Collaborative Performance Prediction for Large Language Models

Anonymous EMNLP submission

Abstract

Comprehensively understanding and accurately 002 predicting the performance of large language models across diverse downstream tasks has emerged as a pivotal challenge in NLP research. 005 The pioneering scaling law on downstream works (Hu et al., 2024; Isik et al., 2024) demon-007 strated intrinsic similarities within model families and utilized such similarities for perfor-009 mance prediction. However, they tend to overlook the similarities between model families 011 and only consider design factors listed in the 012 original scaling law. To overcome these limitations, we introduce a novel framework. Collaborative Performance Prediction (CPP), which significantly enhances prediction accuracy by leveraging the historical performance of var-017 ious models on downstream tasks and other design factors for both model and task. We also collect a collaborative data sourced from 019 online platforms containing both historical performance and additional design factors. With 021 the support of the collaborative data, CPP not only surpasses traditional scaling laws in pre-024 dicting the performance of scaled LLMs but also facilitates a detailed analysis of factor importance, an area previously overlooked.

1 Introduction

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Large Language Models (LLMs) (Brown et al., 2020; Ouyang et al., 2022) have emerged as one of the most important AI research powered by large-scale parameters, high computational resources, and massive training data. With the substantial increase in model sizes, the evaluation cost of LLMs' performance becomes even more significant. For example, testing a single LLM on certain benchmarks often requires \$10K+ and 4K+ GPU hours (Liang et al., 2023). Therefore, understanding the behaviors and predicting the capabilities of LLMs across scales under various tasks becomes a vital question (Ganguli et al., 2022a; Owen, 2024; Finnveden, 2020; Hu et al., 2024) for both researchers and engineers.

Scaling laws (Kaplan et al., 2020; Hoffmann et al., 2022; Hernandez et al., 2022; Gordon et al., 2021; Bahri et al., 2024; Muennighoff et al., 2023) have been powerful tools for predicting the capabilities of LLMs. It indicates a power-law correlation between the model performance and design factors such as computational measure (FLOPs) utilized during training. Although the scaling law was originally proposed as a strong intuitive guide for designing LLM, researchers (Hu et al., 2024; Ruan et al., 2024; Isik et al., 2024) have extended its utility into predicting model performances on various metrics, such as BLEU in Machine Translation, and different tasks. These works can accurately predict model performances by utilizing the similarity within each model family, e.g., models within each family are usually trained on the same dataset. However, there are several issues rooted in their methods: the performance prediction 1) requires transparent design factors that consume substantial training resources to fit the curve, 2) is only tailored to a certain model family and a specific task metric, and 3) neglects the connections among different models and tasks.

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The aforementioned limitations motivate us to design more effective methods for predicting the performance of LLMs on downstream tasks. Two observations sparked our attention. Firstly, A strong similarity exists between model families, e.g., LLama-family and GPT-family. Models from different families behave similarly in prediction distribution (Shrivastava et al., 2023) and emergent phenomenon (Wei et al., 2022). Secondly, with the emerging LLM models and the increasingly diverse tasks, the cost of enumerating and benchmarking models with tasks increases exponentially. Therefore, we aim to utilize the similarities across model families in order to collaboratively predict the model performance over diverse tasks in an accurate yet efficient way.

To incorporate the aforementioned intuitions, we



Figure 1: Framework for Collaborative Performance Prediction of Large Language Models. This schematic delineates two principal components: (1) Collaborative Data, which encompasses a score matrix illustrating the performance of various LLMs across downstream tasks, along with external descriptive factors of both models and tasks; (2) Collaborative Prediction Method, given the model and task IDs to leverage this collaborative data, enabling accurate score prediction.

propose a new scheme, Collaborative Performance Prediction (CPP), to efficiently predict the performance of LLMs on evaluation tasks. This scheme learns the latent representations of LLMs and tasks, which captures the intrinsic similarity among different models and tasks. The interaction (*e.g.*, inner product) between the latent representations of LLMs and tasks can be utilized to predict the performance of LLMs on certain tasks. To fulfil the proposed scheme, we collect the LLM performance data from academic papers, technical reports, and open leaderboards covering 72 models and 29 tasks. To summarize, our scheme has several advantages:

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- Low Training Cost: Compared with methods (Hu et al., 2024) that extend scaling law to various downstream tasks, no pre-training or finetuning of LLM is required in our scheme.
- **Prediction over proprietary model**: Unlike previous methods (Ruan et al., 2024), our scheme supports prediction over proprietary models without knowing key design factors, such as computational measures.
- **Prediction from small to large:** By utilizing cross-family information, our scheme can accurately estimate model performance, *e.g.*, emergent ability, of large models on downstream tasks given the information from small models.
- **Beyond Scaling Laws**: Our scheme is more general and can incorporate diverse factors, such as task description factors.
- Factor-level Interpretability: Our scheme can provide interpretability by analyzing the factors importance of LLMs.

Under our scheme, multiple customized prediction methods (*e.g.*, COLLABORATIVE FITER-ING (Koren et al., 2022)) can be incorporated to predict the performance of LLMs, further validating the feasibility and generality. Our method enables more diverse factors as input, ranging from traditional LLM design factors to task design factors, *e.g.*, targeted ability and few-shot setting. 121

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Upon extensive experimentation within the openreleased core leaderboard of HELM (Liang et al., 2023) and our collected historical matrix, our predictive performance demonstrated exceptionally well. Specifically, even without any input of model factors or task factors: in HELM, we use 50% of the scores to predict the other 50%, the predictive ranking (derived from predicted scores) achieves Accuracy = 10%, and MAE@2 = 39%; in our collected matrix (characterized by a 44% sparsity level) achieves an Accuracy =45%, and the MAE@2 = 84%. Notably, the accuracy of our prediction from small to large LMs significantly exceeded that predicted by scaling laws. Using an analysis method similar to SHAPLEY-VALUES (Lundberg and Lee, 2017; Shapley, 1952), we elucidate the importance of different factors, which surprisingly does not fully align with scaling law (Kaplan et al., 2020). Therefore, our method is undoubtedly more versatile.

2 Related Work

2.1 Downstream Scaling Law and Performance Predictability of LLM

Scaling laws (Kaplan et al., 2020; Hoffmann et al., 2022; Hernandez et al., 2022; Bahri et al., 2024; Muennighoff et al., 2023) for LLMs have increasingly become a focal point in understanding and guiding critical design decisions, such as model size and the characteristics and volume of pre-training data. Traditionally, most research in this area has concentrated on how measures like crossentropy loss or perplexity scale. Subsequent stud-

ies have extended these efforts to the scaling be-157 havior on translation (Isik et al., 2024; Ghorbani 158 et al., 2021; Zhuocheng et al., 2023) and other 159 downstream tasks modeling (Caballero et al., 2023; 160 Henighan et al., 2020). The high predictability 161 in LLMs capability has directly spurred extensive 162 research work (see Survey Anwar et al. (2024)) 163 exploring whether LLMs can demonstrate pre-164 dictability on downstream tasks, which are consid-165 ered highly unpredictable in traditional ML knowl-166 edge (Ganguli et al., 2022a). Particularly, the "emergence" phenomenon (Suzgun et al., 2022; Wei 168 et al., 2022) has challenged predictability, where 169 models suddenly exhibit striking capabilities at 170 specific training reources. Recent studies (Scha-171 effer et al., 2023) have made remarkable achieve-172 ments in breaking the discontinuities in perfor-173 mance brought about by emergence, and Ganguli 174 et al. (2022a); Owen (2024); Finnveden (2020) 175 demonstrated the predictability on downstream 176 tasks, for instance, Hu et al. (2024) directly fits 177 a curve of training resources and downstream task performance by repeatedly pretraining a specific 179 model. Furthermore, Arora and Goyal (2023) pre-180 181 dicted the performance through decomposing the complex capabilities of LMs to some base skills.

> Given that predictability has now been established, we reassess the underlying premises that enable this predictability: the prevailing similarities across multiple models and various downstream tasks (Liu et al., 2023; Perlitz et al., 2024; Polo et al., 2024; Torregrossa et al., 2020; Ilić, 2023). Based on this, we step beyond the limitations defined by scaling laws and propose a new methodology to predict the performance of LLMs on various downstream tasks.

2.2 **Collaborative Filtering**

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Collaborative filtering (CF) (Koren et al., 2022) is a 194 widely used technique in recommendation systems 195 that predicts users' preferences by collecting the historical preferences of many other users. The un-197 derlying assumption of CF is that similar users will 198 share similar preferences on similar items. A sem-199 inal method in CF is matrix factorization (Koren et al., 2009) (MF). It reduces the dimensionality of the user-item matrix by learning the latent factors associated with users and items, respectively. This approach helps handle sparse data and improves scalability. The factorization of the user-item ma-205

trix \mathbf{R} can be represented as

$$\mathbf{R} \approx \mathbf{P}^{\top} \cdot \mathbf{Q} \,, \tag{1}$$

where each column vector in P and Q represents 208 a specific user or item, respectively, with hidden 209 dimension d. The latent representations of users 210 and items capture the user preferences and item 211 properties in the latent space, and the inner product 212 \cdot can be utilized to predict the interaction between 213 users and items. To optimize the latent feature 214 vectors, the following loss function is employed: 215

$$\min_{\mathbf{P},\mathbf{Q}} \quad \sum_{(u,i)\in\Omega} (r_{ui} - \mathbf{p}_u^\top \cdot \mathbf{q}_i)^2, \qquad (2)$$

which measures the squared differences between the observed ratings r_{ui} and the ratings predicted by the model $\mathbf{p}_u^{\top} \cdot \mathbf{q}_i$ for each user-item pair (u, i)in the set Ω of observed interactions.

Here, Yang et al. (2019) transferred the collaborative filtering for ML model selection by predicting the cross-valided errors, which demonstrates CF's adaptability and efficiency in diverse application areas.

Background and Pilot Demonstration 3

Scaling Law on Downstream Tasks 3.1

For classic scaling laws, researchers propose a hypothesized power-law relationship between a model's computational measures C_m (e.g., training FLOPs) and their performance loss L_m (e.g., perplexity). Specifically, for a model m within a family f (e.g., Llama-2 7B, 13B, and 70B), the relationship is hypothesized as

$$\log(L_m) \approx \omega_f \log(C_m) + b_f, \qquad (3)$$

where ω_f and b_f are scaling coefficients customized for each model family. Researchers fit this formula through repeated scaling experiments, then use it to accurately predict performance when larger-scale (C' > C). Some studies (Finnveden, 2020; Owen, 2024) have adapted scaling laws to specific downstream task metrics, proposing that sigmoidal functions are more suitable for predictions, as follows:

$$\sigma^{-1}(S_m) \approx \omega_f \log(C_m) + b_f, \qquad (4)$$

where S_m refers to the normalized downstream scores of models within the range [0, 1]. However, applying scaling laws across different model

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Figure 2: Error Distribution of Predictions (Normalized Score and Rank Derived by Score) Based on the HELM Lite Leaderboard Using Matrix Factorization: We evaluate the effectiveness of Matrix Factorization (MF) using two latent factors, 7 and 10, across 2 training/validation split percentages. Accuracy is defined as the percentage of instances where the predicted rank equals the actual rank. MAE@2 is defined as the percentage of instances where the absolute difference between the predicted rank and the actual rank is 2.

families on various specific tasks presents a tradeoff: fitting unique coefficients for each evaluation scenario (*e.g.*, Llama 2 on MMLU) is a resourceintensive endeavor (Hu et al., 2024); alternatively, estimating these coefficients using a limited number (3-5) of models within the same family may compromise the accuracy of the predictions. Moreover, the recent work (Ruan et al., 2024) extends scaling law by incorporating latent variables to capture the patterns across model families and tasks.

3.2 Pilot Demonstration on HELM

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Scaling laws reveal that models from any family exhibit a similar performance trend as computational measures increase. This insight suggests there are commonalities and connections between different models. These motivate us to employ the MF method to explore more similarities beyond computational measures, *e.g.*, the relationship among the different model families and tasks.

We perform the aforementioned MF on the benchmark matrix to observe the error gap between predicted and truth (normalized) scores. Specifically, we select the core leaderboard provided by HELM for our exploratory experiments with only model name, task name and performance scores. This leaderboard, 68 models and 16 tasks, presented in a score matrix with a density of 82.5%, which includes both open-source and proprietary models, *e.g.*, GPT-4 and Jurassic-2. Our method treats all models and tasks as independent entities without introducing any prior similarity factors. We hope to observe whether MF can predict the remaining scores, giving a small part of the matrix, where we evaluate two training/validation sets split strategies: 10%/90%, 50%/50%. As illustrated in Figure 2, MF can accurately predict most of the missing scores within a low error range, which proves that it can encode the similarity across the model and the task without regression depending on explicit computational measures variable.

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4 Collaborative Performance Prediction

4.1 Definition

Motivated by pilot experiments, here we introduce the concept of "Collaborative Performance Prediction" (CPP) to facilitate the performance prediction of LLMs.

Definition 1. Let $\mathcal{M} = \{M_1, M_2, \dots, M_n\}$ be a set of *n* LLMs, and $\mathcal{T} = \{T_1, T_2, \dots, T_m\}$ be a suite of *m* tasks. Define the Score Matrix **S**, which is an $n \times m$ matrix where each element s_{ij} represents the performance score of model M_i on task T_j . s_{ij} is defined as

$$s_{ij} = \begin{cases} score & if tested, \\ unknown & otherwise. \end{cases}$$
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both model and task. Moreover, we can incorporate or solely rely on the factors describing the LLM and the associated downstream tasks.

4.2 Collaborative Data

based on the known values.

and few-shot settings.



Function: Employ an prediction method \mathcal{F} to es-

timate the unknown elements of **S**, denoted by \hat{s}_{ij} ,

Extention: Accommodate model design factors

 $\mathcal{V}_m = \{V_m^1, V_m^2, \dots, V_m^M\}$, such as common com-

putational meatures, and task design factors $V_t =$

 $\{V_t^1, V_t^2, \ldots, V_t^T\}$, such as targeted capabilities

Based on this definition, our framework consists

of two components: 1) collaborative performance

data, 2) collaborative prediction methods. We

anticipate that an accurate score can be predicted

with the historical performance of various models

on downstream tasks and other design factors for

Figure 3: Distribution of Testing Coverage Across Models and Tasks. The left bar shows the number of tasks each model has been tested on; The right bar illustrates the number of models tested in each specific task.

Unlike the scaling law approach, which requires training resource factors to obtain the correlation between metric scores and factors at a high training cost, our proposed method makes use of evaluation results and other design factors reported from existing studies, referred to as *collaborative* data. Open-source leaderboards, such as Open-LLM¹, HELM, and OpenCompass², have made tremendous efforts on this issue in fairly evaluating different LLMs. Our efforts extend beyond merely (Ruan et al., 2024) utilizing data from opensource leaderboards with matrix sparsity of 0%. We also extract test results from different models' papers, technical reports, and model cards. Ultimately, we have collected a score matrix of n = 72, m = 29 with a density of only 56%. Furthermore, we collected 12 and 4 detailed design factors for models and tasks. These details are listed in Appendix B.1. Our data analysis is shown in Figure 3

and Figure 8.

Data Analysis. Based on the *collective data*, we can make the following observations: a) Uneven 341 distribution of testing resources. We observe 342 significant variability in the deployment of testing 343 efforts, as shown in Figure 3. For instance, models from the LLAMA series have undergone extensive 345 testing across various tasks, in contrast to mod-346 els like GOPHER, where testing has largely stag-347 nated. A similar disparity is also evident among tasks, with MMLU and HELLASWAG receiving 349 considerable evaluation, whereas RACE has been relatively underexplored. This trend suggests that 351 as LLMs proliferate and tasks evolve, the distribu-352 tion of scores across the matrix will increasingly 353 skew, leading to a pronounced long-tail effect in 354 testing coverage for many tasks, barring a few that 355 consistently receive comprehensive evaluations. b) Widespread variations in the scores. It is note-357 worthy that identical models yield varying scores 358 on the same tasks across different studies (Shrivas-359 tava et al., 2023; AI@Meta, 2024), a variation often 360 attributed to differences in prompt settings, model 361 versions, and the volume of test samples employed. 362 Typically, these score variations range within 0.1, 363 with scores normalized between [0, 1]. This phe-364 nomenon underscores the importance of public 365 leaderboards and highlights researchers' need to ar-366 ticulate their testing frameworks when performing 367 customized evaluations clearly. When conflicted, we prefer the results from the Open-LLM leader-369 board in the collective data. c) Missing descrip-370 tion/model card. We advocate for consistently 371 providing complete model cards for open-source 372 and proprietary models. Such a phenomenon is 373 shown in Figure 8 and, unsurprisingly, a long-tail 374 distribution is witnessed. While it is understand-375 able that proprietary models might withhold spe-376 cific details about parameters, they can still divulge 377 information about parameter scale and the extent of 378 pre-training. Furthermore, we recommend a more 379 thorough description of testing tasks, including sug-380 gested few-shot settings and detailed descriptions 381 of targeted capabilities. 382

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4.3 Prediction Methods

In Section 2.2, classical collaborative filtering methods are inspired to conduct the performance prediction. In principle, most collaborative filtering methods can be applied. Here, in addition to the abovementioned MF, we also leverage neural col-

¹https://github.com/bentoml/OpenLLM

²https://opencompass.org.cn/

laborative filtering (He et al., 2017) (NCF) meth-389 ods, which uses a multi-layer perceptron to learn 390 the model-task interaction function to predict the score \hat{s}_{ij} for a model *i* on a task *j*, providing a way to learn non-linearities in the data:

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$$\widehat{s}_{ij} = f(i, j | \mathcal{M}, \mathcal{T}, [\mathcal{V}_i, \mathcal{V}_j], \theta)$$

= MLP(p_i, q_j, [e_{vi}, e_{vj}]), (5)

where \mathcal{M} and \mathcal{T} denote the sets of collaborative models and tasks, and their descriptive factors \mathcal{V}_i , \mathcal{V}_i optionally enrich the input data. Here, p_i and q_i are the latent vectors for model *i* and task *j* that capture the intrinsic properties of models and tasks, as well as embeddings $[e_{vi}, e_{vj}]$ derived from their descriptive factors, and θ represents the parameters of NCF.

Moreover, we further simplify the model to verify whether feasible to predict a score when only inputting the descriptive factors V_i , V_j into the prediction model:

$$\widehat{s}_{ij} = f(i, j | \mathcal{V}_i, \mathcal{V}_j, \theta)$$

= MLP(e_{vi}, e_{vj}), (6)

For both settings, where the goal is to predict the scores accurately, the loss function can be defined as follows:

$$L(\theta) = \frac{1}{N} \sum_{(i,j)\in\mathcal{D}} (\widehat{s}_{ij} - s_{ij})^2, \qquad (7)$$

where N is the total number of scores set \mathcal{D} for training, and s_{ij} is the true score for model *i* and task j.

Experiments 5

In this section, we evaluate the feasibility of CPP 416 from an overall benchmark perspective and a model 417 perspective in Section 5.1 and 5.2, respectively; 418 we then analyze the importance of factors for both 419 models and tasks in Section 5.3. Additionally, 420 a substantial amount of ablation and analysis is 421 placed in the appendix D, such as sparsity, the cor-422 relations in tasks and models, and which models 423 and tasks are more critical for prediction. 424

Experimental Setting. Our validation frame-425 work utilizes the aforementioned collaborative 426 dataset as the score matrix S. We partition scores 427 $\{s_{ij}\}$ into train and validation set, detailed in Ap-428 pendix C.2. 429

Evaluation Metric. To accurately evaluate CPP, we adopt two types of metrics: 1) SCORE-LOSS metrics including MSE Loss and L1 Loss between predicted scores and true scores (normalized) on downstream tasks and 2) RANK-ACCURACY metrics including ACCURACY and MAE@2 between the rank of predicted scores and true scores. We elaborate on these metrics in Appendix C.1.

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5.1 Evaluation from Benchmark Perspective

In this study, we select the abovementioned methods, MF and NCF, to verify whether s_{ij} can be accurately predicted based on the input of model i and task j. To examine whether enhancements is helpful, we modify NCF to support the input of design factors, detailed in Appendix C.2. Based on Figure 4 and Table 1, we can make the following observations:

First, all methods accurately predicted model performance, demonstrating that collaborative filtering mechanisms can predict model outcomes based on collaborative data across different models and tasks. This prediction is achieved without the need for explicit scaling factors or fitting a log-power curve. Second, from MF to NCF, the transformation in interaction mechanisms further enhances accuracy, suggesting that model improvements can further augment the efficacy of our methodology. Additionally, we were able to further increase accuracy by incorporating factors, such as model scaling variables and task descriptions, into the NCF framework alongside ID information. This confirms that incorporating explicit factors can enhance model and task similarities. Finally, among all metrics, we particularly noted that the accuracy of the predictive ranking was acceptable. In other words, researchers can use our method to accurately predict the ranking range of their developed models on test tasks, thereby enhancing model performance on specific tasks.

Predictability with Only Description Factors. We validate whether high predictive accuracy can still be achieved by only inputting the models' and tasks' design factors. As demonstrated in Table 1, the accuracy of predicted rankings (derived from predicted scores) remains high, affirming that our method supports predictions based solely on factors. However, the accuracy is lower compared to other models, suggesting that finer-grained latent similarities remain encoded as potential factors within the identity information across different



Figure 4: Comparative visualization of predictive accuracy across various scoring methods. From left to right: MF, NCF, NCF with Factor Enhancement, and NCF based solely on Factors. Each plot displays the regression between predicted and actual scores, where the solid line represents the regression fit and the shaded area denotes the confidence interval (CI). A line closer to the diagonal, which indicates perfect prediction, signifies higher prediction accuracy. These plots demonstrate the enhanced performance in score prediction achieved through the integration of factors into the NCF method.

Production Mothod	Score-Loss		Rank-Acc	
Treatenin Wieniou	MSE Loss ↓	Mean L1 Loss↓	Mean Prec.(%) ↑	MAE@2(%) ↑
Matrix Factorization	$2.16e^{-2}(1.19e^{-4})$	$9.47e^{-2}(2.89e^{-4})$	44.33(0.69)	83.16(0.73)
Neural Collaborative Filtering	$1.58e^{-2}(4.22e^{-5})$	$8.94e^{-2}(3.10e^{-4})$	41.76(1.22)	84.98(0.42)
+ Factor Enhanced	$1.25e^{-2}(3.35e^{-6})$	$7.88e^{-2}(6.31e^{-5})$	45.45 (0.33)	84.54(0.27)
Only Factor	$1.75e^{-2}(2.07e^{-5})$	$8.57e^{-2}(1.48e^{-4})$	33.47(0.12)	84.08(0.37)

Table 1: Comparison of prediction methods for LLM performance. Bold indicates the best-performed.

models and tasks.

5.2 Evaluation from Model Perspective



Figure 5: Comparison of the predictive performance of collaborative performance prediction (CPP) versus traditional scaling laws (SL) for LLMs: (a) CPP-0, with no prior testing information, and (b) CPP-2, with prior testing on two tasks.

To mimic the utilization of CPP in the real world, this section takes a model perspective to investigate the predictive accuracy of CPP upon each model. Specifically, we propose two scenarios: (i) prediction with no prior testing information and (ii) prediction with prior testing information on 2 tasks. These two scenarios correspond to real-world cases when the model has not been developed or when the model is tested on a few tasks and expects an accurate prediction of its ability on other tasks. In both scenarios, we focus on larger LLMs, e.g., LLama2-70b, as they are more computationally expensive to develop and test, requiring an accurate LLM prediction. 485

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We report the results of CPP and SL on both scenarios in Figure 5 and can draw the following conclusions. Under the CPP-0 scenario, CPP demonstrated greater adaptability across different tasks compared to SL, with points closely aligned along the y = x line ("perfect prediction") in Figure 5 (a). This suggests that CPP has effectively captured task-specific characteristics, such as value ranges, whereas SL, despite achieving a lower MSE-LOSS, tends to concentrate its predictions around 0.5. Under the CPP-2 scenario, the distribution of points of CPP is noticeably closer to y = x, as shown in Figure 5 (b), and its MSE-LOSS is also lower than that of SL. This indicates that leveraging performance data from other tasks considerably enhances the model's cross-task prediction capabilities, underscoring a degree of consistency across tasks for the same model. This approach demonstrates that predictions for scaling LLMs on downstream tasks

can be dynamically improved by evaluating performance on less computationally intensive tasks and using those outcomes to predict scores on subsequent tasks more accurately.

5.3 Factor Importance Analysis via SHAPLEY-VALUE

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In this section, we aim to conduct a factor importance analysis of each design factor over CPP. The Shapley value, a concept derived from cooperative game theory (Shapley, 1952), offers a systematic approach to measuring individual factors' contribution in predictive models (Lundberg and Lee, 2017; Covert et al., 2021). A detailed formulation of the Shapley value is shown in Appendix C.3. Visualization for Shapley values of each design factor is shown in Figure 6.





Based on Figure 6 (a), we can make the following observations regarding model factors. First, we have discovered that in addition to traditionally important factors such as training data size and parameter size mentioned in scaling law (Kaplan et al., 2020), other design factors significantly influence predictive outcomes. These include the model family, context window size, and batch size. Second, the importance of the model family cannot be overlooked, as it may relate to differences in data quality across models, including proprietary data or specific architectural details. For instance, using a particular model family might mean adopting architectures or optimization techniques better suited to specific tasks. Moreover, the size of the context window also significantly affects model performance. A larger context window allows the model to better understand the context in long texts, which is particularly crucial for long-context LLMs (Xiong et al., 2023). Experience (Google, 2024) has shown that such models perform better across a variety of tasks. Batch size, as another crucial factor, affects the stability and speed of model training. An appropriate batch size ensures a balance between the accuracy of gradient estimation and computational efficiency during training.

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As for the importance of task factors, results in Figure 6 (b) show that the *target ability* among all factors is more important. This also implies that similarities between the domains of different tasks can help predict outcomes. This conclusion is consistent with previous observations (Ruan et al., 2024; Perlitz et al., 2024; Polo et al., 2024)

In summary, these findings indicate that LLMs performance prediction should not rely solely on traditional design factors limited by scaling law but also on other key factors that might impact overall model performance.

6 Conclusion and Discussion

Advancing beyond traditional scaling laws on downstream tasks, we propose a collaborative performance prediction framework for large language models. It offers significant advantages, including easy deployment, low training costs, and superior predictive accuracy. Uniquely, it enables the incorporation of additional design factors and supports an in-depth analysis of their impact, including factor importance and correlations in models and tasks. For prediction, we collect a collaborative data containing a large number of historical performance and factors.

The predictive accuracy of our method is expected to improve as it benefits from an expanding pool of collaborative data. Moreover, this approach highlights the potential to identify neglected but vital factors beyond traditional scaling laws, such as task design factors, thereby enriching our comprehension of LLM performance predictability on downstream tasks.

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Limitations

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"Single-source-of-truth". When collecting the *collaborative data*, we hypothesize that each
model's performance on each task is identical.
However, in the real world, the detailed testing setting, for instance, the testing prompt writing, can
influence LLM's performance variance. Although
we observed this, we only saved one score from
different sources. How to incorporate the setting
of testing as an additional dimension remains to be
solved in future works.

Susceptibility to data quality. The prediction accuracy of CPP highly depends on the quality of collaborative data. The current version passively collects collaborative data from online resources. Should information from either of these 606 data sources be incorrect, the prediction capability of CPP would decrease correspondingly. To overcome such a limitation, jointly considering passive information collected from data sources and active information, such as performances of models tested 610 on some tasks by the user, might be a solution. Utilizing techniques such as efficient benchmark-612 ing (Perlitz et al., 2024; Polo et al., 2024) could 613 alleviate the cost of obtaining active information. 614

615 Ethics Statement

The data we use are collected from public papers, technical reports, open leaderboards, and model cards on GitHub.

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A Pilot Demonstrations using Neural Collaborative Filtering

In this section, we supplemented the error distribution in Figure 7, which is generated using neural collaborative filtering on the HELM lite leaderboard. Compared to Figure 2, it is evident that neural collaborative filtering consistently outperforms MF across each setting.

B Collaborative Data

B.1 Data Description

List of Models and Tasks. The table 2 contains all the models and tasks we have collected.

Description Factors for Models and Tasks We have collected the characteristics of models and tasks in relevant aspects through model cards, technical reports, and academic papers. We have organized and introduced these characteristics, as well



Figure 7: Error Distribution of Predictions (Normalized Score and Rank Derived by Score) Based on the HELM Lite Leaderboard Using Neural Collaborative Filtering: We evaluate the effectiveness of Matrix Factorization (MF) using two latent factors, 7 and 10, across 2 training/validation split percentages. Accuracy is defined as the percentage of instances where the predicted rank equals the actual rank. MAE@2 is defined as the percentage of instances where the absolute difference between the predicted rank and the actual rank is 2.

Models	Tasks
'LLama-2-7B', 'LLama-2-13B', 'LLama-2-70B', 'Llama 3 8B', 'Llama 3 70B',	
'GLM-130B', 'LLaMA-7B', 'LLaMA-13B', 'LLaMA-33B', 'LLaMA-65B',	
'GPT-3-175B', 'PaLM-540B', 'Claude-V3 Haiku', 'Claude-V3 Sonnet',	
'Claude-V3 Opus', 'GPT-4', 'gpt-3.5', 'BLOOM-176B', 'Luminous Base-13B',	
'Luminous Extended-30B', 'Luminous Supreme-70B', 'OPT-175B',	
'GPT-NeoX-20B', 'GPT-J-6B', 'sheared llama-2.7B', 'sheared llama-1.3B',	'BoolQ(0-shot)', 'BIG-bench hard(3-shot)', 'WinoGrande(0-shot)', 'WinoGrande(1-shot)',
'INCITE-Base-3B', 'INCITE-Base-7B', 'TinyLlama-1.1B', 'OpenLLaMA-3B-v1',	'Winogrande(5-shot)', 'PIQA(0-shot)', 'SIQA(0-shot)', 'HellaSwag(0-shot)', 'HellaSwag(10-shot)',
'OpenLLaMA-3B-v2', 'Pythia-1.4B', 'Pythia-2.8B', 'Falcon-7B',	'ARC-e', 'ARC-c(0-shot)', 'ARC-c(25-shot)', 'OBQA(zero-shot)', 'MMLU(5-shot)',
'Falcon-40B', 'Falcon-180B', 'Mistral 7B', 'MPT-30B', 'MPT-7B',	'HumanEval(pass@1)','MBPP(3-shot)','GSM8K(4-shot)','MATH(4-shot)',
'chinchilla', 'Pythia-70M', 'Pythia-160M', 'Pythia-410M', 'Pythia-1B',	'TriviaQA(5-shot)', 'NaturalQuestions(0-shot)', 'NaturalQuestions(1-shot)', 'NaturalQuestions(5-shot)',
'Pythia-6.9B', 'Pythia-12B', 'Gopher - 280B', 'Gopher - 44M',	'NaturalQuestions(64-shot)','LAMBADA(0-shot)','AGIEval English (3-5 shot)','RACE-m',
'Gopher - 117M', 'Gopher - 417M', 'Gropher - 1.4B', 'Gopher - 7.1B',	'RACE-h','LogiQA','WSC'
'MT-NLG 530B', 'GLaM', 'Phi-1.5-1.3B', 'Phi-2-2.7B', 'Yi-6b', 'Yi-9b',	
'Baichuan 1-7B', 'Baichuan 1-13B-Base', 'Baichuan 2-7B-Base',	
'Baichuan 2-13B-Base', 'InternLM2-7B', 'InternLM2-20B', 'Skywork-13B',	
'BlueLM-7B', 'Qwen-7B', 'Qwen-14B', 'TigerBot-13b', 'TigerBot-70b',	
'Gemma-2b' 'Gemma-7b'	

Table 2: List of Models and Tasks

as the corresponding embedding methods, as listed in Table 3:

Note that during data collection, not all factors are available. For these missing factors, such as CO2 and GPU hours, we replace them as zero values when entering data.

B.2 Data Analysis

919We conducted a statistical analysis of the data we
collected, specifically examining the number of
models tested for each task, the number of tasks
tested for each model, and the number of models
described by each factor. Since each task is con-
sistently associated with four factors, we did not
create a distribution chart for this aspect.

C Experimental Setup

C.1 Evaluation Metrics

Apart from visualization, we also evaluate the method based on two types of metrics: 1) SCORE-LOSS Metric: we calculate MSE LOSS and L1 LOSS between predicted scores and true scores (normalized) on downstream tasks; 2) RANK-ACCURACY Metric: researchers are sometimes not concerned with detailed scores but rather the rankings the model is in, so we calculate the accuracy of rank derived from the predicted scores, ACCU-RACY and MAE@2. ACCURACY refers to the percentage of instances where the predicted rank equals the true rank, and MAE@2 refers to the percentage of instances where the absolute difference between the predicted rank and the true rank is in 2, the formulation as below:

Model			
Factors	Description	Embedding	
Model Family	Type of model family, e.g., LLAMA 2, PYTHIA	Categorical Embedding	
Pretraining Dataset Size (B)	Data size in miilons of tokens	Numerical Embedding	
Parameter Size (M)	Number of model parameters in millions	Numerical Embedding	
GPUh	GPU hours consumed	Numerical Embedding	
FLOPs	Floating-point operations count	Numerical Embedding	
Context Window	Max context size in tokens, e.g., 1024, 2048	Categorical Embedding	
Batch Size (M)	Size of batches in millions, e.g., 1M, 2M	Categorical Embedding	
Layers	Number of layers in the model	Numerical Embedding	
Number Heads	Number of attention heads	Numerical Embedding	
Key/Value Size	Size of key/value in attention mechanism	Numerical Embedding	
Bottleneck Activation Size	Size of activation in bottleneck layers	Numerical Embedding	
Carbon Emission (tCO2Eq)	Carbon footprint of training	Numerical Embedding	
	Task		
Ability	Type of targeted cognitive ability, <i>e.g.</i> , reasoning	Categorical Embedding	
TaskFamily	Related task family ,e.g., ARC	Categorical Embedding	
Output Format	Format of task output, e.g., binary	Categorical Embedding	
Few-Shot Setting	Description of few-shot learning setting, e.g., zero-shot, 32-shot	Categorical Embedding	

Table 3: Design Factors of Models and Tasks

Accuracy =
$$\left(\frac{\sum_{i=1}^{N} \mathbf{1}(r_i = \hat{r}_i)}{N}\right) \times 100\%, (8)$$

MAE@2 =
$$\left(\frac{\sum_{i=1}^{N} \mathbf{1}(|r_i - \hat{r}_i| \le 2)}{N}\right) \times 100\%,$$
(9)

where N is the total number of validation instances, r_i is the true rank, \hat{r}_i is the predicted rank derived by the predicted score; $\mathbf{1}(\cdot)$ is the indicator function that evaluates to 1 if the argument is true and 0 otherwise; $|\cdot|$ denotes the absolute value.

C.2 Detailed Setting of Validation Prediction Accuracy Experiments

In this section, we details the setup of each experiment in 5.

Different Prediction Methods. Due to the 44% sparsity of the collected collaboration matrix, we used 5% of the known data as the validation set, with the remaining data serving as the observed training set. Through random splitting, we trained each model five times, deriving an average performance and variance. We configured our models with latent factors = 10, learning rate = 0.01, and iteration = 250,000. The Figure 4 is the results when random_seed = 1.

964 Predicting from Small to Large LMs. The fo965 cus here is on how to derive the scaling law ap966 plicable to specific task metrics. Undeniably, tra967 ditional methods do not provide a directly usable

scaling law across all downstream tasks for comparative analysis. However, we observed in the literature (Ruan et al., 2024) that a sigmoidal curve with a single coefficient and a single bias value represents the scaling law for downstream tasks. Moreover, we noticed that this curve's coefficients and bias values have a general range across all tasks, w = [0.5, 2], b = [-10, -3]. Consequently, we set this range of coefficients and bias for this curve and then used the normalized scores of smaller models within the same model family and their corresponding parameter sizes to fit the scaling law curve for each task. This approach generally follows a "pretrain-finetune" methodology. Additionally, CPP-2 refers to randomly selecting two scores from the observed performances of the model to be included in the training data. In this experiment, we use factor-enhanced NCF (setting is same as above).

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C.3 Detailed Setting of Analysis Experiments

Shapley-Value for Factor Importance Analysis. Given a predictive model f and a set of factors N, the Shapley value of a factor i is computed as follows:

$$\phi_i(v) = \sum_{S \subseteq N \setminus \{i\}} \frac{|S|!(|N| - |S| - 1)!}{|N|!}$$

$$\cdot [v(S \cup \{i\}) - v(S)],$$
(10) 992

where:

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• N is the total set of factors.

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Seeled I I Mc	Prior Tasks	Score-Loss		Rank-Acc	
Stateu LLIVIS		MSE Loss	Mean L1 Loss	Mean Prec.(%)	MAE@2(%)
LLaMA 2-70B	CF-0	$1.34e^{-2}$	$8.83e^{-2}$	16.7	50.0
	CF-2	$1.79e^{-2}(1.3e^{-3})$	$1.79e^{-2}(5.6e^{-4})$	$9.1(7.5e^{-3})$	$54.5(5.7e^{-4})$
LLaMA 3-70B	CF-0	$5.63e^{-2}$	$19.27e^{-2}$	14.3	71.4
	CF-2	$1.7e^{-2}(1.41e^{-4})$	$10.7e^{-2} (1.68e^{-3})$	$20.0(4.0e^{-2})$	$90.0(9.0e^{-2})$
LLaMA-65B	CF-0	$1.73e^{-2}$	$9.78e^{-2}$	24.0	80.0
	CF-2	$1.88e^{-2}(1.42e^{-5})$	$10.02e^{-2}(4.1e^{-4})$	$17.3(1.9e^{-3})$	$71.7(4.7e^{-4})$
Luminous Supreme-70B	CF-0	$6.06e^{-2}$	$20.14e^{-2}$	27.27	63.63
	CF-2	$1.45e^{-2}(1.1e^{-5})$	$10.79e^{-2}(6.4e^{-7})$	$16.7(3.1e^{-3})$	$83.3(3.5e^{-3})$
Duthia 17P	CF-0	$2.19e^{-2}$	$11.2e^{-2}$	21.42	71.42
r yulla-12D	CF-2	$1.57e^{-2}(2.1e^{-6})$	$10.88e^{-2}(4.6e^{-8})$	$33.3(2.7e^{-2})$	$66.7(6.9e^{-3})$
ViOb	CF-0	$3.20e^{-2}$	$14.66e^{-2}$	44.4	100.0
11-90	CF-2	$0.9e^{-2}(3.1e^{-4})$	$8.1e^{-2}(5.1e^{-6})$	$71.4(9.1e^{-2})$	100(0)
Baichuan 2-13B-Base	CF-0	$2.70e^{-2}$	$12.84e^{-2}$	57.14	100.0
	CF-2	$1.0e^{-2}(4.9e^{-4})$	$7.5e^{-2}(4.7e^{-4})$	$40.0(6.2e^{-4})$	100.0(0)
Qwen-14B	CF-0	$1.05e^{-2}$	$7.96e^{-2}$	33.3	100.0
	CF-2	$3.1e^{-2}(1.8e^{-3})$	$11.1e^{-2}(6.6e^{-3})$	$25.0(7.1e^{-3})$	$91.7(6.9e^{-3})$
TigerBot-70B	CF-0	$8.02e^{-2}$	$19.26e^{-2}$	12.5	75.0
	CF-2	$4.4e^{-2}(2.9e^{-6})$	$15.3e^{-2}(6.6e^{-5})$	$25.0(6.9e^{-3})$	$83.3(6.1e^{-3})$
Gamma-7B	CF-0	$4.94e^{-2}$	$17.62e^{-2}$	15.79	47.36
	CF-2	$10.2e^{-2}(3.2e^{-5})$	$25.9e^{-2}(1.6e^{-4})$	$26.4(8.6e^{-4})$	$58.8(1.4e^{-2})$
Falcon-180B	CF-0	$5.00e^{-2}$	$17.91e^{-2}$	14.58	57.14
	CF-2	$3.2e^{-2}(2.1e^{-5})$	$10.42e^{-2}(7.8e^{-5})$	$23.94(8.5e^{-2})$	$63.6(2.1e^{-5})$
Gopher-280B	CF-0	$14.48e^{-2}$	$30.76e^{-2}$	15.38	61.53
	CF-2	$10.87e^{-2}(3.6e^{-5})$	$23.59(4.2e^{-4})$	$27.33(1.8e^{-3})$	$66.49(6.8e^{-3})$

Table 4: The accuracy of Predicting Scaled Large LMs in CPP-0, CPP-2.

• S is a subset of factors excluding factor i.

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- |S| is the number of factors in subset S.
- v(S) is the prediction model's output when only the factors in subset S are used.
- v(S∪{i}) is the model's output when the factors in subset S plus factor i are used.
- The factorial terms |S|! and (|N|-|S|-1)! weigh the contribution of each subset according to the number of factors included or excluded, ensuring a fair allocation across all possible combinations.

The Shapley value, $\phi_i(v)$, quantifies the average marginal contribution of a factor *i* across all possible combinations of factors. The formula takes every subset *S* of the total factor set *N* that does not include *i*, calculates the difference in the model's prediction output with and without factor *i*, and averages this difference over all subsets. The averaging is weighted by the factor $\frac{|S|!(|N|-|S|-1)!}{|N|!}$, which corresponds to the number of permutations in which subset *S* appears as a prefix or suffix of the total set when factor *i* is added.

This approach ensures that each factor's contribution is assessed fairly and comprehensively, accounting for interactions with other factors and its unique impact when combined in different ways. Shapley values are particularly useful in machine learning for factor importance analysis because they provide a solid theoretical foundation and are less biased than simpler importance metrics.

The Shapley value algorithm for analyzing feature (factor) importance is computationally intensive, which has led to the development of various approximation methods (Jethani et al., 2022). Fortunately, our predictive model involves a manageable number of factors, allowing us to use the most accurate method of direct computation of Shapley values. Specifically, we apply an enumeration approach to compute Shapley values on a pre-trained factor-enhanced neural collaborative filtering model during the inference stage. This involves systematically masking factors to assess their impact.

For the implementation, we mask factors differently based on their data type as outlined in the Table 3:

- **numerical factors**: we set the input factor values to zero;
- categorical factors: we set the corresponding embedding layer parameters to zero.

We then compute the difference in validation loss

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Figure 8: The detailed distribution of collaborative data.

with and without each factor present, providing us with each factor's marginal contribution. This detailed approach allows us to quantify precisely how much each factor contributes to the predictive performance of the model, providing valuable insights into factor importance and model behavior.

D Ablation Study

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D.1 Ablation on Sparsity Threshold

To ascertain whether matrices composed of collaborative performance data can accurately predict the performance of LLMs, it is essential to consider the critical variable: the matrix **sparsity**. We assessed the impact of sparsity on prediction accuracy by manipulating the sparsity of the training matrix via masking. This method allowed us to obtain a reliable measure of average accuracy, as illustrated in Figure. 9. It is noteworthy that our method of controlling sparsity only reduces the number of training samples. We ensured fairness in each comparative experiment by maintaining a consistent validation set throughout. During the experiment, we maintained the same settings for the learning rate and number of iterations as in the main experiment. To ensure the robustness of our experimental results, each reported outcome represents the average score after conducting five random splits. 1061

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Figure 9: Relationship between matrix sparsity and three key performance metrics: L1 Loss, Accuracy, and MAE@2.

The data we collected inherently has a sparsity of 44%. Hence, we only have the remaining 46% of collaborative data. As sparsity levels range from 49.60% to 88.80% (masking 10% to 80% of the collaborative data), the graph shows a pronounced increase in L1 Loss and a decrease in Accuracy, indicating deteriorating model performance with higher sparsity, especially when sparsity exceeds 60%, where there is a significant drop in accuracy. Conversely, MAE@2 remains relatively stable initially before experiencing fluctuations, suggesting varying impacts on this metric. Interestingly, accuracy even improves when sparsity reaches 50%. We think the possible reason for this might be the presence of an optimal level of information reduction that removes redundant or noisy data without significantly compromising signal integrity. This phenomenon suggests that a moderate level of sparsity could potentially enhance model performance by focusing on more relevant factors.

D.2 Ablation on Predicting Performance on Complex Reasoning and CoT Tasks

From the model perspective, it is crucial for validat-1094 ing the feasibility of predictive methodologies to assess the predictive accuracy on special tasks poten-1096 tially exhibiting "emergent" phenomena (Suzgun et al., 2022; Wei et al., 2022), including complex 1098 reasoning and Chain of Thought (CoT) tasks (Wei 1099 et al., 2023). "Emergent' phenomena refers to the 1100 challenges associated with predicting performance 1101 from smaller models when the scale of a model ex-1102

pands significantly, resulting in discontinuous leaps 1103 in model capabilities. The existence of this phe-1104 nomenon is subject to ongoing debate. Nonetheless, 1105 recent efforts (Ganguli et al., 2022b; Hu et al., 2024; 1106 Owen, 2024; Ruan et al., 2024; Schaeffer et al., 1107 2023) continue to focus on how scaling laws can 1108 be modified to mitigate the "gap" between smaller 1109 and larger models. This may involve modifying 1110 metrics or incorporating additional data points to 1111 linearize the growth curve or alternatively opting 1112 for a sigmoidal curve. 1113

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Theoretically, these challenges are not too difficult for our prediction method, as the underlying mechanism of "emergent" abilities reflects a type of similarity—a commonality that manifests when models exceed a certain scale. By analyzing cross-model similarities—how other larger models demonstrate emergent capabilities compared to their smaller counterparts—we can enhance our predictive accuracy for the current model. Overall, these tasks are pivotal for comprehensive validation processes, *e.g.*, GSM8K (Cobbe et al., 2021), BBH (Suzgun et al., 2022), HUMANEVAL (Chen et al., 2021) and MBPP (Austin et al., 2021).

In detail, if we want to evaluate the performance of predicting a model on these special tasks, the training data is the performance information from other model families, the smaller model of the same family, and the random-selected two non-special tasks prior performance of this model. In our experiment, we tested the 4 models on these tasks, and then we plotted the test results on Figure 10. As illustrated in Figure 10, our predictive scores are more adaptive to each task, where the points are close along the "perfect prediction" line, which means our prediction method captures the similarity in the specific task across models. Our proposed method's MSE Loss is comparable to that of the scaling law, which shows the feasibility of CPP (in CPP-2).

D.3 Correlation between Models

Experiment. We conducted a "leave-one-out" ex-1144 periment to test the impact of Model A on the pre-1145 dictive performance of Model B. This involved 1146 masking Model A and using the performance of 1147 other models to train predictive methods, which 1148 were then validated on Model B to observe changes 1149 in loss. This approach generated a matrix with the 1150 masked model names on the X-axis and the vali-1151 dation model names on the Y-axis, with the values 1152



Figure 10: Comparison of the predictive performance of collaborative performance prediction (CPP) versus traditional scaling laws (SL) for Large Language Models (LLMs) in Complex Reasoning and CoT Tasks.

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representing the change in loss.

The "Leave-one-out" experiment is a robust method commonly used in statistical analysis. To assess the impact of different models on the predictive performance of a specific model, we implemented a strategy where we systematically masked each selected model in the training set. The procedure involved masking each model one at a time and then training and testing the loss on a validation model. This process was repeated across all models, culminating in the creation of a matrix where axis=0 represents the masked model ID, and axis=1 represents the validation model ID. The values in the matrix correspond to the loss observed. This experiment was conducted under three different random seeds to ensure the stability and reliability of the results.

Subsequently, each model was used as a validation set, with the remaining data serving as the training set to calculate the loss for each model. This also resulted in a matrix where axis=1 indicates the validation model ID, and the columns[:, valid model id] represent the corresponding loss for that validation model. We derived a delta loss matrix by calculating the difference between these two matrices.

Given that each validation model has its own range of loss variations, we normalized the delta loss matrix. We then performed a row-based correlation analysis on this normalized matrix to assess the impact of each model on predictive perfor1184mance. The higher the correlation value between1185the two models, the more similar their effects on1186predictions.

1187Analysis.Based on this correlation matrix, we1188further conducted a hierarchical clustering analy-1189sis (Nielsen, 2016). The results indicate that there1190exists a set of models that are similar in their im-1191pact on the predictive performance of the model.1192Other models are far away from them. (Details in1193Table 5)

This analysis not only helps us understand the specific contributions of each model to predictive performance but also reveals the similarities and differences in functionality among the models, providing a crucial basis for model optimization and selection.

We performed a row-wise correlation analysis 13 on this matrix and discovered that models from the same family tend to have similar impacts on predictions, as do models of the same size. After conducting a hierarchical distance analysis, we concluded that a group of models exists that, when more performance data is available, can significantly enhance the accuracy of the predictive models. There are also what might be termed "noise model performances" in our analysis D.3.

D.4 Correlation between Tasks

We also conducted "leave-one-out" experiments on these tasks and created a heatmap figure. 14 of the correlations. Tasks with similar targeted ability testing capabilities demonstrated similar influences, such as GSM8K, MATH (Hendrycks et al., 2021), ARC (Chollet, 2019), and HUMANEVAL, which all require complex reasoning abilities.

E Others

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E.1 Visualization

The figure 15 is the visualization for prediction performance of scaled language models on down-stream tasks.



Figure 11: Instance Distribution of the model factor Shapley value. *X*-axis represents the Shapley value, which indicates the degree of prediction loss change; *Y*-axis indicates the factor names in order of importance from top to bottom. Each point represents an instance.



Figure 12: Instance Distribution of the task factor Shapley value. *X*-axis represents the Shapley value, which indicates the degree of prediction loss change; *Y*-axis indicates the factor names in order of importance from top to bottom. Each point represents an instance.



Figure 13: The correlation heatmap of impacts of different models on prediction performance.



Figure 14: The correlation heatmap of impacts of different tasks on prediction performance.



Figure 15: Prediction performance of various scaled Language Models on downstream tasks. This figure illustrates regression plots comparing the predicted versus actual performance normalized scores for a series of large language models, including Llama-2-70B, Llama-65B, Falcon-180B, Gopher-280B, Pythia-12B, Gemma-7B, TigerBot-70B, Qwen-14B, Luminous Supreme-70B, and Llama-3-70B. Each subplot displays a regression line with a shaded 95% confidence interval and includes the L1 loss for each model's predictions, highlighting the accuracy and variability of predictive capabilities across different models.

Distance Cluster	Models
	LLama-2-7B, LLama-2-13B, LLama-2-70B, Llama 3 8B,
	LLaMA-7B, LLaMA-65B, Claude-V3 Haiku, Claude-V3 Sonnet,
	Claude-V3 Opus, GPT-4, BLOOM-176B, Luminous Extended-30B,
	Luminous Supreme-70B, OPT-175B, GPT-NeoX-20B, sheared llama-2.7B,
1	sheared llama-1.3B, INCITE-Base-3B, INCITE-Base-7B, OpenLLaMA-3B-v1, Pythia-1.4B,
1	Pythia-2.8B, Pythia-70M, Pythia-410M, Pythia-6.9B,
	Gopher - 280B, Gopher - 44M, Gopher - 117M, MT-NLG 530B, GLaM,
	Baichuan 1-7B, Baichuan 1-13B-Base, Baichuan 2-7B-Base, Baichuan 2-13B-Base,
	Skywork-13B, Qwen-7B, Qwen-14B, TigerBot-13b,
	Gemma-2b, Gemma-7b
2	gpt-3.5, Falcon-7B, Pythia-1B, Gropher - 1.4B, Yi-9b, TigerBot-70b
3	LLaMA-33B
4	Yi-6b
5	BlueLM-7B
6	Falcon-40B
7	MPT-7B
8	Falcon-180B
9	PaLM-540B
10	Pythia-160M
11	GPT-J-6B
12	GPT-3-175B, Luminous Base-13B
13	Gopher - 417M
14	Llama 3 70B
15	LLaMA-13B
16	TinyLlama-1.1B
17	Phi-1.5-1.3B
18	Gopher - 7.1B
19	InternLM2-20B
20	GLM-130B
21	MPT-30B
22	chinchilla
23	Mistral 7B
24	InternLM2-7B
25	OpenLLaMA-3B-v2
26	Phi-2-2.7B
27	Pythia-12B

Table 5: Distance Cluster of Models