Hyperbolic Contrastive Learning for Visual Representations beyond Objects

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Abstract

Despite the rapid progress in visual representation learning driven by self-/un-1 2 supervised methods, both objects and scenes have been primarily treated using the 3 same lens. In this paper, we focus on learning representations for objects and scenes explicitly in the same space. Motivated by the observation that visually similar 4 objects are close in the representation space, we argue that the scenes and objects 5 should further follow a hierarchical structure based on their compositionality. To 6 exploit such a structure, we propose a contrastive learning framework where a 7 Euclidean loss is used to learn object representations and a hyperbolic loss is used to 8 9 regularize scene representations according to the hierarchy. This novel hyperbolic objective encourages the scene-object hypernymy among the representations by 10 optimizing the magnitude of their norms. We show that when pretraining on 11 the COCO and OpenImages datasets, the hyperbolic loss improves downstream 12 performance across multiple datasets and tasks, including image classification, 13 object detection, and semantic segmentation. We also show that the properties of 14 the learned representations allow us to solve various vision tasks that involve the 15 interaction between scenes and objects in a zero-shot way. 16

17 **1 Introduction**

Our visual world is diverse and structured. Imagine taking a close-up of a box of cereal in the morning. If we zoom out slightly, we may see different nearby objects such as a bowl of milk, a cup of hot coffee, today's newspaper, or reading glasses. Zooming out further, we will probably recognize that these items are placed on a dining table with the kitchen as background rather than inside a bathroom. Such scene-object structure is diverse, yet not completely random. In this paper, we aim at learning visual representations of both the cereal box (objects) and the entire dining table (scenes) in the same space while preserving such hierarchical structures.

Un-/self-supervised learning has become a standard method to learn visual representations [27, 12, 25 25, 13, 6, 7, 49]. Although these methods attain superior performance over the supervised pretraining 26 on object-centric datasets such as ImageNet [25, 6], inferior results are observed on images depicting 27 multiple objects such as OpenImages or COCO [67]. Several methods have been proposed to mitigate 28 this issue [67, 68, 37, 1], but all focus on learning improved object representations or dense pixel 29 representations, instead of explicitly modeling the representations for scene images. The object 30 representations learned by these methods present a natural topology [66]. That is, the objects from 31 visually similar classes lie close to each other in the representation space. However, it is not clear 32 how the representations of scene images should fit into that topology. Naively applying existing 33 contrastive learning results in sub-optimal topology of scenes and objects as well as unsatisfactory 34 performance as we will show in the experiment. To this end, we argue that a hierarchical structure 35 can be naturally adopted. Considering scenes as the composition of different kinds of objects, we 36

³⁷ can construct a forest structure to describe such relationships, where the root nodes are the visually

³⁸ similar objects, and the scene images consisting of them are placed as the descendants. We call this

³⁹ structure the object-centric scene hierarchy.

The intermediate modeling difficulty induced by 40 this structure is the combinatorial explosion. A 41 finite number of objects can lead to exponentially 42 many kinds of scenes due to the composition. Hy-43 perbolic space is known for its provably better 44 capacity in modeling infinite trees compared with 45 Euclidean space [21, 26, 34]. Therefore, we pro-46 pose to employ a hyperbolic objective to regularize 47 the scene representations. Our framework builds 48 upon MoCo [27], which has been shown to learn 49 good object representations. To learn representa-50 tions of scenes, we sample the co-occurring scene-51 object pairs as the positive pairs, and objects that 52 are not part of that scene as the negative samples, 53 and use these pairs to compute an auxiliary hyper-54 bolic contrastive objective. Our model is trained 55 to reduce the distance between positive pairs and 56 push away the negative pairs in a hyperbolic space. 57

⁵⁸ Contrastive learning models generally compute
⁵⁹ their objectives on a hypersphere [27, 12]. By
⁶⁰ discarding the norm information, these models
⁶¹ effectively circumvent the shortcut of minimizing
⁶² objectives by tuning the norms and obtain better



Figure 1: Illustration of the representation space learned by our models. Object images of the same class tend to gather near the center around similar directions, while the scene images are far away in these directions with larger norms.

downstream performance. At the same time, they also lose control of the representative power in the
magnitude of the norm and leave the images disorganized. However, in hyperbolic space, it is the
magnitude of the norm that is used to model the hypernymy of the hierarchical structure [43, 58, 51].
When projecting the representations to the hyperbolic space, the norm information is preserved and
used to determine the Riemannian distance, which eventually affects our loss. Since the hyperbolic
space is diffeomorphic and conformal to the Euclidean, our hyperbolic contrastive loss is completely
differentiable and complementary to the original contrastive objective.

When training simultaneously with the original contrastive objective for objects and our proposed hyperbolic contrastive objective for scenes, the resulting representation space exhibits the desired hierarchical structure while keeping the object clustering topology intact as shown in Figure 1. We demonstrate the effectiveness of the learned representations on several downstream tasks, from image classification to object detection. We also show that the properties possessed by the representations allow us to perform various vision tasks in a zero-shot way, from label uncertainty quantification to out-of-context object detection. Our contributions are summarized below:

- We propose to learn representations for both object and scene images simultaneously using un-/self-supervised methods. We identify an object-centeric scene hierarchy that the representations are expected to follow.
- 2. We propose a framework with a novel hyperbolic contrastive loss to regularize the scene representations with positive and negative pairs sampled from the hierarchy.
- We show that the magnitude of representation norms effectively reflect the scene-objective
 hypernymy, and such representations transfer better to multiple downstream tasks.

84 2 Method

- ⁸⁵ In this section, we elaborate our approach to learn visual representations of object and scene images.
- ⁸⁶ We start with describing the hierarchical structure between objects and scenes.

87 2.1 Object-Centric Scene Hierarchy

From simple object co-occurrence statistics [20, 39] to finer object relationships [29, 31], using 88 hierarchical relationships between objects and scenes to understand images is not new. Previous 89 studies primarily work on an instance-level hierarchy by dividing an image into its lower-level 90 elements recursively - a scene contains multiple objects, an object has different parts, and each part 91 may consist of even lower-level features [47, 46, 15]. While this is intuitive, it describes a hierarchical 92 structure contained in the individual images. In our task, we would like to work on the structure from 93 the view of the entire dataset to learn a representation space shared by objects and scenes. To this 94 end, we argue that it is more natural to consider an object-centric hierarchy. 95

It is known that when training an image classifier, though not being optimized directly, the objects 96 from visually similar classes often lie close to each other in the representation space [66], which has 97 become the cornerstone of contrastive learning [27, 12]. Motivated by this observation, we believe 98 that the representation of each scene image should also be close to the object clusters it consists of. 99 However, they require a much larger volume due to the exponential number of possible compositions. 100 Another way to think about the object-centric hierarchy is through the generality and specificity as 101 often discussed in the language literature [40, 43]. An object concept is general when standing alone 102 in the visual world, and it will become specific when a certain context is given. For example, "a desk" 103 is thought to be a more general concept than "a desk in a classroom with a boy sitting on it". 104

Therefore, we propose to study an object-centric hierarchy across the entire dataset. Formally, given a set of images $S = \{s_1, s_2, \dots, s_n\}$, $\mathcal{O}_i = \{o_i^1, o_i^2, \dots, o_i^{n_i}\}$ are the object bounding boxes contained in the image s_i . We define the regions of scene $\mathcal{R}_i = \{r_i^1, r_i^2, \dots, r_i^{m_i}\}$ to be partial areas of the image s_i that contain multiple objects such that $r_i^j = \bigcup_k o_i^k$, where $o_i^k \in$ \mathcal{O}_i and object k is in the region j. We define the object-centric forest T = (V, E) to be that V = $S \cup \mathcal{O} \cup \mathcal{R}$, where $\mathcal{R} = \mathcal{R}_1 \cup \dots \cup \mathcal{R}_n$ and $\mathcal{O} = \mathcal{O}_1 \cup \dots \cup \mathcal{O}_n$. For $u, v \in V$, e = (u, v) is an edge of T if $u \subseteq v$ or $v \subseteq u$. Note that the natural scene images S are always put as the leaf nodes.

112 2.2 Representation Learning beyond Objects

To describe our proposed model that is built on this hierarchy, we begin with a brief review of the hyperbolic space and its several properties that will be used in our model. For comprehensive introductions to the Riemannian geometry and hyperbolic space, we refer the readers to [32, 17].

116 2.2.1 Hyperbolic Space

A hyperbolic space (\mathbb{H}^m, g) is a complete, connected Riemannian manifold with constant negative sectional curvature. These special manifolds are all isometric to each other with the isometries defined as $O^+(m, 1)$. Among these isometries, there are five common models that previous studies often work on [5]. In this paper, we choose the Poincaré ball $\mathbb{D}^n := \{p \in \mathbb{R}^n \mid ||p||^2 < r^2\}$ as our basic model [43, 58, 22], where r > 0 is the radius of the ball. The Poincaré ball is coupled with a Riemannian metric $g_{\mathbb{D}}(p) = \frac{4}{(1-||p||^2/r^2)^2}g_{\mathbb{E}}$, where $p \in \mathbb{D}^n$ and $g_{\mathbb{E}}$ is the canonical metric of the Euclidean space. For $p, q \in \mathbb{D}$, the Riemannian distance on the Poincaré ball induced by its metric $g_{\mathbb{D}}$ is defined as follows:

$$d_{\mathbb{D}}(p,q) = 2r \tanh^{-1}\left(\frac{\|-p \oplus q\|}{r}\right),\tag{1}$$

where ⊕ is the Möbius addition and it is clearly differentiable. In addition, the Poincaré ball can be
viewed as a natural counterpart of the hypersphere as it allows all directions, unlike the other models
such as the halfspace or hemisphere models that have constraints on the directions. The hyperbolic
space is globally differomorphic to the Euclidean space, which is stated in the theorem below:

Theorem 1. (*Cartan–Hadamard*). For every point $p \in \mathbb{H}^n$ the exponential map $\exp_p : T_p \mathbb{H}^n \approx \mathbb{R}^n \to \mathbb{H}^n$ is a smooth covering map. Since \mathbb{H}^n is simply connected, it is diffeomorphic to \mathbb{R}^n .

Specifically, for $p \in \mathbb{D}^n$ and $v \in T_p \mathbb{D}^n \approx \mathbb{R}^n$, the exponential map of the Poincaré ball \exp_p : $T_p \mathbb{D}^n \to \mathbb{D}^n$ is defined as

$$\exp_p(v) := p \oplus \left(\tanh\left(\frac{r\|v\|}{r^2 - \|p\|^2}\right) \frac{rv}{\|v\|} \right),\tag{2}$$



Figure 2: Our Hyperbolic Contrastive Learning (HCL) framework has two branches: given a scene image, two object regions are cropped to learn the object representations with a loss defined in the Euclidean space focusing on the representation directions. A scene region as well as a contained object region are used to learn the scene representations with a loss defined in the hyperbolic space that affects the representation norms.

- 133 The exponential map gives us a way to map the output of a network, which is in the Euclidean space,
- to the Poincaré ball. In practice, to avoid numerical issues, we clip the maximal norm of v with $r \varepsilon$ before the projection, where $\varepsilon > 0$. During the backpropagation, we perform RSGD [4] by scaling the gradients with $g_{\mathbb{D}}(p)^{-1}$. Intuitively, this forces the optimizer to take a smaller step when p is
- 137 closer to the boundary. The scaling factor is lower bounded by $\mathcal{O}(\varepsilon^2)$.
- The immediate consequence of the negative curvature is that for any point $p \in \mathbb{H}^m$, there are no conjugate points along any geodesic starting from p. Therefore, the volume grows exponentially
- ¹⁴⁰ faster in hyperbolic space than in Euclidean space. Such a property makes it suitable to embed the
- 141 hierarchical structure that has constant branching factors and exponential number of nodes. This is
- 142 formally stated in the theorem below:

Theorem 2. [21, 26] Given a Poincaré ball \mathbb{D}^n with an arbitrary dimension $n \ge 2$ and any set of points $p_1, \dots, p_m \in \mathbb{D}^n$, there exists a finite weighted tree (T, d_T) and an embedding $f: T \to \mathbb{D}^n$ such that for all i, j,

$$\left| d_T \left(f^{-1} \left(x_i \right), f^{-1} \left(x_j \right) \right) - d_{\mathbb{D}} \left(x_i, x_j \right) \right| = \mathcal{O}(\log(1 + \sqrt{2}) \log(m))$$

Intuitively, the theorem states that any tree can be embedded into a Poincaré disk (n = 2) with low distortion. On the contrary, it is known that the Euclidean space with unbounded number of dimensions is not able to achieve such a low distortion [34]. One useful intuition [51] to help understand the advantage of the hyperbolic space is given two points $p, q \in \mathbb{D}^n$ s.t. ||p|| = ||q||,

$$d_{\mathbb{D}}(p,q) \to d_{\mathbb{D}}(p,0) + d_{\mathbb{D}}(0,q), \text{ as } \|p\| = \|q\| \to r$$
(3)

147 This property basically reflects the fact that the shortest path in a tree is the path through the earliest 148 common ancestor, and it is reproduced in the Poincaré when points are both close to the boundary.

149 2.2.2 Hyperbolic Contrastive Learning

With the theoretical benefits of the hyperbolic space stated above, we propose a contrastive learning framework as shown in Figure 2. We adopt two losses to learn the object and scene representations. First, as shown in the top branch of Figure 2, we crop two views of a jittered and slightly expanded object region as the positive pairs and feed into the base and momentum encoders to calculate the object representations. We denote the output after the normalization to be z_{euc}^1 and z_{euc}^2 . Considering the computational cost of large batch sizes, we follow MoCo [27, 14] to leverage a memory bank to store the negative representations z_{euc}^n which are the features z_{euc}^2 from the previous batches. The Euclidean loss for this image is then calculated as:

$$\mathcal{L}_{\text{euc}} = -\log \frac{\exp\left(\mathbf{z}_{\text{euc}}^{1} \cdot \mathbf{z}_{\text{euc}}^{2} / \tau\right)}{\exp\left(\mathbf{z}_{\text{euc}}^{1} \cdot \mathbf{z}_{\text{euc}}^{2} / \tau\right) + \sum_{n} \exp\left(\mathbf{z}_{\text{euc}}^{1} \cdot \mathbf{z}_{\text{euc}}^{n} / \tau\right)}$$

where τ is a temperature parameter.

While this loss aims at learning object representations, we also design a hyperbolic contrastive 159 objective to learn the representations for scene images. We sample the positive region pairs u and v160 from object-centric scene hierarchy T such that $(u, v) \in E$. In other words, as shown in the bottom 161 branch of Figure 2, the objects contained in one region are required to be a subset of the objects in 162 the other. We sample the negative samples of u to be $\mathcal{N}_u = \{v | (u, v) \notin E\}$. However, building and 163 sampling from the entire hierarchy explicitly is slow and memory consuming. Instead, according to 164 the assumption that there are exponentially more scenes than object classes in practice, given a scene 165 image s, we always sample $u \in \mathcal{R} \cup \{s\}$ to be a scene region, $v \in \mathcal{O}$ to be an object that occurs in u, 166 and \mathcal{N}_u to be the other objects that are not in u. 167

The pair of scene and object images are fed into the base and momentum encoders that share the weights with the Euclidean branch. However, instead of normalizing the output of the encoders, we use the exponential map defined in the equation (2) to project these features in the Euclidean space to the Poincaré ball, which are denoted as z_{hyp}^1 and z_{hyp}^2 . Further, we replace the inner product in the cross-entropy loss with the negative hyperbolic distance as defined in equation (1). We calculate the hyperbolic contrastive loss as follows:

$$\mathcal{L}_{\text{hyp}} = -\log \frac{\exp\left(-d_{\mathbb{D}}(\mathbf{z}_{\text{hyp}}^{1}, \mathbf{z}_{\text{hyp}}^{2})/\tau\right)}{\exp\left(-d_{\mathbb{D}}(\mathbf{z}_{\text{hyp}}^{1}, \mathbf{z}_{\text{hyp}}^{2})/\tau\right) + \sum_{n} \exp\left(-d_{\mathbb{D}}(\mathbf{z}_{\text{hyp}}^{1}, \mathbf{z}_{\text{hyp}}^{n})/\tau\right)}$$

174 When minimizing the distances of all the positive pairs, With the intuition from Equation (3), it would

be beneficial to put the nodes near the root close to the center to achieve a overall lower loss. The

176 overall loss function of our model is as follows:

$$\mathcal{L} = \mathcal{L}_{\rm euc} + \lambda \mathcal{L}_{\rm hyp},$$

where λ is an scaling parameter to control the trade-off between hyperbolic and Euclidean losses.

178 3 Experiments

179 3.1 Implementation Details

Pre-training phase. We pre-train our method on two datasets: COCO [33] and a subset of Open-180 Images [41]. Both of these datasets are multi-object datasets; OpenImages [41] ($\sim 212k$ images) 181 contains 12 objects on average per image and COCO (~ 118 k) contains 6 objects on average. We 182 experiment with both the ground truth bounding box (GT) and using selective search [60] following 183 the previous method [67] (SS) to acquire objects. For the optimizer setups and augmentation recipes, 184 we follow the standard protocol described in MoCo-v2 [14] unless denoted otherwise. We find that a 185 base learning rate of 0.3 works better for us as compared to 0.03. We adopt the linear learning rate 186 scaling receipt that $lr = 0.3 \times \text{BatchSize}/256$ [24] and batch size of 128 by default on 4 NVIDIA 187 p6000 gpus. To ensure fair comparison, we also pre-train the baselines with a learning rate of 0.3. 188 We train our models on both datasets for 200 epochs. For the hyperparameters of our hyperbolic 189 objective, we use r = 4.5, $\lambda = 0.1$, and $\varepsilon = 1e^{-5}$. More details on the OpenImages dataset as well 190 as training setups can be found in Appendix A. 191

Downstream tasks. We evaluate our pre-trained models on image classification, object-detection 192 and semantic segmentation. For classification, we show linear evaluation (lineval) accuracy, i.e we 193 freeze the backbone and only train the final fc layer. We test on VOC [19], ImageNet-100 [57] and 194 ImageNet-1k [16] datasets. To test the discriminative capacity of the representations on both objects 195 and scenes, we create a dataset by mixing the ImageNet-100 and a subset of Place-205 [70] datasets, 196 which we refer to as the INPMix dataset. More details of this dataset can be found in Appendix A. 197 For object detection and semantic segmentation, we show results on the COCO and Pascal VOC 198 trainval2017 datasets. For VOC object detection, COCO object detection and COCO semantic 199 segmentation, we closely follow the common protocols listed in Detectron2 [65]. 200

	Pre-train dataset	Bbox type	VOC	IN-100	INPMix	IN-1k
MoCo-v2	COCO	-	64.79	64.84	41.83	51.17
HCL/\mathcal{L}_{hyp}	COCO	SS	73.13	73.84	51.28	54.21
HCL/\mathcal{L}_{hyp}	COCO	GT	75.55	76.22	51.25	54.52
HCL	COCO	SS	74.19	75.16	51.35	55.03
HCL	COCO	GT	76.51	76.74	51.63	55.63
MoCo-v2	OpenImages	-	69.95	72.80	49.59	54.12
HCL/\mathcal{L}_{hyp}	OpenImages	GT	73.79	77.36	52.96	57.57
HCL	OpenImages	SS	74.31	78.14	53.21	58.12
HCL	OpenImages	GT	75.40	79.08	53.82	58.51

Detection	Dataset	AP	$AP_{50} \\$	AP ₇₅
MoCo-v2	COCO	34.6	53.5	37.0
HCL/\mathcal{L}_{hyp}	COCO	36.1	55.2	37.9
HCL	COCO	37.0	56.1	39.8
MoCo-v2	VOC	51.5	79.4	56.1
LICI C	VOC	527	<u> 20 5</u>	50.4
$\Pi CL - \mathcal{L}_{hyp}$	VUC	55.7	o0.5	59.4
HCL - L _{hyp} HCL	VOC	54.4	80.5 81.4	60.2
HCL - L _{hyp} HCL Segmentation	VOC VOC Dataset	54.4 AP _s	80.3 81.4 AP ₁	60.2 AP _m
HCL - <i>L</i> _{hyp} HCL Segmentation MoCo-v2	VOC VOC Dataset COCO	54.4 AP _s 30.4	81.4 AP ₁ 50.1	60.2 AP _m 32.3
HCL - L _{hyp} HCL Segmentation MoCo-v2 HCL/L _{hyp}	VOC VOC Dataset COCO COCO	54.4 AP _s 30.4 31.5	80.3 81.4 AP ₁ 50.1 52.0	60.2 APm 32.3 33.8
HCL - \mathcal{L}_{hyp} HCL Segmentation MoCo-v2 HCL/ \mathcal{L}_{hyp} HCL	VOC VOC Dataset COCO COCO COCO	54.4 AP _s 30.4 31.5 32.5	80.3 81.4 AP ₁ 50.1 52.0 52.9	39.4 60.2 APm 32.3 33.8 34.6

Table 1: Classification results with linear evaluation. Our Table 2: Object detection and Semantic model improves scene-level classification on the VOC [19] Segmentation results. Our model imand INPMix [70] datasets, and object-level classification on proves on both tasks on COCO [33] and ImageNet-100 [57] and ImageNet-1k [16] datasets.

VOC [19] datasets.

3.2 Main Results 201

This section discusses our main results on the downstream image classification, object detection, 202 and semantic segmentation tasks. As the goal of this paper is not to present another state-of-the-art 203 204 self-supervised learning method, we primarily compare with the backbone model MoCo-v2 [27]. Another important baseline we consider is our model without the hyperbolic loss \mathcal{L}_{hyp} ; therefore only 205

the object representations are learned, which we denote as HCL/ \mathcal{L}_{hyp} . 206

Image classification. As shown in Table 1, HCL improves image classification on both scene-level 207 datasets (VOC and INPMix) and object-level datasets (ImageNet). When pretraining on OpenImages, 208 HCL improves ImageNet lineval accuracy by 0.94% and VOC lineval classification accuracy by 209 1.61 mAP. We observe similar improvements when pretraining on COCO. HCL improves accuracy 210 whether we use ground truth object bounding boxes or boxes generated by selective search. In general, 211 we observe a larger improvement of using HCL on OpenImages than COCO, which supports our 212 observation that HCL would improve more on the dataset with more objects per images. 213

Object detection and semantic segmentation. Table 2 reports the object detection and semantic 214 segmentation results using Mask R-CNN, following [14]. It shows consistent improvements over the 215 baselines on VOC object detection, COCO object detection, and COCO semantic segmentation. 216

Properties of Models Trained with HCL 3.3 217

The visual representations learned by HCL have several useful properties. In this section, we evaluate 218 the representation norm as an measure of the label uncertainty for image classification datasets, and 219 evaluate the object-scene similarity in terms of out-of-context detection. 220



norms of images with different num-

ber of labels in ImageNet-ReaL [3].

Mathad	Indiantor	Datasets			
Method	mulcator	IN-Real	COCO		
MoCo	Entropy	0.633	0.791		
Supervised	Entropy	0.671	0.793		
HCL	Norm	0.655	0.839		
Ensemble	Entropy+Norm	0.717	0.823		

3.3.1 Label Uncertainty Quantification 221

Table 3: NDCG scores of the image rankings based on the different indicators and models, and evaluated by the the number of labels per image.

ImageNet [16] is an image classification dataset consisting of object-centered images, each of which 222 has a single label. As the performance on this dataset gradually saturated, the original labels have 223 been scrutinized more carefully [50, 59, 54, 3, 61]. Prevailing labeling issues in the validation set 224



Figure 3: Images from ImageNet training set. The 5 images on the left have the smallest representation norms among all the images from the same class, and the 5 on the right have the largest norms.

have been recently identified [59, 54, 3], including labeling errors, multi-label images with only a single label provided, and so on. Although Beyer et al. [3] provide reassessed labels for the entire validation set, relabeling the entire training set can be infeasible.

Our learned representations provide a potential automatic way to identify images with multiple labels from datasets like ImageNet. Specifically, we first show in Figure 4 that there is a strong correlation between the representation norms and the number of labels per image according to the reassessed labels. For each class of the ImageNet training set, we rank the images according to their norms. The extreme images of some classes are shown in Figure 3 and also Appendix. Images with smaller

norms tend to capture a single object, while those with larger norms are likely to depict a scene.

To quantitatively evaluate this property, we report the NDCG metric on the ranked images as shown 234 in Table 3. NDCG assesses how often the scene images are ranked at the top. As a baseline, we rank 235 the images based on the entropy of the class probability predicted by a classifier, which is a widely 236 adopted label uncertainty indicator [11, 45]. We use both MoCo-v2 and supervised ResNet-50 as the 237 classifier. As shown in Table 3, using norms with HCL achieves similar rank quality as using entropy 238 with the supervised ResNet-50 on the ImageNet-ReaL dataset. In addition, when combining two 239 ranks using simple ensemble methods such as Borda count, the score is further improved to 0.717. 240 This shows that the entropy and the norm might look at different aspects of the multi-label issue. For 241 example, the entropy indicator can be affected by the bias of the model and the norm indicator can be 242 wrong on the images with multiple objects from the same class. In addition, our method is dataset 243 agnostic and does not need further training. To demonstrate this benefit, we report the same metric on 244 the COCO validation, where we also have the number of labels for each image. Our method achieves 245 much better NDCG scores than the supervised ResNet-50 as shown in Table 3. This finding can be 246 potentially useful to guide label reassessment, or provide an extra signal for model training. 247

248 3.3.2 Out-of-Context Detection

Our hyperbolic loss \mathcal{L}_{hyp} essentially encourages the model to capture the similarity between the 249 object and scene. We further investigate this property on detecting the out-of-context objects, which 250 can be useful in designing data augmentation for object detection [18]. We are especially interested 251 in the out-of-context images with conflicting backgrounds. To this end, we use the out-of-context 252 images proposed in the SUN09 dataset [15]. We first compute the representation of each object as 253 well as the entire scene image with that object masked out. We then calculate the hyperbolic distance 254 between the representations mapped to the Poincaré ball. Some example images from this dataset as 255 well as the distance of each contained object are shown in Figure 5. We find that the out-of-context 256 objects generally have a large distance, i.e. smaller similarity, to the overall scene image. To quantify 257 this finding, we compute the mAP of the object ranking on each image and obtain 0.61 for HCL. As 258 a comparison, the MoCo similarity gives mAP = 0.52 and the random ranking gives mAP = 0.44. 259



Figure 5: Out-of-context images from the SUN09 dataset [15]. The bounding box of each object, as well as its hyperbolic distance to the scene are displayed. The regular objects are in blue and the out-of-context objects are in purple. Note that the out-of-context objects tend to have large distances.

260 4 Main Ablation Studies

In this section, we report the results of several important ablation studies with respect to HCL. All the models are trained on the subset of the OpenImages dataset and linearly evaluated on the

²⁶³ ImageNet-100 and our INPMix datasets. The top-1 accuracy is reported.

Dist. Center	IN-100	IPS	λ	IN-100	IPS	Opti	n. λ	IN-100	IPS
	77.36	52.96	0.01	77.70	53.43	RSG	D 0.1	79.08	53.82
Hyp. Scene	79.08	53.82	0.1	79.08	53.82	RSG	D 0.5	0	0
Hyp. Object	76.96	52.74	0.2	78.64	53.84	SGD	0.1	70.16	48.47
Euc. Scene	76.68	52.58	0.5	0	0	SGD	0.5	74.18	42.75

Table 4: Ablation on the similarityTable 5: Ablation on the Table 6: Ablation on the RSGD ver-
losses trade-off.sus SGD optimizers.

Similarity measure and the center of the scene-object hierarchy. We propose to use the negative 264 hyperbolic distance as the similarity measure of the scene-object pairs. As an alternative, one can 265 use cosine similarity on the hypersphere as the measure just like the original contrastive objective. 266 However, this is basically minimizing the similarity between a single object and multiple objects. 267 These objects are probably from different classes and hence conflict with the original objective. As 268 shown in Table 4, replacing the negative hyperbolic distance with the Euclidean similarity impairs 269 downstream performance. The resulting accuracy is even worse than the model without any loss 270 271 function on the scene-object pairs. In terms of the hierarchy, we also test the assumption of scenecentric hierarchy [46, 47] by sampling the negative pairs as the objects and unpaired scenes. However, 272 we notice a significant decrease in the downstream accuracy with this modification in Table 4. 273

Trade-off between the Euclidean and hyperbolic losses. We adopt the Euclidean loss to learn 274 object-object similarity and the hyperbolic loss to learn object-scene similarity. A hyperparameter λ 275 is used to control the trade-off between them. As shown in Table 4, we find that a smaller $\lambda = 0.01$ 276 leads to marginal improvement. However, we also observe that larger λ s can lead to unstable and even 277 stalled training. With careful inspection, we find that in the early stage of the training, the gradient 278 provided by the hyperbolic loss can be inaccurate but strong, which pushes the representations to 279 be close to the boundary. As a result, the Riemannian SGD causes the gradient to be small and the 280 training is consequently stuck at some the early point. 281

Optimizer. With the observation above, we ask whether RSGD is still necessary for practical usage. We replace the RSGD optimizer with SGD. To avoid the numerical issue when the representations are too close to the boundary, we increase ε from $1e^{-5}$ to $1e^{-1}$. We first notice that this allows larger λ to be used as opposed to the RSGD. However, SGD always yields inferior performance to RSGD. Therefore, it shows that the accurate gradient provided by RSGD is still necessary.

287 5 Related Work

Representation Learning with Hyperbolic Space. Representations are typically learned in Euclidean space. Hyperbolic space has been adopted for its expressiveness in modeling tree-like

structures existing in various domains such as language [58, 21, 51, 43, 44], graphs [2, 8, 9, 48], and 290 vision [30, 10, 56]. The corresponding deep neural network modules have been designed to boost the 291 progress of such applications [9, 22, 35, 55]. The hierarchical structure presented in the datasets can 292 come from multiple factors, motivating the use of hyperbolic space. 1) Generality: the hypernym-293 hyponym property is a natural feature of words (e.g. WordNet [40]) and the hyperbolic space is 294 extensively exploited to learn word embeddings that preserve that property [58, 21, 51, 43, 44]. 295 296 Some image datasets also adopt the classes from WordNet for labeling, e.g. ImageNet [16], and consequently inherits the hierarchy in its labeling system. [36, 69, 38] take advantage of hyperbolic 297 space to capture such information in the visual embeddings. 2) Uncertainty: Several studies have 298 found that applying hyperbolic neural network modules to different tasks leads to a natural modeling 299 of the uncertainty [23, 30, 56]. 3) Compositionality: The compositionality of different basic elements 300 can form a natural hierarchy. We focus on learning the representations that capture the hierarchy 301 between the objects and scenes. The hierarchical representations learned in the hyperbolic space have 302 been applied to various tasks with the aforementioned motivations such as image classification [30] 303 or segmentation [64, 23], zero-/few-shot learning [38, 36], action recognition [38], and video pre-304 diction [56]. In this paper, we aim at learning image representations for general purposes that can 305 transfer to various downstream tasks. 306

Self-Supervised Learning on Scenes. Self-Supervised Learning (SSL) has made great strides in 307 308 closing the performance with supervised methods [12, 14] when pretrained on the object-centric 309 datasets like ImageNet. However, recent works have shown that SSL are limited on the multi-310 object datasets like COCO [52, 63] and OpenImages [41]. Several works have tried to address this issue by proposing different techniques. Dense-CL [63] works on pre-average pool features and 311 uses dense features on pixel level to show improved performance on dense tasks such as semantic 312 segmentation. DetCon [28] uses unsupervised semantic segmentation masks to generate features 313 for the corresponding objects in the two views. CAST [53] uses GradCAM [52] to figure out 314 same objects across views and applies contrastive loss on these features. PixContrast [68] uses 315 pixel-to-propagation consistency pretext task to build features for both dense downstream tasks and 316 discriminative downstream tasks. Pixel-to-Pixel Contrast [62] uses pixel-level contrastive learning 317 to build better features for semantic segmentation. Self-EMD [37] uses earth mover distance with 318 BYOL [25] for pretraining on the COCO dataset. ORL [67] uses selective search to generate object 319 proposals, then applies object-level contrastive loss to enforce object-level consistency. ContraCAM 320 [42] removes the scene bias issue by doing self-supervised object localization and performing 321 contrastive loss on them. One of the reasons below-par performance of SSL methods can be attributed 322 to treating scenes and objects using similar techniques, which often results in similar representations. 323 In our work, instead of treating them in the same functionality, we use a hyperbolic loss, which builds 324 representation that disambiguates scenes and objects based on the norm of the embeddings. Our 325 method not only separates scenes and objects, but also helps us in improving downstream tasks such 326 as image classification. 327

328 6 Closing Remarks

Conclusion We present HCL, a contrastive learning framework that learns visual representation for 329 both objects and scenes in the same representation space. The major novelty of our method is a 330 hyperbolic contrastive objective built on an object-centric scene hierarchy. We show the effectiveness 331 of HCL on several benchmarks including image classification, object detection, and semantic seg-332 mentation. We also demonstrate the useful properties of the representations under several zero-shot 333 settings from detecting out-of-context objects to quantifying the label uncertainty in the datasets like 334 ImageNet. More generally, we hope this paper can encourage studies towards building a more holistic 335 visual representation space and draw attention to the non-Euclidean representation learning. 336

Limitations Our model is shown to improve the classification performance on the ImageNet dataset, 337 but not much on the more fine-grained classification tasks as shown in Appendix B.2. We conjecture 338 that the largest improvement brought by our model to the object representations are modeling the 339 context information, while most of these datasets share a general class whose contexts are more or 340 less similar. In addition, although we provide some insights about the Riemannian optimization, its 341 underlying mechanism in the visual representation learning is still not fully understood. We conduct 342 more experiments on training hyperbolic linear classifiers in Appendix C.1. However, more efforts 343 are needed to fully unleash the potential of non-Euclidean representation learning. 344

345 **7** Societal Impact

Our work is a technical contribution and much of societal impact depends upon the models used in our work. We hope that our work will be used for betterment of the society and doesn't have any negative impact.

349 **References**

- [1] Y. Bai, X. Chen, A. Kirillov, A. Yuille, and A. C. Berg. Point-level region contrast for object detection
 pre-training. *CVPR*, 2022.
- [2] I. Balazevic, C. Allen, and T. Hospedales. Multi-relational poincaré graph embeddings. *NeurIPS*, 2019.
- [3] L. Beyer, O. J. Hénaff, A. Kolesnikov, X. Zhai, and A. van den Oord. Are we done with imagenet?, 2020.
- [4] S. Bonnabel. Stochastic gradient descent on riemannian manifolds. *IEEE Transactions on Automatic Control*, 58(9):2217–2229, 2013.
- J. W. Cannon, W. J. Floyd, R. Kenyon, W. R. Parry, et al. Hyperbolic geometry. *Flavors of geometry*, 31(59-115):2, 1997.
- [6] M. Caron, I. Misra, J. Mairal, P. Goyal, P. Bojanowski, and A. Joulin. Unsupervised learning of visual features by contrasting cluster assignments. *NeurIPS*, 2020.
- [7] M. Caron, H. Touvron, I. Misra, H. Jégou, J. Mairal, P. Bojanowski, and A. Joulin. Emerging properties in self-supervised vision transformers. In *ICCV*, 2021.
- [8] I. Chami, A. Wolf, D.-C. Juan, F. Sala, S. Ravi, and C. Ré. Low-dimensional hyperbolic knowledge graph
 embeddings. In ACL, 2020.
- [9] I. Chami, Z. Ying, C. Ré, and J. Leskovec. Hyperbolic graph convolutional neural networks. *NeurIPS*, 2019.
- [10] J. Chen, J. Qin, Y. Shen, L. Liu, F. Zhu, and L. Shao. Learning attentive and hierarchical representations
 for 3d shape recognition. In *ECCV*, 2020.
- [11] P. Chen, B. B. Liao, G. Chen, and S. Zhang. Understanding and utilizing deep neural networks trained
 with noisy labels. In *ICML*, 2019.
- 12] T. Chen, S. Kornblith, M. Norouzi, and G. Hinton. A simple framework for contrastive learning of visual representations. In *ICML*, 2020.
- T. Chen, S. Kornblith, K. Swersky, M. Norouzi, and G. E. Hinton. Big self-supervised models are strong
 semi-supervised learners. *NeurIPS*, 2020.
- [14] X. Chen, H. Fan, R. Girshick, and K. He. Improved baselines with momentum contrastive learning. *arXiv preprint arXiv:2003.04297*, 2020.
- [15] M. J. Choi, J. J. Lim, A. Torralba, and A. S. Willsky. Exploiting hierarchical context on a large database of object categories. In *CVPR*, 2010.
- [16] J. Deng, W. Dong, R. Socher, L.-J. Li, K. Li, and L. Fei-Fei. Imagenet: A large-scale hierarchical image database. In *CVPR*, 2009.
- [17] M. P. Do Carmo and J. Flaherty Francis. *Riemannian geometry*, volume 6. Springer, 1992.
- [18] N. Dvornik, J. Mairal, and C. Schmid. On the importance of visual context for data augmentation in scene understanding. *PAMI*, 43(6):2014–2028, 2019.
- [19] M. Everingham, L. Van Gool, C. K. Williams, J. Winn, and A. Zisserman. The pascal visual object classes
 (voc) challenge. *IJCV*, 88(2):303–338, 2010.
- [20] C. Galleguillos, A. Rabinovich, and S. Belongie. Object categorization using co-occurrence, location and
 appearance. In *CVPR*, 2008.
- [21] O. Ganea, G. Bécigneul, and T. Hofmann. Hyperbolic entailment cones for learning hierarchical embed dings. In *ICML*, 2018.
- [22] O. Ganea, G. Bécigneul, and T. Hofmann. Hyperbolic neural networks. *NeurIPS*, 2018.
- [23] M. GhadimiAtigh, J. Schoep, E. Acar, N. van Noord, and P. Mettes. Hyperbolic image segmentation. *arXiv* preprint arXiv:2203.05898, 2022.
- P. Goyal, P. Dollár, R. Girshick, P. Noordhuis, L. Wesolowski, A. Kyrola, A. Tulloch, Y. Jia, and K. He.
 Accurate, large minibatch sgd: Training imagenet in 1 hour. *arXiv preprint arXiv:1706.02677*, 2017.
- J.-B. Grill, F. Strub, F. Altché, C. Tallec, P. Richemond, E. Buchatskaya, C. Doersch, B. Avila Pires, Z. Guo,
 M. Gheshlaghi Azar, B. Piot, k. kavukcuoglu, R. Munos, and M. Valko. Bootstrap your own latent a new
 approach to self-supervised learning. In *NeurIPS*, 2020.

- [26] M. Gromov. Hyperbolic groups. In *Essays in group theory*, pages 75–263. Springer, 1987.
- [27] K. He, H. Fan, Y. Wu, S. Xie, and R. Girshick. Momentum contrast for unsupervised visual representation learning. In *CVPR*, 2020.
- [28] O. J. Hénaff, S. Koppula, J.-B. Alayrac, A. van den Oord, O. Vinyals, and J. Carreira. Efficient visual
 pretraining with contrastive detection. In *ICCV*, pages 10086–10096, 2021.
- J. Johnson, R. Krishna, M. Stark, L.-J. Li, D. Shamma, M. Bernstein, and L. Fei-Fei. Image retrieval using
 scene graphs. In *CVPR*, 2015.
- [30] V. Khrulkov, L. Mirvakhabova, E. Ustinova, I. Oseledets, and V. Lempitsky. Hyperbolic image embeddings.
 In *CVPR*, 2020.
- [31] R. Krishna, Y. Zhu, O. Groth, J. Johnson, K. Hata, J. Kravitz, S. Chen, Y. Kalantidis, L.-J. Li, D. A. Shamma,
 et al. Visual genome: Connecting language and vision using crowdsourced dense image annotations. *IJCV*,
 2017.
- 409 [32] J. M. Lee. Introduction to Riemannian manifolds. Springer, 2018.
- [33] T.-Y. Lin, M. Maire, S. J. Belongie, J. Hays, P. Perona, D. Ramanan, P. Dollár, and C. L. Zitnick. Microsoft
 coco: Common objects in context. In *ECCV*, 2014.
- [34] N. Linial, E. London, and Y. Rabinovich. The geometry of graphs and some of its algorithmic applications.
 Combinatorica, 15(2):215–245, 1995.
- 414 [35] Q. Liu, M. Nickel, and D. Kiela. Hyperbolic graph neural networks. *NeurIPS*, 2019.
- [36] S. Liu, J. Chen, L. Pan, C.-W. Ngo, T.-S. Chua, and Y.-G. Jiang. Hyperbolic visual embedding learning for
 zero-shot recognition. In *CVPR*, 2020.
- 417 [37] S. Liu, Z. Li, and J. Sun. Self-emd: Self-supervised object detection without imagenet, 2021.
- [38] T. Long, P. Mettes, H. T. Shen, and C. G. M. Snoek. Searching for actions on the hyperbole. In *CVPR*, 2020.
- [39] T. Mensink, E. Gavves, and C. G. Snoek. Costa: Co-occurrence statistics for zero-shot classification. In
 CVPR, 2014.
- [40] G. A. Miller, R. Beckwith, C. Fellbaum, D. Gross, and K. J. Miller. Introduction to wordnet: An on-line
 lexical database. *International journal of lexicography*, 3(4):235–244, 1990.
- [41] S. K. Mishra, A. B. Shah, A. Bansal, A. N. Jagannatha, A. Sharma, D. Jacobs, and D. Krishnan. Object aware cropping for self-supervised learning. *ArXiv*, abs/2112.00319, 2021.
- [42] S. Mo, H. Kang, K. Sohn, C.-L. Li, and J. Shin. Object-aware contrastive learning for debiased scene representation. In *NeurIPS*, 2021.
- 428 [43] M. Nickel and D. Kiela. Poincaré embeddings for learning hierarchical representations. *NeurIPS*, 2017.
- [44] M. Nickel and D. Kiela. Learning continuous hierarchies in the lorentz model of hyperbolic geometry. In
 ICML, 2018.
- [45] C. Northcutt, L. Jiang, and I. Chuang. Confident learning: Estimating uncertainty in dataset labels. *Journal* of Artificial Intelligence Research, 70:1373–1411, 2021.
- 433 [46] D. Parikh and T. Chen. Hierarchical semantics of objects (hsos). In ICCV, 2007.
- [47] D. Parikh, C. L. Zitnick, and T. Chen. Unsupervised learning of hierarchical spatial structures in images.
 In *CVPR*, 2009.
- [48] J. Park, J. Cho, H. J. Chang, and J. Y. Choi. Unsupervised hyperbolic representation learning via message
 passing auto-encoders. In *CVPR*, 2021.
- [49] A. Radford, J. W. Kim, C. Hallacy, A. Ramesh, G. Goh, S. Agarwal, G. Sastry, A. Askell, P. Mishkin,
 J. Clark, et al. Learning transferable visual models from natural language supervision. In *ICML*, 2021.
- 440 [50] B. Recht, R. Roelofs, L. Schmidt, and V. Shankar. Do imagenet classifiers generalize to imagenet? In
 441 *ICML*, 2019.
- 442 [51] F. Sala, C. De Sa, A. Gu, and C. Ré. Representation tradeoffs for hyperbolic embeddings. In *ICML*, 2018.
- [52] R. R. Selvaraju, M. Cogswell, A. Das, R. Vedantam, D. Parikh, and D. Batra. Grad-cam: Visual explanations
 from deep networks via gradient-based localization. In *ICCV*, 2017.
- [53] R. R. Selvaraju, K. Desai, J. Johnson, and N. Naik. Casting your model: Learning to localize improves
 self-supervised representations. In *CVPR*, 2021.
- [54] V. Shankar, R. Roelofs, H. Mania, A. Fang, B. Recht, and L. Schmidt. Evaluating machine accuracy on imagenet. In *ICML*, 2020.
- 449 [55] R. Shimizu, Y. Mukuta, and T. Harada. Hyperbolic neural networks++. In ICLR, 2021.

- 450 [56] D. Surís, R. Liu, and C. Vondrick. Learning the predictability of the future. In CVPR, 2021.
- 451 [57] Y. Tian, D. Krishnan, and P. Isola. Contrastive multiview coding. In ECCV, 2020.
- [58] A. Tifrea, G. Bécigneul, and O.-E. Ganea. Poincaré glove: Hyperbolic word embeddings. In *ICLR*.
 OpenReview, 2018.
- [59] D. Tsipras, S. Santurkar, L. Engstrom, A. Ilyas, and A. Madry. From imagenet to image classification:
 Contextualizing progress on benchmarks. In *ICML*, 2020.
- [60] J. R. Uijlings, K. E. Van De Sande, T. Gevers, and A. W. Smeulders. Selective search for object recognition.
 IJCV, 104(2):154–171, 2013.
- [61] V. Vasudevan, B. Caine, R. Gontijo-Lopes, S. Fridovich-Keil, and R. Roelofs. When does dough become a bagel? analyzing the remaining mistakes on imagenet. *arXiv preprint arXiv:2205.04596*, 2022.
- [62] W. Wang, T. Zhou, F. Yu, J. Dai, E. Konukoglu, and L. Van Gool. Exploring cross-image pixel contrast for
 semantic segmentation. In *ICCV*, 2021.
- [63] X. Wang, R. Zhang, C. Shen, T. Kong, and L. Li. Dense contrastive learning for self-supervised visual
 pre-training. In *CVPR*, 2021.
- [64] Z. Weng, M. G. Ogut, S. Limonchik, and S. Yeung. Unsupervised discovery of the long-tail in instance
 segmentation using hierarchical self-supervision. In *CVPR*, 2021.
- 466 [65] Y. Wu, A. Kirillov, F. Massa, W.-Y. Lo, and R. Girshick. Detectron2. https://github.com/
 467 facebookresearch/detectron2, 2019.
- [66] Z. Wu, Y. Xiong, S. X. Yu, and D. Lin. Unsupervised feature learning via non-parametric instance
 discrimination. In *CVPR*, 2018.
- [67] J. Xie, X. Zhan, Z. Liu, Y. S. Ong, and C. C. Loy. Unsupervised object-level representation learning from
 scene images. In *NeurIPS*, 2021.
- [68] Z. Xie, Y. Lin, Z. Zhang, Y. Cao, S. Lin, and H. Hu. Propagate yourself: Exploring pixel-level consistency
 for unsupervised visual representation learning. In *CVPR*, 2021.
- 474 [69] J. Yan, L. Luo, C. Deng, and H. Huang. Unsupervised hyperbolic metric learning. In CVPR, 2021.
- [70] B. Zhou, A. Lapedriza, J. Xiao, A. Torralba, and A. Oliva. Learning deep features for scene recognition
 using places database. *NeurIPS*, 2014.

477 Checklist

1. For all authors
(a) Do the main claims made in the abstract and introduction accurately reflect the paper's contributions and scope? [Yes]
(b) Did you describe the limitations of your work? [Yes]
(c) Did you discuss any potential negative societal impacts of your work? [Yes]
(d) Have you read the ethics review guidelines and ensured that your paper conforms to them? [Yes]
2. If you are including theoretical results
(a) Did you state the full set of assumptions of all theoretical results? [N/A]
(b) Did you include complete proofs of all theoretical results? [N/A]
3. If you ran experiments
(a) Did you include the code, data, and instructions needed to reproduce the main experi- mental results (either in the supplemental material or as a URL)? [Yes]
(b) Did you specify all the training details (e.g., data splits, hyperparameters, how they were chosen)? [Yes]
(c) Did you report error bars (e.g., with respect to the random seed after running experi- ments multiple times)? [Yes]
(d) Did you include the total amount of compute and the type of resources used (e.g., type of GPUs, internal cluster, or cloud provider)? [Yes]
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(d) Did you discuss whether and how consent was obtained from people whose data you're using/curating? [N/A]
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5. If you used crowdsourcing or conducted research with human subjects
(a) Did you include the full text of instructions given to participants and screenshots, if applicable? [N/A]
(b) Did you describe any potential participant risks, with links to Institutional Review Board (IRB) approvals, if applicable? [N/A]
(c) Did you include the estimated hourly wage paid to participants and the total amount spent on participant compensation? [N/A]