Expressive and Generalizable Low-rank Adaptation for Large Models via Slow Cascaded Learning

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⁰⁰¹ Abstract

 Efficient fine-tuning plays a fundamental role in modern large models, with low-rank adap- tation emerging as a particularly promising approach. However, the existing variants of LoRA are hampered by limited expressiveness, a tendency to overfit, and sensitivity to hyper- parameter settings. This paper presents LoRA Slow Cascade Learning (*LoRASC*), an inno- vative technique designed to enhance LoRA's expressiveness and generalization capabilities while preserving its training efficiency. Our ap- proach augments expressiveness through a cas- caded learning strategy that enables a mixture- of-low-rank adaptation, thereby increasing the **model**'s ability to capture complex patterns. **Additionally, we introduce a slow-fast update** mechanism and cascading noisy tuning to bol- ster generalization. The extensive experiments on various language and vision datasets, as well as robustness benchmarks, demonstrate that the proposed method not only significantly outperforms existing baselines, but also miti- gates overfitting, enhances model stability, and improves OOD robustness.

⁰²⁶ 1 Introduction

 Foundation models, which are large-scale models pre-trained on extensive datasets and subsequently adapted for specific downstream tasks, have be- come integral to contemporary machine learning frameworks. Fine-tuning these models is essen- tial, yet full parameter fine-tuning often encoun- ters significant memory and computational bottle- necks. As a result, Parameter-Efficient Fine-Tuning (PEFT) techniques, which aim to minimize the number of trainable parameters to reduce training costs and improve training stability, have gained increasing prominence. Among these techniques, Low-Rank Adaptation (LoRA) [\(Hu et al.,](#page-8-0) [2021\)](#page-8-0) stands out due to its efficiency in reducing train- ing costs through low-rank approximation for full-parameter updates. However, despite LoRA's advantages, its limitations in terms of expressiveness **043** and generalization have been noted. Some studies **044** suggest that the inherent low-rankness of LoRA **045** might restrict its expressiveness [\(Xia et al.,](#page-10-0) [2024;](#page-10-0) 046 [Meng et al.,](#page-9-0) [2024;](#page-9-0) [Lialin et al.,](#page-9-1) [2023;](#page-9-1) [Huang and](#page-9-2) **047** [Wei,](#page-9-2) [2024\)](#page-9-2), with a preference for overparameteriza- **048** tion, while others indicate a tendency for LoRA to **049** overfit or exhibit overconfidence [\(Lin et al.,](#page-9-3) [2024;](#page-9-3) **050 [Wang et al.,](#page-10-1) [2023\)](#page-10-1).** 051

In this work, we investigate the potential of cas- **052** cading learning to augment the expressiveness of **053** LoRA. Our approach involves initializing a new **054** LoRA module at the start of each epoch and in- **055** tegrating this module into the backbone network **056** after the epoch concludes. By employing a mixture- **057** of-low-rank adaptation, we effectively increase the **058** model's rank, while maintaining low training costs, **059** as each cascading step consumes no more parame- **060** ters and memory than a single LoRA model. More- **061** over, this method does not add any inference over- **062** head by remerging each LoRA module into the **063** backbone network. 064

To improve LoRA's generalization capabilities, we **065** draw inspiration from optimization techniques. We **066** repurpose certain strategies from optimizers for **067** LoRA, motivated by the observation that initializ- **068** ing a new LoRA module for each epoch can repre- **069** sent a descent direction for the dataset. In optimiza- **070** tion theory, flat minimizers are preferred, as they **071** [a](#page-8-1)re associated with better generalization [\(Hochre-](#page-8-1) **072** [iter and Schmidhuber,](#page-8-1) [1997;](#page-8-1) [Keskar et al.,](#page-9-4) [2016\)](#page-9-4). **073** Inspired by the fact that the moving average mech- **074** [a](#page-9-5)nism guides models towards flat minimizers [\(Iz-](#page-9-5) **075** [mailov et al.,](#page-9-5) [2018\)](#page-9-5), we maintain both fast-updating **076** and its moving average version, the slow-updating **077** LoRA experts. The fast-updating expert is reini- **078** tialized regularly to learn from the data over a set **079** number of steps, while the slow-updating expert **080** undergoes updates via a proportional exponential **081** moving average after the fast-updating cycle com- **082**

 pletes. Additionally, mirroring techniques in deep learning optimizers where noise proportional to the gradient scale is used to find flat minima [\(Xie et al.,](#page-10-2) [2020\)](#page-10-2), we introduce noise at the beginning of each epoch, with the scale tied to the norm of LoRA's **088** weights.

 To verify the effectiveness of the proposed method, we conduct extensive experiments on both lan- guage and vision tasks. For language tasks, we utilized the Llama2 model on 12 datasets (e.g., SuperGLUE, SQuAD, DROP, GSM8K, and In- structEval), Alpaca among other instruct follow- ing benchmarks to demonstrate the effectiveness of our design. We can directly apply our approach [t](#page-9-6)o LoRA, LoRA+ [\(Hayou et al.,](#page-8-2) [2024\)](#page-8-2), Dora [\(Liu](#page-9-6) [et al.,](#page-9-6) [2024\)](#page-9-6), and other members of the LoRA fam- ily, significantly improving their performance in large model transfer learning. For vision tasks, we also validated our approach on the CLIP pre-trained Vit-bigG model with the ImageNet dataset, show- ing a significant performance improvement rela- tive to LoRA on domain adaptation datasets such as Image-R and Image-C. The proposed method consistently outperforms the baselines by a large **107** margin.

¹⁰⁸ 2 Related Work

109 2.1 Low-Rank Adaptation Finetuning

 Low-Rank Adaptation(LoRA) [\(Hu et al.,](#page-8-0) [2021\)](#page-8-0) is a parameter-efficient fine-tuning method designed to adapt large models to new tasks, demonstrat- ing superior performance. LoRA+ [\(Hayou et al.,](#page-8-2) [2024\)](#page-8-2) improves performance and fine-tuning speed by setting different learning rates for the LoRA adapter matrices A and B with a carefully cho-117 sen ratio, maintaining the same computational cost as LoRA. Dora [\(Liu et al.,](#page-9-6) [2024\)](#page-9-6) decomposes the pre-trained weight into two components, magni- tude and direction, for fine-tuning, specifically em- ploying LoRA for directional updates to efficiently minimize the number of trainable parameters. Our work introduces a robust cascading learning sched- ule for various LoRA variants, proving through ex- tensive experiments that it can enhance the training performance of LoRA, LoRA+, and Dora without additional training costs.

128 2.2 Combination of LoRA

129 LoRAhub [\(Huang et al.,](#page-9-7) [2023\)](#page-9-7) presents a simple **130** framework designed for the purposeful assembly **131** of LoRA modules trained on diverse tasks, aiming to achieve adaptable performance on unseen **132** tasks. MOLE [\(Huang and Wei,](#page-9-2) [2024\)](#page-9-2) treats each **133** layer of trained LoRAs as a distinct expert and **134** implements hierarchical weight control by integrat- **135** ing a learnable gating function within each layer. **136** LoRAFlow [\(Wang et al.,](#page-10-3) [2024\)](#page-10-3) utilizes dynamic **137** weights to adjust the impact of different LoRAs. 138 These methods are not in conflict with *LoRASC*, as **139** they focus on learning the combination of LoRA **140** experts across different domains, while our method **141** aims to learn more generalizable experts within a **142** single domain using slow cascade learning. **143**

ReLoRA [\(Lialin et al.,](#page-9-1) [2023\)](#page-9-1) enhances LoRA's fit- **144** ting ability by continuously merging online LoRA **145** into the main network and restarting optimizer pa- **146** rameters during training. It also proposes a jagged **147** cosine scheduler to implement a learning rate re- **148** sume strategy at each step. COLA [\(Xia et al.,](#page-10-0) [2024\)](#page-10-0) 149 explores a similar approach but in a simpler manner, **150** merely restarting optimizer parameters when initializing new LoRAs without adjusting the learning **152** rate schedule. Our work employs a simpler cas- **153** cading learning strategy where each expert learns **154** independently for each epoch, without additional **155** design for learning schedules or optimizer parame- **156** ters. Additionally, we incorporate noise tuning and **157** slow-fast update strategy, ensuring robustness in **158** each expert merged into the pre-trained model. Our **159** method can be applied to various LoRA variants, 160 demonstrating effectiveness across multiple tasks **161** in both language and image domains. **162**

3 Methods **¹⁶³**

3.1 LoRA 164

Low-Rank Adaptation (LoRA) is a parameter- **165** efficient fine-tuning method designed to adapt large **166** pre-trained models to specific tasks with signifi- **167** cantly fewer trainable parameters. Instead of up- **168** dating all parameters of the model, LoRA inserts **169** low-rank matrices into each layer of the pre-trained **170** model, which are then fine-tuned. This reduces the **171** computational burden and the risk of overfitting. **172**

Given a pre-trained weight matrix $W_0 \in \mathbb{R}^{d \times k}$ a neural network, LoRA approximates the update **174** ΔW using two low-rank matrices $A \in \mathbb{R}^{d \times r}$ and 175 $B \in \mathbb{R}^{r \times k}$, where $r \ll \min(d, k)$. The update is 176 defined as: **177**

$$
\Delta W = BA \tag{1} \tag{1}
$$

in **173**

During fine-tuning, instead of updating W, we up- **179**

181 $W = W_0 + \Delta W = W_0 + BA$ (2)

182 This low-rank adaptation significantly reduces the 183 **number of trainable parameters from** $d \times k$ **to** $r \times$ **184** $(d+k)$.

185 3.2 *LoRASC*

186 3.2.1 Cascading LoRA Learning

 Due to the reparameterization nature of low-rank adaptation (LoRA) fine-tuning, employing multi- ple LoRA experts incurs the same inference cost as using a single LoRA expert. This character- istic makes LoRA particularly suitable for inte- gration with cascading learning to enhance perfor- mance in transfer learning tasks. As analyzed in ReLoRA [\(Lialin et al.,](#page-9-1) [2023\)](#page-9-1), reinitializing new LoRA modules during the learning schedule can progressively increase the model's rank, thereby improving its fitting ability.

 In *LoRASC*, we default to learning one LoRA ex- pert per epoch. After training one LoRA expert, it is merged into the main network, and the next expert learns based on the optimized residuals. The optimization schedule for each single LoRA expert is a compressed version of the original full-training schedule: for instance, if a model was originally trained for N epochs, each expert in *LoRASC* com- pletes training in 1 epoch with fixed starting and ending learning rates with the same but compressed scheduler. This makes *LoRASC* easy to apply to any large model transfer learning scenario using LoRA, without requiring changes to hyperparame- ters. The only necessary adjustment is an increase in the learning rate. Since the number of training steps is compressed, each step must be larger to [c](#page-9-8)over the same distance. Additionally, Li et al. [\(Li](#page-9-8) [et al.,](#page-9-8) [2019\)](#page-9-8) found that higher learning rates can lead to stronger generalization ability, which might also explain the improved out-of-domain perfor-mance of our method.

219 Mathematically, the cascading LoRA learning can **220** be described as follows:

221 1. For each epoch t, train a new LoRA expert 222 (A_t, B_t) to minimize the residual error, where $\mathcal L$ is **223** the fine-tuning loss function:

224
$$
(A_t, B_t) = \arg\min_{A_t, B_t} \mathcal{L}(W_{t-1} + B_t A_t),
$$
 (3)

2. Merge the trained LoRA expert into the main **225** network: **226**

$$
W_t = W_{t-1} + B_t A_t \t\t(4) \t\t 227
$$

By iteratively merging each new LoRA expert into **228** the main network, loRA cascading progressively **229** enhances the model's capacity to fit the data with- **230** out increasing the inference cost. **231**

3.2.2 LoRA Slow-Fast Update **232**

To enhance the generalization of large model trans- **233** fer learning, we aim to avoid local optima at each **234** step of cascading. Even with low-rank adaptation, **235** this issue persists due to the imbalance between **236** model parameters and training data. Inspired by **237** SWA [\(Izmailov et al.,](#page-9-5) [2018\)](#page-9-5), which averages model **238** parameters over several epochs to find a more gen- **239** eralized solution, we employ a sliding average **240** method to ensure the stability and robustness of **241** each LoRA merged into the main network. **242**

Specifically, during training, we maintain two **243** LoRA experts at each cascading step t as shown **244** in Fig. [1:](#page-3-0) a slow-updating LoRA $(A_t^{\text{slow}}, B_t^{\text{slow}})$ and a fast-updating LoRA $(A_t^{\text{fast}}, B_t^{\text{fast}})$. At step 246 0, both slow and fast LoRA share the same ini- **247** tialization. During each cascading iteration, fast **248** LoRA undergoes fine-tuning, and after completion, **249** it is averaged with slow LoRA. The slow LoRA **250** is then merged into the pre-trained model, while **251** the fast-updating LoRA is reinitialized for the next **252** iteration. We control the retention proportion of **253** the slow expert with a hyperparameter α . 254

) **245**

(5) **256 257**

(6) **258**

The update rules are given by: **255**

$$
A_{t+1}^{\text{slow}} = \alpha A_t^{\text{slow}} + (1 - \alpha) A_t^{\text{fast}} \tag{5}
$$

$$
B_{t+1}^{\text{slow}} = \alpha B_t^{\text{slow}} + (1 - \alpha) B_t^{\text{fast}} \tag{6}
$$

By employing this slow-fast update strategy, **259** *LoRASC* ensures that each merged LoRA expert **260** contributes to a more generalized solution, enhanc- **261** ing the overall stability and performance of the **262** model in transfer learning scenarios. **263**

3.2.3 Cascading Noisy Tuning **264**

To further enhance generalization, we introduce **265** random noise to the pre-trained model before **266** each new LoRA fine-tuning step. Unlike Noisy- **267** Tune [\(Wu et al.,](#page-10-4) [2022\)](#page-10-4), which adds uniform noise **268** to different parameter matrices according to their **269** standard deviations only once at the beginning of **270**

Figure 1: Iterative pipeline of *LoRASC*. Here, t represents the iteration step, and BA denotes the low-rank learnable vectors in LoRA. The backbone network W always has its gradients turned off, and α is the hyperparameter controlling the pace of the slow-fast update. Our method follows three stages: 1. Fast LoRA expert training, where noise is added to the backbone network, followed by training the fast LoRA on the task data. 2. Slow LoRA expert merging, where a portion of the learned fast LoRA is weighted and merged into the slow LoRA. 3. Update the pretrained model, merging the updated slow LoRA into the backbone network, and prepare for the next iteration.

 fine-tuning, we apply noise before training each new expert. This approach helps the model escape local optima at every slow LoRA step, thereby re-ducing the risk of overfitting.

 Additionally, the presence of the slow-updating LoRA module indicates the direction of parameter changes under the new task. Therefore, we use the standard deviation of the slow LoRA weights to determine the noise scale rather than the pre- trained model's weights. Incorporating this noise before every expert ensures that the model continu- ously explores robust and flatten parameter spaces, thus improving generalization and reducing the ten-dency to overfit.

285 The perturbation is defined as:

286
$$
\widetilde{N}_t = U\left(-\frac{\lambda}{2}, \frac{\lambda}{2}\right) \cdot \operatorname{std}(B_t^{\text{slow}} A_t^{\text{slow}})
$$
 (7)

287 where std stands for standard deviation. The func-288 tion $U(a, b)$ represents uniform distribution noise 289 ranged from a to b, and λ is a hyperparameter that **290** controls the relative noise intensity.

291 3.3 Overview

292 With LoRA cascading learning, slow-fast updates **293** and noisy tuning, the pipeline of our *LoRASC* is as **294** follows:

$$
W_{t-1} = W_{t-1} + N_t \tag{8}
$$

$$
(A_t^{\text{fast}}, B_t^{\text{fast}}) = \arg\min_{A_t^{\text{fast}}, B_t^{\text{fast}}} \mathcal{L}\left(\widetilde{W}_{t-1} + B_t^{\text{fast}} A_t^{\text{fast}}\right)
$$
\n
$$
^{296}
$$
\n(9)

$$
A_t^{\text{slow}} = \alpha A_{t-1}^{\text{slow}} + (1 - \alpha) A_t^{\text{fast}} \qquad (10)
$$

(10) **297 298**

(11) **299 300**

(12) **301**

$$
B_t^{\text{slow}} = \alpha B_{t-1}^{\text{slow}} + (1 - \alpha) B_t^{\text{fast}} \qquad (11)
$$

$$
W_t = \widetilde{W}_{t-1} + B_t^{\text{slow}} A_t^{\text{slow}} \tag{12}
$$

LoRASC pipeline can be seen in Fig. [1.](#page-3-0) Although **302** we use vanilla LoRA to show slow casdade learn- **303** ing, *LoRASC* should be able to boost the perfor- **304** [m](#page-9-6)ance of any LoRA variants, such as DoRA [\(Liu](#page-9-6) **305** [et al.,](#page-9-6) [2024\)](#page-9-6), LoRA+ [\(Hayou et al.,](#page-8-2) [2024\)](#page-8-2), LoRA- **306** FA [\(Zhang et al.,](#page-10-5) [2023\)](#page-10-5), etc. Moreover, *LoRASC* **307** is easy to implement, and we provide pseudocode **308** with more detailed explanations in Algorithm [1.](#page-4-0) **309**

4 Experiments **³¹⁰**

We conducted extensive experiments to demon- **311** strate the effectiveness and robustness of *LoRASC* **312** across both NLP and CV domains. **313**

For language tasks, we conducted our language **314** experiments using the popular open-source large **315** language model, Llama2^{[1](#page-3-1)}. We evaluated our ap-
316 proach on several NLU and GLU tasks, selecting **317** both SuperGLUE [\(Wang et al.,](#page-9-9) [2019a\)](#page-9-9) tasks (in- **318** cluding classification and multiple-choice) and **319** generation tasks. We also tested the model's per- **320** formance in mathematical reasoning using the **321** GSM8K dataset [\(Cobbe et al.,](#page-8-3) [2021\)](#page-8-3). Addition- **322** ally, we performed instruction tuning experiments **323** to verify the transfer learning capability of our **324** method, achieving significant improvements on key **325** metrics such as MMLU [\(Hendrycks et al.,](#page-8-4) [2020\)](#page-8-4), **326**

¹ [https://huggingface.co/meta-llama/](https://huggingface.co/meta-llama/Llama-2-7b-hf) [Llama-2-7b-hf](https://huggingface.co/meta-llama/Llama-2-7b-hf)

- 1: Initialize $W \leftarrow W_0$
- 2: Initialize A^{slow} , B^{slow} \triangleright Initialize slow LoRA matrices
- 3: Initialize $A^{\text{fast}} \leftarrow A^{\text{slow}}$, $B^{\text{fast}} \leftarrow B^{\text{slow}} \triangleright \text{Fast}$ LoRA matrices initialized from slow ones
- 4: for epoch $t = 1$ to T do
- 5: if $t > 1$ then
- 6: Reinitialize A^{fast} , $B^{\text{fast}} \geq \text{Reinitialize}$ fast LoRA matrices for subsequent epochs 7: end if

8:
$$
\widetilde{W} \leftarrow W + U\left(-\frac{\lambda}{2}, \frac{\lambda}{2}\right) \cdot \text{std}(B^{\text{slow}}A^{\text{slow}})
$$

\n9: optimizer
\nInitializeOptimizer $(A^{\text{fast}}, B^{\text{fast}})$
\n10: Ir_scheduled
\nInitializeLRScheduled (optimizer)

11: for batch in training data do

12: Forward pass: $L \leftarrow \mathcal{L}(\tilde{W} + B^{\text{fast}} A^{\text{fast}})$

13: Backward pass: Compute gradients 13: Backward pass: Compute gradients

14: optimizer.step()

15: lr scheduler.step()

16: end for

17: Update slow LoRA:

18: $A^{\text{slow}} \leftarrow \alpha A^{\text{slow}} + (1 - \alpha) A^{\text{fast}}$

19: $B^{\text{slow}} \leftarrow \alpha B^{\text{slow}} + (1 - \alpha) B^{\text{fast}}$

- 20: Merge slow LoRA into main network: $W \leftarrow \widetilde{W} + B^{\text{slow}} A^{\text{slow}}$ 21: end for
- 22: return W

327 DROP [\(Dua et al.,](#page-8-5) [2019\)](#page-8-5), BBH [\(Srivastava et al.,](#page-9-10) **328** [2022\)](#page-9-10) and HumanEval [\(Chen et al.,](#page-8-6) [2021\)](#page-8-6).

For visual tasks, we chose the CLIP ViT-bigG/ $14²$ $14²$ $14²$ as our pretrained model, fine-tuning it on the ImageNet-1K [\(Deng et al.,](#page-8-7) [2009\)](#page-8-7) training set and testing it on the validation set. Subsequently, we evaluated the trained model on perturbed datasets such as ImageNet-A [\(Hendrycks et al.,](#page-8-8) [2021b\)](#page-8-8), ImageNet-C [\(Hendrycks and Dietterich,](#page-8-9) [2019\)](#page-8-9), ImageNet-R [\(Hendrycks et al.,](#page-8-10) [2021a\)](#page-8-10), ImageNet- [V](#page-10-6)2 [\(Recht et al.,](#page-9-11) [2019\)](#page-9-11), ImageNet-Sketch [\(Wang](#page-10-6) [et al.,](#page-10-6) [2019b\)](#page-10-6) and Stylized-ImageNet [\(Geirhos](#page-8-11) [et al.,](#page-8-11) [2018\)](#page-8-11) demonstrating our method's robust-ness and generalization capabilities.

4.1 Implementation Details **341**

For all experiments, we exclusively fine-tuned q 342 [a](#page-9-12)nd v in attention layers as delineated by [Malladi](#page-9-12) **343** [et al.](#page-9-12) [\(2023\)](#page-9-12) and [Ren et al.](#page-9-13) [\(2024\)](#page-9-13). The fine-tuning **344** process utilized single NVIDIA H100 GPU. For **345** all tasks, we explored several learning rates and **346** reported the optimal performance. For the hyper- **347** parameters of *LoRASC*, we explored the factor α 348 of Slow-Fast Update in {0.5, 0.6, 0.8} to control **349** the updating ratio. Additionally, we selected the **350** noise intensity from $\{0.1, 1, 10\}$, which is a sig- 351 nificantly smaller set compared to the default 7 in **352** NoistTune [\(Wu et al.,](#page-10-4) [2022\)](#page-10-4). All the results were **353** averaged across 3 distinct random seeds, and we **354** report the optimal performance. **355**

4.2 Main Results **356**

4.2.1 *LoRASC* for Large Language Model **357**

Experiment setting. For in-domain language **358** transfer learning, we consider the SuperGLUE **359** dataset collection [\(Wang et al.,](#page-9-9) [2019a\)](#page-9-9), includ- **360** [i](#page-8-13)ng: BoolQ [\(Clark et al.,](#page-8-12) [2019\)](#page-8-12), CB [\(De Marn-](#page-8-13) **361** [effe et al.,](#page-8-13) [2019\)](#page-8-13), COPA [\(Roemmele et al.,](#page-9-14) [2011\)](#page-9-14), **362** [M](#page-10-7)ultiRC [\(Khashabi et al.,](#page-9-15) [2018\)](#page-9-15), ReCoRD [\(Zhang](#page-10-7) **363** [et al.,](#page-10-7) [2018\)](#page-10-7), RTE [\(Socher et al.,](#page-9-16) [2013\)](#page-9-16), **364** WiC [\(Pilehvar and Camacho-Collados,](#page-9-17) [2019\)](#page-9-17), and **365** WSC [\(Levesque et al.,](#page-9-18) [2012\)](#page-9-18). We also include 366 SST-2 [\(Dagan et al.,](#page-8-14) [2005\)](#page-8-14) , GSM8K [\(Cobbe et al.,](#page-8-3) **367** [2021\)](#page-8-3) and two question answering(QA) datasets, **368** [S](#page-8-5)QuAD [\(Rajpurkar et al.,](#page-9-19) [2016\)](#page-9-19) and DROP [\(Dua](#page-8-5) **369** [et al.,](#page-8-5) [2019\)](#page-8-5). And we directly used 8-shot direct **370** prompting or GSM8K evaluation^{[3](#page-4-2)}. We adhered to 371 [t](#page-9-12)he experimental configuration described by [Mal-](#page-9-12) **372** [ladi et al.](#page-9-12) [\(2023\)](#page-9-12), randomly selecting 1000 exam- **373** ples for training, 500 for validation, and 1000 for **374** testing across each dataset. The AdamW optimizer **375** was employed, with training spanning 5 epochs, 376 consistent with the baseline settings. A linear learn- **377** ing rate schedule was implemented, with the ini- **378** tial learning rate selected from $\{1 \times 10^{-5}, 5 \times 10^{-5},$ 1×10^{-4} , 5×10^{-4} , 1×10^{-3} . By default the batch size 380 was set to 4 and the LoRA rank was set to 8. For **381** LoRA+, we adhered to its setup by fixing the learn- **382** ing rate of B matrices to be 16 times that of A matri- **383** ces. DoRA decomposes the pre-trained weight into **384** magnitude and direction components, with LoRA **385** efficiently updating the direction component. This **386** means that each LoRA expert represents DoRA's **387** direction component. When applying *LoRASC* to **388** DoRA, we maintain continuous training of the mag- **389**

, **379**

² [https://huggingface.co/laion/](https://huggingface.co/laion/CLIP-ViT-bigG-14-laion2B-39B-b160k)

[CLIP-ViT-bigG-14-laion2B-39B-b160k](https://huggingface.co/laion/CLIP-ViT-bigG-14-laion2B-39B-b160k)

³ <https://github.com/allenai/open-instruct>

Task Task type							SST-2 RTE CB BoolQ WSC WIC MultiRC COPA ReCoRD SQuAD DROP GSM8K \rightarrow classification \rightarrow - multiple choice $-$ -generation - - math -			
LoRA	95.5		87.4 91.1 85.7	70.2 72.4	85.3	85.0	81.2	90.4	51.6	19.5
w/ COLA	95.9		87.7 91.1 85.7	66.4 72.6	85.3	82.0	81.4	90.6	51.6	21.0
w/ LoRASC										
+ Cascade			95.8 87.7 92.9 86.1	71.1 72.3	86.3	88.0	81.6	91.8	52.5	21.5
++ Slow LoRA	96.0		88.0 96.4 86.8	74.0 72.1	86.3	88.0	82.1	92.7	55.3	27.5
$+++$ Noise Tuning 96.1 88.1 96.5 87.4				75.0 72.7	86.6	88.0	82.2	92.9	56.7	27.5
$LoRA+$	95.7		87.0 91.4 85.9	69.2 72.1	85.7	87.0	81.3	90.5	55.8	22.0
w/ LoRASC										
+ Cascade			95.7 87.0 92.9 86.2	71.2 72.8	85.3	88.0	81.9	91.2	55.8	19.5
++ Slow LoRA	95.7		88.1 92.9 85.9	67.3 73.5	85.7	88.0	81.9	92.0	56.3	23.0
+++ Noise Tuning 95.8 88.1 92.9 86.3				71.4 74.1	86.1	88.0	81.9	92.0	56.4	24.0
DoRA			95.4 87.4 96.4 85.7	72.1 71.5	84.7	88.0	81.1	91.1	54.8	21.0
w/LoRASC										
+ Cascade			95.8 87.4 96.4 85.8	65.4 72.8	84.1	88.0	81.6	91.7	52.6	22.5
++ Slow LoRA	95.8		88.1 96.4 85.8	65.4 72.8	86.1	88.0	81.9	92.8	54.8	25.0
$+++$ Noise Tuning 96.0			88.5 96.5 87.6 75.6 72.8		86.8	89.0	82.2	93.3	56.5	25.5

Table 1: Comparative Performance of LoRA, LoRA+, and DoRA enhanced with *LoRASC* across multiple in-domain fine-tuning datasets.

Method	MMLU	DROP	HEval	BBH	GSM8K
LoRA	45.83	32.76	31.26	13.41	11.5
w/ LoRASC					
$+$ Cascade	45.53	32.71	31.61	14.02	11.5
++ Slow LoRA	45.68	33.74	31.38	17.07	12.5
$++$ Noise	45.98	33.02	31.61	15.24	16.5

Table 2: Results on instruction-following tasks. The model was trained on Alpaca and evaluated on InstructEval metrics and GSM8K. *LoRASC* consistently achieves the best performance compare to vanilla LoRA.

 nitude while applying our technique to the direction component. We follow the standard procedure of merging and reinitializing LoRA and align it with the slow-fast update and noisy tuning.

39[4](#page-5-0) **[F](#page-9-20)or instruction tuning, we use the Alpaca⁴ [\(Taori](#page-9-20)** [et al.,](#page-9-20) [2023\)](#page-9-20) dataset for training. The batch size was [s](#page-9-13)et to 128. We follow the training scripts of [Ren](#page-9-13) [et al.](#page-9-13) [\(2024\)](#page-9-13) in our experiment. We finetune our model for 3 epochs. A linear learning rate schedule was applied, with the initial learning rate selected **from** $\{1 \times 10^{-4}, 3 \times 10^{-4}, 5 \times 10^{-4}, 1 \times 10^{-3}\}$. For evaluation we use InstructEval[5](#page-5-1) **401** [\(Chia et al.,](#page-8-15) [2023\)](#page-8-15), 5-shot direct prompting for MMLU , 3-shot direct prompt- ing for BBH and DROP, 0-shot direct prompting for HEval.

405 *LoRASC* exhibits excellent adaptability to LoRA **406** variants. In the experiments shown in Table [1,](#page-5-2) **407** *LoRASC* outperforms the COLA across various

tasks, demonstrating the effectiveness of our LoRA **408** cascading technique. Moreover, *LoRASC* effec- **409** tively boosted the performance of LoRA, LoRA+, **410** and DoRA across 12 in-domain training datasets en- **411** compassing four major tasks: classification, multi- **412** ple choice, generation, and mathematics. *LoRASC* **413** achieved significant improvements across all these **414** tasks, demonstrating its ability to enhance the learn- **415** ing capabilities and in-domain generalization of the **416** LoRA family of models. Moreover, the progressive **417** addition of cascading learning, slow-fast updates, **418** and noisy tuning further improved performance, **419** validating the design of our approach. The robust **420** slow cascading strategy not only enhanced overall **421** performance but also provided strong generaliza- **422** tion capabilities. **423**

LoRASC on Instruction-Following tasks. Ta- **424** ble [2](#page-5-3) presents the performance of our proposed **425** method, *LoRASC*, applied to LoRA across sev- **426** eral instruction-following tasks. These instruction- **427** following tasks are particularly challenging due **428**

⁴ [https://github.com/tatsu-lab/stanford_](https://github.com/tatsu-lab/stanford_alpaca/) [alpaca/](https://github.com/tatsu-lab/stanford_alpaca/)

⁵ <https://github.com/declare-lab/instruct-eval>

Figure 2: Performance of *LoRASC* compared to LoRA and COLA across various ranks and learning schedules in a subset of text transfer learning tasks. It can be observed that *LoRASC* consistently achieves stable performance improvements across all ranks and learning schedules, particularly at higher ranks and longer epochs, where *LoRASC* can mitigate performance degradation caused by overfitting.

 to the weak correlation between the training data and the benchmarks, making them entirely out-of- domain tests. Despite this difficulty, our method achieved notable improvements across various eval- uation metrics used in InstructEval and GSM8K. Furthermore, the design of slow-fast updates and noisy tuning still steadily enhanced the perfor- mance of cascading learning, further validating the effectiveness of our approach and motivation.

438 4.2.2 *LoRASC* for CLIP ViT-bigG

 Experiment setting. For the ImageNet-1K vi- sual classification task, to validate the transfer per- formance of our method on larger vision models, we selected CLIP ViT-bigG/14 as our pre-training backbone.We utilized the AdamW optimizer and a cosine scheduler, training for a total of 10 epochs on the ImageNet-1K training set. The batch size was fixed at 64, and the learning rate was chosen **from** $\{1 \times 10^{-4}, 5 \times 10^{-4}, 1 \times 10^{-3}\}$. For evaluation, we first test our model on the ImageNet-1K valida- tion set using top-1 accuracy. To demonstrate the improvement in our method's transferability and robustness, we conducted further tests on robustness **451** benchmarks from [Mao et al.](#page-9-21) [\(2022\)](#page-9-21) for transfer **452** learning tasks. **453**

Evaluation of *LoRASC* on ImageNet and Ro- **454** bustness Benchmarks. Table [3](#page-7-0) showcases the **455** performance of our proposed method, *LoRASC*, ap- **456** plied to LoRA on ImageNet-1K and several robust- **457** ness benchmarks, including IN-V2, IN-C, IN-R, **458** IN-A, IN-SK, and IN-ST. These benchmarks test **459** the model's robustness and generalization ability **460** beyond the standard ImageNet dataset. Our method **461** demonstrates consistent improvements in top-1 ac- **462** curacy across all evaluated benchmarks. *LoRASC* **463** consistently enhances the robustness and general- **464** ization of the ViT-bigG model across these chal- **465** lenging benchmarks, validating the effectiveness **466** of cascading learning, slow-fast updates, and noisy **467** tuning in improving model performance in diverse **468** and robust scenarios. **469**

Method	ImageNet			$IN-V2$ $IN-C$ $IN-R$ $IN-A$		IN-SK	IN-ST
LoRA	87.1	77.7	66.2	87.1	72.6	64.9	24.1
w/ LoRASC							
+ Cascade	87.1	77.5	66.7	88.5	73.6	65.4	24.3
$++$ Slow LoRA	87.7	78.3	66.8	88.1	73.4	65.2	24.1
+++ Noise Tuning	87.8	78.4	66.8	88.7	73.4	65.5	24.4

Table 3: Top-1 accuracy of various methods on ImageNet-1K and 6 robustness benchmarks. The table compares the baseline LoRA with our three proposed techniques. Our approach demonstrates improved robustness on the ViT-bigG model across all the evaluated benchmarks.

			Experts RTE DROP WIC BoolO ReCoRD SST-2 SOuAD		
	2 87.0 53.8 72.4 85.3		81.3	95.5	92.0
5°	88.1 56.7 72.6 87.4		82.2	96.1	92.9
25.	86.7 51.2 70.5 83.5		814	95.5	92.2.
	125 83.8 50.2 70.5 84.5		812	95.1	90.7
	1250 83.8 49.4 69.4 85.3		811	92.9	881

Table 4: Evaluation with varing expert number of *LoRASC*. The highest average performance for each task is highlighted in bold.

470 4.3 Ablation Study and Analysis

 Larger Ranks and Longer Epochs. As shown in Fig. [2,](#page-6-0) *LoRASC* consistently achieves more stable performance on datasets such as SQuAD, DROP, and GSM8K compared to both LoRA and COLA, which also employs a cascading strategy. This validates our motivation: *LoRASC* is a training strategy that retains LoRA's beneficial properties while seamlessly enhancing its fitting ability and robust generalization.

 Ablation for *LoRASC* Expert Cascade Fre- quency. *LoRASC* defaults to updating once per epoch, as each expert completes training on the entire dataset within one epoch. In Table [4,](#page-7-1) we experimented with different update frequencies. In this setting, we trained for a total of 5 epochs, with each epoch consisting of 250 iterations, resulting in a total training period of 1250 iterations. The table shows that having 5 experts, corresponding to one new expert per epoch, yields the optimal performance. Interestingly, we observe that even with 1250 experts, where a new expert is initial- ized every iteration, the model still achieves highly competitive performance. In this extreme case, fol- lowing Algorithm [1,](#page-4-0) the model cannot iterate the learning rate as each backpropagation step is im- mediately followed by the initialization of a new expert. We speculate that the strong generaliza- tion capability of slow cascading compensates for the weak fitting ability in this scenario. With 2 experts(one expert every 2.5 epochs), which aligns

with COLA's default setting for this scenario, the 501 performance is lower than *LoRASC*'s default of one **502** expert per epoch. This may be due to the model 503 being more prone to local optima after 2.5 epochs, 504 which negatively impacts the effectiveness of slow 505 cascading. 506

5 Conclusion 507

In this paper, we address the limitations of fine- **508** tuning large pre-trained models, particularly the is- **509** sue of overfitting and the high computational costs **510** associated with transferring these models to niche **511** tasks. We introduce a novel technique, *LoRASC*, **512** which enhances the Low-Rank Adaptation (LoRA) 513 approach by integrating cascading learning, slow- **514** fast updates, and noisy tuning. Our method aims to **515** improve the fitting capability and generalization of **516** LoRA models without incurring additional compu- **517** tational costs. **518**

We provide a detailed analysis of *LoRASC* and **519** demonstrate its effectiveness through extensive ex- **520** periments in both the natural language processing **521** (NLP) and computer vision (CV) domains. Our **522** method consistently outperforms baseline LoRA **523** models and their variants (LoRA+, Dora) across 524 multiple datasets and tasks, including SuperGLUE, **525** SQuAD, DROP, GSM8K, and various instruction- **526** following benchmarks. Additionally, our method **527** enhances the robustness and transferability of vi- **528** sion models on ImageNet and several robustness **529** benchmarks. **530**

⁵³¹ Limitations

 While *LoRASC* attempts to find a better balance between model convergence and generalization, it does not fundamentally resolve the issue. Our proposed mechanisms of slow-fast updating and noisy tuning can enhance model generalization and prevent overfitting; however, if the magnitude of these adjustments is too large, it may still lead to difficulties in model convergence. Therefore, 540 it is necessary to adjust the α parameter in the slow-fast merging process and λ in the intensity of noise added to each expert according to the specific task. In our experiments, only a few candidate ad- justments were needed to significantly outperform vanilla LoRA, yet this still incurs additional costs. Adaptive adjustment of these parameters according to the task is a direction for future work that we intend to explore.

 Additionally, while this study only explores LoRA cascading learning for single training tasks and finds it to effectively enhance model performance, in practice, we could combine LoRA experts from [m](#page-9-2)ultiple domains, similar to the MoLE [\(Huang](#page-9-2) [and Wei,](#page-9-2) [2024\)](#page-9-2) approach, to further improve model capabilities. In such cases, how to better perform slow cascading would be an interesting issue to **557** address.

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