A CODESPACE AUTOENCODER FOR LANGUAGE TASKS

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ABSTRACT

Modern language modeling datasets require models to handle compositional reasoning, fact recall, and task-specific constraints. While these tasks are expressed in natural language, they often imply an underlying symbolic representation. In this work, we consider methods for extracting a latent symbolic representation in an unsupervised manner. We propose an autoencoder that models observed text data as being generated from underlying code with a dataset level function library. Our method is non-parametric and leverages in-context learning and code interpretation for inference. Code as the latent symbolic representation offers two key advantages. First, code offers a structured space that can be explored via modular functions; second, code is interpretably executable using deterministic and neural interpreters, enabling compositional and programmatic decoding into text. By identifying and composing patterns in this latent space, we can sample programs that produce correct, diverse, and task-relevant text through program execution. We demonstrate how our method induces a latent space with modern LLMs, explore patterns discovered within it, and evaluate text data synthesized from our induced latent space.

1 INTRODUCTION

Many natural tasks expressed with language have an underlying symbolic process. These latent processes can be represented well by code. For example, consider the example in Figure 1. Correct interpretation and execution of the task requires one to identify processes useful for the task (parsing time strings, comparing timestamps), then compose them properly (compose identified relations). We can enable modeling of more complex tasks by pairing neural and symbolic processes: neural processes discover the underlying symbolic structure, and symbolic processes execute the identified representation.

Given a statement about date and time, state whether the statement is true or false. The number of date/time operands in the statement ranges between 2 and 3.	<pre>def is_before() def is_between() def is_after() re.findall() datetime.strptime()</pre>
Let's say the values are denoted by t1, t2, and t3. The statements follow one of the following ten templates: 't1 occurs before t2, t1 doesn't occur before t2, t1 occurs after t2, t1 doesn't occur after t2, t1 occurs between t2 and t3, t1 doesn't occur between t2 and t3, t1 occurred before t2 but after t3, t1 occurred after t2 but before t3, t1 didn't occur before t2 but after t3, t1 didn't occur after t2 but before t3'. The output should be either 'True' or 'False'. Input: 22:01:41 occurs between 08:47:09 and 11:26:35 AM. Output: False	<pre>def is_before(t1, t2): return datetime.strptime(t1, "%H:%M:%S")< datetime.strptime(t2, "%H:%M:%S") def is_after(t1, t2): return datetime.strptime(t1, "%H:%M:%S")> datetime.strptime(t2, "%H:%M:%S") def is_between(t1, t2, t3): return is_before(t1,t3) and is_after(t1,t2) input = "22:01:41 occurs between 08:47: []" t1,t2,t3 = re.findall(r'\d+:\d+:\d+', input) task_output = is_between(t1,t2,t3)</pre>

Figure 1: The text inquiry (Wang et al., 2022) (left) has an underlying symbolic representation represented by a task-level library of functions (top right) and an instance-level code program (right).

³ Autoencoders are one way to discover these symbolic representations. Autoencoders model mappings to and from a latent space for a given dataset. Exposing this underlying distribution allows us

to manipulate latent processes to decode into domain-relevant text with desired attributes (Bowman et al., 2016).

In this work, we propose an autoencoder that models observed text datasets as being generated from 057 underlying code with a dataset-level function library. Our method is non-parametric and leverages in-context learning (ICL) (Brown, 2020) with per-dataset demonstrations to model the encoder, de-059 coder and prior of the latent codespace. Code as the latent representation allows us to use determin-060 istic programmatic and neural interpreters (Li et al., 2024) to map from latent space back into text. 061 We sustain coverage over all task domains with code programs by interleaving compute operations, 062 fact retrieval, and reasoning steps as necessary. Code programs are composed of modular function; 063 we use these functions to conditionally sample from the latent space to sample and produce text 064 according to target attributes.

065 Our method extracts the symbolic latent space underlying different datasets with minimal human 066 effort by inducing an unsupervised non-parametric autoencoder from a set of given text examples. 067 In this paper, we show that across a variety of datasets, our method effectively unveils underlying 068 symbolic patterns in the datasets. Samples from the induced latent codespace produce more correct 069 and domain-relevant text examples than do non-latent modeling approaches and latent modeling approaches without code as the latent representation. We find that leveraging an executable latent 071 representation is particularly helpful in task settings that are compositional and algorithmic in nature. We also evaluate the effect of using our method to generate synthetic data to train a downstream 072 model for a given task. 073

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2 A NON-PARAMETRIC LATENT MODEL FOR DATASETS

Define a dataset as $x = \{x_i = (t_i, y_i)\}^N$, consisting of a sequence of text-output pairs. We are interested in defining a latent representation of this dataset, $z = \{z_\ell, z_1, \ldots, z_N\}$ consisting of a global term z_ℓ and datapoint specific terms z_i . For each datapoint, we are interested in finding a latent symbolic representation $z_i \in \mathbb{Z}$. In addition, we posit that the dataset has a global shared library structure z_ℓ .

082 Our goal is to infer the latent representation z from the dataset. We write this as a posterior inference 083 problem, p(z|x). Inference of this distribution is intractable since it requires marginalizing over all 084 representations. Instead, optimize a variational posterior q to approximates this objective:

$$\begin{aligned} \arg\min_{q} \mathrm{KL}(q(z|x) \mid\mid p(z|x)) &= \mathrm{KL}(q(z_{\ell}|x) \mid\mid p(z_{\ell}|x)) + \mathop{\mathbb{E}}_{z_{\ell} \sim q(z_{\ell}|x)} \sum_{i} \mathrm{KL}(q(z_{i} \mid z_{\ell}, x_{i}) \mid\mid p(z_{i}|z_{\ell}, x_{i})) \\ &= \mathrm{KL} + \mathop{\mathbb{E}}_{z_{\ell}, z_{i} \sim q} \log \frac{q(z_{i} \mid z_{\ell}, x_{i})}{p(x_{i}|z_{i}, z_{\ell})p(z_{i}|z_{\ell})}. \end{aligned}$$

where the first step comes from KL identities and the assumption that each datapoint x_i is conditionally independent of z_j given the library z_ℓ , and the second step factors out each x_i .

To fully specify the variational objective, we need a variational family for q. In deep learning, it is common to paramaterize q and use gradient descent to minimize this equation. Instead, we use a nonparametric approach to search over a subset of concrete exemplars \mathcal{D} , as example-latent representation pairs. Specifically \mathcal{D} consists of a base library and example-symbol pairs, i.e. $\mathcal{D} = \{\bar{z}_{\ell}, (\bar{x}_1, \bar{z}_1), \dots, (\bar{x}_M, \bar{z}_M)\}$. Given a specific set \mathcal{D} , the variational posterior can be defined through in-context learning (ICL) (Brown, 2020). For each datapoint this is $q(z_i|x_i, z_\ell; \text{ICL}(\mathcal{D}))$, and the full objective is:

$$\arg\min_{\mathbf{D}} \mathrm{KL}(q(z|x;\mathcal{D}) \mid\mid p(z|x))$$

We need to solve this objective by finding the best subset \mathcal{D} for the dataset. This is a combinatorial optimization problem and is intractable to solve by search. We approximate this with rejectionsampling additions to the library and new \bar{z}_j examples. We apply an iterative optimization starting from \mathcal{D}^0 . For a given dataset example x_j , we sample \tilde{z}_ℓ and \tilde{z}_j from the variational posterior, as described above, and reject \tilde{z} that do not score well according to the log ratio. Library-representations pairs that score well are included in the next \mathcal{D}^{j+1} , roughly:

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$$D^{j+1} = D^{j} \cup \{ \tilde{z}_{\ell}, (x_{j}, \tilde{z}_{j}) \}$$
(1)

¹⁰⁸ 3 RELATED WORKS

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Autoencoding Datasets Prior work has explored methods for inducing and analyzing latent vari-111 ables for datasets. Bowman et al. (2016) introduce a RNN-based variational autoencoder (Kingma, 112 2013), which interpolates and generates coherent novel sentences by learning and sampling from 113 a continuous posterior. In contrast, our approach operates within a structured discrete latent space 114 that allows for direct inspection and execution. Friedman et al. (2022) present a method to diag-115 nose datasets by inducing an underlying context-free grammar per dataset to identify "shortcuts" 116 from which they construct adversarial examples to challenge models trained on said datasets. Other works (Qiu et al., 2024; Madaan et al., 2022) study LLMs' ability to propose structured hypotheses 117 over data and apply those hypotheses to new datapoints during inference. Though not explicitly 118 framed as autoencoders, these methods share a similarity with ours, as they refine an "encoder" 119 (structured hypothesis proposer) alongside a static "decoder" (hypothesis interpreter). However, 120 these approaches require hypotheses to satisfy certain symbolic constraints, and therefore constrain 121 their study to a limited set of symbolic tasks. In contrast, our work uses deterministic and neural 122 program execution, allowing us to model a broader range of any text task.

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Library Learning and Program Induction The advantages of breaking programming tasks into 125 subprograms (Zelikman et al., 2022a) and inducing a shared library of reusable subprograms have 126 been demonstrated in prior research. For example, DreamCoder (Ellis et al., 2021) is a wake-sleep 127 algorithm for Bayesian program induction that cycles between searching for programs, building 128 a library of common concepts in the domain, and training a neural search policy on recalled and 129 sampled programs. Similarly, Wang et al. (2024) develop a method to induce a library of verifiable 130 and efficient subprograms during inference. In our work, we induce a development set that optimizes 131 our autoencoding objectives, but unlike these prior works, our approach does not require code to be 132 fully executable. We instead use imagined functions, as in the Chain-of-Code framework (Li et al., 133 2024), which are emulated by a LLM.

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135 **Intermediate Reasoning with LLMs** As LLMs become increasingly capable in language tasks, 136 they have been used for more complex tasks requiring multi-step reasoning (Zhao et al., 2023a;b). 137 Prior works show that prompting a model to "think aloud" during inference enhances their per-138 formance on tasks requiring reasoning (Wei et al., 2022; Nye et al., 2021). To address LLMs' 139 limitations in handling computational tasks or recalling updated facts, tools such as code execution, 140 internet queries, and SMT solvers have been integrated into inference pipelines (Li et al., 2024; Chen et al., 2023; Schick et al., 2023; Press et al., 2023; Lee et al., 2024). Reasoning has also 141 142 been integrated back into the model parameters: the Self-Taught Reasoner (Zelikman et al., 2022b) 143 fine-tunes a model on its own produced and verified reasoning strings. While these works improve inference-time reasoning, they are constrained to the scope of the given data, and they do not attempt 144 to infer structural properties of the dataset itself, which is a focus of our work. 145

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4 A CODESPACE AUTOENCODER FOR LANGUAGE

To apply our framework to extracting code representation, we describe how each term described in Equation 1 can be implemented with code LLMs and interpreters. First we establish the shared structure z_{ℓ} as the library of code functions used by latent code programs of the dataset. Each (x_i, z_i) instance of \mathcal{D} is a paired language example and corresponding code program.

The encoder is implemented as a LLM prompted by dataset-level demonstrations \mathcal{D} via ICL to sample code programs for a given language task instance. The ICL(\mathcal{D}) operation creates a prompt composed of a program induction instruction and example-program pairs of the demonstration set. We are limited by context window size, so we condition on a randomly selected subset rather than all exemplars in \mathcal{D} . We initialize program induction with a hand-written set of domain-general exemplars. These exemplars, prompt instructions, and templates are shared in the Appendix B.

160 The terms in the denominator are a prior $p(z_i|z_\ell)$ over code representations and a decoder $p(x_i | z_i, z_\ell)$ from latent representation back to text. For code, the prior is established by a compiler that rewards syntactically valid programs: $p(z_i | z_\ell) = \mathbb{1}(\text{compiles}(z))$.



Figure 2: The underlying symbolic structure of observed text data (top) is represented by a shared function library and programs (bottom). We search for the set of demonstrations \mathcal{D} that optimizes the variational posterior. We sample from the induced posterior to synthesize new text (right).

Algorithm 1 Codespace Autoencoder Pseudocode	
procedure INFER $(x = \{x_i = (t_i, y_i)\}, \gamma)$	
$\mathcal{D} \leftarrow \{z_\ell^0, []\}$	initialize library and exemplars
for $x_i = (t_i, y_i)$ do	
for $ ilde{z}_\ell, ilde{z}_i \sim q$ do	▷ sample library additions, programs
if $\neg COMPILES(\tilde{z}_i)$ then	⊳ validate syntax
reject	
$\tilde{z}_i(t_i) \leftarrow \operatorname{Exec}(\tilde{z}_i, t_i)$	⊳ execute program
if $textsim(\tilde{z}_i(t_i), y_i) < \gamma$ then	▷ reject samples that fail reconstruction
reject	
$\mathcal{D} \leftarrow \mathcal{D} \cup \{ \tilde{z}_{\ell}, (x_i, \tilde{z}_i) \}$	▷ add to library, save exemplar
break	
return \mathcal{D}	

The decoder term $p(x_i \mid z_i, z_\ell)$ measures how well the sampled code program reconstructs the observed data when executed with the given input. The term is decomposed into terms for the text input and output. The text input is given, so $p(t \mid z) = 1$.

$$p(x \mid z) = p(t \mid z) \times p(y \mid z, t) = p(y \mid z, t)$$

We approximate reconstruction accuracy $p(y \mid z, t)$ with text similarity metric threshold γ :

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$$p(y \mid z, t) = \begin{cases} 1, & \text{textsim}(z(t), y) > \gamma \\ \epsilon & \text{otherwise} \end{cases}$$

For reconstruction z(t), we use a combination of a real interpreter and LLM interpretation.

To cover the scope of NLP tasks that cannot easily be performed programmatically, we allow sampling of programs with interleaved real code lines and imagined functions. We follow the **Chainof-Code** (Li et al., 2024) method of using a Python interpreter as the real interpreter and a LLM as the imaginary interpreter. Specifically, for each line in a code program, we first attempt to execute it with a Python interpreter. If that fails, then we query a LLM to emulate the execution of that code line. The program state is then updated accordingly.

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An overview of our method is sketched in Figure 2, and pseudocode presented in Algorithm 1.

A Textspace Autoencoder for Language To isolate the benefits of code as the latent representation, we consider another representation modality for the latent space: text. Here, we describe the autoencoder model framework in terms of a text-based latent representation: chain-of-thought (CoT) (Wei et al., 2022). Following the keyword prompting methodology of the TinyStories-Instruct (Eldan & Li, 2023) dataset, we describe the shared structure z_{ℓ} as a library of unique keywords used by latent CoT strings of the dataset. Each (x_i, z_i) instance of \mathcal{D} is a paired language example and the corresponding CoT string. The ICL(\mathcal{D}) operation creates a prompt in the same fashion, but using CoT-relevant domain-general exemplars. These exemplars and prompts are shared in the Appendix B.2. The prior over CoT is established by a string checker that rewards strings with a certain CoT template:

$$p(z_i|z_\ell) = \mathbb{1}(z_i = "*$$
 So the answer is $*")$

Reconstruction accuracy is evaluated in the same way as for latent code representations, and the "execution" of the latent representation is string extraction.

5 POSTERIOR SAMPLING

Once we find a \mathcal{D} that optimizes our variational objective, we use it to sample more synthetic examples. Sampling new text from a given dataset is factorized in our autoencoder as follows:

$$p(x_s \mid x_{1:N}) = \sum_{x} p(x_s \mid z, x_{1:N}) p(z \mid x_{1:N})$$

$$= \mathbb{E}_{z \sim p(z|x_{1:N})} p(x_s \mid z, x_{1:N})$$

$$\approx \mathbb{E}_{z \sim q(z|x_{1:N}; \mathcal{D})} p(x_s \mid z, x_{1:N})$$

$$\approx \mathbb{E}_{z_{\ell}, z_s \sim q} p(x_s \mid z_s, z_{\ell}, x_{1:N})$$

The conditioning on $x_{1:N}$ gives us the \mathcal{D} terms. This is used to sample our library z_{ℓ} and to sample the program z_s . Since we do not have access to the observation x_s we sample the z_s using ICL that is unconditioned on the specific text datapoint.

Once sampled from the latent space, observed data x_s is decoded from z_s . A natural language input t_s is proposed for the sampled program, and the program z_s is executed to produce output y_s .

$$p(x_s \mid z_s, z_\ell, x_{1:N}) = p((t_s, y_s) \mid z_s, z_\ell, x_{1:N}) = p(t_s \mid z_s, z_\ell, \{t_i \mid (t_i, y_i) \in x_{1:N}\}) \times p(y_s \mid z_s, t_s)$$

6 EXPERIMENTAL SETUP

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Dataset: Super-NaturalInstructions (SNI) (Wang et al., 2022) is a dataset of 1616 diverse NLP tasks, with expert-written instructions and over 5 million total data instances. The tasks cover 76 task types, some of which can be solved deterministically by a simple computer program (e.g. adding every third element of a list) and some of which are non-algorithmic natural language tasks. We use this categorization by algorithmic and non-algorithmic to study our method on a range of SNI tasks.

We divide the SNI training tasks into sets of 100 in-domain (ID) and 100 out-of-domain (OOD) tasks. Both sets of tasks are composed of 33% tasks with a "synthetic" (algorithmic) source. A latent space is induced for each ID task. Evaluation on the held-out examples from ID tasks comprise ID evaluation, and evaluation with the OOD tasks comprise OOD evaluation.

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Baselines: We compare against two baseline methods. To measure the value of latent modeling, we compare our method against a direct inference (no intermediate reasoning) interpolation baseline. Interpolation uses LLM prompting to generate new data points based on an ICL prompt of the dataset text instances, and does not use a latent space. To measure the value of using code programs as the latent representation, we compare our method against using chain-of-thought (Wei et al., 2022) as the latent representation, as described in Section 4.

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Prompts: All generations are produced by prompting the LLM with instructions and 4 in-context exemplars, or up to the maximum context length. Specific prompts are shared in the Appendix B.

We use 4 hand-written examples of input, programs, and output from the original Chain of Code paper (Li et al., 2024) as seed demonstrations to initialize the model fitting phase. Half of the examples are modified to use the internet search query internet_lookup() functionality that we add to LLM-emulation. These examples are shared in the Appendix B.1.

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270		Recovery Rate (top	o-1 sampling)
271	Latent Rep.	Domain-general ICL	Induced \mathcal{D} ICL
272	-	8	
	CoT	67.25	86.33
273	Code	53 75	70.67
274	Coue	55.75	, 0.07

Table 1: Autoencoding recovery rate increases when conditioned on the induced demonstrations \mathcal{D} . Measured across 1,200 instances across 100 different tasks; Llama3.1 8B model.

Autoencoding Parameters: We experiment with different demonstration set sizes $N \in \{12, 24\}$. We use 2 LLMs of different size: Mistral AI's Mixtral 8x22b Instruction-tuned model (Jiang et al., 2024) and Meta's Llama3.1 8b Instruction-tuned model (Dubey et al., 2024). We use a temperature of 0.7 and top-p value of 0.9. For data generation, we sample $M = \{40, 240\}$ latent representations from the posterior and decode them into text examples.

Executed latent representations are validated using ROUGE-L (Lin, 2004) and BLEU (Papineni et al., 2002) as the text similarity metrics, with corresponding thresholds $\gamma_R = 0.4$ and $\gamma_B =$ 0.3. During posterior sampling, code execution is validated by ICL-prompting a verifier LLM with examples from the demonstration set. Specific details are shared in Appendix A.

LLM-Emulation Parameters: Programs are executed with interleaved execution by the Python interpreter, internet_lookup() with the duckduckgo search engine API (ddg), and LLMemulation with the generating model. The code to do this is slightly modified from that of the Chain of Code (Li et al., 2024) resources, and shared in our publicly-available repository ¹.

293 Synthetic Data Generation Evaluation Training Parameters: Evaluation of synthetically-294 generated data for downstream model training is measured by fine-tuning a Pythia 1.4B model (Bi-295 derman et al., 2023) on the synthesized text examples then evaluating the performance on the heldout test set. The model is trained with 12k steps, batch size 16, DeepSpeedFusedAdam optimizer, 296 and learning rate of 1e-5. 297

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7 RESULTS

301 In this section, we test the effectiveness of our method to identify the underlying symbolic space 302 of a dataset. We measure this by evaluating first how well our symbolic representations are able to 303 recover the original datasets. We then evaluate how well samples from the latent space cover the 304 underlying task domain. Finally, we present results on using the latent space to generate synthetic training data. 305

7.1 FAITHFULNESS OF SYMBOLIC AUTOENCODING

308 We evaluate the extent to which the induced dataset structure and induced exemplars \mathcal{D} optimizes the 309 variational posterior. Using a held-out x_i datapoint, we compare the autoencoder recovery rate when 310 conditioning on our induced \mathcal{D} versus conditioning on a \mathcal{D} just of domain-general demonstrations, 311 i.e. the hand-written domain-generic seed ICL demonstrations. Specifically we compute 312

$$(z_{\ell}, z_j) \sim q(z \mid \{x_j\}; \mathcal{D}) \quad \tilde{x_j} \sim p(x \mid z_j, z_{\ell}),$$

314 and compare \tilde{x}_j to x_j . 315

Table 1 shows that the variational method improves the autoencoding ability over the baseline 316 method for code latent space. We also include evaluation using the CoT-based latent space, where inducing \mathcal{D} also leads to improved recovery.

7.2 EVALUATING THE IDENTIFIED SYMBOLIC SPACE

321 Our goal is to find a latent space from which more programs z_s can be effectively sampled and 322 executed to produce new dataset examples. We compare against the latent CoT baseline, which uses 323

¹released after anonymity period

Task type	Method	Correc Human	Correctness %Domain RelevanceHumanGPT-40HumanGPT-40GPT-40		Relevance % GPT-40	Avg. cossim (\downarrow)	
Algo.	Gold	-	60	-	100	0.81	
Non-algo.	Gold	-	61.7	-	90	0.53	
			Llama3.1	8B			
	Sampling	61.7	18.3	65.0	48.3	0.59	
Algo.	Latent CoT	50	20.0	93.3	90	0.89	
-	Latent Code	78.3	50	96.7	88.3	0.85	
	Sampling	65.0	38.3	43.3	56.7	0.52	
Non-algo.	Latent CoT	60	43.3	96.7	85.0	0.78	
	Latent Code	81.7	36.7	68.3	45.0	0.76	
			Mixtral 8x	22b			
	Sampling	-	20.0	-	100	0.94	
Algo.	Latent CoT	-	38.3	-	98.3	0.94	
-	Latent Code	-	60.0	-	96.7	0.88	
	Sampling	-	60.0	-	100	0.86	
Non-algo.	Latent CoT	-	63.3	-	86.7	0.89	
	Latent Code	-	45.0	-	91.7	0.85	

Table 2: Human, GPT-4o-mini, and diversity evaluation of algorithmic and non-algorithmic text samples from different methods. For each method, we synthesize 240 examples. We examine 3 random algorithmic and 3 random non-algorithmic SNI tasks. Correctness and domain relevance is examined across 20 random samples per task. Diversity is measured with average embedding cosine similarity to centroid per task for all 240 synthesized instances.

a non-symbolic latent space composed of z_i as textual descriptions, and the interpolation baseline, which does not use a latent space.

We aim for examples that are correct, in-domain, and diverse. We evaluate this by sampling points as described in Section 5 for different algorithmic and non-algorithmic tasks. For correctness and domain relevance, we use GPT-4o-mini evaluation ² for 20 examples per method per task, for 6 total tasks: 3 algorithmic and 3 non-algorithmic. Human evaluation numbers are provided for the Llama3.1 8B generations as a control against the GPT-4o-mini judgements. For diversity, we mea-sure average cosine similarity between the Sentence-BERT embedding (Reimers & Gurevych, 2019) centroid for the synthesized dataset and each individual sentence embedding, a more tractable ap-proximation for average pairwise cosine similarity used in prior works for diversity (Tevet & Berant, 2021). These results are summarized in Table 2.

Latent modeling methods produce more consistently domain-relevant and correct examples, though samples from the interpolation baseline become more domain-relevant with a larger model. Between using CoT and code as the latent representation, using code produces more correct data in algorith-mic tasks and using CoT produces more correct data in non-algorithmic tasks. Diversity metrics, when observed with the domain relevance analysis, shows that the sampling baseline produces very diverse data to the point of being out-of-domain, and latent code produces slightly more diverse data than latent CoT.

7.3 SAMPLING SYNTHETIC TRAINING DATA

We compare the results of training a downstream model with data synthesized using our approach versus data synthesized by baseline methods. For these experiments, we train the downstream model on instances synthesized for a group of tasks then evaluate the resulting model on both in-domain and out-of-domain tasks. Table 3 summarizes the resulting performance. In our experiments, data from the sampling baseline generally outperforms data sampled from the latent modeling method. At times, data from the sampling baseline even outperforms Gold data provided by the original dataset.

²Prompt details in Appendix B.3

Synth	esis Parameter	s		OOD ROUGE		ID I	ROUGE
Method	Method Model #Seeds			Algo.	Nonalgo.	Algo.	Nonalgo.
Gold	Gold ; 40 examples			23.09	22.73	40.83	50.12
Sampling	L3.1 8B	24	40	22.89	31.07	31.77	40.66
	Mix 8x22b	24	40	23.89	31.24	35.97	44.39
Latent CoT	Latent CoT Mix 8x22b 2		40	21.92	30.56	34.05	39.14
Latent Code	L3.1 8B	24	40	25.64	28.33	33.22	38.62
	Mix 8x22b 24				31.41	34.22	39.94
Gold	Gold ; 240 examples			24.57	29.15	50.90	57.09
Sampling	L3.1 8B	12	240	22.62	33.2	35.08	44.04
	Mix 8x22b	12	240	20.93	30.43	43.13	48.67
Latent CoT	Mix 8x22b	12	240	20.41	29.23	30.75	39.43
Latent Code	L3.1 8B	12	240	21.72	30.33	32.65	38.22
	Mix 8x22b	12	240	22.12	30.21	35.64	36.91

Table 3: Downstream training results on SNI suggest that the interpolation baseline performs best, at times even yielding higher performance than using Gold data.

Model	Subset	% Programs Using Emulation	Avg. % LLM-emulated lines
L3.1 8B	Algorithmic	0	0
	Non-algorithmic	1.8	0.2
M8x22B	Algorithmic	2.0	0.2
	Non-algorithmic	17.8	2.6

Table 4: Induced latent code programs tend to rarely require LLM-emulation. Non-algorithmic tasks and larger models are more likely to leverage LLM-emulation.

8 QUALITATIVE ANALYSIS

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How often do we LLM-emulate? Table 4 shows the rate of LLM-emulation in code programs in the induced demonstration set. The vast majority of programs are fully deterministically executable, but non-algorithmic tasks tend to use more lines of code that must be LLM-emulated. Larger models perform LLM-emulation more accurately (Li et al., 2024), and are more likely to propose lines that will be LLM-emulated.

An advantage of using code as the latent representation is the transparency of its execution. We can inspect the execution trace ³ to gain insight into what makes the latent code programs correct or incorrect. Example code programs from the induced demonstration sets, along with paired snippets from their execution trace, are shared below:

```
417
                                                     [...]
        Listing 1: This program returns integers
                                                     line: result = []
418
         with certain conditions. This task can
                                                     explanation: Python execution.
419
                                                     delta state: {'answer': []}
        be done entirely programmatically.
                                                     line: for num in numbers:
420
         def get_same_start_end(nums):
                                                     explanation: Python execution.
421
           result = []
                                                     delta state: { num': -98}
           for num in nums:
                                                     line: str_num = str(abs(num))
422
             str_num = str(abs(num))
                                                     explanation: Python execution.
423
             if str_num[0] == str_num[-1] or (
                                                     delta state: {'str_num': '-98'
                  len(str_num) > 1 and str_num
                                                     line: if str_num[0] == str_num[-1] or (len(str_num)
424
                  [0] > str_num[-1]):
                                                          > 1 and str_num[0] > str_num[-1]):
425
               result.append(num)
                                                     explanation: Python execution.
           return result
                                                     delta state: { }
426
                                                     line: for num in nums:
427
                                                     explanation: Python execution.
                                                     delta state: { 'num': 55}
428
                                                     [...]
429
                                                     final state: {'result': [44, 2, 98]}
430
```

³we follow the Chain-of-Code Li et al. (2024) template for LLM-emulated traces

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	Listing 2: To classify tweet toxicity, generated code imports and uses the NLTK sentiment analyzer.	<pre>l] delta state: {'task_input': 'Categorize the comment on the basis of toxicity input: I hate them' } line: comment = extract comment(task input)</pre>
	import nltk	explanation: Let's think step by step. The
	from nltk.sentiment import	task input variable has a full task description
	SentimentIntensityAnalyzer	, then a specified input So the answer is "I
İ	<pre>nltk.download('vader_lexicon')</pre>	hate them"
	<pre>def solve_task(task_input):</pre>	<pre>delta state: {'comment': 'I hate them'}</pre>
	<pre>comment = extract_comment(</pre>	<pre>line: sia = SentimentIntensityAnalyzer()</pre>
	task_input)	explanation: Python execution.
	<pre>sia = SentimentIntensityAnalyzer()</pre>	delta state: {'sia': nltk.sentiment.
	scores = sia.polarity_scores(SentimentIntensityAnalyzer object}
	comment)	line: scores = sia.polarity_scores(comment)
	if scores['compound'] < -0.5:	explanation: Python execution.
	answer = "Yes"	delta state: {'scores': {'neg': 0.787, 'neu': 0.213,
	else:	'pos': 0.0, 'compound': -0.5719}}
	answer = "No"	[]
	return answer	<pre>final state: {'answer': 'Yes'}</pre>

Listing 3: To generate a question that every entity in an input list can be a valid answer to, generated code relies entirely on an imagined function: construct_question

```
def solve_task(task_input):
 answers = task_input.split(", ")
 question = construct_question(
      answers, ret_type="str")
  return question
```

<pre>delta_state: {'task_input': 'Construct a question that every answer in the list is correct and reasonable for it. input: airplanes, snowflakes , footballs, cards/valentines, paper dolls, crane/bird'}</pre>
<pre>line: answers = task_input.split(", ")</pre>
explanation: Python execution
<pre>delta state: {'answer': ['Construct a question</pre>
airplanes', 'snowflakes', 'footballs', 'cards/
<pre>valentines', 'paper dolls', 'crane/bird']}</pre>
<pre>line: question = construct_question(answers,</pre>
ret_tyep="str")
explanation: Let's think step-by-step. All of these
[] So the answer is name something that kids
make out of paper
delta state: {'question': 'name something that kids
<pre>make out of paper' }</pre>

Does the shared structure of the latent space reflect underlying patterns of the task? Table 5 lists the most popular functions for some algorithmic and non-algorithmic SNI tasks. The most popular functions correspond with reasoning steps relevant to the task. For example, evaluating arithmetic under swapped operator strings mandates heavy use of string substitution (re.sub) and expression evaluation (eval). For less algorithmic tasks such as abductive reasoning in generating text to support health facts, functions related to inferring conclusions from facts such as complete_story and generate_sentence are popular. Hybrid tasks such as typo identification use low-level operations such as word_tokenize as well as high-level composed or imagined functions such as get_typo.

Task	Most frequently used functions
Get elements of list between given indices	list_elements,get_elements
Arithmetic under swapped operators	eval,re.sub
Identify typos	<pre>word_tokenize,get_close_matches,get_typo</pre>
Generate text to support health facts	generate_claim,is_supported
Write the middle sentence of a story	complete_story,generate_sentence

Table 5: Popular functions by task.

CONCLUSION

In this work, we present and apply a framework for extracting a latent symbolic representation from any text dataset in an unsupervised manner and without updating any model parameters. We use code programs as the latent representation, and present results comparing the resulting latent space to a non latent modeling approach and to using a text-based latent representation. Our findings show that a codespace autoencoder for language tasks effectively extracts an underlying symbolic
representation for language tasks. We show that code being inherently modular and executable
offers advantages in correctness, particularly for algorithmic tasks, and lends well to interpreting the
induced latent space. We believe that the methods and findings presented in this paper are applicable
to future work in analyzing properties of datasets and generating data, both desired and undesired,
and generating data for downstream tasks.

ETHICS STATEMENT

One point of concern with this work is the ability to use the proposed methodology to generate foul or ill-harming text if given an input dataset exhibiting some of those patterns. We observed several concerning generations in tasks about classifying properties of toxic text, and caution any future practitioners to be aware of this potential danger.

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Reproducibility Statement

We take several steps towards reproducibility. First, we plan to release all code and prompts in a self-contained repository. Additionally, all experiments are run using open-sourced models and datasets that are publicly available on Huggingface. The code repository, publicly-available datasets, and open-source language models make almost all experiments of this paper reproducible. The only numbers that may be inconsistent across reproductions of the experiment are the human evaluation results and GPT-verification results of Table 2.

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A VERIFYING SYNTHESIZED EXAMPLES

A challenge of synthesizing correct examples is the lack of a ground truth output against which to verify the execution of the sampled latent code program. For this, we parameterize a verifier LLM with the learned demonstration set \mathcal{D} by collecting seed demonstrations (z, x, y) according to their reconstruction success $p(x, y \mid z)$. Successful reconstructions are saved as positive examples $v^+ =$ $\{(z, x, y : z(x) \equiv y)\}$ and failed reconstructions as negative $v^{\times} = \{(x, y_{\times}, z_{\times} : z_{\times}(x) \neq y_{\times})\}$. The verifier LLM is parameterized using ICL with these positive and hard negative examples to predict the correctness of an input demonstration:

$$p(x_s, y_s, z_s \mid \mathcal{D}) := p(x_s, z_s(x_s), z_s \mid v^+, v^\times)$$

B PROMPTS

Listing 4: Program induction instruction

Write the Python code to perform the given task. The 'task_output' variable at the end should contain the response to the instruction.

Listing 5: Input generation instruction

Write the natural language instruction that describes what is done by the given Python code. Provide the instruction and all relevant inputs.

Listing 6: Instruction for posterior sampling of latent code programs

Write a sni	ippet of	Python	code t	o compl	ete s	some	task.	The	code
should u	use the	followir	ng func	tions:	{keyv	word	s}.		

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B.1 HAND-WRITTEN EXEMPLAR DEMONSTRATIONS

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                   Listing 7: Demo examples for latent code variational inference.
760
761
      Which sentence has the correct adjective order:
762
      Options:
763
      (A) rubber terrible ship
764
      (B) terrible rubber ship
      --> (B)
765
      # CODE START
766
      import numpy as np
767
      def solve_task(task_input):
768
        options = extract_options(task_input)
        priority = {"opinion": 1, "size": 2, "age": 3, "shape": 4, "
770
            color": 5, "origin": 6, "material": 7, "purpose": 8}
771
        valid_types = list(priority.keys())
772
        scores = []
773
        for option, sentence in options.items():
774
          adjectives = sentence.split(" ")[:-1]
          order = [priority[get_adjective_type(adjective, valid_types,
775
              ret_type=str)] for adjective in adjectives]
776
          scores.append([order[i+1] > order[i] for i in range(len(order)
777
               - 1)].count(True))
778
        answer = list(options.keys())[np.argmax(scores)]
779
        return answer
780
      # CODE END
781
782
      How many countries have I been to? I've been to Bilbao, Death
783
         Valley, Paris, Honolulu, Skye.
784
      --> 4
785
      # CODE START
      def solve_task(task_input):
786
        places = extract_places(task_input)
787
        countries = set()
788
        for place in places:
789
          search_result = lookup_on_internet(f"what country is {place}
790
              in?")
791
          country = extract_country(search_result)
792
          countries.add(country)
793
        answer = len(countries)
794
        return answer
795
      # CODE END
796
      Today is Christmas Eve of 1937. What is the date 10 days ago in MM
797
         /DD/YYYY?
798
      --> 12/14/1937
799
      # CODE START
800
      import datetime
801
      def solve_task(task_input):
802
        parsed_task_input = extract_arguments(task_input)
803
        today = datetime.date(year=parsed_task_input['year'], month=
804
            parsed_task_input['month'], day=parsed_task_input['day'])
805
        date = today - datetime.timedelta(days=parsed_task_input['
806
            days_ago'])
807
        answer = date.strftime("%m/%d/%Y")
        return answer
808
      # CODE END
809
```

```
810
      Recommend a movie similar to Star Wars Episode IV - A New Hope,
811
         Indiana Jones and the Last Crusade, Star Wars Episode V - The
812
         Empire Strikes Back, The Big Lebowski:
813
      --> Blade Runner (1982)
814
      # CODE START
815
      def solve_task(task_input):
        ref_movies = extract_reference_movies(task_input)
816
        ref_movie_infos = []
817
        for movie in ref_movies:
818
          search_result = lookup_on_internet(f"{movie} release year and
819
             genre")
820
          release_year = extract_year(search_result)
821
          genre = extract_genre(search_result)
822
          ref_movie_infos.append((genre, release_year))
823
        answer = get_most_similar_movie(ref_movies, ref_movie_infos,
824
           ret_type="str")
825
        return answer
      # CODE END
826
```

B.2 CHAIN-OF-THOUGHT PROMPTS

827 828

829 830

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840

841

842

843 844 845

Listing 8: CoT induction instruction

Write the thought process to perform the given task.

Listing 9: Input generation instruction for latent CoT

Write the natural language instruction that describes what is shown by the given thought process. Provide the instruction and all relevant inputs.

Listing 10: Instruction for posterior sampling of CoT

Write out the thought process that completes some task. The thought process should include the following terms: {keywords }.

Listing 11: Demo examples for variational inference of latent CoT.

```
846
      Which sentence has the correct adjective order:
847
      Options:
848
      (A) rubber terrible ship
849
      (B) terrible rubber ship
850
      --> (B)
      Let's think step by step.
851
      The priority of adjective categories is, in order: opinion, size,
852
         age, shape, color, origin, material, purpose.
853
      rubber: material
854
      terrible: opinion
855
      The opinion adjective should come before the material adjective. '
856
         terrible rubber ship' follows the correct adjective order. So
857
         the answer is (B).
858
859
      How many countries have I been to? I've been to Bilbao, Death
860
         Valley, Paris, Honolulu, Skye.
861
      --> 4
      Let's think step by step.
862
      We'll group by countries and count:
863
      1. Spain: Bilbao
```

```
864
      2. USA: Death Valley, Honolulu
865
      3. France: Paris
866
      4. UK: Skye
867
      There are 4 countries in total. So the answer is 4.
868
869
      Today is Christmas Eve of 1937. What is the date 10 days ago in MM
870
         /DD/YYYY?
      --> 12/14/1937
871
      Let's think step by step.
872
      Christmas Eve of 1937 is 12/24/1937.
873
      To get the date 10 days ago, subtract 10 from the date section. So
874
          the answer is 12/14/1937.
875
876
      Recommend a movie similar to Star Wars Episode IV - A New Hope,
877
         Indiana Jones and the Last Crusade, Star Wars Episode V - The
878
         Empire Strikes Back, The Big Lebowski:
879
      --> Blade Runner (1982)
880
      Let's think step by step.
      The genre and release year of each of the reference movies are:
881
      Star Wars Episode IV - A New Hope: Sci-fi/Action (1977)
882
      Indiana Jones and the Last Crusade: Adventure/Action (1989)
883
      Star Wars Episode V - The Empire Strikes Back: Family/Sci-fi
884
          (1980)
885
      The Big Lebowski: Comedy/Crime (1998)
886
      A similar movie should have a release date in 1970-2000 and be Sci
887
         -fi/Action/Crime. So the answer is Blade Runner (1982).
888
```

B.3 MEASURING DATA QUALITY WITH GPT-40-MINI

892 893 894

889 890 891

Listing 12: Instruction prompt to verify data quality

895 You are tasked with evaluating the following instances for correctness 896 and domain relevance. 897 Please: 898 1. In [CORRECT] and [/CORRECT] tags, state if the output seems correct 899 based on the input and domain task description. Write Yes or No. 900 2. In [RELEVANT] and [/RELEVANT] tags, assess if the input and output are 901 relevant to the specified domain (e.g., the context of the 902 experiment). Write Yes or No. Provide your reasoning for each answer, if necessary. 903 904 Domain task description: Provide a movie recommendation. 905 Input: Recommend a movie similar to Star Wars Episode IV - A New Hope, 906 Indiana Jones and the Last Crusade, Star Wars Episode V - The Empire 907 Strikes Back, The Big Lebowski: Output: Blade Runner (1982) 908 1. All of these movies are action movies released around 1990 to 2010. So 909 Blade Runner (1982) is an appropriate recommendation. [CORRECT]Yes[/ 910 CORRECT] 911 2. The task is to provide a movie recommendat. This is domain-relevant. [RELEVANT] Yes [/RELEVANT] 912 913 Domain task description: Identify whether the given comment is severely 914 toxic. 915 Input: Sammy wanted to go to where the people were. Where might he go?\ 916 nOptions: (a) race track (b) populated areas (c) desert (d) apartment 917 (e) roadblock Output: (b)

Domain task description: {task_description}

С SYNTHESIZED EXAMPLES

Input: {instance_input}

Output: {instance_output}

CORRECT]

Examples generated by the sampling baseline tend to be easier, out-of-domain, or incorrect. This is likely because sampling simply relies on surface-level generation and prefers generating strings with low perplexity, i.e. it is comfortable with.

1. People are at populous places, so if Sammy wants to go where the

2. The task is to identify whether a given comment is severely toxic.

Determining where Sammy wants to go has nothing to do with

identifying comment toxicity. [RELEVANT]No[/RELEVANT]

people are, he should go there. Option (b) is correct. [CORRECT]Yes[/

Listing 13: Mixtral 8x22b Sampling (incorrect)

In this task you will be given a list of integers. You should only
return an integer if the first digit is the same as the last
digit in the number. If an integer has a single digit, then it
should be returned. If there are no integers that start and
end with the same digit then an empty list ("[]") should be
returned.
input: [989, 597, 930, 637, 648, 647, -972, 943, 269, -486, 530,
974, 993, -631, 431, 979, -701, 560, -928, 935]
output: [989, 993]

Listing 14: Llama3 8.1b Sampling (very easy, OOD)

In this task you will be given a list of integers. You should only return an integer if the first digit is the same as the last digit in the number. If an integer has a single digit, then it should be returned. If there are no integers that start and end with the same digit then an empty list (""[]"") should be returned. input: [0, 1, 2, 3, 4, 5, 6, 7, 8, 9] output: [0, 1, 2, 3, 4, 5, 6, 7, 8, 9]

Examples generated by the latent CoT baseline are good at generating in-domain data, but are often wrong in algorithmic settings.

Listing 15: Llama3 8.1b Latent CoT Baseline (non-algorithmic, correct)

060	
961	In this task, you are given a description of a person (PersonX)
962	and a description of an event. You have to determine whether
963	the description of the person necessarily implies the
964	description of the event, or whether the description of the
065	person may imply the description of the event, or whether the
905	description of the person does not necessarily imply the
966	description of the event. Classify your answers into ""Yes"",
967	""No"", and ""Maybe"". The description of the person and the
968	event may also contain """", a placeholder that can be an
969	object, a person, and/or an action.
970	input: PersonX: PersonX bakes a cake <sep>Event: PersonX</sep>
971	accidentally drops the cake
	COT: Lets think step by step.

972 1. The description of PersonX is that they bake a cake. The 973 description of the event is that they accidentally drop the 974 cake. The two concepts do not match because the description of 975 the event does not imply that PersonX has a certain quality, 976 which is baking a cake. 3. The description of PersonX is that they bake a cake. The 977 description of the event is that they accidentally drop the 978 cake. The two concepts do not match because the description of 979 the event does not imply that PersonX has a certain quality, 980 which is baking a cake. 981 Therefore, the description of PersonX does not necessarily imply 982 the description of the event. 983 However, the description of PersonX may imply the description of 984 the event, because the description of the event is a direct 985 result of the description of PersonX. The description of 986 PersonX is that they bake a cake. The description of the event 987 is that they accidentally drop the cake. The two concepts may match because the description of the event is a direct result 988 of the description of PersonX. Therefore, the description of 989 PersonX may imply the description of the event. 990 However, the description of PersonX does not necessarily imply the 991 description of the event. The description of PersonX is that 992 they bake a cake. The description of the event is that they 993 accidentally drop the cake. The two concepts do not match 994 because the description of the event does not imply that 995 PersonX has a certain quality, which is baking a cake. 996 Therefore, the description of PersonX does not necessarily imply 997 the description of the event. 998 However, the description of PersonX may imply the description of 999 the event, because the description of the event is a direct result of the description of PersonX. The description of 1000 PersonX is that they bake a cake. The description of the event 1001 is that they accidentally drop the cake. The two concepts may 1002 match because the description of the event is a direct result 1003 of the description of PersonX. Therefore, the description of 1004 PersonX may imply the description of the event. 1005 However, the description of PersonX does not necessarily imply the 1006 description of the event. 1007 So the answer is Maybe. 1008

Listing 16: Llama3 8.1b Latent CoT Baseline (algorithmic, wrong)

1010	Listing 16: Llama3 8.1b Latent CoT Baseline (algorithmic, wrong)
1011	In this task, you need to remove all words of a given list in the
1012	sentence. The list of words to be removed is given, for
1013	example, the list ['bear','scissors', 'beach']. Ignore the
1014	words that are not present in the sentence.
1015	input: Sentence: 'a group of people are playing with food on the
1016	beach near a dark place hanging by a seat on the ocean with
1017	sand near a computer'. Remove all words in the given list: ['
1018	<pre>bear','scissors', 'beach'].</pre>
1010	input: a group of people are playing with food near a dark place
1019	hanging by a seat on the ocean with sand near a computer
1020	output: Let's think step by step.
1021	The 3 words to remove are 'bear','scissors', 'beach'.
1022	However, 'beach' is mentioned several times in the sentence, so we
1023	have to remove the first 'beach'.
1024	The sentence is: 'a group of people are playing with food on the
1025	beach near a dark place hanging by a seat on the ocean with
	sand near a computer'.

1026 1027 1028	So	the result dark place computer'.	is 'a gr hanging	oup o: by a	f people seat on	e are the	playi ocean	ng wi with	th food sand ne	near ear a	a
1029 1030	So	the answer dark place	is: a gr hanging	oup o bv a	f people seat on	e are the	playi ocean	ng wi with	th food sand ne	near ar a	a
1031		computer.		- 1 -				-			
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1035											
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1037											
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