FAIRNESS-AWARE GRAPH LEARNING: A BENCHMARK

Anonymous authors

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Abstract

Fairness-aware graph learning has gained increasing attention in recent years. Nevertheless, there lacks a comprehensive benchmark to evaluate and compare different fairness-aware graph learning methods, which blocks practitioners from choosing appropriate ones for broader real-world applications. In this paper, we present an extensive benchmark on ten representative fairness-aware graph learning methods. Specifically, we design a systematic evaluation protocol and conduct experiments on seven real-world datasets to evaluate these methods from multiple perspectives, including group fairness, individual fairness, the balance between different fairness criteria, and computational efficiency. Our in-depth analysis reveals key insights into the strengths and limitations of existing methods. Additionally, we provide practical guidance for applying fairness-aware graph learning methods in applications. To the best of our knowledge, this work serves as an initial step towards comprehensively understanding representative fairnessaware graph learning methods to facilitate future advancements in this area.

1 INTRODUCTION

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Graph-structured data has become ubiquitous across a plethora of real-world applications (Hu 027 et al., 2020; Ying et al., 2019; Dong et al., 2023a; Narayanan et al., 2017), such as social network 028 analysis (Cho et al., 2011; Leskovec et al., 2010; Leskovec & Mcauley, 2012), biological network 029 modeling (Zitnik et al., 2018; Pavlopoulos et al., 2011; Zitnik & Leskovec, 2017), and traffic pattern prediction (Yuan & Li, 2021; Atluri et al., 2018; Derrow-Pinion et al., 2021). To gain 031 a deeper understanding of graph-structured data, graph learning methods, such as Graph Neural Networks (GNNs), are emerging as widely adopted and versatile methods to handle predictive tasks 033 on graphs (Wu et al., 2020; Zhou et al., 2020; Wu et al., 2022; You et al., 2019). However, as we aim 034 for improving utility (e.g., accuracy in node classification tasks), existing graph learning methods have also been found to constantly exhibit algorithmic bias in recent studies, which has raised significant societal concern and attracted attention from both industry and academia (Dong et al., 2023b; Choudhary et al., 2022; Wu et al., 2021). For example, financial agencies have been relying 037 on GNNs to perform decision making in financial services (Wang et al., 2021; Song et al., 2023), e.g., determining whether each loan application should be approved or not based on transaction networks of bank clients. Nevertheless, the outcomes have been found to exhibit bias, such as racial disparities 040 in the rejection rate (Song et al., 2023). As a consequence, addressing the fairness concerns for graph 041 learning methods has become an urgent need (Dong et al.) [2023b; Dai et al.) [2022), especially under 042 high-stake real-world applications such as financial lending (Song et al., 2023; Li et al., 2020) and 043 healthcare decision making (Dai et al.) 2022; Anderson & Visweswaran, 2024).

044 In recent years, various techniques, such as adversarial training (Dai & Wang, 2021; Jiang et al.) 2024; Ling et al., 2023; Cong et al., 2023), optimization regularization (Agarwal et al., 2021; Jiang 046 et al., 2022; Rahmattalabi et al., 2019), and graph structure learning (Dong et al., 2022; Zhang et al., 047 2024; Zhang & Ramesh, 2020), have been adopted to address the fairness concerns in graph learning 048 methods. Nevertheless, despite these existing efforts, we have not yet seen extensive deployment of these fairness-aware graph learning methods. A primary obstacle lies in the lack of a comprehensive comparison across existing fairness-aware graph learning methods, which makes it difficult for 051 practitioners to choose the appropriate ones to use. In fact, a comprehensive comparison of existing fairness-aware graph learning methods not only tells the best-in-class methods under different settings 052 (e.g., different evaluation metrics and datasets from different domains) but also provides a guideline for practitioners to understand the strengths and limitations of different methods in multiple aspects, such as utility, fairness, and efficiency. As such, comprehensively comparing the performances
 between different graph learning methods becomes an urgent need to facilitate a broader application
 of fairness-aware graph learning methods.

Multiple existing works have explored to compare different fairness-aware graph learning methods. For example, Chen et al. (Chen et al., 2024) proposed to categorize and compare existing fairnessaware GNNs by their input, main techniques, and tasks. However, the overwhelming focus on GNNs 060 narrows down the scope of comparison. Another study from Laclau et al. (Choudhary et al., 2022) 061 delivers a more comprehensive comparison of graph learning methods. However, it did not involve 062 any quantitative performance comparison, which thus jeopardizes its practical value for practitioners. 063 In fact, it is challenging to provide a quantitative performance comparison on fairness-aware graph 064 learning methods due to their inconsistencies in terms of the studied fairness notions, experimental settings, and learning tasks. Therefore, lacking quantitative performance comparison becomes a 065 common flaw for most of the related studies (Dai et al., 2022). More recently, Qian et al. (Qian 066 et al., 2024) took an early step to present a quantitative performance benchmark in the area of graph 067 learning. However, they only focus on the comparison of two fairness-aware GNNs, which thus 068 blocks a broader understanding in a broader area of graph learning. Therefore, comprehensive 069 performance comparison of fairness-aware graph learning methods remains underexplored.

071 In this paper, we take an initial step to comprehensively evaluate the performance differences between the most representative fairness-aware graph learning methods. Specifically, we first design a 072 systematic evaluation protocol, which helps ensure consistent settings for the evaluation of different 073 graph learning methods. Second, we collect ten of the most representative graph learning methods 074 and present a comprehensive benchmark on seven real-world graph datasets (including five commonly 075 used and two newly constructed ones) from different perspectives, such as different datasets, fairness 076 notions, and evaluation metrics. Finally, we perform an in-depth analysis based on the experimental 077 results and reveal key insights into the strengths and limitations associated with these fairness-aware 078 graph learning methods. We also provide guidance for practitioners to choose appropriate ones to 079 use, which further facilitates the practical significance of this study.

- 080081 The main contributions of this paper are summarized as follows:
 - **Experimental Protocol Design.** We design a systematic evaluation protocol, which enables the comparison between different fairness-aware graph learning methods under consistent settings. To the best of our knowledge, our work serves as the first step towards comprehensively evaluating the performance of fairness-aware graph learning methods.
 - **Comprehensive Benchmark.** We conduct extensive experiments on seven real-world attributed graph datasets (including five commonly used and two newly constructed ones) and present a comprehensive benchmark over ten fairness-aware graph learning methods, which reveals key insights in understanding their strengths and limitations.
 - Multi-Perspective Analysis & Guidance. We present four significant research questions and perform in-depth analysis from different perspectives based on the benchmarking results. Meanwhile, we also introduce a guide for practitioners to help them choose appropriate methods in real-world applications.

2 PRELIMINARIES

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Background. We use $\mathcal{G} = \{\mathcal{V}, \mathcal{E}\}$ to denote a graph, where \mathcal{V} denotes the set of n nodes and \mathcal{E} 098 represents the set of edges. Here, each node is equipped with an attribute vector, which makes the 099 graph an attributed graph. In this paper, we focus on node classification, which is among the most widely studied graph learning tasks. Typically, in node classification, a graph machine learning model 100 can be represented as a function $f: (\mathcal{V}, \mathcal{E}) \to \hat{Y} \in \mathbb{R}^{n \times c}$, which maps each node $v \in \mathcal{V}$ into a 101 c-dimensional matrix \hat{Y} . Each row in \hat{Y} (denoted as \hat{y}_i for the *i*-th row) is a vector indicating the 102 103 predicted probability distribution across different classes, and c denotes the total number of classes. Meanwhile, the matrix of ground truth labels $Y \in \{0,1\}^{n \times c}$ is provided as the supervision for 104 105 optimization. The primary goal of fairness-aware graph machine learning is to ensure Y bears high levels of utility and fairness at the same time. Without loss of generality, we conduct benchmarking 106 experiments on the popular graph learning task of binary node classification (i.e., c = 2), which 107 aligns with most works in this area (Dong et al., 2023b; Dai & Wang, 2021; Kose & Shen, 2022).

Figure 1: A timeline of the representative fairness-aware graph learning methods. 120 121 Timeline of the Collected Graph Learning Models. To provide a global understanding of fairness-122 aware graph learning methods, we present a high-level overview of the timeline of the representative explorations, which is shown in Figure 1. Specifically, we group these works by the fairness notions 123 they focus on, including group fairness and individual fairness (Dong et al., 2023b). Group fairness 124 emphasizes that the graph learning methods should not yield discriminatory predictions against any 125 demographic subgroups (Dong et al., 2023b; Hardt et al., 2016), where the subgroups are determined 126 by certain categorical sensitive attributes such as gender or race (Mehrabi et al., 2021; Dwork et al., 127 2012). On the other hand, individual fairness argues that similar individuals should be treated 128 similarly (Dwork et al., 2012), i.e., the outcomes corresponding to a pair of individuals in the output 129 space should be close if they are close in the input space (Dong et al., 2023b; Kang et al., 2020b).

Notions and Metrics for Group Fairness. Here, we present the representative notions and metrics under Group Fairness. (1) Statistical Parity. Statistical parity requires that the probability of yielding positive predictions should be the same across different demographic subgroups (Dong et al., 2023b) 133 Dwork et al., [2012]. Here, the rationale is that positive predictions correspond to beneficial decisions 134 in a plethora of real-world applications (Hardt et al., 2016). A commonly used metric to quantify to 135 what extent statistical parity is violated is Δ_{SP} , which is given by 136

$$\Delta_{SP} = |P(\hat{Y} = 1 \mid S = 0) - P(\hat{Y} = 1 \mid S = 1)|, \tag{1}$$

138 where $Y, S \in \{0, 1\}$ denote random variables for the predicted label and the sensitive attribute of 139 any given individual, respectively. (2) Equal Opportunity. Equal opportunity requires that the 140 probability of yielding positive predictions should be the same for those who have a positive ground 141 truth across different demographic subgroups (Hardt et al., 2016). Different from statistical parity, 142 equal opportunity aims to protect individuals' advantaged qualifications against bias arising from 143 subgroup membership (Hardt et al.) 2016). $\Delta_{\rm EO}$ is commonly used to measure to what extent equal opportunity is violated, which is given by

$$\Delta_{EO} = |P(\hat{Y} = 1 | Y = 1, S = 0) - P(\hat{Y} = 1 | Y = 1, S = 1)|,$$
(2)

where Y is the random variable of the ground truth for any given individual. (3) Utility Difference-147 Based Fairness. Its rationale is to reveal the largest utility gap between different demographic 148 subgroups (Ali et al., 2021; Stoica et al., 2020; Rahmattalabi et al., 2021). A commonly used metric 149 is the maximum utility difference across all pairs of demographic subgroups (denoted as Δ_{Utility}). 150 Here, utility refers to the performance in downstream node classification tasks (such as AUC-ROC 151 score), and Δ_{Utility} serves as a fairness metric characterizing such performance gap between different 152 demographic subgroups. 153

Notions and Metrics for Individual Fairness. We now present the representative notions and 154 metrics under Individual Fairness. Different from group fairness, individual fairness does not rely 155 on sensitive attributes. Instead, the rationale of individual fairness is to treat similar individuals 156 similarly (Dwork et al., 2012). We introduce three notions and their corresponding metrics below. (1) 157 Lipschitz-Based Individual Fairness. This notion argues that the (scaled) distance between individuals 158 in the output space should be smaller or equal to their distance in the input space (Kang et al., 2020b). 159 The level of the exhibited bias under this notion is measured by 160

$$B_{\text{Lipschitz}} = \sum_{i} \sum_{j, j \neq i} \left\| \hat{\boldsymbol{y}}_{i} - \hat{\boldsymbol{y}}_{j} \right\|_{F} \cdot \boldsymbol{S}_{ij}, \tag{3}$$



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Table 1: Statistics of the collected real-world graph datasets.

Dataset	Pokec-z	Pokec-n	German Credit	Credit Defaulter	Recidivism	AMiner-S	AMiner-L
#Nodes	67,796	66,569	1,000	30,000	18,876	39,424	129,726
#Edges	882,765	729,129	24,970	200,526	403,977	52,460	591,039
#Attributes	276	265	27	13	18	5,694	5,694

where the S is an oracle similarity matrix that describes the similarity between nodes in the input 169 space. (2) Ranking-Based Individual Fairness. This notion requires that the rankings of the similarity 170 between each individual and all other individuals should be the same between the input and output 171 space (Dong et al.) 2021b). The average top-k similarity between the two ranking lists in the input 172 and output spaces over all individuals is adopted as the fairness metric, where NDCG@k is a 173 common ranking similarity metric, which we denote as Branking. (3) Ratio-Based Individual Fairness. 174 This notion requires that different demographic subgroups should bear similar levels of individual 175 fairness (Song et al., 2022). Group Disparity of Individual Fairness (GDIF) is introduced as the metric, which is given by 176

$$GDIF = \sum_{i,j}^{1 \le i < j \le m} \max\left(\frac{B_{\text{Lipschitz}}^{(i)}}{B_{\text{Lipschitz}}^{(j)}}, \frac{B_{\text{Lipschitz}}^{(j)}}{B_{\text{Lipschitz}}^{(i)}}\right), \tag{4}$$

where $B_{\text{Lipschitz}}^{(i)}$ and $B_{\text{Lipschitz}}^{(j)}$ are the subgroup-level $B_{\text{Lipschitz}}$ from two demographic subgroups i and j; m is the total number of subgroups.

3 **BENCHMARK DESIGN**

In this section, we introduce the design of our benchmark. Specifically, we first present the experimental settings and implementation details of our benchmark. Then we introduce four main research questions we aim to explore in this paper. We note that our experiments are conducted based on node classification, since most commonly used fairness metrics are defined for classification.

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3.1 EXPERIMENTAL SETTINGS AND IMPLEMENTATIONS

Here we introduce the experimental settings, including benchmark datasets, collected fairness-aware 193 graph learning methods, and the implementation details regarding this newly introduced benchmark. 194

195 **Benchmark Datasets.** We collected seven real-world attributed graph datasets of different scales in this benchmark paper, including five existing commonly used ones and two newly constructed ones. 196 These datasets include (1) Pokec-z (Takac & Zabovsky 2012): social network data; (2) Pokec-n (Takac 197 & Zabovsky 2012): social network data; (3) German Credit (Markelle Kelly): a graph based on financial credit; (4) Credit Defaulter (Yeh & Lien 2009): a graph over financial agency clients; (5) 199 *Recidivism* (Jordan & Freiburger 2015): a graph over defendants; (6) AMiner-S (newly constructed): 200 a co-authorship graph over researchers; (5) AMiner-L (newly constructed): a co-authorship graph 201 over researchers. We present the statistics of the collected attributed graph datasets above in Table 1. 202 and a more detailed dataset introduction is given in Appendix. 203

Fairness-Aware Graph Learning Models. We collect ten of the most representative graph learning 204 methods for comparison. We provide a brief introduction for each of them below, where the fairness 205 notion they focus on is marked out in brackets. (1) FairWalk (group fairness). FairWalk (Rahman 206 et al., (2019) is a fairness-aware graph learning method based on DeepWalk, where it achieves bias 207 mitigation by balancing the transition probabilities between different demographic subgroups. (2) 208 CrossWalk (group fairness). CrossWalk (Khajehnejad et al., 2022) is a fairness-aware graph learning 209 method. Specifically, it is developed based on DeepWalk, where such an algorithm achieves bias 210 mitigation by steering random walks across demographic subgroup boundaries for representation 211 learning. (3) FairGNN (group fairness). FairGNN (Dai & Wang, 2021) is a fairness-aware graph 212 learning method base on GNNs, where it achieves bias mitigation by incorporating an adversary 213 to wipe out the information of sensitive attributes in the learned node representations. (4) NIFTY (group fairness). NIFTY (Agarwal et al., 2021) is a fairness-aware graph learning method based on 214 GNNs, where it achieves bias mitigation with an additional optimization regularization term based on 215 counterfactual sensitive attribute perturbation. (5) EDITS (group fairness). EDITS (Dong et al., 2022)

216 is a fairness-aware graph learning framework designed in a pre-processing manner, where it achieves 217 bias mitigation by minimizing the distribution difference between nodes from different demographic 218 subgroups in the node attribute space. (6) FairEdit (group fairness). FairEdit (Loveland et al., 2022) 219 is a fairness-aware graph learning method based on GNNs, where it optimizes the performance on 220 fairness by modifying the graph topology. (7) FairVGNN (group fairness). FairVGNN (Wang et al., 2022) is a fairness-aware graph learning method based on GNNs, where it achieves bias mitigation by identifying and masking sensitive-correlated attribute dimensions. (8) InFoRM (individual fairness). 222 InFoRM (Kang et al., 2020b) is a fairness-aware graph learning method that can be adapted to different 223 models, where it achieves bias mitigation by incorporating a fairness-aware optimization objective 224 based on the Lipschitz condition. (9) REDRESS (individual fairness). REDRESS (Dong et al., 225 2021b) is a fairness-aware graph learning method based on GNNs, where it proposes a fairness-aware 226 optimization objective to improve performance on ranking-based fairness. (10) GUIDE (individual 227 fairness). GUIDE (Song et al., 2022) is a fairness-aware graph learning method based on GNNs, 228 where it uses a fairness-aware optimization objective to enforce similar levels of Lipschitz-based 229 individual fairness across different demographic subgroups. 230

Implementation Details. All benchmarking experiments are implemented with PyTorch and performed on an Nvidia A100 GPU. We obtain the best hyper-parameters by selecting the lowest loss values on the validation node set via grid search, and all results are reported with standard deviation from three different runs. For all GNNs, we adopt the most widely used GCN unless otherwise specified. Comprehensive experimental details, including open-source URLs of the algorithms we have used for reproducibility purposes, are introduced in Appendix.

- 237 3.2 RESEARCH QUESTIONS238
- RQ 1: How well can those representative methods perform under group fairness?

Significance & Experimental Design. Understanding the performance of graph learning methods in terms of group fairness is crucial since it addresses the bias that may arise in applications due to sensitive attributes such as race, gender, and age. We evaluate the collected methods focusing on group fairness on both utility and fairness. Here we adopt the AUC-ROC score as an exemplary metric for utility, while Δ_{SP} , Δ_{EO} , and $\Delta_{Utility}$ are utilized as the metrics for fairness (as in Section 2).

RQ 2: How well can those representative methods perform under individual fairness?

Significance & Experimental Design. Evaluating individual fairness helps to identify and reduce discriminatory practices at the individual level, which is more granular compared with group fairness. To answer this question, we evaluate the collected methods focusing on individual fairness from the perspective of both utility and fairness. Here, we adopt the AUC-ROC score for utility evaluation, while $B_{\text{Lipschitz}}$, NDCG@k, and GDIF are adopted as the metrics for fairness (as in Section 2).

252 RQ 3: How well can existing methods balance different fairness criteria?

Significance & Experimental Design. Understanding how graph learning methods balance different fairness criteria is vital when multiple criteria need to be considered simultaneously (Zhan et al., 2024; Sirohi et al., 2024; Dai et al., 2022). Considering the scarcity of methods under individual fairness, we focus on group fairness for this research question. Specifically, we measure the average ranking corresponding to these methods on Δ_{SP} , Δ_{EO} , and $\Delta_{Utility}$, where a lower average ranking indicates better performance.

RQ 4: How well can those representative methods perform in terms of efficiency?

Significance & Experimental Design. Ensuring that fairness-aware graph learning methods are computationally feasible is essential for their usability in real-world applications. To answer this question, we evaluate the collected methods by their utility vs. running time on each dataset. Better utility with less running time indicates better efficiency.

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- 4 Empirical Investigation
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- In this section, we present benchmarking results and in-depth analysis to answer the four research questions in Section 3.2 Specifically, we first assess group fairness (RQ1) using metrics like statistical parity and equal opportunity, followed by individual fairness (RQ2), which ensures similar treatment

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Metrics	Models	Pokec-z	Pokec-n	German Credit	Credit Defaulter	Recidivism	AMiner-S	AMiner-L
	DeepWalk	66.50 (± 1.34)	$61.85_{(\pm 1.06)}$	56.90 (± 1.75)	53.61 (± 0.66)	$87.18_{(\pm 1.34)}$	$73.58 \scriptscriptstyle (\pm 0.43)$	82.68 (± 3.28)
	FairWalk	$64.92 \scriptscriptstyle (\pm 0.43)$	$61.52 \scriptscriptstyle \ (\pm \ 0.34)$	$54.05_{(\pm 0.83)}$	55.51 (± 0.29)	$72.09 \scriptscriptstyle \ (\pm \ 0.11)$	$65.35 \scriptscriptstyle \ (\pm 0.54)$	$\underline{88.72} \ (\pm \ 0.08)$
	CrossWalk	$58.99 \scriptstyle (\pm 0.27)$	$62.98 \scriptscriptstyle (\pm 0.27)$	$51.42 \ (\pm \ 0.43)$	$54.50 \scriptscriptstyle \ (\pm 0.42)$	$82.89 \scriptscriptstyle (\pm 0.11)$	$64.44 \ (\pm \ 0.52)$	$89.67 (\pm 0.04)$
	GNN	$64.16 \ (\pm \ 0.62)$	$67.05_{(\pm 1.14)}$	67.36 (± 3.59)	$\underline{62.62} \ (\pm \ 0.51)$	$84.60 \ (\pm \ 2.10)$	$\underline{81.95} \ (\pm 1.46)$	$86.82 \scriptscriptstyle (\pm 0.11)$
AUC-ROC	FairGNN	$\underline{69.47} \ (\pm \ 1.04)$	$\underline{68.51} \ (\pm \ 0.51)$	$52.91 (\pm 2.15)$	56.73 (± 3.16)	$92.87 \ (\pm \ 2.42)$	$86.23 \ (\pm \ 0.14)$	OOM
	NIFTY	$62.58 \scriptscriptstyle (\pm 0.14)$	$66.78 \scriptscriptstyle (\pm 0.82)$	$62.94 (\pm 5.78)$	$61.85 (\pm 0.70)$	$85.58 \scriptscriptstyle \ (\pm 0.83)$	$79.28 \ (\pm \ 0.15)$	$86.62 \scriptscriptstyle (\pm 0.69)$
	EDITS	OOM	OOM	$60.02 (\pm 1.10)$	$61.14 \ (\pm \ 0.36)$	$\underline{92.34}~(\pm 0.31)$	OOM	OOM
	FairEdit	OOM	OOM	$56.30 \ (\pm \ 2.33)$	$62.50 \ (\pm \ 0.61)$	$81.97_{\ (\pm\ 0.48)}$	OOM	OOM
	FairVGNN	$71.19 \ (\pm \ 0.94)$	$70.14 \ (\pm \ 0.55)$	65.48 (± 3.46)	$68.81 (\pm 0.81)$	$84.74_{\ (\pm\ 2.70)}$	OOM	OOM
	DeepWalk	5.49 (± 1.07)	$5.90 \ (\pm \ 0.88)$	10.4 (± 1.01)	6.69 (± 0.31)	$6.50 \scriptscriptstyle (\pm 0.18)$	$6.75_{(\pm 0.29)}$	$6.41 (\pm 0.46)$
	FairWalk	0.60 (± 1.89)	0.29 (± 2.12)	3.36 (± 1.01)	$6.20 (\pm 0.32)$	$4.67 (\pm 0.33)$	3.06 (± 0.32)	$\textbf{4.28}~(\pm~0.17)$
	CrossWalk	1.75 (± 1.17)	$0.21 (\pm 1.63)$	$0.35_{(\pm 1.75)}$	6.35 (± 0.51)	$\underline{5.14}~(\pm~0.21)$	$3.59 \scriptscriptstyle (\pm 0.43)$	$\underline{5.60}~(\pm 0.42)$
	GNN	$10.4 (\pm 1.46)$	$14.7 \scriptstyle~(\pm 0.40)$	$32.4 (\pm 1.93)$	$20.6 (\pm 4.34)$	$8.54 \scriptscriptstyle (\pm 0.10)$	$7.28 \scriptscriptstyle \ (\pm \ 0.31)$	$6.75 \ (\pm \ 0.00)$
$\Delta_{ m SP}$	FairGNN	$2.06 (\pm 1.82)$	$8.11 (\pm 1.16)$	$14.2 \ (\pm \ 0.83)$	$\underline{2.51} (\pm 5.61)$	$7.48 \scriptscriptstyle (\pm 0.30)$	$5.36 \ (\pm \ 0.27)$	OOM
	NIFTY	$2.48 (\pm 0.47)$	$2.42 \ (\pm \ 0.84)$	$\underline{0.26}$ (± 0.41)	12.5 (± 3.64)	$7.88 \scriptscriptstyle (\pm 0.43)$	$\underline{3.25} \ (\pm \ 0.52)$	$5.86 \ (\pm \ 0.44)$
	EDITS	OOM	OOM	0.18 (± 1.78)	$10.7 (\pm 0.66)$	$7.36 \ (\pm \ 0.05)$	OOM	OOM
	FairEdit	OOM	OOM	$3.15 (\pm 3.73)$	$1.95 (\pm 0.21)$	$7.39\scriptscriptstyle~(\pm 0.50)$	OOM	OOM
	FairVGNN	$6.33 \scriptstyle (\pm 1.90)$	$5.31 \scriptstyle ~(\pm 1.19)$	$3.13 (\pm 0.28)$	$9.93 \scriptscriptstyle (\pm 0.88)$	$6.54 \scriptscriptstyle (\pm 0.53)$	OOM	OOM

270 Table 2: Comparison of graph learning methods focusing on group fairness. Note that results include 271 AUC-ROC score and Δ_{SP} , and complete results are in Appendix. The best ones are in **bold**; the 272 second best ones are underlined; OOM denotes out-of-memory.

for similar individuals. We then analyze the trade-offs between different fairness criteria (RQ3) and evaluate the computational efficiency of these methods (RQ4). The findings provide valuable insights into the strengths and limitations of each method, guiding the selection of appropriate fairness-aware models for practical use. Due to space limit, we present a subset of the benchmarking results in this section, and the complete results are discussed in Appendix.

4.1 PERFORMANCE UNDER GROUP FAIRNESS (RQ1)

302 We first perform experiments to 303 answer RQ1. Specifically, we 304 present the quantitative results 305 corresponding to those graph 306 learning methods focusing on 307 group fairness in Table 2. Note that we present the results on 308 AUC-ROC score (utility) and 309 Δ_{SP} (fairness) as an example, 310 and the complete results are in 311 Appendix. Here DeepWalk and 312 GNN are added as baselines 313 for shallow embedding methods 314 and GNN-based methods, respec-315 tively. We observe that differ-316 ent methods yield different levels 317 of trade-offs between utility and



Figure 2: Average rankings on AUC-ROC score and Δ_{SP} across all datasets. Methods are ranked in ascending order by the summation of two rankings.

318 fairness. To better understand the strengths and limitations associated with each algorithm, we 319 calculate the average ranking of each method on datasets free from OOM. We show their average rankings (ordered by the summation of two average rankings) in Figure 2 320

321 Finding 1: Fairness-aware graph learning methods excel differently on group fairness. Ac-322 cording to Table 2 and Figure 2, we found that different fairness-aware graph learning meth-323 ods exhibit different types of proficiency between utility and fairness. Specifically, we have the following observations. First, top-ranked methods (those ranked at the left in Figure 2)

Figure 3: Pareto optimal frontier between AUC-ROC score and Δ_{EO} from FairGNN on Credit Default.

are all GNN-based ones. This verifies the natural advantage of GNNs in achieving both accurate and fair predictions owing to their superior fitting ability. Second, fairness-aware shallow embedding methods (i.e., CrossWalk and FairWalk) yield the topranked performances in terms of fairness. Considering that these shallow embedding methods do not take node attributes as input compared with those GNN-based ones, such an observation can be partially attributed to the absence of bias encoded in the node attributes. Third, neither DeepWalk nor GNN yields top-ranked performance under utility. This implies that improving fairness does not necessarily jeopardize utility. This may conflict with the common belief that achieving one necessarily means sacrifices the other, while it aligns with the observations of other representative works in this area (Dai & Wang, 2021; Dong et al., 2022). Additionally, to better characterize the trade-off between utility and

accuracy, we show an exemplary (estimated) Pareto optimal frontier between AUC-ROC score and Δ_{EO} during hyper-parameter search in Figure 3. We observe that such a frontier implicitly prevents a graph learning model from further improving the performance under both evaluation metrics.

4.2 PERFORMANCE UNDER INDIVIDUAL FAIRNESS (RQ2)

We then answer RQ2 by comparing the performance of graph machine learning methods focusing on individual fairness. Similar to RQ1, we will explore their performance on both utility and fairness. Specifically, we choose the AUC-ROC score as an exemplary metric for utility, and we adopt the three metrics for individual fairness presented in Section 2 to measure the level of individual fairness. Without loss of generality, we adopt a common setting of k = 10 for the ranking-based individual fairness metric NDCG@k (Dong et al.) 2021b). We present the experimental results in Table 3 and the complete results with supplementary discussion are given in Appendix.

354 Finding 2: Fairness-aware graph learning methods exhibit different levels of versatility on 355 individual fairness. According to Table 3, we have the following observations. First, in terms of 356 utility, we observe that improving individual fairness typically leads to stronger compromise on utility. 357 The vanilla GNN generally achieves the best utility across most datasets. The collected fairness-aware 358 graph learning methods generally sacrifice a certain level of utility in order to improve the level of 359 individual fairness. Second, in terms of fairness, we observe that these methods exhibit different levels of versatility. Specifically, InFoRM, REDRESS, and GUIDE yield the best performance on those 360 individual fairness goals they are equipped with by design, i.e., Lipschitz-based fairness (measured 361 with $B_{\text{Lipschitz}}$, ranking-based fairness (measured by NDCG@k), and ratio-based fairness (measured 362 by GDIF), respectively. However, GUIDE also delivers the second best $B_{\text{Lipschitz}}$ and NDCG@k on four out of the seven datasets at the same time, which makes it the most versatile method among 364 the studied three. This implies that compared with the other two methods, GUIDE contributes to a more general improvement in terms of the levels of individual fairness instead of only optimizing 366 one objective and sacrificing others. Such an advantage can be attributed to the compositional design 367 of its objective function, which consists of different fairness objectives (Song et al., 2022). Similar 368 versatility is also observed in InFoRM, which yields the second-best performance on GDIF in three 369 out of the seven datasets. Hence, we conclude that these methods exhibit different levels of versatility 370 under individual fairness.

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4.3 TRADE-OFF BETWEEN DIFFERENT FAIRNESS CRITERIA (RQ3)

We now answer RQ3 by comparing the performance of fairness-aware graph learning methods under different fairness metrics. Considering the scarcity of methods under individual fairness, here we focus on group fairness and discuss the results over individual fairness in Appendix. Specifically, for each of the three group fairness metrics given in Section 2, we calculate the average ranking of each method on those datasets free from OOM, and we present the comparison of their average rankings



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Metrics	Models	Pokec-z	Pokec-n	German Credit	Credit Defaulter	Recidivism	AMiner-S	AMiner-L
	GNN	$66.50 \scriptscriptstyle (\pm 0.53)$	$67.62_{(\pm 0.76)}$	$69.70_{(\pm 3.48)}$	$62.29 \scriptscriptstyle (\pm 4.85)$	$82.47 (\pm 1.41)$	$82.23 \scriptscriptstyle (\pm 0.56)$	$88.15 \ (\pm \ 0.11)$
AUC DOC	InFoRM	$60.53 \scriptscriptstyle (\pm 3.67)$	$64.12 \scriptscriptstyle (\pm 4.12)$	$63.61 \scriptscriptstyle (\pm 4.93)$	$62.72_{\ (\pm\ 5.87)}$	$\underline{79.66}_{(\pm \ 6.58)}$	$69.75_{\ (\pm \ 5.18)}$	$\underline{73.72}_{(\pm 7.97)}$
AUC-NOC	REDRESS	$62.31 \scriptscriptstyle \ (\pm \ 6.52)$	$\underline{64.70}_{(\pm4.88)}$	$63.79 \scriptscriptstyle (\pm 4.40)$	$\underline{64.39}~(\pm 5.25)$	$69.52 \scriptscriptstyle (\pm 5.58)$	OOM	OOM
	GUIDE	$\underline{63.55}_{(\pm 3.62)}$	$60.36\scriptscriptstyle~(\pm~4.43)$	$\underline{65.56}_{(\pm 4.18)}$	$64.64 \ (\pm 3.86)$	$75.09_{\ (\pm\ 5.41)}$	$\underline{73.34}_{(\pm4.28)}$	OOM
	GNN	$2.5e6_{(\pm\ 2e4)}$	$5.5e3 \scriptscriptstyle (\pm 3e3)$	$\underline{3.6e3}_{(\pm\ 2e3)}$	1.3e4 (± 7e3)	$1.2e7_{\ (\pm\ 3e5)}$	$2.2e6_{(\pm 3e5)}$	$\underline{3.2e7}_{(\pm 5e5)}$
B	InFoRM	$9.1e2 (\pm 1e2)$	$3.4e3 \scriptstyle (\pm 4e3)$	2.0e2 (± 7e2)	5.2e1 (± 3e2)	$4.7e3 \scriptstyle (\pm 9e3)$	$9.7e3 \scriptstyle (\pm 4e3)$	$9.8e4 \ (\pm \ 3e3)$
DLipschitz	REDRESS	$2.0e5 \scriptscriptstyle (\pm 1 e 4)$	$1.9e5_{\ (\pm\ 2e4)}$	$7.0e3 \scriptscriptstyle (\pm 1e3)$	$1.2e4~\scriptstyle (\pm 3e3)$	$\underline{2.6e4}_{(\pm 6e3)}$	OOM	OOM
	GUIDE	$\underline{1.8e3}_{(\pm\ 3e2)}$	$\underline{4.0e3}_{(\pm\ 6e2)}$	$6.4e3 \scriptstyle (\pm 9e2)$	$\underline{4.2e3}_{(\pm 3e2)}$	$1.1e5 \ \scriptscriptstyle (\pm \ 1e4)$	$\underline{1.5e4}~(\pm~7e3)$	OOM
	GNN	$44.56\scriptscriptstyle~(\pm 0.59)$	$37.01 \scriptscriptstyle \ (\pm 0.26)$	$31.42_{(\pm 1.49)}$	$\underline{39.01}~(\pm 1.05)$	$15.31 \scriptscriptstyle \ (\pm \ 0.32)$	$43.74 \scriptscriptstyle (\pm 0.70)$	$37.75 \scriptscriptstyle (\pm 0.19)$
NDCC@k	InFoRM	$48.78\scriptscriptstyle~(\pm 3.62)$	$44.09_{\ (\pm\ 3.00)}$	$\underline{35.89}_{(\pm 3.69)}$	$37.11_{(\pm 3.18)}$	$19.81 \scriptscriptstyle \ (\pm 1.74)$	$38.85 \scriptscriptstyle (\pm 2.07)$	$\underline{33.34}_{(\pm1.70)}$
INDCG@h	REDRESS	$54.30 \scriptscriptstyle (\pm 3.08)$	$48.53 \ (\pm \ 3.85)$	$42.82 (\pm 3.62)$	$42.74_{(\pm 2.11)}$	$25.30 (\pm 1.96)$	OOM	OOM
	GUIDE	$\underline{49.02}_{(\pm2.72)}$	$\underline{47.27}_{(\pm \ 4.72)}$	$32.70_{(\pm 2.02)}$	$37.38 \scriptscriptstyle (\pm 2.69)$	$\underline{21.50}_{(\pm\ 2.18)}$	$\underline{39.16}_{(\pm2.26)}$	OOM
GDIF	GNN	$\underline{111.92}_{(\pm\ 0.81)}$	$232.16_{\ (\pm\ 24.2)}$	125.87 (± 11.1)	$166.78_{\ (\pm\ 36.1)}$	$112.78_{(\pm 1.29)}$	$\underline{114.05}_{(\pm 1.17)}$	$112.72_{(\pm 1.21)}$
	InFoRM	$118.07 \ (\pm \ 10.2)$	$\underline{116.17}_{(\pm \ 5.65)}$	$136.94_{(\pm 10.3)}$	$\underline{160.62} \ (\pm 11.2)$	$112.90_{\ (\pm\ 8.66)}$	$125.36\scriptscriptstyle~(\pm~11.4)$	$\underline{127.84}_{(\pm8.51)}$
	REDRESS	$167.56\scriptscriptstyle~(\pm~7.12)$	$124.08_{\ (\pm\ 10.8)}$	$139.98_{(\pm \ 8.84)}$	$163.84 \ (\pm \ 5.75)$	$\underline{109.58}_{(\pm \ 7.33)}$	OOM	OOM
	GUIDE	$108.75 \scriptstyle (\pm 5.89)$	$110.58 (\pm 9.36)$	112.35 (± 8.27)	149.97 (± 5.14)	$104.17_{(\pm 8.21)}$	$112.28_{\ (\pm\ 7.80)}$	OOM

378 Table 3: Comparison of graph learning methods focusing on individual fairness. Note that results 379 include AUC-ROC score, BLipschitz, NDCG@k, and GDIF; complete results are in Appendix. The 380 best ones are in **bold**; the second best ones are underlined; OOM denotes out-of-memory.

in Figure 4. Generally, a good trade-off indicates that the superiority in one fairness metric does not significantly sacrifice the fairness levels measured by other metrics.

Finding 3: Fairness-aware graph learning methods struggle for a balance. According to Figure 4, we have the following observations. First, fairness-aware graph learning methods



based on shallow embedding methods, i.e., FairWalk and Cross-Walk, generally outperform those GNNbased ones when considering the balance over all three fairness metrics. Notably, they also achieve the best performance on both $\Delta_{\rm SP}$ and $\Delta_{\rm EO}$. This aligns with the observations shown in Section 4.1, which can be attributed to the ab-

416 Figure 4: Average rankings on Δ_{SP} , Δ_{EO} , and $\Delta_{Utility}$ across all datasets. 417 Methods are ranked in ascending order by the summation of average rank-418 ings on all three fairness metrics.

419 sence of bias brought by node attributes. Second, we note that the utility difference-based fairness 420 (measured with Δ_{Utility}) is not an explicit optimization goal for any of these methods. Despite this, 421 top-ranked fairness-aware methods based on GNNs (e.g., FairGNN and FairEdit) clearly outperform 422 those based on shallow embedding methods in terms of Δ_{Utility} . This can be attributed to the superior 423 fitting ability of GNNs and informative node attributes, which implicitly helps ensure that no subgroup 424 bears significantly worse performance than others. Based on the above observations, we conclude that these methods always struggle for a balance between different fairness metrics, and one method 425 can hardly do well on all of them. 426

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COMPUTATIONAL EFFICIENCY (RQ4) 4.4

Finally, we answer RQ4 by comparing the computational efficiency of the collected fairness-aware 430 graph learning methods. Here, we utilize running time in seconds to measure efficiency, and we also 431 collect the associated utility (measured with AUC-ROC score). We present an exemplary comparison

across all collected graph learning models (two baselines and ten fairness-aware ones) on the Credit
 Default dataset in Figure 5. The comparison on other datasets is presented and discussed in Appendix.

Finding 4: Fairness-aware graph learning methods generally sacrifice efficiency. According to Figure 5, we have the following observations. First, fairness-aware graph learning methods based on GNNs exhibit a clear sacrifice on efficiency, where EDITS under group fairness

437 and REDRESS under 438 individual fairness 439 sacrifice the most. This 440 can be attributed to 441 computationally their expensive optimization 442 strategy: EDITS re-443 quires optimizing the 444 whole graph topology, 445 while REDRESS calcu-446 lates different similarity 447 rankings (across all 448 nodes) in every learning 449 epoch. In contrast to the 450 clear sacrifice on effi-451 ciency, we also observe 452 that most fairness-aware graph learning methods 453 maintain a relatively 454 high level of utility, 455



Figure 5: An exemplary comparison of AUC-ROC and running time across different collected graph learning methods on Credit Default dataset.

which remains consistent with the general utility assessment shown in Section 4.1. Second, although 456 those based on shallow embedding methods bear longer running time (than most GNN-based ones), 457 they only marginally sacrifice efficiency. A primary reason is that compared with GNN-based ones, 458 they usually do not introduce much additional computation in the calculation and optimization of the 459 objective function. In fact, both FairWalk and CrossWalk facilitate their fairness levels by adopting 460 different transition probability distributions to perform random walks on graphs. Meanwhile, we 461 also notice that those based on shallow embedding methods generally bear worse utility than 462 the GNN-based ones, which is also consistent with the discussion in Section 4.1. Based on the 463 observations above, we conclude that these fairness-aware methods generally sacrifice efficiency compared with the vanilla baseline methods. 464

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5 A GUIDE FOR PRACTITIONERS

Based on the discussion above, we conclude that each fairness-aware graph learning method bears its
strengths and limitations from different perspectives. Therefore, it becomes crucial to select the most
suitable methods to use carefully. To assist practitioners in making informed decisions in real-world
applications, this section provides a guide to help choose the most appropriate fairness-aware graph
learning methods such that their strengths can be fully leveraged to address fairness-related concerns
while maintaining a proper level of performance.

Specifically, we propose to organize this guide from two perspectives, including group fairness 475 and individual fairness. From the perspective of group fairness, if the main priority is to achieve 476 the best performance on typical group fairness metrics such as Δ_{SP} and Δ_{FO} , while utility and 477 efficiency are less of a concern, fairness-aware shallow embedding methods including FairWalk 478 and CrossWalk are recommended choices. The reason is that these methods can generally achieve 479 top-ranked performance in terms of group fairness, although the corresponding utility and efficiency 480 are usually inferior to GNN-based methods. If the main priority is to achieve a good balance between 481 utility and group fairness, GNN-based methods such as FairVGNN, EDITS, FairEdit, and NIFTY are 482 recommended. This is because these methods usually achieve a more satisfactory trade-off between 483 utility and group fairness compared with those based on shallow embedding methods. Furthermore, we note that FairGNN maintains a better trade-off among all three fairness metrics, which makes 484 it more suitable for applications with significant emphasis on optimizing different types of fairness. 485 From the perspective of individual fairness, since each method bears a different fairness optimization

goal, we recommend selecting the one with the most desired goal of individual fairness. Meanwhile, we notice that GUIDE achieves a superior balance between $B_{\text{Lipschitz}}$ and GDIF compared with the other two methods. Hence GUIDE is recommended if higher levels of individual fairness is desired.

6 RELATED WORKS

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Benchmarking Graph Learning Methods. Existing studies have explored two mainstream bench-493 marks for graph learning methods, i.e., usability-oriented ones and trustworthiness-oriented ones. 494 Specifically, usability-oriented ones focus on evaluating models' capabilities in accomplishing spe-495 cific graph learning tasks, including node classification (Shchur et al., 2018; Izadi et al., 2020; Luan 496 et al., 2021), link prediction (Bordes et al., 2013; Shang et al., 2018; Suchanek et al., 2007), and 497 representation learning (Stier & Granitzer; Ren et al., 2020). In addition to those focusing on utility 498 (e.g., F1-score in node classification tasks), a few existing studies also explored efficiency, such as comparisons on training time (Said et al., 2023) and memory usage (Huang et al., 2023). On the other 499 500 hand, trustworthiness-oriented ones mainly aim to provide comprehensive analysis on how well graph learning models can be trusted, such as studies from the perspective of robustness (Bojchevski & 501 Günnemann, 2019; Zügner & Günnemann, 2019) and interpretability (Agarwal et al., 2018; Xuanyuan 502 et al., 2023). However, from the perspective of algorithmic fairness, existing benchmarks remain scarce. To the best of our knowledge, Qian et al. (Qian et al., 2024) took an initial step towards 504 developing a fairness-aware graph learning benchmark. However, only two representative works are 505 evaluated in their benchmark, which limits the insights it reveals. Different from the existing research 506 work above, our work serves as an initial step towards a comprehensive benchmark on fairness-aware 507 graph learning methods, which reveals key insights on their strengths and limitations and exhibits the 508 potential to facilitate broader applications.

509 Fairness-Aware Graph Learning. In graph learning tasks, unfairness can be defined with different 510 criteria and exhibited from different perspectives (Dong et al.) (2023b). In general, two fairness notions 511 are the most widely discussed ones by existing studies, i.e., group fairness and individual fairness. 512 Specifically, group fairness emphasizes that the learning methods should not yield discriminatory 513 predictions or decisions targeting individuals belonging to any particular sensitive subgroup (race, 514 gender, etc.) (Dwork et al., 2011). Common approaches to mitigate the bias revealed by the notion 515 of group fairness include rebalancing (Khajehnejad et al., 2022; Farnadi et al., 2018; Current et al., 516 2022; Buyl & Bie, 2021), adversarial learning (Dai & Wang, 2021; Khajehnejad et al., 2020; Xu et al., 2021; Bose & Hamilton, 2019), edge rewiring (Dong et al., 2022; Li et al., 2021; Kose & Shen, 2022; 517 Jalali et al.), and orthogonal projection (Palowitch & Perozzi, 2020; Zeng et al., 2021). On the other 518 hand, *individual fairness* notion requires models to treat similar individuals similarly (Dwork et al., 519 2011). Existing works that mitigate the bias revealed by individual fairness include optimization with 520 constraints (Gupta & Dukkipati, 2021) and regularizations (Fan et al., 2021; Dong et al., 2021a; Kang 521 et al., 2020a; Lahoti et al., 2019). Other fairness issues have also been studied in recent years Liu 522 et al. (2023); Arun et al. (2023). However, since they have not been widely adopted in real-world 523 applications, they are not the main focus of this paper. Despite the abundant efforts, there still lacks 524 a comprehensive benchmark to facilitate the understanding of those representative fairness-aware graph learning methods. We present a comprehensive benchmark to provide guidance based on the 526 results over a wide range of representative fairness-aware graph learning methods.

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7 CONCLUSION

530 In this paper, we introduced a comprehensive benchmark for fairness-aware graph learning methods, 531 which bridges a critical gap between the current literature and broader applications. Specifically, 532 we designed a systematic evaluation protocol, collected ten representative methods, and conducted 533 extensive experiments on seven real-world attributed graph datasets from various domains. Our 534 in-depth analysis revealed key insights into the strengths and limitations of existing methods in terms of group fairness, individual fairness, balancing different fairness criteria, and computational 536 efficiency. These findings, along with the practical guide we provided, offer valuable guidance for 537 practitioners to select appropriate methods based on their specific requirements. While we focused on the node classification task in this paper, evaluations on other graph learning tasks remain a future 538 direction to be explored, which will further enrich the understanding of the performance of these methods and expand their applicability across a wider range of applications.

540 REFERENCES

- 542 Chirag Agarwal, Owen Queen, Himabindu Lakkaraju, and Marinka Zitnik. An explainable ai library
 543 for benchmarking graph explainers. 2018.
- Chirag Agarwal, Himabindu Lakkaraju, and Marinka Zitnik. Towards a unified framework for fair
 and stable graph representation learning. In *Uncertainty in Artificial Intelligence*, pp. 2114–2124.
 PMLR, 2021.
- Junaid Ali, Mahmoudreza Babaei, Abhijnan Chakraborty, Baharan Mirzasoleiman, Krishna P. Gummadi, and Adish Singla. On the fairness of time-critical influence maximization in social networks, 2021.
- Joshua W Anderson and Shyam Visweswaran. Algorithmic individual fairness for healthcare: A scoping review. *medRxiv*, pp. 2024–03, 2024.
- Arvindh Arun, Aakash Aanegola, Amul Agrawal, Ramasuri Narayanam, and Ponnurangam Ku maraguru. Cafin: Centrality aware fairness inducing in-processing for unsupervised representation
 learning on graphs. In *ECAI 2023*, pp. 101–108. IOS Press, 2023.
- Gowtham Atluri, Anuj Karpatne, and Vipin Kumar. Spatio-temporal data mining: A survey of problems and methods. *ACM Computing Surveys (CSUR)*, 51(4):1–41, 2018.
- Aleksandar Bojchevski and Stephan Günnemann. Certifiable robustness to graph perturbations.
 Advances in Neural Information Processing Systems, 32, 2019.
- Antoine Bordes, Nicolas Usunier, Alberto Garcia-Duran, Jason Weston, and Oksana Yakhnenko.
 Translating embeddings for modeling multi-relational data. Advances in neural information processing systems, 26, 2013.
- Avishek Joey Bose and William L. Hamilton. Compositional fairness constraints for graph embeddings, 2019.
- Maarten Buyl and Tijl De Bie. Debayes: a bayesian method for debiasing network embeddings, 2021.
- April Chen, Ryan A Rossi, Namyong Park, Puja Trivedi, Yu Wang, Tong Yu, Sungchul Kim, Franck
 Dernoncourt, and Nesreen K Ahmed. Fairness-aware graph neural networks: A survey. ACM
 Transactions on Knowledge Discovery from Data, 18(6):1–23, 2024.
- Eunjoon Cho, Seth A Myers, and Jure Leskovec. Friendship and mobility: user movement in location based social networks. In *Proceedings of the 17th ACM SIGKDD international conference on Knowledge discovery and data mining*, pp. 1082–1090, 2011.
- Manvi Choudhary, Charlotte Laclau, and Christine Largeron. A survey on fairness for machine learning on graphs. *arXiv preprint arXiv:2205.05396*, 2022.
- Zicun Cong, Baoxu Shi, Shan Li, Jaewon Yang, Qi He, and Jian Pei. Fairsample: Training fair and
 accurate graph convolutional neural networks efficiently. *IEEE Transactions on Knowledge and Data Engineering*, 2023.
- Sean Current, Yuntian He, Saket Gurukar, and Srinivasan Parthasarathy. Fairegm: Fair link prediction and recommendation via emulated graph modification. In *Equity and Access in Algorithms, Mechanisms, and Optimization*, EAAMO '22. ACM, October 2022. doi: 10.1145/3551624.
 3555287. URL http://dx.doi.org/10.1145/3551624.3555287.
- Enyan Dai and Suhang Wang. Say no to the discrimination: Learning fair graph neural networks with limited sensitive attribute information, 2021.
- Enyan Dai, Tianxiang Zhao, Huaisheng Zhu, Junjie Xu, Zhimeng Guo, Hui Liu, Jiliang Tang, and
 Suhang Wang. A comprehensive survey on trustworthy graph neural networks: Privacy, robustness,
 fairness, and explainability. *arXiv preprint arXiv:2204.08570*, 2022.
- Austin Derrow-Pinion, Jennifer She, David Wong, Oliver Lange, Todd Hester, Luis Perez, Marc
 Nunkesser, Seongjae Lee, Xueying Guo, Brett Wiltshire, et al. Eta prediction with graph neural
 networks in google maps. In *Proceedings of the 30th ACM International Conference on Information* & Knowledge Management, pp. 3767–3776, 2021.

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594	Guimin Dong, Mingyue Tang, Zhiyuan Wang, Jiechao Gao, Sikun Guo, Lihua Cai, Robert Gutierrez,
595	Bradford Campbel, Laura E Barnes, and Mehdi Boukhechba. Graph neural networks in iot: A
596	survey. ACM Transactions on Sensor Networks, 19(2):1–50, 2023a.

- Yushun Dong, Jian Kang, Hanghang Tong, and Jundong Li. Individual fairness for graph neural 598 networks: A ranking based approach. In Proceedings of the 27th ACM SIGKDD Conference on Knowledge Discovery & Data Mining, KDD '21, pp. 300–310, New York, NY, USA, 2021a. 600 Association for Computing Machinery. ISBN 9781450383325. doi: 10.1145/3447548.3467266. 601 URL https://doi.org/10.1145/3447548.3467266
- Yushun Dong, Jian Kang, Hanghang Tong, and Jundong Li. Individual fairness for graph neural 603 networks: A ranking based approach. In Proceedings of the 27th ACM SIGKDD Conference on 604 Knowledge Discovery & Data Mining, pp. 300-310, 2021b. 605
- Yushun Dong, Ninghao Liu, Brian Jalaian, and Jundong Li. Edits: Modeling and mitigating data bias for graph neural networks. In Proceedings of the ACM web conference 2022, pp. 1259–1269, 2022. 607
- 608 Yushun Dong, Jing Ma, Song Wang, Chen Chen, and Jundong Li. Fairness in graph mining: A survey. 609 IEEE Transactions on Knowledge and Data Engineering, 2023b. 610
- Cynthia Dwork, Moritz Hardt, Toniann Pitassi, Omer Reingold, and Rich Zemel. Fairness through 611 awareness, 2011. 612
- 613 Cynthia Dwork, Moritz Hardt, Toniann Pitassi, Omer Reingold, and Richard Zemel. Fairness through 614 awareness. In Proceedings of the 3rd innovations in theoretical computer science conference, pp. 615 214-226, 2012.
- 616 Wei Fan, Kunpeng Liu, Rui Xie, Hao Liu, Hui Xiong, and Yanjie Fu. Fair graph auto-encoder for 617 unbiased graph representations with wasserstein distance. In 2021 IEEE International Conference 618 on Data Mining (ICDM), pp. 1054–1059, 2021. doi: 10.1109/ICDM51629.2021.00122. 619
- Golnoosh Farnadi, Pigi Kouki, Spencer K. Thompson, Sriram Srinivasan, and Lise Getoor. A 620 fairness-aware hybrid recommender system, 2018. 621
- 622 Shubham Gupta and Ambedkar Dukkipati. Protecting individual interests across clusters: 623 Spectral clustering with guarantees. ArXiv, abs/2105.03714, 2021. URL https://api. 624 semanticscholar.org/CorpusID:234339805.
 - Moritz Hardt, Eric Price, and Nati Srebro. Equality of opportunity in supervised learning. Advances in neural information processing systems, 29, 2016.
- Weihua Hu, Matthias Fey, Marinka Zitnik, Yuxiao Dong, Hongyu Ren, Bowen Liu, Michele Catasta, 628 and Jure Leskovec. Open graph benchmark: Datasets for machine learning on graphs. Advances in 629 neural information processing systems, 33:22118–22133, 2020. 630
- Shenyang Huang, Farimah Poursafaei, Jacob Danovitch, Matthias Fey, Weihua Hu, Emanuele Rossi, 632 Jure Leskovec, Michael Bronstein, Guillaume Rabusseau, and Reihaneh Rabbany. Temporal graph 633 benchmark for machine learning on temporal graphs, 2023.
- 634 Mohammad Rasool Izadi, Yihao Fang, Robert Stevenson, and Lizhen Lin. Optimization of graph 635 neural networks with natural gradient descent, 2020. 636
- Zeinab S. Jalali, Weixiang Wang, Myunghwan Kim, Hema Raghavan, and Sucheta Soundarajan. On 637 the Information Unfairness of Social Networks, pp. 613–521. doi: 10.1137/1.9781611976236.69. 638 URL https://epubs.siam.org/doi/abs/10.1137/1.9781611976236.69. 639
- 640 Zhimeng Jiang, Xiaotian Han, Chao Fan, Zirui Liu, Na Zou, Ali Mostafavi, and Xia Hu. Fmp: 641 Toward fair graph message passing against topology bias. arXiv preprint arXiv:2202.04187, 2022.
- Zhimeng Jiang, Xiaotian Han, Chao Fan, Zirui Liu, Na Zou, Ali Mostafavi, and Xia Hu. Chasing 643 fairness in graphs: A gnn architecture perspective. In Proceedings of the AAAI Conference on 644 Artificial Intelligence, volume 38, pp. 21214–21222, 2024. 645
- Kareem L Jordan and Tina L Freiburger. The effect of race/ethnicity on sentencing: Examining 646 sentence type, jail length, and prison length. Journal of Ethnicity in Criminal Justice, 13(3): 647 179-196, 2015.

648 649 650 651 652	Jian Kang, Jingrui He, Ross Maciejewski, and Hanghang Tong. Inform: Individual fairness on graph mining. In <i>Proceedings of the 26th ACM SIGKDD International Conference on Knowledge Discovery & Data Mining</i> , KDD '20, pp. 379–389, New York, NY, USA, 2020a. Association for Computing Machinery. ISBN 9781450379984. doi: 10.1145/3394486.3403080. URL https://doi.org/10.1145/3394486.3403080.
653 654 655 656	Jian Kang, Jingrui He, Ross Maciejewski, and Hanghang Tong. Inform: Individual fairness on graph mining. In <i>Proceedings of the 26th ACM SIGKDD international conference on knowledge discovery & data mining</i> , pp. 379–389, 2020b.
657 658 659	Ahmad Khajehnejad, Moein Khajehnejad, Mahmoudreza Babaei, Krishna P. Gummadi, Adrian Weller, and Baharan Mirzasoleiman. Crosswalk: Fairness-enhanced node representation learning, 2022.
660 661 662	Moein Khajehnejad, Ahmad Asgharian Rezaei, Mahmoudreza Babaei, Jessica Hoffmann, Mahdi Jalili, and Adrian Weller. Adversarial graph embeddings for fair influence maximization over social networks, 2020.
663 664 665	O. Deniz Kose and Yanning Shen. Fair node representation learning via adaptive data augmentation, 2022.
666 667 668 669	Preethi Lahoti, Krishna P. Gummadi, and Gerhard Weikum. Operationalizing individual fairness with pairwise fair representations. <i>Proceedings of the VLDB Endowment</i> , 13(4):506–518, December 2019. ISSN 2150-8097. doi: 10.14778/3372716.3372723. URL http://dx.doi.org/10.14778/3372716.3372723.
670 671	Jure Leskovec and Julian Mcauley. Learning to discover social circles in ego networks. Advances in neural information processing systems, 25, 2012.
672 673 674 675	Jure Leskovec, Daniel Huttenlocher, and Jon Kleinberg. Signed networks in social media. In <i>Proceedings of the SIGCHI conference on human factors in computing systems</i> , pp. 1361–1370, 2010.
676 677 678	Peizhao Li, Yifei Wang, Han Zhao, Pengyu Hong, and Hongfu Liu. On dyadic fairness: Exploring and mitigating bias in graph connections. In <i>International Conference on Learning Representations</i> , 2021. URL https://openreview.net/forum?id=xqGS6PmzNq6.
679 680 681	Yanying Li, Yue Ning, Rong Liu, Ying Wu, and Wendy Hui Wang. Fairness of classification using users' social relationships in online peer-to-peer lending. In <i>Companion Proceedings of the Web Conference 2020</i> , pp. 733–742, 2020.
682 683 684 685	Hongyi Ling, Zhimeng Jiang, Youzhi Luo, Shuiwang Ji, and Na Zou. Learning fair graph representa- tions via automated data augmentations. In <i>International Conference on Learning Representations</i> (<i>ICLR</i>), 2023.
686 687 688	Zemin Liu, Trung-Kien Nguyen, and Yuan Fang. On generalized degree fairness in graph neural networks. In <i>Proceedings of the AAAI Conference on Artificial Intelligence</i> , volume 37, pp. 4525–4533, 2023.
689 690	Donald Loveland, Jiayi Pan, Aaresh Farrokh Bhathena, and Yiyang Lu. Fairedit: Preserving fairness in graph neural networks through greedy graph editing. <i>arXiv preprint arXiv:2201.03681</i> , 2022.
692 693 694	Sitao Luan, Chenqing Hua, Qincheng Lu, Jiaqi Zhu, Mingde Zhao, Shuyuan Zhang, Xiao-Wen Chang, and Doina Precup. Is heterophily a real nightmare for graph neural networks to do node classification?, 2021.
695 696	Kolby Nottingham Markelle Kelly, Rachel Longjohn. The uci machine learning repository. URL https://archive.ics.uci.edu .
697 698 699	Ninareh Mehrabi, Fred Morstatter, Nripsuta Saxena, Kristina Lerman, and Aram Galstyan. A survey on bias and fairness in machine learning. <i>ACM computing surveys (CSUR)</i> , 54(6):1–35, 2021.
700 701	Annamalai Narayanan, Mahinthan Chandramohan, Rajasekar Venkatesan, Lihui Chen, Yang Liu, and Shantanu Jaiswal. graph2vec: Learning distributed representations of graphs. <i>arXiv preprint arXiv:1707.05005</i> , 2017.

- 702 John Palowitch and Bryan Perozzi. Monet: Debiasing graph embeddings via the metadata-orthogonal 703 training unit, 2020. 704 Georgios A Pavlopoulos, Maria Secrier, Charalampos N Moschopoulos, Theodoros G Soldatos, 705 Sophia Kossida, Jan Aerts, Reinhard Schneider, and Pantelis G Bagos. Using graph theory to 706 analyze biological networks. *BioData mining*, 4:1–27, 2011. 707 708 Xiaowei Qian, Zhimeng Guo, Jialiang Li, Haitao Mao, Bingheng Li, Suhang Wang, and Yao Ma. Addressing shortcomings in fair graph learning datasets: Towards a new benchmark. arXiv preprint 709 arXiv:2403.06017, 2024. 710 711 Tahleen Rahman, Bartlomiej Surma, Michael Backes, and Yang Zhang. Fairwalk: Towards fair graph 712 embedding. 2019. 713 Aida Rahmattalabi, Phebe Vayanos, Anthony Fulginiti, Eric Rice, Bryan Wilder, Amulya Yadav, and 714 Milind Tambe. Exploring algorithmic fairness in robust graph covering problems. Advances in 715 neural information processing systems, 32, 2019. 716 717 Aida Rahmattalabi, Shahin Jabbari, Himabindu Lakkaraju, Phebe Vayanos, Max Izenberg, Ryan Brown, Eric Rice, and Milind Tambe. Fair influence maximization: A welfare optimization 718 approach. In Proceedings of the AAAI Conference on Artificial Intelligence, volume 35, pp. 719 11630-11638, 2021. 720 721 Feiliang Ren, Juchen Li, Huihui Zhang, Shilei Liu, Bochao Li, Ruicheng Ming, and Yujia Bai. 722 Knowledge graph embedding with atrous convolution and residual learning, 2020. 723 Anwar Said, Roza G. Bayrak, Tyler Derr, Mudassir Shabbir, Daniel Moyer, Catie Chang, and Xenofon 724 Koutsoukos. Neurograph: Benchmarks for graph machine learning in brain connectomics, 2023. 725 Chao Shang, Yun Tang, Jing Huang, Jinbo Bi, Xiaodong He, and Bowen Zhou. End-to-end structure-726 aware convolutional networks for knowledge base completion, 2018. 727 728 Oleksandr Shchur, Maximilian Mumme, Aleksandar Bojchevski, and Stephan Günnemann. Pitfalls 729 of graph neural network evaluation. Relational Representation Learning Workshop, NeurIPS 2018, 730 2018. 731 Anuj Kumar Sirohi, Anjali Gupta, Sayan Ranu, Sandeep Kumar, and Amitabha Bagchi. Graphgini: 732 Fostering individual and group fairness in graph neural networks. arXiv preprint arXiv:2402.12937, 733 2024. 734 735 Weihao Song, Yushun Dong, Ninghao Liu, and Jundong Li. Guide: Group equality informed 736 individual fairness in graph neural networks. In Proceedings of the 28th ACM SIGKDD Conference on Knowledge Discovery and Data Mining, pp. 1625–1634, 2022. 737 738 Zixing Song, Yuji Zhang, and Irwin King. Towards fair financial services for all: A temporal 739 gnn approach for individual fairness on transaction networks. In Proceedings of the 32nd ACM 740 International Conference on Information and Knowledge Management, pp. 2331–2341, 2023. 741 Julian Stier and Michael Granitzer. Deepgg: a deep graph generator. In Advances in Intelligent 742 Data Analysis XIX: 19th International Symposium on Intelligent Data Analysis, IDA 2021, Porto, 743 Portugal, April 26–28, 2021, Proceedings, pp. 325. Springer Nature. 744 Ana-Andreea Stoica, Jessy Xinyi Han, and Augustin Chaintreau. Seeding network influence in 745 biased networks and the benefits of diversity. In Proceedings of The Web Conference 2020, pp. 746 2089-2098, 2020. 747 748 Fabian M. Suchanek, Gjergji Kasneci, and Gerhard Weikum. Yago: a core of semantic knowledge. 749 In Proceedings of the 16th International Conference on World Wide Web, WWW '07, pp. 697–706, 750 New York, NY, USA, 2007. Association for Computing Machinery. ISBN 9781595936547. doi: 10.1145/1242572.1242667. URL https://doi.org/10.1145/1242572.1242667. 751 752 Lubos Takac and Michal Zabovsky. Data analysis in public social networks. In International scientific 753 conference and international workshop present day trends of innovations, volume 1, 2012. 754
- Jianian Wang, Sheng Zhang, Yanghua Xiao, and Rui Song. A review on graph neural network methods in financial applications. *arXiv preprint arXiv:2111.15367*, 2021.

- 756 Yu Wang, Yuying Zhao, Yushun Dong, Huiyuan Chen, Jundong Li, and Tyler Derr. Improving fairness in graph neural networks via mitigating sensitive attribute leakage. In Proceedings of the 758 28th ACM SIGKDD conference on knowledge discovery and data mining, pp. 1938–1948, 2022. 759 Le Wu, Lei Chen, Pengyang Shao, Richang Hong, Xiting Wang, and Meng Wang. Learning fair 760 representations for recommendation: A graph-based perspective. In *Proceedings of the Web* 761 *Conference 2021*, pp. 2198–2208, 2021. 762 763 Shiwen Wu, Fei Sun, Wentao Zhang, Xu Xie, and Bin Cui. Graph neural networks in recommender 764 systems: a survey. ACM Computing Surveys, 55(5):1–37, 2022. 765 Zonghan Wu, Shirui Pan, Fengwen Chen, Guodong Long, Chengqi Zhang, and S Yu Philip. A 766 comprehensive survey on graph neural networks. IEEE transactions on neural networks and 767 learning systems, 32(1):4-24, 2020. 768 Bingke Xu, Yue Cui, Zipeng Sun, Liwei Deng, and Kai Zheng. Fair representation learning in 769 knowledge-aware recommendation. In 2021 IEEE International Conference on Big Knowledge 770 (ICBK), pp. 385-392, 2021. doi: 10.1109/ICKG52313.2021.00058. 771 772 Han Xuanyuan, Pietro Barbiero, Dobrik Georgiev, Lucie Charlotte Magister, and Pietro Lió. Global 773 concept-based interpretability for graph neural networks via neuron analysis, 2023. 774 I-Cheng Yeh and Che-hui Lien. The comparisons of data mining techniques for the predictive 775 accuracy of probability of default of credit card clients. *Expert systems with applications*, 36(2): 776 2473-2480, 2009. 777 Zhitao Ying, Dylan Bourgeois, Jiaxuan You, Marinka Zitnik, and Jure Leskovec. Gnnexplainer: 778 Generating explanations for graph neural networks. Advances in neural information processing 779 systems, 32, 2019. 780 781 Jiaxuan You, Rex Ying, and Jure Leskovec. Position-aware graph neural networks. In International 782 conference on machine learning, pp. 7134–7143. PMLR, 2019. 783 Haitao Yuan and Guoliang Li. A survey of traffic prediction: from spatio-temporal data to intelligent 784 transportation. *Data Science and Engineering*, 6(1):63–85, 2021. 785 786 Ziqian Zeng, Rashidul Islam, Kamrun Naher Keya, James Foulds, Yangqiu Song, and Shimei Pan. 787 Fair representation learning for heterogeneous information networks, 2021. 788 Duna Zhan, Dongliang Guo, Pengsheng Ji, and Sheng Li. Bridging the fairness divide: Achieving 789 group and individual fairness in graph neural networks. arXiv preprint arXiv:2404.17511, 2024. 790 791 Guixian Zhang, Debo Cheng, Guan Yuan, and Shichao Zhang. Learning fair representations via rebalancing graph structure. *Information Processing & Management*, 61(1):103570, 2024. 792 793 Yue Zhang and Arti Ramesh. Learning fairness-aware relational structures. arXiv preprint 794 arXiv:2002.09471, 2020. Jie Zhou, Ganqu Cui, Shengding Hu, Zhengyan Zhang, Cheng Yang, Zhiyuan Liu, Lifeng Wang, 796 Changcheng Li, and Maosong Sun. Graph neural networks: A review of methods and applications. 797 AI open, 1:57-81, 2020. 798 799 Marinka Zitnik and Jure Leskovec. Predicting multicellular function through multi-layer tissue 800 networks. Bioinformatics, 33(14):i190-i198, 2017. 801 Marinka Zitnik, Monica Agrawal, and Jure Leskovec. Modeling polypharmacy side effects with 802 graph convolutional networks. *Bioinformatics*, 34(13):i457-i466, 2018. 803 804 Daniel Zügner and Stephan Günnemann. Certifiable robustness and robust training for graph 805 convolutional networks. In Proceedings of the 25th ACM SIGKDD International Conference on Knowledge Discovery & Data Mining, pp. 246–256, 2019. 806 808
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000 DOCUMENTATION OF NEW DATASETS А

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Introduction of New Datasets. In this benchmark, we introduce two new crafted datasets: AMiner-S 003 and AMiner-L, which are coauthor networks constructed from the AMiner network (Wan et al., 2019) 004 in two different ways. The AMiner-S dataset is extracted from AMiner by its largest connected component, and contains 39,424 nodes, 52,460 edges, and 5,694 attributes in total. Here the nodes 006 denote the researchers, the edges represent the co-authorship between researchers, and the attributes 007 are created from the abstracts of the associated papers. In addition, the sensitive attribute is the 800 continent of the affiliation of each researcher belongs to, and the task associated with this dataset is to predict the primary research field of each researcher. The AMiner-L dataset is extracted from 009 AMiner by random walk, which has 129,726 nodes, 591,039 edges, and 5,694 attributes in total. All 010 the settings including the sensitive attribute and the associated tasks are the same with AMiner-S. It is worth-noting that both datasets AMiner-S and AMiner-L are anonymous and thus have no privacy 012 concern, which ensures compliance with privacy regulations such as the General Data Protection 013 Regulation (GDPR) and allows for broader sharing and usage across institutions. 014

Intended Uses. The two datasets are designed for research in the field of graph learning, especially 015 designed for fairness-related research on graphs. The datasets allow researchers to evaluate their 016 fairness-aware graph learning algorithms, thus empower them to measure and mitigate bias that may 017 exhibit by graph learning algorithms. 018

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В REPRODUCIBILITY

022 In this section, we will introduce the details of the experiments for the purpose of reproducibility. We first provide a detailed description of benchmark datasets employed in this study. Subsequently, we 024 describe the implementation of the experiments on these datasets, followed by an in-depth explanation 025 of code basis and hardware support of the implementation.

026 Benchmark Datasets. We collected seven real-world attributed graph datasets in this benchmark 027 paper, including five existing commonly used ones and two newly constructed ones. We provide a brief introduction for each as follows. (1) Pokec-z (Takac & Zabovsky 2012). The Pokec-z 029 dataset is sampled from Pokec, which is the most popular on-line social network in Slovakia. Pokec contains anonymized data of the whole social network in 2012, in which the profiles contain gender, 031 age, hobbies, interest, education, working field, etc. Here the region corresponding to each user is 032 considered as the sensitive attributes, and the task is to predict the working field of each user. (2) 033 *Pokec-n (Takac & Zabovsky)* [2012). The Pokec-n dataset is sampled from Pokec as well, while the 034 users in Pokec-n come from different geographical regions compared with those in Pokec-z. Pokec-n shares the same settings on sensitive attributes and predictive task as those of Pokec-z. (3) German 035 Credit (Markelle Kelly). The German Credit dataset is a credit graph, where nodes represent clients 036 in a German bank and they are connected based on the similarity of their credit accounts. Here the 037 task is to classify the credit risks of clients into high/low, and gender is considered as the sensitive 038 attribute. (4) Credit Defaulter (Yeh & Lien, 2009). Credit contains clients who are connected based 039 on the similarity of their spending and payment patterns. Here the task is to classify whether each 040 client will default on the credit card payment or not, and age is considered as the sensitive attribute. 041 (5) Recidivism (Jordan & Freiburger, 2015). Recidivism dataset is a graph of defendants who got 042 released on bail at the U.S state courts during 1990-2009. These defendants are connected based 043 on the similarity of past criminal records and demographics. The task is to determine whether a 044 defendant deserves bail or not, and their race is considered as the sensitive attribute. (6) AMiner-S (newly constructed). AMiner-S is a co-author graph we extracted from the AMiner network (Wan 045 et al., 2019) by its largest connected component. Here nodes represent the researchers in different 046 fields, and edges denote the co-authorship between researchers. The sensitive attribute is the continent 047 of the affiliation each researcher belongs to, and the task is to predict the primary research field of 048 each researcher. (5) AMiner-L (newly constructed). AMiner-L is a co-author graph we extracted from 049 the AMiner network by random walk. Compared with AMiner-S, AMiner-L bears a larger scale. 050 AMiner-L shares the same settings on sensitive attributes and predictive task as those of AMiner-S. 051

Experimental Settings. All experiments are repeated for three times. For a fair comparison, we 052 perform a grid search to tune hyperparameters for all algorithms. For most of the experiments, we adopt Adam optimizer. All major experiments can be executed with the provided code.

Metrics	Models	Pokec-z	Pokec-n	German Credit	Credit Defaulter	Recidivism	AMiner-S	AMiner-L
	DeepWalk	$66.44 (\pm 1.33)$	63.58 (± 1.06)	62.52 (± 3.59)	$71.64 (\pm 0.48)$	$90.14 (\pm 1.52)$	$86.35 (\pm 0.27)$	88.54 (± 1.56)
	FairWalk	$64.62 \ (\pm 0.34)$	$61.08 \ (\pm 0.33)$	$68.70 (\pm 0.00)$	$69.48 (\pm 0.27)$	$75.32 (\pm 0.10)$	$79.75 (\pm 0.08)$	$96.18 (\pm 0.01)$
	CrossWalk	$57.98 (\pm 0.23)$	$61.58 (\pm 0.27)$	63.85 (± 1.59)	$67.07 (\pm 0.12)$	$88.05 (\pm 0.10)$	$79.73 (\pm 0.12)$	$96.21 (\pm 0.03)$
	GNN	$66.04 (\pm 0.43)$	$68.12 (\pm 1.09)$	$66.94 (\pm 1.01)$	$76.41 (\pm 1.88)$	$86.68 (\pm 2.50)$	$89.97 (\pm 0.62)$	$91.21 \ (\pm \ 0.01)$
ACC	FairGNN	$66.41 (\pm 1.00)$	$66.80 (\pm 0.52)$	67.32 (± 2.52)	79.91 (± 14.1)	<u>90.77</u> (± 2.98)	$92.22 (\pm 0.18)$	OOM
	NIFTY	$63.35 (\pm 0.13)$	$68.26 (\pm 0.81)$	64.13 (± 2.16)	65.55 (± 0.09)	$86.49 (\pm 0.74)$	$89.27 (\pm 0.03)$	$91.92 (\pm 0.19)$
	EDITS	OOM	OOM	62.25 (± 4.95)	$71.02 (\pm 0.34)$	90.99 (± 0.14)	OOM	OOM
	FairEdit	OOM	OOM	$65.93 (\pm 2.84)$	$71.01 (\pm 3.63)$	$83.86 (\pm 0.44)$	OOM	OOM
	FairVGNN	67.52 (± 3.77)	68.09 (± 0.51)	70.10 (± 0.58)	<u>78.66</u> (± 4.29)	85.69 (± 5.37)	OOM	OOM
	DeepWalk	$66.50 \ (\pm 1.34)$	$61.85 \ (\pm 1.06)$	$56.90 (\pm 1.75)$	53.61 (± 0.66)	$87.18 (\pm 1.34)$	$73.58 \ (\pm \ 0.43)$	$82.68 (\pm 3.28)$
	FairWalk	$64.92 (\pm 0.43)$	$61.52 (\pm 0.34)$	$54.05 (\pm 0.83)$	55.51 (± 0.29)	$72.09 (\pm 0.11)$	$65.35 (\pm 0.54)$	$88.72 (\pm 0.08)$
	CrossWalk	$58.99 (\pm 0.27)$	$62.98 (\pm 0.27)$	51.42 (± 0.43)	$54.50 (\pm 0.42)$	$82.89 (\pm 0.11)$	$64.44 (\pm 0.52)$	$89.67 (\pm 0.04)$
AUC-ROC	GNN	$64.16 (\pm 0.62)$	$67.05 (\pm 1.14)$	67.36 (± 3.59)	$62.62 (\pm 0.51)$	$84.60 (\pm 2.10)$	$81.95 (\pm 1.46)$	$86.82 (\pm 0.11)$
Score	FairGNN	$69.47 (\pm 1.04)$	$68.51 (\pm 0.51)$	52.91 (± 2.15)	56.73 (± 3.16)	92.87 (± 2.42)	$86.23 (\pm 0.14)$	OOM
	NIFTY	62.58 (± 0.14)	$66.78 (\pm 0.82)$	$62.94 (\pm 5.78)$	$61.85 (\pm 0.70)$	$85.58 (\pm 0.83)$	$79.28 (\pm 0.15)$	$86.62 (\pm 0.69)$
	EDITS	OOM	OOM	$60.02 (\pm 1.10)$	61.14 (± 0.36)	$92.34 (\pm 0.31)$	OOM	OOM
	FairEdit	OOM	OOM	56.30 (± 2.33)	$62.50 (\pm 0.61)$	$81.97 (\pm 0.48)$	OOM	OOM
	FairVGNN	71.19 (± 0.94)	70.14 (± 0.55)	$65.48 (\pm 3.46)$	68.81 (± 0.81)	84.74 (± 2.70)	OOM	OOM
	DeepWalk	$5.49 (\pm 1.07)$	$5.90~(\pm~0.88)$	$10.4 (\pm 1.01)$	$6.69 (\pm 0.31)$	$6.50\;(\pm\;0.18)$	$6.75 (\pm 0.29)$	$6.41 \ (\pm 0.46)$
	FairWalk	0.60 (± 1.89)	$0.29 (\pm 2.12)$	3.36 (± 1.01)	$6.20 (\pm 0.32)$	4.67 (± 0.33)	3.06 (± 0.32)	4.28 (± 0.17)
	CrossWalk	$1.75 (\pm 1.17)$	0.21 (± 1.63)	$0.35 (\pm 1.75)$	$6.35 (\pm 0.51)$	$5.14 (\pm 0.21)$	$3.59 (\pm 0.43)$	$5.60 (\pm 0.42)$
	GNN	$10.4 (\pm 1.46)$	$14.7 (\pm 0.40)$	32.4 (± 1.93)	$20.6 (\pm 4.34)$	$8.54 (\pm 0.10)$	$7.28 (\pm 0.31)$	$6.75 (\pm 0.00)$
$\Delta_{ m SP}$	FairGNN	$2.06 (\pm 1.82)$	$8.11 (\pm 1.16)$	$14.2 (\pm 0.83)$	$2.51 (\pm 5.61)$	$7.48 (\pm 0.30)$	5.36 (± 0.27)	OOM
	NIFTY	$2.48 (\pm 0.47)$	$2.42 (\pm 0.84)$	$0.26 (\pm 0.41)$	$12.5 (\pm 3.64)$	$7.88 (\pm 0.43)$	$3.25 (\pm 0.52)$	$5.86 (\pm 0.44)$
	EDITS	OOM	OOM	0.18 (± 1.78)	$10.7 (\pm 0.66)$	$7.36 (\pm 0.05)$	OOM	OOM
	FairEdit	OOM	OOM	3.15 (± 3.73)	$1.95 (\pm 0.21)$	$7.39 (\pm 0.50)$	OOM	OOM
	FairVGNN	6.33 (± 1.90)	5.31 (± 1.19)	3.13 (± 0.28)	9.93 (± 0.88)	6.54 (± 0.53)	OOM	OOM
	DeepWalk	$7.31 (\pm 1.19)$	$4.85 (\pm 2.07)$	$13.7 (\pm 2.17)$	$5.79 (\pm 1.21)$	$4.48 \ (\pm 0.38)$	$11.5 (\pm 1.47)$	$11.1 \ (\pm 3.11)$
	FairWalk	0.20 (± 1.35)	0.08 (± 2.47)	$2.68 (\pm 0.86)$	$4.40 (\pm 0.64)$	$1.34 (\pm 1.03)$	$2.54 (\pm 1.90)$	$2.44 (\pm 1.01)$
	CrossWalk	$1.27 (\pm 0.96)$	$1.46 (\pm 1.10)$	4.59 (± 1.83)	$1.16 (\pm 0.60)$	$1.70 (\pm 0.50)$	$2.23 (\pm 0.79)$	$4.50 (\pm 1.77)$
	GNN	$8.99 (\pm 1.07)$	$17.2 (\pm 1.13)$	$23.4 (\pm 1.48)$	$19.2 (\pm 4.41)$	$6.85 (\pm 0.23)$	$12.3 (\pm 0.65)$	8.87 (± 0.22)
$\Delta_{ m EO}$	FairGNN	$\frac{0.29}{2.25}$ (± 1.06)	$9.84 (\pm 0.98)$	$9.31 (\pm 0.03)$	$1.62 (\pm 5.94)$	$3.60 (\pm 0.24)$	$6.26 (\pm 0.60)$	OOM
	NIFTY	$3.25 (\pm 0.47)$	$6.17 (\pm 0.88)$	$3.37 (\pm 0.45)$	9.89 (± 3.73)	3.14 (± 0.24)	0.70 (± 1.54)	6.63 (± 0.22)
	EDITS	OOM	OOM	$\frac{2.19}{10.4}$ (± 7.06)	7.74 (± 0.48)	$4.63 (\pm 0.53)$	OOM	OOM
	FairEdit	OOM	OOM	$10.1 (\pm 2.95)$	0.94 (± 0.24)	$7.04 (\pm 0.63)$	OOM	OOM
	FairVGNN	2.41 (± 2.09)	7.61 (± 0.85)	1.80 (± 0.10)	7.34 (± 0.39)	5.62 (± 0.45)	OOM	OOM
	DeepWalk	3.38 (± 1.48)	$0.21 (\pm 1.27)$	17.0 (± 4.27)	6.61 (± 0.96)	$0.68 (\pm 1.53)$	$0.95 (\pm 0.39)$	2.28 (± 1.14)
$\Delta_{ m Utility}$	FairWalk	4.04 (± 0.36)	$0.24 (\pm 0.40)$	$10.6 (\pm 1.05)$	2.33 (± 0.39)	1.95 (± 0.32)	$0.39 (\pm 0.32)$	$1.43 (\pm 0.10)$
	CrossWalk	$0.93 (\pm 0.26)$	2.86 (± 0.46)	16.8 (± 2.18)	9.27 (± 0.46)	$1.96 (\pm 0.16)$	5.10 (± 0.20)	$1.88 (\pm 0.12)$
	GNN	2.19 (± 1.09)	2.57 (± 1.21)	$\frac{2.90}{2.10}$ (± 1.19)	4.63 (± 2.63)	1.26 (± 2.66)	$0.33 (\pm 0.74)$	$1.60 (\pm 0.04)$
	FairGNN	0.18 (± 1.02)	0.02 (± 0.60)	9.19 (± 2.71)	1.42 (± 12.13)	$1.52 (\pm 2.96)$	3.72 (± 0.15)	OOM
	NIFTY	$0.64 (\pm 0.30)$	1.85 (± 0.82)	3.35 (± 3.25)	3.75 (± 0.98)	$4.60 (\pm 0.77)$	4.70 (± 0.09)	4.22 (± 0.16)
	EDITS	OOM	OOM	3.06 (± 5.28)	11.6 (± 2.25)	0.29 (± 0.17)	OOM	OOM
	FairEdit	OOM	OOM	0.44 (± 4.66)	$\frac{2.10}{6.71}$ (± 4.61)	2.75 (± 0.43)	OOM	OOM
	FairVGNN	6.79 (± 3.65)	$0.87 (\pm 0.64)$	$17.1 (\pm 0.68)$	6.71 (± 3.63)	$2.31 (\pm 6.06)$	OOM	OOM

Table 1: Performance comparison between different group fairness-aware graph learning models. The best ones are in **Bold**, and OOM represents out-of-memory.

Graph Learning Models. We implement all fairness-aware graph learning algorithms with their official open-source code. The graph learning models and their associated code links are listed below.

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- FairWalk: https://github.com/EnderGed/Fairwalk.
- CrossWalk: https://github.com/ahmadkhajehnejad/CrossWalk.
- FairGNN: https://github.com/EnyanDai/FairGNN.
- NIFTY: https://github.com/chirag126/nifty. Under MIT license.
- EDITS: https://github.com/yushundong/EDITS.
- FairEdit: https://github.com/royull/FairEdit.
- FairVGNN: https://github.com/yuwvandy/fairvgnn.
- InFoRM: https://github.com/jiank2/inform. Under MIT license.
- REDRESS: https://github.com/yushundong/REDRESS.
- *GUIDE*: https://github.com/mikesong724/GUIDE. Under MIT license.
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Hardware. We conduct all experiments with NVIDIA A6000 GPU (48GB memory), AMD EPYC CPU (2.87 GHz), and 512GB of RAM.

Metrics	Models	Pokec-z	Pokec-n	German Credit	Credit Defaulter	Recidivism	AMiner-S	AMiner-L
	GNN	$65.71 (\pm 0.54)$	$68.50 (\pm 0.77)$	67.13 (± 2.12)	74.43 (± 3.60)	84.55 (± 1.56)	90.06 (± 0.32)	93.12 (± 0.11
ACC	InFoRM	61.87 (± 3.75)	66.08 (± 3.66)	59.40 (± 5.09)	69.36 (± 5.21)	80.52 (± 5.94)	87.41 (± 5.61)	89.05 (± 5.21
ACC	REDRESS	62.35 (± 4.28)	$65.39 (\pm 4.62)$	63.08 (± 4.86)	68.12 (± 4.70)	77.77 (± 7.35)	OOM	OOM
	GUIDE	$\underline{62.86}~(\pm~5.54)$	$63.01 (\pm 5.63)$	$60.93 (\pm 3.91)$	$67.07 (\pm 6.67)$	$80.06 (\pm 5.20)$	$87.66 (\pm 5.46)$	OOM
	GNN	$66.50 (\pm 0.53)$	$67.62 (\pm 0.76)$	69.70 (± 3.48)	62.29 (± 4.85)	82.47 (± 1.41)	$82.23 (\pm 0.56)$	88.15 (± 0.11
AUC-ROC	InFoRM	60.53 (± 3.67)	$64.12 (\pm 4.12)$	63.61 (± 4.93)	62.72 (± 5.87)	79.66 (± 6.58)	69.75 (± 5.18)	73.72 (± 7.97
Score	REDRESS	$62.31 (\pm 6.52)$	$64.70 (\pm 4.88)$	63.79 (± 4.40)	64.39 (± 5.25)	69.52 (± 5.58)	OOM	OOM
	GUIDE	$\underline{63.55}~(\pm~3.62)$	$60.36 (\pm 4.43)$	$\underline{65.56}~(\pm 4.18)$	64.64 (± 3.86)	$75.09 (\pm 5.41)$	$\underline{73.34} \ (\pm \ 4.28)$	OOM
	GNN	$10.19 (\pm 0.26)$	14.27 (± 0.36)	32.97 (± 5.82)	20.51 (± 1.37)	8.56 (± 0.37)	7.24 (± 0.11)	6.57 (± 0.13)
•	InFoRM	$4.74 (\pm 0.50)$	6.62 (± 0.42)	34.15 (± 3.67)	25.97 (± 0.79)	7.57 (± 0.26)	$1.45 (\pm 0.24)$	$2.12 (\pm 0.39)$
$\Delta_{\rm SP}$	REDRESS	$16.35 (\pm 0.65)$	23.75 (± 1.58)	42.28 (± 1.62)	$10.84 (\pm 0.65)$	2.01 (± 0.58)	OOM	OOM
	GUIDE	$15.81 \ (\pm \ 0.22)$	$13.23 (\pm 0.67)$	$39.18 (\pm 1.78)$	$17.34 (\pm 1.07)$	$4.58 (\pm 0.44)$	$2.15 (\pm 0.41)$	OOM
	GNN	9.20 (± 0.87)	17.47 (± 0.47)	23.34 (± 7.89)	18.76 (± 1.29)	6.98 (± 1.20)	12.07 (± 1.77)	8.98 (± 0.47)
•	InFoRM	3.02 (± 0.24)	9.13 (± 0.43)	30.22 (± 3.38)	26.21 (± 1.11)	5.45 (± 0.33)	2.58 (± 0.21)	5.69 (± 0.26)
$\Delta_{\rm EO}$	REDRESS	$20.64 (\pm 0.28)$	26.01 (± 1.42)	37.57 (± 1.99)	10.38 (± 0.32)	0.10 (± 0.62)	OOM	OOM
	GUIDE	$10.93 \ (\pm \ 0.30)$	$20.45 \ (\pm 0.90)$	$36.74 (\pm 1.43)$	16.72 (± 1.50)	$2.29 (\pm 0.23)$	$3.26 (\pm 0.22)$	OOM
$\Delta_{ m Utility}$	GNN	2.37 (± 0.63)	2.68 (± 0.70)	1.44 (± 3.79)	4.84 (± 3.52)	0.12 (± 1.58)	0.99 (± 0.33)	1.03 (± 0.16)
	InFoRM	2.45 (± 4.76)	4.86 (± 5.50)	7.63 (± 5.54)	13.87 (± 4.04)	0.46 (± 5.82)	8.42 (± 7.59)	0.46 (± 7.31)
	REDRESS	8.65 (± 5.87)	1.85 (± 5.17)	8.14 (± 5.70)	7.79 (± 4.81)	4.60 (± 7.09)	OOM	OOM
	GUIDE	$1.73 (\pm 4.84)$	5.55 (± 4.23)	$12.63 (\pm 3.23)$	$10.99 \ (\pm 6.08)$	$1.84 (\pm 5.59)$	1.36 (± 5.53)	OOM
	GNN	2.5e6 (± 2e4)	5.5e3 (± 3e3)	3.6e3 (± 2e3)	1.3e4 (± 7e3)	1.2e7 (± 3e5)	2.2e6 (± 3e5)	3.2e7 (± 5e5)
B	InFoRM	9.1e2 (± 1e2)	3.4e3 (± 4e3)	$2.0e2 (\pm 7e2)$	5.2e1 (± 3e2)	4.7e3 (± 9e3)	9.7e3 (± 4e3)	9.8e4 (± 3e3)
DLipschitz	REDRESS	2.0e5 (± 1e4)	1.9e5 (± 2e4)	$7.0e3 (\pm 1e3)$	1.2e4 (± 3e3)	2.6e4 (± 6e3)	OOM	OOM
	GUIDE	1.8e3 (± 3e2)	$\underline{4.0e3}$ (± 6e2)	$6.4e3 (\pm 9e2)$	$\underline{4.2e3}$ (± 3e2)	$1.1e5 (\pm 1e4)$	$\underline{1.5e4}$ (± 7e3)	OOM
	GNN	44.56 (± 0.59)	37.01 (± 0.26)	31.42 (± 1.49)	39.01 (± 1.05)	15.31 (± 0.32)	$43.74 (\pm 0.70)$	37.75 (± 0.19
NDCC@k	InFoRM	48.78 (± 3.62)	44.09 (± 3.00)	35.89 (± 3.69)	37.11 (± 3.18)	$19.81 (\pm 1.74)$	38.85 (± 2.07)	33.34 (± 1.70)
NDCG@ĸ	REDRESS	54.30 (± 3.08)	48.53 (± 3.85)	42.82 (± 3.62)	42.74 (± 2.11)	25.30 (± 1.96)	OOM	OOM
	GUIDE	$\underline{49.02}~(\pm~2.72)$	$47.27 (\pm 4.72)$	$32.70 (\pm 2.02)$	37.38 (± 2.69)	$\underline{21.50}$ (± 2.18)	$\underline{39.16}(\pm2.26)$	OOM
	GNN	111.92 (± 0.81)	232.16 (± 24.2)	125.87 (± 11.1)	166.78 (± 36.1)	112.78 (± 1.29)	114.05 (± 1.17)	112.72 (± 1.2)
CDIF	InFoRM	$118.07 (\pm 10.2)$	$116.17 (\pm 5.65)$	136.94 (± 10.3)	160.62 (± 11.2)	$112.90 (\pm 8.66)$	$125.36 (\pm 11.4)$	127.84 (± 8.5
GDIF	REDRESS	$167.56 \ (\pm \ 7.12)$	$124.08 \ (\pm 10.8)$	139.98 (± 8.84)	163.84 (± 5.75)	$109.58 (\pm 7.33)$	OOM	OOM
	GUIDE	$108.75 (\pm 5.89)$	$110.58\;(\pm\;9.36)$	$112.35 (\pm 8.27)$	$149.97 (\pm 5.14)$	$104.17 (\pm 8.21)$	$\textbf{112.28}~(\pm~7.80)$	OOM

Table 2: Performance comparison between different individual fairness-aware graph learning models. The best ones are in **Bold**, and OOM represents out-of-memory.

Dependencies. We list all major packages and their associated versions in our implementation.

- python == 3.9.0
- pygdebias == 1.1.1
- torch == 1.12.0 + cu116
- torch-cluster == 1.6.0
- torch-geometric == 2.1.0
- cuda == 11.6
- pandas == 1.4.3
- numpy == 1.22.4
- networkx == 2.8.5
- dgl == 1.1.2 + cu116
- scikit-learn == 1.1.1
- scipy == 1.9.0

С SUPPLEMENTARY RESULTS & DISCUSSION

Supplementary Discussion on RQ1. We perform additional experiments on graph learning algo-rithms focusing on group fairness and present the results in Table 1 and Figure 1. According to the comprehensive empirical results, we have the consistent observation that different fairness-aware graph learning methods show different advantages in balancing utility and fairness. Specifically, we observe that GNN-based algorithms are among the highest-ranking methods (e.g., most top-ranked results come from GNN-based methods), which verifies the advantage of GNNs in achieving both utility and fairness objectives due to their exceptional fitting ability. In addition, fairness-aware shallow embedding methods achieve the best performance with respect to fairness, especially on the



text, which demonstrate the consistency over a wide range of datasets and metrics. 195 196 Supplementary Discussion on RQ3. We further discuss RQ3 based on the additional results in 197 Table 1 and Table 2. Specifically, we find that shallow embedding methods and GNN-based methods excel on different fairness metrics, which also implies a struggle for a balance between different 199 fairness metrics. This observation align with the finding in the main text, which demonstrate the consistency over a wide range of datasets and metrics.

201 Supplementary Discussion on RQ4. We present additional results on the computational efficiency 202 of the collected fairness-aware graph learning methods in Figure 2. We found that fairness-aware 203 graph learning methods generally sacrifice efficiency. Specifically, GNN-based fairness-aware 204 graph learning algorithms exhibit a clear sacrifice on efficiency, which can be attributed to their 205 computationally expensive optimization strategy. Meanwhile, algorithms based on shallow embedding 206 methods only marginally sacrifice efficiency, which is resulted from the marginal improvement of additional computation burden in the optimization process compared to those GNN-based ones. All 207 observations above align with the finding in the main text, which demonstrate the consistency over a 208 wide range of datasets. 209

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D **BROADER IMPACTS**

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213 This paper presents a comprehensive benchmark for fairness-aware graph learning, which provides extensive evaluation and comparison of existing fairness-aware graph learning algorithms. As a result, 214 we provide insights and guidance to empower better fairness-aware graph learning algorithms in the 215 future, and help facilitate broader applications such as financial lending (Song et al., 2023; Li et al.,



Figure 2: The comparison of AUC-ROC and running time across different fairness-aware graph learning methods on different datasets.

2020), healthcare decision making (Dai et al.) 2022; Anderson & Visweswaran, 2024), and policy making (He et al., 2024). At the same time, we note that our work does not have significant negative social impacts we feel necessary to mention here.

References

- Joshua W Anderson and Shyam Visweswaran. Algorithmic individual fairness for healthcare: A scoping review. *medRxiv*, pp. 2024–03, 2024.
- Enyan Dai, Tianxiang Zhao, Huaisheng Zhu, Junjie Xu, Zhimeng Guo, Hui Liu, Jiliang Tang, and Suhang Wang. A comprehensive survey on trustworthy graph neural networks: Privacy, robustness, fairness, and explainability. *arXiv preprint arXiv:2204.08570*, 2022.
- Erhu He, Yiqun Xie, Alexander Sun, Jacob Zwart, Jie Yang, Zhenong Jin, Yang Wang, Hassan Karimi, and Xiaowei Jia. Fair graph learning using constraint-aware priority adjustment and graph masking in river networks. In *Proceedings of the AAAI Conference on Artificial Intelligence*, volume 38, pp. 22087–22095, 2024.
- Kareem L Jordan and Tina L Freiburger. The effect of race/ethnicity on sentencing: Examining sentence type, jail length, and prison length. *Journal of Ethnicity in Criminal Justice*, 13(3): 179–196, 2015.
- Yanying Li, Yue Ning, Rong Liu, Ying Wu, and Wendy Hui Wang. Fairness of classification using users' social relationships in online peer-to-peer lending. In *Companion Proceedings of the Web Conference 2020*, pp. 733–742, 2020.
- Kolby Nottingham Markelle Kelly, Rachel Longjohn. The uci machine learning repository. URL
 https://archive.ics.uci.edu.
- Zixing Song, Yuji Zhang, and Irwin King. Towards fair financial services for all: A temporal gnn approach for individual fairness on transaction networks. In *Proceedings of the 32nd ACM International Conference on Information and Knowledge Management*, pp. 2331–2341, 2023.

270 271 272	Lubos Takac and Michal Zabovsky. Data analysis in public social networks. In International scientific conference and international workshop present day trends of innovations, volume 1, 2012.
273	Huaiyu Wan, Yutao Zhang, Jing Zhang, and Jie Tang. Aminer: Search and mining of academic social networks. <i>Data Intelligence</i> 1(1):58–76, 2019
274	
275 276	I-Cheng Yeh and Che-hui Lien. The comparisons of data mining techniques for the predictive accuracy of probability of default of credit card clients. <i>Expert systems with applications</i> 36(2):
277	2473_2480_2009
278	2475 2400, 2007.
279	
280	
281	
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