A COMPREHENSIVE GRAPH POOLING BENCHMARK: EFFECTIVENESS, ROBUSTNESS AND GENERALIZABILITY

Anonymous authors

006

008 009 010

011

013

014

015

016

017

018

019

021

023

025

026

027

028 029 030

031

Paper under double-blind review

Abstract

Graph pooling has gained attention for its ability to obtain effective node and graph representations for various downstream tasks. Despite the recent surge in graph pooling approaches, there is a lack of standardized experimental settings and fair benchmarks to evaluate their performance. To address this issue, we have constructed a comprehensive benchmark that includes 17 graph pooling methods and 28 different graph datasets. This benchmark systematically assesses the performance of graph pooling methods in three dimensions, i.e., effectiveness, robustness, and generalizability. We first evaluate the performance of these graph pooling approaches across different tasks including graph classification, graph regression and node classification. Then, we investigate their performance under potential noise attacks and out-of-distribution shifts in real-world scenarios. We also involve detailed efficiency analysis, backbone analysis, parameter analysis and visualization to provide more evidence. Extensive experiments validate the strong capability and applicability of graph pooling approaches in various scenarios, which can provide valuable insights and guidance for deep geometric learning research. The source code of our benchmark is available at https://anonymous. 4open.science/r/Graph_Pooling_Benchmark-8EDD.

1 INTRODUCTION

032 Recently, graph neural networks (GNNs) have garnered significant attention with extensive bench-033 marks (Tan et al., 2023; Li et al., 2024; Hu et al., 2020a) due to their remarkable ability to process 034 graph-structured data across various domains including social networks (Wu et al., 2020a; Yang et al., 2021; Zhang et al., 2022), rumor detection (Bian et al., 2020; Zhang et al., 2023), biological 035 networks (Wu et al., 2018; Choi et al., 2020), recommender systems (Ma et al., 2020a) and community detection (Alsentzer et al., 2020; Sun et al., 2022). Graph pooling approaches play a crucial 037 role in GNNs by enabling the hierarchical reduction of graph representations, which is essential for capturing multi-scale structures and long-range dependencies (Liu et al., 2022a; Wu et al., 2022b; Dwivedi et al., 2023). They can preserve crucial topological semantics and relationships, which have 040 shown effective for tasks including graph classification, node clustering, and graph generation (Liu 041 et al., 2022a; 2020; Grattarola et al., 2022a; Li et al., 2024). In addition, by aggregating nodes and 042 edges, graph pooling can also simplify large-scale graphs, facilitating the application of GNNs in 043 real-world problems (Defferrard et al., 2016; Ying et al., 2018b; Mesquita et al., 2020; Zhang et al., 044 2020b; Tsitsulin et al., 2023b). Therefore, understanding and enhancing graph pooling approaches 045 is the key to increasing GNN performance, driving the progress of deep geometric learning.

In literature, existing graph pooling approaches can be roughly divided into two categories (Bianchi & Lachi, 2024; Liu et al., 2022a), i.e., node dropping pooling (Knyazev et al., 2019; Lee et al., 2019; Ranjan et al., 2020; Ma et al., 2020b; Zhang et al., 2020a; Zhou et al., 2022; Pang et al., 2021; Bacciu et al., 2023; Zhang et al., 2020a; 2019; Song et al., 2024) and node clustering pooling approaches (Ying et al., 2018a; Bianchi et al., 2020; Duval & Malliaros, 2022; Wu et al., 2022a; Hansen & Bianchi, 2023; Tsitsulin et al., 2023a; Bianchi, 2022), based on the strategies used to simplify the graph. node dropping pooling utilizes a learnable scoring function to remove nodes with relatively low significance scores, resulting in lower computational costs, while node clustering pooling approaches typically treat graph pooling as a node clustering problem, where clusters are considered

as new nodes for the coarsened graph (Liu et al., 2022b; Bianchi & Lachi, 2024). Even though graph 055 pooling research is becoming increasingly popular, there is still no standardized benchmark that al-056 lows for an impartial and consistent comparison of various graph pooling methods. Furthermore, due 057 to the diversity and complexity of graph datasets, numerous experimental settings have been used 058 in previous studies, such as varied proportions of training data and train/validation/test splits (Bian et al., 2020; Hansen & Bianchi, 2023; Dwivedi et al., 2023; Xu et al., 2024b). As a result, a comprehensive and publicly available benchmark of graph pooling approaches is highly expected that 060 can facilitate the evaluation and comparison of different approaches, ensuring the reproducibility of 061 results and further advancing the area of graph machine learning. 062

063 Towards this end, we present a comprehensive graph pooling benchmark, which includes 17 graph 064 pooling methods and 28 datasets across different graph machine learning problems. In particular, we extensively investigate graph pooling approaches across three key perspectives, i.e., effective-065 ness, robustness, and generalizability. To begin, we provide a fair and thorough effectiveness com-066 parison of existing graph pooling approaches across graph classification, graph regression and node 067 classification. Then, we evaluate the robustness of graph pooling approaches under both noise at-068 tacks on graph structures and node attributes. In addition, we study the generalizability of different 069 approaches under out-of-distribution shifts from both size and density levels. Finally, we include efficiency comparison, parameter analysis and backbone analysis for completeness. 071

Based on extensive experimental results, we have made the following observations: (1) Node clus-072 tering pooling methods outperform node dropping pooling methods in terms of robustness, gener-073 alizability, and performance on graph regression tasks. (2) Node clustering pooling methods incur 074 higher computational costs, and both approaches exhibit comparable performance on graph clas-075 sification tasks. (3) AsymCheegerCutPool and ParsPool demonstrate strong performance in graph 076 classification tasks. (4) As the scale of graph data decreases, the performance gap between dif-077 ferent graph pooling methods in node classification tasks increases, with KMISPool and ParsPool 078 exhibiting outstanding performance. (5) Most graph pooling approaches experience significant per-079 formance degradation due to distribution shifts and are also challenged by class imbalance issues, 080 but the extent of this impact varies across different datasets. (6) Node clustering pooling is relatively 081 superior to node dropping pooling in terms of robustness and generalizability, while KMISPool 082 demonstrates relatively better robustness and generalizability in node dropping pooling methods.

- ⁰⁸³ The main contributions of this paper are as follows:
- 084 085

Comprehensive Benchmark. We present a comprehensive graph pooling benchmark, which incorporates 17 state-of-the-art graph pooling approaches and 28 diverse datasets across graph classification, graph regression, and node classification.

• *Extensive Analysis.* To investigate the pros and cons of graph pooling approaches, we thoroughly evaluate current approaches from three perspectives, i.e., *effectiveness, robustness,* and *generaliz-ability*, which can serve as guidance for researchers in different applications.

 Open-source Material. We have made our benchmark of all these graph pooling approaches available and reproducible, and we believe our benchmark can benefit researchers in both graph machine learning and interdisciplinary fields.

095 096

097

2 PRELIMINARIES

Notations. Consider a graph G characterized by a vertex set V and an edge set E. The features associated with each vertex are represented by the matrix $X \in \mathbb{R}^{|V| \times d}$, where |V| denotes the number of vertices, and d signifies the dimensionality of the attribute vectors. The adjacency relationships within the graph are encapsulated by the adjacency matrix $A \in \{0, 1\}^{|V| \times |V|}$, where an entry A[i, j] = 1 indicates the presence of an edge between vertex v_i and vertex v_j ; otherwise, A[i, j] = 0.

Graph Pooling (Liu et al., 2022b; Grattarola et al., 2022b; Bianchi & Lachi, 2024). The aim of graph pooling is to reduce the spatial size of feature maps while preserving essential semantics, which thereby decreases computational complexity and memory usage. In this work, we focus on hierarchical pooling approaches (Ying et al., 2018b). Let POOL denote a graph pooling function



Figure 1: Overview of our hierarchical backbone for graph classification and graph regression.

which maps G to a graph G' = (V', E') with the reduced size:

116

117 118 119

120 121

122

137 138 139

145 146 147

148

149

150

$$G' = \text{POOL}(G), \tag{1}$$

where |V'| < |V|. the process has two main principal components, i.e., *reduction*, and *connection* (Grattarola et al., 2022b). In particular, the reduction component aims to generate pooled nodes and their attributes in G' during the connection. The connection component computes the edges E' among the V' nodes.

Graph Classification and Regression (Knyazev et al., 2019; Chen et al., 2019; Grattarola et al., 128 2022b). The two primary graph-level tasks are graph regression and graph classification. Here, a 129 graph dataset \mathcal{G} is provided as a set of graph-label pairs (G_i, y_i) , where y_i denotes the label for 130 graph G_i . The objective is to train a powerful discriminative model f that predicts the correct label 131 y_i given an input graph G_i . In graph classification, y_i are categorical labels $1, \dots, K$ with K as 132 the number of classes, while in graph regression, y_i are continuous values. A well-trained graph 133 classification model should output labels that closely match the true labels, and similarly, a graph 134 regression model should predict values that are nearly identical to the ground truth values. In these 135 tasks, graph pooling always accompanies graph convolutional operators. In formulation, the basic updating rule is written as follows: 136

$$\boldsymbol{H}^{(l+1)} = \sigma(\tilde{\boldsymbol{D}}^{-\frac{1}{2}}\tilde{\boldsymbol{A}}\tilde{\boldsymbol{D}}^{-\frac{1}{2}}\boldsymbol{H}^{(l)}\boldsymbol{W}^{(l)}), \qquad (2)$$

where $H^{(l)}$ denotes the node feature matrix at layer l, $W^{(l)}$ denotes the weight matrix at the corresponding layer, $\tilde{A} = A + I$ is the adjacency matrix A plus the identity matrix I, \tilde{D} is the degree matrix of \tilde{A} , and σ is a nonlinear activation function (Kipf & Welling, 2016a). The pooling layers can be formulated as:

$$\boldsymbol{H}^{(pool)} = \text{POOL}(\boldsymbol{H}^{(L)}), \qquad (3)$$

where $H^{(pool)}$ is the node feature matrix after pooling We iteratively conduct graph convolution and graph pooling operators and adopt a readout function to output the graph representation for downstream tasks. The overview of the basic hierarchical backbone can be found in Figure 1.

Node Classification (Kipf & Welling, 2016a; Veličković et al., 2018; Perozzi et al., 2014). The aim 151 of node classification is to assign semantic labels to nodes in a graph according to their attributes 152 and relationships with different nodes. Each dataset involves a graph G, consisting of nodes v_i and 153 their corresponding labels y_i . |V| is divided into a labeled set V^l and a unlabeled set V^u . We are 154 required to train a graph neural network model that can predict the missing labels of nodes in V^u 155 using the attributes of other nodes. U-Net framework (Ronneberger et al., 2015) is widely used 156 to incorporate pooling operations for node classification. In the encoder part, U-Net progressively 157 applies pooling and graph convolution to downsample the graphs and extract multi-scale features. 158 The decoder part of U-Net utilizes upsampling and graph convolution to gradually upsample the low-resolution feature maps back to the original graph size. Residual connections are employed 159 to directly transfer the feature maps from the encoder to the decoder, facilitating the preservation 160 of fine-grained semantics during upsampling (Ronneberger et al., 2015; Ibtehaz & Rahman, 2020; 161 Leng et al., 2018). For more information about the U-Net, please refer to Appendix B.

Methods		Datasets	Tasks
Node Dropping Poolin	g		
TopKPool	NIPS'19	MNIST, COLLAB, PROTEINS, D&D	Graph Classification
SAGPool	ICML'19	D&D, PROTEINS, NCI1, NCI109, FRANKENSTEIN	Graph Classification
ASAPool	AAAI'20	D&D, PROTEINS, NCI1, NCI109, FRANKENSTEIN	Graph Classification
PANPool	NIPS'20	PROTEINS, PROTEINS_FULL, NCI1, AIDS, MUTAGENCITY	Graph Classification
COPool	ECMLPKDD'22	BZR, AIDS, NCI1, NCI109, PROTEINS, QM7, IMDB-M	Graph Classification, Graph Regression
CGIPool	SIGIR'22	NCI1, NCI109, MUTAG, IMDB-B, IMDB-M, COLLAB, PROTEINS	Graph Classification
KMISPool	AAAI'23	D&D, REDDIT-B, REDDIT-5K, REDDIT-12K, Github	Graph Classification, Node Classification
GSAPool	WWW'20	D&D, NCI1, NCI109, MUTAG	Graph Classification
HGPSLPool	Arxiv'19	D&D, PROTEINS, NCI1, NCI109, ENZYMES, MUTAG	Graph Classification
Node Clustering Pooli	ng		
AsymCheegerCutPool	ICML'23	Cora, Citeseer, Pubmed, DBLP	Node Classification
DiffPool	NIPS'18	D&D, PROTEINS, COLLAB, ENZYMES, REDDIT-MULTI	Graph Classification
MincutPool	ICML'20	D&D, PROTEINS, COLLAB, REDDIT-B, MUTAG, QM9	Graph Classification, Graph Regression
DMoNPool	JMLR'23	Cora, Citeseer Pubmed, Coauthor	Node Classification
HoscPool	CIKM'22	Cora, Citeseer Pubmed, Coauthor, DBLP, Email-EU	Node Classification
JustBalancePool	Arxiv'22	Cora, Citeseer, Pubmed, DBLP	Node Classification
SEPool	ICML'22	IMDB-B, IMDB-M, COLLAB, MUTAG, Cora, Citeseer, Pubmed	Graph Classification, Node Classification
ParsPool	ICLR'24	D&D, PROTEINS, NCI1, NCI109, Ogbg-molpcba, Cora, Citeseer, Pubmed	Graph Classification, Node Classification

162	Table 1: Overview of experimental details of graph pooling research. These papers utilize differen
162	settings, which validates the necessity of building a comprehensive and fair benchmark.

178

188 189

3 GRAPH POOLING BENCHMARK

179 3.1 GRAPH POOLING APPROACHES

Our benchmark contains 17 state-of-the-art graph pooling approaches (detailed in Table 1): Top-KPool (Knyazev et al., 2019), SAGPool (Lee et al., 2019), ASAPool (Ranjan et al., 2020), PANPool (Ma et al., 2020b), COPool (Zhou et al., 2022), CGIPool (Pang et al., 2021), KMIS-Pool (Bacciu et al., 2023), GSAPool (Zhang et al., 2020a), HGPSLPool (Zhang et al., 2019), Asym-CheegerCutPool (Hansen & Bianchi, 2023), DiffPool (Ying et al., 2018a), MincutPool (Bianchi et al., 2020), DMoNPool (Tsitsulin et al., 2023a), HoscPool (Duval & Malliaros, 2022), JustBalancePool (Bianchi, 2022), SEPool (Wu et al., 2022a), and ParsPool (Song et al., 2024). More information related to the selected pooling methods can be found in the Appendix C.

3.2 DATASETS

190 To systematically evaluate graph pooling methods, we integrate 28 datasets from different domains. 191 For graph classification, we select eleven publicly available datasets from TUDataset (Morris et al., 192 2020), including seven molecules datasets, i.e., MUTAG (Debnath et al., 1991), NCI1 (Wale et al., 193 2008), NCI109 (Wale et al., 2008), COX2 Sutherland et al. (2003), AIDS Riesen & Bunke (2008), 194 FRANKENSTEIN Orsini et al. (2015), and Mutagenicity Debnath et al. (1991), four bioinformat-195 ics datasets, i.e. D&D (Shervashidze et al., 2011), PROTEINS (Borgwardt et al., 2005), PRO-196 TEINS_FULL (Borgwardt et al., 2005), and ENZYMES (Schomburg et al., 2004), three social net-197 work dataset, i.e., IMDB-BINARY (IMDB-B) (Cai & Wang, 2018), IMDB-MULTI (IMDB-M) (Cai 198 & Wang, 2018), and COLLAB (Cai & Wang, 2018). We also include a large-scale graph classifi-199 cation dataset, Ogbg-molpcba, from the Open Graph Benchmark (OGB) (Hu et al., 2020b). For graph regression, we choose six datasets from MoleculeNet (Wu et al., 2018) including QM7, QM8, 200 BACE, ESOL, FreeSolv, and Lipophilicity. For node classification, we utilize three citation net-201 works, i.e., Cora, Citeseer, and Pubmed (Yang et al., 2016), three website networks, i.e., Cornell, 202 Texas, and Wisconsin (Pei et al., 2020), and the GitHub dataset (Rozemberczki et al., 2021). We 203 also obtain a large-scale dataset, Ogbn-arxiv, from OGB (Hu et al., 2020b). More information about 204 the summary statistics and description of the datasets are detailed in the Appendix D. 205

206 207 3.3 EVALUATION PROTOCOLS

208 Our benchmark evaluation encompasses three key aspects, i.e., effectiveness, robustness, and gen-209 eralizability. We perform a hyperparameter search for all pooling methods; detailed information 210 can be found in Appendix E. Firstly, we conduct a performance comparison of graph pooling ap-211 proaches across three tasks including graph classification, graph regression, and node classification. 212 For graph and node classification tasks, we employ average precision for Ogbg-molpcba, and accuracy for remaining datasets as the evaluation metric. For graph regression, we use root mean 213 square error (RMSE) for ESOL, FreeSolv, and Lipophilicity (Wu et al., 2018). Following previous 214 research (Xu et al., 2024b), we use the area under the receiver operating characteristic (AUROC) 215 curve to evaluate BACE, and mean absolute error (MAE) for QM7 and QM8. Secondly, our bench-

216 Table 2: Results of graph classification for different graph pooling methods. The mean and variance 217 of average precision (Ogbg-molpcba) and accuracy (remaining datasets) are reported. The best and 218 2nd best are noted in bold font and underlined, respectively. OOM denotes out of GPU memory, 219 and OOT denotes cannot be computed within 24 hours.

Methods	Ogbg-molpcba	PROTEINS	NCI1	NCI109	MUTAG	D&D	IMDB-B	IMDB-M	COLLAB	Avg.	R
Node Drop Pooling											
TopKPool	15.79 ± 0.42	70.83±1.25	$70.34{\pm}1.80$	69.65±1.61	$82.76 {\pm} 4.88$	69.07±5.52	74.44±3.71	48.44 ± 3.46	75.38±1.13	70.11	1
SAGPool	21.08 ± 2.19	74.64±1.53	73.10±1.21	71.29 ± 0.82	81.61 ± 5.86	73.27±1.12	75.33±3.31	48.74 ± 3.09	77.91±2.22	71.99)
ASAPool	OOT	73.69±1.48	73.48±1.03	70.45 ± 0.84	72.41±10.15	OOT	71.56±3.46	46.96±3.72	OOT	68.09)
PANPool	21.81±0.99	70.60 ± 1.67	73.29 ± 1.07	70.84±1.23	78.16 ± 8.60	73.27 ± 4.05	73.33±3.57	47.70 ± 3.58	$78.40{\pm}2.80$	70.70	1
COPool	25.50 ± 2.46	75.24±2.46	74.10 ± 1.06	71.35±1.05	83.91±3.25	73.57±0.42	74.44 ± 4.40	48.89 ± 3.82	81.33±1.15	72.85	1
CGIPool	23.78±6.71	73.57±1.49	75.72 ± 1.65	73.81±0.42	86.21 ± 4.88	72.07 ± 1.47	74.22 ± 3.62	46.22 ± 2.02	80.40 ± 1.71	72.78	5
KMISPool	26.85 ± 0.28	70.63 ± 1.01	73.15 ± 2.19	73.17±1.10	80.46 ± 4.30	70.57±1.70	72.89 ± 3.62	46.96 ± 2.47	80.71±0.49	71.07	1
GSAPool	26.95±1.36	72.14±1.09	71.12±1.33	70.65 ± 1.45	87.36±1.63	72.97±1.27	74.67±3.93	46.37±4.13	$76.84{\pm}2.11$	71.52	1
HGPSLPool	22.78 ± 0.51	72.02 ± 1.73	72.22 ± 0.42	70.35 ± 1.31	71.26 ± 12.70	73.27 ± 2.78	72.89 ± 4.37	46.81 ± 2.19	79.24 ± 0.80	69.76	
Node Clustering Pooli	ng										
AsymCheegerCutPool	$24.82 {\pm} 0.60$	$74.60{\pm}1.96$	75.90±1.69	73.98±1.88	$89.66 {\pm} 2.82$	74.47±2.36	74.89 ± 3.14	$48.30 {\pm} 3.63$	$80.62{\pm}1.06$	74.05	;
DiffPool	25.21 ± 0.42	74.80 ± 1.71	74.72 ± 1.82	75.16±0.35	80.46 ± 5.86	73.57±1.85	74.44 ± 0.63	47.70 ± 4.01	78.89 ± 0.55	72.47	
MincutPool	24.97 ± 0.41	72.42 ± 1.71	75.53 ± 1.15	74.30±1.33	85.06±1.63	71.77 ± 2.12	73.78 ± 3.94	45.93 ± 2.55	76.53±1.60	71.91	
DMoNPool	24.75 ± 0.67	68.45 ± 4.79	72.45 ± 0.15	71.18 ± 1.66	75.86 ± 5.63	75.38 ± 0.42	73.33 ± 3.81	47.26 ± 1.68	77.07 ± 0.44	70.12	1
HoscPool	24.63 ± 0.37	72.42 ± 0.74	$76.88 {\pm} 0.61$	76.13±1.97	85.06±1.63	71.77 ± 2.12	74.67 ± 1.96	45.93±2.77	78.18±1.69	72.63	7
JustBalancePool	25.19 ± 0.42	68.85 ± 2.97	76.34 ± 0.46	$76.34{\pm}1.51$	81.61±1.63	71.77 ± 2.12	74.89 ± 4.09	45.93 ± 5.08	77.87±1.26	71.70	J
SEPool	OOT	62.25 ± 4.57	62.77±2.25	63.74 ± 2.30	67.22 ± 8.41	80.26±3.04	77.00±4.05	54.13±3.71	$75.64{\pm}2.04$	67.88	5
ParsPool	26.63 ± 0.30	75.02 ± 0.64	77.07±0.23	76.20±0.44	79.31±5.63	76.10 ± 0.80	75.11±2.20	49.48 ± 0.91	83.60±0.50	73.99)

mark evaluates the robustness of graph pooling approaches in both graph-level and node-level tasks across two perspectives: structural robustness and feature robustness (Li & Wang, 2018). In particular, we add and drop edges of graphs to study structural robustness and mask node features to investigate feature robustness. Thirdly, we employ size-based and density-based distribution shifts to evaluate the generalizability of different pooling methods in graph-level tasks under real-world 238 scenarios (Gui et al., 2022). We also use degree-based and closeness-based distribution shifts to assess the generalizability of different pooling methods in node-level tasks. In addition to these three views, we conduct a further analysis of these graph pooling approaches including the comparison of 240 efficiency, visualization, and different backbone parameter choices.

241 242 243

244 245

246 247

248

249

250

251

252 253 254

255

232 233

234

235

236

237

239

4 EXPERIMENT

4.1 EXPERIMENTAL SETTINGS

All graph pooling methods in our benchmark are implemented by PyTorch (Paszke et al., 2019). Graph convolutional networks serve as the default encoders for all algorithms. The experimental setup includes a Linux server equipped with NVIDIA A100 GPUs, with an Intel Xeon Gold 6354 CPU. The software stack comprises PyTorch 1.11.0, PyTorch-geometric 2.1.0 (Fey & Lenssen, 2019), and Python 3.9.16. More details about experimental settings can be found in Appendix E.

4.2 EFFECTIVENESS ANALYSIS

Performance on Graph Classification. To begin, we investigate the performance of different graph 256 pooling approaches on graph classification. The results of compared approaches on seven popular 257 datasets are recorded in Table 2. Firstly, in general, ParsPool, AsymCheegerCutPool, and COPool 258 are the three best-performing pooling models, and the performance of all 17 pooling methods varies 259 significantly across different datasets. No single pooling method consistently outperforms the oth-260 ers across all datasets. Secondly, it is noteworthy that SEPool achieves significant advantages on 261 D&D, IMDB-B, and IMDB-M. This is because SEPool's coding tree structure, and these datasets 262 are characterized by high clustering coefficients Watts & Strogatz (1998), which benefits the cod-263 ing tree method because the hierarchical nature of the tree can better capture and represent these 264 localized, highly connected substructures (Wu et al., 2022a). However, SEPool also implies greater 265 computational resource overhead, which presents challenges when processing large-scale graph data 266 such as Ogbg-molpcba. *Thirdly*, the methods with the highest average accuracy are ParsPool and AsymCheegerCutPool. ParsPool can capture a personalized pooling structure for each individual 267 graph, while AsymCheegerCutPool calculates cluster assignments based on a tighter relaxation in 268 terms of Graph Total Variation (GTV) (Song et al., 2024; Hansen & Bianchi, 2023). These methods 269 are flexible, and the datasets differ significantly in diameter, degree, and clustering coefficients.

Table 3: Results of graph regression for different pooling methods. The mean and variance of MAE (QM7, QM8), AUROC (BACE), RMSE (ESOL, FreeSolv, Lipophilicity) are reported. - denotes cannot converge.

Methods	QM7	QM8	BACE	ESOL	FreeSolv	Lipophilicity	Rank
Node Drop Pooling							
TopKPool	63.39±9.66	$0.021{\pm}0.001$	0.85±0.02	$0.96 {\pm} 0.06$	$1.92{\pm}0.37$	$0.80{\pm}0.02$	8.1
SAGPool	97.69±11.19	$0.023 {\pm} 0.001$	$0.84{\pm}0.01$	$1.16 {\pm} 0.07$	2.31 ± 0.66	$0.93 {\pm} 0.06$	13.1
ASAPool	56.79 ± 6.17	$0.029 {\pm} 0.008$	$0.85{\pm}0.02$	$0.92{\pm}0.03$	$1.92{\pm}0.37$	$0.78 {\pm} 0.05$	8.2
PANPool	53.04 ± 1.20	$0.015 {\pm} 0.000$	$0.83 {\pm} 0.02$	$1.01{\pm}0.03$	$1.80{\pm}0.10$	$0.84{\pm}0.01$	9.7
COPool	84.22 ± 3.28	$0.020{\pm}0.001$	$0.85{\pm}0.01$	$0.98 {\pm} 0.07$	$1.85 {\pm} 0.24$	$0.85 {\pm} 0.02$	8.5
CGIPool	97.41±16.25	$0.020{\pm}0.001$	$0.84{\pm}0.03$	$1.59{\pm}0.62$	$2.49 {\pm} 0.97$	$0.83 {\pm} 0.07$	11.7
KMISPool	80.51 ± 21.34	0.017 ± 0.001	$0.85{\pm}0.02$	$0.95 {\pm} 0.04$	$1.29{\pm}0.18$	$0.81{\pm}0.03$	5.9
GSAPool	106.72 ± 22.90	0.021 ± 0.001	$0.85{\pm}0.02$	$0.96 {\pm} 0.08$	1.95 ± 0.26	$0.82{\pm}0.03$	8.8
HGPSLPool	47.88±0.83	$0.015 {\pm} 0.000$	$0.84{\pm}0.01$	$1.02{\pm}0.06$	$1.62 {\pm} 0.09$	$0.76 {\pm} 0.01$	7.8
Node Clustering Poolin	ıg						
AsymCheegerCutPool	64.91±8.30	0.031 ± 0.005	0.84 ± 0.01	0.99 ± 0.12	2.00 ± 0.18	0.95 ± 0.11	12.9
DiffPool	54.98 ± 3.44	0.037 ± 0.010	0.84 ± 0.02	0.81 ± 0.05	1.20 ± 0.09	0.73 ± 0.03	8.0
MincutPool	-	0.020 ± 0.001	$\textbf{0.85} \pm \textbf{0.02}$	0.76 ± 0.02	1.19 ± 0.18	0.73 ± 0.02	4.3
DMoNPool	-	0.021 ± 0.001	$\textbf{0.85} \pm \textbf{0.02}$	$\textbf{0.68} \pm \textbf{0.02}$	$\underline{1.16\pm0.15}$	$\textbf{0.69} \pm \textbf{0.02}$	3.5
HoscPool	$59.44{\pm}21.48$	0.019 ± 0.002	0.84 ± 0.01	0.76 ± 0.02	$\textbf{1.14} \pm \textbf{0.13}$	0.72 ± 0.02	4.6
JustBalancePool	-	0.022 ± 0.004	$\textbf{0.85} \pm \textbf{0.02}$	$\underline{0.74\pm0.03}$	1.26 ± 0.16	$\underline{0.70\pm0.01}$	4.9

Table 4: Results of **node classification** for different pooling methods. No Pooling denotes without pooling layers.

Methods	Ogbn-arxiv	Cora	Citeseer	Pubmed	Cornell	Texas	Wisconsin	Github	Avg.	Rank
TopKPool	$53.36 {\pm} 0.03$	88.91±0.93	$77.56 {\pm} 0.85$	86.13±0.34	49.09±2.57	$54.18 {\pm} 4.80$	$51.58 {\pm} 3.05$	86.95±0.20	67.91	8.00
SAGPool	$53.39 {\pm} 0.02$	$89.18 {\pm} 0.65$	77.56 ± 0.81	86.07 ± 0.70	81.09 ± 3.74	55.64 ± 2.95	51.32 ± 3.53	$86.99 {\pm} 0.22$	73.48	5.33
ASAPool	OOM	$89.10 {\pm} 0.86$	$77.76 {\pm} 1.01$	$85.74 {\pm} 0.18$	79.64±2.91	54.55 ± 4.74	50.79 ± 3.49	OOM	72.93	6.83
PANPool	OOM	89.05 ± 0.96	77.20 ± 0.98	$85.88 {\pm} 0.11$	78.91 ± 2.47	56.36 ± 5.14	50.53 ± 3.18	OOM	72.99	8.00
COPool	OOM	89.00 ± 0.70	77.26 ± 0.89	85.27 ± 0.27	77.82 ± 3.13	56.36 ± 5.98	52.37 ± 2.68	$86.68 {\pm} 0.20$	73.01	7.50
CGIPool	$53.60 {\pm} 0.39$	89.15 ± 0.84	$77.40 {\pm} 0.81$	$85.92 {\pm} 0.66$	$81.82{\pm}4.30$	54.55 ± 4.15	51.05 ± 3.85	$86.88 {\pm} 0.22$	73.32	6.33
KMISPool	$53.38 {\pm} 0.08$	$89.74 {\pm} 0.02$	77.75 ± 0.01	$87.80 {\pm} 0.01$	79.56±1.31	81.42 ± 1.64	82.31 ± 0.50	87.09 ± 0.04	83.10	2.50
GSAPool	$53.76 {\pm} 0.11$	89.05 ± 0.77	77.16 ± 0.92	86.21±0.73	80.36 ± 3.71	54.18 ± 3.88	51.84 ± 4.29	$87.12 {\pm} 0.09$	73.13	6.67
HGPSLPool	OOM	$89.08 {\pm} 0.83$	$77.84 {\pm} 0.67$	OOM	58.55 ± 3.71	55.27 ± 3.37	51.58 ± 1.75	OOM	69.71	6.33
SEPool	OOT	$83.17 {\pm} 0.00$	$70.47 {\pm} 0.00$	79.33 ± 0.80	$51.35 {\pm} 0.00$	66.66 ± 6.50	57.51 ± 0.85	OOT	68.08	8.67
ParsPool	OOM	$84.51 {\pm} 0.35$	$74.27 {\pm} 0.38$	$89.20{\pm}0.00$	$72.07{\pm}6.49$	$81.98{\pm}6.49$	$82.35 {\pm} 17.94$	OOM	80.73	5.50
No Pooling	$\underline{53.61{\pm}0.07}$	$\underline{89.48{\pm}0.27}$	$77.69 {\pm} 0.24$	$86.10{\pm}0.06$	$48.83{\pm}1.24$	$56.50{\pm}1.11$	$54.43{\pm}1.54$	$86.46{\pm}0.02$	68.84	5.17

288 289

290

291

293

301

302 Performance on Graph Regression. We further explore the performance of different pooling meth-303 ods through graph-level regression tasks. As shown in Table 3, we can observe that: *Firstly*, overall, 304 node clustering pooling methods outperform node dropping pooling methods, with DMoNPool and MincutPool showing the best performance. The possible reason is that in graph regression tasks, the 305 model's objective is to predict a continuous numerical output. Such tasks typically require capturing 306 global structural features and continuity within the graph. Compared to node clustering pooling, 307 node dropping pooling tends to lose more global information (Tsitsulin et al., 2023a; Bianchi et al., 308 2020). DMoNPool and MincutPool are more inclined to maintain the global characteristics of the 309 graph rather than emphasizing the representation of locally important structures, which may result 310 in their performance being inferior to that of ParsPool, AsymCheegerCutPool, and COPool in graph 311 classification tasks. Secondly, in the BACE dataset, the performance of most pooling methods tends 312 to be consistent, whereas in other datasets, there is a greater variance in performance. The possible 313 reason is that although the graphs in the BACE dataset are relatively large, the average diameter 314 is relatively small, so different pooling methods face fewer challenges in summarizing the global 315 structural information of the graphs, which may lead to more consistent performance.

316 **Performance on Node Classification.** Table 4 presents the performance of various pooling methods 317 in node classification tasks. We observe the following: *Firstly*, KMISPool and ParsPool demonstrate 318 the best overall performance, significantly outperforming other methods on small-scale datasets 319 such as Cornell, Texas, and Wisconsin. Secondly, node classification models without pooling layers 320 achieve comparable results to most pooling methods across the majority of datasets. A potential rea-321 son for this is that pooling operations tend to lose substantial node information, which consequently weakens performance in node classification tasks. *Thirdly*, the scalability of ASAPool, PANPool, 322 HGPSLPool, SEPool, and ParsPool still requires improvement, as they face memory/runtime bot-323 tlenecks, making it cannot complete training on larger datasets such as Ogbn-arxiv or GitHub.

Dataset	Ptb Method	TopKPool	SAGPool	ASAPool	PANPool	KMISPool	DiffPool	MincutPool	JustBalancePoo
	ADD	73.58±5.77	72.76±3.87	74.59 ± 3.74	39.63±42.27	71.14±0.57	73.78±2.59	72.36±2.92	75.00±1.49
PROTEINS	DROP	71.95 ± 2.28	$73.58 {\pm} 2.55$	72.76 ± 1.88	$38.62{\pm}42.97$	$71.34{\pm}1.32$	$71.34{\pm}1.80$	$71.75 {\pm} 2.07$	73.37±1.25
	MASK	$72.56 {\pm} 3.11$	$73.78{\pm}3.45$	$71.14{\pm}2.55$	$72.88{\pm}4.71$	72.97 ± 2.24	$72.97{\pm}0.29$	$72.36{\pm}3.24$	70.12 ± 2.28
	ADD	$65.91 {\pm} 0.65$	67.53±2.25	$71.42{\pm}1.53$	$66.29 {\pm} 0.40$	$72.66{\pm}1.40$	72.66±0.20	$70.77 {\pm} 1.80$	73.96±0.08
NCI1	DROP	63.16 ± 1.52	$61.64{\pm}1.46$	64.07 ± 0.73	65.53 ± 1.31	$73.58{\pm}3.00$	66.18 ± 2.22	$65.05 {\pm} 0.73$	64.18 ± 1.61
	MASK	$63.86{\pm}1.39$	$63.16{\pm}2.10$	$66.94{\pm}0.87$	$66.18{\pm}0.61$	$65.15{\pm}2.30$	68.23±2.73	$67.10{\pm}2.07$	67.91 ± 1.98
	ADD	66.18±0.73	$68.55 {\pm} 1.13$	$69.62{\pm}2.11$	$64.84{\pm}2.74$	75.32±0.99	73.33±0.97	$71.34{\pm}2.89$	$71.29 {\pm} 2.79$
NCI109	DROP	63.59 ± 1.40	64.61 ± 1.49	$64.24{\pm}1.86$	$65.64{\pm}1.26$	73.85 ± 2.95	66.18±2.22	$65.05 {\pm} 0.73$	64.18 ± 1.61
	MASK	$65.22{\pm}1.97$	$66.61 {\pm} 0.92$	$65.65 {\pm} 1.08$	$\overline{66.29 \pm 0.91}$	$66.34{\pm}1.85$	$\underline{66.99{\pm}2.71}$	$68.23{\pm}0.47$	66.61±3.43
	ADD	86.21±5.63	$79.31{\pm}2.82$	$75.86{\pm}10.15$	$68.97 {\pm} 4.88$	$80.46{\pm}4.30$	72.41±9.75	$78.16{\pm}4.30$	$68.97 {\pm} 4.88$
MUTAG	DROP	87.36±4.30	63.22 ± 13.9	$72.41{\pm}14.90$	68.97 ± 2.82	$80.46 {\pm} 4.30$	$78.16{\pm}1.63$	74.71 ± 9.89	75.86±11.26
	MASK	$\textbf{78.16}{\pm}\textbf{16.26}$	64.37 ± 9.05	$60.92 {\pm} 7.09$	$71.26 {\pm} 3.25$	$83.91{\pm}8.13$	$78.16{\pm}4.30$	$77.01 {\pm} 3.25$	70.11 ± 4.30

Table 5: Results of **graph classification under random noise attack** for different pooling methods.

	Table of	5: Results	s of node	classifica	ation und	er rando	m noise	апаск 10	r ameren	t pooling	methods.
	Dataset	Ptb Method	TopKPool	SAGPool	ASAPool	PANPool	COPool	CGIPool	KMISPool	GSAPool	HGPSLPool
	Cora	ADD	$73.90{\pm}0.24$	$74.41 {\pm} 0.12$	OOM	$75.75{\pm}0.14$	$69.52{\pm}0.58$	$70.01 {\pm} 0.24$	$75.64{\pm}0.03$	$74.29{\pm}0.15$	$75.58{\pm}0.14$
		DROP	85.01 ± 0.09	85.45 ± 0.36	$85.40 {\pm} 0.19$	85.11±0.20	85.06 ± 0.13	$85.04 {\pm} 0.23$	85.83±0.21	$85.30 {\pm} 0.33$	$85.60 {\pm} 0.19$
		MASK	87.70±0.16	$87.75 {\pm} 0.18$	$\textbf{87.94}{\pm}\textbf{0.12}$	$87.48 {\pm} 0.24$	$86.88{\pm}0.26$	$87.42{\pm}0.03$	$87.81 {\pm} 0.17$	$\underline{87.83{\pm}0.37}$	87.59±0.24
		ADD	$62.64{\pm}0.19$	$62.47 {\pm} 0.41$	63.43±0.14	$63.38 {\pm} 0.37$	$62.62{\pm}0.21$	$61.94{\pm}0.29$	$63.52{\pm}0.20$	$62.69{\pm}0.23$	$63.42{\pm}0.21$
	Citeseer	DROP	75.31±0.26	$75.50 {\pm} 0.19$	75.81±0.04	$75.52{\pm}0.10$	$75.18 {\pm} 0.46$	$75.34{\pm}0.12$	$76.54{\pm}0.32$	$75.32{\pm}0.29$	76.00 ± 0.21
		MASK	$73.29{\pm}0.27$	$73.41 {\pm} 0.25$	73.57±0.17	$73.42 {\pm} 0.20$	$73.54{\pm}0.44$	$73.28{\pm}0.49$	$73.63{\pm}0.10$	$73.45{\pm}0.20$	73.30 ± 0.24

70.62±0.12 68.21±0.11 67.92±0.45 71.59±0.01 70.83±0.17

85.55±0.04 85.68±0.04 85.59±0.13 85.30±0.06 85.59±0.06

83.75±0.06 83.31±0.07 83.78±0.17 83.83±0.02 84.36±0.11

OOM

OOM

OOM

OOM

OOM

OOM

Pubmed

345 346

342

343

344

347

4.3 ROBUSTNESS ANALYSIS

71.06±0.25 70.75±0.41

85.46+0.09 86.03+0.12

84.24±0.04 84.34±0.06

ADD

DROP

MASK

The compared performance for three types of random noise on eight graph pooling methods on the 348 PROTEINS, NCI1, NCI109, and MUTAG datasets are shown in Table 5. With a probability of 50%, 349 edges of the graph are randomly removed or added, and node features are randomly masked. We 350 can observe that: Firstly, overall, node clustering pooling demonstrates better robustness against three types of attacks compared to node dropping pooling. Secondly, among node dropping pooling 351 methods, KMISPool generally performs the best. However, for small datasets such as MUTAG, Top-352 KPool achieves the highest performance under noise attacks, because its node selection mechanism 353 is less sensitive to local noise variations (Knyazev et al., 2019). Thirdly, noise attacking increases 354 the performance fluctuations of pooling methods, making their prediction results more unstable. 355 Fourthly, in larger datasets such as PROTEINS, NCI1, and NIC109, dropping edges has a greater 356 impact on performance, whereas for MUTAG, masking node features has a more significant effect. 357

Table 6 presents the results of the robustness analysis for node-level tasks. From Table 6, we observe the following: *Firstly*, random attacks on the graph lead to a decrease in performance on node classification tasks, with different types of attacks causing varying degrees of performance degradation. Randomly adding edges has the most negative impact on performance, while randomly deleting edges has the least impact. *Secondly*, for larger graphs such as Cora, Citeseer, and Pubmed, KMIS-Pool performs the best, whereas for smaller graphs such as Cornell, Texas, and Wisconsin, ASAPool performs better. Appendix F.1 provides results for the robustness analysis of node-level tasks.

As depicted in As shown in Figure 2, the model's performance generally declines as the noise intensity increases. It is observed that, at the same level of noise, the impact on accuracy is more pronounced on smaller datasets Cora and CiteSeer, while it is relatively minor on larger dataset Pubmed. Among the three types of noise, although the accuracy of nearly all methods decreases amidst fluctuations, KMISPool and PANPool exhibit the strongest robustness, while COPool performs relatively poorly, despite the fact that most pooling methods show very similar performance.

370 371 372

4.4 GENERALIZABILITY ANALYSIS

Table 7 and Table 8 presents the performance of different graph pooling methods under out-of-distribution shifts. For the graph-level datasets D&D and NCI1, we implement two types of distribution shifts. The first type is based on the number of nodes, where the smallest 50% of graphs by node count are used as the training set, and the largest 20% as the test set, with the remainder serving as the validation set (Bevilacqua et al., 2021; Chen et al., 2022). Following the same criteria, the second type of out-of-distribution shifts are generated based on graph density (Chen et al., 2022).



Figure 2: Performance of different approaches w.r.t. different rates of random noise.

403 Table 7: Results of graph classification under distribution shifts. Size and density denote two types of shifts across training and test datasets. Micro-F1 and Macro-F1 metrics are provided for 405 each shift type.

		Dð	&D		NCI1			
Method	Si	ize	Der	sity	Si	ze	Der	nsity
	Micro-F1	Macro-F1	Micro-F1	Macro-F1	Micro-F1	Macro-F1	Micro-F1	Macro-F1
Node Drop Pooling								
TopKPool	68.08 ± 1.60	63.69±1.13	31.98±15.37	29.43±15.16	$25.89 {\pm} 0.46$	24.98±0.43	53.48±2.11	51.02 ± 3.14
SAGPool	81.36 ± 2.49	74.47 ± 1.48	55.37 ± 0.89	$50.14 {\pm} 0.97$	25.08 ± 2.39	$23.90{\pm}2.95$	47.00 ± 3.60	45.86 ± 3.49
ASAPool	OOT	OOT	OOT	OOT	26.29 ± 3.66	25.29 ± 4.42	53.17 ± 1.85	$51.34{\pm}1.18$
PANPool	77.68 ± 8.37	71.44 ± 6.50	$41.92{\pm}10.72$	40.36 ± 10.05	25.00 ± 0.00	$23.74 {\pm} 0.08$	52.08 ± 2.24	49.14 ± 0.66
COPool	64.41±5.66	60.37±3.74	47.91±2.51	44.30 ± 1.81	27.99 ± 3.86	27.17 ± 4.48	54.67 ± 2.22	53.09 ± 2.35
CGIPool	75.99 ± 6.65	69.62 ± 5.58	56.38±1.76	51.10 ± 1.45	28.16 ± 5.18	27.26 ± 5.81	56.20 ± 0.86	53.93 ± 1.12
KMISPool	80.23 ± 5.24	73.30 ± 4.04	54.58 ± 5.26	49.81±3.62	50.97 ± 9.51	49.02 ± 7.87	55.42 ± 1.47	51.27 ± 0.30
GSAPool	58.19 ± 26.99	53.06 ± 25.69	33.79 ± 20.93	29.39±19.01	26.21 ± 1.24	25.19 ± 1.56	50.31±3.39	49.32 ± 2.65
HGPSLPool	85.59±1.20	78.34±1.66	52.43 ± 2.25	49.59 ± 1.89	$19.66 {\pm} 0.52$	17.52 ± 0.66	56.95 ± 1.64	51.93 ± 1.14
Node Clustering Pooling								
AsymCheegerCutPool	$74.47 {\pm} 0.06$	$73.60 {\pm} 0.06$	$86.13 {\pm} 0.00$	$50.86 {\pm} 0.01$	$48.87 {\pm} 3.06$	$45.42{\pm}1.65$	$70.01 {\pm} 0.00$	$46.95 {\pm} 0.00$
DiffPool	73.87 ± 0.02	73.35 ± 0.02	86.49 ± 0.02	47.44±0.01	$19.50 {\pm} 0.00$	16.63 ± 0.01	69.53±0.00	50.87 ± 0.15
MincutPool	69.97±0.17	67.95±0.17	87.39±0.00	46.63 ± 0.00	$19.58 {\pm} 0.00$	16.69 ± 0.00	$68.64 {\pm} 0.00$	$50.31 {\pm} 0.09$
DMoNPool	72.67 ± 0.11	72.25 ± 0.13	82.52 ± 0.00	$54.21 {\pm} 0.00$	79.29 ± 0.04	$64.30 {\pm} 0.00$	$68.92 {\pm} 0.00$	$48.76 {\pm} 0.02$
HoscPool	70.27 ± 0.01	69.20 ± 0.00	87.39±0.00	46.63 ± 0.00	24.60 ± 0.27	23.39 ± 0.36	$70.48 {\pm} 0.01$	56.55 ± 0.35
JustBalancePool	68.77 ± 0.00	67.82 ± 0.02	87.39±0.00	46.63 ± 0.00	$19.98 {\pm} 0.00$	$17.28 {\pm} 0.01$	$68.64 {\pm} 0.00$	$50.31 {\pm} 0.09$
ParsPool	68.36 ± 1.60	62.50 ± 1.76	63.06 ± 4.84	48.35 ± 0.86	52.59 ± 4.46	49.95 ± 3.32	56.27 ± 1.97	52.96 ± 0.88

402

404

421 For the node-level datasets Cora and Citeseer, the first type of out-of-distribution shift is the top 422 50% of nodes with the highest degrees as the training set, the bottom 25% with the lowest degrees 423 as the test set, and the remaining nodes as the validation set. The second type is based on closeness centrality (the reciprocal of the sum of the shortest path lengths from a node to all other nodes). 424 We use the 50% of nodes with the lowest closeness as the training set, the 25% with the highest 425 closeness as the test set, and the remaining nodes as the validation set. For further details and more 426 experiments for the generalizability analysis, please refer to the Appendix D.4 and Appendix F.2. 427

428 From Tables 7 and 8, we have the following observations. *Firstly*, node-level out-of-distribution 429 shifts also reduce the performance of pooling models, but the extent of this reduction is smaller compared to out-of-distribution shifts in graph classification tasks. The potential reason is that, in 430 node-level tasks, the propagation of information are usually confined to the local neighborhood of 431 nodes, whereas graph-level tasks require handling information spread over a larger scope. Secondly,

		Co	ora			Cite	eseer		
Method	Degree		Closeness		Deg	Degree		Closeness	
	Micro-F1	Macro-F1	Micro-F1	Macro-F1	Micro-F1	Macro-F1	Micro-F1	Macro-F1	
TopKPool	83.65±0.50	82.29±0.47	83.21±0.18	81.98±0.31	67.27±0.35	63.60±0.26	72.28±0.67	65.64±1.0	
SAGPool	84.19±0.12	82.73±0.27	81.68 ± 1.54	80.34±1.55	$65.46 {\pm} 0.61$	62.22 ± 0.49	72.28 ± 1.10	66.35±1.87	
ASAPool	$\overline{83.16 \pm 0.00}$	82.24 ± 0.13	84.10 ± 0.37	82.97 ± 0.32	67.47±0.23	63.94±0.31	$72.84{\pm}0.49$	65.27±1.74	
PANPool	84.00 ± 0.37	$82.83 {\pm} 0.37$	84.44±0.30	83.44±0.36	$67.63 {\pm} 0.26$	63.85±0.28	73.45±0.86	67.48±1.75	
COPool	83.90±0.12	82.62 ± 0.13	$81.14{\pm}1.72$	80.00 ± 1.01	66.43±0.59	62.93 ± 0.42	$72.80 {\pm} 0.00$	67.14±0.42	
CGIPool	83.21±0.77	82.24 ± 0.82	82.27±0.55	$80.91 {\pm} 0.80$	65.66±1.34	$62.14{\pm}1.46$	72.36 ± 0.46	66.80±0.91	
KMISPool	$84.00 {\pm} 0.18$	82.57±0.15	83.55±0.39	$82.36 {\pm} 0.41$	67.35±0.15	63.69 ± 0.14	72.72 ± 0.30	66.51±0.39	
GSAPool	83.70±0.07	82.19±0.27	83.16±0.32	$81.89 {\pm} 0.37$	67.07±0.49	$63.56 {\pm} 0.42$	$72.84{\pm}0.44$	66.33±0.37	
HGPSLPool	$84.19 {\pm} 0.00$	$82.83 {\pm} 0.04$	$83.46 {\pm} 0.79$	$82.32 {\pm} 0.89$	67.67±0.15	64.13±0.16	73.20 ± 0.46	67.95±0.4	
	MUTAG	_	49	IMDB-MULTI			COLLAN	3	

Table 8: Results of **node classification under distribution shifts**. Degree and closeness denote two types of shifts across training and test datasets.



Figure 3: Comparison of performance, training time, and memory usage across different approaches.

Macro-F1 is generally lower than Micro-F1, which indicates that the model has weaker recognition capabilities for minority classes. *Thirdly*, node clustering pooling exhibits better generalizability than node dropping pooling in graph classification tasks. *Fourthly*, HGPSLPool and PANPool exhibit the best performance, potentially due to the fact that HGPSLPool combines graph convolution with spectral clustering, enabling it to better capture higher-order relationships and local topological structures, which is advantageous in node-level tasks. Meanwhile, PANPool utilizes an adaptive pooling strategy that adjusts the pooling method to suit different node feature distributions, enhancing the model's robustness and generalization capability under out-of-distribution conditions.



Figure 4: The t-SNE visualization w.r.t. different pooling ratios of TopKPool and SAGPool.

4.5 FURTHER ANALYSIS

Efficiency Comparison. In this part, we conduct an efficiency analysis of graph pooling methods
 on the MUTAG, IMDB-MULTI, and COLLAB datasets. We calculate the time of the algorithms by
 measuring the duration needed to complete 200 epochs of training with the 512 batch size. For space
 efficiency, we compute the GPU memory utilization during the training process. From Figure 3, it
 can be observed that ASAPool, DiffPool, MincutPool, and JustBalancePool exhibit significantly
 higher time and space costs. In contrast, node dropping pooling methods such as TopKPool, SAG-







Figure 6: Performance w.r.t. different pooling ratios for four pooling methods.

509 Pool, and KMISPool demonstrate lower time and space costs. The underlying reason is that node 510 clustering pooling methods require converting graph data into an adjacency matrix form and simpli-511 fying the graph through clustering rather than directly removing nodes.

512 Visualization. Figure 4 shows the t-SNE visualization for TopKPool and SAGPool under different 513 pooling ratios. From the results, we observe that as the pooling ratio increases from 0.1 to 0.9, the 514 different classes form more distinct clusters in the t-SNE plot when the pooling ratio is low. As the 515 pooling ratio increases, the model retains more nodes, leading to a greater overlap between nodes of 516 different classes and a reduction in inter-class separability. Moreover, when the pooling ratio is 0.9, 517 SAGPool shows a higher degree of class separability compared to TopKPool.

518 Backbone Analysis. Figure 5 presents the performance of four pooling methods based on GCN-519 Conv (Kipf & Welling, 2016b), GATConv (Veličković et al., 2017), SAGEConv (Hamilton et al., 520 2017), and GraphConv (Morris et al., 2019) on four datasets, NCI1, NCI109, PROTEINS, and 521 PROTEINS_FULL. On average, as the backbone models change, most pooling methods exhibit sig-522 nificant performance fluctuations, and no single backbone model consistently maintains a leading 523 position. Except for the PROTEINS_FULL, the performance of GraphConv is relatively better.

524 Parameter Analysis. Figure 6 shows the performance of four pooling methods on the COX2, AIDS, 525 FRANKENSTEIN, and Mutagenicity datasets. From the results, we observe that as the pooling rate 526 increases from 0.1 to 0.9, the performance increases before reaching saturation in most cases. The 527 performance variation among different pooling methods is significant as the pooling ratio changes, 528 it is necessary to adjust the pooling ratio when employing pooling methods. 529

- 530 5 CONCLUSION
- 531

496

500

501

502

504

505

506 507

508

532 In this paper, we construct the first graph pooling benchmark that includes 17 state-of-the-art ap-533 proaches and 28 different graph datasets across graph classification, graph regression, and node 534 classification. We find that node clustering pooling methods outperform node dropping pooling 535 methods in terms of robustness and generalizability, but at the cost of higher computational ex-536 penses. This benchmark systematically analyzes the effectiveness, robustness, and generalizability 537 of graph pooling methods. We also make our benchmark publically available to advance the fields of graph machine learning and applications. One limitation of our benchmark is the lack of more 538 complicated settings under label scarcity. In future works, we would extend our graph pooling benchmark to more realistic settings such as semi-supervised learning and few-shot learning.

540 REFERENCES

547

553

559

561

577

578

579

580

581

582

583

- Emily Alsentzer, Samuel Finlayson, Michelle Li, and Marinka Zitnik. Subgraph neural networks.
 Advances in Neural Information Processing Systems, 33:8017–8029, 2020.
- Davide Bacciu, Alessio Conte, and Francesco Landolfi. Generalizing downsampling from regular data to graphs. In *Proceedings of the AAAI Conference on Artificial Intelligence*, volume 37, pp. 6718–6727, 2023.
- Jinheon Baek, Minki Kang, and Sung Ju Hwang. Accurate learning of graph representations with graph multiset pooling. *arXiv preprint arXiv:2102.11533*, 2021.
- Beatrice Bevilacqua, Yangze Zhou, and Bruno Ribeiro. Size-invariant graph representations for graph classification extrapolations. In *International Conference on Machine Learning*, pp. 837– 851. PMLR, 2021.
- Smriti Bhagat, Graham Cormode, and S Muthukrishnan. Node classification in social networks.
 Social network data analytics, pp. 115–148, 2011.
- Tian Bian, Xi Xiao, Tingyang Xu, Peilin Zhao, Wenbing Huang, Yu Rong, and Junzhou Huang. Ru mor detection on social media with bi-directional graph convolutional networks. In *Proceedings of the AAAI conference on artificial intelligence*, volume 34, pp. 549–556, 2020.
- Filippo Maria Bianchi. Simplifying clustering with graph neural networks. *arXiv preprint arXiv:2207.08779*, 2022.
- Filippo Maria Bianchi and Veronica Lachi. The expressive power of pooling in graph neural net works. Advances in Neural Information Processing Systems, 36, 2024.
- Filippo Maria Bianchi, Daniele Grattarola, and Cesare Alippi. Spectral clustering with graph neural networks for graph pooling. In *International conference on machine learning*, pp. 874–883.
 PMLR, 2020.
- Karsten M Borgwardt, Cheng Soon Ong, Stefan Schönauer, SVN Vishwanathan, Alex J Smola, and
 Hans-Peter Kriegel. Protein function prediction via graph kernels. *Bioinformatics*, 21(suppl_1):
 i47–i56, 2005.
- 571
 572
 573
 Chen Cai and Yusu Wang. A simple yet effective baseline for non-attributed graph classification. arXiv preprint arXiv:1811.03508, 2018.
- David Camacho, Angel Panizo-LLedot, Gema Bello-Orgaz, Antonio Gonzalez-Pardo, and Erik
 Cambria. The four dimensions of social network analysis: An overview of research methods,
 applications, and software tools. *Information Fusion*, 63:88–120, 2020.
 - Ting Chen, Song Bian, and Yizhou Sun. Are powerful graph neural nets necessary? a dissection on graph classification. *arXiv preprint arXiv:1905.04579*, 2019.
 - Yongqiang Chen, Yonggang Zhang, Yatao Bian, Han Yang, MA Kaili, Binghui Xie, Tongliang Liu, Bo Han, and James Cheng. Learning causally invariant representations for out-of-distribution generalization on graphs. *Advances in Neural Information Processing Systems*, 35:22131–22148, 2022.
- Edward Choi, Zhen Xu, Yujia Li, Michael Dusenberry, Gerardo Flores, Emily Xue, and Andrew Dai.
 Learning the graphical structure of electronic health records with graph convolutional transformer.
 In *Proceedings of the AAAI conference on artificial intelligence*, volume 34, pp. 606–613, 2020.
- Myriam Ciordia, Laura Pérez-Benito, Francisca Delgado, Andrés A Trabanco, and Gary Tresadern.
 Application of free energy perturbation for the design of bace1 inhibitors. *Journal of Chemical information and modeling*, 56(9):1856–1871, 2016.
- Asim Kumar Debnath, Rosa L Lopez de Compadre, Gargi Debnath, Alan J Shusterman, and Corwin Hansch. Structure-activity relationship of mutagenic aromatic and heteroaromatic nitro compounds. correlation with molecular orbital energies and hydrophobicity. *Journal of medicinal chemistry*, 34(2):786–797, 1991.

- 594 Michaël Defferrard, Xavier Bresson, and Pierre Vandergheynst. Convolutional neural networks on 595 graphs with fast localized spectral filtering. Advances in neural information processing systems, 596 29, 2016. 597 John S Delaney. Esol: estimating aqueous solubility directly from molecular structure. Journal of 598 chemical information and computer sciences, 44(3):1000–1005, 2004. 600 Alexandre Duval and Fragkiskos Malliaros. Higher-order clustering and pooling for graph neural 601 networks. In Proceedings of the 31st ACM International Conference on Information & Knowledge 602 Management, pp. 426-435, 2022. 603 Vijay Prakash Dwivedi, Chaitanya K Joshi, Anh Tuan Luu, Thomas Laurent, Yoshua Bengio, and 604 Xavier Bresson. Benchmarking graph neural networks. Journal of Machine Learning Research, 605 24(43):1-48, 2023. 606 607 Federico Errica, Marco Podda, Davide Bacciu, and Alessio Micheli. A fair comparison of graph 608 neural networks for graph classification. arXiv preprint arXiv:1912.09893, 2019. 609 Matthias Fey and Jan E. Lenssen. Fast graph representation learning with PyTorch Geometric. In 610 ICLR Workshop on Representation Learning on Graphs and Manifolds, 2019. 611 612 Hongyang Gao and Shuiwang Ji. Graph u-nets. In international conference on machine learning, 613 pp. 2083–2092. PMLR, 2019. 614 615 Daniele Grattarola, Daniele Zambon, Filippo Maria Bianchi, and Cesare Alippi. Understanding pooling in graph neural networks. IEEE transactions on neural networks and learning systems, 616 2022a. 617 618 Daniele Grattarola, Daniele Zambon, Filippo Maria Bianchi, and Cesare Alippi. Understanding 619 pooling in graph neural networks. *IEEE transactions on neural networks and learning systems*, 620 2022b. 621 622 Shurui Gui, Xiner Li, Limei Wang, and Shuiwang Ji. Good: A graph out-of-distribution benchmark. Advances in Neural Information Processing Systems, 35:2059–2073, 2022. 623 624 Will Hamilton, Zhitao Ying, and Jure Leskovec. Inductive representation learning on large graphs. 625 Advances in neural information processing systems, 30, 2017. 626 627 Jonas Berg Hansen and Filippo Maria Bianchi. Total variation graph neural networks. In International Conference on Machine Learning, pp. 12445–12468. PMLR, 2023. 628 629 Weihua Hu, Matthias Fey, Marinka Zitnik, Yuxiao Dong, Hongyu Ren, Bowen Liu, Michele Catasta, 630 and Jure Leskovec. Open graph benchmark: Datasets for machine learning on graphs. Advances 631 in neural information processing systems, 33:22118–22133, 2020a. 632 633 Weihua Hu, Matthias Fey, Marinka Zitnik, Yuxiao Dong, Hongyu Ren, Bowen Liu, Michele Catasta, and Jure Leskovec. Open graph benchmark: Datasets for machine learning on graphs. Advances 634 in neural information processing systems, 33:22118–22133, 2020b. 635 636 Nabil Ibtehaz and M Sohel Rahman. Multiresunet: Rethinking the u-net architecture for multimodal 637 biomedical image segmentation. Neural networks, 121:74-87, 2020. 638 639 Wei Ju, Siyu Yi, Yifan Wang, Qingqing Long, Junyu Luo, Zhiping Xiao, and Ming Zhang. A survey 640 of data-efficient graph learning, 2024. 641 Thomas N Kipf and Max Welling. Semi-supervised classification with graph convolutional net-642 works. arXiv preprint arXiv:1609.02907, 2016a. 643 644 Thomas N Kipf and Max Welling. Semi-supervised classification with graph convolutional net-645 works. arXiv preprint arXiv:1609.02907, 2016b. 646
- 647 Boris Knyazev, Graham W Taylor, and Mohamed Amer. Understanding attention and generalization in graph neural networks. *Advances in neural information processing systems*, 32, 2019.

648 649	Junhyun Lee, Inyeop Lee, and Jaewoo Kang. Self-attention graph pooling. In <i>International conference on machine learning</i> , pp. 3734–3743. PMLR, 2019.
651 652	Jiaxu Leng, Ying Liu, Tianlin Zhang, Pei Quan, and Zhenyu Cui. Context-aware u-net for biomedical image segmentation. In 2018 IEEE International Conference on Bioinformatics and Biomedicine (BIBM), pp. 2535–2538, IEEE, 2018.
654 655	Tao Li and Jiexiang Wang. Distributed averaging with random network graphs and noises. <i>IEEE Transactions on Information Theory</i> , 64(11):7063–7080, 2018.
657 658 659	Zhixun Li, Xin Sun, Yifan Luo, Yanqiao Zhu, Dingshuo Chen, Yingtao Luo, Xiangxin Zhou, Qiang Liu, Shu Wu, Liang Wang, et al. Gslb: The graph structure learning benchmark. <i>Advances in Neural Information Processing Systems</i> , 36, 2024.
660 661 662	Chuang Liu, Yibing Zhan, Jia Wu, Chang Li, Bo Du, Wenbin Hu, Tongliang Liu, and Dacheng Tao. Graph pooling for graph neural networks: Progress, challenges, and opportunities. <i>arXiv preprint</i> <i>arXiv:2204.07321</i> , 2022a.
663 664 665 666	Chuang Liu, Yibing Zhan, Jia Wu, Chang Li, Bo Du, Wenbin Hu, Tongliang Liu, and Dacheng Tao. Graph pooling for graph neural networks: Progress, challenges, and opportunities. <i>arXiv preprint</i> <i>arXiv:2204.07321</i> , 2022b.
667 668 669	Meng Liu, Hongyang Gao, and Shuiwang Ji. Towards deeper graph neural networks. In <i>Proceedings</i> of the 26th ACM SIGKDD international conference on knowledge discovery & data mining, pp. 338–348, 2020.
670 671 672 673	Nina Lukashina, Alisa Alenicheva, Elizaveta Vlasova, Artem Kondiukov, Aigul Khakimova, Emil Magerramov, Nikita Churikov, and Aleksei Shpilman. Lipophilicity prediction with multitask learning and molecular substructures representation. <i>arXiv preprint arXiv:2011.12117</i> , 2020.
674 675 676	Chen Ma, Liheng Ma, Yingxue Zhang, Jianing Sun, Xue Liu, and Mark Coates. Memory augmented graph neural networks for sequential recommendation. In <i>Proceedings of the AAAI conference on artificial intelligence</i> , volume 34, pp. 5045–5052, 2020a.
677 678 679 680	Zheng Ma, Junyu Xuan, Yu Guang Wang, Ming Li, and Pietro Liò. Path integral based convolution and pooling for graph neural networks. <i>Advances in Neural Information Processing Systems</i> , 33: 16421–16433, 2020b.
681 682	Diego Mesquita, Amauri Souza, and Samuel Kaski. Rethinking pooling in graph neural networks. Advances in Neural Information Processing Systems, 33:2220–2231, 2020.
683 684 685 686	Caitlyn L Mills, Rohan Garg, Joslynn S Lee, Liang Tian, Alexandru Suciu, Gene D Cooperman, Penny J Beuning, and Mary Jo Ondrechen. Functional classification of protein structures by local structure matching in graph representation. <i>Protein Science</i> , 27(6):1125–1135, 2018.
687 688	David L Mobley and J Peter Guthrie. Freesolv: a database of experimental and calculated hydration free energies, with input files. <i>Journal of computer-aided molecular design</i> , 28:711–720, 2014.
689 690 691 692 693	Grégoire Montavon, Matthias Rupp, Vivekanand Gobre, Alvaro Vazquez-Mayagoitia, Katja Hansen, Alexandre Tkatchenko, Klaus-Robert Müller, and O Anatole Von Lilienfeld. Machine learning of molecular electronic properties in chemical compound space. <i>New Journal of Physics</i> , 15(9): 095003, 2013.
694 695 696	Christopher Morris, Martin Ritzert, Matthias Fey, William L Hamilton, Jan Eric Lenssen, Gaurav Rattan, and Martin Grohe. Weisfeiler and leman go neural: Higher-order graph neural networks. In <i>Proceedings of the AAAI conference on artificial intelligence</i> , volume 33, pp. 4602–4609, 2019.
697 698 699 700	Christopher Morris, Nils M Kriege, Franka Bause, Kristian Kersting, Petra Mutzel, and Marion Neumann. Tudataset: A collection of benchmark datasets for learning with graphs. <i>arXiv preprint arXiv:2007.08663</i> , 2020.
700	Ghaith Mqawass and Petr Popov. graphlambda: Fusion graph neural networks for binding affinity prediction. <i>Journal of Chemical Information and Modeling</i> , 2024.

702 703 704	Francesco Orsini, Paolo Frasconi, and Luc De Raedt. Graph invariant kernels. In <i>Twenty-Fourth</i> <i>International Joint Conference on Artificial Intelligence</i> , 2015.
705 706 707	Yunsheng Pang, Yunxiang Zhao, and Dongsheng Li. Graph pooling via coarsened graph infomax. In Proceedings of the 44th International ACM SIGIR Conference on Research and Development in Information Retrieval, pp. 2177–2181, 2021.
708 709 710	Adam Paszke, Sam Gross, Francisco Massa, Adam Lerer, James Bradbury, Gregory Chanan, Trevor Killeen, Zeming Lin, Natalia Gimelshein, Luca Antiga, et al. Pytorch: An imperative style, high-performance deep learning library. <i>Advances in neural information processing systems</i> , 32, 2019.
711 712 713	Hongbin Pei, Bingzhe Wei, Kevin Chen-Chuan Chang, Yu Lei, and Bo Yang. Geom-gcn: Geometric graph convolutional networks. <i>arXiv preprint arXiv:2002.05287</i> , 2020.
714 715 716	Bryan Perozzi, Rami Al-Rfou, and Steven Skiena. Deepwalk: Online learning of social repre- sentations. In <i>Proceedings of the 20th ACM SIGKDD international conference on Knowledge</i> <i>discovery and data mining</i> , pp. 701–710, 2014.
717 718 719	Lianke Qin, Zhao Song, and Baocheng Sun. Is solving graph neural tangent kernel equivalent to training graph neural network? <i>arXiv preprint arXiv:2309.07452</i> , 2023.
720 721 722	Ekagra Ranjan, Soumya Sanyal, and Partha Talukdar. Asap: Adaptive structure aware pooling for learning hierarchical graph representations. In <i>Proceedings of the AAAI conference on artificial intelligence</i> , volume 34, pp. 5470–5477, 2020.
723 724 725 726 727	Kaspar Riesen and Horst Bunke. Iam graph database repository for graph based pattern recognition and machine learning. In <i>Structural, Syntactic, and Statistical Pattern Recognition: Joint IAPR</i> <i>International Workshop, SSPR & SPR 2008, Orlando, USA, December 4-6, 2008. Proceedings</i> , pp. 287–297. Springer, 2008.
728 729 730 731	Olaf Ronneberger, Philipp Fischer, and Thomas Brox. U-net: Convolutional networks for biomed- ical image segmentation. In <i>Medical image computing and computer-assisted intervention–</i> <i>MICCAI 2015: 18th international conference, Munich, Germany, October 5-9, 2015, proceed-</i> <i>ings, part III 18</i> , pp. 234–241. Springer, 2015.
732 733 734	Benedek Rozemberczki, Carl Allen, and Rik Sarkar. Multi-scale attributed node embedding. <i>Journal of Complex Networks</i> , 9(2):cnab014, 2021.
735 736 737	Ida Schomburg, Antje Chang, Christian Ebeling, Marion Gremse, Christian Heldt, Gregor Huhn, and Dietmar Schomburg. Brenda, the enzyme database: updates and major new developments. <i>Nucleic acids research</i> , 32(suppl_1):D431–D433, 2004.
738 739 740	Nino Shervashidze, Pascal Schweitzer, Erik Jan Van Leeuwen, Kurt Mehlhorn, and Karsten M Borg- wardt. Weisfeiler-lehman graph kernels. <i>Journal of Machine Learning Research</i> , 12(9), 2011.
741 742 743	Nahian Siddique, Sidike Paheding, Colin P Elkin, and Vijay Devabhaktuni. U-net and its variants for medical image segmentation: A review of theory and applications. <i>Ieee Access</i> , 9:82031–82057, 2021.
744 745 746	Yunchong Song, Siyuan Huang, Xinbing Wang, Chenghu Zhou, and Zhouhan Lin. Graph parsing networks. <i>arXiv preprint arXiv:2402.14393</i> , 2024.
747 748 749	Mengzhu Sun, Xi Zhang, Jiaqi Zheng, and Guixiang Ma. Ddgcn: Dual dynamic graph convolutional networks for rumor detection on social media. In <i>Proceedings of the AAAI conference on artificial intelligence</i> , volume 36, pp. 4611–4619, 2022.
750 751 752 752	Jeffrey J Sutherland, Lee A O'brien, and Donald F Weaver. Spline-fitting with a genetic algorithm: A method for developing classification structure- activity relationships. <i>Journal of chemical in- formation and computer sciences</i> , 43(6):1906–1915, 2003.
754 755	Cheng Tan, Siyuan Li, Zhangyang Gao, Wenfei Guan, Zedong Wang, Zicheng Liu, Lirong Wu, and Stan Z Li. Openstl: A comprehensive benchmark of spatio-temporal predictive learning. <i>Advances in Neural Information Processing Systems</i> , 36:69819–69831, 2023.

756 757 758	Anton Tsitsulin, John Palowitch, Bryan Perozzi, and Emmanuel Müller. Graph clustering with graph neural networks. <i>Journal of Machine Learning Research</i> , 24(127):1–21, 2023a.
759 760	Anton Tsitsulin, John Palowitch, Bryan Perozzi, and Emmanuel Müller. Graph clustering with graph neural networks. <i>Journal of Machine Learning Research</i> , 24(127):1–21, 2023b.
761 762 763	Petar Veličković, Guillem Cucurull, Arantxa Casanova, Adriana Romero, Pietro Lio, and Yoshua Bengio. Graph attention networks. <i>arXiv preprint arXiv:1710.10903</i> , 2017.
764 765	Petar Veličković, William Fedus, William L Hamilton, Pietro Liò, Yoshua Bengio, and R Devon Hjelm. Deep graph infomax. <i>arXiv preprint arXiv:1809.10341</i> , 2018.
767 768	Nikil Wale, Ian A Watson, and George Karypis. Comparison of descriptor spaces for chemical compound retrieval and classification. <i>Knowledge and Information Systems</i> , 14:347–375, 2008.
769 770 771	Duncan J Watts and Steven H Strogatz. Collective dynamics of 'small-world'networks. <i>nature</i> , 393 (6684):440–442, 1998.
772 773 774	Oliver Wieder, Stefan Kohlbacher, Mélaine Kuenemann, Arthur Garon, Pierre Ducrot, Thomas Sei- del, and Thierry Langer. A compact review of molecular property prediction with graph neural networks. <i>Drug Discovery Today: Technologies</i> , 37:1–12, 2020.
775 776 777	Junran Wu, Xueyuan Chen, Ke Xu, and Shangzhe Li. Structural entropy guided graph hierarchical pooling. In <i>International conference on machine learning</i> , pp. 24017–24030. PMLR, 2022a.
778 779 780	Lingfei Wu, Peng Cui, Jian Pei, Liang Zhao, and Xiaojie Guo. Graph neural networks: foundation, frontiers and applications. In <i>Proceedings of the 28th ACM SIGKDD Conference on Knowledge Discovery and Data Mining</i> , pp. 4840–4841, 2022b.
781 782 783 784	Yongji Wu, Defu Lian, Yiheng Xu, Le Wu, and Enhong Chen. Graph convolutional networks with markov random field reasoning for social spammer detection. In <i>Proceedings of the AAAI conference on artificial intelligence</i> , volume 34, pp. 1054–1061, 2020a.
785 786 787	Zhenqin Wu, Bharath Ramsundar, Evan N Feinberg, Joseph Gomes, Caleb Geniesse, Aneesh S Pappu, Karl Leswing, and Vijay Pande. Moleculenet: a benchmark for molecular machine learning. <i>Chemical science</i> , 9(2):513–530, 2018.
788 789 790 791	Zonghan Wu, Shirui Pan, Fengwen Chen, Guodong Long, Chengqi Zhang, and S Yu Philip. A comprehensive survey on graph neural networks. <i>IEEE transactions on neural networks and learning systems</i> , 32(1):4–24, 2020b.
792 793	Shunxin Xiao, Shiping Wang, Yuanfei Dai, and Wenzhong Guo. Graph neural networks in node classification: survey and evaluation. <i>Machine Vision and Applications</i> , 33(1):4, 2022.
794 795 796 797	Fanding Xu, Zhiwei Yang, Lizhuo Wang, Deyu Meng, and Jiangang Long. Mespool: Molecular edge shrinkage pooling for hierarchical molecular representation learning and property prediction. <i>Briefings in Bioinformatics</i> , 25(1):bbad423, 2024a.
798 799 800 801	Fanding Xu, Zhiwei Yang, Lizhuo Wang, Deyu Meng, and Jiangang Long. Mespool: Molecular edge shrinkage pooling for hierarchical molecular representation learning and property prediction. <i>Briefings in Bioinformatics</i> , 25(1):bbad423, 2024b.
802 803 804 805	Liangwei Yang, Zhiwei Liu, Yingtong Dou, Jing Ma, and Philip S Yu. Consistec: Enhancing gnn for social recommendation via consistent neighbor aggregation. In <i>Proceedings of the 44th international ACM SIGIR conference on Research and development in information retrieval</i> , pp. 2141–2145, 2021.
806 807 808	Zhilin Yang, William Cohen, and Ruslan Salakhudinov. Revisiting semi-supervised learning with graph embeddings. In <i>International conference on machine learning</i> , pp. 40–48. PMLR, 2016.
000	Zi Ye Yogan Java Kumar Gob Ong Sing Fengyan Song and Junsong Wang. A comprehensive

- Zhitao Ying, Jiaxuan You, Christopher Morris, Xiang Ren, Will Hamilton, and Jure Leskovec. Hierarchical graph representation learning with differentiable pooling. *Advances in neural information processing systems*, 31, 2018a.
- Zhitao Ying, Jiaxuan You, Christopher Morris, Xiang Ren, Will Hamilton, and Jure Leskovec. Hier archical graph representation learning with differentiable pooling. *Advances in neural information processing systems*, 31, 2018b.
- Jianke Yu, Hanchen Wang, Xiaoyang Wang, Zhao Li, Lu Qin, Wenjie Zhang, Jian Liao, and Ying
 Zhang. Group-based fraud detection network on e-commerce platforms. In *Proceedings of the*29th ACM SIGKDD Conference on Knowledge Discovery and Data Mining, pp. 5463–5475,
 2023.
- Kaiwei Zhang, Junchi Yu, Haichao Shi, Jian Liang, and Xiao-Yu Zhang. Rumor detection with diverse counterfactual evidence. In *Proceedings of the 29th ACM SIGKDD Conference on Knowledge Discovery and Data Mining*, pp. 3321–3331, 2023.
- Liang Zhang, Xudong Wang, Hongsheng Li, Guangming Zhu, Peiyi Shen, Ping Li, Xiaoyuan Lu,
 Syed Afaq Ali Shah, and Mohammed Bennamoun. Structure-feature based graph self-adaptive
 pooling. In *Proceedings of The Web Conference 2020*, pp. 3098–3104, 2020a.
- Yanfu Zhang, Hongchang Gao, Jian Pei, and Heng Huang. Robust self-supervised structural graph neural network for social network prediction. In *Proceedings of the ACM Web Conference 2022*, pp. 1352–1361, 2022.
- Zhen Zhang, Jiajun Bu, Martin Ester, Jianfeng Zhang, Chengwei Yao, Zhi Yu, and Can Wang.
 Hierarchical graph pooling with structure learning. *arXiv preprint arXiv:1911.05954*, 2019.
- Zhen Zhang, Fan Wu, and Wee Sun Lee. Factor graph neural networks. *Advances in Neural Information Processing Systems*, 33:8577–8587, 2020b.
- Zhen Zhang, Jiajun Bu, Martin Ester, Jianfeng Zhang, Zhao Li, Chengwei Yao, Huifen Dai, Zhi Yu, and Can Wang. Hierarchical multi-view graph pooling with structure learning. *IEEE Transactions on Knowledge and Data Engineering*, 35(1):545–559, 2021.
- Xiaowei Zhou, Jie Yin, and Ivor W Tsang. Edge but not least: Cross-view graph pooling. In
 Joint European Conference on Machine Learning and Knowledge Discovery in Databases, pp. 344–359. Springer, 2022.

865 866

867 868

869

A RELATED WORK

APPENDIX

A.1 GRAPH CLASSIFICATION AND GRAPH REGRESSION

870 Graphs provide an effective tool to represent interaction among different objects (Wu et al., 2020b). 871 Graph classification (Baek et al., 2021) is a fundamental graph machine learning problem, which 872 aims to classify each graph into its corresponding category. The majority of current works adopt 873 message passing mechanisms (Wu et al., 2020b), where each node receives information from its 874 neighbors in a recursive manner. Then, a graph readout function is adopted to summarize all node 875 representations into a graph-level representation for downstream classification. Graph classification has extensive applications in various domains such as molecular property prediction (Wieder et al., 876 2020) and protein function analysis (Mills et al., 2018). Graph regression (Qin et al., 2023) is close 877 to graph classification which maps graph-level data into continuous vectors. Researchers usually 878 utilize graph regression to formulate molecular property predictions (Mgawass & Popov, 2024). 879 Graph pooling has been an important topic in graph-level tasks (Knyazev et al., 2019; Lee et al., 880 2019; Ranjan et al., 2020; Ma et al., 2020b; Zhou et al., 2022; Pang et al., 2021; Bacciu et al., 2023; 881 Zhang et al., 2020a; 2019; Hansen & Bianchi, 2023; Ying et al., 2018a; Bianchi et al., 2020; Tsitsulin 882 et al., 2023a; Duval & Malliaros, 2022; Bianchi, 2022), which generally utilize a hierarchical way 883 to refine the graph structures (Bianchi & Lachi, 2024; Liu et al., 2022b). In this work, we generally 884 study the performance of graph pooling on graph-level tasks and validate the effectiveness of graph 885 pooling approaches in most cases.

886 887

A.2 NODE CLASSIFICATION

889 Node classification aims to classify each node in a graph based on its attributes and relationship with the other nodes (Xiao et al., 2022; Ju et al., 2024). Node classification has various applications in the 890 real world, including social network analysis (Camacho et al., 2020), knowledge graphs (Ye et al., 891 2022), bioinformatics (Bhagat et al., 2011) and online commerce services (Yu et al., 2023). Graph 892 neural networks have been widely utilized to solve the problem by learning semantics information 893 across nodes by neighborhood propagation. Since graph pooling would reduce the number of nodes, 894 recent works utilize a U-Net architecture (Gao & Ji, 2019), which involves down-sampling and 895 up-sampling with residue connections. In this work, we systematically evaluate the performance 896 of graph pooling on node classification and observe that graph pooling has limited improvement 897 compared with basic graph neural network architectures. 898

899 900

A.3 PREVIOUS BENCHMARK RESEARCH

901 Previous studies have built benchmark for graph-related tasks (Errica et al., 2019; Hu et al., 2020b). 902 In particular, Errica et al. (2019) is a benchmark including six different GNN models across nine 903 commonly used TUDataset datasets. Open Graph Benchmark (OGB) (Hu et al., 2020b) evaluate dif-904 fernet graph neural network approaches experiments on graph classification, graph regression, and node classification. Errica et al. (2019) only involve one graph pooling method and Hu et al. (2020b) 905 does not involve any graph pooling methods. In comparison, our method focuses on graph pooling 906 techniques rather than graph neural networks. Moroever, our benchmark explores the robustness of 907 these methods by introducing noise attacks in both graph classification and node classification tasks 908 and investigate their generalizability through out-of-distribution shifts. 909

- 910
- 911 912

B DETAILS OF U-NET BASED NODE CLASSIFICATION

Most existing studies that combine node classification with pooling have utilized the U-Net architecture (Wu et al., 2022a; Song et al., 2024; Zhang et al., 2021). Figure A.1 shows the overview
of the U-Net framework. Pooling plays a crucial role in the U-Net structure, as it progressively reduces the graph size in the downsampling path to extract important global features while preserving
essential local information. In the upsampling path, pooling facilitates the fusion of features from
the downsampling path with those being progressively recovered in the upsampling path through

922 923 924

925

926 927

928

929 930 931

932 933

948 949

950 951

952



Figure A.1: Overview of the graph U-Net framework for node classification.

skip connections, thereby assisting the model in accurately performing graph node classification or
other tasks. Pooling not only simplifies the graph's complexity but also provides the model with
multi-scale feature representation capabilities.

937 In the downsampling path, the input feature matrix is first subjected to graph convolution, where the 938 product of the adjacency matrix and the feature matrix, along with the weighted sum of the weight 939 matrix and the bias term, yields the activated feature matrix $\mathbf{H}^{(l+1)}$. Next, a pooling operation is 940 applied, reducing the number of nodes by selecting those with higher scores, thereby transforming 941 the original feature matrix ($\mathbf{H}^{(l+1)}$ and adjacency matrix $\mathbf{A}^{(l)}$ into a smaller feature matrix $\mathbf{H'}^{(l+1)}$ and a corresponding adjacency matrix $A^{\prime(l+1)}$. In the upsampling path, the pooled feature matrix 942 943 $\mathbf{H}^{(l+1)}$ is first upsampled to restore the original number of nodes, generating a new feature matrix 944 $\mathbf{H}^{\prime\prime(l+1)}$. Then, the restored feature matrix is concatenated with the corresponding feature matrix 945 $\mathbf{H}^{(l)}$ from the downsampling path, forming the merged feature matrix $\mathbf{H}_{merged}^{(l+1)}$. Finally, the merged 946 feature matrix undergoes another graph convolution, resulting in the output feature matrix $\mathbf{H}^{(l+2)}$. 947

C DETAILS OF SELECTED POOLING METHODS

C.1 NODE DROPPING POOLING

TopKPool (Knyazev et al., 2019). TopKPool utilizes the attention mechanism to learn the scores of
 different nodes and then selects the nodes with top scores, which can learn important local portions
 from original graphs.

- SAGPool (Lee et al., 2019). SAGPool utilizes a different graph neural network to learn importance
 scores, which can guide the pooling process effectively.
- ASAPool (Ranjan et al., 2020). ASAPool considers the neighboring subgraphs to represent nodes and then adopts the attention mechanism to generate subgraph representations. The importance nodes are selected by a graph neural networks with local extremum information.
- PANPool (Ma et al., 2020b). PANPool constructs the maximal entropy transition (MET) matrix
 based on graph Laplacian, which can generate importance scores for different nodes.
- 964
 965
 966
 967
 968
 968
 969
 969
 969
 960
 960
 961
 962
 963
 964
 964
 965
 964
 965
 966
 966
 966
 966
 967
 968
 968
 969
 969
 969
 960
 960
 960
 960
 960
 961
 962
 962
 963
 964
 964
 964
 964
 965
 964
 965
 966
 966
 967
 968
 968
 969
 969
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
 960
- 967
 968
 969
 969
 969
 970
 961
 962
 963
 964
 965
 965
 966
 966
 967
 968
 969
 969
 970
 970
 970
 970
 970
 971
 971
 972
 972
 973
 974
 974
 975
 975
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
 976
- **KMISPool** (Bacciu et al., 2023). KMISPool incorporates the Maximal k-Independent Sets (k-MIS) into graph pooling, which can detect the important nodes in the graph with topological preserved.

GSAPool (Zhang et al., 2020a). GSAPool integrates both structural and attribute information in different components. These scores from different components are then fused to guide the graph pooling process.

HGPSLPool (Zhang et al., 2019). HGPSLPool not only utilizes graph pooling to determine important nodes from the original graph, but also leverages graph structure learning to explore the topological information in the pooled graph.

979 980

981

C.2 NODE CLUSTERING POOLING

 AsymCheegerCutPool (Hansen & Bianchi, 2023). AsymCheegerCutPool conducts graph clustering to generate the assignment of each node according to graph total variation (GTV). Each cluster is aggregated in a hierarchical manner during graph pooling.

DiffPool (Ying et al., 2018a). DiffPool introduces a learnable soft assignment of each node during
 graph clustering, and then maps each cluster into the coarsened nodes in the pooling graph.

MincutPool (Bianchi et al., 2020). MincutPool relaxes the classic normalized mincut problem into a continuous fashion, and then optimizes a graph neural network to achieve this. The graph clustering results are adopted to guide the graph pooling process.

DMoNPool (Tsitsulin et al., 2023a). DMoNPool introduces an objective based on modularity for
 graph clustering and then adds a regularization term to avoid trivial solutions during optimization.
 Similarly, graph clustering results are leveraged for graph pooling.

HoscPool (Duval & Malliaros, 2022). HoscPool combines higher-order relationships in the graph
 with graph pooling based on motif conductance. It minimizes a relaxed motif spectral clustering
 objective and involves multiple motifs to learn hierarchical semantics.

JustBalancePool (Bianchi, 2022). JustBalancePool consists of two components. On the one hand, it aims to reduce the local quadratic variation during graph clustering. On the other hand, it involves a balanced term to reduce the risk of degenerate solutions.

SEPool (Wu et al., 2022a). SEPool generates a clustering assignment matrix in one go through a global optimization algorithm, avoiding the suboptimality associated with layer-by-layer pooling.

ParsPool (Song et al., 2024). ParsPool is characterized by the introduction of a graph parsing algorithm that adaptively learns a personalized pooling structure for each graph. ParsPool is inspired by bottom-up grammar induction and can generate a flexible pooling tree structure for each graph.

1006

1008

D DETAILED DESCRIPTION OF DATASETS

1009 D.1 GRAPH CLASSIFICATION

Table A.1 provides descriptive statistics of the selected datasets, revealing that our chosen datasets encompass graph data of varying scales and features. This diversity establishes a robust foundation for benchmarking. The following are detailed descriptions of these datasets:

Ogbg-molpcba comprises a collection of 437,929 molecules, each represented as a graph where nodes are atoms and edges indicate chemical bonds between atoms. Each node is associated with features such as atom type, valence, and charge. The dataset involves 128 biological activity labels, each representing a binary classification task that indicates whether a molecule exhibits a specific biological activity (Hu et al., 2020b).

PROTEINS represents protein structures; nodes denote secondary structure elements (SSEs) and the edges indicate the relationships between these SSEs that are in close proximity. The primary goal of this dataset is to assist in the classification of proteins into different structural classes based on their amino acid sequences and structure— structural characteristics. Each graph's label is the protein class, so the dataset covers diverse protein structures (Borgwardt et al., 2005).

PROTEINS_FULL is an extended version of PROTEINS. Each graph directly represents a protein structure: nodes correspond to SSEs like alpha helices and beta sheets (Borgwardt et al., 2005).

NCI1 is a collection of chemical compound graphs. Originating from the National Cancer Institute (NCI) database, each graph sample is a compound in which nodes represent atoms and edges represent the bonds between them. The dataset is binary-class labeled, indicating biological activity via compounds' anti-cancer activity against specific cell lines (Wale et al., 2008).

NCI109 is also a collection of chemical compound graphs derived from NCI. Similarly, each node in the graph denotes an atom and each edge denotes a bond. The two classes in NCI109 are about compounds' ability to inhibit or interact with the specified cancer cell line (Wale et al., 2008).

MUTAG consists of 188 chemical molecule graphs, where each node represents an atom. The nodes have different atomic types, such as carbon, nitrogen, oxygen, etc. Edges represent chemical bonds between atoms, such as single or double bonds, indicating their connections in the molecule. The objective is to predict whether each molecule is mutagenic, with positive labels indicating mutagenic molecules and negative labels indicating non-mutagenic molecules (Morris et al., 2020).

1039 D&D is a dataset of protein structure graphs for graph classification. Each graph in this dataset
 represents a protein, with nodes corresponding to amino acids and edges corresponding to the spatial
 or sequential proximity between these amino acids. The primary objective of the D&D dataset is to
 classify proteins into one of two categories: enzymes or non-enzymes (Shervashidze et al., 2011).

1043 IMDB-B is a collection of social network graphs derived from the Internet Movie Database (IMDB).
1044 Each graph is about a collaboration network from movies whereby nodes stand for actors or actresses and edges indicate that the two actors appeared in the same movie — this dataset comprises two classes reflecting the movie genres (Cai & Wang, 2018).

IMDB-M, similar to IMDB-B, represents each movie as a graph where the nodes represent actors and the edges represent co-appearances of actors in the same movie. However, the nodes in IMDB-M are categorized into three classes, and it includes a larger number of actors (Cai & Wang, 2018).

COLLAB consists of 5,000 graphs, each representing a collaboration network of a group of authors in different research fields. In each graph, nodes represent authors, and edges represent collaborations between authors, indicating that the connected authors have co-authored at least one paper. The graphs have three classes, each corresponding to an academic research field. (Morris et al., 2020).

1054 1055 1056 1057 COX2 consists of 467 graphs, where each graph corresponds to a molecule. The nodes represent atoms, and the edges represent chemical bonds, and the graph label indicates whether the molecule is a COX-2 inhibitor (Sutherland et al., 2003).

AIDS consists of 2,000 graphs. Each graph corresponds to a molecule, where the nodes represent individual atoms and the edges represent chemical bonds between these atoms. The goal is to predict the inhibitory effect of molecules on HIV based on their structure. (Riesen & Bunke, 2008).

FRANKENSTEIN consists of 4,337 graphs. Each graph in this dataset represents a chemical compound, where the nodes correspond to atoms, and the edges represent the bonds between them. The graph labels indicate whether the molecule is considered an active compound (Orsini et al., 2015).

Mutagenicity contains 4,337 molecular graphs. In Mutagenicity, each graph represents a molecule, where the nodes are atoms and the edges denote chemical bonds between the nodes. The classification goal is to predict whether a molecule is mutagenic or not (Debnath et al., 1991).

1067 1068

1069 D.2 GRAPH REGRESSION

1070

Table A.2 provides an overview of the selected datasets in terms of their tasks, compounds and their features, recommended splits, and metrics. A more detailed description is provided below.

QM7 and QM8 are benchmark datasets in computational chemistry, designed to facilitate the development and evaluation of machine learning approaches for quantum mechanical property prediction. It contains approximately 7,165 (QM7) and 21,786 (QM8) molecular structures, each characterized by their calculated properties using quantum chemistry methods, specifically focusing on electronic spectra (Wu et al., 2018; Montavon et al., 2013).

BACE is a collection of biochemical data used to evaluate computational methods for drug discovery. The dataset includes a total of 1,522 compounds, each annotated with their binding affinities,

Datasets	Graphs	Classes	Avg. Nodes	Avg. Edges	Node Attr.	Avg. Diameter	Avg. Degree	Avg. CC
Ogbg-molpcba	437,929	2*128	26.00	27.50	-	12.00	2.20	0.00
PROTEINS	1,113	2	39.06	72.82	+(1)	11.14	3.73	0.51
PROTEINS_full	1,113	2	39.06	72.82	+ (29)	11.14	3.73	0.51
NCI1	4,110	2	29.87	32.30	-	11.45	2.16	0.00
NCI109	4,127	2	29.68	32.13	-	11.21	2.16	0.00
MUTAG	188	2	17.90	39.60	+(7)	8.22	2.19	0.00
D&D	1,178	2	284.32	715.66	-	16.45	4.92	0.48
IMDB-B	1,000	2	19.77	96.53	-	1.86	8.89	0.95
IMDB-M	1,500	3	13.00	65.94	-	1.47	8.10	0.97
COLLAB	5,000	3	74.49	2457.22	-	1.86	37.36	0.89
COX2	467	2	41.22	43.45	+ (3)	13.79	2.11	0.00
AIDS	2,000	2	15.69	16.20	+ (4)	6.56	2.01	0.01
FRANKENSTEIN	4,337	2	16.90	17.88	+ (780)	7.86	2.06	0.01
Mutagenicity	4,337	2	30.32	30.77	-	9.10	2.04	0.00

1080 Table A.1: Summary statistics of datasets for graph classification. CC denotes the clustering coef-1081 ficient, and Diameter representing the maximum value of the shortest path between any two nodes 1082

Table A.2: Details of datasets for graph regression.

Datasets	Tasks	Compounds	Split	Avg. Nodes	Avg. Edges	Avg. Diameter	Avg. Degree	Avg. CC
QM7	1	7,165	Scaffold	6.79	6.44	4.21	1.89	0.06
QM8	12	21,786	Random	7.77	8.09	4.35	2.08	0.09
BACE	1	1,522	Scaffold	34.09	36.86	4.35	2.08	0.01
ESOL	1	1,128	Random	13.30	13.69	7.02	1.98	0.00
FreeSolv	1	643	Random	8.76	8.43	5.06	1.84	0.00
Lipophilicity	1	4,200	Random	27.04	29.50	13.85	2.18	0.00

1106

as well as molecular descriptors and fingerprints to facilitate the development and assessment of 1107 machine learning modelsa (Wu et al., 2018; Ciordia et al., 2016). 1108

ESOL is a prominent resource in cheminformatics, designed for evaluating machine learning models 1109 on the prediction of aqueous solubility of small molecules. The dataset, derived from the work 1110 of Delaney, encompasses a diverse range of chemical compounds with experimentally determined 1111 solubility values expressed in logS, where S is the solubility in mols per liter. It includes 1128 1112 compounds, serving as a benchmark for solubility prediction tasks (Delaney, 2004; Wu et al., 2018). 1113

1114 **FreeSolv** is a dataset containing hydration-free energies for small molecules in an aqueous solution. It comprises data for a wide range of organic molecules, providing both experimental values and 1115 calculated predictions based on molecular simulations (Mobley & Guthrie, 2014; Wu et al., 2018). 1116

1117 Lipophilicity is primarily utilized for studying and evaluating molecular lipophilicity. This dataset 1118 comprises 4,200 compounds sourced from the ChEMBL database, with experimentally measured partition coefficient (logD) values that reflect the distribution behavior of compounds in a water-1119 octanol system (Lukashina et al., 2020; Wu et al., 2018). 1120

1121

1122 D.3 NODE CLASSIFICATION 1123

1124 Table A.3 presents descriptive statistics of the seven datasets used for node classification. It is evi-1125 dent that there is a significant variance in the scale of the selected datasets, each possessing distinct 1126 characteristics. Further background information and details about these datasets are provided below. 1127

Ogbn-arxiv comprises a collection of 169,343 scientific publications classified into 40 distinct cat-1128 egories. Each paper is represented by a node with a 128-dimensional feature, which comes from 1129 the average of word embeddings in the corresponding title and abstract. Edges indicate citation 1130 relationships between papers (Hu et al., 2020b). 1131

Cora comprises a collection of 2,708 scientific publications classified into seven distinct categories. 1132 Each publication in the dataset is represented as a node in a citation network, where edges indicate 1133 citation relationships between papers (Yang et al., 2016).

-1	4	0	л
5	1	J	4

Table A.3: Summary statistics of datasets for **node classification**.

Datasets	Number of Nodes	Number of Edges	Number of Features	Number of Classes	Diameter	Avg. Degree	Avg. CC
Ogbn-arxiv	169,343	1,166,243	128	40	23	13.72	0.23
Cora	2,708	10,556	1,433	7	NA	3.90	0.24
CiteSeer	3,327	9,104	3,703	6	NA	2.74	0.14
PubMed	19,717	88,648	500	3	18	4.50	0.06
Cornell	183	298	1,703	5	8	3.06	0.17
Texas	183	325	1,703	5	8	3.22	0.20
Wisconsin	251	515	1,703	5	8	3.71	0.21
Github	37,700	578,006	0	2	7	15.33	0.01

¹¹⁴²

CiteSeer is a widely used citation network dataset. It comprises scientific publications categorized
 into six classes, with each publication represented by a 3,327-dimensional binary vector recording
 the presence or absence of specific words (Yang et al., 2016).

PubMed consists of scientific publications from the PubMed database, categorized into three classes
based on their Medical Subject Headings (MeSH) terms. Each node has a sparse bag-of-words
vector derived from the content of the corresponding publication (Yang et al., 2016).

Cornell, Texas, and Wisconsin are made up of nodes that represent web pages and edges which denote hyperlinks between these pages. Each node has a class which denotes the topic of the web page; this allows tasks including node classification and link prediction to be performed. The datasets differ in size: Cornell and Texas each have 183 nodes while Wisconsin has 251 nodes (Pei et al., 2020).

Github includes node attributes representing the features of developers, such as their interests, skills, and contributions to various repositories. The edges within the network capture the interactions and collaborations of developers, creating a multi-faceted graph structure (Rozemberczki et al., 2021).

1158

1159 D.4 OUT-OF-DISTRIBUTION SHIFTS

Size shifts. For the selected datasets, including NCI1, D&D, NCI109, and IMDB-B, we utilized the data provided by the authors of size-invariant-GNNs (Bevilacqua et al., 2021). In this setup, the graphs with the smallest 50% of nodes are used as the training set, those with the largest 20% of nodes are used as the test set, and the remaining graphs were used as the validation set. The data can be downloaded from https://www.dropbox.com/s/38eg3twe4dd1hbt/data.zip.

Density shifts. For the selected datasets, we divide the datasets based on graph density: the 50% of graphs with the lowest density are used as the training set, the 20% with the highest density are used as the test set, and the remaining graphs are used as the validation set. After applying density shifts, the following densities are observed: for D&D, the training set density is 0.0274, the validation set density is 0.0536, the test set density is 0.1142; for NCI1, the training set density is 0.1229, the validation set density is 0.1920, the test set density is 0.2786; for NCI109, the training set density is 0.1248, the validation set density is 0.1943, the test set density is 0.2770; for IMDB-B, the training set density is 0.6574, the validation set density is 1.1074, the test set density is 1.7427.

1173 **Degree shifts.** For the selected datasets, we divide the datasets based on node degree: the 50%1174 of nodes with the highest degree are used as the training set, the 25% with the lowest degree are 1175 used as the test set, and the remaining nodes are used as the validation set. After applying degree 1176 shifts, we can observe that: for Cora, the training set average degree is 5.9431, the validation set 1177 average degree is 2.4225, and the test set average degree is 1.2836; for Citeseer, the training set 1178 average degree is 4.3313, the validation set average degree is 1.3430, and the test set average degree is 0.9424; for Pubmed, the training set average degree is 7.9148, the validation set average degree 1179 is 1.1552, and the test set average degree is 1.0000; for Cornell, the training set average degree is 1180 3.2198, the validation set average degree is 0.1111, and the test set average degree is 0.0000; for 1181 Texas, the training set average degree is 3.3626, the validation set average degree is 0.4222, and 1182 the test set average degree is 0.0000; for Wisconsin, the training set average degree is 3.7600, the 1183 validation set average degree is 0.7258, and the test set average degree is 0.0000. 1184

Closeness shifts. For the selected datasets, we divide the datasets based on node closeness: the 50% of nodes with the lowest closeness are used as the training set, the 25% with the highest closeness are used as the test set, the remaining nodes used as the validation set. After applying closeness shifts, we can observe that: for Cora, the training set average closeness is 0.1076, the validation set average

Methods		Hyperparameter space
Node Dropping Pooling		
TopKPool	NIPS'19	Pooling ratio: 0.1, 0.3, 0.5, 0.7, 0.9
SAGPool	ICML'19	Pooling ratio: 0.1, 0.3, 0.5, 0.7, 0.9
ASAPool	AAAI'20	Pooling ratio: 0.1, 0.3, 0.5, 0.7, 0.9
PANPool	NIPS'20	Pooling ratio: 0.1, 0.3, 0.5, 0.7, 0.9
COPool	ECMLPKDD'22	Pooling ratio: 0.1, 0.3, 0.5, 0.7, 0.9; K: 1, 2, 3
CGIPool	SIGIR'22	Pooling ratio: 0.1, 0.3, 0.5, 0.7, 0.9
KMISPool	AAAI'23	The independent sets K : 1, 2, 3, 4, 5
GSAPool	WWW'20	Pooling ratio: 0.1, 0.3, 0.5, 0.7, 0.9; Alpha: 0.2, 0.4, 0.6, 0.8
HGPSLPool	Arxiv'19	Pooling ratio: 0.1, 0.3, 0.5, 0.7, 0.9
ParsPool	ICLR'24	Parsingnet layers: 1, 2, 3; Deepsets layers: 1, 2, 3
Node Clustering Pooling	2	
AsymCheegerCutPool	ICML'23	MLP layers: 1, 2; MLP hidden channels: 64, 128, 256
DiffPool	NIPS'18	Not applicable
MincutPool	ICML'20	Temperature: 1, 1.5, 1.8, 2.0
DMoNPool	JMLR'23	Clusters: 2, 4, 6, 8, 10, 12
HoscPool	CIKM'22	Mu: 0.2, 0.5, 0.8; Alpha: 0.2, 0.5, 0.8
JustBalancePool	Arxiv'22	Not applicable
SEPool	ICML'22	Tree depth: 1, 2, 3; Number of blocks: 1, 2, 3, 4

Table A.4: Details of hyperparameter tuning for different pooling methods

closeness is 0.1560, the test set average closeness is 0.1786; for Citeseer, the training set average closeness is 0.0679, the test set average closeness is 0.0832; for Pubmed, the training set average closeness is 0.1448, the validation set average closeness is 0.1669, the test set average closeness is 0.1850; for Cornell, the training set average closeness is 0.2690, the validation set average closeness is 0.2899, the validation set average closeness is 0.3887, the test set average closeness is 0.4047; for Wisconsin, the training set average closeness is 0.2630, the validation set average closeness is 0.3686, the test set average closeness is 0.3855.

1217 1218

1209

1219 E ADDITIONAL EXPERIMENTAL DETAILS

1220 1221

1222

E.1 GRAPH CLASSIFICATION

The classification model comprises three primary components: GCNConv layers, pooling methods, 1223 and a global average pooling layer. The hidden and output channels for this model are both set to 64. 1224 Initially, the data passes through three GCNConv layers with ReLU activation functions, followed 1225 by two pooling layers, before arriving at a global average pooling layer. The embedding output 1226 from this global layer undergoes further processing through a linear layer with ReLU activation, 1227 having dimensions (64, 32), followed by another linear layer without any activation function but 1228 with dimensions (32, number of classes). The final output can be available after applying softmax 1229 to the embedding output. All models use the Adam optimizer with a learning rate of 0.001 and 1230 are trained for 200 epochs by minimizing the negative log-likelihood loss function. For Ogbg-1231 molpcba, the data is divided into training, validation, and test sets with an 80%, 10%, and 10% split, respectively. The remaining datasets are divided into training, validation, and test sets with a 70%, 1232 15%, and 15% split. Each trial is repeated multiple times with different random seeds. 1233

1234

1235 E.2 GRAPH REGRESSION

1236

We use a backbone network inspired by MESPool (Xu et al., 2024a) for graph regression. The model mainly consists of three GINConv layers with ReLU activation functions and BatchNorm, along with two pooling layers, followed by a global average pooling layer. All channels (both hidden and output) are set to 64. The embedding output from the global average pooling layer passes through another linear layer with ReLU activation, having dimensions (64, 32). All models use the Adam optimizer with a learning rate of 0.001 and are trained for 200 epochs by minimizing the negative log-likelihood loss function. All data are processed using a 5-fold cross-validation and are run on multiple different seeds.

1244

1245 E.3 NODE CLASSIFICATION

1247 For node classification, we utilize a U-Net architecture, which we divide into a downsampling con-1248 volutional part and an upsampling convolutional part (Siddique et al., 2021). The downsampling convolutional section includes two GCNConv layers with ReLU activation functions, with pooling 1249 1250 applied between these layers. In the upsampling convolutional section, we use the indices saved during pooling for upsampling, restoring features to their pre-pooling size. The upsampled features 1251 are then fused with the corresponding residual features from the downsampling path, either through 1252 summation or concatenation. Finally, the fused features are processed and activated through a GCN-1253 Conv layer. All models employ the Adam optimizer with a learning rate set to 0.001 and are trained 1254 for 200 epochs using cross-entropy loss. All data are processed using a 5-fold cross-validation and 1255 are run on multiple different seeds. 1256

1257 E.4 HYPERPARAMETER TUNING

Details of hyperparameter tuning for different pooling methods can be found in Table A.4. We performed hyperparameter searches for each dataset in each task.

- ¹²⁶² F Additional Experiments
- 1264 F.1 ROBUSTNESS ANALYSIS

1266 Table A.5 shows the additional robustness analysis on more node-level datasets. From Table A.5, 1267 we observe the following: Firstly, for smaller node classification datasets such as Cornell, Texas, 1268 and Wisconsin, masking node features results in the greatest performance loss, while edge deletion leads to the smallest performance loss. The potential reason is that these smaller datasets inherently 1269 possess higher local characteristics and structural sparsity, making node features more critical for the 1270 model's classification tasks. Secondly, consistent with the robustness analysis on Cora, Citeseer, and 1271 Pubmed, ASAPool and KMISPool demonstrate superior performance, indicating that these pooling 1272 methods exhibit stronger robustness in node classification tasks. 1273

1273

1261

1275 F.2 GENERALIZABILITY ANALYSIS

Table A.6 presents the results of size-based and density-based distribution shifts on NCI109 and IMDB-B, respectively. From Table A.6, we obtain conclusions similar to those in the main text: for the NCI109 dataset, node dropping pooling methods perform worse than node clustering pooling methods, whereas on the IMDB-B dataset, node dropping pooling methods outperform node clustering pooling methods. Overall, AsymCheegerCutPool, MinCutPool, and DMoNPool outperform other pooling methods.

1282
1283
1284Table A.7 presents the results of degree-based and closeness-based distribution shifts on node clas-
sification tasks across four datasets: Pubmed, Cornell, Texas, and Wisconsin. We observe the fol-
lowing: *Firstly*, KMISPool and GSAPool generally perform the best, yet no single pooling method
consistently leads across all datasets. *Secondly*, the issue of class imbalance persists, and it is more
pronounced in smaller datasets such as Cornell, Texas, and Wisconsin. *Thirdly*, smaller datasets like
Cornell, Texas, and Wisconsin are more sensitive to distribution shifts compared to the larger dataset
Pubmed, resulting in more significant performance degradation.

- 1289
- 1290
- 1291
- 1292
- 1294
- 1295

	Tab	ole A.5: R	Results of	node cla	ssificatio	n under	random	noise att	ack.	
Dataset	Ptb Method	TopKPool	SAGPool	ASAPool	PANPool	COPool	CGIPool	KMISPool	GSAPool	HGPSLPool
Cornell	ADD DROP MASK	46.64 ± 0.25 61.73 ± 1.17 46.99 ± 0.90	46.45±0.77 62.09±1.84 47.36±1.56	47.18±1.03 62.29±1.15 47.91±2.46	$\begin{array}{r} 47.00 \pm 1.18 \\ \hline 61.93 \pm 0.95 \\ 47.00 \pm 0.45 \end{array}$	46.63±0.25 62.25±0.44 48.11 ±1.17	46.63 ± 0.92 61.36 ± 2.00 46.63 ± 1.03	46.81±0.67 63.19±1.79 47.74±1.13	$\begin{array}{r} 46.81 \pm 1.12 \\ \underline{63.01 \pm 0.54} \\ 47.01 \pm 1.35 \end{array}$	46.45±0.45 62.46±1.33 47.55±1.19
Texas	ADD DROP MASK	58.63±0.67 64.47±2.02 57.56±0.92	61.37±0.94 64.47±0.42 57.93±1.55	$\begin{array}{r} \underline{60.48 \pm 0.62} \\ \hline 63.92 \pm 2.38 \\ \textbf{58.85 \pm 1.44} \end{array}$	59.92±0.92 64.30±0.89 57.19±0.91	59.01±0.44 63.92±1.96 57.37±1.33	58.99±1.14 63.57±1.40 57.56±0.93	$58.83{\pm}0.49 \\ 65.57{\pm}1.59 \\ \overline{58.10{\pm}1.09}$	59.37±1.39 65.57±1.33 57.93±0.92	58.63±0.23 63.57±2.06 57.92±0.43
Wisconsi	ADD DROP MASK	54.46 ± 0.99 61.23 ± 1.23 47.02 ± 0.55	53.66 ± 0.98 60.55 ± 1.15 47.94 ± 0.18	56.18±1.49 60.29±1.68 49.80±0.86	55.52±0.21 59.76±1.72 48.60±1.14	55.78±0.98 60.43±1.79 52.59±0.01	55.78±1.30 59.36±0.87 48.35±0.49	54.99±0.34 60.16±0.66 49.53±1.15	54.73±0.48 60.43±0.95 48.20±1.11	53.65±0.37 61.36±1.17 48.08±0.96

Table A.6: Results of graph classification under distribution shifts.

		NC	[109			IMD	B-B	
Method	Si	ze	Der	sity	Si	ze	Der	sity
	Micro-F1	Macro-F1	Micro-F1	Macro-F1	Micro-F1	Macro-F1	Micro-F1	Macro-F1
Node Dropping Pooling								
TopKPool	25.10±0,81	22.90±1.01	55.92±2.57	$54.88 {\pm} 1.42$	56.00±1.22	$53.34{\pm}2.26$	72.00 ± 5.94	68.13±5.78
SAGPool	24.07±1.29	$21.64{\pm}1.58$	53.31±1.74	$51.46 {\pm} 0.98$	67.67 ± 5.10	67.44 ± 4.97	74.27 ± 3.92	67.13±5.78
ASAPool	22.57 ± 0.70	$19.42{\pm}1.04$	58.42 ± 2.73	57.09 ± 2.02	$73.83{\pm}12.43$	$73.70{\pm}12.36$	$80.80 {\pm} 4.94$	78.70±4.15
PANPool	25.73 ± 0.11	$23.80 {\pm} 0.12$	56.25 ± 1.63	$54.34{\pm}1.93$	66.50±9.34	65.73±10.38	76.27 ± 4.21	71.65 ± 4.67
COPool	$24.94{\pm}1.72$	22.77 ± 2.31	57.10 ± 2.20	55.39 ± 1.21	65.33±2.72	65.13±2.94	72.40 ± 9.91	69.52±8.26
CGIPool	$24.54{\pm}1.19$	22.39 ± 1.46	$61.36 {\pm} 0.84$	57.98 ± 3.78	$72.83 {\pm} 8.00$	72.69 ± 7.87	$71.60{\pm}5.44$	63.60±7.27
KMISPool	43.78 ± 5.82	43.24 ± 5.33	58.08 ± 3.45	50.03 ± 6.64	75.33 ± 4.78	75.16±4.61	$78.80{\pm}0.86$	73.74±0.63
GSAPool	25.97 ± 3.11	24.00 ± 4.03	53.04 ± 1.30	52.64 ± 1.16	70.17 ± 3.70	69.17±4.45	$78.80{\pm}0.86$	73.11±0.99
HGPSLPool	21.54 ± 0.22	18.17 ± 0.43	58.18 ± 2.26	55.06 ± 3.02	69.33±4.71	69.25 ± 4.76	75.07 ± 1.86	70.37±1.81
ParsPool	42.68 ± 0.81	41.97 ± 0.74	59.91±1.13	56.13 ± 2.70	75.00 ± 3.63	74.92 ± 3.57	$76.00{\pm}2.99$	71.63±3.00
Node Clustering Pooling								
AsymCheegerCutPool	79.18±0.00	49.92±0.12	$68.53 {\pm} 0.00$	44.29 ± 0.00	$71.50 {\pm} 0.60$	$71.45 {\pm} 0.60$	$78.80 {\pm} 0.00$	73.75±0.00
DiffPool	21.38 ± 0.00	17.61 ± 0.00	$69.47 {\pm} 0.00$	$48.65 {\pm} 0.02$	69.17±0.70	67.31±0.83	65.20±1.10	62.72±0.76
MinCutPool	31.83 ± 0.77	30.50 ± 0.90	70.76 ± 0.00	56.27 ± 0.02	70.17 ± 0.01	68.28 ± 0.03	$78.40 {\pm} 0.01$	73.91±0.02
DMoNPool	79.41±0.01	$55.84 {\pm} 0.01$	67.44±0.05	55.80 ± 0.13	74.33±1.59	73.85 ± 1.61	77.33±0.13	72.56±0.20
HoscPool	33.73 ± 2.35	$30.58 {\pm} 2.13$	69.54 ± 0.05	54.41 ± 0.03	72.83 ± 0.09	72.37 ± 0.10	77.20 ± 0.04	73.43±0.05
JustBalancePool	58.43 ± 4.14	44.15 ± 1.17	$71.26 {\pm} 0.00$	$58.08 {\pm} 0.01$	76.17±0.17	74.69 ± 0.35	$78.40 {\pm} 0.01$	73.91±0.02

		Pub	omed			Co	rnell			
Method	De	gree	Clos	eness	De	gree	Closeness			
	Micro-F1	Macro-F1	Micro-F1	Macro-F1	Micro-F1	Macro-F1	Micro-F1	Macro-F1		
TopKPool	81.66±0.32	81.11±0.38	85.66±0.09	82.36±0.24	34.07±2.10	22.35±2.92	57.78±4.80	25.56±8.37		
SAGPool	83.07±1.02	82.57±1.07	85.96±0.34	82.73±0.38	36.30±4.19	24.39±4.03	$61.48 {\pm} 4.57$	31.54±8.24		
ASAPool	82.11 ± 0.12	$81.94{\pm}0.55$	85.02 ± 0.54	82.12 ± 0.77	34.07±1.05	$\overline{20.94 \pm 3.40}$	$\overline{60.74 \pm 2.77}$	26.33±2.21		
PANPool	81.65 ± 0.12	81.15 ± 0.11	85.55 ± 0.03	82.16±0.20	35.56 ± 0.00	23.55±0.90	54.07 ± 2.10	18.58±3.28		
COPool	$80.42{\pm}0.14$	$79.82 {\pm} 0.20$	$84.99 {\pm} 0.35$	81.81±0.29	35.56±1.81	22.64±3.21	49.63 ± 6.87	21.09±3.44		
CGIPool	80.35±1.33	79.69±1.32	84.97±0.75	$81.74 {\pm} 0.90$	36.30±4.19	25.34±4.15	60.00 ± 1.81	27.48±3.60		
KMISPool	83.41±0.02	$82.92{\pm}0.03$	$85.66 {\pm} 0.07$	$82.50 {\pm} 0.12$	$34.81{\pm}1.05$	22.99 ± 2.00	58.52 ± 5.54	24.70 ± 8.45		
GSAPool	83.15 ± 0.81	82.61 ± 0.83	85.83 ± 0.32	82.70 ± 0.50	35.56 ± 1.81	23.23±1.21	$62.22{\pm}1.81$	30.06±4.20		
HGPSLPool	OOM	OOM	OOM	OOM	34.07±1.05	21.39±1.41	57.78±1.81	23.63±1.61		
		Теу	as		Wisconsin					
		10/								
Method	Deg	gree	Close	ness	Deg	ree	Close	ness		
Method	Deg Micro-F1	gree Macro-F1	Close Micro-F1	ness Macro-F1	Deg Micro-F1	ree Macro-F1	Close Micro-F1	ness Macro-F1		
Method TopKPool	Deg Micro-F1 40.74±2.10	gree Macro-F1 27.06±2.71	Close Micro-F1 61.48±1.05	mess Macro-F1 19.39±0.07	Deg Micro-F1 26.88±1.52	ree Macro-F1 19.88±1.97	Close Micro-F1 17.74±2.28	ness Macro-F1 15.34±1.55		
Method TopKPool SAGPool	Deg Micro-F1 40.74±2.10 39.26±1.05	gree Macro-F1 27.06±2.71 23.52±0.35	Close Micro-F1 61.48±1.05 62.22±1.81	mess Macro-F1 19.39±0.07 19.44±0.35	Deg Micro-F1 26.88±1.52 27.42±1.32	ree Macro-F1 19.88±1.97 25.32±0.98	Close Micro-F1 17.74±2.28 18.28±0.76	ness Macro-F1 15.34±1.55 14.85±0.25		
Method TopKPool SAGPool ASAPool	Deg Micro-F1 40.74±2.10 39.26±1.05 40.74±2.77	ree Macro-F1 27.06±2.71 23.52±0.35 23.87±0.67	Close Micro-F1 61.48±1.05 62.22±1.81 62.96±1.05	mess Macro-F1 19.39±0.07 19.44±0.35 19.58±0.20	Deg Micro-F1 26.88±1.52 27.42±1.32 29.03±3.48	ree Macro-F1 19.88±1.97 25.32±0.98 20.17±1.42	Close Micro-F1 17.74±2.28 18.28±0.76 15.59±2.74	ness Macro-F1 15.34±1.55 14.85±0.25 11.63±4.27		
Method TopKPool SAGPool ASAPool PANPool	Deg Micro-F1 40.74±2.10 39.26±1.05 40.74±2.77 40.00±3.63	$\begin{array}{c} \textbf{ree} \\ \textbf{Macro-F1} \\ \hline \textbf{27.06\pm2.71} \\ 23.52\pm0.35 \\ 23.87\pm0.67 \\ 23.64\pm1.13 \end{array}$	Close Micro-F1 61.48±1.05 62.22±1.81 62.96±1.05 63.70±1.05	mess Macro-F1 19.39±0.07 19.44±0.35 19.58±0.20 19.72±0.20	Deg Micro-F1 26.88±1.52 27.42±1.32 29.03±3.48 30.11±3.31	ree Macro-F1 19.88±1.97 25.32±0.98 20.17±1.42 22.99±1.60	Close Micro-F1 17.74±2.28 18.28±0.76 15.59±2.74 23.66±10.56	ness Macro-F1 15.34±1.55 14.85±0.25 11.63±4.27 15.42±5.61		
Method TopKPool SAGPool ASAPool PANPool COPool	Deg Micro-F1 40.74±2.10 39.26±1.05 40.74±2.77 40.00±3.63 39.26±1.05	ree Macro-F1 27.06±2.71 23.52±0.35 23.87±0.67 23.64±1.13 23.44±0.32	Close Micro-F1 61.48±1.05 62.22±1.81 62.96±1.05 63.70±1.05 63.70±2.10	mess Macro-F1 19.39±0.07 19.44±0.35 19.58±0.20 19.72±0.20 19.72±0.39	Deg Micro-F1 26.88±1.52 27.42±1.32 29.03±3.48 30.11±3.31 28.49±1.52	ree Macro-F1 19.88±1.97 25.32±0.98 20.17±1.42 22.99±1.60 19.94±1.50	Close Micro-F1 17.74±2.28 18.28±0.76 15.59±2.74 23.66±10.56 16.13±3.95	ness Macro-F1 15.34±1.55 14.85±0.25 11.63±4.27 15.42±5.61 16.68±3.84		
Method TopKPool SAGPool ASAPool PANPool COPool CGIPool	Deg Micro-F1 40.74±2.10 39.26±1.05 40.74±2.77 40.00±3.63 39.26±1.05 40.00±1.81	Zime Macro-F1 27.06±2.71 23.52±0.35 23.87±0.67 23.64±1.13 23.44±0.32 23.85±0.52	$\begin{array}{c} \textbf{Close} \\ \textbf{Micro-F1} \\ \hline 61.48 {\pm} 1.05 \\ 62.22 {\pm} 1.81 \\ 62.96 {\pm} 1.05 \\ 63.70 {\pm} 1.05 \\ \hline 63.70 {\pm} 2.10 \\ \hline 60.74 {\pm} 1.05 \end{array}$	mess Macro-F1 19.39±0.07 19.44±0.35 19.58±0.20 19.72±0.20 19.72±0.39 19.25±0.18	Deg Micro-F1 26.88±1.52 27.42±1.32 29.03±3.48 30.11±3.31 28.49±1.52 25.27±2.74	mee Macro-F1 19.88±1.97 25.32±0.98 20.17±1.42 22.99±1.60 19.94±1.50 20.01±2.23	Close Micro-F1 17.74±2.28 18.28±0.76 15.59±2.74 23.66±10.56 16.13±3.95 27.96±19.01	ness Macro-F1 15.34±1.55 14.85±0.25 11.63±4.27 15.42±5.61 16.68±3.84 20.37±11.58		
Method TopKPool SAGPool ASAPool PANPool COPool CGIPool KMISPool	Deg Micro-F1 40.74±2.10 39.26±1.05 40.74±2.77 40.00±3.63 39.26±1.05 40.00±1.81 38.52±1.05	Zite Macro-F1 27.06±2.71 23.52±0.35 23.87±0.67 23.64±1.13 23.44±0.32 23.85±0.52 23.19±0.10 23.44±0.32	$\begin{array}{c} \textbf{Close} \\ \textbf{Micro-F1} \\ \hline 61.48 \pm 1.05 \\ 62.22 \pm 1.81 \\ 62.96 \pm 1.05 \\ 63.70 \pm 1.05 \\ \hline 63.70 \pm 2.10 \\ \hline 60.74 \pm 1.05 \\ \hline \textbf{63.70} \pm 1.05 \\ \hline \textbf{63.70} \pm 1.05 \end{array}$	mess Macro-F1 19.39±0.07 19.44±0.35 19.58±0.20 19.72±0.20 19.72±0.20 19.72±0.20 19.25±0.18 19.72±0.20	Deg Micro-F1 26.88±1.52 27.42±1.32 29.03±3.48 30.11±3.31 28.49±1.52 25.27±2.74 31.72±4.23	macro-F1 19.88±1.97 25.32±0.98 20.17±1.42 22.99±1.60 19.94±1.50 20.01±2.23 22.58±2.76	Close Micro-F1 17.74±2.28 18.28±0.76 15.59±2.74 23.66±10.56 16.13±3.95 27.96±19.01 16.67±0.76	ness Macro-F1 15.34±1.55 14.85±0.25 11.63±4.27 15.42±5.61 16.68±3.84 20.37±11.58 14.20±0.97 14.20±0.97		
Method TopKPool SAGPool ASAPool PANPool COPool CGIPool KMISPool GSAPool	Deg Micro-F1 40.74±2.10 39.26±1.05 40.74±2.77 40.00±3.63 39.26±1.05 40.00±1.81 38.52±1.05 40.74±2.10	Z7.06±2.71 23.52±0.35 23.64±1.13 23.44±0.32 23.85±0.52 23.19±0.10 26.90±2.72	Close Micro-F1 61.48±1.05 62.22±1.81 62.96±1.05 63.70±2.10 60.74±1.05 63.70±1.05 62.22±0.00	mess 19.39±0.07 19.44±0.35 19.58±0.20 19.72±0.20 19.72±0.39 19.25±0.18 19.72±0.20 19.44±0.00	Deg Micro-F1 26.88±1.52 27.42±1.32 29.03±3.48 30.11±3.31 28.49±1.52 25.27±2.74 31.72±4.23 26.88±3.31	ree Macro-F1 19.88±1.97 25.32±0.98 20.17±1.42 22.99±1.60 19.94±1.50 20.01±2.23 22.58±2.76 18.51±1.18	Close Micro-F1 17.74±2.28 18.28±0.76 15.59±2.74 23.66±10.56 16.13±3.95 27.96±19.01 16.67±0.76 15.59±1.52	Macro-F1 15.34±1.55 14.85±0.25 11.63±4.27 15.42±5.61 16.68±3.84 20.37±11.58 14.20±0.97 12.75±1.41		