
Towards finding consensus about similarity of symbolic encodings associated with concepts between LLMs and human brain

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Abstract

1 Large Language Models (LLMs) and Multimodal Large Language Models (LLMs)
2 have shown unbelievable improvement in performance in various Natural Language
3 Understanding and Multimodal understanding tasks. The recent works evaluate
4 representations, alignment, various of types of reasoning, grounding - text, video
5 and audio inputs - over the tasks evaluating LLMs and MLLMs. The recent
6 LLMs with "reasoning" or "thinking" phases generating reasoning traces (Chain-of-
7 Thoughts or CoTs), enacting inference-time decision-making by "thinking" before
8 generating a final response Feng et al. [2025] have shown new directions inspired
9 from Kahneman [2011]. This approach leverages Reinforcement-Learning based
10 finetuning along with rewards signals from variants of reward models while scaling
11 up test-time compute. This paper re-introduces the previously examined individual
12 findings from few different works Silver and Mitchell [2023] Pavlick [2023], Shani
13 et al. [2025], Geh et al. [2024b], Opedal et al. [2024], Saparov and He [2023] and
14 more. This paper attempts to find if there is a common consensus about similarity
15 of symbolic encodings between LLMs and human brain. The symbolic encodings
16 refer to alignment of symbols (words and sentences) w.r.t concepts, conceptual
17 categories and conceptual structures.

18 1 Introduction

19 Earliest Connectionist systems have been developed from the idea to represent information in the form
20 of the tensor product vectors to capture the representations of symbolic structures Smolensky [1987]
21 Piantadosi et al. [2024]. The goal of Cognitive architectures is to replicate human cognition Saparov
22 and Mitchell [2022]. However recent studies that attempt to answer "what are the Large Language
23 Models (LLMs) supposed to model" Blank [2023] suggest lack of consensus from perspectives from
24 within cognitive sciences studies. Recent cognitive science studies note that the LLMs operate at
25 subsymbolic level, similar to humans, as reiterated from Silver and Mitchell [2023] that symbols are
26 characterizations of subsymbolic processes of thought and this in itself makes symbols crucial for
27 intelligent systems. There is a greater emphasis on LLMs capturing the human-like encodings of
28 symbolic and conceptual information, and their relevance to reasoning.

29 Large Language Models (LLMs) have shown exceptional improvement in reasoning and semantic
30 understanding, on Natural Language Understanding tasks OpenAI et al. [2024b]. LLMs also expand
31 their language learning capabilities to translate/convert a natural language textual input into a pro-
32 gramming languages such as C, Java and Python Brown et al. [2020]. Saparov and He [2023] and
33 Olausson et al. [2023] involving First Order Logic aligned methods suggest LLMs fail at planning
34 stages and that they suffer from "fallacy of the converse" in Natural Language Inference (NLI) tasks.
35 Vision Large Language Models (VLLMs) have extended the capabilities over Multimodal reasoning

36 tasks such as Visual Question Answering (VQA), Vision Language Retrieval (VLR) and Natural
37 Language for Visual Reasoning (NLVR) than the other Multimodal AI systems Manzoor et al. [2023].
38 More recent GPT-4o can also effectively process the textual, visual and audio inputs OpenAI et al.
39 [2024a]. The recent work to evaluate if LLMs can learn low-resource languages using In-Context
40 Learning (Zhang et al. [2024] and creating Constructed Languages by decomposing language design
41 into phases using an LLM pipeline Alper et al. [2025] demonstrate advancement in new language
42 learning and creation (*known as Computational conlanging*) tasks. Grounding conceptual spaces
43 in language-only models Patel and Pavlick [2022] has also been evaluated while Multimodal Large
44 Language Models (MLLMs) struggle with OCR-scanned documents for visual text grounding Li et al.
45 [2025] though MLLMs have improved on multi-modal understanding tasks Zhao et al. [2023]. With
46 LLMs' and MLLMs' increasing availability to public and subsequent rise in the usage by the public,
47 recent works such as enabling unbiased discourse with mediation during democratic deliberation
48 Tessler et al. [2024], evaluation of Theory-of-Mind (ToM) concepts via social reasoning capabilities
49 in LLMs Gandhi et al. [2023], implicature-based inference in pragmatic understanding Ruis et al.
50 [2023], human-like affective cognition in LLMs Gandhi et al. [2024] have evaluated high-level
51 cognitive behaviors and various interesting applications of LLMs.

52 **2 Similarity of symbolic encodings between LLMs and Humans**

53 To discuss about the similarity of symbolic encodings that focus on concepts, between humans and
54 LLMs, I bring together few works to attempt to verify similarity of symbolic encodings and also
55 present a potential counter argument.

56 Recent works on the role of symbols Silver and Mitchell [2023] hypothesize symbols characterize
57 sub-symbolic processes that help to communicate a thought. Silver and Mitchell [2023] distinguishes
58 between symbolic representations and concept representations and proposes and asks some key
59 Neuro-Symbolic questions. Silver and Mitchell [2023] attempts to question if symbols play an
60 internal role for the agent beyond external communication such as contributing towards agent's
61 reasoning processes in learning, memory storage and retrieval. For context, conrep (concept's neural
62 representation) is agent's internal neural activity that encodes concept referred by a symbol and
63 symrep (symbol's neural representation) agent's internal neural activity that encodes symbol. Silver
64 and Mitchell [2023] suggests that concept representations are associated with a symbol - where a
65 symbol can be an English word, Portuguese word or a picture and further describes properties of LLMs
66 by drawing analogy between symreps and conreps. Some of the properties of LLMs as noted in
67 Silver and Mitchell [2023] suggests LLMs represent conreps of words and sentences (where words,
68 sentences are symbols) in the form of vectors of neural activations, such as Word embeddings that
69 capture the meaning of the words which may be used to predict the neural activation of individual
70 words in human brain. The authors also suggest the similarity of symbol encodings from LLMs to
71 humans and viceversa. LLMs process each word in the input (symbols) and generate an associated
72 conrep (the neural activation) by learning which other words in the input it needs to give "attention"
73 to, a mechanism used by an autoregressive model of word sequences. The transformer architecture
74 explores which other words in the textual input are most relevant to modify the conrep associated with
75 current word and then determines how to modify conrep (add's a learned vector to current word's
76 conrep). Other properties of LLMs are that they learn to modify context-free conreps associated with
77 individual words by taking into account the specific context of the sentence containing the word. I
78 present some of the findings from Silver and Mitchell [2023] from comparison between human brain
79 neural activations to that of LLMs' for symbolic and neural representations, as follows:

- 80 1. Consistent encodings of symbols upon reading the same word leads to "repeatable distributed
81 patterns of neural activity/vectors of neural activity" Silver and Mitchell [2023].
- 82 2. Encodings of symbols focus on concepts, meaning patterns of neural activity associated with
83 symbol stimuli (such as "cat") describe its associated concept (conrep), not just its symbol
84 (symrep), including sound of the word cat, the images of cat, even sense of touching a cat.

85 **2.1 Text-only LLMs and similarity of symbolic encodings**

86 Connecting the dots from Silver and Mitchell [2023] with findings from Pavlick [2023] suggests
87 that text-only LLMs, despite lack of groundings, are able to grasp conceptual structure of language.
88 Grounding defined as "the ability to tie a word for which they have learned a representation to its

89 referent in the non-linguistic world" Pavlick [2023]. The analyses and emphasis on symbols and
90 grounding in Language Models Pavlick [2023] in text-only LLMs suggests conceptual structures are
91 captured and how they can be leveraged for mapping LLMs to grounded conceptual spaces, even
92 without built-in multi-modal understanding in LLMs such as in GPT-2 and GPT-3. Drawing upon
93 this idea, the contextual information and conceptual structures learnt by the words such as color or
94 direction, indicate that extent to which conceptual structure of LLMs reflects the conceptual structure
95 of non-linguistic world. For example, the inputs are in textual format containing what "left" means
96 in a textual description of gridworld. A key finding of Pavlick [2023] is that LLMs tend to do well on
97 these example tasks even in isomorphic rotated worlds and they are not using naive memorisation to
98 succeed in such tasks. Further authors suggest that such learnt conceptual structure can be used to
99 ground by leveraging data-efficient approaches. The authors note the limitation of text-only LLMs
100 that for complex visual inputs grounding, a textual input depiction is unlikely to have required grasp
101 of complex conceptual structures inherent within such visual inputs (non-linguistic world).

102 Combining one of the key findings from Silver and Mitchell [2023], the question is: do the findings
103 from Pavlick [2023] that linguistic world models tend to capture conceptual structures, might suggest
104 encodings focus on concepts to describe symbol stimuli such as "left" describe its associated concepts
105 in the textual gridworld and its related concepts of "right" in the same gridworld?

106 2.2 Using compression-meaning tradeoff evaluation as a measure for comparing similarity of 107 symbolic encodings

108 Another interesting work Shani et al. [2025] discussed on how humans and LLMs trade-off between
109 compression and preservation of semantic meaning and explores if LLMs develop conceptual struc-
110 tures analogous to human cognition. The authors further suggest human concepts balance semantic
111 richness and cognitive manageability suggestive of Information compression. This resonates with the
112 ideas from Silver and Mitchell [2023] that suggest symbols are characterization of our thoughts that
113 allows to explain subsymbolic thinking to ourselves and others (synonymous to "reasoning traces",
114 "thinking" phases in LLMs) and act as constraints for inference and learning about the world. There
115 are three key research questions in Shani et al. [2025] that ask 1) "how do emergent concepts in LLMs
116 align with human-defined conceptual categories?" Shani et al. [2025] referred to as *representational*
117 *compactness*, 2) "do LLMs and humans exhibit similar internal geometric structures within these
118 concepts?" Shani et al. [2025] *semantic preservation* and 3) "how do humans and LLMs differ in
119 their strategies for balancing meaning preservation and information compression?" Shani et al. [2025]
120 referred as "*compression-meaning tradeoff*" *measure*. The authors further draw on the Information
121 theoretical constructs such as Rate-Distortion measure Theory (RDT) and Information Bottleneck
122 principle (IB), where rate R is the representational complexity needed to represent source X as C
123 where R is subjected to maximum distortion D (fidelity loss, w.r.t semantic preservation). The goal
124 is to optimize $R + \lambda D$ for evaluation of representational efficiency. More details about how IB, RDT
125 and objective are formulated in A.2. The findings pertaining to semantic preservation suggest there is
126 above-chance alignment with human conceptual categories and do not fully mirror nuanced prototype
127 structures evident in human typicality judgments. The typicality here refers to "robin" as a "typical
128 bird", "bat" as atypical (because it is a mammal within the context of comparative human conceptual
129 category of "bird") Shani et al. [2025]. Lastly the compression-meaning tradeoff evaluation results
130 suggests superior information-theoretic efficiency in LLMs' conceptual representations in compari-
131 son to human conceptual structures, which strongly suggests divergence in the strategies used for
132 balancing informational compression with semantic meaning. This suggests that there is similarity
133 in alignments with human conceptual categories and ability to recover human-like categories from
134 their item embeddings, though both employ different strategies for compression-semantic balance.
135 The idea focuses using information-theoretic measures for measuring and comparing compression-
136 semantic tradeoffs between both humans and LLMs for alignment with human conceptual categories,
137 which is a different method to that of methods used in Silver and Mitchell [2023] and Pavlick [2023].

138 Based on the findings from Silver and Mitchell [2023] there seems to be agreement with that of the
139 findings in Shani et al. [2025] that there is similarity and presence of alignment between human
140 conceptual categories with that of items/tokens as symbols/symbol stimuli (by information-theoretic
141 measures), though there is divergence between the strategies employed by LLMs and humans for
142 compression-meaning tradeoffs exists. There seems to be potential consensus that LLMs do tend to
143 capture conceptual structures relevant to symbols/tokens for current token embeddings, similar to
144 that of humans.

145 2.3 Works regarding hallucinations, cognitive biases, logical reasoning and more

146 There are several works examining the presence of cognitive biases Gupta et al. [2023] Opedal et al.
147 [2024], logical fallacies Lalwani et al. [2024] addressing hallucinations, Li et al. [2024] Gu et al.
148 [2025] reviews LLMs as judges, RAG-based methods Fan et al. [2024], Feng et al. [2024] that suggest
149 LLMs replicate inherent biases, beliefs of the humans. Recent works on Wang et al. [2024] suggest
150 various aspects of human-centric perspectives and analyze cognition at individual and collective
151 spaces respectively. The evaluation of deductive reasoning through First order logic based tasks to
152 derive and evaluate conclusions from logical premises Saparov and He [2023] which suggests room
153 for improvement in planning for LLMs. These works also have potential to resonate similarity of
154 symbolic encodings, since humans themselves suffer from these potential drawbacks, LLMs resonate
155 these common drawbacks from the humans Krawczyk [2017].

156 3 Alternative Views

157 3.1 Insights from Non-Canonical tokenization for similarity of symbolic encodings

158 Another recent work Geh et al. [2024a] examines tokenization encodes text into canonical tokens.
159 The authors discuss importance of Byte-Pair Encodings (BPE) commonly used in LLMs which
160 repeatedly merges most frequent byte pair of tokens into the new token into merge table and each
161 one of the entries are assigned priorities. The results are further processed by splitting the string into
162 constituent characters, then combines the pair of tokens that have highest priority merge rule which
163 results in canonical tokenization. The BPE method with dropout adds more mass to non-canonical
164 tokenizations. The key finding from the authors are that majority of non-canonical tokenizations
165 belong to non-English cases with large portions consisting of code and other language tokens which
166 is word-dependent. Some of the non-canonical tokenizations contain grammatically correct words,
167 but longer texts seem to contain some mass attributed to non-canonical tokenizations. The authors
168 extend this interesting finding to verify that instead of using single tokenization, if aggregating over
169 all tokenizations each weighted by their probability, then to compute marginal probability of the
170 string x . Their study showed there is most of the probability mass over canonical tokenization. These
171 findings and further experimentation showed improvement in accuracy for non-canonical tokenization
172 concluding there is signal in the *non-canonical tokenization* space suggesting they retain meaningful
173 information.

174 At the language level, the findings from Geh et al. [2024a] show that non-canonical tokenizations
175 capture more meaningful information, under controlled configurations for downstream tasks such as
176 Question and Answer datasets (Q&A). How can we map non-canonical tokens that seem to capture
177 meaningful information in Q&A tasks with that of symreps and conreps from human brain imaging
178 in an analogous Q&A task ? Does this suggest that the canonical vs non-canonical tokenization
179 techniques can lead to vectors of activations until "symbol stimuli" in LLMs? Example: $[B, a, t]$
180 are canonical tokens seen by an LLM during tokenization until LLM searches and finds relevant
181 tokenizations and it's associated concept of "Bat", within the context (whether it's a baseball bat
182 or "Bat" as a "mammal"), while humans receive symbol stimuli for *Bat* as an English word, or as
183 a picture based on symreps and conreps respectively. Do these present similarities of encodings of
184 symbols at conceptual level or do we need to find another meeting point to compare the similarities
185 of symbolic encodings ?

186 3.2 Conclusion

187 This work broadly studies key works for consensus towards similarity of symbolic encodings between
188 LLMs and human brain, by drawing inspiration from Silver and Mitchell [2023]. Combining the
189 aforementioned analyses, there are sufficient evidences that suggest similarity exists. Two contrasting
190 research questions emerge that - to what extent is the similarity acceptable VS to what extent is the
191 dissimilarity desirable VS domain/task-based expert human cognition (finetuned) VS general human
192 cognition (pretrained) - seems to be restricting where to draw the line for consensus over similarity of
193 symbolic encodings between LLMs and human brain.

194 **References**

- 195 Morris Alper, Moran Yanuka, Raja Giryes, and Gašper Beguš. Conlangcrafter: Constructing
196 languages with a multi-hop llm pipeline. *arXiv preprint arXiv:2508.06094*, 2025.
- 197 Idan A Blank. What are large language models supposed to model? *Trends in Cognitive Sciences*, 27
198 (11):987–989, 2023.
- 199 Tom B. Brown, Benjamin Mann, Nick Ryder, Melanie Subbiah, Jared Kaplan, Prafulla Dhariwal,
200 Arvind Neelakantan, Pranav Shyam, Girish Sastry, Amanda Askell, Sandhini Agarwal, Ariel
201 Herbert-Voss, Gretchen Krueger, Tom Henighan, Rewon Child, Aditya Ramesh, Daniel M. Ziegler,
202 Jeffrey Wu, Clemens Winter, Christopher Hesse, Mark Chen, Eric Sigler, Mateusz Litwin, Scott
203 Gray, Benjamin Chess, Jack Clark, Christopher Berner, Sam McCandlish, Alec Radford, Ilya
204 Sutskever, and Dario Amodei. Language models are few-shot learners, 2020. URL <https://arxiv.org/abs/2005.14165>.
- 206 Wenqi Fan, Yujuan Ding, Liangbo Ning, Shijie Wang, Hengyun Li, Dawei Yin, Tat-Seng Chua, and
207 Qing Li. A survey on rag meeting llms: Towards retrieval-augmented large language models. In
208 *Proceedings of the 30th ACM SIGKDD conference on knowledge discovery and data mining*, pages
209 6491–6501, 2024.
- 210 Shangbin Feng, Weijia Shi, Yike Wang, Wenxuan Ding, Vidhisha Balachandran, and Yulia Tsvetkov.
211 Don’t hallucinate, abstain: Identifying llm knowledge gaps via multi-llm collaboration. *arXiv*
212 *preprint arXiv:2402.00367*, 2024.
- 213 Sicheng Feng, Gongfan Fang, Xinyin Ma, and Xinchao Wang. Efficient reasoning models: A survey,
214 2025. URL <https://arxiv.org/abs/2504.10903>.
- 215 Kanishk Gandhi, Jan-Philipp Fränken, Tobias Gerstenberg, and Noah Goodman. Understanding
216 social reasoning in language models with language models. *Advances in Neural Information*
217 *Processing Systems*, 36:13518–13529, 2023.
- 218 Kanishk Gandhi, Zoe Lynch, Jan-Philipp Fränken, Kayla Patterson, Sharon Wambu, Tobias Gersten-
219 berg, Desmond C. Ong, and Noah D. Goodman. Human-like affective cognition in foundation
220 models, 2024. URL <https://arxiv.org/abs/2409.11733>.
- 221 Renato Lui Geh, Honghua Zhang, Kareem Ahmed, Benjie Wang, and Guy Van den Broeck. Where is
222 the signal in tokenization space? *arXiv preprint arXiv:2408.08541*, 2024a.
- 223 Renato Lui Geh, Honghua Zhang, Kareem Ahmed, Benjie Wang, and Guy Van den Broeck. Where is
224 the signal in tokenization space?, 2024b. URL <https://arxiv.org/abs/2408.08541>.
- 225 Jiawei Gu, Xuhui Jiang, Zhichao Shi, Hexiang Tan, Xuehao Zhai, Chengjin Xu, Wei Li, Yinghan Shen,
226 Shengjie Ma, Honghao Liu, Saizhuo Wang, Kun Zhang, Yuanzhuo Wang, Wen Gao, Lionel Ni,
227 and Jian Guo. A survey on llm-as-a-judge, 2025. URL <https://arxiv.org/abs/2411.15594>.
- 228 Shashank Gupta, Vaishnavi Shrivastava, Ameet Deshpande, Ashwin Kalyan, Peter Clark, Ashish
229 Sabharwal, and Tushar Khot. Bias runs deep: Implicit reasoning biases in persona-assigned llms.
230 *arXiv preprint arXiv:2311.04892*, 2023.
- 231 Daniel Kahneman. *Thinking, fast and slow*. macmillan, 2011.
- 232 Daniel Krawczyk. *Reasoning: The neuroscience of how we think*. Academic Press, 2017.
- 233 Abhinav Lalwani, Lovish Chopra, Christopher Hahn, Caroline Trippel, Zhijing Jin, and Mrinmaya
234 Sachan. Nl2fol: translating natural language to first-order logic for logical fallacy detection. *arXiv*
235 *preprint arXiv:2405.02318*, 2024.
- 236 Haitao Li, Qian Dong, Junjie Chen, Huixue Su, Yujia Zhou, Qingyao Ai, Ziyi Ye, and Yiqun
237 Liu. Llms-as-judges: A comprehensive survey on llm-based evaluation methods, 2024. URL
238 <https://arxiv.org/abs/2412.05579>.
- 239 Ming Li, Ruiyi Zhang, Jian Chen, Jiuxiang Gu, Yufan Zhou, Franck Dernoncourt, Wanrong Zhu,
240 Tianyi Zhou, and Tong Sun. Towards visual text grounding of multimodal large language model,
241 2025. URL <https://arxiv.org/abs/2504.04974>.

- 242 Muhammad Arslan Manzoor, Sarah Albarri, Ziting Xian, Zaiqiao Meng, Preslav Nakov, and Shang-
 243 song Liang. Multimodality representation learning: A survey on evolution, pretraining and its
 244 applications. *ACM Transactions on Multimedia Computing, Communications and Applications*, 20
 245 (3):1–34, 2023.
- 246 Theo X Olausson, Alex Gu, Benjamin Lipkin, Cedegao E Zhang, Armando Solar-Lezama, Joshua B
 247 Tenenbaum, and Roger Levy. Linc: A neurosymbolic approach for logical reasoning by combining
 248 language models with first-order logic provers. *arXiv preprint arXiv:2310.15164*, 2023.
- 249 Andreas Opedal, Alessandro Stolfo, Haruki Shirakami, Ying Jiao, Ryan Cotterell, Bernhard
 250 Schölkopf, Abulhair Saparov, and Mrinmaya Sachan. Do language models exhibit the same
 251 cognitive biases in problem solving as human learners?, 2024. URL [https://arxiv.org/abs/](https://arxiv.org/abs/2401.18070)
 252 [2401.18070](https://arxiv.org/abs/2401.18070).
- 253 OpenAI, :, Aaron Hurst, Adam Lerer, Adam P. Goucher, Adam Perelman, Aditya Ramesh, Aidan
 254 Clark, AJ Ostrow, Akila Welihinda, Alan Hayes, Alec Radford, Aleksander Mądry, Alex Baker-
 255 Whitcomb, Alex Beutel, Alex Borzunov, Alex Carney, Alex Chow, Alex Kirillov, Alex Nichol, Alex
 256 Paino, Alex Renzin, Alex Tachard Passos, Alexander Kirillov, Alexi Christakis, Alexis Conneau,
 257 Ali Kamali, Allan Jabri, Allison Moyer, Allison Tam, Amadou Crookes, Amin Tootoochian,
 258 Amin Tootoonchian, Ananya Kumar, Andrea Vallone, Andrej Karpathy, Andrew Braunstein,
 259 Andrew Cann, Andrew Codispoti, Andrew Galu, Andrew Kondrich, Andrew Tulloch, Andrey
 260 Mishchenko, Angela Baek, Angela Jiang, Antoine Pelisse, Antonia Woodford, Anuj Gosalia,
 261 Arka Dhar, Ashley Pantuliano, Avi Nayak, Avital Oliver, Barret Zoph, Behrooz Ghorbani, Ben
 262 Leimberger, Ben Rossen, Ben Sokolowsky, Ben Wang, Benjamin Zweig, Beth Hoover, Blake
 263 Samic, Bob McGrew, Bobby Spero, Bogo Gertler, Bowen Cheng, Brad Lightcap, Brandon
 264 Walkin, Brendan Quinn, Brian Guarraci, Brian Hsu, Bright Kellogg, Brydon Eastman, Camillo
 265 Lugaresi, Carroll Wainwright, Cary Bassin, Cary Hudson, Casey Chu, Chad Nelson, Chak Li,
 266 Chan Jun Shern, Channing Conger, Charlotte Barette, Chelsea Voss, Chen Ding, Cheng Lu,
 267 Chong Zhang, Chris Beaumont, Chris Hallacy, Chris Koch, Christian Gibson, Christina Kim,
 268 Christine Choi, Christine McLeavey, Christopher Hesse, Claudia Fischer, Clemens Winter, Coley
 269 Czarnecki, Colin Jarvis, Colin Wei, Constantin Koumouzelis, Dane Sherburn, Daniel Kappler,
 270 Daniel Levin, Daniel Levy, David Carr, David Farhi, David Mely, David Robinson, David Sasaki,
 271 Denny Jin, Dev Valladares, Dimitris Tsipras, Doug Li, Duc Phong Nguyen, Duncan Findlay,
 272 Edede Oiwoh, Edmund Wong, Ehsan Asdar, Elizabeth Proehl, Elizabeth Yang, Eric Antonow, Eric
 273 Kramer, Eric Peterson, Eric Sigler, Eric Wallace, Eugene Brevdo, Evan Mays, Farzad Khorasani,
 274 Felipe Petroski Such, Filippo Raso, Francis Zhang, Fred von Lohmann, Freddie Sulit, Gabriel Goh,
 275 Gene Oden, Geoff Salmon, Giulio Starace, Greg Brockman, Hadi Salman, Haiming Bao, Haitang
 276 Hu, Hannah Wong, Haoyu Wang, Heather Schmidt, Heather Whitney, Heewoo Jun, Hendrik
 277 Kirchner, Henrique Ponde de Oliveira Pinto, Hongyu Ren, Huiwen Chang, Hyung Won Chung,
 278 Ian Kivlichan, Ian O’Connell, Ian O’Connell, Ian Osband, Ian Silber, Ian Sohl, Ibrahim Okuyucu,
 279 Ikai Lan, Ilya Kostrikov, Ilya Sutskever, Ingmar Kanitscheider, Ishaan Gulrajani, Jacob Coxon,
 280 Jacob Menick, Jakub Pachocki, James Aung, James Betker, James Crooks, James Lennon, Jamie
 281 Kiros, Jan Leike, Jane Park, Jason Kwon, Jason Phang, Jason Teplitz, Jason Wei, Jason Wolfe,
 282 Jay Chen, Jeff Harris, Jenia Varavva, Jessica Gan Lee, Jessica Shieh, Ji Lin, Jiahui Yu, Jiayi
 283 Weng, Jie Tang, Jieqi Yu, Joanne Jang, Joaquin Quinonero Candela, Joe Beutler, Joe Landers,
 284 Joel Parish, Johannes Heidecke, John Schulman, Jonathan Lachman, Jonathan McKay, Jonathan
 285 Uesato, Jonathan Ward, Jong Wook Kim, Joost Huizinga, Jordan Sitkin, Jos Kraaijeveld, Josh
 286 Gross, Josh Kaplan, Josh Snyder, Joshua Achiam, Joy Jiao, Joyce Lee, Juntang Zhuang, Justyn
 287 Harriman, Kai Fricke, Kai Hayashi, Karan Singhal, Katy Shi, Kavin Karthik, Kayla Wood, Kendra
 288 Rimbach, Kenny Hsu, Kenny Nguyen, Keren Gu-Lemberg, Kevin Button, Kevin Liu, Kiel Howe,
 289 Krithika Muthukumar, Kyle Luther, Lama Ahmad, Larry Kai, Lauren Itow, Lauren Workman,
 290 Leher Pathak, Leo Chen, Li Jing, Lia Guy, Liam Fedus, Liang Zhou, Lien Mamitsuka, Lilian Weng,
 291 Lindsay McCallum, Lindsey Held, Long Ouyang, Louis Feувrier, Lu Zhang, Lukas Kondraciuk,
 292 Lukasz Kaiser, Luke Hewitt, Luke Metz, Lyric Doshi, Mada Aflak, Maddie Simens, Madelaine
 293 Boyd, Madeleine Thompson, Marat Dukhan, Mark Chen, Mark Gray, Mark Hudnall, Marvin
 294 Zhang, Marwan Aljubeih, Mateusz Litwin, Matthew Zeng, Max Johnson, Maya Shetty, Mayank
 295 Gupta, Meghan Shah, Mehmet Yatbaz, Meng Jia Yang, Mengchao Zhong, Mia Glaese, Mianna
 296 Chen, Michael Janner, Michael Lampe, Michael Petrov, Michael Wu, Michele Wang, Michelle
 297 Fradin, Michelle Pokrass, Miguel Castro, Miguel Oom Temudo de Castro, Mikhail Pavlov, Miles
 298 Brundage, Miles Wang, Minal Khan, Mira Murati, Mo Bavarian, Molly Lin, Murat Yesildal, Nacho

299 Soto, Natalia Gimelshein, Natalie Cone, Natalie Staudacher, Natalie Summers, Natan LaFontaine,
300 Neil Chowdhury, Nick Ryder, Nick Stathas, Nick Turley, Nik Tezak, Niko Felix, Nithanth Kudige,
301 Nitish Keskar, Noah Deutsch, Noel Bundick, Nora Puckett, Ofir Nachum, Ola Okelola, Oleg Boiko,
302 Oleg Murk, Oliver Jaffe, Olivia Watkins, Olivier Godement, Owen Campbell-Moore, Patrick
303 Chao, Paul McMillan, Pavel Belov, Peng Su, Peter Bak, Peter Bakkum, Peter Deng, Peter Dolan,
304 Peter Hoeschele, Peter Welinder, Phil Tillet, Philip Pronin, Philippe Tillet, Prafulla Dhariwal,
305 Qiming Yuan, Rachel Dias, Rachel Lim, Rahul Arora, Rajan Troll, Randall Lin, Rapha Gontijo
306 Lopes, Raul Puri, Reah Miyara, Reimar Leike, Renaud Gaubert, Reza Zamani, Ricky Wang, Rob
307 Donnelly, Rob Honsby, Rocky Smith, Rohan Sahai, Rohit Ramchandani, Romain Huet, Rory
308 Carmichael, Rowan Zellers, Roy Chen, Ruby Chen, Ruslan Nigmatullin, Ryan Cheu, Saachi
309 Jain, Sam Altman, Sam Schoenholz, Sam Toizer, Samuel Miserendino, Sandhini Agarwal, Sara
310 Culver, Scott Ethersmith, Scott Gray, Sean Grove, Sean Metzger, Shamez Hermani, Shantanu
311 Jain, Shengjia Zhao, Sherwin Wu, Shino Jomoto, Shirong Wu, Shuaiqi, Xia, Sonia Phene, Spencer
312 Papay, Srinivas Narayanan, Steve Coffey, Steve Lee, Stewart Hall, Suchir Balaji, Tal Broda, Tal
313 Stramer, Tao Xu, Tarun Gogineni, Taya Christianson, Ted Sanders, Tejal Patwardhan, Thomas
314 Cunningham, Thomas Degry, Thomas Dimson, Thomas Raoux, Thomas Shadwell, Tianhao
315 Zheng, Todd Underwood, Todor Markov, Toki Sherbakov, Tom Rubin, Tom Stasi, Tomer Kaftan,
316 Tristan Heywood, Troy Peterson, Tyce Walters, Tyna Eloundou, Valerie Qi, Veit Moeller, Vinnie
317 Monaco, Vishal Kuo, Vlad Fomenko, Wayne Chang, Weiyi Zheng, Wenda Zhou, Wesam Manassra,
318 Will Sheu, Wojciech Zaremba, Yash Patil, Yilei Qian, Yongjik Kim, Youlong Cheng, Yu Zhang,
319 Yuchen He, Yuchen Zhang, Yujia Jin, Yunxing Dai, and Yury Malkov. Gpt-4o system card, 2024a.
320 URL <https://arxiv.org/abs/2410.21276>.

321 OpenAI, Josh Achiam, Steven Adler, Sandhini Agarwal, Lama Ahmad, Ilge Akkaya, Florencia Leoni
322 Aleman, Diogo Almeida, Janko Altenschmidt, Sam Altman, Shyamal Anadkat, Red Avila, Igor
323 Babuschkin, Suchir Balaji, Valerie Balcom, Paul Baltescu, Haiming Bao, Mohammad Bavarian,
324 Jeff Belgum, Irwan Bello, Jake Berdine, Gabriel Bernadett-Shapiro, Christopher Berner, Lenny
325 Bogdonoff, Oleg Boiko, Madelaine Boyd, Anna-Luisa Brakman, Greg Brockman, Tim Brooks,
326 Miles Brundage, Kevin Button, Trevor Cai, Rosie Campbell, Andrew Cann, Brittany Carey, Chelsea
327 Carlson, Rory Carmichael, Brooke Chan, Che Chang, Fotis Chantzis, Derek Chen, Sully Chen,
328 Ruby Chen, Jason Chen, Mark Chen, Ben Chess, Chester Cho, Casey Chu, Hyung Won Chung,
329 Dave Cummings, Jeremiah Currier, Yunxing Dai, Cory Decareaux, Thomas Degry, Noah Deutsch,
330 Damien Deville, Arka Dhar, David Dohan, Steve Dowling, Sheila Dunning, Adrien Ecoffet, Atty
331 Eleti, Tyna Eloundou, David Farhi, Liam Fedus, Niko Felix, Simón Posada Fishman, Juston Forte,
332 Isabella Fulford, Leo Gao, Elie Georges, Christian Gibson, Vik Goel, Tarun Gogineni, Gabriel
333 Goh, Rapha Gontijo-Lopes, Jonathan Gordon, Morgan Grafstein, Scott Gray, Ryan Greene, Joshua
334 Gross, Shixiang Shane Gu, Yufei Guo, Chris Hallacy, Jesse Han, Jeff Harris, Yuchen He, Mike
335 Heaton, Johannes Heidecke, Chris Hesse, Alan Hickey, Wade Hickey, Peter Hoeschele, Brandon
336 Houghton, Kenny Hsu, Shengli Hu, Xin Hu, Joost Huizinga, Shantanu Jain, Shawn Jain, Joanne
337 Jang, Angela Jiang, Roger Jiang, Haozhun Jin, Denny Jin, Shino Jomoto, Billie Jonn, Heewoo
338 Jun, Tomer Kaftan, Łukasz Kaiser, Ali Kamali, Ingmar Kanitscheider, Nitish Shirish Keskar,
339 Tabarak Khan, Logan Kilpatrick, Jong Wook Kim, Christina Kim, Yongjik Kim, Jan Hendrik
340 Kirchner, Jamie Kiros, Matt Knight, Daniel Kokotajlo, Łukasz Kondraciuk, Andrew Kondrich,
341 Aris Konstantinidis, Kyle Kosic, Gretchen Krueger, Vishal Kuo, Michael Lampe, Ikai Lan, Teddy
342 Lee, Jan Leike, Jade Leung, Daniel Levy, Chak Ming Li, Rachel Lim, Molly Lin, Stephanie
343 Lin, Mateusz Litwin, Theresa Lopez, Ryan Lowe, Patricia Lue, Anna Makanju, Kim Malfacini,
344 Sam Manning, Todor Markov, Yaniv Markovski, Bianca Martin, Katie Mayer, Andrew Mayne,
345 Bob McGrew, Scott Mayer McKinney, Christine McLeavey, Paul McMillan, Jake McNeil, David
346 Medina, Aalok Mehta, Jacob Menick, Luke Metz, Andrey Mishchenko, Pamela Mishkin, Vinnie
347 Monaco, Evan Morikawa, Daniel Mossing, Tong Mu, Mira Murati, Oleg Murk, David Mély,
348 Ashvin Nair, Reiichiro Nakano, Rajeev Nayak, Arvind Neelakantan, Richard Ngo, Hyeonwoo
349 Noh, Long Ouyang, Cullen O’Keefe, Jakub Pachocki, Alex Paino, Joe Palermo, Ashley Pantuliano,
350 Giambattista Parascandolo, Joel Parish, Emy Parparita, Alex Passos, Mikhail Pavlov, Andrew Peng,
351 Adam Perelman, Filipe de Avila Belbute Peres, Michael Petrov, Henrique Ponde de Oliveira Pinto,
352 Michael Pokorný, Michelle Pokrass, Vitchyr H. Pong, Tolly Powell, Alethea Power, Boris Power,
353 Elizabeth Proehl, Raul Puri, Alec Radford, Jack Rae, Aditya Ramesh, Cameron Raymond, Francis
354 Real, Kendra Rimbach, Carl Ross, Bob Rotsted, Henri Roussez, Nick Ryder, Mario Saltarelli, Ted
355 Sanders, Shibani Santurkar, Girish Sastry, Heather Schmidt, David Schnurr, John Schulman, Daniel
356 Selsam, Kyla Sheppard, Toki Sherbakov, Jessica Shieh, Sarah Shoker, Pranav Shyam, Szymon

357 Sidor, Eric Sigler, Maddie Simens, Jordan Sitkin, Katarina Slama, Ian Sohl, Benjamin Sokolowsky,
358 Yang Song, Natalie Staudacher, Felipe Petroski Such, Natalie Summers, Ilya Sutskever, Jie
359 Tang, Nikolas Tezak, Madeleine B. Thompson, Phil Tillet, Amin Tootoonchian, Elizabeth Tseng,
360 Preston Tuggle, Nick Turley, Jerry Tworek, Juan Felipe Cerón Uribe, Andrea Vallone, Arun
361 Vijayvergiya, Chelsea Voss, Carroll Wainwright, Justin Jay Wang, Alvin Wang, Ben Wang,
362 Jonathan Ward, Jason Wei, CJ Weinmann, Akila Welihinda, Peter Welinder, Jiayi Weng, Lillian
363 Weng, Matt Wiethoff, Dave Willner, Clemens Winter, Samuel Wolrich, Hannah Wong, Lauren
364 Workman, Sherwin Wu, Jeff Wu, Michael Wu, Kai Xiao, Tao Xu, Sarah Yoo, Kevin Yu, Qiming
365 Yuan, Wojciech Zaremba, Rowan Zellers, Chong Zhang, Marvin Zhang, Shengjia Zhao, Tianhao
366 Zheng, Juntang Zhuang, William Zhuk, and Barret Zoph. Gpt-4 technical report, 2024b. URL
367 <https://arxiv.org/abs/2303.08774>.

368 Roma Patel and Ellie Pavlick. Mapping language models to grounded conceptual spaces. In
369 *International conference on learning representations*, 2022.

370 Ellie Pavlick. Symbols and grounding in large language models. *Philosophical Transactions of the*
371 *Royal Society A*, 381(2251):20220041, 2023.

372 Steven T Piantadosi, Dyana CY Muller, Joshua S Rule, Karthikeya Kaushik, Mark Gorenstein,
373 Elena R Leib, and Emily Sanford. Why concepts are (probably) vectors. *Trends in Cognitive*
374 *Sciences*, 28(9):844–856, 2024.

375 Laura Ruis, Akbir Khan, Stella Biderman, Sara Hooker, Tim Rocktäschel, and Edward Grefenstette.
376 The goldilocks of pragmatic understanding: Fine-tuning strategy matters for implicature resolution
377 by llms, 2023. URL <https://arxiv.org/abs/2210.14986>.

378 Abulhair Saparov and He He. Language models are greedy reasoners: A systematic formal analysis
379 of chain-of-thought, 2023. URL <https://arxiv.org/abs/2210.01240>.

380 Abulhair Saparov and Tom M. Mitchell. Towards General Natural Language Understanding with
381 Probabilistic Worldbuilding. *Transactions of the Association for Computational Linguistics*, 10:
382 325–342, 04 2022. ISSN 2307-387X. doi: 10.1162/tacl_a_00463. URL [https://doi.org/10.](https://doi.org/10.1162/tacl_a_00463)
383 [1162/tacl_a_00463](https://doi.org/10.1162/tacl_a_00463).

384 Chen Shani, Dan Jurafsky, Yann LeCun, and Ravid Shwartz-Ziv. From tokens to thoughts: How
385 llms and humans trade compression for meaning, 2025. URL [https://arxiv.org/abs/2505.](https://arxiv.org/abs/2505.17117)
386 [17117](https://arxiv.org/abs/2505.17117).

387 Daniel L Silver and Tom M Mitchell. The roles of symbols in neural-based ai: They are not what you
388 think! In *Compendium of Neurosymbolic Artificial Intelligence*, pages 1–28. IOS Press, 2023.

389 Paul Smolensky. Analysis of distributed representation of constituent structure in connectionist
390 systems. In D. Anderson, editor, *Neural Information Processing Systems*, volume 0. American
391 Institute of Physics, 1987. URL [https://proceedings.neurips.cc/paper_files/paper/](https://proceedings.neurips.cc/paper_files/paper/1987/file/66f041e16a60928b05a7e228a89c3799-Paper.pdf)
392 [1987/file/66f041e16a60928b05a7e228a89c3799-Paper.pdf](https://proceedings.neurips.cc/paper_files/paper/1987/file/66f041e16a60928b05a7e228a89c3799-Paper.pdf).

393 Michael Henry Tessler, Michiel A Bakker, Daniel Jarrett, Hannah Sheahan, Martin J Chadwick,
394 Raphael Koster, Georgina Evans, Lucy Campbell-Gillingham, Tantum Collins, David C Parkes,
395 et al. Ai can help humans find common ground in democratic deliberation. *Science*, 386(6719):
396 eadq2852, 2024.

397 Jing Yi Wang, Nicholas Sukiennik, Tong Li, Weikang Su, Qianyue Hao, Jingbo Xu, Zihan Huang,
398 Fengli Xu, and Yong Li. A survey on human-centric llms, 2024. URL [https://arxiv.org/](https://arxiv.org/abs/2411.14491)
399 [abs/2411.14491](https://arxiv.org/abs/2411.14491).

400 Chen Zhang, Mingxu Tao, Quzhe Huang, Zhibin Chen, and Yansong Feng. Can llms learn a new
401 language on the fly? a case study on zhuang. In *The Second Tiny Papers Track at ICLR 2024*, 2024.

402 Yang Zhao, Zhijie Lin, Daquan Zhou, Zilong Huang, Jiashi Feng, and Bingyi Kang. Bubogpt:
403 Enabling visual grounding in multi-modal llms, 2023. URL [https://arxiv.org/abs/2307.](https://arxiv.org/abs/2307.08581)
404 [08581](https://arxiv.org/abs/2307.08581).

405 **A Technical Appendices and Supplementary Material**

406 **A.1 About properties of LLMs discussed in Silver and Mitchell [2023]**

407 The two additional properties not included in aforementioned discussion, due to focus on "language"
408 relevant similarity comparisons:

- 409 1. Encodings are multi-modal, meaning representations in human brain and Artificial Neural
410 Networks "get similar patterns" whether hearing or writing, word could be in English or
411 Portugese, "where full representations are spread across sensory and motor modalities"
412 Silver and Mitchell [2023].
- 413 2. Dual Architecture draws upon Kahneman's theory of thinking fast and slow, by using two
414 systems named: System 1 that thinks fast and System 2 that thinks slow by applying rules,
415 logic and evidences. "Kahneman's theory suggests brain learns quickly to activate a neural
416 pattern Y, if it was frequently coactivated with neural pattern X" Silver and Mitchell [2023].
417 For example even if the image of "peach" or symrep of "peach is partial or vague such as
418 canned peaches, or smashed peaches, brain generates conrep of typical peach. This seems to
419 be modulated by grounded perception.

420 **A.2 Formulations for compression-meaning tradeoff evaluation as a measure for comparing 421 similarity of symbolic encodings between LLMs and humans Shani et al. [2025]**

422 IB seeks a compressed representation C of an input X that maximizes information about relevant
423 variable Y minimizing $I(X; C)$, mutual information C retains about X , is the bottleneck cost. The
424 goal \mathcal{L} to balance RDT's rate and distortion, \mathcal{L} designed to explicitly balance complexity term R ,
425 representing X through conceptual clusters C . By RDT theory, $X : X, x_1, x_2 \dots \in X$ is a source
426 sequence. The reproduction sequence is a potential output $\hat{X} : \hat{X}, \hat{x}_1 \hat{x}_2 \dots \in \hat{X}$ and the distortion
427 measures the loss or distance (that are normalized/normal distortion measures). The distortion
428 measures, for RDT for the the goal \mathcal{L} , is for semantic information lost or obscured within the clusters
429 (variance of each $x_i \in X$ embeddings relative to concept cluster centroids). To combine the three
430 research questions with RDT and IB formulations, where X are the token embeddings, $\mathcal{L}(X, C; \beta) =$
431 $Complexity(X, C) + \beta \cdot Distortion(X, C)$ The further formulations $I(X; C) = H(X) - H(X | C)$
432 applies to initial and conditional entropies respectively. If Cluster assignments C make the specific
433 items X more predictable, then that signifies greater compression. The complexity $Complexity(X, C)$
434 and its details of formulations expressed in terms of respective entropy formalizes representational
435 compactness. The Distortion term $Distortion(X, C)$ measures loss of semantic fidelity incurred
436 by grouping items into clusters, which is measured as average intra-cluster variance of the item
437 embeddings and this formalizes semantic preservation. The unified objective $\mathcal{L}(X, C; \beta)$ combines
438 $Complexity(X, C)$ i.e. representational compactness and $Distortion(X, C)$ i.e. semantic preservation
439 together formalizes compression-meaning tradeoff.

440 Further by using k-means and other relevant applicable metrics, the findings relevant to represen-
441 tational compactness suggest above-chance alignment with human conceptual categories and can
442 recover human-like categories from their embeddings.

443 **A.3 Details about Canonical vs non-canonical tokenization problem formulation**

444 For each string x , canonical tokenizer yields a canonical tokenization vector v^* , which is evaluated
445 by LLM for canonical probability $p(v^*, x)$, which is one of the exponential number of possible
446 tokenizations and space. The distribution of tokenization space from Geh et al. [2024a] shows larger
447 probability mass on the canonical tokenization.

448 For computing marginals, the findings suggest that for short strings, the results seem to show that
449 canonical probability is close to true marginal. For the longer texts, the approximate marginal
450 approaches closer to canonical tokenization probability.