REWARD UNCERTAINTY FOR EXPLORATION IN PREFERENCE-BASED REINFORCEMENT LEARNING

Xinran Liang¹, **Katherine Shu**¹, **Kimin Lee**^{1*}, **Pieter Abbeel**^{1*} ¹University of California, Berkeley

Abstract

Conveying complex objectives to reinforcement learning (RL) agents often requires meticulous reward engineering. Preference-based RL methods are able to learn a more flexible reward model based on human preferences by actively incorporating human feedback, i.e. teacher's preferences between two clips of behaviors. However, poor feedback-efficiency still remains a problem in current preference-based RL algorithms, as tailored human feedback is very expensive. To handle this issue, previous methods have mainly focused on improving query selection and policy initialization. At the same time, recent exploration methods have proven to be a recipe for improving sample-efficiency in RL. We present an exploration method specifically for preference-based RL algorithms. Our main idea is to design an intrinsic reward by measuring the novelty based on learned reward. Specifically, we utilize disagreement across ensemble of learned reward models. Our intuition is that disagreement in learned reward model reflects uncertainty in tailored human feedback and could be useful for exploration. Our experiments show that exploration bonus from uncertainty in learned reward improves both feedback- and sample-efficiency of preference-based RL algorithms on complex robot manipulation tasks from MetaWorld benchmarks, compared with other existing exploration methods that measure the novelty of state visitation.

1 INTRODUCTION

In reinforcement learning (RL), reward function specifies correct objectives to RL agents. However, it is difficult and time-consuming to carefully design suitable reward functions for a variety of complex behaviors (e.g., cooking or book summarization (Wu et al., 2021)). Furthermore, if there are complicated social norms we want RL agents to understand and follow, conveying a reliable reward function to include such information may remain to be an open problem (Amodei et al., 2016; Hadfield-Menell et al., 2017). Overall, engineering reward functions purely by human efforts for all tasks remains to be a significant challenge.

An alternative to resolve the challenge of reward engineering is preference-based RL (Christiano et al., 2017; Ibarz et al., 2018; Lee et al., 2021b). Compared to traditional RL setup, preference-based RL algorithms are able to teach RL agents without the necessity of designing reward functions. Instead, the agent uses feedback, usually in the form of (human) teacher preferences between two behaviors, to learn desired behaviors indicated by teacher. Therefore, instead of using carefully-designed rewards from the environment, the agent is able to learn a more flexible reward function suitably aligned to teacher feedback.

However, preference-based RL usually requires a large amount of teacher feedback, which may be timely or sometimes infeasible to collect. To improve feedback-efficiency, prior works have investigated several sampling strategies (Biyik & Sadigh, 2018; Sadigh et al., 2017; Biyik et al., 2020; Lee et al., 2021c). These methods aim to select more informative queries to improve the quality of the learned reward function while asking for fewer feedback from teacher. Another line of works focus on policy initialization. Ibarz et al. (2018) initialized the agent's policy with imitation learning from the expert demonstrations, and Lee et al. (2021b) utilized unsupervised pre-training of RL agents before collecting for teacher preferences in the hope of learning diverse behaviors in a self-supervised way to reduce total amount of human feedback.

^{*} Equal advising.



Figure 1: Illustration of RUNE. The agent interacts with the environment and learns an ensemble of reward functions based on teacher preferences. For each state-action pair, the total reward is a combination of the extrinsic reward, the mean of the ensemble's predicted values, and the intrinsic reward, the standard deviation between the ensemble's predicted values.

Exploration, in the context of standard RL, has addressed the problems of sample-efficiency (Stadie et al., 2015; Bellemare et al., 2016; Pathak et al., 2017; 2019; Liu & Abbeel, 2021; Seo et al., 2021b). When extrinsic rewards from the environment is limited, exploration has been demonstrated to allow RL agents to learn diverse behaviors. However, limited previous works have studied the effects of exploration in preference-based RL.

Inspired by recent success of exploration methods, we present RUNE: **R**eward **UN**certainty for Exploration, a simple and efficient exploration method specifically for preference-based RL algorithms. Our main idea is to incorporate uncertainty from learned reward function as an exploration bonus. Specifically, we capture the novelty of human feedback by measuring the reward uncertainty (e.g., variance in predictions of ensemble of reward functions). Since reward functions is optimized and learned to align to human feedback, exploration based on reward uncertainty may also reflect high uncertainty in information from teacher feedback. We hope that the proposed intrinsic reward contains information from teacher feedback and can guide exploration that better align to human preferences. Our experiment results show that RUNE can improve both sample- and feedback-efficiency of preference-based RL algorithms (Lee et al., 2021b).

We highlight the main contributions of our paper below:

- We propose a new exploration method based on uncertainty in learned reward functions for preference-based RL algorithms.
- For the first time, we show that *exploration* can improve the sample- and feedback-efficiency of preference-based RL algorithms.

2 RELATED WORK

Human-in-the-loop reinforcement learning. We mainly focus on one promising direction that utilizes the human preferences (Akrour et al., 2011; Christiano et al., 2017; Ibarz et al., 2018; Lee et al., 2021b; Leike et al., 2018; Pilarski et al., 2011; Wilson et al., 2012) to train RL agents. Christiano et al. (2017) scaled preference-based learning to utilize modern deep learning techniques, and Ibarz et al. (2018) improved the efficiency of this method by introducing additional forms of feedback such as demonstrations. Recently, Lee et al. (2021b) proposed a feedback-efficient RL algorithm by utilizing off-policy learning and pre-training.

To improve sample- and feedback-efficiency of human-in-the-loop RL, previous works (Christiano et al., 2017; Ibarz et al., 2018; Lee et al., 2021b; Leike et al., 2018) mainly focus on methods such as selecting more informative queries Christiano et al. (2017) and pre-training of RL agents Ibarz et al. (2018); Lee et al. (2021b). We further investigate effects of different exploration methods in preference-based RL algorithm. We follow a common approach of exploration methods in RL: generating intrinsic rewards as exploration bonus Pathak et al. (2019). Instead of only using learned reward function from human feedback as RL training objective, we alter the reward function to include a combination of the extrinsic reward (the learned rewards) and an intrinsic reward (explo-

ration bonus). In particular, we present an exploration method with intrinsic reward that measures the disagreement from learned reward models.

Exploration in reinforcement learning. The trade off between exploitation and exploration is a critical topic in RL. If agents don't explore enough, then they may learn sub optimal actions. Exploration algorithms aim to encourage the RL agent to visit a wide range of states in the environment. Thrun (1992) showed that exploration methods that utilize the agent's history has been shown to perform much better than random exploration. Hence, a common setup is to include an intrinsic reward as an exploration bonus. The intrinsic reward can be defined by Count-Based methods which keep count of previously visited states and rewards the agents for visiting new states Bellemare et al. (2016); Tang et al. (2017); Ostrovski et al. (2017).

Another option is to use a curiosity bonus for the intrinsic reward Houthooft et al. (2016); Pathak et al. (2017); Sekar et al. (2020). Curiosity represents how expected and unfamiliar the state is. One way to quantify curiosity is to predict the next state from current state and action Pathak et al. (2017), then use prediction error as an estimate of curiosity. If the error is high, that means the next state is unfamiliar and should be explored more. Similarly, instead of predicting the next state, prediction errors from training a neural network to approximate a random function Burda et al. (2018) can serve as a valid estimate of curiosity. If there are multiple models, then curiosity can also be described as the disagreement between the models Pathak et al. (2019). A high disagreement means that the models are unsure about the prediction and need to explore in that direction more.

A different approach maximizes the entropy of visited states by incorporating state entropy into the intrinsic reward. State entropy can be estimated by approximating the state density distribution Hazan et al. (2019); Lee et al. (2019), approximating the k-nearest neighbor entropy of a randomly initialized encoder Seo et al. (2021a), or using off-policy RL algorithms to maximize the k-nearest neighbor state entropy estimate in contrastive representation space for unsupervised pre-training Srinivas et al. (2020); Liu & Abbeel (2021). These methods encourage agents to explore diverse states.

Our approach adds an intrinsic reward that drives exploration to preference-based RL algorithms. We take advantage of an ensemble of reward models in preference-based RL algorithms, which is not available in other traditional RL settings. To estimate novelty of states and actions, we utilize the disagreement between reward models for our intrinsic reward, in hope of encouraging exploration aligned to directions of human preferences.

Trajectory generation in preference-based reinforcement learning. Previous works in preference-based reinforcement learning have investigated several methods to better explore diverse trajectories but close to current optimal policy Wirth et al. (2017).

One line of works computes agent's stochastic policies that are slightly deviated from optimal policies. Christiano et al. (2017) uses Trust Region Policy Optimization (TRPO) Schulman et al. (2015) and synchronized A3C Mnih et al. (2016). These RL algorithms define stochastic policies to ensure exploration of action space and deviations from optimal policies. However, these exploration methods based on stochastic RL algorithms does not include information from human preferences to drive exploration.

Another line of works designs one or multiple criterion to select from multiple possible stochastic policy candidates. Wilson et al. (2012) proposes to sample several policies from posterior distribution of policy space after updating human preferences. However, such methods come a the cost of requiring many samples collected beforehand. While these methods similarly aims to reduce uncertainty in human preferences, RUNE uses a different metric to estimate such uncertainty through reward functions ensemble. This is different from previous works and is simple, scalable, and easy to implement.

A different approach allows human to guide exploration by directly providing additional trajectories. Zucker et al. (2010) proposes a user-guided exploration method that shows samples of trajectories to human. Human can provide additional feedback to guide exploration. While this method receives exact information from human, it requires additional human labels, which are usually expensive and time-consuming to collect. RUNE however tries to extract information from human feedback revealed in learned reward functions, which doesn't require additional human input.

3 PRELIMINARIES

Preference-based reinforcement learning. We consider an agent interacting with an environment in discrete time Sutton & Barto (2018). At each timestep t, the agent receives a state s_t from the environment and chooses an action a_t based on its policy π .

In traditional reinforcement learning, the environment also returns a reward $r(\mathbf{s}_t, \mathbf{a}_t)$ that evaluates the quality of agent's behavior at timestep t. The goal of agent is to maximize the discounted sum of rewards. However, in the preference-based RL framework, we don't have such a reward function returned from the environment. Instead, a (human) teacher provides preferences between the agent's behaviors and the agent learns its policy from feedbacks (Christiano et al., 2017; Ibarz et al., 2018; Lee et al., 2021b; Leike et al., 2018).

Formally, a segment σ is a sequence of time-indexed observations and actions $\{(\mathbf{s}_1, \mathbf{a}_1), ..., (\mathbf{s}_H, \mathbf{a}_H)\}$. Given a pair of segments (σ^0, σ^1) that describe two behaviors, a teacher indicates which segment is preferred, i.e., $y = (\sigma^0 \succ \sigma^1)$ or $(\sigma^1 \succ \sigma^0)$, that the two segments are equally preferred $y = (\sigma^1 = \sigma^0)$, or that two segments are incomparable, i.e., discarding the query. The goal of preference-based RL is to train an agent to perform behaviors desirable to a human teacher using as few feedback as possible.

In preference-based RL algorithms, a policy π_{ϕ} and reward function \hat{r}_{ψ} are updated as follows:

- Step 1 (agent learning): The policy π_{ϕ} interacts with environment to collect experiences and we update it using existing RL algorithms to maximize the sum of the learned rewards \hat{r}_{ψ} .
- Step 2 (reward learning): The reward function \hat{r}_{ψ} is optimized based on the feedback received from a teacher.
- Repeat *Step 1* and *Step 2*.

To incorporate human preferences into *reward learning*, we optimize reward function \hat{r}_{ψ} as follows. Following the Bradley-Terry model (Bradley & Terry, 1952), we first model preference predictor of a pair of segments based on reward function \hat{r}_{ψ} as follows:

$$P_{\psi}[\sigma^{1} \succ \sigma^{0}] = \frac{\exp\sum_{t} \widehat{r}_{\psi}(\mathbf{s}_{t}^{1}, \mathbf{a}_{t}^{1})}{\sum_{i \in \{0,1\}} \exp\sum_{t} \widehat{r}_{\psi}(\mathbf{s}_{t}^{i}, \mathbf{a}_{t}^{i})},\tag{1}$$

where $\sigma^i \succ \sigma^j$ denotes the event that segment *i* is preferable to segment *j*. Here, the intuition is that segments with more desirable behaviors should have higher predicted reward values from \hat{r}_{ψ} . To align preference predictors of \hat{r}_{ψ} with labels received from human preferences, preference-based RL algorithms translate updating reward function to a binary classification problem. Specifically, the reward function \hat{r}_{ψ} parametrized by ψ is updated to minimize the following cross-entropy loss:

$$\mathcal{L}^{\text{Reward}} = - \mathop{\mathbb{E}}_{(\sigma^0, \sigma^1, y) \sim \mathcal{D}} \left[\mathbb{I}\{y = (\sigma^0 \succ \sigma^1)\} \log P_{\psi}[\sigma^0 \succ \sigma^1] + \mathbb{I}\{y = (\sigma^1 \succ \sigma^0)\} \log P_{\psi}[\sigma^1 \succ \sigma^0] \right]$$
(2)

where we are given a set D of segment pairs and corresponding human preferences.

Once reward function \hat{r}_{ψ} has been optimized from human preferences, preference-based RL algorithms train RL agents with any existing RL algorithms, treating predicted rewards from \hat{r}_{ψ} as reward function returned from the environment.

4 RUNE

In this section, we present RUNE: **R**eward **UN**certainty for Exploration (Figure 1), which encourages human-guided exploration for preference-based RL. The key idea of RUNE is to incentivize exploration by providing an intrinsic reward based on reward uncertainty. Our main hypothesis is that the reward uncertainty captures the novelty of human feedback, which can lead to useful behaviors for preference-based RL.



(a) Door Close (b) Door Open (c) Drawer Open (d) Sweep Into (e) Door Unlock (f) Window Close

Figure 2: Examples of rendered images of robotic manipulation tasks from Meta-world. We consider learning several manipulation skills using preferences from a scripted teacher.

4.1 REWARD UNCERTAINTY FOR EXPLORATION

In preference-based RL, capturing the novelty of human feedback can be crucial for efficient reward learning. To this end, we propose to utilize an intrinsic reward based on ensemble of reward functions. Specifically, for each timestep, the intrinsic reward is defined as follows:

$$r^{\text{int}}(\mathbf{s}_t, \mathbf{a}_t) := \widehat{r}_{\text{std}}(\mathbf{s}_t, \mathbf{a}_t), \tag{3}$$

where \hat{r}_{std} is the empirical standard deviation of all reward functions $\{\hat{r}_{\psi_i}\}_{i=1}^N$. We initialize the model parameters of all reward functions with random parameter values for inducing an initial diversity. Here, our intuition is high variance of reward functions indicates high uncertainty from human preferences, which means we collected less teacher preferences on those states and actions. Therefore, in order to generate more informative queries and improve confidence in learned reward functions, we encourage our agent to visit more uncertain state-action pairs with respect to the learned reward functions.

We remark that exploration based on ensembles has been studied in the literature (Osband et al., 2016; Chen et al., 2017; Pathak et al., 2019; Lee et al., 2021a). For example, Chen et al. (2017) proposed an exploration strategy that considers both best estimates (i.e., mean) and uncertainty (i.e., variance) of Q-functions and Pathak et al. (2019) utilized the disagreement between forward dynamics models. However, our method is different in that we propose an alternative intrinsic reward based on reward ensembles, which can capture the uncertainty from human preferences.

4.2 TRAINING OBJECTIVE BASED ON INTRINSIC REWARDS

Once we learn reward functions $\{\hat{r}_{\psi_i}\}_{i=1}^N$ from human preferences, agent is usually trained with RL algorithm guided by extrinsic reward:

$$r^{\text{ext}}(\mathbf{s}_t, \mathbf{a}_t) = \widehat{r}_{\text{mean}}(\mathbf{s}_t, \mathbf{a}_t), \tag{4}$$

where \hat{r}_{mean} is the empirical mean of all reward functions $\{\hat{r}_{\psi_i}\}_{i=1}^N$. To encourage exploration, we train a policy to maximize the sum of both extrinsic reward and intrinsic reward in equation 3:

$$r_t^{\text{total}} := r^{\text{ext}}(\mathbf{s}_t, \mathbf{a}_t) + \beta_t \cdot r^{\text{int}}(\mathbf{s}_t, \mathbf{a}_t), \tag{5}$$

where $\beta_t \ge 0$ is a hyperparameter that determines the trade off between exploration and exploitation at training time step t. Similar to Seo et al. (2021b), we use an exponential decay schedule for β_t throughout training to encourage the agent to focus more on extrinsic reward from learned reward function predictions as training proceeds, i.e., $\beta_t = \beta_0 (1 - \rho)^t$, where ρ is a decay rate.

While the proposed intrinsic reward would converge to 0 as more feedback queries are collected during training, we believe our learned reward functions improve over training as we collect more feedback queries from teacher preferences. The full procedure of RUNE is summarized in Algorithm 1.

5 EXPERIMENTS

We designed our experiments to answer the following questions:

• Can exploration methods improve the sample- and feedback-efficiency of preference-based RL algorithms?



Figure 3: Learning curves on robotic manipulation tasks as measured on the success rate. Exploration methods consistently improves the sample-efficiency of PEBBLE. In particular, RUNE provides larger gains than other existing exploration baselines. The solid line and shaded regions represent the mean and standard deviation, respectively, across five runs.

- How does RUNE compare to other exploration schemes in preference-based RL setting?
- How does RUNE influence reward learning in preference-based RL?

5.1 Setup

In order to verify the efficacy of exploration in preference-based RL, we focus on having an agent solve a range of complex robotic manipulation skills from Meta-World (Yu et al., 2020) (see Figure 2). Similar to prior works (Christiano et al., 2017; Lee et al., 2021b;c), the agent learns to perform a task only by getting feedback from an oracle scripted teacher that provides clean preferences between trajectory segments according to the sum of ground truth reward values for each trajectory segment. Because the simulated human teacher's preferences are generated by a ground truth reward values, we measure the true average return of trained agents as evaluation metric.

We consider a combination of RUNE and PEBBLE (Lee et al., 2021b), an off-policy preference-based RL algorithm that utilizes unsupervised pre-training and soft actor-critic (SAC) method (Haarnoja et al., 2018) (see Appendix A for more details about algorithm procedure and Appendix B for more experimental details). To address the issue that there can be multiple reward functions that align to the same set of teacher preferences, we bound all predicted reward values to a normalized range of (-1, 1) by adding tanh activation function after the output layer in network architectures.

For all experiments including PEBBLE and RUNE, we train an ensemble of 3 reward functions according to Equation 2. Specifically, we use different random initialization for each network in the ensemble. We use the same set of training data, i.e. sampled set of feedback queries, but different random batches to train each network in the ensemble. Parameters of each network are independently optimized to minimize the cross entropy loss of their respective batch of training data according to Equation 2. In addition, we use original hyperparameters of preference-based RL algorithm, which are specified in Appendix B and report mean and standard deviations across 5 runs respectively.

5.2 IMPROVING SAMPLE-EFFICIENCY

To evaluate sample-efficiency of our method, we compare to the following exploration methods:

- State entropy maximization (StateEnt; Mutti et al. 2021; Liu & Abbeel 2021): Maximizing the entropy of state visitation distribution H(s). We utilize a particle estimator (Singh et al., 2003), which approximates the entropy by measuring the distance between k-nearest neighbors (k-NN) for each state.
- Disagreement Pathak et al. (2019): Maximizing disagreement proportional to variance in predictions from ensembles $Var\{g_i(\mathbf{s}_{t+1}|\mathbf{s}_t,\mathbf{a}_t)\}_{i=1}^N$. We train an en-

semble of forward dynamics models to predict ground truth next state from current state and action $g_i(\mathbf{s}_{t+1}|\mathbf{s}_t, \mathbf{a}_t)$ by minimizing sum of prediction errors, i.e. $\sum_{i=1}^{N} ||g_i(\mathbf{s}_{t+1}|\mathbf{s}_t, \mathbf{a}_t) - s_{t+1}||_2$.

• ICM Pathak et al. (2017): Maximizing intrinsic reward proportional to prediction error $||g(\mathbf{s}_{t+1}|\mathbf{s}_t, \mathbf{a}_t) - \mathbf{s}_{t+1}||_2$. We train a single dynamics model to predict ground truth next state from current state and action $g(\mathbf{s}_{t+1}|\mathbf{s}_t, \mathbf{a}_t)$ via regression.

For all methods we consider, we carefully tune a range of hyperparameters and report the best results. In particular, we consider $\beta_0 = 0.05$ and $\rho \in \{0.001, 0.0001, 0.00001\}$ for all exploration methods, and $k \in \{5, 10\}$ for state entropy based exploration. We provide more details about training and implementation in Appendix B.

Figure 3 shows the learning curves of PEBBLE with various exploration methods. First, we remark that previous exploration methods (i.e., StateEnt, Disagree and ICM), which encourage agents to visit novel states, consistently improve sample-efficiency of PEBBLE on various tasks. This shows the potential and efficacy of exploration methods to further improve sample-efficiency of preference-based RL algorithms.

In particular, in Figure 3, compared to existing previous exploration methods, RUNE consistently exhibits superior sample efficiency in all tasks we consider. This suggests that exploration based on reward uncertainty is suitable for preference-based RL algorithms, as such it encourages visitations to states and actions that are uncertain with respect to human feedback and thus can capture the novelty in a distinctive perspective. We provide additional experiment results about better sample-efficiency in Figure 9(a) of Appendix C.

We also emphasize the simplicity and efficiency of RUNE compared to other existing schemes (such as ICM and Disagree) because our method does not introduce additional model architectures (e.g., ensemble of forward dynamics models) to compute exploration bonus as intrinsic rewards.

5.3 IMPROVING FEEDBACK-EFFICIENCY

In this section, we also verify whether our proposed exploration method can improve the feedbackefficiency of both off-policy and on-policy preference-based RL algorithms. We consider PEB-BLE Lee et al. (2021b), an off-policy preference-based RL algorithm that utilizes unsupervised pretraining and soft actor-critic (SAC) method (Haarnoja et al., 2018), and PrefPPO Lee et al. (2021c), an on-policy preference-based RL algorithm that utilizes unsupervised pretraining and proximal policy gradient (PPO) method (Schulman et al., 2017), respectively.

As shown in Table 1, we compare performance of PEBBLE and PrefPPO with and without RUNE respectively using different budgets of feedback queries during training. With fewer total queries, we stop asking for human preferences earlier in the middle of training. We use asymptotic success rate converged at the end of training steps as evaluation metric. Table 1 suggests that RUNE achieves consistently better asymptotic performance using fewer number of human feedback; additionally RUNE shows more robust performance with respect to different budgets of available human feedbacks. This shows potential of exploration in scaling preference-based RL to real world scenarios where human feedback are usually expensive and time-consuming to obtain.

We report corresponding learning curves to show better sample efficiency of RUNE compared to PEBBLE or PrefPPO under wide variety of tasks environments in Figure 6, 7, 8, 5 of Appendix C.

5.4 ABLATION STUDY

Ensemble size. As intrinsic rewards of RUNE only depend on learned reward functions, we investigate the effects of different number of reward function ensembles. In particular, we consider $\{3, 5, 7\}$ number of reward function ensembles. In Figure 4(a), sample-efficiency of RUNE remains robust and stable with different number in the ensemble of reward functions. Additionally, RUNE can achieve better sample-efficiency in preference-based RL while requiring fewer number of reward functions ensembles. This shows potentials of RUNE specifically suitable for preference-based RL in improving compute efficiency, as it reduces the necessity of training additional reward functions architectures and still achieves comparable performance.

TASK	FEEDBACK QUERIES	METHOD	CONVERGENT SUCCESS RATE
DRAWER OPEN	10000	PEBBLE	0.98 ± 0.08
		PEBBLE + RUNE	1 ± 0
	5000	PEBBLE	0.94 ± 0.08
		PEBBLE + RUNE	0.99 ± 0.02
Sweep Into	10000	PEBBLE	0.8 ± 0.4
		PEBBLE + RUNE	1 ± 0
	5000	PEBBLE	0.8 ± 0.08
		PEBBLE + RUNE	0.9 ± 0.14
Door Unlock	5000	PEBBLE	0.66 ± 0.42
		PEBBLE + RUNE	0.8 ± 0.4
	2500	PEBBLE	0.64 ± 0.45
		PEBBLE + RUNE	$ $ 0.8 \pm 0.4
	4000	PEBBLE	1 ± 0
DOOR OPEN		PEBBLE + RUNE	1 ± 0
DOOK OPEN	2000	PEBBLE	0.9 ± 0.2
		PEBBLE + RUNE	$ $ 1 \pm 0
Door Close	1000	PEBBLE	1 ± 0
		PEBBLE + RUNE	1 ± 0
	500	PEBBLE	0.8 ± 0.4
		PEBBLE + RUNE	$ $ 1 \pm 0
WINDOW CLOSE	1000	PEBBLE	0.94 ± 0.08
		PEBBLE + RUNE	1 ± 0
	500	PEBBLE	0.86 ± 0.28
		PEBBLE + RUNE	0.99 ± 0.02
BUTTON PRESS	20000	PREFPPO	0.46 ± 0.20
		PREFPPO + RUNE	0.64 ± 0.18
	10000	PrefPPO	0.35 ± 0.31
		PREFPPO + RUNE	0.51 ± 0.27

Table 1: Success rate of off- and on-policy preference-based RL algorithms (e.g. PEBBLE and PrefPPO) in addition to RUNE with different budgets of feedback queries. The results show the mean averaged and standard deviation computed over five runs and the best results are indicated in bold. All learning curves (including means and standard deviations) are in Appendix C.

Number of queries per feedback session. Human preferences are usually expensive and timeconsuming to collect. As shown in Table 1, RUNE is able to achieve better asymptotic performance under different budgets of total human preferences. We further investigate the effects of different queries in each feedback session on performance of PEBBLE and RUNE. In particular, we consider $\{10, 50\}$ number of queries per feedback session equally spread out throughout training. In Figure 4(b), we indicate asymptotic performance of PEBBLE baseline by dotted horizontal lines. It shows that as 80% of feedbacks are eliminated, asymptotic success rate of PEBBLE baseline largely drops, while in contrast RUNE remains superior performance in both sample-efficiency and asymptotic success. Thus RUNE is robust to different number of available feedback queries constraints and thus a suitable exploration method specifically beneficial for preference-based RL.

Quality of learned reward functions. We use Equivalent-Policy Invariant Comparison (EPIC) distance Gleave et al. (2020) between learned reward functions and ground truth reward values as evaluation metrics. Gleave et al. (2020) suggests that EPIC distance is robust to coverage distributions of states and actions and is thus a reliable metric to quantify distance between different reward functions under the same transition dynamics. We generate (s, a) from each task uniformly and independently at random in order to obtain a wide coverage of state distributions.

As in Figure 4(c), compared to PEBBLE, reward functions learned from RUNE are closer to ground truth reward evaluated based on EPIC distance and converges faster during training. We provide additional analysis on different task environments in Figure 9(b) and 9(c) of Appendix C.



Figure 4: Ablation study on (a) Door Open, (b) Window Close, and (c) Door Close. We measure (a) Effects of different number of learned reward model ensembles on RUNE; (b) Effects of different number of queries received per feedback session on PEBBLE and RUNE; and (c) EPIC distance between the ensemble of learned reward functions and true reward in the task environment. The solid line and shaded regions represent the mean and standard deviation, respectively, across five runs. The dotted line in Figure 4(b) indicates asymptotic success rate of PEBBLE baseline with same hyperparameters.

We further analyze quality of reward functions learned by RUNE compared to true reward in Figure 10 of Appendix C. Learned rewards optimized by RUNE is well-aligned to true reward, as it can capture diverse patterns of true reward values from the environment.

6 DISCUSSION

In this paper, we present RUNE, a simple and efficient exploration method for preference-based RL algorithms. To improve sample- and feedback-efficiency of preference-based RL, different from previous works, we investigate the benefits of exploration methods in preference-based RL. We show the significant potential of incorporating intrinsic rewards to drive exploration because it improves sample-efficiency of preference-based RL.

For our proposed exploration scheme RUNE, we show that it is useful for preference-based RL because it showcases consistently superior performance in both sample- and feedback-efficiency compared to other existing exploration methods. Here we emphasize that RUNE takes advantage of information in reward functions learned from human feedback, to measure the novelty of states and actions for exploration. This is different from existing estimates of uncertainty for exploration, as our method in particular encourages exploration aligned to teacher preferences.

In conclusion, we hope that our work could demonstrate the potential of exploration to improve sample- and feedback-efficiency of preference-based RL, and to encourage future works to develop novel exploration methods guided by human feedback.

ACKNOWLEDGEMENTS

This research is supported in part by Open Philanthropy. We thank anonymous reviewers for critically reading the manuscript and suggesting substantial improvements.

REFERENCES

Riad Akrour, Marc Schoenauer, and Michele Sebag. Preference-based policy learning. In *Joint European Conference on Machine Learning and Knowledge Discovery in Databases*, 2011.

Dario Amodei, Chris Olah Olah, Jacob Steinhardt, Paul Christiano, John Schulman, and Dan Mané. Concrete problems in ai safety. In *arXiv preprint arXiv:1606.06565*, 2016.

- Marc Bellemare, Sriram Srinivasan, Georg Ostrovski, Tom Schaul, David Saxton, and Remi Munos. Unifying count-based exploration and intrinsic motivation. In *Advances in Neural Information Processing Systems*, 2016.
- Erdem Biyik and Dorsa Sadigh. Batch active preference-based learning of reward functions. In *Conference on Robot Learning*, 2018.
- Erdem Biyik, Nicolas Huynh, Mykel J Kochenderfer, and Dorsa Sadigh. Active preference-based gaussian process regression for reward learning. In *Robotics: Science and Systems*, 2020.
- Ralph Allan Bradley and Milton E Terry. Rank analysis of incomplete block designs: I. the method of paired comparisons. *Biometrika*, 39(3/4):324–345, 1952.
- Yuri Burda, Harrison Edwards, Amos Storkey, and Oleg Klimov. Exploration by random network distillation. In *International Conference on Learning Representations*, 2018.
- Richard Y Chen, Szymon Sidor, Pieter Abbeel, and John Schulman. Ucb exploration via qensembles. arXiv preprint arXiv:1706.01502, 2017.
- Paul F Christiano, Jan Leike, Tom Brown, Miljan Martic, Shane Legg, and Dario Amodei. Deep reinforcement learning from human preferences. In Advances in Neural Information Processing Systems, 2017.
- Adam Gleave, Michael Dennis, Shane Legg, Stuart Russell, and Jan Leike. Quantifying differences in reward functions. *arXiv preprint arXiv:2006.13900*, 2020.
- Tuomas Haarnoja, Aurick Zhou, Pieter Abbeel, and Sergey Levine. Soft actor-critic: Off-policy maximum entropy deep reinforcement learning with a stochastic actor. In *International Conference on Machine Learning*, 2018.
- Dylan Hadfield-Menell, Smitha Milli, Pieter Abbeel, Stuart Russell, and Anca Dragan. Inverse reward design. In Advances in Neural Information Processing Systems, 2017.
- Elad Hazan, Sham Kakade, Karan Singh, and Abby Van Soest. Provably efficient maximum entropy exploration. In *International Conference on Machine Learning*, 2019.
- Rein Houthooft, Xi Chen, Yan Duan, John Schulman, Filip De Turck, and Pieter Abbeel. Vime: Variational information maximizing exploration. In *Advances in Neural Information Processing Systems*, 2016.
- Borja Ibarz, Jan Leike, Tobias Pohlen, Geoffrey Irving, Shane Legg, and Dario Amodei. Reward learning from human preferences and demonstrations in atari. In *Advances in Neural Information Processing Systems*, 2018.
- Diederik P Kingma and Jimmy Ba. Adam: A method for stochastic optimization. In *International Conference on Learning Representations*, 2015.
- Kimin Lee, Michael Laskin, Aravind Srinivas, and Pieter Abbeel. Sunrise: A simple unified framework for ensemble learning in deep reinforcement learning. In *International Conference on Machine Learning*, 2021a.
- Kimin Lee, Laura Smith, and Pieter Abbeel. Pebble: Feedback-efficient interactive reinforcement learning via relabeling experience and unsupervised pre-training. In *International Conference on Machine Learning*, 2021b.
- Kimin Lee, Laura Smith, Anca Dragan, and Pieter Abbeel. B-pref: Benchmarking preferencebased reinforcement learning. In *Thirty-fifth Conference on Neural Information Processing Systems Datasets and Benchmarks Track (Round 1)*, 2021c. URL https://openreview.net/ forum?id=ps95-mkHF_.
- Lisa Lee, Benjamin Eysenbach, Emilio Parisotto, Eric Xing, Sergey Levine, and Ruslan Salakhutdinov. Efficient exploration via state marginal matching. *arXiv preprint arXiv:1906.05274*, 2019.

- Jan Leike, David Krueger, Tom Everitt, Miljan Martic, Vishal Maini, and Shane Legg. Scalable agent alignment via reward modeling: a research direction. *arXiv preprint arXiv:1811.07871*, 2018.
- Hao Liu and Pieter Abbeel. Behavior from the void: Unsupervised active pre-training. *arXiv preprint arXiv:2103.04551*, 2021.
- Volodymyr Mnih, Adria Puigdomenech Badia, Mehdi Mirza, Alex Graves, Timothy Lillicrap, Tim Harley, David Silver, and Koray Kavukcuoglu. Asynchronous methods for deep reinforcement learning. In *International Conference on Machine Learning*, 2016.
- Mirco Mutti, Lorenzo Pratissoli, and Marcello Restelli. A policy gradient method for task-agnostic exploration. In *Proceedings of the AAAI Conference on Artificial Intelligence*, 2021.
- Ian Osband, Charles Blundell, Alexander Pritzel, and Benjamin Van Roy. Deep exploration via bootstrapped dqn. In Advances in neural information processing systems, 2016.
- Georg Ostrovski, Marc G Bellemare, Aaron van den Oord, and Rémi Munos. Count-based exploration with neural density models. In *International Conference on Machine Learning*, 2017.
- Deepak Pathak, Pulkit Agrawal, Alexei A Efros, and Trevor Darrell. Curiosity-driven exploration by self-supervised prediction. In *International Conference on Machine Learning*, 2017.
- Deepak Pathak, Dhiraj Gandhi, and Abhinav Gupta Gupta. Self-supervised exploration via disagreement. In *International Conference on Machine Learning*, 2019.
- Patrick M Pilarski, Michael R Dawson, Thomas Degris, Farbod Fahimi, Jason P Carey, and Richard S Sutton. Online human training of a myoelectric prosthesis controller via actor-critic reinforcement learning. In *International Conference on Rehabilitation Robotics*, 2011.
- Dorsa Sadigh, Anca D Dragan, Shankar Sastry, and Sanjit A Seshia. Active preference-based learning of reward functions. In *Robotics: Science and Systems*, 2017.
- John Schulman, Sergey Levine, Pieter Abbeel, Michael Jordan, and Philipp Moritz. Trust region policy optimization. In *International conference on machine learning*, pp. 1889–1897. PMLR, 2015.
- John Schulman, Filip Wolski, Prafulla Dhariwal, Alec Radford, and Oleg Klimov. Proximal policy optimization algorithms. arXiv preprint arXiv:1707.06347, 2017.
- Ramanan Sekar, Oleh Rybkin, Kostas Daniilidis, Pieter Abbeel, Danijar Hafner, and Deepak Pathak. Planning to explore via self-supervised world models. In *International Conference on Machine Learning*, 2020.
- Younggyo Seo, Lili Chen, Jinwoo Shin, Honglak Lee, Pieter Abbeel, and Kimin Lee. State entropy maximization with random encoders for efficient exploration. In *International Conference on Machine Learning (ICML)*, 2021a.
- Younggyo Seo, Lili Chen, Jinwoo Shin, Honglak Lee, Pieter Abbeel, and Kimin Lee. State entropy maximization with random encoders for efficient exploration. *arXiv preprint arXiv:2102.09430*, 2021b.
- Harshinder Singh, Neeraj Misra, Vladimir Hnizdo, Adam Fedorowicz, and Eugene Demchuk. Nearest neighbor estimates of entropy. *American journal of mathematical and management sciences*, 23(3-4):301–321, 2003.
- Aravind Srinivas, Michael Laskin, and Pieter Abbeel. Curl: Contrastive unsupervised representations for reinforcement learning. In *International Conference on Machine Learning*, 2020.
- Bradly C Stadie, Sergey Levine, and Pieter Abbeel. Incentivizing exploration in reinforcement learning with deep predictive models. *arXiv preprint arXiv:1507.00814*, 2015.

Richard S Sutton and Andrew G Barto. Reinforcement learning: An introduction. MIT Press, 2018.

- Haoran Tang, Rein Houthooft, Davis Foote, Adam Stooke, OpenAI Xi Chen, Yan Duan, John Schulman, Filip DeTurck, and Pieter Abbeel. # exploration: A study of count-based exploration for deep reinforcement learning. In *Advances in Neural Information Processing Systems*, 2017.
- Sebastian Thrun. The role of exploration in learning control. In *Handbook of Intelligent Control: Neural, Fuzzy and Adaptive Models*, 1992.
- Aaron Wilson, Alan Fern, and Prasad Tadepalli. A bayesian approach for policy learning from trajectory preference queries. In *Advances in Neural Information Processing Systems*, 2012.
- Christian Wirth, Riad Akrour, Gerhard Neumann, and Johannes Fürnkranz. A survey of preferencebased reinforcement learning methods. *Journal of Machine Learning Research*, 18(136):1–46, 2017. URL http://jmlr.org/papers/v18/16-634.html.
- Jeff Wu, Long Ouyang, Daniel M Ziegler, Nissan Stiennon, Ryan Lowe, Jan Leike, and Paul Christiano. Recursively summarizing books with human feedback. *arXiv preprint arXiv:2109.10862*, 2021.
- Tianhe Yu, Deirdre Quillen, Zhanpeng He, Ryan Julian, Karol Hausman, Chelsea Finn, and Sergey Levine. Meta-world: A benchmark and evaluation for multi-task and meta reinforcement learning. In *Conference on Robot Learning*, 2020.
- Matt Zucker, J Andrew Bagnell, Christopher G Atkeson, and James Kuffner. An optimization approach to rough terrain locomotion. In 2010 IEEE International Conference on Robotics and Automation, pp. 3589–3595. IEEE, 2010.

Appendix

A ALGORITHM DETAILS

RUNE. We provide the full procedure for RUNE with PEBBLE Lee et al. (2021b), an off-policy preference-based RL algorithm, in Algorithm 1.

Algorithm 1 RUNE: Reward Uncertainty for Exploration

1: Initialize policy π_{ϕ} and reward model \hat{r}_{ψ} 2: Initialize replay buffer B3: // UNSUPERVISED PRE-TRAINING 4: Maximize the state entropy $\mathcal{H}(\mathbf{s}) = -\mathbb{E}_{\mathbf{s} \sim p(\mathbf{s})} \left[\log p(\mathbf{s})\right]$ 5: // POLICY LEARNING 6: for each training step t do 7: // REWARD LEARNING 8: if iteration % K == 0 then Generate queries from replay buffer $\{(\sigma^0, \sigma^1)\}_{i=1}^{N_{query}} \sim \mathcal{B}$ and corresponding human 9: feedback $(y_i)_{i=1}^{N_{query}}$ Update reward model \widehat{r}_{ψ} according to equation 2 10: 11: // RELABEL BOTH EXTRINSIC AND INTRINSIC REWARD 12: Relabel entire replay buffer \mathcal{B} using \widehat{r}_{ψ} Relabel extrinsic reward $r_{\psi}^{\text{ext}}(\mathbf{s}_j, \mathbf{a}_j) = \hat{r}_{\text{mean}}(\mathbf{s}_j, \mathbf{a}_j)$ Relabel intrinsic reward $r_{\psi}^{\text{int}}(\mathbf{s}_j, \mathbf{a}_j) = \hat{r}_{\text{std}}(\mathbf{s}_j, \mathbf{a}_j)$ 13: 14: 15: end if // UPDATE POLICY 16: 17: for each gradient step do Sample minibatch from replay buffer $\{(\mathbf{s}_j, \mathbf{a}_j, \mathbf{s}_{j+1}, r_{\psi}^{\mathsf{ext}}(\mathbf{s}_j, \mathbf{a}_j), r_{\psi}^{\mathsf{int}}(\mathbf{s}_j, \mathbf{a}_j)\}_{j=1}^B \sim \mathcal{B}$ 18: $\begin{array}{l} \text{Update } \beta_t \leftarrow \beta_0 (1-\rho)^t \\ \text{Let } r_j^{\texttt{total}} \leftarrow r_j^{\texttt{ext}} + \beta_t \cdot r_j^{\texttt{int}} \end{array}$ 19: 20: Update ϕ with transitions $\{(\mathbf{s}_j, \mathbf{a}_j, \mathbf{s}_{j+1}, r_{\psi}^{\texttt{total}}(\mathbf{s}_j, \mathbf{a}_j)\}_{i=1}^B$ 21: 22: end for 23: // INTERACTION WITH ENVIRONMENT 24: for each timestep t do 25: Collect \mathbf{s}_{t+1} by taking $\mathbf{a}_t \sim \pi_{\phi}(\mathbf{a}_t | \mathbf{s}_t)$ Store transitions $\mathcal{B} \leftarrow \mathcal{B} \cup \{(\mathbf{s}_t, \mathbf{a}_t, \mathbf{s}_{t+1}, \widehat{r}_{\psi}(\mathbf{s}_t, \mathbf{a}_t))\}$ 26: end for 27: 28: end for

Hyperparameter	Value	
Segment Length	50	
Number of Unsupervised Pre-training Steps	9000	
Interaction time	10000	
Reward batch	50 (Door Close, Door Open), 100 (Drawer Open)	
Total feedback	1000 (Door Close), 5000 (Door Open), 10000 (Drawer Open)	
Sampling scheme	Disagreement Sampling	
Reward model number of layers	3	
Reward model number of hidden units	256	
Reward model activation functions	LeakyRelu	
Reward model output activation function	TanH	
Number of reward functions	3	
Optimizer	Adam (Kingma & Ba, 2015)	
Initial learning rate	0.0003	

Table 2: Hyperparameters of the PEBBLE algorithm.

Hyperparameter	Value	Hyperparameter	Value
Initial temperature	0.1	Hidden units per each layer	256
Learning rate	0.0003	Batch Size	512
Critic target update freq	2	Critic EMA $ au$	0.005
(β_1,β_2)	(.9, .999)	Discount γ	.99
Optimizer	Adam (Kingma & Ba, 2015)		

Table 3: Hyperparameters of the SAC algorithm. Most hyperparameters values are unchanged across environments with the exception for learning rate.

B EXPERIMENTAL DETAILS

B.1 TRAINING DETAILS

For our method, we use the publicly released implementation repository of the PEBBLE algorithm (https://github.com/pokaxpoka/B_Pref) with the full list of hyperparameters specified in Table 2 and the SAC algorithm (https://github.com/denisyarats/pytorch_sac) with the full list of hyperparameters specified in Table 3.

B.2 IMPLEMENTATION DETAILS OF EXPLORATION METHODS

For all exploration methods, we follow implementation of the publicly release repository of RE3 (https://github.com/younggyoseo/RE3) to update policy with $r^{\text{total}} = r^{\text{ext}} + \beta_t \cdot r^{\text{int}}$.

RUNE. We emphasize one simplicity in the implementation of RUNE. Following relabeling technique in Lee et al. (2021b), after each update in reward learning step, we relabel the entire replay buffer *B* to store both predicted reward functions learned from human feedback (extrinsic rewards r^{ext}), and uncertainty in updated reward functions (intrinsic rewards r^{int} in RUNE). This is because our learned reward functions parameters remain unchanged during RL training or agent interaction with the environment between subsequent feedback sessions. Thus, in RL training, $r^{\text{total}} = r^{\text{ext}} + \beta_t \cdot r^{\text{int}}$ can be directly taken from replay buffer. As for hyperparameter related to exploration, we consider $\beta_0 = 0.05$, $\rho \in \{0.001, 0.0001, 0.00001\}$.

State Entropy Maximization. See et al. (2021b) We use intrinsic reward $r^{\text{int}}(\mathbf{s}_t) = ||\mathbf{s}_t - \mathbf{s}_t^{k-\text{NN}}||_2$ followed See et al. (2021b) and Liu & Abbeel (2021). We use raw state space to compute entropy values as intrinsic rewards. We use code for unsupervised pre-training from the publicly release implementation repository of PEBBLE algorithm (https://github.com/pokaxpoka/B_ Pref) to compute k-NN and estimate state entropy. As the size of replay buffer grows significantly as training time increases, we sample a random mini-batch B' from replay buffer B and compute k-NN with respect to random mini-batch. We use minibatch size 512, which is reported as a default hyperparameter in See et al. (2021b). As for hyperparameters related to exploration, we consider $\beta_0 = 0.05$, $\rho \in \{0.001, 0.0001, 0.00001\}$, and $k \in \{5, 10\}$.

Disagreement. Pathak et al. (2019) We train an ensemble of 5 forward dynamics model g_i , following original results in Pathak et al. (2019). These dynamics models are trained to predict next state \mathbf{s}_{t+1} based on current state and action $(\mathbf{s}_t, \mathbf{a}_t)$, i.e. minimize $\sum_{i=1}^{5} ||g_i(\mathbf{s}_{t+1}|\mathbf{s}_t, \mathbf{a}_t) - \mathbf{s}_{t+1}||_2$. We use intrinsic reward proportional to variance in ensemble of predictions $r^{\text{int}}(\mathbf{s}_t, \mathbf{a}_t) = Var\{g_i(\mathbf{s}_{t+1}|\mathbf{s}_t, \mathbf{a}_t)\}_{i=1}^N$. For consistency we use same neural network architecture and optimization hyperparameters as reward functions specified in Table 2. We follow implementation of Disagreement agent in publicly released repository URLB (https://anonymous.4open.science/r/urlb). As for hyperparameter related to exploration, we consider $\beta_0 = 0.05$, $\rho \in \{0.001, 0.0001, 0.00001\}$.

ICM. Pathak et al. (2017) We train a single forward dynamics model g to predict next state \mathbf{s}_{t+1} based on current state and action $(\mathbf{s}_t, \mathbf{a}_t)$, i.e. minimize $||g(\mathbf{s}_{t+1}|\mathbf{s}_t, \mathbf{a}_t) - \mathbf{s}_{t+1}||_2$. We use intrinsic reward proportional to prediction error of trained dynamics model, i.e. $r^{\text{int}}(\mathbf{s}_t, \mathbf{a}_t) = ||g(\mathbf{s}_{t+1}|\mathbf{s}_t, \mathbf{a}_t) - \mathbf{s}_{t+1}||_2$. For consistency we use same neural network architecture and optimization hyperparameters as reward functions specified in Table 2. We follow implementation of ICM agent



(a) Door Close (feedback (b) Door Close (feedback (c) Button Press (feed- (d) Button Press (feed- = 500) = 250) back=20K) back=10K)

Figure 5: RUNE performs better than PEBBLE and PrefPPO in variety of manipulation tasks using different budgets of feedback queries. The solid/dashed line and shaded regions represent the mean and standard deviation, respectively, across five runs.



Figure 6: RUNE performs better than PEBBLE in Door Open using different budgets of feedback queries. The solid/dashed line and shaded regions represent the mean and standard deviation, respectively, across five runs.

in publicly released repository URLB (https://anonymous.4open.science/r/urlb). As for hyperparameter related to exploration, we consider $\beta_0 = 0.05$, $\rho \in \{0.001, 0.0001, 0.00001\}$.

C ADDITIONAL EXPERIMENT RESULTS

Improving Feedback-Efficiency. We provide additional experimental results on various tasks from Meta-World benchmark Yu et al. (2020) using different budgets of feedback queries during training. We report asymptotic evaluation success rate at the end of training in Table 1. Here we report corresponding learning curves and additional results of wider choices of total feedback queries. We observe RUNE performs consistently at least same or better than PEBBLE baseline in different tasks with different budgets of feedback queries.

Improving Sample-Efficiency. As shown in Figure 9(a), RUNE outperforms other existing exploration baselines measured on the episode return of Pick Place. This shows applicability of our method on harder tasks.

Reward Functions Learned by RUNE. We provide additional analysis of reward functions learned by RUNE, compared to true reward function defined by Meta-World environments. Figure 10 demonstrates in all tasks we consider, learned reward functions optimized by RUNE is well-aligned to true reward from teacher feedback, because it can capture diverse patterns of true reward values from the environment.



(a) Drawer Open (feedback = 7K) (b) Drawer Open (feedback = 5K) (c) Drawer Open (feedback = 3K)

Figure 7: RUNE performs better than PEBBLE in Drawer Open using different budgets of feedback queries. The solid/dashed line and shaded regions represent the mean and standard deviation, respectively, across five runs.



(d) Sweep Into (feedback = 5K) (e) Window Close(feedback=500) (f) Door Unlock (feedback=2500)

Figure 8: RUNE performs better than PEBBLE in variety of manipulation tasks using different budgets of feedback queries. The solid/dashed line and shaded regions represent the mean and standard deviation, respectively, across five runs.



Figure 9: (a) RUNE achieves better sample-efficiency on manipulation tasks from Meta-World benchmark. (b/c) EPIC distance between the ensemble of learned reward functions and true reward in task environments. The solid/dashed line and shaded regions represent the mean and standard deviation, respectively, across five runs.



Figure 10: Time series of normalized learned reward (blue) and the ground truth reward (red) using rollouts from a policy optimized by RUNE.