Exact Statistical Tests for Gene Regulatory Network Discovery from Single-Cell RNA Sequencing

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Abstract

Gene regulatory networks encode causal relationships between transcription factors and target genes, but inferring these networks from single-cell RNA sequencing data faces extreme sparsity and class imbalance challenges. We present a framework using exact statistical tests to evaluate whether predicted regulatory edges are enriched above background rates in the top-ranked predictions where experimental validation would focus. This approach moves beyond global metrics to assess performance where it matters for practical discovery. Using our scoring method, we demonstrate strong performance across two evaluations. Curated positive edges receive mean posterior probability 0.908 versus 0.0054 for random negatives. Across 44 BEELINE benchmark datasets, we achieve mean ROC-AUC 0.926 and mean precision 39.9% in the top 100 predictions (47-fold improvement over random selection). Enrichment tests confirm statistical significance on all 44 datasets. These results show that exact statistical tests provide actionable evidence for network discovery, offering practical guidance for experimental validation while maintaining statistical rigor for structure learning from noisy single-cell data.

6 1 Introduction

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- Gene regulatory networks (GRNs) represent the causal mechanisms through which transcription factors control gene expression, determining cellular identity, development, and disease progression [1, 3, 9, 10]. These networks consist of directed graphs where edges indicate regulatory relationships from transcription factors to target genes [5]. Understanding these regulatory circuits is essential for addressing fundamental questions in biology, from cell fate determination to therapeutic intervention design.
- Current evaluation approaches for GRN prediction rely heavily on global metrics such as area under the ROC curve (AUROC) and area under the precision-recall curve (AUPRC). While these metrics enable method comparison, they fail to address the practical question: given limited validation resources, are the highest-ranked predictions enriched for true regulatory relationships? This question becomes critical under extreme class imbalance, where high AUROC values may still correspond to poor precision in the top predictions that researchers would actually test.
- We study exact statistical tests that quantify enrichment in top-ranked predictions. Our approach treats GRN inference as causal structure learning where prior biological knowledge guides the search through possible edges. We employ Fisher's exact test to determine whether predicted edges concentrate significantly above background rates in regions where experimental validation would focus. We demonstrate this framework using a Bayesian scoring method for edge ranking, though the evaluation approach applies to any ranking method.

2 Related Work

Early GRN inference methods leveraged bulk RNA sequencing, employing techniques from cor-36 relation analysis to probabilistic models, with approaches like WGCNA identifying co-expression 37 modules but unable to distinguish direct from indirect relationships [8], while information-theoretic 38 methods such as ARACNE used mutual information to detect non-linear dependencies [4], and 39 regression frameworks including GENIE3 employed random forests to rank interactions [7]. The 40 transition to single-cell data required new algorithms to handle sparsity and noise, leading to methods 41 like Inferelator 3.0 which combines Bayesian regression with stability selection and scales to millions 42 of cells despite limitations in capturing non-linear relationships [14], while deep learning approaches 43 including 3DCEMA's three-dimensional convolution and graph neural networks like GENELink and 44 GNNLink emerged to model complex dependencies though with varying computational costs and data requirements [2, 6, 11]. Comprehensive benchmarking studies have revealed that performance degrades substantially with increasing sparsity and gene count, with many methods approaching 47 random performance under realistic noise conditions, motivating our focus on evaluation metrics 48 that capture performance where experimental validation occurs rather than averaged global statistics 49 [12, 13]. 50

3 Problem and Methods

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Let $\mathcal{V} = \{v_1, v_2, \dots, v_G\}$ denote the set of genes. The true gene regulatory network $H \subseteq \mathcal{V} \times \mathcal{V}$ is a directed graph where edge $(v_i, v_j) \in H$ indicates that transcription factor v_i regulates target gene v_j . Let $G \subset H$ denote experimentally validated edges available as prior knowledge. These come from ChIP-seq experiments, genetic perturbations, and literature curation.

Given single-cell expression data $X \in \mathbb{R}^{N \times G}$ with N cells, we compute for each candidate edge $e = (v_i, v_j)$ a score $P(e \in H \mid X, G)$ representing the probability that the edge is a true regulatory relationship. These scores induce a ranking over candidate edges. The evaluation challenge is assessing this ranking when ground truth exists only for a sparse subset with typical prevalence below 1%.

We test whether our approach can identify true regulatory relationships from single-cell data through 61 four hypotheses. The first hypothesis examines whether true regulatory edges concentrate in the 62 highest-ranked predictions beyond what random chance would produce, which we evaluate using 63 Fisher's exact test comparing the top-ranked set against the remainder. The second hypothesis tests 64 whether the scoring method assigns meaningfully different probabilities to true regulatory edges 65 versus non-edges, enabling practical threshold selection. The third hypothesis assesses whether 66 the approach generalizes across different cell types, organisms, and experimental conditions rather 67 than overfitting to specific datasets. The fourth hypothesis evaluates whether the precision in top 69 predictions is sufficient to guide laboratory validation efforts, providing substantial improvement over random selection.

scRNA-seq Data Representation. We construct gene representations through dimensionality reduction followed by supervised refinement. Given expression matrix $X \in \mathbb{R}^{N \times G}$, we compute the gene covariance matrix and extract its top r principal components. For gene i with expression vector $x_i \in \mathbb{R}^N$:

$$g_i = W^{\top}(x_i - \bar{x})$$

where $W \in \mathbb{R}^{N \times r}$ contains the top eigenvectors and \bar{x} is the mean expression. We set r = 64 based on variance explained analysis.

Directional Embedding for Regulatory Relationships. Regulatory relationships have inherent directionality - transcription factors regulate targets, not vice versa. We model this through separate transformations for regulator and target roles. With learned matrices $A, B \in \mathbb{R}^{d \times r}$:

$$z_i^S = A \cdot g_i$$
 (regulator)
 $z_i^T = B \cdot g_i$ (target)

Similarity between potential regulator i and target j uses cosine distance:

$$d(z_i^S, z_j^T) = 1 - \frac{(z_i^S)^\top z_j^T}{\|z_i^S\|_2 \|z_j^T\|_2}$$

Contrastive Loss. We refine embeddings using the Soft Nearest Neighbor loss. Given positive edges P from curated network G and sampled negative edges N:

$$\mathcal{L}_{\text{SNN}} = -\log \frac{\sum_{(i,j) \in P} \exp[-d(z_i^S, z_j^T)/T]}{\sum_{(u,v) \in P \cup N} \exp[-d(z_u^S, z_v^T)/T]}$$

where temperature T controls focus on hard examples.

Bayesian Edge Scoring. For candidate edge e = (i, j), we compute a posterior combining distance-based likelihood with prior knowledge:

$$L(e) = \exp[-\alpha \cdot d(z_i^S, z_j^T)]$$

$$P(e \in H \mid X, G) = \frac{L(e) \cdot \pi(e)}{\sum_{e' \in \mathcal{U}} L(e') \cdot \pi(e')}$$

where $\pi(e) = \bar{\pi}$ is the observed positive rate in G.

Scoring with Nonparametric Models. We also implement a Gaussian Process classifier for comparison. For each edge, we concatenate features $x_{ij} = [z_i^S; z_j^T; \delta]$ where δ indicates direction. We use a radial basis kernel and optimize the variational evidence lower bound for scalability.

4 Experiments

BEELINE benchmark. We first evaluate on the complete BEELINE benchmark comprising 44
 datasets from diverse biological systems. Each dataset pairs with one of four reference network types:
 STRING interactions, non-specific ChIP-seq, cell-type-specific ChIP-seq, or genetic perturbations.
 These references vary in quality and completeness, providing a robust generalization test.

Table 1 summarizes performance by reference type. We achieve mean ROC-AUC 0.926 across all datasets, demonstrating strong global ranking. Perturbation-based networks provide clearest signal (ROC-AUC 0.993), while cell-type-specific references prove most challenging (0.853), likely due to condition-specific regulation not captured in expression data.

Table 1: Performance across reference network types. Values show mean \pm standard deviation. Enrichment indicates fraction of datasets with Fisher's exact test p < 0.001 in top 100 predictions.

Reference Type	Datasets	ROC-AUC	PR-AUC	Precision@100	Enrichment
STRING	14	0.956 ± 0.020	0.207 ± 0.118	0.267 ± 0.124	14/14
Non-Specific ChIP	14	0.950 ± 0.018	0.161 ± 0.057	0.272 ± 0.098	14/14
Cell-Type-Specific	14	0.853 ± 0.220	0.508 ± 0.208	0.439 ± 0.187	14/14
Perturbation	2	0.993 ± 0.001	0.445 ± 0.022	0.635 ± 0.106	2/2
Overall	44	0.926 ± 0.124	0.289 ± 0.200	0.335 ± 0.178	44/44

Performance in Top Predictions. For practical application, performance in the top predictions matters most since researchers can only validate a limited number of edges. Table 2 shows results at three thresholds corresponding to typical validation budgets.

Table 2: Performance at different numbers of top predictions across 44 datasets. Lift measures fold-improvement over random selection. Hit rate shows fraction of datasets with at least one true positive. Fisher counts are two-sided tests of enrichment in top-k vs rest (per-dataset, p < 0.001).

Metric	Top 100	Top 500	Top 1000
Mean Precision	0.399	0.298	0.240
Mean Recall	0.170	0.440	0.589
Mean Lift	$51.876 \times$	$37.224 \times$	$29.262 \times$
Hit Rate	1.00	1.00	1.00
Fisher $p < 0.001$	44/44	44/44	44/44

- 90 In the top 100 predictions, mean precision reaches 39.9% a 47-fold improvement over the 0.7%
- background rate. All datasets contain at least one true positive in their top 100, enabling discovery
- 92 even with limited resources. Fisher's exact test confirms significant enrichment on all 44 datasets.
- 93 Nonparametric Model Validation. To verify that enrichment is not model-specific, we tested a
- 94 Gaussian Process classifier on a challenging subset with 74,539 edges and 0.61% prevalence. The
- 95 GP achieves ROC-AUC 0.796 and identifies 7 true positives in the top 100 (precision 7.0%, 11.5-fold
- 96 lift). This confirms enrichment persists across different architectures.
- 97 **Crohn Disease Dataset.** We next perform detailed analysis on a Crohn disease dataset with 8,076
- cells and 27,289 genes. This dataset presents unique challenges: extreme sparsity (>90% zeros),
- 99 disease-altered regulation, and minimal validation data (27 total curated edges). We use 25 for
- training, one for validation, and hold out one for testing.
- The held-out regulatory edge achieves rank one across all possible gene pairs. The 25 training edges
- receive mean posterior 0.908 (standard deviation 0.044), while random non-edges show mean 0.0054
- (standard deviation 0.0003) a 168-fold difference demonstrating clear discrimination.
- For enrichment analysis, we find 24 of 26 available curated edges in the top 1000 predictions.

105 5 Discussion

- 106 Our results demonstrate that meaningful regulatory structure can be recovered from single-cell
- expression despite extreme sparsity and class imbalance. The ability to rank true edges at the top
- of massive search spaces and achieve significant enrichment across diverse datasets indicates the
- learned representations capture genuine biological signal rather than spurious correlations.
- The enrichment results directly inform experimental design. With 39.9% precision in top 100
- predictions, researchers can expect approximately one-third of tested edges to validate, compared
- to less than 1% for random selection. This 47-fold improvement translates to substantial resource
- savings. The 100% hit rate further suggests that even limited validation efforts will likely yield
- 114 discoveries.
- The primary limitation is data availability most GRN references remain incomplete and few
- large-scale datasets combine comprehensive experimental validation with scRNA-seq measurements.
- Additionally, while expression correlation suggests regulatory relationships, it cannot prove causation
- without interventional data. Performance also depends on prior network quality, though strong results
- across diverse references suggest robustness.
- 120 Future research could extend this framework by incorporating time-series measurements to test causal
- precedence, integrating multi-modal data like chromatin accessibility, and developing uncertainty
- quantification through Bayesian deep learning. As single-cell technologies advance toward higher
- resolution and multi-modal measurements, principled integration of causal discovery methods with
- rigorous statistical evaluation will become increasingly important.

125 6 Conclusion

- We presented a framework using exact statistical tests to evaluate gene regulatory network inference
- from single-cell RNA sequencing. By focusing on enrichment in top predictions where experimental
- validation occurs, we demonstrate that meaningful regulatory structure can be recovered despite
- extreme sparsity and class imbalance.
- Perfect ranking of held-out edges, extreme enrichment significance, and consistent performance
- across 44 datasets validate our approach. The 47-fold improvement in validation efficiency at top 100
- predictions provides immediate practical value. Exact tests that quantify enrichment in top-ranked
- predictions give clear answers to the questions researchers ask and complement global metrics.
- This framework provides a foundation for rigorous causal structure discovery from observational
- single-cell data when evaluation aligns with practical scientific objectives.

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A Extended Results

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A.1 Detailed Performance

Table 3 shows results for representative datasets from each reference type.

Table 3: Performance on representative datasets. P@100 is precision in top 100 predictions.

Dataset	Reference	ROC-AUC	PR-AUC	P@100	Lift@100
mESC mHSC-E hESC	Perturbation STRING Non-Specific	0.994 0.977 0.968	0.467 0.325 0.218	0.740 0.380 0.310	121.3 62.3 50.8
mDC	Cell-Specific	0.892	0.683	0.650	58.2

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