32.5</b>

400 As shown in Table 6, incorporating input-based importance calculation improves performance on  
401 benchmarks, highlighting its effectiveness in PE-DyRA.

## 402 4.5.3 LAYER-WISE RANK DYNAMICS

403 To analyze the dynamic rank adjustment mechanism, we track the evolution of allocated ranks and  
404 corresponding importance rankings for representative layers during training (Figure 3, (a) rank dy-  
405 namics; (b) importance ranking, where smaller values denote higher importance).424 Figure 3: Evolution of dynamic rank allocation and layer importance during training.  
425426 We observe clear differences across layers. `layer10.intermediate` consistently maintains  
427 high importance throughout training, leading to an increase in its allocated rank. In contrast,  
428 `layer11.output` exhibits low importance and rapidly reduces its rank at the beginning of training.  
429 Other layers show fluctuating importance rankings, resulting in relatively stable rank changes.  
430 Notably, `layer8.intermediate` remains among the top in importance ranking, causing its rank  
431 to increase at each update; however, the number of its ranks fluctuates up and down over time. This  
432 suggests that certain triples at the rank level have low importance and are thus pruned.

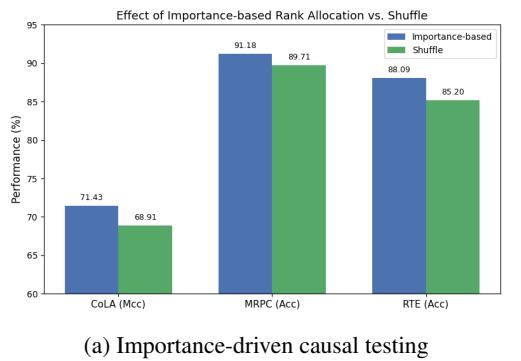
432 4.5.4 PERFORMANCE UNDER DIFFERENT RANK BUDGETS  
433

434 As shown in Table 13 in Appendix I.2, we also test the fine-tuning performance of the proposed  
435 method on some datasets with different rank budgets. It can be observed that the proposed method  
436 achieves performance improvement under different budgets.

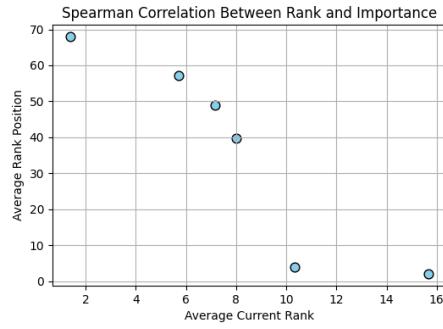
438 4.5.5 ABLATION STUDY ON RANK ADJUSTMENT SIZE  
439

440 Our method performs rank updates every  $T$  steps, where the adjustment size (number of ranks  
441 pruned/expanded) critically affects performance. We evaluate adjustment sizes  $\{4, 8, 12, 24\}$  on  
442 DeBERTaV3-base with initial rank  $r = 8$  to analyze this effect.

443 As shown in Table 14 in Appendix I.2, when the dynamic rank adjustment is small, the model’s  
444 ability to improve is limited; when it is large, pruning trained ranks and introducing new ones can  
445 destabilize training. The optimal adjustment value depends on both the model architecture and the  
446 initial rank size.

448 4.5.6 IMPORTANCE-DRIVEN CAUSAL TESTING AND SPEARMAN CORRELATION  
449  
450  
451

(a) Importance-driven causal testing



(b) Spearman correlation

464 Figure 4: Effectiveness of importance-guided dynamic rank allocation. (a) Causal test comparing  
465 importance-based allocation with random shuffle. (b) Spearman correlation between mean allocated  
466 rank and mean importance ranking.

467  
468 In Figure 4a, we test causality by randomizing the importance order during training, making rank ad-  
469 justment random. The resulting performance drop across datasets confirms that importance-to-rank  
470 assignment is indeed effective. In Figure 4b, we analyze the correlation between layer importance  
471 and assigned rank. The strong Spearman correlation confirms that dynamic rank assignment aligns  
472 well with learned importance.

474 5 CONCLUSION AND FUTURE WORK  
475  
476

478 This study proposes PE-DyRA, an efficient dynamic rank adjustment method that improves parame-  
479 ter utilization. Experiments demonstrate that PE-DyRA outperforms existing fine-tuning approaches  
480 across diverse tasks, validating its effectiveness for large-scale models under limited resources.

481 However, there is still much future work to be done in this research. The size of the adjusted rank  
482 in the update is currently fixed as a parameter, and it can be extended to an adaptive method to  
483 determine the size of the adjusted rank in the update independently. In the future, we will explore  
484 more appropriate measures of importance, apply our method to larger models, and extend it to  
485 various tasks such as federation, multi-task, and domain adaptation. These promising challenges  
remain to be explored in future research efforts.

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648 A THE USE OF LARGE LANGUAGE MODELS  
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650 A large language model (LLM) was used to assist in refining the writing style and polishing the  
651 language of this paper. We gratefully acknowledge its contribution in improving the readability and  
652 clarity of the manuscript. All LLM-generated content was reviewed and corrected by the authors to  
653 maintain accuracy and preserve the original meaning.

654  
655 B PROOF OF PARETO-OPTIMAL PARAMETER EFFICIENCY  
656

657 We formalize the rank allocation problem under a fixed total rank budget  $R_{\text{total}}$  using a Lagrangian  
658 framework. Consider  $L$  LoRA layers, each assigned a rank  $r_l > 0$ , with layer importance scores  
659  $G_l > 0$ . We assume that the layer-wise contribution to the overall loss can be approximated as

$$660 \quad 661 \quad 662 \quad L(\{r_l\}) = \sum_{l=1}^L \frac{G_l}{\sqrt{r_l}}, \quad (9)$$

663 subject to the total rank budget constraint  
664

$$665 \quad 666 \quad 667 \quad \sum_{l=1}^L r_l = R_{\text{total}}. \quad (10)$$

668 Our goal is to minimize equation 9 subject to equation 10, yielding the most parameter-efficient rank  
669 allocation.

670 **Lagrangian formulation.** We construct the Lagrangian  
671

$$672 \quad 673 \quad 674 \quad \mathcal{J}(\{r_l\}, \lambda) = \sum_{l=1}^L G_l r_l^{-1/2} + \lambda \left( \sum_{l=1}^L r_l - R_{\text{total}} \right), \quad (11)$$

675 where  $\lambda$  is the Lagrange multiplier for the total rank constraint.

676 **Optimality condition.** Taking the derivative of equation 11 with respect to  $r_l$  and setting it to zero  
677 for optimality, we obtain

$$678 \quad 679 \quad \frac{\partial \mathcal{J}}{\partial r_l} = -\frac{1}{2} G_l r_l^{-3/2} + \lambda = 0. \quad (12)$$

680 Equation equation 12 implies that  
681

$$682 \quad G_l r_l^{-3/2} = 2\lambda, \quad \forall l. \quad (13)$$

683 Since the right-hand side is independent of  $l$ , we have  
684

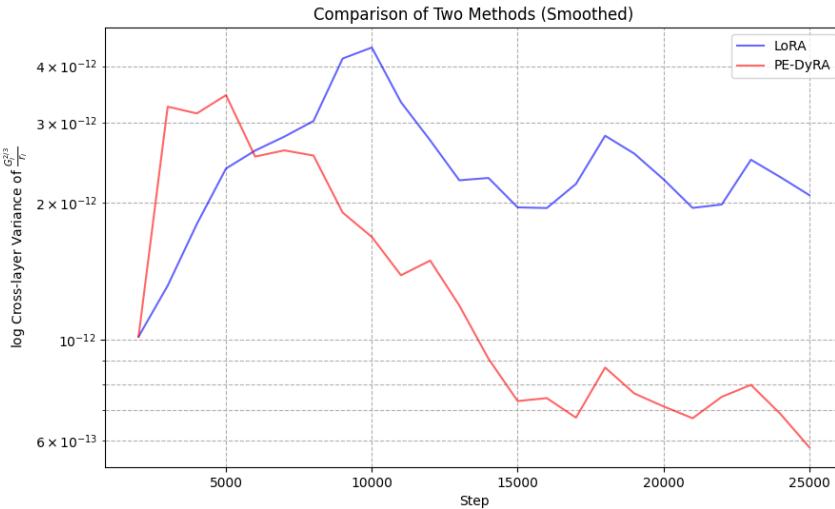
$$685 \quad r_l^{3/2} \propto G_l \quad \Rightarrow \quad r_l \propto G_l^{2/3}. \quad (14)$$

686 **Global optimality.** Each term  $G_l r_l^{-1/2}$  is strictly convex in  $r_l > 0$ , so the total objective equation 9  
687 is strictly convex, and the constraint equation 10 is linear. Therefore, any stationary point satisfying  
688 equation 13 is the unique global minimizer. Thus, this is the globally Pareto-optimal rank allocation.

689 **Implications.** Compared to any static allocation (uniform  $r_l = R_{\text{total}}/L$ ), the dynamic allocation  
690 achieves a strictly lower loss in equation 9 whenever the importance scores  $G_l$  are not all equal. This  
691 formally establishes that allocating ranks proportionally to  $G_l^{2/3}$  is Pareto-optimal under the given  
692 model.

693 For the SST-2 dataset, both LoRA(using SVD triples) and PE-DyRA methods are used to verify  
694 the above results, and the following graphs are plotted: The horizontal axis is the step during the  
695 training process; The vertical axis is the log variance of  $G_l^{2/3}/r_l$  across layers (which indicates how  
696 much the value deviates from the constant across layers).

697 As shown in Figure 5, under the dynamic strategy, the cross-layer variance of  $G_l^{2/3}/r_l$  gradually  
698 decreases during training, indicating that the model progressively approaches the Pareto optimal  
699 condition. Moreover, the variance under the dynamic strategy is consistently lower than that of the  
700 static LoRA strategy, suggesting that the dynamic rank adjustment achieves a more Pareto-efficient  
701 parameter allocation.

Figure 5: Comparison of Cross-layer variance of  $G_l^{2/3}/r_l$  during SST-2 training.

### C ADDITIONAL EXPERIMENTS ON SQuAD v2.0

To further illustrate the performance difference between LoRA and PE-DyRA, we provide a bar chart comparison of representative evaluation metrics, including HasAns F1, NoAns F1, Exact Match, and Overall F1 on SQuAD v2.0.

As shown in Figure 6, PE-DyRA matches LoRA on HasAns F1 while substantially improving NoAns F1, leading to higher Exact Match and Overall F1. This demonstrates that PE-DyRA maintains strong performance on answerable questions and enhances robustness on unanswerable ones.

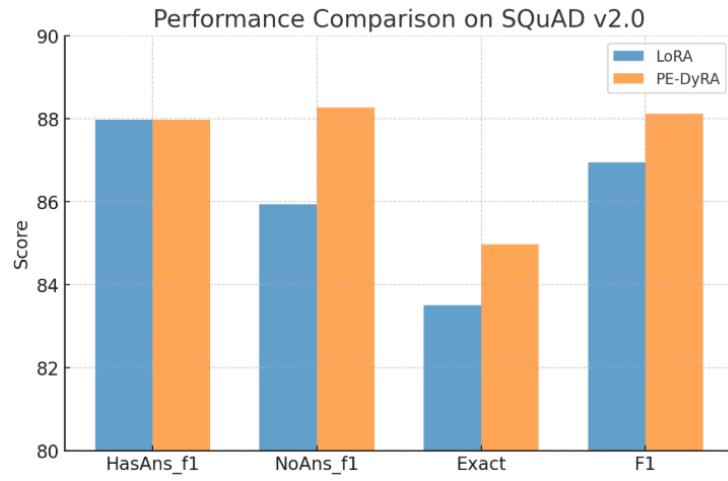


Figure 6: Comparison of evaluation metrics between LoRA and PE-DyRA on SQuAD v2.0.

### D THE RESULTING RANK DISTRIBUTION

Methods were applied to SST-2 using the DeBERTaV3-base model and the respective final rank distributions were saved.

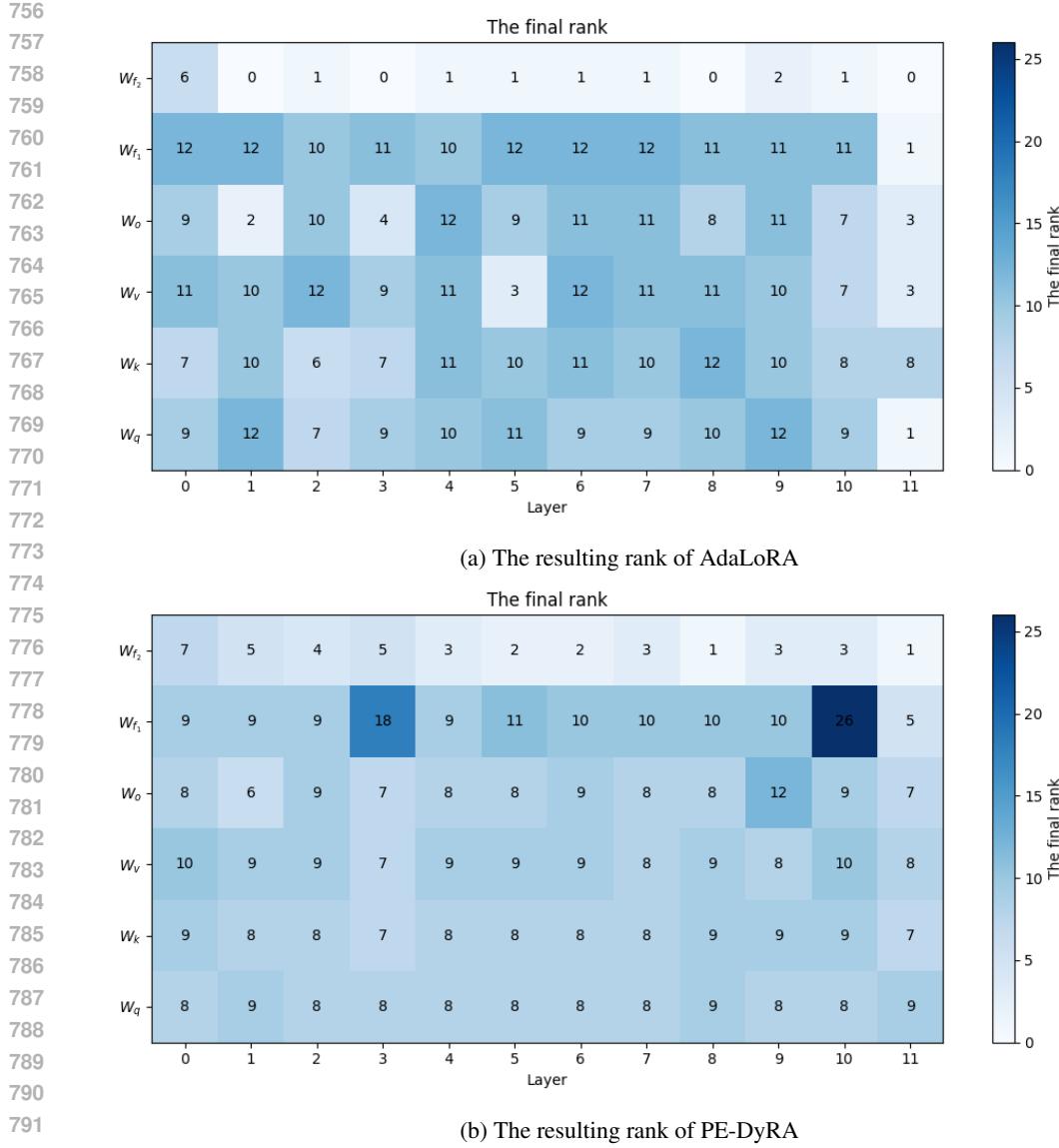


Figure 7: Comparative rank allocation patterns across model layers.

As shown in Figure 7, in the case of limited resources, the proposed method tends to produce relatively concentrated rank distributions. This may be one of the reasons why it is more effective in low-resource settings: by prioritizing assigning higher ranks to critical modules, methods are able to maintain adequate representation of important modules even with a limited parameter budget, thus achieving superior overall performance.

## E EXPERIMENTAL SETTINGS

### E.1 TRAINING DETAILS ON GLUE BENCHMARK

In the GLUE Benchmark, the model we used was DebertaV3-Base, with a rank size of 8. The specific details of the experimental hyperparameters are shown in the table 7.

Table 7: Hyper-parameter setup of PE-DyRA for GLUE benchmark.

Dataset	learning rate	batch size	# epochs	$\gamma$	$t_i$	$\Delta_T$	$t_f$	$k$
MNLI	$5 \times 10^{-4}$	32	7	0.1	3000	1000	65000	12
RTE	$1.2 \times 10^{-3}$	32	50	0.3	300	100	2600	12
QNLI	$9 \times 10^{-4}$	32	5	0.1	1000	500	10000	12
MRPC	$1 \times 10^{-3}$	32	30	0.1	600	150	1100	12
QQP	$6 \times 10^{-4}$	32	9	0.1	5000	1000	80000	12
SST-2	$8 \times 10^{-4}$	32	24	0.1	1000	1000	25000	12
CoLA	$1 \times 10^{-3}$	32	35	0.1	700	100	7000	12
STS-B	$2.2 \times 10^{-3}$	32	25	0.3	800	200	1500	12

Table 8: Hyper-parameter setup of PE-DyRA for mathematical reasoning and code generation.

Model	Dataset	learning rate	batchsize	# epochs	$t_i$	$\Delta_T$	$t_f$	$k$
LLaMA2-7B	MetaMath	$2 \times 10^{-4}$	16	5	2000	1000	11250	12
	Python	$2 \times 10^{-4}$	16	5	2000	1000	12765	12
LLaMA3-8B	MetaMath	$5 \times 10^{-5}$	16	5	2000	1000	11250	12
	Python	$1 \times 10^{-4}$	16	5	2000	1000	12765	12

## E.2 TRAINING DETAILS ON MATHEMATICAL REASONING AND CODE GENERATION

In the Mathematical Reasoning and Code Generation task, the LLaMA2-7B and LLaMA3-8b models were used, with an initial rank size of 4. The specific details of the experimental hyperparameters are shown in the table 8.

## E.3 TRAINING DETAILS ON SUMMARIZATION AND QA

Table 9: Hyper-parameter setup of PE-DyRA for summarization and QA.

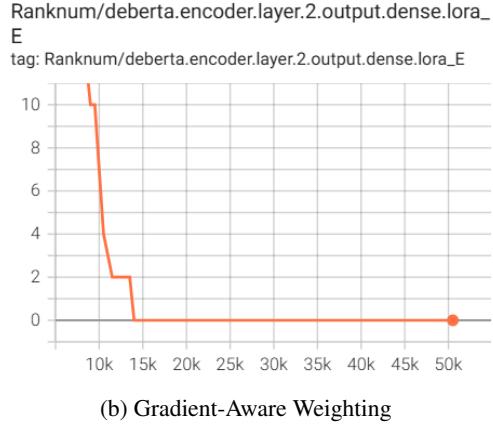
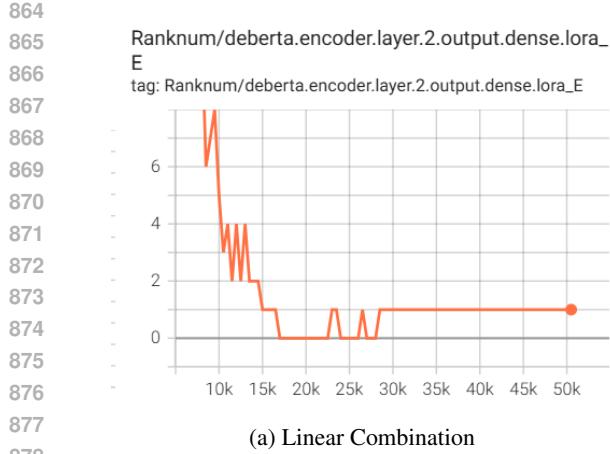
Dataset	learning rate	batch size	# epochs	$\gamma$	$t_i$	$\Delta_T$	$t_f$	$k$
XSum	$2 \times 10^{-4}$	24	25	0.1	6000	1500	180000	12
SQuAD v2.0	$1.2 \times 10^{-3}$	16	25	0.1	5000	1000	190000	12

For the summary and question-answering tasks, the XSum dataset uses the BART-large model, while the SQuAD v2.0 (Rajpurkar et al., 2018) uses the DebertaV3-Base model. The initial rank size used is 4. The specific details of the experimental hyperparameters are shown in the table 9.

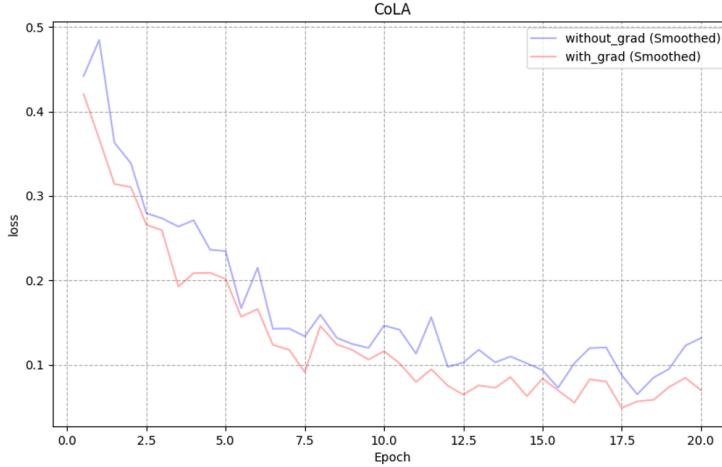
## F EMPIRICAL VALIDATION OF GRADIENT-AWARE WEIGHTING

To validate the proposed gradient-aware weighting scheme for triple importance scores, we track rank evolution during training using a temporary zero-masking strategy with initialized. As shown in Figure 8, with a simple linear combination of importance scores(Figure 8a), pruned ranks often reactivate, indicating unstable importance evaluation. In contrast, the gradient-aware scheme(Figure 8b) keeps pruned ranks consistently suppressed, better reflecting optimization dynamics and this is consistent with the effect we want.

As shown in Figure 9, we monitor the change in loss for both cases with and without using the gradient-aware weighting scheme. Through the loss change during training, it can be seen that using gradient information weighting can accelerate the optimization and make the optimization process more stable.



879 Figure 8: Comparison of rank evolution under two importance aggregation schemes: (a) linear  
880 combination leads to unstable pruning with ranks repeatedly reappearing, while (b) gradient-aware  
881 weighting yields stable pruning dynamics.



898 Figure 9: Training loss comparison with/without gradient weighting

## 901 G TIME–MEMORY–ACCURACY COMPARISON

903 Table 10: Comparison of training time, memory usage, and accuracy among different methods.

905  
906

Dataset	Method	#Params	Runtime/epoch(s)	Peak Memory $\Delta$	Acc (%)
SST-2	LoRA	1.33M	220.64	4306MB	95.18
	AdaLoRA	1.99M	403.09	4321MB	95.53
	PE-DyRA	1.33M	341.22	4315MB	95.98
	LoRA	1.33M	31.40	11439MB	89.70
MRPC	AdaLoRA	1.99M	38.99	11461MB	90.93
	PE-DyRA	1.33M	37.23	11446MB	91.18
	LoRA	1.33M	21.65	11439MB	86.28
RTE	AdaLoRA	1.99M	26.65	11461MB	87.00
	PE-DyRA	1.33M	26.79	11446MB	88.09

916 As shown in Table 10, our proposed PE-DyRA achieves consistently higher accuracy than LoRA and  
917 AdaLoRA while maintaining comparable parameter scale and memory usage. Notably, PE-DyRA

918 substantially reduces runtime (e.g., 220.64s vs. 341.22s on SST-2), demonstrating the effectiveness  
 919 of dynamic rank adjustment.  
 920

## 922 H ORTHOGONALITY REGULARIZATION LOSS

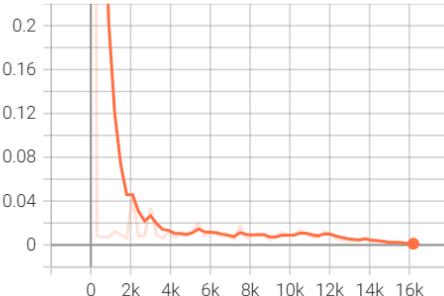
924  
 925 In the main text, we introduced the orthogonality regularization term, as defined in equation 2,  
 926 which encourages the low-rank factors  $\mathbf{A}$  and  $\mathbf{B}$  to remain close to an orthogonal basis, thereby  
 927 stabilizing training. The overall training objective can then be written as:  $\mathcal{L}_{\text{total}} = \mathcal{L}_{\text{train}} + \lambda \mathcal{R}_{\text{orth}}$ ,  
 928 where  $\mathcal{L}_{\text{train}}$  denotes the standard training loss, and  $\lambda$  is the regularization coefficient.  
 929

930 Orth\_regu\_loss/deberta.encoder.layer.0.intermediate.

931 dense.lora\_A

932 tag:

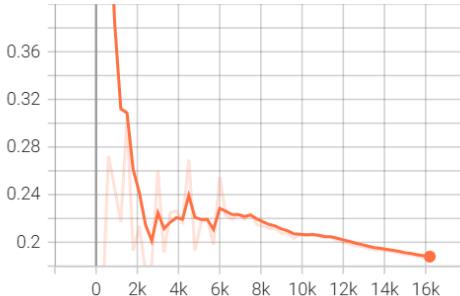
933 Orth\_regu\_loss/deberta.encoder.layer.0.intermediate.dense.lo  
 934 ra\_A



941 (a)  $\mathcal{R}_{\text{orth}}$  of LoRA-A in a specific layer

935 train/orth\_regu\_loss

936 tag: train/orth\_regu\_loss



942 (b) Overall training orthogonal loss

943 Figure 10: Dynamics of orthogonal regularization during training.

948 Figure 10 shows that the orthogonal loss decreases rapidly within each layer early in training and  
 949 then stabilizes, indicating effective local enforcement of orthogonality. Globally, despite layer-wise  
 950 fluctuations, the model consistently maintains orthogonality throughout training, demonstrating that  
 951 the regularization stabilizes both local representations and overall low-rank adaptation.

## 953 I ADDITIONAL FIGURES ALGORITHMS AND TABLES

### 956 I.1 FIGURES

958 Figure 11 is mentioned in Section 3.2.1.

### 961 I.2 TABLES

963 Table 11: DeBERTa-v3-base NLU benchmark results.

966 Method	967 QNLI	968 MRPC	969 QQP	969 STS-B	969 MNLI	969 SST-2	969 CoLA	969 RTE	969 Avg
PiSSA	94.07	90.20	91.92	91.54	<b>90.30</b>	95.53	71.41	<b>88.09</b>	89.13
PE-DyRA+PiSSA	<b>94.36</b>	<b>90.44</b>	<b>92.25</b>	<b>91.81</b>	90.22	<b>95.98</b>	<b>72.28</b>	87.00	<b>89.29</b>

970 Table 11 and Table 12 reports the detailed results corresponding to Section 4.4.

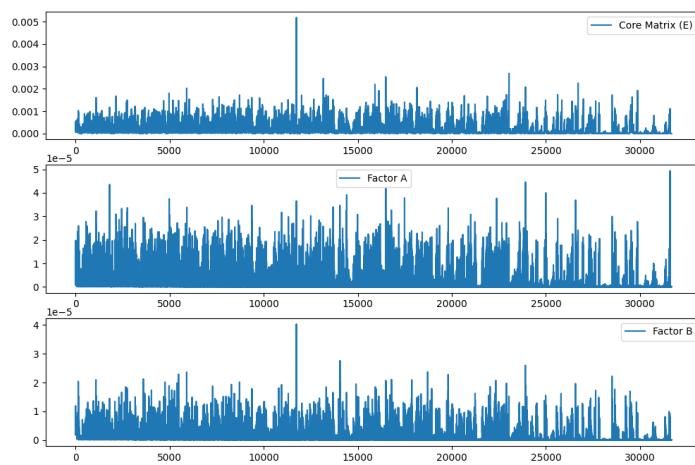


Figure 11: The gradient changes of the core matrix and factor matrix during the training process.

Table 12: LLaMA models code generation results.

Model	Method	Performance	
		MBPP	MBPP+
LLaMA2-7B	DoRA	38.4	28.3
	PE-DyRA+DoRA	<b>39.7</b>	<b>31.2</b>
	QLoRA	32.8	27.0
	PE-DyRA+QLoRA	<b>34.7</b>	27.0
LLaMA3-8B	DoRA	72.0	61.4
	PE-DyRA+DoRA	<b>73.0</b>	<b>63.0</b>
	QLoRA	70.6	60.6
	PE-DyRA+QLoRA	<b>74.3</b>	<b>63.8</b>

Table 13: Performance under different rank budgets.

Dataset	Method	rank=4	rank=8	rank=16	rank=32
CoLA	LoRA	68.57	69.33	71.03	69.92
	PE-DyRA	<b>71.43</b>	<b>71.43</b>	<b>71.80</b>	<b>70.85</b>
STS-B	LoRA	91.5	91.66	91.62	91.52
	PE-DyRA	<b>91.83</b>	<b>91.98</b>	<b>91.81</b>	<b>91.98</b>
MRPC	LoRA	90.44	89.70	89.22	90.2
	PE-DyRA	<b>91.18</b>	<b>91.18</b>	<b>90.2</b>	<b>90.44</b>

Table 13 reports the detailed results corresponding to Section 4.5.4.

Table 14 reports the detailed results corresponding to Section 4.5.5.

### I.3 THE ALGORITHM FOR COMPUTING IMPORTANCE SCORE AND BIDIRECTIONAL RANK ADJUSTMENT STRATEGY

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Table 14: Performance comparison with different rank adjustment sizes.

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**Algorithm 1** Computation of Overall Triple Importance Score

1037

**Require:** Parameters  $\Theta = \{A, E, B\}$ , input activations  $X$ , loss  $L$ 

1039

**Ensure:** Overall importance score  $S$ 

1040

**1: Step 1: Gradient-based triple importance**

1041

2: Compute component-level scores  $S_A^{\text{grad}}, S_E^{\text{grad}}, S_B^{\text{grad}}$  using  $\nabla L$ 

1042

3: **for all**  $K \in \{A, E, B\}$  **do**

1043

4: Compute sensitivity score:  $S_K^{\text{grad}} \leftarrow f_{\text{grad}}(K, \nabla_K L)$ 

1044

5: **end for**

1045

6: Fuse scores with gradient-aware weights:

1046

$$S_{G_i}^{\text{grad}} \leftarrow \omega_A S_{A_i}^{\text{grad}} + \omega_E S_{E_i}^{\text{grad}} + \omega_B S_{B_i}^{\text{grad}}, \text{ where } \omega_K = \frac{\|\nabla_K L\|}{\sum_{H \in \{A, E, B\}} \|\nabla_H L\|}$$

1047

**7: Step 2: Input-based triple importance**

1048

8: Compute input-based scores  $S^{\text{inp}}$  from  $X$ 

1049

$$S_{G_i}^{\text{inp}} = |e_i| \cdot \sum_{k=1}^{d_1} S_{ki} \cdot \|\mathbf{B}_i\|_2, \quad i = 1, \dots, r,$$

1050

**9: Step 3: Final aggregation**

1051

10: Compute overall score:

1052

$$S_{G_i} = \alpha \cdot S_{G_i}^{\text{grad}} + (1 - \alpha) \cdot S_{G_i}^{\text{inp}}, \text{ where } \alpha \text{ is appropriately chosen within } [0.0, 1.0].$$

1053

11: **return**  $S$ 

1054

1055

1056

**Algorithm 2** Bidirectional Rank Adjustment Strategy

1057

1058

1: **Input:** LoRA layers with rank-level triples  $\{G_i = (A_i, E_i, B_i)\}$ , total rank  $r$ , pruning size  $k$ 

1059

2: **Output:** Updated low-rank matrix  $\Delta W_{\text{adjusted}}$ 

1060

3:

1061

**4: Step 1: Compute importance scores**

1062

5: Compute rank-level importance scores  $S(G_i)$  for all triples  $G_i$ 

1063

6: (computation procedure detailed in Algorithm 1).

1064

7:

1065

**8: Step 2: Pruning Phase**

1066

9: Select the  $k$  triples with the lowest importance scores:

1067

$$\mathcal{P} = \operatorname{argmin}_{\mathcal{S}, |\mathcal{S}|=k} \sum_{G \in \mathcal{S}} S(G)$$

1068

11: Retain the remaining triples:

1069

$$\Delta W_{\text{pruned}} = \sum_{i \in \mathcal{K}} r_i, \quad \mathcal{K} = \{i \mid i \notin \mathcal{P}\}$$

13:

1070

**14: Step 3: Expansion Phase**

1071

15: For each layer  $\ell$ , compute layer-level importance score:

1072

$$S_{\text{layer}}^{(\ell)} = \frac{1}{r_\ell} \sum_{i=1}^{r_\ell} S(G_i)$$

1073

17: Select top- $k$  layers for expansion:

1074

$$\mathcal{E} = \operatorname{argmax}_{\mathcal{S}, |\mathcal{S}|=k} \sum_{\ell \in \mathcal{S}} S_{\text{layer}}^{(\ell)}$$

1075

19: Expand ranks on selected layers:

1076

$$\Delta W_{\text{adjusted}} = \Delta W_{\text{pruned}} + \sum_{j \in \mathcal{E}} r_j^{\text{new}}$$

1077

21:

1078

22: **return**  $\Delta W_{\text{adjusted}}$ 

1079