000 001 002 FA I RGE N: CONTROLLING FAIR GENERATIONS IN DIF-FUSION MODELS VIA ADAPTIVE LATENT GUIDANCE

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ABSTRACT

Diffusion models have shown remarkable proficiency in generating photorealistic images, but their outputs often exhibit biases toward specific social groups, raising ethical concerns and limiting their wider adoption. This paper tackles the challenge of mitigating generative bias in diffusion models while maintaining image quality. We propose FairGen, an adaptive latent guidance mechanism enhanced by an auxiliary memory module, which operates during inference to control the generation distribution. This paradigm allows for flexibility and effectiveness to control the generation at any target level. The latent guidance module dynamically adjusts the direction in the latent space to influence specific attributes, while the memory module tracks prior generation statistics and steers the generation direction to align with the target distribution. To evaluate $FairGen$ comprehensively, we introduce a bias evaluation benchmark tailored for diffusion models, spanning diverse domains such as employment, education, finance, and healthcare, along with complex user-generated prompts. Extensive empirical evaluations demonstrate that FairGen outperforms existing bias mitigation approaches, achieving substantial bias reduction while preserving generation quality (e.g., 31.8% bias score reduction on Stable Diffusion 2 model). Furthermore, FairGen offers precise and flexible control over various properties of the output distribution, enabling nuanced adjustments to the generative process.

1 INTRODUCTION

032 033 034 035 036 037 038 Text-to-image diffusion models [\(Nichol et al., 2021;](#page-11-0) [Saharia et al., 2022\)](#page-11-1) have shown remarkable capabilities when generating photorealistic images from text input, leading to new real-world applications. Notably, stable diffusion models [\(Rombach et al., 2022;](#page-11-2) [Podell et al., 2023;](#page-11-3) [Esser et al., 2024\)](#page-10-0) and DALL-E models [\(Ramesh et al., 2022;](#page-11-4) [Betker et al., 2023\)](#page-10-1) have gained widespread popularity, attracting millions of users from various demographic groups and being utilized in a wide range of contexts, for example, reinforcement-learning based control [\(Pearce et al., 2023;](#page-11-5) [Chi et al., 2023\)](#page-10-2) and life-science [\(Cao et al., 2024;](#page-10-3) [Chung et al., 2022\)](#page-10-4).

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040 041 042 043 044 045 046 047 048 However, the widespread application of diffusion models has raised concerns regarding social biases that may be embedded within the generated outputs, necessitating thorough verification of these outputs and posing challenges to the development of fully automated generation systems. Specifically, a series of benchmark studies [\(Bakr et al., 2023;](#page-10-5) [Lee et al., 2024;](#page-10-6) [Cui et al., 2023;](#page-10-7) [Wan & Chang, 2024;](#page-11-6) [Wan et al., 2024;](#page-11-7) [Luccioni et al., 2023;](#page-11-8) [Naik & Nushi, 2023\)](#page-11-9) have identified gender biases within diffusion models in the context of occupational depictions as well as the underrepresentation of certain social groups such as African Americans. This finding underscores the primary research question of this paper: *How can bias in text-to-image diffusion models be mitigated without compromising the quality of the generated content?*

049 050 051 052 053 Existing approaches to bias mitigation in diffusion models have demonstrated significant limitations, particularly in their inability to effectively and flexibly control the generation distribution to achieve a desired balance (e.g., mirroring the true societal distribution of male and female in generated outputs [\(Luccioni et al., 2023\)](#page-11-8)). Prompt intervention methods [\(Bansal et al., 2022;](#page-10-8) [Fraser et al., 2023;](#page-10-9) [Bianchi](#page-10-10) [et al., 2023\)](#page-10-10), which alter user input prompts, often result in a considerable degradation of generation quality, as measured by the alignment between generated content and the original input text. Similarly,

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071 072 073 074 075 076 Figure 1: Overview of **FairGen**: **FairGen** comprises two key components: the *Indicator Guidance Module* and the *Latent Guidance Module*. The Indicator Guidance Module determines the target attribute to control during the current generation based on past generation statistics stored in the memory module, the input prompt, and the desired target distribution. The Latent Guidance Module computes the latent direction needed to enforce the target attribute, using the current input prompt and the selected attribute.

079 080 081 082 083 084 085 model fine-tuning approaches [\(Orgad et al., 2023;](#page-11-10) [Shen et al., 2023;](#page-11-11) [Zhang et al., 2023\)](#page-11-12) typically involve adjusting the model within a specific subdomain, which compromises the overall generation quality and lacks flexibility, requiring retraining to adapt to different target distributions. Latent intervention techniques [\(Friedrich et al., 2023\)](#page-10-11), which introduce static vectors into the latent space for attribute control, are limited by their inability to dynamically adjust to varying inputs and may prove ineffective with different prompts, i.e. we find that the best latent space control is input prompt dependent.

086 087 088 089 090 091 092 093 094 095 096 097 098 099 100 101 102 103 In this paper, we introduce **FairGen**, an adaptive latent guidance module integrated with an indicator guidance module. This mechanism operates at the inference step of a pre-trained diffusion model, allows for precise control of the generation distribution to meet the desired target distribution, and offers greater flexibility and effectiveness compared to existing methods. We provide the overview of FairGen in Figure [1.](#page-1-0) The latent guidance module computes the latent direction needed to enforce the target attribute, using the current input prompt and the selected attribute. The indicator guidance module determines the target attribute to control during the current generation based on past generation statistics stored in the memory module, the input prompt, and the desired target distribution. In particular, the adaptive latent guidance module takes as input: (1) the user input prompt, (2) the latent representation of the prompt from the diffusion model at a particular step, and (3) the sensitive attributes under consideration. It outputs the right guidance vector direction in the diffusion latent space at that time step for that particular input and attribute. We use a guidance vector orthogonal to the original noise space for an effective control, inspired by related works in sparse or orthogonal vector interpolation [\(Ng et al., 2011;](#page-11-13) [Ortiz-Jimenez et al., 2024\)](#page-11-14). The guidance indicator module takes the inputs listed above, and outputs a scalar direction as guidance, conditioned on an auxiliary module which has records of past generation statistics and the desired generation distribution specified by users. The adaptive latent guidance module and guidance indicator module jointly determine the adaptive guidance direction, leading to a flexible and effective fair generation paradigm.

104 105 106 107 We find that current bias evaluation benchmarks [\(Bakr et al., 2023;](#page-10-5) [Lee et al., 2024;](#page-10-6) [Cui et al., 2023;](#page-10-7) [Wan & Chang, 2024;](#page-11-6) [Wan et al., 2024;](#page-11-7) [Luccioni et al., 2023;](#page-11-8) [Naik & Nushi, 2023\)](#page-11-9) exhibit three major limitations - a narrow range of domains, overly simplistic input prompt structures, and a limited set of attributes. To address these shortcomings, we propose a comprehensive bias evaluation benchmark HBE that encompasses a wider array of domains, prompt structures, and sensitive attributes compared

108 109 110 to previous benchmarks. In summary, HBE provides 3X more target domains with more complex input prompt structures than prior bias evaluation benchmark.

111 112 113 114 115 116 117 118 Our comprehensive empirical evaluation and ablation studies reveal that (1) FairGen outperforms other leading bias mitigation techniques in terms of bias reduction while having superior generation quality scores (31.8% bias score reduction on Stable Diffusion 2 model), (2) FairGen demonstrates greater effectiveness in scenarios involving the interplay of multiple attributes compared to other baseline approaches $(15.4\%$ bias score reduction on Stable Diffusion 2 model), (3) FairGen provides a robust and adaptable mechanism for controlling generation distributions to achieve targeted levels $(25.4\%$ bias score reduction), and (4) each component of FairGen significantly contributes to its overall performance improvements (21.2% bias score reduction for guidance module training).

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2 PRELIMINARIES

We denote the diffusion process indexed by time step t with the diffusion length T by $\{x_t\}_{t=0}^T$. Denoising Diffusion Probabilistic Models (DDPM) [\(Ho et al., 2020\)](#page-10-12) construct a discrete Markov chain $\{x_t\}_{t=0}^T$ at discrete times t following $p(x_t|x_{t-1}) \sim \mathcal{N}(x_t; \sqrt{1-\beta_t}x_{t-1}, \beta_t \mathbf{I})$ where β_t is a sequence of positive noise scales (e.g., chosen based on linear scheduling, cosine scheduling). With $\alpha_t := 1 - \beta_t$, $\bar{\alpha}_t := \prod_{s=1}^t \alpha_s$, and $\sigma_t = \sqrt{\beta_t(1 - \bar{\alpha}_{t-1})/(1 - \bar{\alpha}_t)}$, the reverse (sampling) process can be formulated as:

$$
\mathbf{x}_{t-1} = \frac{1}{\sqrt{\alpha_t}} \left(\mathbf{x}_t - \frac{1 - \alpha_t}{\sqrt{1 - \bar{\alpha}_t}} \boldsymbol{\epsilon}_{\theta}(\mathbf{x}_t, t) \right) + \sigma_t \mathbf{z}
$$
(1)

where z is drawn from $\mathcal{N}(\mathbf{0}, \mathbf{I})$. ϵ_{θ} parameterized with θ is the model that approximates the perturbation ϵ in the diffusion process and is trained via the *density gradient loss* \mathcal{L}_d :

> $\mathcal{L}_d = \mathbb{E}_{t,\boldsymbol{\epsilon}} \left[\frac{\beta_t^2}{2\sigma_t^2\alpha_t(1-\bar{\alpha}_t)}\|\boldsymbol{\epsilon} - \boldsymbol{\epsilon}_{\theta}(\sqrt{\bar{\alpha}_t}\mathbf{x}_0 + \sqrt{1-\bar{\alpha}_t}\boldsymbol{\epsilon},t)\|_2^2 \right]$ (2)

where ϵ is drawn from $\mathcal{N}(\mathbf{0}, \mathbf{I})$ and t is uniformly sampled from $[T] := \{1, 2, ..., T\}$.

Since we mainly consider the text-conditioned diffusion model, we notate the perturbation estimator $\epsilon_{\theta}(x_t, t, c)$, where additional argument for text conditions c is also fed into the estimator for denoising, following [\(Ho & Salimans, 2022\)](#page-10-13).

3 FAIRGEN

144 145 146 147 148 In this section, we illustrate our fair diffusion model generation pipeline FairGen. In Section [3.1,](#page-2-0) we provide the overview of FairGen which consists of a latent guidance module and an indicator guidance module. In Section [3.2,](#page-3-0) we illustrate the latent guidance module which computes latent direction to enforce the target attribute. In Section [3.3,](#page-4-0) we show the indicator guidance module which provides scalar control signal to select the target attribute to be enforced and a memory module.

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3.1 OVERVIEW OF FAIRGEN

152 153 154 155 156 157 We observe that the existing bias mitigation method with modified input prompts [\(Bakr et al., 2023;](#page-10-5) [Lee et al., 2024;](#page-10-6) [Cui et al., 2023;](#page-10-7) [Wan & Chang, 2024;](#page-11-6) [Wan et al., 2024;](#page-11-7) [Luccioni et al., 2023;](#page-11-8) [Naik &](#page-11-9) [Nushi, 2023\)](#page-11-9) will degrade the generation quality, while finetuning-based method [\(Orgad et al., 2023;](#page-11-10) [Shen et al., 2023;](#page-11-11) [Zhang et al., 2023\)](#page-11-12) also degrades image quality and requires additional training to adapt to different target generation distributions (e.g., different portions of males vs. females). Therefore, we propose FairGen to impose fair generations via guidance in diffusion latent space.

158 159 160 161 Note that a sufficient condition to control the generation distribution is to control the sensitive attribute of individual generations. Specifically, if we are able to control the gender of each generation, then we should also be able to control the overall gender distribution in outputs with additional memory mechanism. To achieve that, FairGen adds latent guidance in addition to the noise estimate by diffusion models $\epsilon_\theta(x_t, t, c)$. Formally, the updated FairGen-guided noise estimate

162 163 $\epsilon_{\text{FairGen}}(\boldsymbol{x}_t, t, c)$ can be formulated as:

$$
\epsilon_{\text{FairGen}}(\boldsymbol{x}_t, t, \boldsymbol{c}) = \epsilon_{\theta}(\boldsymbol{x}_t, t, \boldsymbol{c}) + \underbrace{I(\boldsymbol{c}, \mathcal{M}, (a_1, a_2))}_{\text{Indication Gulance Scalar} } \cdot \underbrace{f_{\text{ALD}}(\boldsymbol{x}_t, \boldsymbol{c}, (a_1, a_2))}_{\text{Adaptive Latent Guidance Direction}} \tag{3}
$$

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Here, c is the input prompt as text conditions, and a_1 and a_2 are two feasible attributes (e.g., "male" and "female" for gender attribute). The function $I(c, \mathcal{M}, (a_1, a_2))$ represents the indicator guidance model that determines the scalar for the guidance direction (e.g., 1 denoting male generation guidance, -1 denoting female generation guidance), based on memory module M. The function $f_{\text{ALD}}(x^t, c, (a_1, a_2))$ denotes the noise estimate used to edit the attribute a_1 towards the attribute a_2 , given the latent variable x_t and the prompt c.

This formulation can be generalized to multiple multi-dimensional attributes as follows:

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\epsilon_{\text{FairGen}}(\boldsymbol{x}_t, t, \boldsymbol{c}) = \epsilon_{\theta}(\boldsymbol{x}_t, t, \boldsymbol{c}) + \sum_{\mathcal{A} \in \mathcal{A}} \sum_{a_i, a_j \in \mathcal{A}} \underbrace{I(\boldsymbol{c}, \mathcal{M}, (a_i, a_j))}_{\text{Indication Guidance Scalar}\; \text{Adaptive Latent Guidance Direction}} \tag{4}
$$

179 180 In this generalized form, $\mathcal A$ is a set of multi-dimensional attribute groups (e.g., gender, race, age), and a_i and a_j are attributes within the same attribute group A. A diagram illustrating the overview of the proposed method can be found in Figure [1.](#page-1-0)

3.2 ADAPTIVE LATENT GUIDANCE MODULE

184 185 186 187 188 In this part, we will illustrate how FairGen generates the adaptive latent guidance direction $f_{\text{ALD}}(x_t, c, (a_i, a_j))$. One straightforward thought can be imposing classifier guidance at each time step, but we adopt a classifier-free way here for better flexibility. Specifically, we view the adaptive latent guidance direction as the vector difference between the direction towards attribute a_i and the direction towards attribute a_i . This process can be formulated as:

$$
f_{\text{ALD}}(\boldsymbol{x}_t, \boldsymbol{c}, (a_i, a_j)) = \boldsymbol{\epsilon}_{\theta}(\boldsymbol{x}_t, t, K(\boldsymbol{c}, a_i)) - \boldsymbol{\epsilon}_{\theta}(\boldsymbol{x}_t, t, K(\boldsymbol{c}, a_j))
$$
(5)

192 193 194 195 where $K(c, a_i)$ and $K(c, a_j)$ are the attribute-aware text conditions derived from the original text condition and target attribute a_i or a_j . Specifically, if the input prompt c is "A computer programmer works hard in office", the expected attribute-aware text condition $K(c, female)$ would be "A female" computer programmer works hard in office".

196 197 198 199 200 201 To achieve the attribute-aware text condition generation, we train a language model L for prompt editing. Since we tend to need the guidance towards attribute a_i and a_j simultaneously, we train a single language model L to output the attribute-aware guidance prompts $K(c, a_i)$ and $K(c, a_i)$ simultaneously. Formally, we train a language model which takes original prompt c and target attributes a_i, a_j as input and outputs the corresponding guidance prompts:

$$
K(\mathbf{c}, a_i), K(\mathbf{c}, a_j) \leftarrow L(\mathbf{c}, a_i, a_j) \tag{6}
$$

204 205 206 207 208 This paradigm ensures that the guidance prompts $K(c, a_i)$ and $K(c, a_j)$ are similar so that $\epsilon_{\theta}(x_t, t, K(c, a_i))$ and $\epsilon_{\theta}(x_t, t, K(c, a_i))$ lies in the same space and their difference demonstrates orthogonality to the diffusion noise estimate direction $\epsilon_{\theta}(x_t, t, c)$. This concept is inspired by findings in multi-task learning literature, where such orthogonal directions often lead to more effective generalization and task-specific adaptation [Wang et al.](#page-11-15) [\(2023\)](#page-11-15).

209 210 211 212 213 214 215 Specifically, we finetune Mistral-7B-Instruct-v0.2 model with the training set of our **HBE** dataset, which presents a holistic bias evaluation data instances across diverse domains and sensitive attributes with multiple input prompt templates (details in Section [4\)](#page-5-0). The model training consists of two phases: supervised fine-tuning (SFT) and direct preference optimization (DPO) [\(Rafailov et al., 2024\)](#page-11-16). In the SFT phase, we leverage the attribute-aware (i.e., gender, race, age) guidance prompts during data construction of HBE. We specify the attribute editing task in the input instructions and ask the language model to output pairs of guidance prompts corresponding to attribute a_i and a_j . Then we apply LoRA [\(Hu et al., 2021\)](#page-10-14) to fine-tune model L with the annotated

216 217 218 219 220 221 222 223 instances. The supervised fine-tuning process ensures that L learns from labeled data to produce accurate mappings. In the DPO phase, based on model L after SFT, we collect a bunch of output guidance prompts and evaluate them on the validation set of HBE. We assign each pair of output guidance prompts a utility score which measures the effectiveness of controlling target attributes and generated image quality. We use these scores and 50% quantiles to annotate positive and negative outputs. Then, we apply DPO to further refine L to prioritize the guidance directions that align best with the desired noise estimates. This dual approach enables L to generate high-quality and contextually relevant guidance, enhancing the performance of the adaptive latent guidance model.

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3.3 INDICATOR GUIDANCE MODULE

228 229 230 231 232 In this part, we mainly illustrate how FairGen generates the indicator guidance scalor $I(c, \mathcal{M}, (a_i, a_j)) \in \{+1, -1\}$. Basically, it determines which attribute the current generation will push towards (+1 for attribute a_i and -1 for attribute a_j) and which attribute it will push away from the other attribute. The decision process adaptively depends on current text condition prompt c and the memory with past generation statistics records M .

233 234 235 236 237 238 239 240 Baseline indicator guidance: probabilistic generation. Prior bias mitigation methods [\(Bansal et al.,](#page-10-8) [2022;](#page-10-8) [Fraser et al., 2023;](#page-10-9) [Bianchi et al., 2023;](#page-10-10) [Friedrich et al., 2023\)](#page-10-11) apply a probabilistic generation paradigm to enforce the target generation distribution. Concretely, if the target portion of females is P_t , then with probability P_t , they enforce a female generation at this round and otherwise enforce a male generation. However, such a paradigm shows undesirably variance, especially in the case that the desired attribute may not be precisely enforced. Moreover, the indicator decision is also not adaptive to input prompt, making it hard to control fair generations for different prompts with the same objective.

241 242 243 244 245 246 247 248 249 250 251 252 253 254 255 256 257 258 259 260 261 262 263 Indicator guidance in **FairGen**. We leverage a structured memory module-based determination mechanism that dynamically adapts to the context of each prompt. This memory module $\mathcal M$ maintains a record of query features, which are extracted using a feature extractor E , and clusters representing different contexts. The purpose of this memory is to allow the model to provide context-aware guidance based on the prompt's specific characteristics. It achieves this by organizing past feature representations into clusters, which are updated over time to improve the diversity and richness of the guidance offered. The memory operates within a predefined budget B , meaning that it can only store a limited number (up to B) of clusters. When a new prompt c is processed, its features $E(c)$ are compared against the existing clusters. If a match is found (i.e., ℓ_2 distance below a predefined threshold), the model generates outputs conditioned on the cluster's statistical properties. Concretely, the statistical property is the portion of generations for different target attributes. The conditional generation is according to the past generation statistics and the target distribution P_t . For instance, if we aim to achieve a balanced generation of males and females for computer programmer cluster and the past generation shows more males, then the mechanism determines females as the target attribute for the current generation. If no suitable cluster exists and the memory budget permits, a new cluster is created for the prompt's feature. Once the budget is exhausted, K-nearest neighbor (KNN) clustering is used to reallocate memory resources, ensuring the most relevant clusters are maintained. Each time a cluster is used for generation, its statistical properties are updated to reflect the latest output, allowing the memory module to evolve in line with the diversity of inputs. In practice, we prompt LLM to output the main objective in input prompt (e.g., "computer programmer") to extract the query features. In this way, different prompts regarding the same objective will clearly be mapped into the same cluster for subsequence generations as below.

264 265 266 267 268 Once we match the prompt c to a specific cluster, we will compare the past generation statistics with the target distribution level. The attribute that is more underrepresented among a_i and a_j will be enforced in generation in this round. For instance, the input prompt in Figure [1](#page-1-0) will be mapped into the cluster corresponding to the computer programmer and if all past generations are males, our indicator module will enforce a female generation in this round.

269 In Appendix [C,](#page-12-0) we provide the analysis of the variance of baseline indicator guidance and $FairGen$ memory-based guidance. We show that the variance of baseline guidance is sensitive to the precision

270 271 272 273 274 275 276 Table 1: Comparison between HBE benchmark and existing diffusion model bias evaluation benchmarks, including HRS [\(Bakr et al., 2023\)](#page-10-5), PST [\(Wan & Chang, 2024\)](#page-11-6), HEIM [\(Lee et al., 2024\)](#page-10-6), StableBias [\(Luccioni et al., 2023\)](#page-11-8), MMDT [\(Anonymous, 2024\)](#page-10-15), and SBE [\(Naik & Nushi, 2023\)](#page-11-9). We conduct the comparisons for target domains including occupation (occ), education (edu), healthcare (hea), criminal justice (cri), finance (fin), politics (pol), technology (tec), sports (spo), daily activities (act), trains (tra), prompt structures in the benchmark including simple phrases (phrase) and complex scenario descriptions (complex), and considered sensitive attributes: gender (G), race (R), age (A).

of guidance effectiveness and can be exploded easily, while the variance of FairGen memory-based guidance is more stable and effective.

4 HOLISTIC BIAS EVALUATION BENCHMARK (HBE)

293 294 295 296 297 298 299 300 301 302 303 304 305 To fairly evaluate the bias of diffusion models, it is important to make ensure the benchmark is reasonable and comprehensive. Current bias evaluation benchmarks exhibit three major limitations: 1) they are predominantly focused on a narrow range of domains, especially in the context of occupations, which are not representative of the broader diversity of domains. For example, benchmarks like HRS [\(Bakr et al., 2023\)](#page-10-5) and PST [\(Wan & Chang, 2024\)](#page-11-6) solely target occupation-based biases, while neglecting crucial domains such as healthcare, finance, and daily activities; 2) they rely on overly simplistic input prompt structures (e.g., a photo described as <attribute>), which fail to reflect the complexity of real-world user input that often involves more intricate descriptions. Most benchmarks such as HEIM [\(Lee et al., 2024\)](#page-10-6) and StableBias [\(Luccioni et al., 2023\)](#page-11-8) focus exclusively on simple phrases, offering no challenge in terms of interpreting prompts with more complex, scenario-based descriptions. 3) a large portion of benchmarks [\(Wan & Chang, 2024;](#page-11-6) [Lee](#page-10-6) [et al., 2024\)](#page-10-6) primarily consider a limited set of attributes, focusing mostly on gender and race while neglecting other critical sensitive attributes, such as age.

306 307 308 309 310 311 312 313 314 315 316 To address these shortcomings, we propose a comprehensive bias evaluation benchmark, HBE, that encompasses a wider array of domains, prompt structures, and sensitive attributes compared to previous benchmarks. Specifically, we develop a set of 2,000 prompts that span diverse domains, including occupations, education, healthcare, criminal justice, finance, politics, technology, sports, daily activities, and traits. Our benchmark uniquely addresses domains that have been underexplored, such as criminal justice, technology, and finance, ensuring that bias evaluation extends into areas that reflect societal structures more fully. Furthermore, our benchmark includes complex prompt structures, such as scenarios involving detailed descriptions, which present a more challenging evaluation than static prompts that simply describe an individual. Unlike other benchmarks that rely solely on simplistic prompts, HBE incorporates both simple and complex input structures to better simulate real-world user interactions.

317 318 319 320 321 We construct the dataset following these steps: (1) we use Mistral-7B-Instruct-v0.2 model to identify the objectives that can be considered in different domains (e.g., different diseases in healthcare domains, different political positions in the politics domain); (2) we then use the same Mistral model to construct scenarios involving the objective as the input prompts; and (3) we finally partition the 2000 prompts into training set, validation set and test set with 40%, 10%, 50% portions.

322 323 We also compare our benchmark to existing benchmarks, highlighting its comprehensive coverage of domains and prompt structures that set it apart from the existing bias evaluation standards in Table [1.](#page-5-1) We provide some selective examples across diverse domains in Table [8](#page-12-1) in Appendix [A.](#page-12-2)

| | | Gender | | Race | | Age | | Gender+Race+Age | |
|-------|----------------------|--------|-------|-------|-------|-------|-------|-----------------|-------|
| Model | Method | В | Q | В | Q | B | Q | B | Q |
| SD2 | Vanilla generation | 0.734 | 0.276 | 0.500 | 0.276 | 0.894 | 0.276 | 0.709 | 0.276 |
| | Prompt intervention | 0.508 | 0.247 | 0.379 | 0.240 | 0.749 | 0.243 | 0.792 | 0.256 |
| | Finetune-based | 0.339 | 0.228 | 0.257 | 0.232 | 0.734 | 0.243 | 0.732 | 0.227 |
| | FairDiffusion | 0.714 | 0.260 | 0.364 | 0.258 | 0.729 | 0.257 | 0.682 | 0.248 |
| | FairGen | 0.231 | 0.270 | 0.217 | 0.262 | 0.683 | 0.272 | 0.601 | 0.267 |
| | Vanilla generation | 0.730 | 0.296 | 0.718 | 0.296 | 0.829 | 0.296 | 0.759 | 0.296 |
| SDXL | Prompt intervention | 0.483 | 0.279 | 0.364 | 0.284 | 0.784 | 0.285 | 0.746 | 0.289 |
| | Finetune-based | 0.302 | 0.269 | 0.286 | 0.273 | 0.638 | 0.254 | 0.683 | 0.287 |
| | FairDiffusion | 0.452 | 0.286 | 0.334 | 0.288 | 0.675 | 0.277 | 0.723 | 0.250 |
| | FairGen | 0.267 | 0.293 | 0.257 | 0.290 | 0.604 | 0.287 | 0.658 | 0.257 |

324 325 326 Table 2: Bias score $B(\downarrow)$ and quality score $Q(\uparrow)$ on our HBE benchmark on two types of text-toimage diffusion models stable diffusion 2 (SD2) and stable diffusion XL (SDXL) across different sensitive attributes and the combination of them.

Table 3: Bias scores $B(\downarrow)$ for different target portion P_t of attribute male on HBE benchmark. The average (Avg) and standard deviation (Std) of the bias scores are also reported.

| Target portion P_t 0.0 0.2 | | | 0.4 | 0.6 | 0.8 | | 1.0 Avg | Std |
|--|-------|-------|-------|-------------------------|-------|---|-------------|-------|
| Vanilla generation 0.982 0.863 0.772 0.673 0.583 0.482 0.726 | | | | | | | | 0.168 |
| Prompt intervention $\begin{array}{ ccc } 0.745 & 0.635 & 0.554 & 0.473 & 0.332 \end{array}$ | | | | | | $0.255 \; \; 0.499$ | | 0.168 |
| Finetune-based \vert 0.372 | | | | | | 0.356 0.332 0.305 0.285 0.264 0.319 | | 0.038 |
| FairDiffusion | 0.836 | 0.802 | 0.734 | 0.623 | 0.602 | 0.553 | 0.692 | 0.105 |
| FairGen | 0.272 | 0.261 | | 0.248 0.228 0.219 | | 0.201 ± 0.238 | | 0.025 |

5 EXPERIMENTS

5.1 EVALUATION SETUP

354 355 356 357 358 359 Fairness evaluation metrics. We employ two different metrics group bias score B and quality score Q to measure the fairness of text-to-image models and the quality of generated images, respectively. The group bias score B measures the absolute difference between the actual portions and the target portions in the generations. The quality score Q measures the conformity of the generated images to the user input prompt. Concretely, we use the CLIP score between the generated images and the user input prompt as the quality score Q in the evaluations.

360 361 362 363 364 More formally, we denote the text-to-image model mapping as $M(\cdot): \mathcal{V} \mapsto \mathcal{Y}$, where V is the text space and $\mathcal Y$ is the image space for text-to-image models. We denote all possible values for a sensitive attribute as a set A (e.g., $A = \{male, female\}$ for gender). We use $v_i \in V$ ($i \in \{1, ..., n\}$) to denote n test data samples. We use a discriminator $D: \mathcal{Y} \mapsto \mathcal{A}$ to identify the sensitive attributes of generations. Then, the group bias score B can be formulated as:

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B = \frac{1}{n} \sum_{i=1}^{n} \mathbb{E}_{a_k, a_j \in \mathcal{A}, a_k \neq a_j} \left[\left| \mathbb{P} \left[D(M(v_i)) = a_k \right] - \mathbb{P} \left[D(M(v_i)) = a_j \right] \right| \right],\tag{7}
$$

369 370 371 Here, the probability $\mathbb{P}[\cdot]$ is estimated by Monte-Carlo methods with T times of sampling (T = 10) across the evaluations). In the multi-attribute controlling case, we further take the expectation over the sets of sensitive attributes.

372 373 374 375 376 377 Dataset & models. We evaluate FairGen and other strong bias mitigation baselines on stable bias dataset [\(Luccioni et al., 2023\)](#page-11-8) and our comprehensive bias evaluation benchmark HBE, introduced in Section [4.](#page-5-0) We consider two types of text-to-image diffusion models: stable diffusion 2 model (SD2) [\(Rombach et al., 2022\)](#page-11-2) and stable diffusion XL model (SDXL) [\(Podell et al., 2023\)](#page-11-3). We implemented the attribute discrimination model $D(\cdot)$ by question-answering form with vision-language model InstructBLIP-2, following [\(Luccioni et al., 2023;](#page-11-8) [Bakr et al., 2023\)](#page-10-5). We also validate the efficacy of the attribute discrimination model in Table [9](#page-12-3) in Appendix [B.](#page-12-4)

378 5.2 BIAS EVALUATION OF FAIRGEN

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381 382 383 384 385 386 387 388 389 390 391 392 393 394 395 396 397 398 We compare FairGen with the following strong baselines in bias mitigation: (1) vanilla generation via classifier-free guidance [\(Nichol et al., 2021\)](#page-11-0), (2) prompt intervention based baseline [\(Bansal](#page-10-8) [et al., 2022\)](#page-10-8), (3) finetuning-based method with distribution alignment loss [\(Shen et al., 2023\)](#page-11-11), and (4) latent intervention-based method [\(Friedrich et al., 2023\)](#page-10-11). The prompt intervention methods modify the input prompts with attribute specification and adopt probabilistic generation to achieve target distribution. The finetuning-based methods fine-tune the diffusion model on a fair distribution with distribution-alignment loss. The latent intervention methods impose a static global attribute direction for controlling. Table [2](#page-6-0) demonstrates the bias reduction capabilities and generation quality of FairGen on two types of text-to-image diffusion models, Stable Diffusion 2 (SD2) and Stable Diffusion XL (SDXL), across sensitive attributes such as gender, race, age, and their combination. The bias score B (lower is better) and quality score Q (higher is better) are evaluated for various bias mitigation methods. Across all sensitive attributes and their combinations, FairGen consistently achieves the lowest bias scores, indicating its superior ability to mitigate bias compared to other approaches. For instance, in the case of gender bias, FairGen achieves a bias score of 0.231 for SD2 and 0.267 for SDXL, significantly outperforming the other baselines. Similarly, when considering the combination of gender, race, and age, FairGen maintains the lowest bias scores while preserving generation quality. Notably, F airGen also sustains high generation quality, with Q scores that are competitive with or superior to vanilla generation (soft upper bound of quality scores without any interventions). These results underline FairGen's ability to balance bias mitigation with image generation quality, especially in complex scenarios involving multiple intersecting sensitive attributes.

399 400 401 Table [4](#page-7-0) presents the bias score B and quality score Q for various bias mitigation methods evaluated on the stable bias occupation dataset [\(Luccioni et al., 2023\)](#page-11-8).

402 403 404 405 406 407 408 409 410 Among all methods, FairGen demonstrates the most significant bias reduction, achieving a bias score of 0.160, which is substantially lower than the other baselines. This again indicates its superior performance in mitigating bias in various datasets. While the finetune-based method also shows notable bias reduction with a score of 0.392, FairGen surpasses it by a large margin and is also more flexible to the change of target portions. Additionally, FairGen maintains a high generation quality score ($Q = 0.297$), which is com-

Table 4: Bias score $B(\downarrow)$ and quality score $Q(\uparrow)$ on stable bias occupation dataset.

411 412 413 petitive with vanilla generation ($Q = 0.303$) and higher than most other approaches. This indicates that FairGen strikes an effective balance between minimizing bias and preserving image quality.

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415 5.3 ABLATION STUDY

5.3.1 EFFECTIVENESS OF FAIRGEN WITH DIFFERENT TARGET GENERATION DISTRIBUTIONS

419 420 421 422 423 424 425 426 427 428 429 430 431 It is important to note that the desired generation distribution may not be exactly balanced. We sometimes also expect that the distribution reflects the real-world distribution. It requires the flexibility of bias mitigation methods to control the generation portions at particular levels. Therefore, we also evaluate FairGen and other strong bias mitigation baselines with different target portions. The results in Table [3](#page-6-1) demonstrate that FairGen provides a robust and adaptable mechanism for controlling generation distributions to achieve targeted levels since the average bias is lower than other baselines at all levels. Specifically, FairGen demonstrates both the lowest average bias score and the smallest standard deviation, which indicates that it consistently maintains a low bias across different target portions. This stability is critical, as it suggests that FairGen is not only effective at minimizing bias on average but also performs reliably across a wide range of scenarios. In contrast, while the finetune-based approach achieves relatively low bias scores, its standard deviation is notably higher than that of FairGen. This higher variability implies that the finetune-based approach may be less predictable or stable when applied across different target portions. Methods like Vanilla generation and FairDiffusion also exhibit higher standard deviations, indicating a less consistent ability to manage bias across the different target portions.

432 433 5.3.2 EFFECTIVENESS OF SFT AND DPO

434 435 436 437 438 439 440 441 442 443 444 During the training of guidance prompt generation model in Section [3.2,](#page-3-0) we leverage a dual-phase mechanism: SFT which imposes attribute-aware prompt generation and DPO which further refines model with fairness generation utility feedback. In this part, we directly verify the effectiveness of SFT and DPO. We prompt LLM to add attribute specification as a baseline and compare it with FairGen (SFT) and FairGen (SFT+DPO). As shown in Table [5,](#page-8-0) the baseline LLM prompting achieves a bias score B of 0.203 and a quality score Q of 0.298. When SFT is applied, we observe a reduction in bias to 0.168 while maintaining a similar

Table 5: Effectiveness of SFT and DPO in the training of the adaptive latent guidance module on Stable bias occupation dataset.

445 446 447 448 449 quality score of 0.299, indicating that SFT benefits LLM capacity for attribute-aware guidance prompt generation. Furthermore, adding DPO to SFT further reduces the bias score to 0.160, while keeping the fairness quality virtually unchanged, suggesting that DPO enhances the model by including additional feedback on quality of guidance prompts, which benefits the model to capture more nuanced correlations between prompt structures and fairness utilities.

5.3.3 FAIRGEN WITH DIFFERENT DIFFUSION TIME STEPS

452 453 454 455 456 457 458 459 460 In this part, we explore the impact of diffusion time steps to apply FairGen guidance on the effectiveness of bias mitigation and generation quality. The results in Table [6](#page-8-1) demonstrate that applying latent guidance at the early diffusion stage (within the first 25% time steps) will not effectively guide fair generations since later denoising will downplay the early guidance, while applying guidance at a later stage (last 25% time steps) only will degrade the align-

Table 6: Effectiveness of applying FairGen at different diffusion time steps on HBE benchmark with gender as sensitive attributes.

461 462 463 ment between generated images and input text. Therefore, we adopt guidance at the intermediate stage (middle 25% time steps) which achieves better tradeoffs between bias mitigation effectiveness and generation quality.

5.4 RUNTIME EVALUATION

Table 7: Comparison of runtime (hours) between **FairGen** and other bias mitigation baselines on stable diffusion 2 model on HBE benchmark. instance wise runtime

We also evaluate the runtime of **FairGen** and other bias mitigation baselines in both the training phase and inference phase in Table [7.](#page-8-2) As a training-free method, **FairGen** induces no training computational costs. In the inference stage, although **FairGen** induces $1 + 2|\mathcal{A}|$ noises estimates in each diffusion step, where $|\mathcal{A}|$ is the number of sensitive attributes, the adaptive guidance is only enforced at a small portion of intermediate diffusion steps (details in Section [5.3.3\)](#page-8-3). Additionally, the noise estimates for different attributes are independent and parallelized in the inference. Therefore, **FairGen** only leads to marginal runtime overhead compared to the baselines while mitigating the bias significantly.

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5.5 VISUALIZATION EXAMPLES

485 In Figure [2,](#page-9-0) we present a series of image generations produced by **FairGen**, demonstrating its ability to precisely control the gender attribute while maintaining a high level of image fidelity.

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Figure 2: Image generations by FairGen to control a balanced gender distribution.

The figure highlights several key aspects of our model's capabilities: (1) **FairGen** effectively adjusts the gender attribute across all generations, ensuring a balanced distribution between male and female representations. (2) The generated images exhibit high fidelity, preserving fine details in both the subjects and their surrounding environment. This demonstrates the robustness of **FairGen** in generating photorealistic images, even under conditions where specific attributes (e.g., gender) are modified. (3) Importantly, **FairGen** is able to control gender attributes without intervening with the background elements or scene composition.

6 RELATED WORK

504 505 506 507 508 509 510 511 512 513 514 Bias mitigation in diffusion models. Several approaches have been proposed to mitigate bias in text-to-image models, typically focusing either by refining model weights [\(Orgad et al., 2023;](#page-11-10) [Shen](#page-11-11) [et al., 2023;](#page-11-11) [Zhang et al., 2023\)](#page-11-12) or optimizing prompts and generation processes [\(Bansal et al., 2022;](#page-10-8) [Fraser et al., 2023;](#page-10-9) [Bianchi et al., 2023\)](#page-10-10). However, these methods often compromise the quality of the generated images and lack the flexibility to address a wide range of sensitive attributes. A closely related approach or our FairGen, FairDiffusion [Friedrich et al.](#page-10-11) [\(2023\)](#page-10-11), employs guidance generation to control attributes, but it relies on a static, global attribute direction. We show that this makes it insufficiently adaptive to varying input prompts. In this paper, we introduce an adaptive latent guidance method, where we train a guidance prompter model capable of dynamically and flexibly controlling different generation attributes, allowing for more effective bias mitigation without sacrificing generation quality.

515 516 517 518 519 520 521 522 523 524 525 526 527 528 529 530 531 Bias evaluation in diffusion models. The presence of unfairness and bias in text-to-image diffusion models can perpetuate harmful stereotypes and degrade model value by reinforcing spurious correlations, which limits the widespread and responsible deployment of these models. Current fairness evaluations for text-to-image models mainly consider input prompts which target a narrow set of attributes or domains, such as occupations or physical characteristics [\(Bakr et al., 2023;](#page-10-5) [Lee et al.,](#page-10-6) [2024;](#page-10-6) [Cui et al., 2023;](#page-10-7) [Wan & Chang, 2024;](#page-11-6) [Wan et al., 2024;](#page-11-7) [Luccioni et al., 2023;](#page-11-8) [Naik & Nushi,](#page-11-9) [2023\)](#page-11-9). For instance, HRS [\(Bakr et al., 2023\)](#page-10-5) and PST [\(Wan & Chang, 2024\)](#page-11-6) predominantly examine occupation-based biases, overlooking important sectors like healthcare, finance, and everyday activities. Additionally, benchmarks like HEIM [\(Lee et al., 2024\)](#page-10-6) and StableBias [\(Luccioni et al., 2023\)](#page-11-8) are based on overly simplified prompt structures (e.g., <attribute> photo), which fail to capture the complexity and nuance of real-world user inputs, which often contain richer, scenario-based descriptions. Many evaluations, such as those in [\(Wan & Chang, 2024;](#page-11-6) [Lee et al., 2024\)](#page-10-6), limit their scope to a small set of sensitive attributes, primarily focusing on gender and race, while neglecting other critical attributes like age. In contrast, we introduce a more comprehensive, representative, and stereotype-aware fairness evaluation benchmark. This benchmark covers a broader range of sensitive attributes and domains, sampled from realistic statistical distributions and rigorously filtered. Our evaluations reveal that even models that have undergone extensive debiasing processes continue to exhibit significant bias and fairness issues when tested against this benchmark.

532 533 534 535 536 537 538 539 Conclusion In conclusion, the proposed F a i r Gen presents a significant advancement in addressing the challenge of generative bias in diffusion models. By integrating an adaptive latent guidance mechanism with an auxiliary memory module, $FairGen$ not only mitigates bias but also maintains high-quality image generation. The dynamic adjustment of latent space attributes and the use of past generation statistics for informed guidance have proven to be effective strategies in controlling generation distribution. Through extensive evaluations across various domains, FairGen has demonstrated superior performance in reducing bias compared to existing techniques, while also offering precise and flexible control over targeted distributions. This work paves the way for more equitable and socially responsible applications of diffusion models in real-world scenarios.

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A SELECTIVE EXAMPLES ON HBE BENCHMARK

Table 8: Selective examples on HBE benchmark across different domains.

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681 682

B EFFICACY OF MODEL JUDGE

683 684 685 686 687 688 689 690 691 692 Across the evaluations, we detect the attributes of persons in generated images by performing question-answering with the InstructBLIP-2 model. Specifically, we directly ask the visionlanguage model to do a classification task for gender, race, or age. In this part, we evaluate the alignment between the model judge and the human judge. Using Amazon Sagemaker GroundTruth platform, we invited Amazon Mechnical Turk workers to annotate the gender, race, and age for 100 images. For each of the 100 images, we obtained the labels across different sensitive attributes. We then computed the efficacy of model judge in Table [9.](#page-12-3) The results show that model judge by

Table 9: Evaluation of the precision of attribute discrimination model.

693 InstructBLIP-2 shows overall desirable attribute detection performance.

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C THEORETICAL ANALYSIS

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698 C.1 ANALYSIS OF PROBABILISTIC GENERATION

699 700 701 Consider a binary-attribute case with sensitive attributes a_1, a_2 . Suppose that we want to control the target portion of generation with attribute a_1 to be P_t . Further suppose that the precision of the generation-evaluation framework is p and the recall is r . Let n be the total number of generations (sample size).

702 703 We can derive the expected number of true positives and negatives generated to be:

$$
TP = pP_t n \tag{8}
$$

$$
TN = \left(1 - P_t - \frac{pP_t}{r} + pP_t\right)n\tag{9}
$$

707 708 709 Let X be the number of generations with attribute a_1 , then we know that X is a Bernoulli random variable drawn from Binomial $(n, \frac{r}{n})$ $\frac{1}{p}P_t$) if prompts are i.i.d..

The bias score B is then a random variable $B = |X - (n - X)|/n =$ 2 $\left|\frac{2}{n}X-1\right|$. We can derive the variance of B.

$$
E[B^2] = E\left[\left(\frac{4}{n^2} X^2 - \frac{4}{n} X + 1 \right) \right]
$$
 (10)

$$
=\frac{4}{n^2}E[X^2]-\frac{4}{n}E[X]+1
$$
\n(11)

$$
= \frac{4}{n^2} \left(n p_{rp} (1 - p_{rp}) + n^2 p_{rp}^2 \right) - \frac{4}{n} n p_{rp} + 1 \tag{12}
$$

$$
= 1 - 4p_{rp}(1 - p_{rp})\frac{n-1}{n}
$$
\n(13)

Also, we have:

$$
E[B]^2 = \left(\sum_{k=0}^n \left| \frac{2}{n}k - 1 \right| P(X = k)\right)^2
$$
 (14)

Finally, we have:

$$
\mathbb{V}[B] = 1 - 4\frac{r}{p}P_t(1 - \frac{r}{p}P_t)\frac{n-1}{n} - \left(\sum_{k=0}^n \left|\frac{2}{n}k - 1\right| \binom{n}{k} p_{rp}^k (1 - p_{rp})^{n-k}\right)^2 \tag{15}
$$

$$
= 1 - 4p_{rp}(1 - p_{rp})\frac{n-1}{n} - \left(\sum_{k=0}^{n} \left| \frac{2}{n}k - 1 \right| {n \choose k} (\frac{r}{p}P_t)^k (1 - \frac{r}{p}P_t)^{n-k}\right)^2
$$
(16)

736 737 second term can be approximated with Gaussian assumption, we can see later whether we need such simplification

C.2 ANALYSIS OF GUIDANCE INDICATOR MODEL

740 741 742 743 Consider the binary case where we aim to control the sensitive attribute of male or female, we denote P[actually generate a male target is to generate a male] $= p$ and $\mathbb{P}[\text{actually generate a female}]\ = q. \ p \text{ and } q \text{ can be bounded by em-}$ pirical statistics on validation set via concentration inequalities.

744 745 746 747 748 749 We consider a random variable X_i such that $X_i = 1$ if generation i is a male and $X_i = 0$ if generation i is a female. Let $S_n = X_1 + ... + X_n$. Suppose we target a distribution of 50% male-female. According to our algorithm, we have: if $S_k < k/2$, $S_{k+1} = S_k + 1$ w.p. p and $S_{k+1} = S_k$ w.p. $1 - p$; if $S_k \ge k/2$, $S_{k+1} = S_k$ w.p. q and $S_{k+1} = S_k + 1$ w.p. $1 - q$. The target is to analyze the distribution of $S_k - k/2$, which corresponds to how biased the generations have been.

750 751 752 753 Via variable exchange, we can reduce the analysis into solving a biased random walk problem. Consider a random process $\{T_k = S_k - k/2\}$ with $T_0 = 0$. If $T_l \leq 0$, $T_{k+1} = T_k + 0.5$ with probability p and $T_{n+1} = T_n - 0.5$ with probability $1 - p$; If $T_k > 0$, $T_{k+1} = T_k - 0.5$ with probability q and $T_{k+1} = T_k + 0.5$ with probability $1 - q$; Compute the distribution of T_n .

754 When
$$
T_k \leq 0
$$
, the expected change is given by

$$
\mathbb{E}[\Delta T_k | T_k \le 0] = 0.5p - 0.5(1 - p) = p - \frac{1}{2}.
$$

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 Thus, if $p > 0.5$, there is a positive drift, meaning the process tends to increase when $T_k \leq 0$.

When $T_k > 0$, the expected change is given by

$$
\mathbb{E}[\Delta T_k | T_k > 0] = 0.5(1 - q) - 0.5q = \frac{1}{2} - q.
$$

Thus, if $q < 0.5$, there is a negative drift, meaning the process tends to decrease when $T_k > 0$.

The process ${T_k}$ exhibits a drift toward zero:

- When $T_k \leq 0$, the process drifts upward if $p > 0.5$.
- When $T_k > 0$, the process drifts downward if $q < 0.5$.

Thus, in the long term, the process is expected to oscillate around zero. The stationary distribution $f(T_n)$ for large n will be approximately Gaussian, centered around zero, with variance depending on the values of p and q .

 For large n , we have approximately

 $T_n \sim \mathcal{N}(0, \sigma^2),$

where σ^2 is determined by the probabilities p and q and can be computed from the recurrence relations of the random walk.

D PRELIMINARIES

Score-based diffusion models [\(Song et al., 2021\)](#page-11-17) use stochastic differential equations (SDEs). The diffusion process $\{x_t\}_{t=0}^T$ is indexed by a continuous time variable $t \in [0, 1]$. The diffusion process can be formulated as:

$$
d\mathbf{x} = f(\mathbf{x}, t)dt + g(t)d\mathbf{w}
$$
\n(17)

where $f(\mathbf{x},t): \mathbb{R}^n \mapsto \mathbb{R}^n$ is the drift coefficient characterizing the shift of the distribution, $g(t)$ is the diffusion coefficient controlling the noise scales, and w is the standard Wiener process. The reverse process is characterized via the reverse time SDE of Equation [\(17\)](#page-14-0):

$$
d\mathbf{x} = [f(\mathbf{x}, t) - g(t)^2 \nabla_{\mathbf{x}} \log p_t(\mathbf{x})]dt + g(t)d\mathbf{w}
$$
\n(18)

where $\nabla_{\mathbf{x}} \log p_t(\mathbf{x})$ is the time-dependent score function that can be approximated with neural networks s_θ parameterized with θ , which is trained via the score matching loss \mathcal{L}_s :

$$
\mathcal{L}_s = \mathbb{E}_t \left[\lambda(t) \mathbb{E}_{\mathbf{x}_t | \mathbf{x}_0} || \mathbf{s}_\theta(\mathbf{x}_t, t) - \nabla_{\mathbf{x}_t} \log(p(\mathbf{x}_t | \mathbf{x}_0)) ||_2^2 \right]
$$
(19)

 where $\lambda : [0, 1] \to \mathbb{R}$ is a weighting function and t is uniformly sampled over [0, 1].

Since the SDE formulation in Equation [\(17\)](#page-14-0) is typically discretized for numerical computations, we basically consider the discrete process formulation as Equation [\(1\)](#page-2-1) in the following part.

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