Do LLMs Play Dice? Exploring Probability Distribution Sampling in Large Language Models for Behavioral Simulation

Anonymous ACL submission

Abstract

With the rapid advancement of large language models (LLMs) for handling complex language tasks, an increasing number of studies are employing LLMs as agents to emulate the sequential decision-making processes of humans often represented as Markov decision-making processes (MDPs). The actions in MDPs adhere to specific probability distributions and require iterative sampling. This arouses curiosity regarding the capacity of LLM agents to comprehend probability distributions, thereby guiding 011 012 the agent's behavioral decision-making through probabilistic sampling and generating behavioral sequences. To answer the above question, we divide the problem into two main aspects: 016 sequence simulation with known probability distribution and sequence simulation with un-017 known probability distribution. Our analysis indicates that LLM agents can understand prob-020 abilities, but they struggle with probability sampling. Their ability to perform probabilistic 021 sampling can be improved to some extent by 022 integrating coding tools, but this level of sampling precision still makes it difficult to simulate human behavior as agents.

1 Introduction

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With the rapid development of artificial intelligence technology, large language models (LLMs), as a key component, have demonstrated powerful language understanding and generation capabilities (Zhao et al., 2023; Kojima et al., 2022). In addition to language generation, people have begun to explore the field of introducing LLMs into the decision-making process, such as simulating human sequential decision-making processes as an agent, and LLM agents have gradually shown their excellent potential in simulating human behaviors and decision-making (Li et al., 2023; Gao et al., 2023; Leng and Yuan, 2024; Brand et al., 2023; Horton, 2023). This brings great convenience to research in fields such as computer science, behavioral science, psychology, and sociology. For example, the core conversational robots (Zhou et al., 2024b) and social robots of LLMs can more realistically simulate human speech and behavior. LLM agents have demonstrated promising results in various tasks simulating human behavior (Taylor et al., 2022; Yuan et al., 2022; Aher et al., 2023; He et al., 2024). However, whether LLM agents can effectively simulate human behavior sequences remains an open question and requires careful validation. 042

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Human behavior can often be effectively modeled using Markov decision processes (MDPs). Numerous studies have applied this framework to simulate human behaviors such as planning (Callaway et al., 2017; Guojiang et al., 2007; Redding et al., 2012). MDPs consist of four key components: states, actions, transition probabilities, and rewards. Within this framework, an agent in a given state selects an action, leading to a transition to the next state based on defined probabilities, and receives associated rewards. The parallel between human behavior and MDPs stems from the tendency of decision-making processes to depend on current circumstances and available actions, rather than solely on past experiences. When confronted with a situation, humans typically make decisions based on their present state and the feasible choices, aiming to optimize future benefits or satisfaction. This mirrors the states, action selections, and rewards accrued through state transitions in MDPs.

In MDPs, sequences of actions follow a specific probability distribution. Similarly, human behavioral sequences theoretically adhere to probabilistic distributions as well. Considering the feasibility of using MDPs to model human behavior, an LLMbased agent should generate actions that match a probability distribution if it truly simulates human behavior. But can LLM agents do this? The most direct way to validate this is to explore their probability distribution sampling capabilities. Figure 1 illustrates our approach to assessing LLM's under-



Figure 1: The decision-making process of the LLM agent is a MDP, and the generated action sequence A conforms to a certain probability distribution. We input *Prompt1* for the known probability distribution and *Prompt2* for the unknown probability distribution, analyze the probability distribution of A generated by the LLM agent, and finally evaluate the behavioral simulation capability of the LLM agent.

standing and sampling capabilities of probability distributions. We outline two tasks of varying complexity: simulating scenarios with known probability distributions and generating sequences with probability distribution is not clear. Our evaluation of multiple LLMs in these scenarios aims to assess the potential and limitations of LLM agents in simulating human decision-making processes.

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In the first scenario, we propose questions about known probability distributions. Using these questions to prompt LLM agents for probability sampling, we analyze both the probability distributions and the generated sequences answered by the LLM agents. However, obtaining an accurate probability distribution is often challenging in practical scenarios. Therefore, we shift our focus to sequence generation in situations where the probability distribution is unclear. Online social networks are increasingly utilized in real-life scenarios (Sakaki et al., 2013; Panzarasa et al., 2009), prompting us to use these networks as contextual backgrounds. By observing varying activity levels corresponding to different behavior sequences generated by LLM agents, we indirectly assess the rationality of the sequences sampled. Ultimately, we instruct LLM agents to sample from probability distributions by generating code, aiming to evaluate whether programming tools can assist LLM agents in improving their sampling success rate.

Our analysis suggests that the probability sampling performance of LLM agents is not very good. While LLM agents demonstrate some understanding of simple probability distributions, their success rates in sampling sequences adhering to known distributions are limited. Moreover, they struggle with unknown probability distributions. However, when coupled with programming tools, LLM agents can achieve higher success rates in sampling these distributions by invoking appropriate functions. Yet, their abilities to sample from complex probability distributions remain comparatively weak, and even with the integration of programming tools, enhancements in sampling capability are elusive. Consequently, prudent consideration is necessary before employing LLM directly for simulating human behavior. 114

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Our main contributions are:

- Explore the LLM agent's ability to understand and sample probability distributions from both the perspectives of known and unknown probability distributions.
- A method of using programming tools to assist sampling is proposed to improve the effect of the LLM agent in the probability distribution sampling process and is effective in simple probability distributions.
- Our experimental results reveal the limitations 139 of LLM agents in terms of probability distributions when simulating human behavior. 141

2 Background

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2.1 MDPs of Human Behavior

The modeling of human behavior in MDPs could include the following aspects (Tan and Cheng, 2009):

Human behavior can be understood as transitions between different states of state space (S), which may include emotional states, social identities, and more. In each state, humans can choose from a series of possible actions or decisions of action space (A). These actions lead to state changes with certain probabilities, represented by the state transition probability P. Human behavior is driven by rewards and punishments, described by the reward function R. To maximize benefits, humans adopt various strategies, captured by a policy π , which maps the probability of taking action a in state s.

Humans typically have long-term goals, such as maximizing life satisfaction, career achievement, or health. The objective in an MDP is to find a policy π that maximizes the expected cumulative reward. A common objective function is the total discounted return G_t :

$$G_t = \sum_{k=0}^{\infty} \gamma^k R_{t+k+1},\tag{1}$$

where t represents current time, γ ($0 \le \gamma \le 1$) is the discount factor, representing the present value of future rewards.

Based on the above discussion, human behavior can usually be regarded as conforming to a certain probability distribution. Given characteristics, there is a defined probability distribution (Viti et al., 2015). Some simple behaviors conform to common probability distributions (Yan et al., 2012; Hu and Han, 2008; Wang et al., 2011). Additionally, many real-world human behaviors may be complex and composed of multiple distributions (Tenorth et al., 2013; Sorensen et al., 2017).

Human behavior can be modeled as MDPs, where actions in MDPs can be interpreted as behaviors that follow a series of probability distributions (Korthikanti et al., 2010). If LLM agents can accurately simulate human behavior, the sequences of behaviors they generate should align with these probability distributions.

185 2.2 Large Language Models as Agent

In recent years, with the rapid development ofLLM, more and more studies have discovered the

great potential of LLM agents in simulating usergenerated behaviors. Behavior simulation can generate user research data and facilitate research in recommendation systems, human-computer interaction, social science research, etc. (Hämäläinen et al., 2023; Kim and Lee, 2023; Li et al., 2023). Social network simulation has many applications in understanding human social behavior patterns, policy formulation and planning, disaster management, etc. (Panzarasa et al., 2009; Sakaki et al., 2013; Jiang and Ferrara, 2023). Many studies have shown that LLM agents can exhibit certain social behavior capabilities, simulate individuals in social networks at a micro level, and imitate human behavior (Gao et al., 2023; Leng and Yuan, 2024). 188

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In addition to the analysis and research on the human-like behavior of LLM agents in various fields, owing to the complexity of human thinking and their outstanding learning and tool usage abilities, several studies (Yao et al., 2023; Schick et al., 2023; Shinn et al., 2023; Zhou et al., 2024a) have designed an agent framework with LLMs as the core. This framework provides LLMs with additional modules such as profile management, reasoning, and tool usage, enabling more accurate simulation of human speech and behavior.

The complexity of human behavior poses challenges for artificial intelligence in simulating it. The capability of LLM agents to simulate human behavior through probability distribution remains to be fully explored.

3 Verification Methodology

To determine if LLMs can effectively simulate action sampling, we have designed experiments to address the following four research questions:

RQ1: Do LLM agents have the ability to understand probability distributions?

RQ2: Do LLM agents have the ability to sample simple known probability distributions?

RQ3: Do LLM agents have the ability to sample complex unknown probability distributions?

RQ4: Can LLM agents improve their probability distribution sampling ability by combining programming tools?

To verify these issues, we evaluated LLMs on two levels: known and unknown behavioral probability distributions. Additionally, we used code tools to explore LLMs' probability distribution sampling ability.

3.1 Known Probability Distribution

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To verify if LLM agents can understand and sample from a given probability distribution, we compared the expected probability distribution with the probability distribution of the generated behavior sequence through hypothesis testing. This approach addresses RQ1 and RQ2.

3.1.1 Experimental Design

To explore the ability of LLM agents to understand probability distributions, two sets of controlled experiments were designed.

Firstly, given a problem with a known probability distribution P_X , we ask LLM agents to predict an action sequence A based on the problem, forming the prompt *prom*. Our expectation is that the probability distribution P_A that action sequence A conforms to matches P_X . For example, given the average math score from the last semester, we ask LLM agents to predict the next scores. Secondly, leveraging the improvement to LLMs through the chain of thought (CoT) approach, we add "what probability distribution does this sequence conform to" to *prom*, resulting in *prom_D*. This guide the LLM agents to identify the probability distribution. See the Appendix A.1.1 for prompts used in this part of the experiment.

We also extract the type of the probability distribution from the LLM agents' answers to verify if they can understand probability distributions.

3.1.2 Evaluation Metrics

We designe evaluation metrics to assess the probability distribution understanding and sampling capabilities of LLM agents.

Firstly, considering P_A , unanswered and incorrect answers are regarded as negative samples. Only correct answers are regarded as positive samples. The proportion of positive samples *acc-pd* is calculated to measure the LLM's ability to understand probability distributions.

Secondly, to evaluate the performance of the LLMs in sampling the probability distribution P_X ., we employ Kolmogorov-Smirnov test (KS test) (Jr., 1951). In KS test, The statistic D is used to assess whether two samples from the same distribution by comparing their empirical distribution functions. The empirical distribution functions $F_m(x)$ and $G_n(x)$ for the sample from P_X and P_A represent the proportion of samples less than or equal to x.

$$D = \sup_{x} |F_m(x) - G_n(x)|, \qquad (2)$$

where \sup_x denotes the supremum over all possible values of x. Finally, we assess the fit between the sample sequence and the target probability distribution using the mean p-value *p*-mean from the KS test. When the p-value is greater than the significance level α , the test is considered to have passed, and the statistical test pass rate is denoted as *success-ks*.

Additionally, the *p*-mean is obtained on the pvalue after outlier processing. Since the calculated average value is easily affected by outliers, the interquartile range (IQR) outlier detection method was used to detect outliers in the experimental data and replace them with the median. In IQR outlier detection, the interquartile range r is the distance between the upper quartile Q3 and the lower quartile Q1. The normal value interval is [Q1 - 1.5r, Q3 + 1.5r], and other values are considered outliers.

3.2 Unknown Probability Distribution

To answer RQ3, we used online social networks as the background to evaluate the simulation capability of LLM agents through a comparative analysis of the results.

3.2.1 Experimental Design

In online social network platforms, user activity level l represents the user's level of activity on the platform and affects users' behavior or actions. Compared to low-activity-level users, high-activitylevel users frequent social platforms more often, post more comments, browse more posts, and are more likely to like and comment on the posts they browse. Therefore, even though the probability distribution of these behaviors is unknown, a comparative analysis of the probability distributions of sampled results with different l can help determine whether the user action sequences generated by LLM agents adheres to these patterns.

We set the activity level variable l in the prompt $prom_l$, along with six activity indicators. These indicators include active behavior: the duration of browsing, the number of visits to the social platform, and the number of posts in a day; and interactive behavior: the likes, reposts, and comments on 100 posts. We use $prom_l$ as the dialogue input for LLMs, prompting them to generate the corresponding information. See Appendix A.1.2 for the prompts used in this part of the experiment. The ability of LLMs to simulate user behavior sequences is analyzed by comparing the generated

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results across different values of *l*.

3.2.2 Evaluation Metrics

For active behaviors such as browsing duration, number of visits, and number of posts, we directly compare the results generated by LLM agents. Taking browsing duration as an example, as activity level increases, so does browsing duration.

In interactive behaviors such as likes, reposts, and comments, we observed contradictory responses from LLMs. When LLM agents were tasked with generating binary sequences for likes, shares, and comments, and then asked to report the counts of these actions, the numbers they provided did not match the sequences they actually generated. Therefore, we use a more fine-grained actual generated sequence to represent the LLMs sampling sequence and use the number of likes, reposts, and comments in the action sequence as the frequency of LLMs generation. Take likes as an example, $S_i = \{b_0, b_1, b_2, \dots, b_{n_i-2}, b_{n_i-1}, b_{n_i}\}$ represents the like sequence sampled by LLM agents when $l = l_i$. Here, n_i is the length of the sequence, b_j represents the *j*-th element in the sequence, and the value of b_i is 1 or 0, indicating like or not like, respectively. As l increases, so does the frequency of likes. Therefore,

$$c_1/n_1 < c_2/n_2 < c_2/n_3$$

s.t. $l_1 < l_2 < l_3$, (3)

where c_i represents the number of 1s in S_i .

For the experimental group that meets the above conditions, the simulation is considered successful. All data combinations corresponding to different activity levels are cross-checked to calculate the simulation success rate *success-simu*.

3.3 Methods for Code Experiments

In this section, the goal of our designed experiment is to answer RQ4. Given that the sampling performance of LLM agents in probability distributions is not very good, we considered whether external tools could be used to improve the LLM agents' probability distribution sampling capabilities. Considering that LLMs have code generation capabilities (Chen et al., 2021), Python code can be generated and sampled with the help of Python tools. Therefore, we asked LLM agents to solve the above problems by generating Python code through $prom_{code}$. See the Appendix A.1.3 for prompts related to this part of the experiment. After running codes, we used the same method to obtain results.

In experiments with known probability distributions, LLM agents are required to generate Python code based solely on $prom_D$. Since the probability distribution is known, the generated Python code is considered correct if the appropriate probability distribution sampling function is called, the parameters are correct, and there are no other code errors. In other cases, the code is considered incorrect. Therefore, no further KS test is required. In the experiment of unknown probability distributions, $prom_{code}$ requires the LLM agent to generate Python code. After running the Python code, the results are analyzed using the same method as in the previous experimental method. 384

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4 Experiment

Based on the four questions we raised in Section 3 and the previous validation methods, in this section, we will introduce our experimental setup and present the experimental results in sequence.

4.1 Experimental Setups

4.1.1 Known Probability Distribution

We select the following probability distributions. The **Poisson** distribution describes the number of events occurring within a fixed interval of time or space. The **Uniform** distribution describes a situation where all possible values have equal probability. The **Normal** distribution describes data that are symmetrically distributed around the mean. The **Exponential** distribution describes the time intervals between events in a Poisson process, characterized by a constant event rate. The **Binomial** distribution describes the number of successes in a fixed number of independent trials, each with the same probability of success.

4.1.2 Unknown Probability Distribution

In this part of the experiment, we selected three activity levels: 0.2, 0.5, and 0.8, with the maximum activity level set at 1. For the activity measurement index, we chose the duration of browsing, the number of visits to the social platform, the number of posts in a day, and the likes, reposts, and comments on 100 posts. These metrics will all vary with the activity level.

4.1.3 Models

Five large language models were selected for the experiment of known probability distributions: GPT-4 (Achiam et al., 2023), GPT-3.5 (GPT-3.5), Claude 2.1 (Bai et al., 2022), Llama2 (Touvron et al., 2023),

Prompts	Mathada	Probability Distribution					
	Methous	Poisson	Uniform	Normal	Exponential	Binomial	
prom	one-step	7.0E-21	7.4E-03	1.6E-03	5.8E-33	1.6E-13	
	multi-step	2.1E-41	8.5E-03	9.7E-23	5.8E-33	2.6E-01	
$prom_D$	one-step	8.5E-09	3.2E-03	4.0E-03	5.8E-33	6.5E-08	
	multi-step	2.1E-41	8.6E-03	3.0E-39	1.6E-13	1.3E-03	

Table 1: Comparison of the *p*-mean of different methods for GPT-3.5 under prom and $prom_D$.

and Vicuna (Chiang et al., 2023). Building on this foundation, four additional large language models were included for the experiment of unknown probability distributions: ERNIEBot (ERNIE Bot), ChatGLM (Du et al., 2021), Gemini (Team et al., 2023), and Mixtral (Jiang et al., 2024). Given the complexity of unknown probability distributions and the diversity among models, we conducted a more comprehensive set of experiments.

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4.2 Experimental Results

The LLM's probability distribution sampling ability was evaluated in the following four aspects.Examples of LLM's answers in the experiment are shown in Appendix A.2.

In experiments where the prompt is *prom*, the Poisson distribution experiment of GPT-4, and the Exponential distribution experiment of GPT-3.5, GPT-4, and Claude2.1, the LLM agents could answer the distribution. Therefore, in these four groups of experiments, we reused the data from the experiment where the prompt is $prom_D$.

4.2.1 Efficient Action Sampling

When instructing LLM agents to generate se-454 455 quences, we compared the multi-step method with the one-step method, as shown in Table 1. In the 456 multi-step method, actions are generated one at a 457 time within the same context, repeated 100 times, 458 while the one-step method generates a complete 459 sequence of length 100 at once. During the text 460 generation process by LLMs, the prefix that has al-461 ready been generated is taken into account. Gener-462 ating 100 actions at once generally yields similar or 463 better results compared to generating one action at 464 465 a time, except in the case of Binomial distribution. However, the majority of results from both methods 466 did not achieve the level of statistical significance. 467 Therefore, considering both effectiveness and effi-468 ciency, we opt for the one-step approach. 469

Madala	Metrics	Probability Distribution					
wouers		Poisson	Uniform	Normal	Exponential	Binomial	
GPT-3.5	p-mean	7.0E-21	7.4E-03	1.6E-03	5.8E-33	1.6E-13	
	success-ks	0%	5%	25%	0%	0%	
CDT 4	p-mean	6.5E-08	4.6E-03	1.1E-02	6.5E-09	2.9E-03	
GF 1-4	success-ks	0%	0%	40%	0%	30%	
Claude 2.1	p-mean	5.1E-56	1.2E-02	9.3E-03	1.2E-10	2.2E-06	
	success-ks	0%	45%	45%	0%	0%	
11	p-mean	3.3E-115	7.8E-17	9.2E-10	0.0	2.5E-05	
Liamaz	success-ks	0%	0%	10%	5%	0%	
Vicuna	p-meann	1.8E-57	1.6E-204	7.1E-03	1.1E-46	3.8E-04	
	success- ks	0%	5%	50%	0%	15%	

Table 2: The *p*-mean and the *success-ks* when the probability distribution is known and the prompt is *prompt*. Bold data indicates the model with the largest *p*-mean on this probability distribution.

4.2.2 Understanding of Probability Distributions

If LLM agents can identify the probability distribution P_X that a random variable conforms to, it reflects LLM agents' ability to understand probability distributions concerning question RQ1.

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As depicted in Figure 2, when LLM agents are not required to answer probability distributions, except for the Exponential distribution of GPT-3.5 and the Poisson and Exponential distribution of GPT-4, LLM agents rarely take the initiative to answer the question of what distribution it conforms to. However, this does not imply that they do not know the P_X . In the prom_D scenario, except for partial probability distributions of Vicuna and Llama2, the *acc-pd* of other models is higher, reaching more than 80%. Similar results were observed in the $prom_{code}$ experiment. This demonstrates that LLMs have a certain ability to understand probability distributions and can infer the probability distribution based on the questions, although the *acc-pd* of the vicuna model is lower than other models.

4.2.3 Sampling from A Known Probability Distribution

In this section, we answered question RQ2. For the random variable X and the probability distribution P_X it obeys, the KS test is employed to assess whether the sequence sampled by the LLM agent conforms to P_X . Here, we set the significance level α in the KS test to the commonly used 0.01, the average p-value is denoted as *p*-mean, and the test pass rate is *success-ks*.

As shown in Table 2 and Table 3, from the perspective of *success-ks*, most models can achieve the highest test pass rate on the Normal distribution, while the *success-ks* on other probability distribu-



■ Possion ■ Uniform ■ Normal ■ Exponential ■ Binomial

Figure 2: Comparison of the *acc-pd* of different prompts for each LLM agent under different probability distributions

Models	Metrics	Probability Distribution					
		Poisson	Uniform	Normal	Exponential	Binomial	
GPT-3.5	p-mean success-ks	8.5E-09 0%	3.2E-03 0%	4.0E-03 50%	5.8E-33 0%	6.5E-08 20%	
GPT-4	p-mean $success$ - ks	6.5E-08 0%	3.2E-03 0%	3.4E-03 20%	6.5E-09 0%	1.5E-02 40%	
Claude 2.1	p-mean $success$ - ks	6.5E-06 0%	1.1E-02 55%	5.6E-02 45%	1.2E-10 0%	2.3E-04 10%	
Llama2	p-mean success-ks	8.8E-46 0%	1.0E-08 0%	1.6E-07 10%	7.8E-38 0%	1.6E-02 50%	
Vicuna	p-mean success-ks	2.2E-31 0%	1.6E-09 0%	5.8E-03 25%	2.2E-123 0%	3.9E-10 10%	

Table 3: The *p*-mean and the success-ks when the probability distribution is known and the prompt is $prompt_D$. Bold data indicates the model with the largest *p*-mean on this probability distribution.

tions is lower, and in many cases the *success-ks* is 0%. Judging from the *p-mean*, the simulation performance of all models on Normal, Uniform, and Binomial distribution is much higher than on the Exponential and Poisson distribution. At the same time, during our experiments, we found that the Vicuna model often incorrectly answered questions about other probability distributions as Normal distributions. We speculate that the reason for this phenomenon may be that there is more data consistent with the Normal distribution in the LLMs training data, while there is less data for Exponential and Poisson distribution.

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The probability distribution sampling performance of GPT-4 is better than other models in half of the experimental groups, followed by Claude2.1 with better performance. In addition, by comparing experiments with prom and $prom_D$, we found that instructing LLM agents by adding "what probability distribution does this sequence conform to" in the prompt can increase the *p*-mean. This suggests that this method can enhance the distribution sampling ability of LLM agents, although the p-value often fails to reach the significance level α . Therefore, we conclude that while LLM agents lack the inherent ability to sample from known probability distributions, tools can be employed to enhance their performance with simple distributions.

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4.2.4 Sampling from An Unknown Probability Distribution

For different activity levels *l*, the *success-simu* is calculated based on various activity indicators to measure the rationality of the behavior simulated by LLM agents when the probability distribution is unknown concerning question RQ3.

As seen in Figure 3, most *success-simu* of various models are less than 30%, especially Llama2, ERNIEBot, ChatGLM, and Gemini, with an average *success-simu* of only slightly more than 10%. Furthermore, there is significant performance variance among models under different activity indicators, indicating that most of the sampling results of unknown probability distributions by LLM agents do not meet the required conditions, and LLM agents lack the ability to sample unknown probability distributions.

4.2.5 Probability Distribution Sampling Combined with Code Tools

In this section, we answered question RQ4. In the code experiment section, $prom_{code}$ leads LLM agents to generate Python code, and the results are obtained by running the Python code.

In experiments with known probability distributions, the accuracy of the code *acc-code* and the *acc-pd* are calculated. It can be seen from Table 4 and Figure 2 that the *acc-code* and the



Figure 3: Comparison of the *success-simu* of $prom_l$ and $prom_{code}$ for each LLM agent under unknown probability distributions. "Duration" is the browsing duration, "Sessions" is the number of visits to the social platform, "Likes" is the proportion of likes, "Reposts" is the proportion of forwarding, "Comments" is the proportion of comments, and "Posts" is the number of posts.

Madala	Probability Distribution						
Models	Poisson	Uniform	Normal	Exponential	Binomial		
GPT-3.5	100%	100%	100%	75%	100%		
GPT-4	100%	100%	100%	100%	100%		
Claude 2.1	75%	100%	95%	100%	100%		
Llama2	5%	100%	65%	0%	55%		
Vicuna	15%	40%	65%	10%	65%		

Table 4: In the case of known probability distribution, the *acc-code* of each model on the probability distribution by generating Python code.

acc-pd of GPT-3.5, GPT-4, and Claude2.1 have reached nearly 100% in most probability distributions, while Llama2 and Vicuna do not perform as well. But overall, there has been significant improvement in sampling known probability distributions through Python code.

In the experiment with unknown probability distributions, the running results of the code were statistically evaluated in the same way. As shown in Figure 3, we found that combining code tools cannot improve the unknown probability distribution sampling ability of LLM agents, and the *success-simu* of each model is still low. Moreover, during the experiment, we found that most LLM agents use code to randomly generate results without considering activity levels *l*. We speculate that because the problem of unknown probability distribution is relatively complex, and there is no suitable Python tool function that can directly generate results, LLM agents still need to generate code through their own reasoning and then obtain results through the code. Unlike the problem of known probability distribution, where they only need to reason about the correct probability distribution and parameters, they can usually get the correct code. When reasoning skills are still lacking, it is difficult to generate better code. 583

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5 Conclusion

This paper evaluates the reliability of LLM agents' behavior simulations from the perspective of novel probability distributions. We explore their capabilities through KS tests of known distributions and evaluations of unknown distributions. Our findings indicate that while LLM agents have some understanding of probability distributions, their sampling abilities are insufficient. Consequently, it is challenging to generate behavior sequences that conform to specific distributions solely with LLMs. This limitation arises from the probabilistic nature of LLMs' word prediction, which results in a layered probability distribution. Even with programming tools, improving sampling performance for complex distributions remains difficult. Due to the probabilistic nature of actions in MDPs, without effective sampling capabilities, LLM agents struggle to simulate human behavior accurately. Future work will focus on enhancing the LLM agent's probability distribution sampling abilities to improve behavioral simulations.

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612 Limitations

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613Due to resource limitations, some experiments lack614comprehensive evaluation. For example, when615comparing the similarity between multi-step gen-616erated sequences and sequences containing 100617digits generated at once, only the GPT-3.5 model618was evaluated.

Additionally, the experiment in this article is based on prompt engineering and faces issues of instability. Before conducting experiments, we compared various prompts and selected those that were relatively better and elicited better responses from the LLM. Future work will further address this issue by developing more diverse prompts and enhancing the robustness of evaluations.

627 Ethics Statement

This study adheres to rigorous ethical standards to ensure the integrity and credibility of the research. The primary focus is on evaluating the reliability of LLM agents' behavior simulations, which does not involve any human participants or sensitive data. Transparency is maintained through clear reporting of methods and results. The study was approved by the appropriate ethics review board, and efforts were made to responsibly use resources and consider the future implications of the research findings.

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A Appendix

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A.1 Prompts

We guide LLM agents to generate sequences through prompts. The prompts used in the experiment are as follows.

A.1.1 Prompts for Known Probability Distributions

This section shows the prompts for known probability distributions. Table 5 is prom and Table 6 is $prom_D$.

Probability distributions	prom
Poisson distribution	In the past, an average of 3 babies were born per hour. Estimate the number of babies born per hour 100 times in the future. List these 100 numbers (duplicates are allowed), separated by commas.
Uniform distribution	Simulate 100 rolls of the dice and list the 100 points separated by commas.
Normal distribution	A classmate's average score on the math test last semester was 70 points. List his possible scores on 100 math tests this year. List these 100 grades (can be repeated), separated by commas.
Exponential distribution	Assume that a coffee shop has an average of one customer coming in every ten minutes, guess how long it will take to wait for the next customer 100 times, and list these 100 numbers, separated by commas.
Binomial distribution	Assume you have a 30% probability of answer- ing "0" and a 70% probability of answering "1". Please answer 100 times. All answers are separated by commas.

Table 5: *prom* for different probability distributions in experiments with known probability distributions.

$prom_D$

prom + What probability distribution does this sequence conform to

Table 6: $prom_D$ in experiments with known probability distributions. We only added a sentence after each *prom*.

A.1.2 Prompts for Unknown Probability Distributions

This section shows the prompts for unknown probability distributions. Table 7 is the template of $prom_l$. 852

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A.1.3 Prompts for Code Experiments

This section shows the prompts for code experiments. Table 8 is the template of $prom_{code}$.

A.2 Experimental Examples

A.2.1 Examples in Known Probability Distributions Experiments

Some examples of LLM agents' answers in known probability distribution experiments are shown in Figure 4.

A.2.2 Examples in Unknown Probability Distributions Experiments

An example of LLM agents' answer in the unknown probability distribution experiments is shown in Table 9.

A.2.3 Examples in Code Experiments

Some examples of LLM agents' answers in the code experiment are shown in Table 10 and Table 11.

$prom_l$

Please make sure to provide a simulated answer to the question, ignoring background information about the social platform and the user. Assume you are a user on an online social platform, with a user activity level of [l]. Please provide the total time spent browsing the platform during idle time in a day (in minutes), the number of browsing sessions, and the number of posts made by the user. Additionally, please provide a complete set of likes, shares, and comments on 100 posts (using 1 to represent likes, shares, and comments, and 0 to represent no likes, shares, and comments, separated by commas).

Please strictly adhere to the following format for output:

Browsing Duration:

Number of Browsing Sessions: Likes:

Shares:

Comments:

Number of Posts:

Below is an example of an answer: Browsing Duration: 30

Number of browsing Sessions: 3

Likes: (a string of 100 0s and 1s, where 1 represents a like and 0 represents no like, separated by commas)

Shares: (a string of 100 0s and 1s, where 1 represents a share and 0 represents no share, separated by commas)

Comments: (a string of 100 0s and 1s, where 1 represents a comment and 0 represents no comment, separated by commas)

Number of Posts: 3

Table 7: $prom_l$ in unknown probability distribution experiments, where l in [] represents different levels of activity.

Experiments	$prom_{code}$
known probability distribution	Directly give Python code to solve the following problems: $+ prom_D$.
unknown probability distribution	Directly give Python code to solve the following problems: $+ prom_l$

Table 8: $prom_{code}$ in code experiments.



Figure 4: Some examples in known probability distributions experiments. The four pictures respectively represent the frequency histograms of vicuna in the Binomial distribution, Claude in the Exponential distribution, GPT-4 in the Normal distribution, and llama in the Uniform distribution under *prom*. The red line represents the ideal probability density function curve.

An example answer of Claude2.1

Table 9: An example answer of Claude2.1 in experiments when the probability distribution is unknown.

An example answer of GPT-3.5

```
import random
```

```
def next_customer_wait_time():
    # Average time between customers in minutes
    average_time_between_customers = 10
    # Generate random wait time following exponential distribution
    wait_time = random.expovariate(1 / average_time_between_customers)
    return wait_time
# Simulate waiting time for the next customer 100 times
waiting_times = [next_customer_wait_time() for _ in range(100)]
# Print the waiting times separated by commas
print(', '.join(map(str, waiting_times)))
```

Table 10: An example answer of GPT-3.5 in code experiments when the probability distribution is Exponential distribution.

```
An example answer of GPT-4
```

```
import random
# Constants
TIME_SPENT_BASELINE \text{=} 45
# Assume an average user spends 45 minutes a day
ACTIVITY_LEVEL = 0.2
NUM_POSTS = 100
# User-specific calculations
time_spent_browsing = TIME_SPENT_BASELINE * ACTIVITY_LEVEL
number_of_sessions = random.randint(1, 5)
# Assume 1-5 sessions for a low activity user
number_of_posts = round(ACTIVITY_LEVEL * 2)
# Assume an active user posts twice per day
# Social interactions are random according to the activity level
likes = [random.choice([0, 1]) for _ in range(NUM_POSTS)]
shares = [random.choice([0, 1]) for _ in range(NUM_POSTS)]
comments = [random.choice([0, 1]) for _ in range(NUM_POSTS)]
# Output
print(f"Browsing Duration: {time_spent_browsing:.2f}")
print(f"Number of Browsing Sessions: {number_of_sessions}")
print('Likes:', ':'.join(map(str, likes)))
print('Shares:', ':'.join(map(str, shares)))
print('Comments:', ':'.join(map(str, comments)))
print(f"Number of Posts: {number_of_posts}")
```

Table 11: An example answer of GPT-4 in code experiments when the probability distribution is unknown.