000 001 002 003 SCALING SPARSE AUTOENCODER CIRCUITS FOR IN-CONTEXT LEARNING

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ABSTRACT

Sparse autoencoders (SAEs) are a popular tool for interpreting large language model activations, but their utility in addressing open questions in interpretability remains unclear. In this work, we demonstrate their effectiveness by using SAEs to deepen our understanding of the mechanism behind in-context learning (ICL). We identify abstract SAE features that encode the model's knowledge of which task to execute and whose latent vectors causally induce the task zero-shot. This aligns with prior work showing that ICL is mediated by task vectors. We further demonstrate that these task vectors are well approximated by a sparse sum of SAE latents, including these task-execution features. To explore the ICL mechanism, we adapt the sparse feature circuits methodology of [Marks et al.](#page-13-0) [\(2024\)](#page-13-0) to work for the much larger Gemma-1 2B model, with 30 times as many parameters, and to the more complex task of ICL. Through circuit finding, we discover task-detecting features with corresponding SAE latents that activate earlier in the prompt, that detect when tasks have been performed. They are causally linked with taskexecution features through the attention layer and MLP.

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1 INTRODUCTION

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> **029 030 031 032 033 034 035 036 037 038 039** Sparse autoencoders (SAEs; [Ng](#page-13-1) [\(2011\)](#page-13-1); [Bricken et al.](#page-11-0) [\(2023\)](#page-11-0); [Cunningham et al.](#page-12-0) [\(2023\)](#page-12-0)) are a promising method for interpreting large language model (LLM) activations. However, the full potential of SAEs in interpretability research remains to be explored, since most recent SAE research either i) interprets a single SAE's features rather than the model's computation as a whole [\(Bricken](#page-11-0) [et al., 2023\)](#page-11-0), or ii) performs high-level interventions in the model, but does not interpret the effect on the downstream computation caused by the interventions [Templeton et al.](#page-15-0) [\(2024b\)](#page-15-0). In this work, we address these limitations by interpreting in-context learning (ICL), a widely studied phenomenon in LLMs. In summary, we show that SAEs enable a) the discovery of novel circuit components (task-detection features; Section [4.2\)](#page-7-0) and b) making existing interpretations of ICL more precise, by e.g. decomposing task vectors [\(Todd et al., 2024;](#page-15-1) [Hendel et al., 2023\)](#page-13-2) into task-execution features (Section [3\)](#page-3-0).

> **040 041 042 043 044 045 046 047 048** In-context learning (ICL; [Brown et al.](#page-11-1) [\(2020\)](#page-11-1)) is a fundamental capability of large language models that allows them to adapt to new tasks without fine-tuning. ICL is a significantly more complex and important task than other behaviors commonly studied in circuit analysis (such as IOI in [Wang et al.](#page-15-2) [\(2022\)](#page-15-2) and [Kissane et al.](#page-13-3) [\(2024\)](#page-13-3), or subject-verb agreement and Bias-in-Bios in [Marks et al.](#page-13-0) [\(2024\)](#page-13-0)). Recent work by [Todd et al.](#page-15-1) [\(2024\)](#page-15-1) and [Hendel et al.](#page-13-2) [\(2023\)](#page-13-2) has introduced the concept of task vectors to study ICL in a simple setting, which we follow throughout this paper.^{[1](#page-0-0)} In short, task vectors are internal representations of tasks formed by language models during the processing of few-shot prompts, such as "hot \rightarrow cold, big \rightarrow small, fast \rightarrow slow". These vectors can be extracted and added into different LLM forward passes to induce 0-shot task performance, making LLMs predict that "slow" follows "fast \rightarrow " without explicit context. Section [2.3](#page-3-1) provides a full introduction.

> **049 050 051** To identify task-execution features, we decomposed task vectors using SAEs. To achieve this, we needed to go beyond existing methods for solving the classical dictionary problem of decomposing a vector into a sparse sum of dictionary vectors [\(Elad, 2010\)](#page-12-1). To do this, we developed a bespoke

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¹Task vectors [\(Hendel et al., 2023\)](#page-13-2) are also called "function vectors" [\(Todd et al., 2024\)](#page-15-1), but we use "task vectors" throughout this paper for consistency.

054 055 056 057 058 059 060 method for LLMs we call the TASK VECTOR CLEANING (TVC) algorithm. By running the TVC algorithm, we found task-execution features: features that can partially replace task vectors taken alone and have highly interpretable max-activating token patterns. We validate the causal relevance of these task features through a series of steering experiments on tasks, spanning several categories like translation or factual recall. The experiments demonstrate that identified task features encode crucial information about task execution, are causally implicated in the model's ICL capabilities, and can play the same role as task vectors.

061 062 063 064 065 066 067 We adapted the Sparse Feature Circuits (SFC) methodology of [Marks et al.](#page-13-0) [\(2024\)](#page-13-0) to work on the more complex ICL task and the larger Gemma-1 2B model [\(Gemma Team, 2024\)](#page-12-2). This adaptation allowed us to discover and analyze the subgraph of key SAE latents involved in ICL, providing a more comprehensive view of the ICL circuit. Using this adaptation, we found **task-detection features** with SFC: features that play a crucial role in identifying the specific task being performed earlier in the prompt. Task-detection features are tightly connected with task-execution features through attention, as part of the whole ICL circuit.

068 069 070 071 072 Our findings not only advance our understanding of ICL mechanisms but also demonstrate the potential of SAEs as a powerful tool for interpretability research on larger language models. By unifying the task vectors view with SAEs and uncovering two of the most important causally implicated feature families behind ICL, we pave the way for future work to control and monitor ICL further, to improve either the safety or capabilities of models.

- **073 074** Our main contributions are as follows:
	- 1. We demonstrate that SAEs can be effectively used to explain mechanisms behind a complex set of ICL tasks in a Gemma-1 2B, which has 10-35x more parameters than prior models typically studied at this depth in comparable, circuits-style mechanistic interpretability research [\(Wang et al., 2022;](#page-15-2) [Marks et al., 2024\)](#page-13-0). We show that causal circuit finding algorithms and SFC specifically straightforwardly scale up to larger models and SAEs with different architectures (Appendix [B\)](#page-16-0).
	- 2. We identify two core bottlenecks in the ICL circuit task-detection features and task**execution features** (see Appendix [C,](#page-17-0) [F,](#page-25-0) [G\)](#page-28-0) – and study their interactions (Section [3.2\)](#page-5-0). This provides new insights into how LLMs process and execute ICL tasks. Specifically, we discover task-detection features that identify the task being performed earlier in the prompt, which are then moved by attention heads to trigger task-execution features (Figure [8\)](#page-8-0).
		- 3. We present a novel transformer-specific sparse linear decomposition algorithm (Section [3.1\)](#page-3-2) that decomposes task vectors [\(Hendel et al., 2023\)](#page-13-2) into a small set of mostly task-relevant features, enabling more precise analysis of ICL mechanisms.

Figure 1: A diagram of the in-context learning circuit, showing task detection features (yellow) causing task execution features (blue) which cause the model to output the antonym (left \rightarrow right). A more concrete circuit, along with texts these features activate on, can be seen in Figure [9.](#page-17-1)

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110 111 2.1 SPARSE AUTOENCODERS (SAES)

112 113 114 115 116 117 118 119 120 Sparse autoencoders (SAEs) are neural networks designed to learn efficient representations of data by enforcing sparsity in the hidden layer activations [\(Elad, 2010\)](#page-12-1). In the context of language model interpretability, SAEs are used to decompose the high-dimensional activations of language models into more interpretable features [\(Cunningham et al., 2023;](#page-12-0) [Bricken et al., 2023\)](#page-11-0). The basic idea behind SAEs is to train a neural network to reconstruct its input while constraining the hidden layer to have sparse activations. This process typically involves an encoder that maps the input to a sparse hidden representation, a decoder that reconstructs the input from this sparse representation, and loss task that balances reconstruction accuracy with sparsity 2 . The encoding step is as follows, with f denoting the pre-activation features and W_{enc} and b_{enc} the encoder weights and biases respectively:

$$
\mathbf{f}(\mathbf{x}) = \sigma(\mathbf{W}_{\text{enc}}\mathbf{x} + \mathbf{b}_{\text{enc}}) \tag{1}
$$

For JumpReLU SAEs [\(Rajamanoharan et al., 2024b\)](#page-14-0), the activation function and decoder are (with H being the Heaviside step function, θ the threshold parameter and $\mathbf{W}_{\text{dec}}/\mathbf{b}_{\text{dec}}$ the decoder affine parameters):

$$
\hat{\mathbf{x}}(\mathbf{f}) = \mathbf{W}_{\text{dec}}(\mathbf{f} \odot H(\mathbf{f} - \theta)) + \mathbf{b}_{\text{dec}} \tag{2}
$$

In our work, we train SAEs on residual stream activations and attention outputs, and also train transcoders^{[3](#page-2-1)} on MLP layers, all of which use the improved Gated SAE architecture [\(Rajamanoharan](#page-14-1) [et al., 2024a\)](#page-14-1).

2.2 SPARSE FEATURE CIRCUITS

136 137 138 139 140 Sparse Feature Circuits (SFCs) are a methodology introduced by [Marks et al.](#page-13-0) [\(2024\)](#page-13-0) to identify and analyze causal subgraphs of sparse autoencoder features that explain specific model behaviors. This approach combines the interpretability benefits of SAEs with causal analysis to uncover the mechanisms underlying language model behavior. The SFC methodology involves several key steps:

- 1. Decomposing model activations into sparse features using SAEs
- 2. Calculating the Indirect Effect (IE, [Pearl](#page-14-2) [\(2001\)](#page-14-2) of each feature on the target behavior
- 3. Identifying a set of causally relevant features based on IE thresholds

4. Constructing a circuit by analyzing the connections between these features

The IE of a model component is measured by intervening on that component and observing the change in the model's output. For a component a and a metric m , the IE is defined using do-calculus [\(Pearl, 2009\)](#page-14-3) as in [Marks et al.](#page-13-0) [\(2024\)](#page-13-0) as:

$$
IE(m; a) = m(x | do(a = a')) - m(x)
$$
\n(3)

152 153 154 155 Where $m(x|do(a = a'))$ represents the value of the metric when we intervene to set the value of component a to a', and $m(x)$ is the original value of the metric. In practice, attribution patching [\(Syed](#page-15-3) [et al., 2023\)](#page-15-3) is used to approximate IE, allowing for efficient computation across many components simultaneously.

SFC is described in detail in [\(Marks et al., 2024\)](#page-13-0). We describe our modifications in Appendix [E.](#page-21-0)

¹⁵⁸ 159 160 ²Typically, the L_1 penalty on activations is used [\(Bricken et al., 2023\)](#page-11-0) with some modifications [\(Rajamanoha](#page-14-1)[ran et al., 2024a;](#page-14-1) [Conerly et al., 2024\)](#page-11-2), although there are alternatives: [Rajamanoharan et al., 2024b;](#page-14-0) [Farrell,](#page-12-3) [2024;](#page-12-3) [Riggs & Brinkman, 2024.](#page-14-4)

³Transcoders are a modification of SAEs that take MLP input and convert it into MLP output instead of trying to reconstruct the residual stream.

162 163 2.3 TASK VECTORS

164 165 166 167 Continuing from the high-level description in Section [1,](#page-0-1) task vectors were independently discovered by [Hendel et al.](#page-13-2) [\(2023\)](#page-13-2) and [Todd et al.](#page-15-1) [\(2024\)](#page-15-1). The key idea behind task vectors is that they capture the essence of a task demonstrated in a few-shot prompt, allowing the model to apply this learned task to new inputs without explicit fine-tuning. Task vectors have several important properties:

- 1. They can be extracted from the model's hidden states given ICL prompts as inputs.
- 2. When added to the model's activations in a zero-shot setting, they can induce task performance without explicit context.
- 3. They appear to encode abstract task information, independent of specific input-output examples.

To illustrate the concept, consider the following simple prompt for an antonym task in the Example [1,](#page-3-3) where boxes represent distinct tokens:

183 184 Example 1: All token types in an example

input: prompt, input, arrow, output,

186 187 188 newline (target tokens for calculating the loss on included)

Figure 2: Overview of the task vector cleaning algorithm (see Figure [10;](#page-18-0) TV stands for task vector).

In this case, the task vector would encode the abstract notion of "finding the antonym" rather than specific word pairs. Task vectors are typically collected by averaging the residual stream of " \rightarrow " tokens at a specific layer across multiple ICL prompts for a given task. This averaged representation can then be used to study the model's internal task representations and to manipulate its behavior in zero-shot settings. We perform our analysis on the datasets derived from [Todd et al.](#page-15-1) [\(2024\)](#page-15-1). Details can be found in Appendix [A.](#page-15-4)

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3 DISCOVERING TASK-EXECUTION FEATURES

3.1 DECOMPOSING TASK VECTORS

200 201 202 203 204 205 206 To gain a deeper understanding of task vectors, we attempted to decompose them using sparse autoencoders (SAEs). However, several of our initial naive approaches faced significant challenges. Firstly, direct SAE reconstruction, i.e. passing the task vector as input to the SAE, produced noisy results with more than 10 nonzero SAE features on average on layers of interest^{[4](#page-3-4)}, most of which were irrelevant to the task. Moreover, this reconstruction noticeably reduced the vector's performance. These issues arose partly because task vectors are out-of-distribution inputs for SAEs, as they aggregate information from different residual streams rather than representing a single one.

207 208 209 We then explored inference-time optimization (ITO) [\(Smith, 2024\)](#page-15-5) as an alternative. However, this method also failed to reconstruct task vectors using a low number of SAE features while maintaining high performance.

210 211 Given these observations, we developed a novel method called task vector cleaning. It produces optimized SAE decomposition weights $\theta \in \mathbb{R}^{d_{SAE}}$ for a task vector v_{tv} . At a high level, the method:

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- 1. Initializes θ with weights from SAE decomposition of v_{tv} .

²¹⁴ 215 ⁴Layers where steering with task vectors decreased loss significantly (Figure [3a\)](#page-4-0). We found 3-5 interpretable features. Our cleaning algorithm can usually reduce the number to 2-4. The usual residual SAE L0 is around 44. as highlighted in the Figure [3b](#page-4-0)

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89.80 arrow 6.46 output 3.2 input 0.54 newline	Token Type		Mass $(\%)$
		prompt	0.00

Table 1: Activation masses for executor features across different token types, averaged across all tasks. We can notice they activate largely on arrow tokens.

Figure 5: Heatmap showing the effect of steering with individual task-execution features for each task. Most features boost exactly one task, with a few exceptions for similar tasks like translating to English. Full and unfiltered versions of the heatmap are available in Appendix [F.](#page-25-0)

324 325 4 APPLYING SFC TO ICL

326 327 328 329 330 331 After identifying task-execution features through our task vector analysis, we sought to expand our understanding of the in-context learning (ICL) circuit. To this end, we apply the Sparse Feature Circuits (SFC) methodology [\(Marks et al., 2024\)](#page-13-0) to the Gemma-1 2B model. However, due to the increased complexity of ICL tasks and the larger model size, the original SFC approach did not work out of the box. We had to implement several key modifications to address the challenges we encountered.

333 4.1 OUR MODIFICATIONS

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335 4.1.1 TOKEN POSITION CATEGORIZATION AND FEATURE AGGREGATION

336 337 338 339 We modified the SFC approach to better handle the structured nature of ICL prompts. Instead of treating each SAE feature as a separate node, we categorized token positions into the following groups:

- Prompt: The initial instruction tokens (e.g., "Follow the pattern:")
- Input: The last token before each arrow in an example pair
- Arrow: The arrow token itself $(\tilde{\cdot} \rightarrow \tilde{\cdot})$
- Output: The last token before each newline in an example pair
- Newline: The newline token
- Extra: Any tokens not covered by the above categories (e.g., in multi-token inputs or outputs)

348 349 350 351 352 Each pair of an SAE feature and a token type was assigned its own graph node. The effects of the feature were aggregated across all tokens of the corresponding type. This categorization allowed us to evaluate how features affect all tokens within the same category, separating features based on their role in the ICL circuit. It also enabled us to selectively disable parts of the circuit for one task while testing another, verifying the task specificity of the identified circuits.

353 354 4.1.2 LOSS FUNCTION MODIFICATION

355 356 357 358 359 360 361 362 An ICL prompt can be viewed as an (x, y) pair, where x represents the entire prompt except for the last pair's output, and y represents this output. The original SFC paper suggested using the log probabilities of y conditioned on x for such datasets. However, this approach often resulted in task-relevant features having high negative IEs on other example pairs in the prompt. This was likely due to the circuit's effect on those pairs being lost to either diminishing gradients in backpropagation or because copying circuits were much more relevant to predicting the last pair. By considering all pairs except the first one, we amplified the effect of the task-solving circuit relative to the numerous cloning circuits that activate due to the repetitive nature of ICL prompts.

363 364 4.1.3 SFC EVALUATION

365 366 367 368 To evaluate the quality of our SFC modification, we conducted a series of ablation experiments across the same dataset of ICL tasks. Our primary metric for evaluation was faithfulness, which measures how much of the original task performance is maintained after ablating specific features. We calculated faithfulness using the following formula:

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 $F(M) = \frac{M - M_a}{M_n - M_a}$ (4)

372 373 Where M is the current metric (loss), M_a is the fully ablated model metric, and M_n is the non-ablated model metric.

374 375 376 377 We evaluated the impact of ablating features for one task on the performance of all other tasks. Specifically, we ablated the nodes with highest Indirect Effects (IEs) first, continuing until we reached a faithfulness of 0.5 for the target task. Faithfulness of 0.5 corresponds to half of the original performance, i.e. a significantly destructive ablation for the target task. This approach allowed us to assess both the specificity of the circuits discovered and their impact on related tasks. Our analysis

Figure 6: We study how useful the most important nodes on task A are for performance on task B. Specifically, we ablate the most important features for task A (the ablated task on the y -axis) so that faithfulness reduces by 0.5, and measure how much faithful reduces on another task B (the tested task on the x -axis).

397 398 399 400 revealed that it is possible to significantly reduce faithfulness by disabling just a few hundred nodes. Furthermore, we found that we could reduce the number of active nodes to less than a thousand while keeping the performance almost intact. Extra details and faithfulness/completeness charts can be found in Appendix [E.](#page-21-0)

401 402 Figure [6](#page-7-1) presents a heatmap showing the change in faithfulness for various tasks when ablating the highest IE nodes for a single task. Several key observations can be made from this visualization:

- Task Specificity: Ablating most tasks does not significantly impact the performance of others, indicating that the discovered circuits are largely task-specific. This suggests that there are no common high-IE ICL-specific nodes across tasks.
- Related Task Effects: Tasks are grouped into categories, and we observe that ablation of related tasks has a higher effect on all tasks within the same group. This is visible as squares along the diagonal, particularly noticeable in the translation group.
- Performance Improvement: For some tasks, we observe that faithfulness rises well above 1.0 after ablation of other tasks. We hypothesize that this occurs because we reduce the confusion of the model by removing irrelevant execution paths.

413 414 415 416 417 It is worth noting that we excluded the **person_profession** and **football_player_position** tasks from Figure [6](#page-7-1) due to the very small difference between their fully ablated and non-ablated losses. This resulted in highly unstable faithfulness calculations for these tasks. We attribute this small difference partially to our modified loss function, as we found that calculating the loss only from the last pair results in a higher loss difference.

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4.2 TASK-DETECTION FEATURES

421 422 423 424 425 426 427 428 429 430 Our modified SFC analysis revealed a second crucial component of the ICL mechanism: taskdetection features. These features activate on instances of a complete task in the training data, specifically on the token that **completes the task**, contrary to executors that activate right before them. Both task-detection and task-execution features showed high Indirect Effects (IEs) in the extracted sparse feature circuits, with task-detection features connected to task execution features through attention output and transcoder nodes. We applied our task vector cleaning algorithm to extract task-detection features, identifying layer 11 as optimal for steering, preceding the layer 12 task-execution features. The details can be found in Appendix [G.](#page-28-0) As with executor features, we present the steering heatmap in Figure [7](#page-8-1) and the activation mass percentages in Table [2.](#page-8-1) We again see the task and token-type specificity of these features.

431 To evaluate the causal connection between task-detection features and task-execution features, we selected the most relevant detection and execution pairs based on steering effects and confirmed that

Table 2: Activation masses for task-detection features across different token types, averaged across all tasks. We can notice that they activate almost exclusively on output tokens.

Figure 7: Heatmap showing the effect of steering with the task-detection feature most relevant to each task, on every task. We see that task detection features are typically specific to the task, with exceptions for similar tasks.

450 451 452 their max activating patterns aligned with their hypothesized circuit roles. We then ablated detection directions while fixing attention patterns and measured the decrease in execution activations. Figure [8](#page-8-0) presents the results.

467 468 469 Figure 8: Heatmap showing the causal effect of the top task-detection features of each task, on the activation of the top task-execution features for every task. Averaged across all initial non-zero activations in all tasks.

The results of our causal connection analysis reveal several key insights. First, we observe strong causal connections between most task-detection and their corresponding task-execution features, supporting our hypothesis about their roles in the ICL circuit. Second, we note significant interconnectivity among translation tasks, suggesting shared circuitry for this group of related tasks. Interestingly, two tasks (person profession and present simple gerund) showed unexpectedly weak connections between their detection and execution features, warranting further investigation.

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5 RELATED WORK

480 481 482 483 484 485 Mechanistic Interpretability [Olah et al.](#page-13-4) [\(2020\)](#page-13-4) defines a framing for mechanistic interpretability in terms of *features* and *circuits*. It claims that neural network latent spaces have directions in them called features that correspond to meaningful variables. These features interact through model components sparsely to form circuits: interpretable computation subgraphs relevant to particular tasks. These circuits can be found through manual inspection in vision models [\(Cammarata et al.,](#page-11-3) [2020\)](#page-11-3). In language models, they can be found through manual patching [\(Wang et al., 2022;](#page-15-2) [Hanna](#page-13-5) [et al., 2023;](#page-13-5) [Lieberum et al., 2023;](#page-13-6) [Chan et al., 2022\)](#page-11-4) or automated circuit discovery [\(Conmy et al.](#page-12-4)

486 487 488 [\(2023\)](#page-12-4); [Syed et al.](#page-15-3) [\(2023\)](#page-15-3); [Bhaskar et al.](#page-11-5) [\(2024\)](#page-11-5), though see [Miller et al.](#page-13-7) [\(2024\)](#page-13-7)). [Marks et al.](#page-13-0) [\(2024\)](#page-13-0) extends this research area to use **Sparse Autoencoders**, as discussed below.

489 490 491 492 493 494 495 496 497 498 499 500 501 In-Context Learning (ICL) ICL was first introduced in [Brown et al.](#page-11-1) [\(2020\)](#page-11-1) and refers to models learning to perform tasks from prompt information at test time. There is a large area of research studying its applications [\(Dong et al., 2024\)](#page-12-5), high-level mechanisms [\(Min et al., 2022\)](#page-13-8) and limitations [\(Peng et al., 2023\)](#page-14-5). [Elhage et al.](#page-12-6) [\(2021\)](#page-12-6) and [Olsson et al.](#page-14-6) [\(2022\)](#page-14-6) find *induction heads* partly responsible for in-context learning. However, since these attention heads do more than just induction [\(Goldowsky-Dill et al., 2023\)](#page-12-7), and are not sufficient for complex task-following, induction heads alone cannot explain ICL. [Anil et al.](#page-10-0) [\(2024,](#page-10-0) Appendix G) proposes a mechanistic hypothesis for an aspect of simple in-context task behavior. [Hendel et al.](#page-13-2) [\(2023\)](#page-13-2) and [Todd et al.](#page-15-1) [\(2024\)](#page-15-1) find that simple in-context learning tasks create strong directions in the residual stream adding which makes it possible for a network to perform tasks zero-shot, but does not explain how task vectors form nor what interpretable components the task vectors are composed of. A more detailed discussion can be found in Appendix [H.](#page-29-0) Of particular interest is [Wang et al.,](#page-15-6) which investigates a simple ICL classification task and finds similar results with different terminology (information flow instead of circuits, "label words" instead of task-detection features).

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504 505 506 507 508 509 510 511 512 513 514 515 516 Sparse Autoencoders A major roadblock to mechanistic interpretability research is superposition [\(Elhage et al., 2022b\)](#page-12-8), where the interpretable units of neural network do not tend to align with the basis directions (e.g. neurons). Sparse autoencoders [\(Ng, 2011;](#page-13-1) [Bricken et al., 2023\)](#page-11-0) are one method of addressing this roadblock, and multiple works since proposed improvements to SAE training [\(Rajamanoharan et al., 2024b;](#page-14-0) [Bussmann et al., 2024;](#page-11-6) [Braun et al., 2024;](#page-11-7) [Gao et al., 2024;](#page-12-9) [Templeton](#page-15-0) [et al., 2024b\)](#page-15-0), and we use several more in our work [\(Rajamanoharan et al., 2024a;](#page-14-1) [Adam Jermyn,](#page-10-1) [2024;](#page-10-1) [Conerly et al., 2024\)](#page-11-2). [Cunningham et al.](#page-12-0) [\(2023\)](#page-12-0), building on [Bills et al.](#page-11-8) [\(2023\)](#page-11-8), apply [Conmy](#page-12-4) [et al.](#page-12-4) [\(2023\)](#page-12-4) to find circuits in small language models. [Marks et al.](#page-13-0) [\(2024\)](#page-13-0) adapt [Syed et al.](#page-15-3) [\(2023\)](#page-15-3) in the SAE basis to find circuits and address a practical bias reduction problem. [Kissane et al.](#page-13-3) [\(2024\)](#page-13-3) apply a slightly different automated SAE algorithm (similar to ours in that it operates on single prompts) to IOI [\(Wang et al., 2022\)](#page-15-2), using SAEs on the attention layer outputs and residual stream. [Dunefsky et al.](#page-12-10) [\(2024\)](#page-12-10) introduce *transcoders* (which are also briefly discussed in [Templeton et al.](#page-15-7) [\(2024a\)](#page-15-7) and [Li et al.](#page-13-9) [\(2023\)](#page-13-9)) to simplify analysis of circuits involving MLPs. We build on their work and train transcoders as part of our suite of Gemma-1 SAEs.

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6 CONCLUSION

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Limitations Our work focused on the simple task vector setting to study ICL (Section [2.3\)](#page-3-1), which does not capture all ways that ICL is used in practice (generally involving far more tokens and open-ended tasks). We also only interpreted Gemma-1 2B. Therefore, other LLM architectures or model sizes could lead to different results (though this is not likely, since task vectors exist across models [\(Todd et al., 2024\)](#page-15-1)). Finally, the complexity of the task studied meant our interpretations have some approximation error: attention heads matter for the detection-execution connection, but the succeeding MLP is necessary to capture the full effect (Section [4.2\)](#page-7-0). This means that our explanation needs to include moving parts aside from task-detection attention output features. It is possible to model the effects of the MLP through transcoder features, but we leave that for future work.

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530 531 532 533 534 535 Future Work Future work could extend SFC methods to work on more than a band of layers in the middle of the model (Section [2.2\)](#page-2-2). Since many features correspond to individual input tokens and output predictions (due to the three stages of inference in LLMs; [Elhage et al.](#page-12-11) [\(2022a\)](#page-12-11); [Lad](#page-13-10) [et al.](#page-13-10) [\(2024\)](#page-13-10)), this will require further adaptation of the SFC methodology. Moreover, our multiple contributions will hopefully spur further work that finds new tasks to interpret or explain in greater depth than prior work, as discussed in our concluding paragraph below.

536 537 538 539 To summarize our work: we use SAEs to explain in-context learning in greater detail than any prior mechanistic interpretability work. This provides strong evidence that Sparse Autoencoders are valuable circuit analysis tools, and the innovations developed: TVC (Section [3.1\)](#page-3-2), SFC improvements (Section [2.2\)](#page-2-2) and an SAE training codebase in JAX with open SAE weights (Section [7\)](#page-10-2) are likely to help enable lots of other SAE research to tackle more ambitious tasks and larger models.

540 541 7 REPRODUCIBILITY STATEMENT

542 543 544 545 We are committed to fostering reproducibility and advancing research in the field of mechanistic interpretability. To support this goal, we plan to release the following resources upon successful acceptance of this paper:

- **546 547 548**
- **549 550**

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- 1. Two JAX libraries optimized for TPU:
	- A library for Sparse Autoencoder (SAE) training
	- A library for SAE inference and model analysis, built upon Penzai with our custom Llama and Gemma ports
- 2. A full suite of SAEs for Gemma 2B, along with a dataset of their max activating examples
	- 3. Two custom dashboards used in our analysis:
		- A dashboard for browsing max activating examples
		- An interactive dashboard for exploring extracted Sparse Feature Circuits (SFC)

556 557 558 559 560 561 These resources will enable researchers to replicate our experiments, extend our work, and conduct their own investigations using our tools and methodologies. The release of our custom dashboards will provide additional transparency and facilitate a deeper exploration of our results. Due to the complexity of our infrastructure, we only share anonymized versions of our analysis, cleaning, and SFC scripts, which still require our JAX libraries to run. We hope that reviewers will find this, along with the detailed methodologies described in the paper, sufficient evidence of reproducibility.

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861 862 863 Our dataset for circuit finding is primarily derived from the function vectors paper [\(Todd et al., 2024\)](#page-15-1), which provides a diverse set of tasks for evaluating the existence and properties of function vectors in language models. We supplemented this dataset with three additional algorithmic tasks to broaden the scope of our analysis:

- Extract the first element from an array of length 4
- Extract the second element from an array of length 4
- Extract the last element from an array of length 4

The complete list of tasks used in our experiments with task descriptions is as follows:

893 894 895 896 This diverse set of tasks covers a wide range of linguistic and cognitive abilities, including geographic knowledge, language translation, grammatical transformations, and simple algorithmic operations. By using this comprehensive task set, we aimed to thoroughly investigate the in-context learning capabilities of the Gemma 1 2B model across various domains.

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B SAE TRAINING

900 901 902 903 904 905 906 907 908 909 Our Gemma 1 2B SAEs are trained with a learning rate of 1e-3 and Adam betas of 0.0 and 0.99 for 150M (± 100) tokens of FineWeb [\(Penedo et al., 2024\)](#page-14-7). The methodology is overall similar to [\(Bloom, 2024\)](#page-11-9). We initialize encoder weights orthogonally and set decoder weights to their transpose. We initialize decoder biases to 0. We use [Rajamanoharan](#page-14-8) [\(2024\)](#page-14-8)'s ghost gradients variant (ghost gradients applied to dead features only, loss multiplied by the proportion of death features) with the additional modification of using softplus instead of exp for numerical stability. A feature is considered dead when its density (according to a 1000-batch buffer) is below 5e-6 or when it has not fired in 2000 steps. We use Anthropic's input normalization and sparsity loss for Gemma 1 2B [\(Conerly et al.,](#page-11-2) [2024\)](#page-11-2). We found it to improve Gated SAE training stability. We modified it to work with transcoders by keeping track of input and output norms separately and predicting normed outputs.

910 911 912 913 We convert our Gated SAEs into JumpReLU SAEs after training, implementing algorithms like TVC and SFC in a unified manner for all SAEs in this format (including simple SAEs). The conversion procedure involves setting thresholds to replicate the effect of the gating branch. For further details, see [Rajamanoharan et al.](#page-14-0) [\(2024b\)](#page-14-0).

914 915 916 917 We use 4 v4 TPU chips running Jax [\(Bradbury et al., 2018\)](#page-11-10) (Equinox [\(Kidger & Garcia, 2021\)](#page-13-11)) to train our SAEs. We found that training with Huggingface's Flax LM implementations was very slow. We reimplemented LLaMA [\(Dubey et al., 2024\)](#page-12-12) and Gemma [\(Gemma Team, 2024\)](#page-12-2) in Penzai [\(Johnson, 2024\)](#page-13-12) with a custom layer-scan transformation and quantized inference kernels as well as support for loading from GGUF compressed model files. We process an average of around 4400 tokens per second, which makes training SAEs and not caching LM activations the main bottleneck. For this and other reasons, we don't do SAE sparsity coefficient sweeps to increase TPU utilization.

 For caching, we use a distributed ring buffer which contains separate pointers on each device to allow for processing masked data. The (in-place) buffer update is in a separate JIT context. Batches are sampled randomly from the buffer for each training step.

 We train our SAEs in bfloat16 precision. We found that keeping weights and scales in bfloat16 and biases in float32 performed best in terms of the number of dead features and led to a Pareto improvement over float32 SAEs.

 For training Phi 3 [\(Abdin et al., 2024\)](#page-10-3) SAEs, we use data generated by the model unconditionally, similarly to (Xu et al.,)^{[5](#page-18-2)}. The resulting dataset we train the model on contains many math problems and is formatted as a natural-seeming interaction between the user and the model.

 Each SAE training run takes us about 3 hours. We trained 3 models (a residual SAE, an attention output SAE, and a transcoder) for each of the 18 layers of the model. This is about 1 week of v4-8 TPU time.

Our SAEs and training code will be made public after paper acceptance.

C EXAMPLE CIRCUITS

 An example output of our circuit cleaning algorithm can be found in Figure [9.](#page-17-1) We can see the flow of information through a single high-IE attention feature from a task-detection feature (activating on output tokens) to transcoder and residual execution features (activating on arrow tokens). The feature activates on antonyms on the detection feature #11050: one can assume the first sequence began as "Short Term Target", making the second half an antonym.

We will release a web interface for viewing maximum activating examples and task feature circuits.

Figure 10: An overview of our Task Vector Cleaning algorithm. TV stands for Task Vector.

D TASK VECTOR CLEANING ALGORITHM

The task vector cleaning algorithm is a novel approach we developed to isolate task-relevant features from task vectors. Figure [10](#page-18-0) provides an overview of this algorithm.

999 1000 1001 1002 Our process begins with collecting residuals for task vectors using a batch of 16 and 16-shot prompts. We then calculate the SAE features for these task vectors. We explored two methods: (1) calculating feature activation and then averaging across tokens, and (2) averaging across tokens first and then calculating the task vector. They had similar performances.

1003 1004 The cleaning process is performed on a training batch of 24 pairs, with evaluation conducted on an additional 24 pairs. All prompts are zero-shot. An example prompt is as follows:

Example 2: The steered token is highlighted in red. Loss is calculated on the yellow token.

1016 1017 1018 1019 The algorithm is initialized with the SAE reconstruction as a starting point. It then iteratively steers the model on the reconstruction layer and calculates the loss on the training pairs. To promote sparsity, we add the L_1 norm of weights with coefficient l to the loss function. The algorithm implements early stopping when the L_0 norm remains unchanged for *n* iterations.

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       def tvc_algorithm(task_vector, model, sae):
    2 initial_weights = sae.encode(task_vector)
    3 def tvc_loss(weights, tokens):
    4 task_vector = sae.decode(weights)
    5 mask = tokens == self.separator
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⁵Phi-3 is trained primarily with instruction following data, making it an aligned chat model.

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      6 model.residual_stream[layer, mask] += task_vector
      7 # loss only on the "output" tokens,
      8 # ignoring input and prompt tokens
      9 loss = logprobs(model.logits, tokens, ...)
      10 return loss + l1_coeff * l1_norm(weights)
     11 weights = initial_weights.copy()
     12 optimizer = adam(weights, 1r=0.15)13 last_10, without_change = 0, 0 # early stopping
     14 for _ in range(1000):
      15 grad = jax.grad(tvc_loss)(weights, tokens)
      16 weights = optimizer.step(grad)
      17 if l0_norm(weights) != last_l0:
      18 last_l0, without_change = l0_norm(weights), 0
      19 elif without_change >= 50:
      20 break
     21 return weights
                             Algorithm 1: Pseudocode for Task Vector Cleaning.
       The hyperparameters l, n, and learning rate \alpha can be fixed for a single model. We experimented with
        larger batch sizes but found that they did not significantly improve the quality of extracted features
       while substantially slowing down the algorithm due to gradient accumulation.
       The algorithm takes varying amounts of time to complete for different tasks and models. For Gemma
       1, it stops at 100-200 iterations, which is close to 40 seconds at 5 iterations per second.
        It's worth noting that we successfully applied this method to the recently released Gemma 2 2B and
        9B models using the Gemma Scope SAE suite (Lieberum et al., 2024). It was also successful with the
        Phi-3 3B model (Abdin et al., 2024) and with our SAEs, which were trained similarly to the Gemma
       1 2B SAEs.
       D.1 L_1 SWEEPS
       To provide more details about the method's effectiveness across various models and SAE widths, we
        conducted L_1 coefficient sweeps with our Phi-3 and Gemma 1 2B SAEs, as well as Gemma Scope
        Gemma 2 SAEs. We chose two SAE widths for Gemma 2 2B and 9B: 16k and 65k. For Gemma 2
        2B we also sweeped across several different target SAE l0 norms. We studied only the optimal task
        vector layer for each model: 12 for Gemma 1, 16 for Gemma 2, 18 for Phi-3, and 20 for Gemma 2
        9B. We used a learning rate of 0.15 with the Gemma 1 2B, Phi-3, and Gemma 2 2B 65k models, 0.3
       with Gemma 2 2B 16k, and 0.05 with 200 early stopping steps for Gemma 2 9B.
        Figures 11, 12, 13 compare TVC and ITO against original task vectors. The X-axis displays the
        fraction of active task vector SAE features used. The Y-axis displays the TV loss delta, calculated
        as (L_{TV} - L_{Method})/L_{Zero}, where L_{TV} is the loss from steering with the task vector, L_{Method}is the loss after it has been cleaned using the corresponding method, and L_{Zero} is the uninformed
       (no-steering) model loss. This metric shows improvement over the task vector relative to the loss of
        the uninformed model. Points were collected from all tasks using 5 different L_1 coefficient values.
        We observe that our method often improves task vector loss and can reduce the number of active
        features to one-third of those in the original task vector while maintaining relatively intact performance.
        In contrast, ITO rarely improves the task vector loss and is almost always outperformed by TVC.
        Figures 14, 15 and 16 show task-mean loss decrease (relative to no steering loss) and remaining TV
        features fraction plotted against L_1 sweep coefficients. We see that L_1 coefficients between 0.001
        and 0.025 result in relatively intact performance, while significantly reducing the amount of active
        SAE features. From Figure 15 we can notice that the method performs better with higher target l0
        SAEs, being able to affect the loss with just a fraction of active SAE features.
```


 to task vectors for Phi-3. The Y-axis shows relative improvement over task vector loss, while the X-axis shows the fraction of active TV features used. Metric calculation details are available in [D.1](#page-19-0)

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1172 1173 1174 Figure 13: Performance of ITO and TVC across different tasks and optimization parameters compared to task vectors for Gemma 2 Gemma Scope SAEs. The Y-axis shows the relative improvement over the loss from steering with a task vector, while the X-axis shows the fraction of active TV features used. Metric calculation details are available in Appendix [D.1.](#page-19-0)

1177 E DETAILS OF OUR SFC IMPLEMENTATION

- **1178 1179**
- **1180** E.1 IMPLEMENTATION DETAILS

1181 1182 Our implementation of circuit finding attribution patching is specialized for Jax and Penzai.

1183 1184 1185 1186 We first perform a forward-backward pass on the set of prompts, collecting residuals and gradients from the metric to residuals. We collect gradients with jax , grad by introducing "dummy" zerovalued inputs to the metric computation function that are added to the residuals of each layer. Note that we do not use SAEs during this stage.

1187 We then perform an SAE encoding step and find the nodes (residual, attention output, and transcoder SAE features and error nodes) with the highest indirect effects using manually computed gradients

1235 1236 Figure 14: L¹ coefficient sweeps across different models and SAEs. All metrics are averaged across all tasks. Error bars show the standard deviation of the average for each case. Metric calculation details are available in [D.1.](#page-19-0)

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1289 1290 Figure 15: L_1 coefficient sweeps across different target SAE sparsities and widths for Gemma 2 2B. All metrics are averaged across all tasks. Error bars show the standard deviation of the average for each case. Metric calculation details are available in Appendix [D.1.](#page-19-0)

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 Figure 16: L_1 coefficient sweeps across two SAE widths for Gemma 2 9B. All metrics are averaged across all tasks. Error bars show the standard deviation of the average for each case. Metric calculation details are available in [D.1.](#page-19-0)

 from the metric. After that, we find the features with the top K indirect effects for each layer and position mask and treat them as candidates for circuit edge targets. We compute gradients with respect to the metric to the values of those nodes, propagate them to "source features" up to one layer above, and multiply by the values of the source features. This way, we can compute indirect effects for circuit edges and prune the initially fully connected circuit. However, like [Marks et al.](#page-13-0) [\(2024\)](#page-13-0), we do not perform full ablation of circuit edges.

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       We include a simplified implementation of node-only SFC in Algorithm 2.
     1 # resids_pre: L x N x D - the pre-residual stream at layer L
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    2 # resids mid: L x N x D - the middle of the residual stream
     3 # (between attention and MLP) at layer L
     4 # grads_pre: L x N x D - gradients from the metric to resids_pre
       # grads_mid: L x N x D - gradients from the metric to resids_mid
       # all of the above are computed with a forward and backward
    7 # pass without SAEs
    8
    9 # saes_resid: L - residual stream SAEs
    10 # saes_attn: L - attention output SAEs
    11 # transcoders_attn: L - transcoders predicting resids_pre[l+1]
    12 # from resids mid[l]
    13
    14 def indirect effect for residual node(layer):
    15 sae_encoding = saes_resid[layer].encode(
    16 resids_pre[layer])
    17 grad_to_sae_latents = jax.vjp(
    18 saes_resid[layer].decode,
    19 sae_encoding
    20 )(grads_pre[l])
    21 return (grad_to_sae_latents * sae_encoding).sum(-1)
    22
    23 def indirect_effect_for_attention_node(layer):
    24 sae_encoding = saes_attn[layer].encode(
```

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    25 resids_mid[layer] - resids_pre[layer])
    26 grad_to_sae_latents = jax.vjp(
    27 saes_attn[layer].decode,
    28 sae_encoding
    29 )(grads_mid[l])
    30 return (grad_to_sae_latents * sae_encoding).sum(-1)
    31
    32 def indirect_effect_for_transcoder_node(layer):
    33 sae_encoding = transcoders[layer].encode(
    34 resids_mid[layer])
    35 grad_to_sae_latents = jax.vjp(
    36 transcoders[layer].decode,
    37 sae_encoding
    38 ) (qrads_pre[1+1])
    39 return (grad_to_sae_latents * sae_encoding).sum(-1)
```
Algorithm 2: Pseudocode for Sparse Feature Circuits indirect effect calculation.

E.2 FAITHFULNESS CHARTS

 Figure [17](#page-25-1) shows the average effect of node trimming on faithfulness in all tasks. We follow the methodology of [Marks et al.](#page-13-0) [\(2024\)](#page-13-0) thresholding removing nodes with low IE first. We can see that the circuits keep at least 0.8 faithfulness on average with just 1000 nodes (on layers 11-17).

Figure 17: Average faithfulness across tasks depending on the number of nodes left in the circuit.

Figure [18](#page-26-0) shows the averaged inverse node trimming effect on faithfulness across all tasks. [Marks](#page-13-0) [et al.](#page-13-0) [\(2024\)](#page-13-0) calls this metric completeness and calculates it as the faithfulness of the model just with the circuit ablated. We calculate it by thresholding the nodes starting with those that have the highest IE. We can see that the ablation of even just several hundred nodes has a drastic impact on faithfulness. These results were also computed with the window of layers being 11-17).

F STEERING WITH TASK-EXECUTION FEATURES

 To evaluate the causal relevance of our identified ICL features, we conducted a series of steering experiments. Our methodology employed zero-shot prompts for task-execution features, measuring effects across a batch of 32 random pairs.

 We set the target layer as 12 using Figure [3a](#page-4-0) and extracted all task-relevant features on it using our cleaning algorithm. To determine the optimal steering scale, we conducted preliminary experiments using manually identified task-execution features across all tasks. Through this process, we established an optimal steering scale of 15, which we then applied consistently across all subsequent experiments.

1450 1451 1452 1453 The setup involved a batch of 16 ICL prompts, each containing 32 examples for each task. We collected all features from the cleaned task vectors for every task. Similar to positive steering, we steered with features on arrow tokens, but this time multiplying the direction by -1. Prompts this time contained several arrow tokens, and we steered on all of them simultaneously.

1454 1455 1456 1457 An important distinction from positive steering is that performance degradation in negative steering may occur due to two factors: (1) our causal intervention on the ICL circuit and (2) the steering scale being too high. To address this, we measured accuracy across all pairs in the batch instead of loss, as accuracy does not decrease indefinitely. We also observed that features no longer share a common optimal scale. Consequently, for each task pair, we iterated over several scales between 1 and 30.

1458 en_es ● ● ● ● ● ● ● ● ● Effect strength en_fr **1459** ● ● ● ● ● ● ● ● ● 1 en_it ● ● ● ● ● ● ● ● ● **1460** country_capital ● ● ● ● ● ● ● ● on_religio ● ● ● ● ● ● ● ● ● **1461** location_language ● ● ● ● ● ● ● ● 0.8 ● ● ● ● ● ● ● ● ● person_language **1462** П football_player_position ● ● ● ● ● ● singular_plural ● ● ● ● ● ● ● ● ● ● **1463** present_simple_gerund ● ● ● ● ● ● ● ● п 0.6 algo_las ● ● ● ● ● ● ● ● ● ● **1464** Task present_simple_past_perfect ● ● ● ● ● ● ● ● person_profession ● ● ● ● ● ● ● **1465** present_simple_past_simple ● ● ● ● ● ● ● ● ● 0.4 location_continent ● ● ● ● ● ● **1466** location_country ● ● ● ● ● ● ● ● ● algo_second ● ● ● ● ● ● ● ● ● ● ● **1467** algo_first ● ● ● ● ● ● ● ● ● 0.2 ● ● ● ● ● ● ● ● ● ● ● ● ● ● **1468** antonyms ● ● ● ● ● ● ● ● ● ● plural_singular **1469** fr_en ● ● ● ● ● ● ● ● ● ● ● ● ● ● ● ● ● ● it_en **1470** 0 es_en ● ● ● ● ● ● ● ● ● 1830 13458 11172 11173 26987 27268 14612 32320 12943 9662 22906 10720 19097 19112 24925 7106 27401 25576 7739 211 1763
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28 San Brass **1471** 5579 16490 2930 26594 161₁ 1988
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1989 1989 **1472** ● Feature is in task vector | ● Feature is present after cleaning Feature

1473 1474 1475 1476 Figure 19: Full version of the heatmap in Figure [5](#page-5-2) showing the effect of steering with individual task-execution features for each task. The features present in the task vector of the corresponding task are marked with dots. Green dots show the features that were extracted by cleaning. Red dots are features present in the original task vector. Not all original features from the task vectors are present.

1479 1480 1481 For each feature, we then selected a scale that reduced accuracy by at least 0.1 for at least one task. Steering results at this scale were used for this feature across all tasks.

1482 1483 1484 1485 1486 1487 Figure [20](#page-27-1) displays the resulting heatmap. While we observe some degree of task specificity — and even note that some executing features from Figure [19](#page-27-0) have their expected effects — we also find that negative steering exhibits significantly lower task specificity. Additionally, we observe that non-taskspecific features have a substantial impact in this experiment. This suggests that steering experiments alone may not suffice for a comprehensive analysis of the ICL mechanism, thus reinforcing the importance of methods such as our modification of SFC.

1502 1503 1504 Figure 20: Negative steering heatmap. Displays accuracy decrease after optimal scale negative steering on full ICL prompts. Green circles show which features were present in the cleaned task vector of the corresponding task. More details in Appendix [F.1](#page-26-1)

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1507 F.2 GEMMA 2 2B POSITIVE STEERING

1508 1509 1510 1511 Additionally, we conducted zero-shot steering experiments with Gemma 2 2B 16k and 65k SAEs. Contrary to Gemma 1 2B, task executors from Gemma 2 2B did not have a single common optimal steering scale. Thus, we added an extra step to the experiment: for each feature and task pair, we performed steering with several scales from 30 to 300, and then selected the scale that had maximal loss decrease on any of the tasks. We then used this scale for this feature in application to all other

1512 1513 1514 tasks. Figure [22a](#page-29-1) and Figure [22b](#page-29-1) contain steering heatmaps for Gemma 2 2B 16k SAEs and Gemma 2 2B 65k SAEs respectively.

1515 1516 1517 We observe a relatively similar level of executor task-specificity compared to Gemma 1. One notable difference between 16k and 65k SAEs is that 65k cleaned task vectors appear to contain more features with a strong effect on the task. However, this may be due to the l_1 regularization coefficient being too low.

1535 1536 1537 1538 1539 Figure 21: Unfiltered version of the heatmap in Figure [7](#page-8-1) showing the effect of steering with individual task-execution features for each task. The features present in the task vector of the corresponding task are marked with dots. Green dots show the features that were extracted by cleaning. Red dots are the features present in the original task vector. Since the chart only contains features from cleaned task vectors, not all features from the original task vectors are present.

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1541 1542 G TASK-DETECTION FEATURES

1543 1544 1545 1546 For our investigation of task-detection features, we employed a methodology similar to that used for task execution features, with a key modification. We introduced a fake pair to the prompt and focused our steering on its output. This approach allowed us to simulate the effect of the detection features the way it happens on real prompts.

1547 1548 1549 1550 1551 Our analysis revealed that layers 10 and 11 were optimal for task detection, with performance notably declining in subsequent layers. We selected layer 11 for our primary analysis due to its proximity to layer 12, where we had previously identified the task execution features. This choice potentially facilitates a more direct examination of the interaction between detection and execution mechanisms.

1552 1553 1554 1555 The steering process for detection features followed the general methodology outlined in Appendix [F,](#page-25-0) including the use of a batch of 32 random pairs, extraction of task-relevant features, and application of post-processing steps to normalize and highlight significant effects. The primary distinction lies in the application of the steering to the prompt.

1556 1557 This approach allowed us to create a comprehensive representation of the causal relationships between task-detection features and the model's ability to recognize specific tasks, as visualized in Figure [7.](#page-8-1)

1564 1565 Example 4: Task-detection steering setup. The steered token is highlighted in red and the loss is calculated on the yellow token.

1594 1595 1596 1597 1598 1599 Figure 22: Unfiltered positive steering heatmap for Gemma 2 2B SAEs showing the effect of steering with individual task-execution features for each task. Steering scales were optimized for each feature. The features present in the task vector of the corresponding task are marked with dots. Green dots show the features that were extracted by cleaning. Red dots are the features present in the original task vector. Since the chart only contains features from cleaned task vectors, not all features from the original task vectors are present.

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This section will cover work on understanding ICL not mentioned in Section [5.](#page-8-2)

H ICL INTERPRETABILITY LITERATURE REVIEW

1604 1605 1606 1607 1608 1609 Raventós et al. provides evidence for two different Bayesian algorithms being learned for linear regression ICL: one for limited task distributions and one that is similar to ridge regression. It also intriguingly shows that the two solutions lie in different basins of the loss landscape, a phase transition necessary to go from one to the other. While interesting, it is not clear if the results apply to real-world tasks.

1610 1611 1612 1613 1614 1615 The existence of discrete task detection and execution features hinges on the assumption that incontext learning works by classifying the task to perform and not by learning a task. [Pan et al.](#page-14-10) aims to disentangle the two with a black-box approach that mixes up outputs to force the model to learn the task from scratch. [Si et al.](#page-14-11) look at biases in task recognition in ambiguous examples through a black-box lens. We find more clear task features for some tasks than others but do not consider whether this is linked to how common a task is in pretraining data.

1616 1617 1618 1619 [Xie et al.](#page-15-9) proposes that in-context learning happens because language models aim to model a latent topic variable to predict text with long-range coherence. [Wang et al.](#page-15-10) [\(2024\)](#page-15-10) show following the two proposed steps rigorously improves results in real-world models. However, they do not endeavor to explain the behavior of non-finetuned models by looking at internal representations; instead, they aim to improve ICL performance.

1620 1621 1622 1623 1624 [Han et al.](#page-13-14) use a weight-space method to find examples in training data that promote in-context learning using a method akin to [Grosse et al.](#page-12-13) [\(2023\)](#page-12-13), producing results similar to per-token loss analyses in [Olsson et al.](#page-14-6) [\(2022\)](#page-14-6), and, similarly to the studies mentioned above, finds that those examples involve long-range coherence. Our method is also capable of finding examples in data that are similar to ICL, and we find crisp examples for many tasks being performed Appendix [I.](#page-30-0)

1625 1626 1627 1628 1629 [Bansal et al.](#page-11-11) offers a deeper look into induction heads, scaling up [Olsson et al.](#page-14-6) [\(2022\)](#page-14-6) the way we scale up [Marks et al.](#page-13-0) [\(2024\)](#page-13-0). Crucially, it finds that MLPs in later layers cannot be removed while preserving ICL performance, indirectly corroborating our findings from Section [4.2.](#page-7-0) [Chen et al.](#page-11-12) come up with a proof that states that gradient flow converges to a generalized version of the algorithm suggested by [Olsson et al.](#page-14-6) [\(2022\)](#page-14-6) when trained on n-gram Markov chain data.

1630 1631 1632 1633 1634 1635 1636 1637 1638 [Garg et al.](#page-12-14) studies the performance of toy models trained on in-context regression various *function classes*. [Yadlowsky et al.](#page-15-11) find that Transformers trained on regression with multiple function classes have trouble combining solutions for learning those functions. [Oswald et al.](#page-14-12) construct a set of weights for linear attention Transformers that reproduce updates from gradient descent and find evidence for the algorithm being represented on real models trained on toy tasks. [Mahankali et al.](#page-13-15) proves that this algorithm is optimal for single-layer transformers on noisy linear regression data. [Shen et al.](#page-14-13) questions the applicability of this model to real-world transformers. [Bai et al.](#page-10-4) finds that transformers can switch between multiple different learning algorithms for ICL. [Dai et al.](#page-12-15) find multiple similarities between changes made to model predictions from in-context learning and weight finetuning.

1639 1640 1641 While important, we do not consider this direction of interpreting transformers trained on regression for concrete function classes through primarily white-box techniques. Instead, we aim to focus on clear discrete tasks which are likely to have individual features.

1642 1643 1644 1645 1646 1647 1648 1649 The results of [Wang et al.](#page-15-6) are perhaps the most similar to our findings. The study finds "anchor tokens" responsible for aggregating semantic information, analogous to our "output tokens" (Section [2.3\)](#page-3-1) and task-detection features. They tackle the full circuit responsible for ICL bottom-up and intervene on models using their understanding, improving accuracy. Like this paper, they do not deeply investigate later attention and MLP layers. Our study uses SAE features to find strong linear directions on output and arrow tokens corresponding to task detection and execution respectively, offering a different perspective. Additionally, we consider over 20 diverse token-to-token tasks, as opposed to the 4 text classification datasets considered in citewang_{label2}023.

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1651 1652 I MAX ACTIVATING EXAMPLES

1653 1654 1655 1656 1657 This section contains max activating examples for some executor and detector features for Gemma 1 2B, as described in [\(Bricken et al., 2023\)](#page-11-0). They are computed by iterating over the training data distribution (FineWeb) and sampling activations of SAE features that fall within disjoint buckets for the activation value of span 0.5. We can observe that the degree of intuitive interpretability depends on the amount of task-similar contexts in the training data and SAE width.

1658 1659 1660 We also provide max activating examples for Gemma 2 2B executor features from Figures [22b](#page-29-1) and [22a.](#page-29-1) These max activating examples are taken from the Neuronpedia [\(Lin, 2023\)](#page-13-16) and are available in Figures [26](#page-33-0) and [25.](#page-33-1)

1661 1662 1663 1664 1665 1666 Here we can notice the main difference between executors and detectors: executors mainly activate **before the task completion,** while detectors activate on the **token that completes the task**. We also found that in Gemma 1 2B detector features for some tasks were split between several token-level features (like the journalism feature in Figure [24f\)](#page-32-0), and they did not create a single feature before the task executing features activated. We attribute this to the limited expressivity of the SAEs that we used.

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 Figure 26: Max activating examples for Gemma 2 2B 65k executor features from the Figure [22b](#page-29-1)