

# 000 001 002 003 004 005 006 007 008 009 010 011 012 013 014 015 016 017 018 019 020 021 022 023 024 025 026 027 028 029 030 031 032 033 034 035 036 037 038 039 040 041 042 043 044 045 046 047 048 049 050 051 052 053 LOOKAHEADKV: FAST AND ACCURATE KV CACHE EVICTION BY GLIMPSING INTO THE FUTURE WITHOUT GENERATION

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Paper under double-blind review

## ABSTRACT

Transformer-based large language models (LLMs) rely on key-value (KV) caching to avoid redundant computation during autoregressive inference. While this mechanism greatly improves efficiency, the cache size grows linearly with the input sequence length, quickly becoming a bottleneck for long-context tasks. Existing solutions mitigate this problem by evicting prompt KV that are deemed unimportant, guided by estimated importance scores. Notably, a recent line of work improves eviction quality by “glimpsing into the future”, in which a low-cost draft generator first produces a surrogate response that mimics the target model’s true response, which is subsequently used to estimate the importance scores of cached KV. In this paper, we propose LookaheadKV, a lightweight eviction framework that leverages the strength of surrogate future response without the need for costly draft generation. LookaheadKV augments transformer layers with parameter-efficient modules trained to predict true importance scores with high accuracy. Our design ensures negligible runtime overhead comparable to existing inexpensive heuristics, while achieving accuracy superior to more costly approximation methods. Extensive experiments on long-context understanding benchmarks, across a wide range of models, demonstrate that our method not only outperforms recent competitive baselines in long-context understanding tasks by 25%, but also reduces the eviction cost by up to 14.5 $\times$ , leading to significantly faster time-to-first-token.

## 1 INTRODUCTION

Long context length of Large Language Models (LLMs) is becoming increasingly critical for many emerging applications: processing long documents (Bai et al., 2024; Wang et al., 2024a; Hsieh et al., 2024), repository-level code understanding and generation (Luo et al., 2024; Liu et al., 2024; Jimenez et al., 2024), in-context learning (Li et al., 2025), extension to long multi-modal inputs such as video (Wang et al., 2024b), etc. However, a central challenge in enabling these applications is that the key-value (KV) cache size grows linearly in sequence length, which rapidly becomes a bottleneck for inference, restricting scalable deployment of such applications on both mobile devices and the cloud. For example, even for moderate-sized models, such as LLaMA3.1–70B (Dubey et al., 2024) in half-precision, storing a single 64K-token sequence already takes up 40GB of memory, while scaling to 512K tokens requires 160GB, exceeding the memory capacity of high-end consumer hardware.

A growing line of work addresses this challenge by identifying salient tokens to achieve effective KV cache eviction without loss of performance (Li et al., 2024; Cai et al., 2024; Galim et al., 2025; Wang et al., 2025; Zhang et al., 2023). Early methods often rely on simple heuristics, in which token importance is estimated based on the self-attention scores of the input tokens. SnapKV (Li et al., 2024), for instance, leverages the attention weights between the suffix of the input and the preceding context to estimate the importance of each prompt token. However, investigations in recent studies (SpecKV (Galim et al., 2025), LAQ (Wang et al., 2025)) reveal that leveraging the model’s response, rather than the input suffix, can greatly improve the eviction quality. Furthermore, they show that

Source code to reproduce our results is available, released in supplementary.

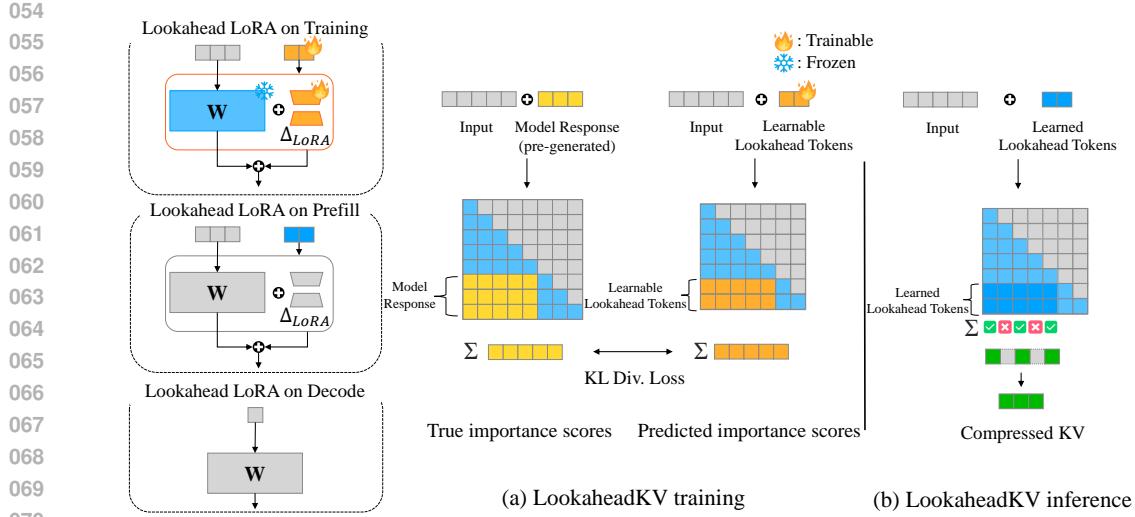


Figure 1: (a) Overview of LookaheadKV training (b) Overview of LookaheadKV inference.

a low-cost generated draft response, which closely approximates the true response, can serve as a powerful proxy for accurately estimating the importance scores. For example, SpecKV employs a smaller auxiliary model to produce draft tokens to approximate the target model’s response, while Lookahead Q-Cache (LAQ) first applies a cheap KV eviction scheme to the target model, such as SnapKV, to obtain draft tokens, which in turn are used to approximate true importance scores.

While these draft-based methods substantially improve eviction quality, they often struggle with a fundamental trade-off between performance and efficiency, due to the need for costly draft token generation. Figure 2 presents the trade-off between accuracy and overhead of different approaches using the QASPER benchmark (Dasigi et al., 2021) and LLaMA3.1-8B-Instruct (Dubey et al., 2024) with a cache budget size of 128. While cheaper approaches like SnapKV are fast, inducing minimal overhead, they suffer a severe performance degradation under highly constrained budget settings. On the other hand, LAQ (Wang et al., 2025), a draft-based approach, shows impressive results even in extremely limited budget settings. However, it incurs a prohibitive computational overhead by generating an extra draft response, which limits its practicality in latency-sensitive applications such as mobile devices.

To overcome this limitation, we introduce LookaheadKV, a novel KV cache eviction method that augments LLMs with parameter-efficient modules, capable of accurately predicting future attention patterns, without the need for costly draft token generation. As shown in Figure 2, our method effectively overcomes the accuracy-overhead trade-off, achieving minimal performance loss with negligible overhead. LookaheadKV, as depicted in Figure 1, our method employs a set of learnable special tokens, together with *Lookahead LoRA* modules, novel low-rank adapters that selectively activate for the special tokens, to produce queries that can reliably estimate token-importance scores. By fine-tuning these modules to predict the true importance scores, LookaheadKV effectively minimizes the quality loss incurred by KV cache eviction with marginal inference overhead.

To rigorously assess the effectiveness of LookaheadKV, we evaluate it on a diverse set of long-context benchmarks (Bai et al., 2024; Hsieh et al., 2024; Ye et al., 2025) across multiple models of varying sizes (Dubey et al., 2024; Yang et al., 2025). Experimental results consistently demonstrate that LookaheadKV outperforms strong baselines across multiple budgets and context lengths while incurring significantly less eviction latency.

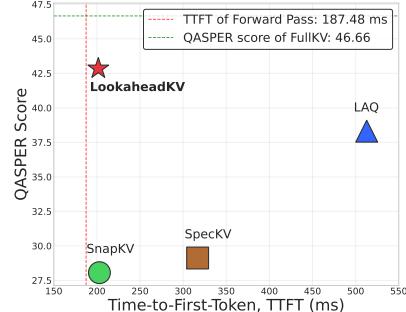


Figure 2: Accuracy-overhead Trade-off across KV cache eviction methods.

108 To summarize, our contributions are as follows:  
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110 • We propose LookaheadKV, to the best of our knowledge, the first KV cache eviction frame-  
 111 work that employs learnable lookahead tokens and special LoRA modules to accurately  
 112 predict the importance scores from the model’s true response without generating costly  
 113 approximate response.  
 114 • Through extensive experiments, we demonstrate that the proposed approach is effective  
 115 and robust across different models and context lengths, and especially under low-budget  
 116 settings, making our method particularly useful in resource-constrained environments.  
 117 • By conducting a rigorous analysis of eviction latency, both theoretically and empirically,  
 118 we demonstrate that our method incurs negligible eviction overhead of less than 2.16% at  
 119 32K context length, while being 14.5× faster than draft-based methods.

120  
 121 **2 BACKGROUND**  
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123 The primary objective of the KV cache eviction methods considered in this work, including our  
 124 proposed approach, is to accurately estimate the importance score of individual key-value pairs of  
 125 prompt tokens using attention weights, in order to guide the eviction process. In the following  
 126 section, we formally define the problem of KV cache eviction and briefly discuss how prior methods  
 127 have approached it.

128 **KV cache eviction using importance scores.** Let  $X = \{x_1, \dots, x_{n_{in}}\}$  be an input token sequence  
 129 (e.g., a user instruction, part of a code snippet, etc.) and  $Y = \{y_1, \dots, y_{n_{out}}\}$  the model’s generated  
 130 response to  $X$ . For a given layer and attention head in an LLM, the attention scores of the complete  
 131 sequence are given by:

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$$\mathbf{Q} = \begin{bmatrix} \mathbf{X} \\ \mathbf{Y} \end{bmatrix} \mathbf{W}_q \quad \mathbf{K} = \begin{bmatrix} \mathbf{X} \\ \mathbf{Y} \end{bmatrix} \mathbf{W}_k \quad \mathbf{A} = \text{Softmax}\left(\frac{\mathbf{Q} \mathbf{K}^\top}{\sqrt{d}}\right), \quad (1)$$

133 where  $\mathbf{X} = [\mathbf{x}_1, \dots, \mathbf{x}_{n_{in}}]^\top \in \mathbb{R}^{n_{in} \times d}$  and  $\mathbf{Y} = [\mathbf{y}_1, \dots, \mathbf{y}_{n_{out}}]^\top \in \mathbb{R}^{n_{out} \times d}$  are the hidden states  
 134 of the input prompt and model-generated response, respectively. For better readability, we omit  
 135 the layer and head index. We define the ground-truth importance scores  $\mathbf{s}_{GT} = [s_1, \dots, s_{n_{in}}]$  of the  
 136 KV cache as the average cross-attention scores between the queries of  $\mathbf{Y}$  and the keys of  $\mathbf{X}$ , i.e.,  
 137  $s_j = \frac{1}{n_{out}} \sum_{i=n_{in}+1}^{n_{in}+n_{out}} \mathbf{A}_{i,j}$ . Intuitively, these scores quantify the relative contribution of each prompt  
 138 token’s key-value pair to the model’s response generation. Based on these scores, the pruned KV  
 139 cache can be obtained by retaining a subset of (e.g., TopK) important KV pairs to minimize the  
 140 attention output perturbation, such that:

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$$\text{Attn}(x, \mathbf{KV}_{\text{orig}}) \approx \text{Attn}(x, \mathbf{KV}_{\text{GT}}), \quad (2)$$

142 where  $\mathbf{KV}_{\text{orig}}$  and  $\mathbf{KV}_{\text{GT}}$  are the original and evicted KV cache using the ground-truth importance  
 143 scores, respectively.

144 However, since the model’s true future response is unknown during the prefill phase, such scores  
 145 cannot be computed directly. Consequently, prior methods resorted to constructing a surrogate re-  
 146 sponse sequence  $\tilde{\mathbf{Y}} = [\tilde{y}_1, \dots, \tilde{y}_{n_{\text{window}}}]^\top \in \mathbb{R}^{n_{\text{window}} \times d}$  to approximate the model’s (partial) future  
 147 response and predict the attention pattern:

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$$\tilde{\mathbf{Q}} = \begin{bmatrix} \mathbf{X} \\ \tilde{\mathbf{Y}} \end{bmatrix} \mathbf{W}_q \quad \tilde{\mathbf{K}} = \begin{bmatrix} \mathbf{X} \\ \tilde{\mathbf{Y}} \end{bmatrix} \mathbf{W}_k \quad \tilde{\mathbf{A}} = \text{Softmax}\left(\frac{\tilde{\mathbf{Q}} \tilde{\mathbf{K}}^\top}{\sqrt{d}}\right), \quad (3)$$

149 resulting in the estimated importance score vector  $\mathbf{s}_{\text{approx}} = [\tilde{s}_1, \dots, \tilde{s}_{n_{in}}]$ , whose entries are computed  
 150 as  $\tilde{s}_j = \frac{1}{n_{\text{window}}} \sum_{i=n_{in}+1}^{n_{in}+n_{\text{window}}} \tilde{\mathbf{A}}_{i,j}$ . In short, these methods aim to obtain the estimated score vector  
 151 whose ranking is similar to that of the ground-truth, such that the overlap between the retained KV  
 152 pairs and  $\mathbf{KV}_{\text{GT}}$  is high. Various approaches have been suggested to approximate the future response  
 153 for effective KV cache eviction.

154 **SnapKV.** SnapKV (Li et al., 2024) proposes to use the suffix of input prompt to compute the estimate  
 155 of the true future importance scores. Because SnapKV requires only marginal extra computation to

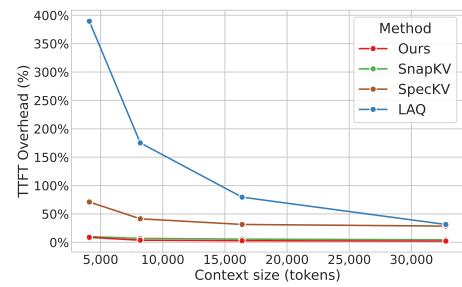
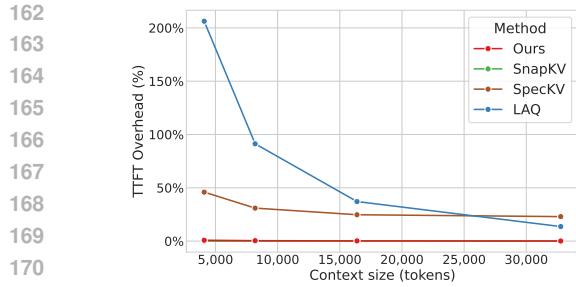


Figure 3: Time-to-First-Token (TTFT) latency overhead ratio across context lengths. Similar to SnapKV, LookaheadKV introduces negligible TTFT overhead across all tested context lengths; draft-based methods (LAQ, SpecKV) incur substantial latency, especially for shorter contexts.

perform eviction, as it uses attention weights that are already computed during the prefill forward pass, it has widely been adopted as a cheap and effective heuristic for KV cache eviction.

**SpecKV and LAQ.** Recently, several methods have proposed to use a low-cost generator to generate a (partial) approximate response first, and subsequently use it to estimate the true future importance scores. Notably, SpecKV (Galim et al., 2025) employs a smaller LLM to first generate a draft response, while Lookahead Q-Cache (LAQ) (Wang et al., 2025) first applies SnapKV to the target model to generate a draft response, which is in turn used to approximate the future importance.

These draft-based methods have consistently shown superior performance compared to cheaper heuristics (Li et al., 2024), demonstrating the effectiveness of employing surrogate future response, i.e., by “glimpsing into the future”. However, the extra draft generation step still incurs substantial additional compute, resulting in significant increase in latency, as shown in Figure 3. In summary, existing methods face a clear trade-off: inexpensive heuristics are fast but less accurate, whereas draft-based techniques improve performance at the cost of increased inference time.

### 3 PROPOSED METHOD: LOOKAHEADKV

To overcome the challenge of fast and accurate importance prediction, we introduce LookaheadKV, a framework that augments the LLM with a set of lightweight learnable modules which are optimized to predict ground-truth importance scores and guide the eviction process. LookaheadKV achieves the best of both worlds: 1) it eliminates the need for generating a draft response for each query, resulting in significantly faster KV cache eviction, and 2) it employs learned special tokens that serve as approximate future response for importance estimation, leveraging the strength of draft-based methods. The following section (and Figure 1) presents the detailed workflow of LookaheadKV.

#### 3.1 MAIN COMPONENTS

**Learnable Lookahead Tokens.** LookaheadKV initially performs KV cache eviction using a set of learnable special tokens during the pre-fill phase, and subsequently decodes auto-regressively with the retained KV cache. Specifically, for given input prompt tokens  $X$ , LookaheadKV appends a sequence of trainable “soft” lookahead tokens  $L = \{l_1, \dots, l_{n_{\text{lookahead}}}\}$  whose queries in the attention layers are used to estimate the attention pattern of the true model response. In essence, these tokens are trained to compress the attention information of the true response to serve as the “observation window” in the eviction phase. **These tokens are new tokens added to the vocabulary, each with an embedding of shape  $\mathbb{R} \in d$  that is randomly initialized.** Note that the lookahead tokens are used during the prefill stage only for eviction, and adds zero additional overhead for decoding.

**Lookahead LoRA.** To enhance the quality of estimation, we introduce *Lookahead LoRA*, a novel low-rank adapter module that only activates for the lookahead tokens. **While predicting attention patterns across all layers and heads using only the lookahead tokens is challenging due to their limited capacity, Lookahead LoRA provides complementary performance gains by allowing these tokens to learn richer representations, enabling their queries to more accurately predict token importance.**

The selective activation mechanism of the LoRA modules ensures that the outputs of normal input tokens are unchanged, preserving the original model behavior. Moreover, since the original model weights remain unaltered, LookaheadKV modules can be selectively enabled or disabled depending on the particular requirements of a given application, thereby broadening the method’s applicability.

Combining the modules together, LookaheadKV computes the queries and keys of the complete sequence as follows:

$$\mathbf{Q}_{\text{LKV}} = \begin{bmatrix} \mathbf{X} \\ \mathbf{L} \end{bmatrix} \mathbf{W}_q + \begin{bmatrix} \mathbf{0} \\ \mathbf{L} \end{bmatrix} \Delta \mathbf{W}_q \quad \mathbf{K}_{\text{LKV}} = \begin{bmatrix} \mathbf{X} \\ \mathbf{L} \end{bmatrix} \mathbf{W}_k + \begin{bmatrix} \mathbf{0} \\ \mathbf{L} \end{bmatrix} \Delta \mathbf{W}_k, \quad (4)$$

where  $\mathbf{L} \in \mathbb{R}^{n_{\text{lookahead}} \times d}$  denotes the hidden states of the lookahead embeddings, and  $\Delta \mathbf{W}_q, \Delta \mathbf{W}_k$  are the Lookahead LoRA modules for query and key projections. Similar to prior methods (Li et al., 2024), we use the attention matrix  $\mathbf{A}_{\text{LKV}} = \text{Softmax}(\frac{\mathbf{Q}_{\text{LKV}} \mathbf{K}_{\text{LKV}}^\top}{\sqrt{d}})$ , to estimate the importance score  $\tilde{s}_j = \frac{1}{n_{\text{lookahead}}} \sum_{i=n_{\text{in}}+1}^{n_{\text{in}}+n_{\text{lookahead}}} \mathbf{A}_{\text{LKV}}_{i,j}$ , and retain Top-K KV pairs with the highest importance scores.

### 3.2 LOOKAHEADKV TRAINING

We train LookaheadKV modules to compress the attention pattern of the true future response, using the model-generated responses as target. Specifically, given a data pair  $(X, Y)$ , one iteration of LookaheadKV training consists of the following steps:

1. **GT Forward Pass.** For each layer  $l = 1, \dots, L$  and head  $h = 1, \dots, H$ , the ground-truth importance scores  $\mathbf{s}_{\text{GT}}^{l,h}$  between the input prompt  $X$  and model-generated response  $Y$  are computed.
2. **Lookahead Forward Pass.** Similarly, for each layer  $l$  and head  $h$ , we obtain the importance score estimates  $\mathbf{s}_{\text{LKV}}^{l,h}$  between the input prompt  $X$  and the lookahead tokens  $L$ .
3. **Loss Computation.** We first normalize all score vectors so that they sum to 1, and compute the average KL divergence loss between the GT and LookaheadKV importance scores across all heads and layers:

$$\mathcal{L} = \frac{1}{L} \frac{1}{H} \sum_l^L \sum_h^H \text{KL}(\text{Norm}(\mathbf{s}_{\text{GT}}^{l,h}) \parallel \text{Norm}(\mathbf{s}_{\text{LKV}}^{l,h})). \quad (5)$$

The loss is backpropagated to update the weights of the lookahead embeddings and Lookahead LoRA modules, while all other LLM layers remain frozen. The pseudo-code for LookaheadKV training and eviction is given in Algorithm 1 and Algorithm 2.

**Training Objective.** We want to ultimately optimize the similarity of the ranking between the two importance score vectors, such that we obtain TopK indices identical to those from ground-truth importance scores. Inspired from works on distilling attention scores (Wang et al., 2020; Izacard & Grave, 2021), we minimize the KL divergence between these normalized attention scores. As our attentions scores are normalized, this KL divergence is equivalent to the popular ListNet (Cao et al., 2007) ranking loss, with  $\phi$  of ListNet as identity instead of exp. We note that, while we employ normalized average attention scores as the importance metric throughout the experiments, any suitably defined token-wise importance metric can be used for training, provided that it can be computed for each token.

**Lookahead LoRA Overhead.** In principle, one can apply Lookahead LoRA to only a subset of the linear layers to tradeoff accuracy and latency. However, even when Lookahead LoRA is applied to every linear layer, there is a minor increase ( $>1.3\%$ ) in latency compared to not using Lookahead LoRA at all (see Table 5 for ablation results), while significantly boosting performance compared to not using LoRA. Consequently, we train LookaheadKV with LoRA modules applied to all linear layers.

To avoid materializing the full attention score matrix, we use FlashAttention (Dao et al., 2022) in the forward pass, coupled with eager attention for importance score computation and loss backpropagation, as detailed in Section C.

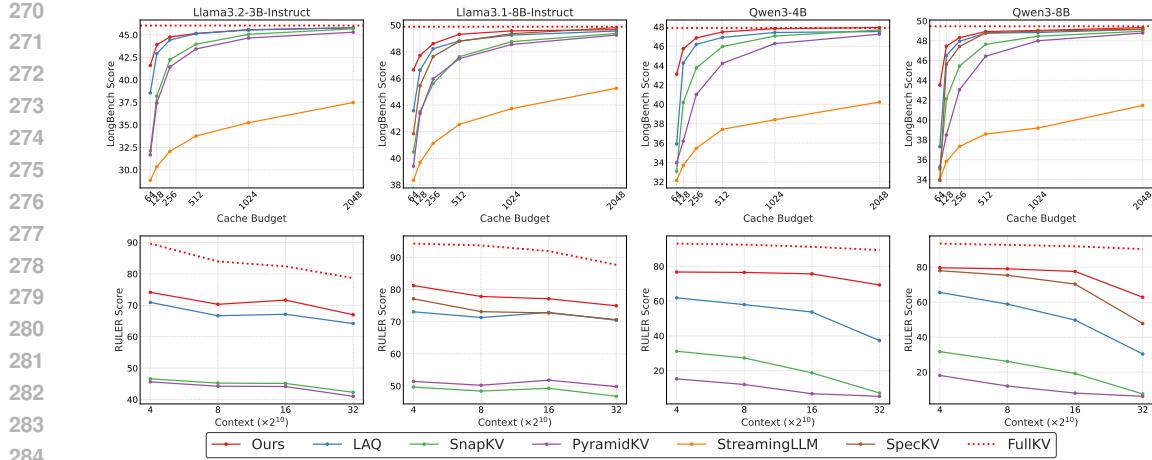


Figure 4: Top row: Average LongBench results across multiple budgets and models. Bottom row: Average RULER results across varying context lengths with a fixed budget of 128. Across all tested models, budgets and context lengths, LookaheadKV consistently demonstrates superior performance.

## 4 EXPERIMENTS

### 4.1 TRAINING

**Dataset.** To encourage the model to learn from diverse attention patterns, we curate training samples of varying lengths and sources, comprising of both instruction-following datasets as well as pretraining texts. We collect 50K samples from the long\\_sft subset of the ChatQA2 (Xu et al., 2025) dataset, 20K samples from the Tulu (Lambert et al., 2025) instruction-following dataset, 7K samples from the Stack (Kocetkov et al., 2023), and 9K few-shot completion data samples that we create based on the training splits of the MetaMath, ARC, and HellaSwag datasets, originally curated in Pal et al. (2024). For instruction-following data, we remove the last assistant response, and use the target model to obtain the  $(X, Y)$  pairs of input prompt and model response. For pretraining documents, we first truncate the text at random positions to obtain  $X$ , and use the target model to complete the sequence to obtain  $Y$ . We limit the maximum input sequence length to 16K, and generate all training responses using greedy decoding and max generation length of 512.

**Training Details.** We apply LookaheadKV on two widely used open-source architectures, LLaMA (Dubey et al., 2024) and Qwen (Yang et al., 2025), covering three model sizes each: LLaMA3.2-1B, LLaMA3.2-3B, LLaMA3.1-8B, Qwen3-1.7B, Qwen3-4B, and Qwen3-8B. For all models, we set the lookahead size  $n_{\text{lookahead}} = 32$ , and apply LoRA to all projection and feed-forward modules ( $\mathbf{W}_q$ ,  $\mathbf{W}_k$ ,  $\mathbf{W}_v$ ,  $\mathbf{W}_o$ ,  $\mathbf{W}_{up}$ ,  $\mathbf{W}_{down}$ , and  $\mathbf{W}_{gate}$ ) with rank  $r = 8$  and scaling factor  $\alpha = 32$ . This configuration introduces less than 0.5% additional trainable parameters across all models, as summarized in Table 1. Full hyperparameter settings are provided in Table 16.

### 4.2 EVALUATION SETUP

We evaluate our method on two popular long-context benchmarks: LongBench (Bai et al., 2024) and RULER (Hsieh et al., 2024). LongBench is a multi-task benchmark that comprehensively assesses long-context understanding across diverse tasks, such as question answering, summarization, few-shot learning, and code completion. We report results on the 16 English tasks, and use the average score as the main metric. RULER is another multi-task synthetic benchmark, primarily comprising 13 Needle-in-a-Haystack-style subtasks. Each sample can be constructed at varying sequence

Table 1: Additional trainable parameters introduced by LookaheadKV.

| Model       | Trainable Params |            |
|-------------|------------------|------------|
|             | Params           | % of Model |
| LLaMA3.2-1B | 5.4M             | 0.44       |
| LLaMA3.2-3B | 11.9M            | 0.37       |
| LLaMA3.1-8B | 20.6M            | 0.26       |
| Qwen3-1.7B  | 8.5M             | 0.49       |
| Qwen3-4B    | 16.2M            | 0.40       |
| Qwen3-8B    | 21.5M            | 0.26       |

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Table 2: **MT-Bench** evaluation results. **Bold** and **underlined** values indicate best and second best scores, respectively.

| Model                     | Budget | PyramidKV   | SnapKV      | StreamingLLM | SpecKV      | LAQ         | LookaheadKV |
|---------------------------|--------|-------------|-------------|--------------|-------------|-------------|-------------|
| <i>FullKV score: 5.72</i> |        |             |             |              |             |             |             |
| LLaMA3.2-1B               | 64     | 4.64        | 4.70        | 4.54         | N/A         | <u>5.03</u> | <b>5.21</b> |
|                           | 128    | 5.10        | 5.39        | 4.94         | N/A         | <u>5.45</u> | <b>5.60</b> |
|                           | 256    | 5.49        | <b>5.67</b> | 5.37         | N/A         | <u>5.64</u> | 5.62        |
|                           | 512    | <u>5.73</u> | 5.71        | 5.68         | N/A         | <u>5.73</u> | <b>5.79</b> |
| <i>FullKV score: 7.35</i> |        |             |             |              |             |             |             |
| LLaMA3.2-3B               | 64     | 6.30        | 6.28        | 5.96         | <u>6.52</u> | 6.48        | <b>6.87</b> |
|                           | 128    | 6.93        | <u>7.03</u> | 6.42         | <u>7.02</u> | 6.93        | <b>7.26</b> |
|                           | 256    | 7.19        | <u>7.30</u> | 7.20         | 7.28        | <b>7.43</b> | <u>7.30</u> |
|                           | 512    | <b>7.46</b> | 7.24        | 7.24         | <u>7.34</u> | 7.27        | 7.15        |
| <i>FullKV score: 7.77</i> |        |             |             |              |             |             |             |
| LLaMA3.1-8B               | 64     | 6.85        | 6.80        | 6.17         | 6.77        | <u>7.1</u>  | <b>7.26</b> |
|                           | 128    | 7.39        | 7.50        | 6.84         | 7.34        | <u>7.54</u> | <b>7.63</b> |
|                           | 256    | 7.76        | 7.72        | 7.41         | 7.84        | 7.72        | <b>7.92</b> |
|                           | 512    | 7.82        | 7.78        | 7.73         | <b>7.89</b> | 7.85        | 7.86        |
| <i>FullKV score: 7.19</i> |        |             |             |              |             |             |             |
| Qwen3-1.7B                | 64     | 5.81        | 5.95        | 5.83         | N/A         | <u>6.19</u> | <b>6.70</b> |
|                           | 128    | 6.38        | 6.65        | 6.16         | N/A         | <u>6.91</u> | <b>7.12</b> |
|                           | 256    | 6.90        | 6.94        | 6.91         | N/A         | <u>7.02</u> | <b>7.20</b> |
|                           | 512    | 7.09        | 7.03        | 7.08         | N/A         | <u>7.20</u> | <b>7.29</b> |
| <i>FullKV score: 8.02</i> |        |             |             |              |             |             |             |
| Qwen3-4B                  | 64     | 6.85        | 6.60        | 6.24         | 7.05        | 7.06        | <b>7.69</b> |
|                           | 128    | 7.55        | 7.71        | 7.24         | 7.78        | 7.70        | <b>8.12</b> |
|                           | 256    | 7.90        | <b>8.20</b> | 7.87         | 8.11        | 8.12        | 8.06        |
|                           | 512    | <b>8.15</b> | 8.12        | 8.00         | 8.02        | <u>8.06</u> | 8.08        |
| <i>FullKV score: 8.48</i> |        |             |             |              |             |             |             |
| Qwen3-8B                  | 64     | 7.33        | 7.26        | 6.81         | <u>7.69</u> | 7.58        | <b>8.04</b> |
|                           | 128    | 7.85        | 7.94        | 7.64         | <u>7.97</u> | 8.24        | <b>8.41</b> |
|                           | 256    | 8.42        | 8.43        | 8.34         | 8.45        | <b>8.56</b> | 8.51        |
|                           | 512    | 8.43        | 8.36        | 8.44         | 8.50        | <b>8.63</b> | <u>8.53</u> |

lengths, allowing systematic evaluation of scaling behavior. Similar to LongBench, we use average score as the main metric, and report the results at 4K, 8K, 16K and 32K context lengths.

**Baselines.** We compare our method against popular KV-cache eviction methods: **1) SnapKV** (Li et al., 2024), **2) PyramidKV** (Cai et al., 2024), and **3) StreamingLLM** (Xiao et al., 2024). Additionally, we include stronger, more recent baselines that involve costly approximate future response generation, including **4) Lookahead Q-Cache** (LAQ) (Wang et al., 2025), and for 8B-scale models, **5) SpecKV** (Galim et al., 2025). In all experiments, Llama3.2-1B-Instruct and Qwen3-1.7B are used as draft models for Llama3.1-8B-Instruct and Qwen3-8B, respectively. We follow the standard eviction configuration settings for all baseline methods, which we detail in Section F

### 4.3 PERFORMANCE RESULTS

**LongBench evaluation.** Figure 4 shows the average LongBench scores of LookaheadKV and baselines, across cache budget settings ranging from 64 to 2048. Our method consistently demonstrates superior performance across all models and all budgets tested, demonstrating the effectiveness and robustness of our approach. Overall, results show that expensive draft-based methods, e.g., LAQ and SpecKV, outperform cheaper baselines, corroborating that employing approximate future response for importance estimation is effective. Nevertheless, our method significantly outperforms the draft-based approaches, especially at lower budget settings, highlighting that learning to estimate future importance is crucial for performance preservation. Due to space limitation, we report the results of 1B-scale models in Section E.

**RULER evaluation.** We report the RULER evaluation results of all methods with a fixed budget of 128 in Figure 4 (1B-scale results are provided in Section E). LookaheadKV consistently outperforms other baseline approaches here as well, maintaining strong performance across all evaluated context lengths. Further, note that while we limit the maximum training sequence length of LookaheadKV to 16K, our method generalizes to longer context length of 32K. We conduct additional experiments on the impact of training context length in Section 5.4.

378  
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381 Table 3: Theoretical and empirical cost analysis of LLaMA3.1-8B at  $C = 128$ .  
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| Context Length | Method             | Theoretical Cost |                     |           |                    | Empirical Cost |                    |
|----------------|--------------------|------------------|---------------------|-----------|--------------------|----------------|--------------------|
|                |                    | Compute (TFLOPs) | Memory Traffic (GB) | TTFT (ms) | TTFT Overhead (ms) | TTFT (ms)      | TTFT Overhead (ms) |
| 8192           | Forward Pass Only  | 136              | 13                  | 257       | N/A                | 291            | N/A                |
|                | LookaheadKV (ours) | 137              | 13                  | 258       | 1.03               | 302            | 11                 |
|                | SnapKV             | 136              | 13                  | 257       | 0.01               | 311            | 20                 |
|                | SpecKV             | 159              | 81                  | 337       | 79.53              | 411            | 121                |
|                | LAQ                | 137              | 445                 | 492       | 234.59             | 800            | 509                |
| 32768          | Forward Pass Only  | 928              | 13                  | 1754      | N/A                | 1760           | N/A                |
|                | LookaheadKV (ours) | 929              | 13                  | 1755      | 1.74               | 1798           | 38                 |
|                | SnapKV             | 928              | 13                  | 1754      | 0.01               | 1838           | 78                 |
|                | SpecKV             | 1115             | 106                 | 2156      | 402.80             | 2263           | 503                |
|                | LAQ                | 930              | 451                 | 1993      | 239.26             | 2314           | 554                |

392  
393  
394 **Long-Form output evaluation.** We further  
395 evaluate LookaheadKV on the **HTML to TSV**  
396 task from LongProc (Ye et al., 2025), which  
397 involves extracting structured information from  
398 long HTML documents and converting it into  
399 TSV format. This benchmark tests not only the  
400 model’s ability to process long-context inputs, but  
401 also its capacity to generate long-form outputs.  
402 We assess LookaheadKV and baseline methods  
403 under two input–output settings: 12K–0.5K and  
404 23K–2K tokens, both at a fixed cache budget ra-  
405 tio of 30%.

406 Figure 5 presents the results on the HTML to  
407 TSV task. Across both sequence-length configu-  
408 rations, LookaheadKV consistently outperforms  
409 prior approaches. We hypothesize that Looka-  
410 headKV, which learns to predict the attention pattern of the entire future response, is particularly  
411 superior in long-form generation tasks compared to draft-based methods that rely only on partial  
412 future response as the observation window.

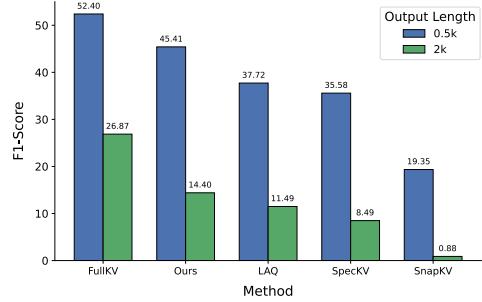
413 **MT-Bench evaluation.** To test our method under multi-turn conversation setting, we evaluated  
414 LookaheadKV and baselines on MT-Bench (Zheng et al., 2023), a benchmark covering diverse  
415 domains, e.g., writing, coding, and math. The generated responses are evaluated using Qwen3-  
416 235B-A22B as the LLM judge. The results in Table 2 indicate that LookaheadKV is either on par  
417 or superior across all models and budgets tested. Similar to other evaluation results, we observe  
418 that our method is especially favorable at lower budget settings (e.g.,  $C = [64, 128]$ ). On the other  
419 hand, the performance gap quickly narrows at higher budgets since the context length of MT-Bench  
420 samples are relatively short compared to benchmarks targeting long-context capabilities.

## 421 5 ANALYSIS

### 422 5.1 EFFICIENCY COMPARISON

423 To assess the efficiency of our method against the baselines, we measure the Time-To-First-Token  
424 (TTFT) of LLaMA3.1-8B across multiple context lengths using their official implementations, with  
425 the exception of LAQ which we re-implement since it does not have an official implementation. Fur-  
426 thermore, since the latency of a method can vary significantly depending on the implementation, we  
427 conduct rigorous analysis and derive the theoretical latency for each method, based on the analytical  
428 model proposed in Davies et al. (2025). We discuss further details in Section B.

429 Table 3 presents the results of the TTFT analysis for 8K and 32K context lengths (see Table 15  
430 for 4K and 16K results). Overall, we observe that draft-based methods incur significant overhead,



425 Figure 5: HTML-to-TSV evaluation results us-  
426 ing LLaMA3.1-8B.

432 Table 4: Average LongBench performance at different temperature settings on LLaMA3.1-8B, with  
 433  $C = 128$ . LookaheadKV outperforms baselines across all tested temperature settings.

| Method    | FullKV         | SnapKV         | SpecKV         | LAQ            | LookaheadKV           |
|-----------|----------------|----------------|----------------|----------------|-----------------------|
| Greedy    | 49.88          | 43.50          | 45.45          | 46.61          | <b>47.72</b>          |
| $T = 0.2$ | 49.58 (-0.60%) | 43.29 (-0.48%) | 44.99 (-1.01%) | 46.73 (+0.26%) | <b>47.75</b> (+0.06%) |
| $T = 0.8$ | 47.82 (-4.13%) | 41.39 (-4.85%) | 43.43 (-4.44%) | 45.27 (-2.87%) | <b>45.81</b> (-4.00%) |

439  
 440 Table 5: 2D ablation across lookahead sizes and trainable modules, on LLaMA3.2-1B. Average  
 441 LongBench scores with cache budget of 64 and TTFT overhead are reported.

| Module   | $n_{\text{lookahead}} = 4$ |             | $n_{\text{lookahead}} = 8$ |             | $n_{\text{lookahead}} = 16$ |             | $n_{\text{lookahead}} = 32$ |             | $n_{\text{lookahead}} = 64$ |             | $n_{\text{lookahead}} = 128$ |             |
|----------|----------------------------|-------------|----------------------------|-------------|-----------------------------|-------------|-----------------------------|-------------|-----------------------------|-------------|------------------------------|-------------|
|          | score                      | overhead(%) | score                      | overhead(%) | score                       | overhead(%) | score                       | overhead(%) | score                       | overhead(%) | score                        | overhead(%) |
| emb-only | 25.5                       | 3.4         | 25.7                       | 3.8         | 26.4                        | 3.4         | 26.4                        | 4.2         | <b>25.8</b>                 | <b>7.3</b>  | <b>26.2</b>                  | <b>10.7</b> |
| QV       | 26.5                       | 3.7         | 26.4                       | 4.1         | 26.9                        | 4.0         | 26.9                        | 4.4         | <b>26.7</b>                 | <b>7.7</b>  | <b>27.1</b>                  | <b>10.7</b> |
| all      | 26.6                       | 4.2         | 27.0                       | 4.2         | 27.0                        | 4.7         | 27.1                        | 5.0         | <b>27.1</b>                 | <b>8.5</b>  | <b>27.0</b>                  | <b>11.0</b> |

442 either due to increased computation (SpecKV) or memory traffic (LAQ). On the contrary, Looka-  
 443 headKV requires marginal additional cost across all tested context lengths, achieving 14.5 times  
 444 faster eviction overhead compared to LAQ at 32K sequence length.

## 445 5.2 EFFECT OF STOCHASTIC DECODING

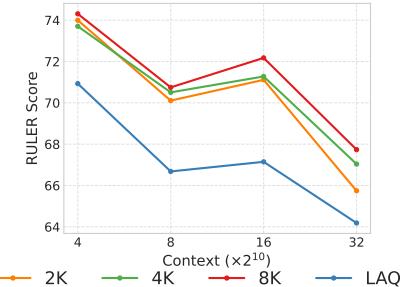
446 To analyze the effect of stochastic generation on LookaheadKV’s performance, we evaluate our  
 447 method using two temperature settings: [0.2, 0.8]. Results in Table 4 show that LookaheadKV  
 448 maintains superior performance over all other baselines across all temperature settings. Further, we  
 449 observe that performance degradation at high temeprature setting (3-4% at  $T = 0.8$ ) is consistent  
 450 across all methods, including FullKV, indicating that stochasticity in inference affects all approaches  
 451 similarly. We further discuss the interplay between stochastic decoding for training data generation  
 452 and LookaheadKV performance in Section E.3

## 461 5.3 ABLATION ON TRAINABLE MODULES

462 We study the impact of lookahead size  $n_{\text{lookahead}}$  and LoRA placement through a 2D ablation across  
 463 six lookahead sizes (4, 8, 16, 32, **64**, **128**) and three configurations: emb-only (No LoRA ap-  
 464 plied), QV (LoRA applied to Q and V), and all (LoRA applied to all linear layers). The results  
 465 indicate that both larger lookahead windows and broader LoRA coverage generally improve aver-  
 466 age LongBench performance. However, performance gains saturate at  $n_{\text{lookahead}} = 32$ ; increasing  
 467 the lookahead size beyond this point yields diminishing returns while incurring a noticeable increase  
 468 in inference overhead. On the other hand, applying Lookahead LoRA to all layers results in rela-  
 469 tively minor rise in TTFT while significantly improving the performance across all lookahead sizes.  
 470 Based on this analysis, we set  $n_{\text{lookahead}} = 32$  and apply LoRA to all linear modules in our main  
 471 experiments.

## 473 5.4 ROBUSTNESS TO TRAINING CONTEXT LENGTH

474 Transformer-based language models trained with  
 475 fixed context lengths often struggle to generalize be-  
 476 yond their training window. Similarly, one may raise  
 477 concern about the context length generalization of our  
 478 method. To examine this effect, we apply Looka-  
 479 headKV training to LLaMA-3B with limited training  
 480 context lengths of 2K, 4K, and 8K, and evaluate on  
 481 RULER (Figure 6). We observe that while longer  
 482 training context lengths yield better performance as  
 483 expected, training on shorter contexts still remains ef-  
 484 fective with relatively minor degradation in perfor-  
 485 mance, demonstrating that our method generalizes ro-  
 486 bustly to unseen sequence lengths.



487 Figure 6: RULER evaluation on Looka-  
 488 headKV trained with shorter contexts.

486 6 RELATED WORK  
487  
488489 **KV Cache Eviction.** Early analyses revealed that attention scores tend to be sparse (Zhang et al.,  
490 2023), implying that only a small subset of KV entries substantially contributes to the attention  
491 output. Subsequent work showed that the importance of these tokens remains stable throughout  
492 generation, i.e., tokens deemed important early on tend to stay important (Liu et al., 2023). These ob-  
493 servations motivated a range of eviction methods aimed at discarding unimportant KV entries while  
494 preserving model performance. A representative method is H2O (Heavy-Hitter Oracle) (Zhang et al.,  
495 2023), which proposes an eviction policy that considers the historical importance of tokens based on  
496 attention weights. NACL (Chen et al., 2024) performs eviction in a chunk-wise fashion, computing  
497 token importance locally within each chunk.  
498499 **Prefill KV Cache Eviction.** Another line of work, which we discuss extensively in our paper,  
500 focuses on eviction of prefill KV-cache. SnapKV (Li et al., 2024) introduced the notion of an “ob-  
501 servation window” consisting of the suffix of the input prompt, which is used to predict important  
502 tokens to keep for subsequent response generation. Further, SpecKV (Galim et al., 2025) proposed  
503 to generate an approximate response with a smaller model and use the resulting tokens as a more re-  
504 liable observation window for future importance prediction. Similarly, Lookahead Q-Cache (Wang  
505 et al., 2025) first applies a cheap eviction method, such as SnapKV, to obtain a partial low-cost  
506 draft response, then re-evicts KV entries based on the importance scores derived from the draft.  
507 KV-zip (Kim et al., 2025) adopts a query-agnostic strategy by inserting a repeated prompt and mea-  
508 suring which KV entries are essential for accurately reconstructing the input. Orthogonal to these  
509 approaches, several works proposed to allocate non-uniform budgets for each layer (Cai et al., 2024)  
510 and head (Feng et al., 2024) to further improve performance.  
511512 **Prompt Tuning for Task Adaptation.** Another line of work closely related to ours is parameter-  
513 efficient finetuning through learned prompts. Prompt Tuning (Lester et al., 2021) inserts a sequence  
514 of continuous, learnable embeddings into the frozen LLM for downstream task adaptation, while  
515 Prefix-Tuning (Li & Liang, 2021) extends this idea by pre-pending learned vectors across multiple  
516 layers. Further, P-Tuning v2 (Liu et al., 2022) demonstrated that prompt-based adaptation scales  
517 well across a wide range of model sizes. Unlike conventional prompt-tuning methods that aim to  
518 improve task performance, our work leverages learned prompts to predict internal model statistics,  
519 thereby enhancing computational efficiency rather than accuracy.  
520521 Training objectives similar to ours have been used in distillation (Wang et al., 2020), or in rank-  
522 ing/retrieval (Cao et al., 2007; Izacard & Grave, 2021). Some contemporaneous works (Greenewald  
523 et al., 2025; Peng et al., 2025; Samragh et al., 2025) also propose LoRA modules that selectively  
524 activate only for some tokens.  
525526 7 CONCLUSION AND LIMITATION  
527  
528529 We introduce LookaheadKV, a trainable prefill-time KV cache eviction framework that accurately  
530 predicts token importance without relying on draft generation. The method augments a frozen LLM  
531 with a small set of learnable lookahead tokens and Lookahead LoRA modules that activate only  
532 on these tokens. Trained to match ground-truth importance distributions across layers and heads,  
533 LookaheadKV achieves performance superior to costly draft generation-based approaches while  
534 adding negligible inference overhead. Empirically, across LLaMA and Qwen model families and  
535 multiple long-context benchmarks, our approach consistently outperforms training-free heuristics  
536 and draft-based baselines, especially in low-budget regimes and long-from output tasks, while in-  
537 troducing less than 0.5% additional parameters and incurring only a marginal increase in prefill  
538 latency.  
539540 Due to limited compute resources, we were unable to conduct experiments on larger-sized models.  
541 However, experimental results indicate that LookaheadKV improves both performance and latency  
542 of KV cache eviction across a variety of model sizes. Further LookaheadKV currently focuses on the  
543 prefill KV cache eviction; extending LookaheadKV to also perform decoding-stage eviction remains  
544 an interesting future work.  
545

540 8 REPRODUCIBILITY STATEMENT  
541542 Our source code is released in supplementary to reproduce our results, and pseudo-code is also  
543 provided in Section A. Section G provides links to datasets and evaluation benchmarks used, and  
544 Section 4.1 describes the pre-processing steps on the data.  
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756 A PSEUDO-CODE  
757758  
759 The pseudocode for LookaheadKV training and eviction is described in Algorithm 1 and Algo-  
760 rithm 2, respectively.

761

762 **Algorithm 1** LookaheadKV Training  
763764 **Require:** dataset  $\mathcal{D}$  of input-response pairs

```

765   1: scores  $\leftarrow \emptyset$                                  $\triangleright$  GT importance scores
766   2: estimates  $\leftarrow \emptyset$                              $\triangleright$  score estimates using LookaheadKV
767   3: for each training sample  $(X, Y)$  in dataset  $\mathcal{D}$  do
768     4:   for each layer  $l$  do                                 $\triangleright$  GT pass
769       5:     for each head  $h$  in layer  $l$  do
770         6:            $S \leftarrow$  GT importance score for head  $(l, h)$ 
771         7:           scores.append( $S$ )
772       8:     end for
773   9:   end for
774 10:   for each layer  $l$  do                                 $\triangleright$  lookahead pass
775     11:     for each head  $h$  in layer  $l$  do
776       12:        $\hat{S} \leftarrow$  importance scores using lookahead embeddings for head  $(l, h)$ 
777       13:       estimates.append( $\hat{S}$ )
778     14:     end for
779   15:   end for
780   16:    $L \leftarrow 0$                                           $\triangleright$  compute loss
781   17:   for all  $(S, \hat{S})$  in scores, estimates do
782     18:      $L \leftarrow L + \text{KL}(\text{Norm}(S) \parallel \text{Norm}(\hat{S}))$ 
783   19:   end for
784   20:    $L \leftarrow \frac{L}{|\text{scores}|}$ 
785   21:   L.backward()
786 22: end for

```

787

788

789 **Algorithm 2** LookaheadKV Eviction  
790791 **Require:** Input prompt  $X = \{x_1, \dots, x_{n_{\text{in}}}\}$ 792 **Require:** cache budget  $k$ 

```

793   1: Append learned lookahead tokens to input and compute the sequence embeddings  $\hat{\mathbf{X}} = [\mathbf{X} \mathbf{L}]^\top$ 
794   2:  $\triangleright$  shape:  $(n_{\text{in}} + n_{\text{lookahead}}) \times d$ 
795   3: Perform a prefill forward pass with  $\hat{\mathbf{X}}$ :
796   4: for each layer  $l$  do
797     5:   for each head  $h$  do                                 $\triangleright$  shape:  $(n_{\text{in}} + n_{\text{lookahead}}) \times (n_{\text{in}} + n_{\text{lookahead}})$ 
798       6:      $\mathbf{A} \leftarrow \text{Softmax}\left(\frac{QK^\top}{\sqrt{d}}\right)$ 
799       7:      $\hat{\mathbf{A}} \leftarrow \mathbf{A}[n_{\text{in}} :, : n_{\text{in}}]$            $\triangleright$  attention between lookahead tokens and input prompt
800       8:      $\mathbf{s} \leftarrow \text{MeanReduce}(\hat{\mathbf{A}})$            $\triangleright$  score vector, shape:  $1 \times n_{\text{in}}$ 
801       9:      $\mathcal{I} \leftarrow \text{TopK}(\mathbf{s}, k)$            $\triangleright$  select Top- $k$  indices
802      10:     $K^{\text{kept}} \leftarrow K[\mathcal{I}]$ 
803      11:     $V^{\text{kept}} \leftarrow V[\mathcal{I}]$ 
804      12:    Cache  $(K^{\text{kept}}, V^{\text{kept}})$            $\triangleright$  evict unimportant KV pairs and cache retained pairs
805      13:    Compute attention output for MLP layer
806      14:  Compute MLP output for next layer
807 15: end for
808 16: return

```

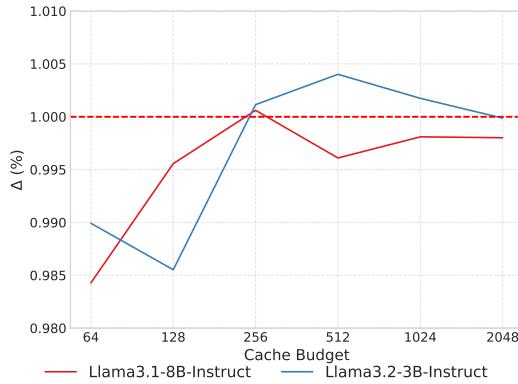
809

810 B THEORETICAL ESTIMATION DETAILS  
811812 This section details our methodology for theoretically estimation the Time-to-First-Token (TTFT)  
813 latency for various KV cache eviction algorithms. Our analysis is based on the analytical model for  
814 FLOPs and memory traffic proposed by Davies et al. (2025). To align configurations of theoretical  
815 estimates with them of actual measurements, we simulate the execution of LLaMA3.1-8B on a  
816 single NVIDIA H100 80GB GPU with a batch size of 1, assuming all weights and activations are  
817 in half-precision. We set KV cache budget size of 128, lookahead size as 32, and window size as  
818 32. We only consider tensor operations which are dominant parts of the computations. To provide  
819 estimates that closely reflect real-world performance, our calculations incorporate practical hardware  
820 utilization by assuming a flops efficiency of 0.7 and a memory efficiency of 0.9, as described in Li  
821 (2023).  
822823 To isolate the specific overhead introduced by each eviction algorithm, we first establish a baseline  
824 by calculating the theoretical latency of a single forward pass. The TTFT overhead for each eviction  
825 method is then determined by subtracting this baseline forward pass latency from the method’s total  
826 estimated TTFT. For LAQ, the total latency is calculated by summing the costs of its three con-  
827 secutive steps—the first eviction, low-cost generation of pseudo response, and the second eviction.  
828 Similarly, the total latency of SpecKV is estimated by aggregating the latencies of its draft prefill,  
829 draft decode, and target model eviction phases. A comprehensive implementation of the code to  
830 derive theoretical estimates of all baselines is available in the Supplementary Materials.  
831832 C IMPLEMENTATION OPTIMIZATION  
833834 Efficient attention implementations such as FlashAttention (Dao et al., 2022) do not materialize the  
835 full attention score matrix, but is required in our setting to compute importance scores and enable  
836 gradient backpropagation. A possible solution is to compute the complete attention matrix using  
837 native PyTorch (i.e., eager attention), but this quickly leads to an out-of-memory error as the matrix  
838 size grows quadratically with the sequence length, which is incompatible with our training setting  
839 (upto 16K sequence length). Fortunately, for our objective, we only require the cross-attention scores  
840 between the generated response and the entire input sequence, and the response length is typically  
841 much shorter than the input prompt.  
842843 Leveraging this observation, we adopt the following approach: for the attention layers’ forward  
844 computation, we use flash attention, while for the importance score computation and loss back-  
845 propagation, we employ eager attention to only compute the partial attention score matrix with the  
846 queries of model response and keys of the entire sequence. This reduces the memory requirement of  
847 eager attention from  $\mathcal{O}((|X| + |Y|)^2)$  to  $\mathcal{O}(|X| \cdot |Y| + |Y|^2)$ , where  $|X|$  and  $|Y|$  denote the lengths  
848 of the input prompt and model response, respectively, with  $|X| \gg |Y|$ .  
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864 **D NEED FOR DATA GENERATION**  
865

866 One of the requirements of LookaheadKV training is that the target model’s generated responses  
 867 must be available as training data. However, generating these responses from the model can some-  
 868 times be costly, e.g., when applying LookaheadKV across multiple models. Hence, to assess  
 869 whether this requirement of can be relaxed, we evaluate an alternative setting where training uses  
 870 the responses from the source datasets instead of model-generated outputs.

871 We observe in Figure 7 that this substitution leads to a relatively minor drop in average LongBench  
 872 performance in lower-budget regimes. We hypothesize that if the attention distribution of the model-  
 873 generated responses and that of the source dataset responses are moderately similar, our method can  
 874 still successfully learn to accurately predict the importance scores. Overall, these results suggest  
 875 that, in scenarios where training data generation is impractical, using source responses provides a  
 876 viable and effective alternative.

891 Figure 7: Performance ratio of training using model-generated data vs. source data.  
892

918 E ADDITIONAL RESULTS  
919920 In this section, we provide additional experimental results excluded from the main text due to page  
921 limitation.  
922923 E.1 RULER EVALUATION ON LONGER CONTEXTS  
924925 To explore the capability of LookaheadKV on longer contexts, we evaluate our method on RULER at  
926 64k and 128k context lengths using LLaMA3.1-8B-Instruct with a cache budget of 128. We sample  
927 50 random examples per task from the RULER benchmark. As shown in Table 6, LookaheadKV  
928 achieves the best performance at these context lengths as well, showing that the effectiveness of our  
929 method scales to even longer context lengths.  
930931 Table 6: RULER evaluation results on longer context lengths using Llama3.1-8B-Instruct at  $C =$   
932 128.  
933

| Context Length | FullKV | LookaheadKV  | SnapKV | SpecKV | LAQ   |
|----------------|--------|--------------|--------|--------|-------|
| 64k            | 88.48  | <b>71.00</b> | 36.15  | 65.08  | 64.73 |
| 128k           | 77.98  | <b>55.83</b> | 27.64  | 53.16  | 50.91 |

937  
938  
939 E.2 EFFECT OF COMBINING SUFFIX WINDOW  
940941 To test the effect of incorporating suffix window, as proposed in SnapKV (Li et al., 2024), we  
942 augment LookaheadKV by also including queries of the last 32 prompt tokens for importance score  
943 estimation. As shown in Table 7, we observe a slight drop in performance when SnapKV importance  
944 scores are included. The degraded performance when averaging LookaheadKV importance scores  
945 with SnapKV scores, compared to using LookaheadKV scores alone, indicates that the importance  
946 predicted by our method is superior to SnapKV.  
947948 Table 7: Average LongBench scores using LookaheadKV window only and LookaheadKV +  
949 SnapKV-style suffix window, evaluated using LLaMA3.2-1B-Instruct with  $C = 64$ .  
950

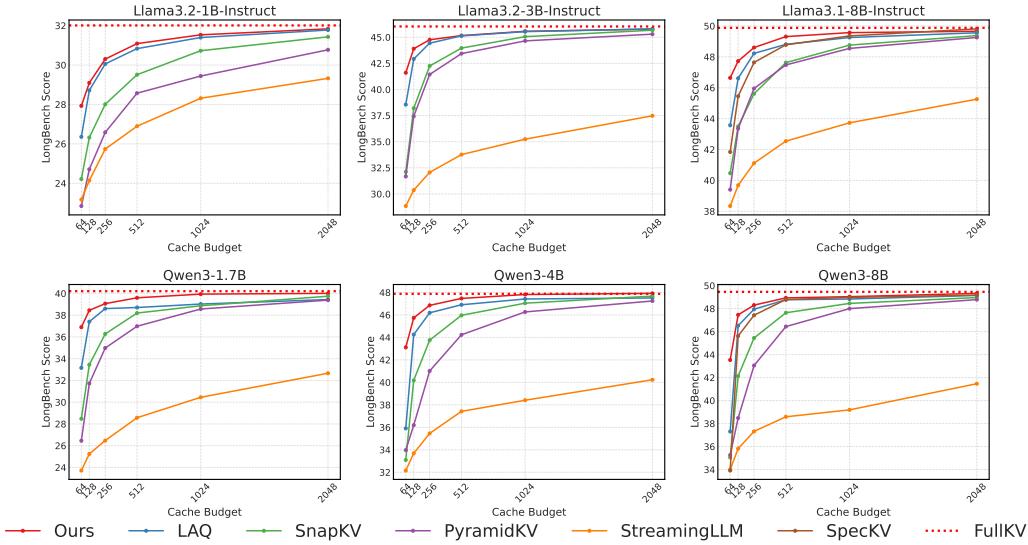
| FullKV | LookaheadKV  | LookaheadKV<br>+ Suffix Window |
|--------|--------------|--------------------------------|
| 32.01  | <b>29.10</b> | 28.52 (-1.99%)                 |

955  
956 E.3 DISCUSSION OF GENERATION STOCHASTICITY IN LOOKAHEADKV TRAINING  
957958 For LookaheadKV training, various stochastic decoding methods may be employed to generate  
959 training data. One may hypothesize that the attention matrices induced by responses generated with  
960 higher stochasticity may diverge significantly from those induced by greedy responses, potentially  
961 limiting the generalizability of LookaheadKV modules trained exclusively on greedy responses to  
962 stochastic inference scenarios. To investigate this, we quantify the similarity between importance  
963 score vectors induced by greedy responses and those generated under varying temperature settings.  
964965 Table 8 presents recall@512 and Kendall rank correlation coefficients comparing importance scores  
966 induced by greedy decoding against stochastic decoding at multiple temperatures using LLaMA3.1-  
967 8B. The scores are averaged over 30 randomly selected samples from our training data, across all  
968 layers and heads. Even at relatively high temperature ( $T = 0.8$ ), we observe strong persistence of  
969 attention patterns. Notably, the deviation is smaller than that induced by responses of a specula-  
970 tive model (Llama3.2-1B, equivalent to the SpecKV setting). This indicates that the ground-truth  
971 importance scores induced by stochastically generated responses are highly similar to the scores  
972 induced by greedy responses, which in turn indicates that greedy-generated training data provides  
973 sufficiently robust learning signals for stochastic settings.  
974

972  
 973 Table 8: Importance score similarity with stochastic response using various temperatures vs. greedy  
 974 response on LLaMA3.1-8B. LLaMA3.2-1B presents the similarity of importance scores using  
 975 greedy response generated with LLaMA3.2-1B vs. LLaMA3.1-8B.  
 976

| Generation Method | $T = 0.2$ | $T = 0.4$ | $T = 0.6$ | $T = 0.8$ | LLaMA3.2-1B |
|-------------------|-----------|-----------|-----------|-----------|-------------|
| Recall@512 (%)    | 95.06     | 93.73     | 91.40     | 91.37     | 88.66       |
| Kendall's Tau     | 91.44     | 88.63     | 84.61     | 84.79     | 80.05       |

979  
 980 E.4 RESULTS ON LONGBENCH  
 981



1000 Figure 8: Full Longbench results across multiple cache budgets. 1B-scale results are included.  
 1001

Table 9: LongBench evaluation results for Llama3.2-1B

| 1026         | 1027  | 1028  | 1029  | 1030  | 1031  | 1032  | 1033  | 1034  | 1035  | 1036  | 1037  | 1038  | 1039 | 1040  | 1041  | 1042  | 1043  | 1044                        | 1045  | 1046  | LLMs  | Single-Document QA |       |          | Multi-Document QA |         |           | Summarization |           |       | Few-shot Learning |        |        | Synthetic |       | Code |      |  |  |
|--------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|------|-------|-------|-------|-------|-----------------------------|-------|-------|-------|--------------------|-------|----------|-------------------|---------|-----------|---------------|-----------|-------|-------------------|--------|--------|-----------|-------|------|------|--|--|
|              |       |       |       |       |       |       |       |       |       |       |       |       |      |       |       |       |       |                             |       |       | NrtQA | Qasper             | MF-en | HotpotQA | 2WikiMQA          | Musique | GovReport | QMSum         | MultiNews | TREC  | TriviaQA          | SAMSum | PCount | Pre       | Lcc   | RB-P | Avg. |  |  |
| FullKV       | 19.24 | 15.96 | 42.47 | 35.53 | 29.42 | 19.87 | 28.34 | 22.18 | 25.64 | 64.00 | 80.85 | 38.83 | 3.00 | 4.78  | 38.63 | 43.35 | 32.01 | <i>KV Cache Size = 64</i>   |       |       |       |                    |       |          |                   |         |           |               |           |       |                   |        |        |           |       |      |      |  |  |
| StreamingLLM | 14.42 | 12.30 | 24.02 | 24.04 | 24.05 | 9.35  | 13.56 | 19.23 | 13.61 | 35.50 | 68.94 | 29.09 | 4.00 | 3.71  | 37.61 | 37.33 | 23.17 | <i>KV Cache Size = 128</i>  |       |       |       |                    |       |          |                   |         |           |               |           |       |                   |        |        |           |       |      |      |  |  |
| SnapKV       | 14.24 | 12.18 | 30.53 | 27.30 | 25.66 | 12.44 | 14.27 | 19.27 | 12.37 | 35.00 | 73.57 | 29.29 | 2.00 | 4.49  | 38.01 | 36.84 | 24.22 | PyramidKV                   | 13.33 | 11.36 | 26.05 | 25.34              | 24.01 | 10.57    | 13.64             | 19.49   | 11.96     | 35.00         | 69.95     | 27.75 | 1.50              | 4.33   | 35.25  | 36.01     | 22.85 |      |      |  |  |
| PyramidKV    | 17.21 | 12.76 | 37.30 | 30.27 | 27.36 | 14.22 | 16.42 | 20.09 | 14.28 | 39.50 | 76.02 | 31.19 | 3.00 | 4.58  | 39.15 | 38.37 | 26.36 | LAQ                         | 17.69 | 13.30 | 40.80 | 33.66              | 29.80 | 16.95    | 18.76             | 20.65   | 18.97     | 45.50         | 80.12     | 34.77 | 2.50              | 3.22   | 33.69  | 36.47     | 27.93 |      |      |  |  |
| LookaheadKV  | 17.38 | 14.92 | 41.39 | 35.46 | 29.22 | 17.47 | 20.13 | 20.78 | 21.24 | 51.50 | 80.27 | 36.19 | 3.00 | 4.17  | 34.75 | 37.68 | 29.10 | <i>KV Cache Size = 256</i>  |       |       |       |                    |       |          |                   |         |           |               |           |       |                   |        |        |           |       |      |      |  |  |
| StreamingLLM | 14.84 | 12.36 | 24.67 | 25.48 | 23.86 | 8.73  | 14.71 | 19.58 | 15.50 | 38.00 | 71.61 | 31.82 | 3.50 | 3.79  | 38.81 | 39.03 | 24.14 | SnapKV                      | 15.74 | 12.59 | 35.87 | 29.77              | 26.43 | 14.17    | 16.17             | 20.35   | 16.47     | 36.50         | 78.04     | 31.84 | 3.50              | 4.57   | 39.03  | 40.15     | 26.32 |      |      |  |  |
| PyramidKV    | 14.84 | 12.10 | 33.63 | 27.73 | 23.95 | 11.77 | 15.27 | 19.79 | 13.99 | 35.50 | 74.17 | 30.50 | 1.50 | 4.71  | 37.90 | 37.99 | 24.71 | LAQ                         | 18.63 | 13.65 | 41.78 | 34.75              | 29.59 | 16.57    | 18.89             | 20.88   | 19.19     | 44.00         | 79.29     | 34.89 | 2.54              | 4.25   | 39.43  | 41.06     | 28.71 |      |      |  |  |
| LookaheadKV  | 17.38 | 14.70 | 40.25 | 36.52 | 30.45 | 18.50 | 21.75 | 20.91 | 22.46 | 57.50 | 80.09 | 38.05 | 4.00 | 4.50  | 36.19 | 40.73 | 30.30 | <i>KV Cache Size = 512</i>  |       |       |       |                    |       |          |                   |         |           |               |           |       |                   |        |        |           |       |      |      |  |  |
| StreamingLLM | 14.74 | 12.39 | 25.28 | 26.71 | 23.87 | 8.88  | 16.99 | 19.67 | 17.97 | 44.50 | 74.85 | 35.96 | 3.50 | 3.90  | 40.37 | 42.19 | 25.74 | SnapKV                      | 16.59 | 13.78 | 38.80 | 32.54              | 28.11 | 16.55    | 18.55             | 20.00   | 19.69     | 41.50         | 73.91     | 33.70 | 4.00              | 4.58   | 39.15  | 41.26     | 28.01 |      |      |  |  |
| PyramidKV    | 15.11 | 13.08 | 37.31 | 32.03 | 25.36 | 12.60 | 16.91 | 20.10 | 17.78 | 40.50 | 76.61 | 32.34 | 3.50 | 4.65  | 37.13 | 40.32 | 26.58 | LAQ                         | 18.31 | 14.64 | 41.83 | 35.34              | 29.61 | 17.27    | 20.68             | 21.21   | 21.37     | 52.00         | 79.62     | 36.99 | 4.04              | 4.17   | 40.44  | 43.37     | 30.06 |      |      |  |  |
| LookaheadKV  | 18.23 | 14.70 | 40.25 | 36.52 | 30.45 | 18.50 | 21.75 | 20.91 | 22.46 | 57.50 | 80.09 | 38.05 | 4.00 | 4.50  | 36.19 | 40.73 | 30.30 | <i>KV Cache Size = 1024</i> |       |       |       |                    |       |          |                   |         |           |               |           |       |                   |        |        |           |       |      |      |  |  |
| StreamingLLM | 14.62 | 12.86 | 26.37 | 27.03 | 24.19 | 9.96  | 19.02 | 19.61 | 20.99 | 52.50 | 76.92 | 36.50 | 2.54 | 3.64  | 40.76 | 42.83 | 26.90 | SnapKV                      | 17.58 | 14.17 | 40.91 | 34.57              | 29.19 | 16.74    | 20.32             | 20.78   | 22.10     | 52.50         | 80.29     | 34.65 | 3.00              | 4.58   | 38.20  | 42.59     | 29.51 |      |      |  |  |
| PyramidKV    | 16.55 | 13.48 | 39.67 | 32.62 | 28.38 | 15.59 | 18.50 | 20.87 | 20.54 | 48.50 | 79.30 | 34.43 | 4.00 | 4.50  | 38.79 | 41.42 | 28.57 | LAQ                         | 18.45 | 15.26 | 41.93 | 34.75              | 30.44 | 17.63    | 22.39             | 21.45   | 23.11     | 57.50         | 79.04     | 37.81 | 4.00              | 4.17   | 40.76  | 44.64     | 30.83 |      |      |  |  |
| LookaheadKV  | 18.32 | 14.87 | 41.62 | 36.05 | 30.10 | 18.77 | 23.06 | 21.49 | 23.57 | 63.50 | 80.40 | 38.73 | 3.00 | 4.75  | 37.12 | 42.04 | 31.09 | <i>KV Cache Size = 2048</i> |       |       |       |                    |       |          |                   |         |           |               |           |       |                   |        |        |           |       |      |      |  |  |
| StreamingLLM | 17.10 | 14.71 | 31.30 | 31.33 | 26.60 | 11.20 | 22.94 | 20.21 | 24.89 | 59.00 | 79.81 | 38.02 | 4.04 | 4.00  | 39.49 | 44.55 | 29.32 | SnapKV                      | 17.73 | 15.74 | 42.03 | 36.12              | 29.48 | 19.34    | 24.30             | 21.75   | 25.22     | 62.50         | 80.90     | 38.22 | 3.00              | 4.75   | 38.28  | 43.52     | 31.43 |      |      |  |  |
| PyramidKV    | 18.83 | 14.50 | 41.40 | 35.75 | 28.89 | 17.40 | 22.05 | 21.14 | 24.97 | 60.50 | 80.62 | 37.33 | 2.50 | 4.50  | 38.51 | 43.46 | 30.77 | LAQ                         | 19.03 | 15.61 | 40.93 | 34.10              | 30.23 | 18.99    | 25.75             | 21.55   | 25.49     | 64.50         | 79.73     | 38.66 | 3.50              | 4.33   | 40.35  | 45.65     | 31.78 |      |      |  |  |
| LookaheadKV  | 18.18 | 16.08 | 42.13 | 35.45 | 30.13 | 19.89 | 26.34 | 21.23 | 25.63 | 64.00 | 80.90 | 39.52 | 3.00 | 4.70  | 38.06 | 44.13 | 31.84 | <i>KV Cache Size = 512</i>  |       |       |       |                    |       |          |                   |         |           |               |           |       |                   |        |        |           |       |      |      |  |  |
| StreamingLLM | 13.41 | 17.66 | 22.58 | 23.72 | 23.88 | 7.65  | 16.15 | 19.24 | 17.97 | 47.50 | 76.22 | 40.17 | 0.00 | 13.50 | 46.27 | 37.64 | 26.47 | SnapKV                      | 15.94 | 18.73 | 38.02 | 33.35              | 28.02 | 11.74    | 15.40             | 20.80   | 15.71     | 47.00         | 81.65     | 38.77 | 0.00              | 86.00  | 45.47  | 38.55     | 33.45 |      |      |  |  |
| PyramidKV    | 17.07 | 19.74 | 38.19 | 33.18 | 29.09 | 13.95 | 17.92 | 21.26 | 17.67 | 56.00 | 81.47 | 39.26 | 0.00 | 91.50 | 45.19 | 38.23 | 34.98 | LAQ                         | 18.38 | 21.08 | 45.04 | 38.04              | 33.52 | 15.36    | 20.17             | 22.70   | 18.78     | 62.50         | 85.21     | 41.79 | 0.14              | 92.00  | 42.94  | 40.84     | 37.41 |      |      |  |  |
| LookaheadKV  | 19.46 | 23.27 | 44.59 | 37.81 | 33.82 | 17.97 | 23.71 | 23.12 | 21.70 | 65.50 | 85.56 | 42.38 | 0.12 | 92.75 | 44.80 | 38.61 | 38.45 | <i>KV Cache Size = 256</i>  |       |       |       |                    |       |          |                   |         |           |               |           |       |                   |        |        |           |       |      |      |  |  |
| StreamingLLM | 13.41 | 17.66 | 22.58 | 23.72 | 23.88 | 7.65  | 16.15 | 19.24 | 17.97 | 47.50 | 76.22 | 40.17 | 0.00 | 13.50 | 46.27 | 37.64 | 26.47 | SnapKV                      | 15.94 | 18.73 | 38.02 | 33.35              | 28.02 | 11.74    | 15.40             | 20.80   | 15.71     | 47.00         | 81.65     | 38.77 | 0.00              | 91.50  | 45.19  | 38.23     | 34.98 |      |      |  |  |
| PyramidKV    | 17.07 | 19.74 | 38.19 | 33.18 | 29.09 | 13.95 | 17.92 | 21.26 | 17.67 | 56.00 | 81.47 | 39.26 | 0.00 | 91.50 | 45.19 | 38.23 | 34.98 | LAQ                         | 18.38 | 21.08 | 45.04 | 38.04              | 33.52 | 15.36    | 20.17             | 22.70   | 18.78     | 62.50         | 85.21     | 41.79 | 0.14              | 92.00  | 42.94  | 40.84     | 37.41 |      |      |  |  |
| LookaheadKV  | 19.60 | 24.30 | 45.69 | 38.81 | 34.02 | 17.91 | 25.51 | 23.11 | 23.15 | 70.00 | 85.37 | 42.16 | 0.12 | 91.00 | 45.29 | 38.98 | 39.06 | <i>KV Cache Size = 512</i>  |       |       |       |                    |       |          |                   |         |           |               |           |       |                   |        |        |           |       |      |      |  |  |
| StreamingLLM | 13.92 | 18.40 | 25.10 | 24.91 | 24.77 | 7.67  | 20.38 | 19.63 | 20.78 | 61.00 | 81.80 | 40.38 | 0.00 | 12.50 | 47.28 | 38.62 | 28.57 | SnapKV                      | 19.32 | 22.22 | 44.07 | 36.25              | 30.04 | 15.66    | 22.20             | 22.15   | 21.73     | 70.50         | 84.81     | 40.54 | 0.14              | 94.50  | 46.75  | 40.26     | 38.20 |      |      |  |  |
| PyramidKV    | 17.95 | 20.69 | 41.43 | 36.22 | 29.68 | 14.96 | 20.39 | 21.52 | 20.01 | 66.00 | 84.65 | 40.16 | 0.14 | 93.50 | 45.61 | 38.83 | 36.98 | LAQ                         | 16.99 | 22.67 | 46.97 | 38.10              | 33.62 | 16.38    | 24.58             | 23.39   | 22.99     | 71.50         | 84.71     | 42.25 | 0.00              | 94.00  | 40.85  | 40.30     | 38.71 |      |      |  |  |
| LookaheadKV  | 19.04 | 24.66 | 44.68 | 39.04 | 33.66 | 17.64 | 27.46 | 23.31 | 24.17 | 73.00 | 85.37 | 42.87 | 0.17 | 94.00 | 45.27 | 39.25 | 39.60 | <i>KV Cache Size = 1024</i> |       |       |       |                    |       |          |                   |         |           |               |           |       |                   |        |        |           |       |      |      |  |  |
| StreamingLLM | 15.32 | 18.63 | 26.90 | 27.88 | 26.44 | 8.47  | 23.56 | 20.34 | 23.82 | 65.50 | 84.00 | 41.69 | 0.00 | 18.00 | 46.93 | 39.71 | 30.45 | SnapKV                      | 18.68 | 24.05 | 44.25 | 38.57              | 30.72 | 16.63    | 24.97             | 22.28   | 23.62     | 71.50         | 85.26     | 40.43 | 0.50              | 95.00  | 46.39  | 39.03     | 38.87 |      |      |  |  |
| PyramidKV    | 18.   |       |       |       |       |       |       |       |       |       |       |       |      |       |       |       |       |                             |       |       |       |                    |       |          |                   |         |           |               |           |       |                   |        |        |           |       |      |      |  |  |

Table 11: LongBench evaluation results for Llama3.2-3B

| 1080                        | 1081  | 1082  | 1083  | 1084  | 1085  | 1086  | 1087  | 1088  | 1089  | 1090  | 1091  | 1092  | 1093 | 1094  | 1095  | 1096  | 1097  | 1098 | 1099 | 1100 | LLMs  | Single-Document QA |       |          | Multi-Document QA |         |           | Summarization |           |      | Few-shot Learning |        |        | Synthetic |     |      | Code |  |  |
|-----------------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|------|-------|-------|-------|-------|------|------|------|-------|--------------------|-------|----------|-------------------|---------|-----------|---------------|-----------|------|-------------------|--------|--------|-----------|-----|------|------|--|--|
|                             |       |       |       |       |       |       |       |       |       |       |       |       |      |       |       |       |       |      |      |      | NrtQA | Qasper             | MF-en | HotpotQA | 2WikiMQA          | Musique | GovReport | QMSum         | MultiNews | TREC | TriviaQA          | SAMSum | PCount | Pre       | Lcc | RB-P | Avg. |  |  |
| FullKV                      | 27.45 | 43.30 | 54.45 | 55.63 | 43.43 | 31.61 | 32.24 | 24.61 | 25.00 | 73.00 | 88.76 | 43.65 | 0.75 | 96.50 | 64.29 | 61.39 | 47.88 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| <i>KV Cache Size = 64</i>   |       |       |       |       |       |       |       |       |       |       |       |       |      |       |       |       |       |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| StreamingLLM                | 12.46 | 23.96 | 25.93 | 38.56 | 33.40 | 19.47 | 13.74 | 19.71 | 13.04 | 39.50 | 75.48 | 34.33 | 0.50 | 64.50 | 51.42 | 48.46 | 32.15 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| SnapKV                      | 15.28 | 25.03 | 31.61 | 40.00 | 34.95 | 18.83 | 12.88 | 19.78 | 12.49 | 40.50 | 75.62 | 33.69 | 1.00 | 69.00 | 51.48 | 47.38 | 33.10 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| PyramidKV                   | 15.50 | 24.84 | 34.33 | 40.70 | 35.07 | 19.39 | 13.48 | 19.85 | 13.03 | 41.50 | 76.69 | 33.95 | 1.50 | 73.00 | 52.98 | 47.77 | 33.97 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| LAQ                         | 16.55 | 30.74 | 46.21 | 40.58 | 38.10 | 18.35 | 14.96 | 20.74 | 14.48 | 43.50 | 71.25 | 34.40 | 1.50 | 81.25 | 53.45 | 48.45 | 35.91 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| <b>LookaheadKV</b>          | 20.49 | 37.99 | 51.37 | 54.71 | 42.30 | 30.90 | 22.10 | 22.98 | 18.71 | 58.50 | 88.85 | 39.71 | 1.00 | 92.00 | 55.89 | 52.33 | 43.11 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| <i>KV Cache Size = 128</i>  |       |       |       |       |       |       |       |       |       |       |       |       |      |       |       |       |       |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| StreamingLLM                | 15.69 | 23.56 | 26.02 | 38.03 | 32.38 | 18.86 | 14.79 | 19.67 | 15.20 | 45.50 | 78.32 | 37.32 | 0.50 | 65.50 | 55.83 | 51.76 | 33.68 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| SnapKV                      | 19.56 | 29.48 | 43.55 | 49.81 | 37.95 | 25.99 | 16.27 | 21.17 | 16.16 | 49.50 | 86.31 | 38.10 | 1.50 | 95.00 | 58.75 | 53.78 | 40.18 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| PyramidKV                   | 15.88 | 27.32 | 38.51 | 40.25 | 33.56 | 20.45 | 14.72 | 20.88 | 14.65 | 45.00 | 76.75 | 35.06 | 1.50 | 89.50 | 55.58 | 49.49 | 36.19 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| LAQ                         | 21.44 | 37.82 | 53.26 | 54.98 | 42.75 | 32.08 | 20.44 | 23.69 | 18.86 | 60.50 | 87.55 | 40.48 | 2.50 | 93.00 | 60.85 | 57.87 | 44.25 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| <b>LookaheadKV</b>          | 25.17 | 40.13 | 52.28 | 55.10 | 43.47 | 31.38 | 24.83 | 24.46 | 21.57 | 67.00 | 88.85 | 41.37 | 1.00 | 96.50 | 61.00 | 57.77 | 45.74 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| <i>KV Cache Size = 256</i>  |       |       |       |       |       |       |       |       |       |       |       |       |      |       |       |       |       |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| StreamingLLM                | 15.66 | 25.74 | 28.99 | 37.34 | 32.47 | 19.02 | 17.65 | 20.12 | 18.02 | 49.50 | 81.97 | 38.87 | 1.00 | 66.50 | 59.45 | 55.05 | 35.46 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| SnapKV                      | 24.64 | 35.80 | 47.67 | 54.45 | 40.78 | 29.60 | 19.84 | 22.75 | 19.68 | 60.00 | 87.64 | 39.46 | 1.00 | 96.00 | 62.57 | 58.24 | 43.76 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| PyramidKV                   | 18.31 | 31.30 | 44.14 | 51.08 | 36.87 | 25.14 | 18.68 | 22.04 | 17.78 | 56.50 | 85.53 | 38.77 | 1.50 | 95.50 | 59.16 | 53.92 | 41.01 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| LAQ                         | 26.88 | 40.94 | 53.82 | 55.76 | 43.22 | 31.53 | 23.34 | 24.03 | 21.57 | 68.50 | 87.72 | 41.61 | 2.00 | 93.50 | 62.60 | 62.03 | 46.19 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| <b>LookaheadKV</b>          | 26.25 | 41.08 | 53.03 | 55.21 | 43.28 | 31.99 | 27.13 | 25.09 | 23.46 | 71.50 | 88.76 | 41.89 | 1.00 | 96.50 | 63.42 | 60.09 | 46.86 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| <i>KV Cache Size = 512</i>  |       |       |       |       |       |       |       |       |       |       |       |       |      |       |       |       |       |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| StreamingLLM                | 18.02 | 27.64 | 30.11 | 39.03 | 33.32 | 20.70 | 21.47 | 20.39 | 21.96 | 60.50 | 85.45 | 40.27 | 0.50 | 59.50 | 62.54 | 57.33 | 37.42 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| SnapKV                      | 25.27 | 39.10 | 51.45 | 54.22 | 42.21 | 32.86 | 23.30 | 23.53 | 22.33 | 70.00 | 88.76 | 40.24 | 1.00 | 96.50 | 64.28 | 60.45 | 45.97 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| PyramidKV                   | 21.93 | 34.53 | 49.40 | 53.99 | 40.38 | 30.21 | 21.87 | 22.72 | 20.77 | 67.00 | 88.24 | 40.05 | 1.00 | 96.50 | 61.47 | 57.70 | 44.24 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| LAQ                         | 26.50 | 42.56 | 53.88 | 55.24 | 43.25 | 32.14 | 25.92 | 24.46 | 23.42 | 73.00 | 87.72 | 42.94 | 1.50 | 93.50 | 62.99 | 61.47 | 46.91 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| <b>LookaheadKV</b>          | 26.86 | 41.97 | 53.10 | 55.59 | 43.97 | 32.09 | 29.57 | 25.35 | 24.61 | 72.00 | 88.76 | 42.85 | 1.50 | 96.50 | 63.83 | 60.96 | 47.47 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| <i>KV Cache Size = 1024</i> |       |       |       |       |       |       |       |       |       |       |       |       |      |       |       |       |       |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| StreamingLLM                | 20.48 | 30.08 | 32.30 | 42.20 | 34.23 | 20.65 | 24.81 | 20.84 | 24.19 | 64.50 | 87.39 | 40.95 | 1.00 | 47.00 | 64.74 | 59.17 | 38.41 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| SnapKV                      | 25.91 | 41.72 | 52.26 | 56.50 | 43.15 | 32.08 | 26.69 | 24.53 | 24.02 | 71.50 | 88.76 | 41.77 | 1.00 | 96.50 | 64.46 | 61.91 | 47.05 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| PyramidKV                   | 25.81 | 39.40 | 51.89 | 53.26 | 42.26 | 32.08 | 25.11 | 23.72 | 23.61 | 70.00 | 88.76 | 41.10 | 1.00 | 96.50 | 63.93 | 61.88 | 46.27 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| LAQ                         | 27.40 | 43.93 | 54.30 | 55.95 | 43.62 | 31.66 | 28.18 | 25.16 | 24.64 | 73.00 | 87.77 | 43.33 | 1.75 | 93.50 | 62.54 | 62.00 | 47.42 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| <b>LookaheadKV</b>          | 27.47 | 42.45 | 53.70 | 55.64 | 43.85 | 32.40 | 30.68 | 24.98 | 25.21 | 73.00 | 88.76 | 42.96 | 1.00 | 96.50 | 64.61 | 61.89 | 47.82 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| <i>KV Cache Size = 2048</i> |       |       |       |       |       |       |       |       |       |       |       |       |      |       |       |       |       |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| StreamingLLM                | 20.87 | 34.01 | 36.39 | 44.11 | 37.06 | 21.93 | 28.06 | 21.64 | 25.16 | 67.50 | 88.39 | 41.55 | 0.50 | 52.00 | 63.58 | 60.98 | 40.23 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| SnapKV                      | 26.80 | 43.04 | 53.50 | 55.54 | 44.01 | 33.33 | 29.49 | 24.64 | 24.86 | 73.00 | 88.76 | 41.94 | 1.25 | 96.50 | 64.10 | 62.08 | 47.68 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| PyramidKV                   | 25.74 | 42.42 | 53.91 | 55.34 | 43.12 | 33.06 | 27.70 | 24.21 | 24.74 | 72.00 | 88.76 | 41.54 | 1.25 | 96.50 | 63.81 | 61.78 | 47.24 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| LAQ                         | 27.21 | 43.52 | 53.62 | 55.67 | 43.89 | 31.73 | 30.42 | 24.93 | 25.04 | 73.00 | 87.72 | 43.77 | 1.50 | 93.25 | 63.02 | 61.92 | 47.51 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| <b>LookaheadKV</b>          | 27.48 | 42.86 | 53.71 | 55.31 | 43.82 | 32.42 | 31.79 | 24.75 | 25.33 | 73.00 | 88.76 | 43.34 | 1.25 | 96.50 | 64.18 | 62.23 | 47.92 |      |      |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |

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Table 12: LongBench evaluation results for Qwen3-4B

| 1104                      | 1105  | 1106  | 1107  | 1108  | 1109  | 1110  | 1111  | 1112  | 1113  | 1114  | 1115  | 1116  | 1117 | 1118  | 1119  | 1120  | 1121  | 1122 | LLMs  | Single-Document QA |       |          | Multi-Document QA |         |           | Summarization |           |      | Few-shot Learning |        |        | Synthetic |     |      | Code |  |  |
|---------------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|------|-------|-------|-------|-------|------|-------|--------------------|-------|----------|-------------------|---------|-----------|---------------|-----------|------|-------------------|--------|--------|-----------|-----|------|------|--|--|
|                           |       |       |       |       |       |       |       |       |       |       |       |       |      |       |       |       |       |      | NrtQA | Qasper             | MF-en | HotpotQA | 2WikiMQA          | Musique | GovReport | QMSum         | MultiNews | TREC | TriviaQA          | SAMSum | PCount | Pre       | Lcc | RB-P | Avg. |  |  |
| FullKV                    | 27.45 | 43.30 | 54.45 | 55.63 | 43.43 | 31.61 | 32.24 | 24.61 | 25.00 | 73.00 | 88.76 | 43.65 | 0.75 | 96.50 | 64.29 | 61.39 | 47.88 |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| <i>KV Cache Size = 64</i> |       |       |       |       |       |       |       |       |       |       |       |       |      |       |       |       |       |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| StreamingLLM              | 12.46 | 23.96 | 25.93 | 38.56 | 33.40 | 19.47 | 13.74 | 19.71 | 13.04 | 39.50 | 75.48 | 34.33 | 0.50 | 64.50 | 51.42 | 48.46 | 32.15 |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| SnapKV                    | 15.28 | 25.03 | 31.61 | 40.00 | 34.95 | 18.83 | 12.88 | 19.78 | 12.49 | 40.50 | 75.62 | 33.69 | 1.00 | 69.00 | 51.48 | 47.38 | 33.10 |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| PyramidKV                 | 15.50 | 24.84 | 34.33 | 40.70 | 35.07 | 19.39 | 13.48 | 19.85 | 13.03 | 41.50 | 76.69 | 33.95 | 1.50 | 73.00 | 52.98 | 47.77 | 33.97 |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| LAQ                       | 16.55 | 30.74 | 46.21 | 40.58 | 38.10 | 18.35 | 14.96 | 20.74 | 14.48 | 43.50 | 71.25 | 34.40 | 1.50 | 81.25 | 53.45 | 48.45 | 35.91 |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |
| <b>LookaheadKV</b>        | 20.49 | 37.99 | 51.37 | 54.   |       |       |       |       |       |       |       |       |      |       |       |       |       |      |       |                    |       |          |                   |         |           |               |           |      |                   |        |        |           |     |      |      |  |  |

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Table 13: LongBench evaluation results for Llama3.1-8B

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| LLMs                        | Single-Document QA |        |       |          | Multi-Document QA |         |           |       | Summarization |       |          | Few-shot Learning |        |        | Synthetic |       | Code  |  |
|-----------------------------|--------------------|--------|-------|----------|-------------------|---------|-----------|-------|---------------|-------|----------|-------------------|--------|--------|-----------|-------|-------|--|
|                             | NrtQA              | Qasper | MF-en | HotpotQA | 2WikiMqa          | Musique | GovReport | QMSum | MultiNews     | TREC  | TriviaQA | SAMSum            | PCount | Pre    | Lcc       | RB-P  | Avg.  |  |
| FullKV                      | 31.63              | 46.66  | 56.93 | 58.10    | 48.50             | 31.57   | 34.46     | 25.28 | 26.98         | 72.50 | 91.65    | 43.79             | 6.64   | 99.50  | 65.12     | 58.78 | 49.88 |  |
| <i>KV Cache Size = 64</i>   |                    |        |       |          |                   |         |           |       |               |       |          |                   |        |        |           |       |       |  |
| StreamingLLM                | 25.75              | 21.75  | 31.22 | 49.09    | 42.11             | 23.98   | 17.29     | 20.99 | 16.04         | 38.50 | 82.81    | 34.50             | 7.50   | 99.50  | 54.27     | 48.14 | 38.34 |  |
| SnapKV                      | 27.37              | 24.99  | 41.77 | 54.27    | 45.27             | 27.52   | 16.75     | 21.73 | 16.32         | 39.00 | 86.32    | 36.58             | 7.50   | 98.50  | 55.57     | 48.07 | 40.47 |  |
| PyramidKV                   | 24.25              | 22.87  | 41.03 | 53.07    | 43.55             | 26.36   | 16.46     | 21.52 | 15.61         | 38.50 | 81.95    | 36.68             | 7.50   | 99.50  | 54.40     | 47.20 | 39.40 |  |
| LAQ                         | 27.62              | 33.71  | 52.35 | 55.85    | 48.92             | 28.06   | 19.74     | 23.19 | 18.90         | 46.00 | 88.29    | 40.62             | 6.83   | 100.00 | 55.55     | 51.49 | 43.57 |  |
| SpeckV                      | 24.87              | 26.57  | 51.22 | 55.29    | 46.57             | 25.42   | 19.78     | 22.29 | 19.20         | 33.50 | 85.12    | 39.14             | 8.50   | 97.00  | 57.78     | 57.19 | 41.84 |  |
| LookaheadKV                 | 30.62              | 41.46  | 55.77 | 56.42    | 48.56             | 30.30   | 23.54     | 24.08 | 21.23         | 60.50 | 91.62    | 42.56             | 7.50   | 99.50  | 58.74     | 53.86 | 46.64 |  |
| <i>KV Cache Size = 128</i>  |                    |        |       |          |                   |         |           |       |               |       |          |                   |        |        |           |       |       |  |
| StreamingLLM                | 24.95              | 21.50  | 32.56 | 50.67    | 42.89             | 24.31   | 18.49     | 21.25 | 18.19         | 40.50 | 85.57    | 38.28             | 7.50   | 99.50  | 59.03     | 49.72 | 39.68 |  |
| SnapKV                      | 29.13              | 28.06  | 51.23 | 56.79    | 45.30             | 27.81   | 19.99     | 23.03 | 19.73         | 46.00 | 89.72    | 40.44             | 7.50   | 99.50  | 59.50     | 52.19 | 43.50 |  |
| PyramidKV                   | 27.70              | 28.86  | 52.00 | 56.76    | 46.11             | 28.13   | 19.86     | 22.81 | 20.03         | 44.50 | 88.41    | 39.73             | 7.50   | 99.50  | 59.84     | 51.96 | 43.36 |  |
| LAQ                         | 30.48              | 38.31  | 55.73 | 57.50    | 49.13             | 29.67   | 22.42     | 24.20 | 21.59         | 60.50 | 92.09    | 41.04             | 7.25   | 99.50  | 60.54     | 55.83 | 46.61 |  |
| SpeckV                      | 29.22              | 29.12  | 54.05 | 56.54    | 46.30             | 29.90   | 22.65     | 23.18 | 21.25         | 52.00 | 90.02    | 42.14             | 8.83   | 99.50  | 61.11     | 61.38 | 45.45 |  |
| LookaheadKV                 | 31.32              | 42.85  | 56.78 | 57.04    | 47.44             | 30.82   | 25.18     | 24.33 | 23.09         | 65.50 | 92.24    | 42.96             | 7.50   | 99.50  | 61.75     | 55.29 | 47.72 |  |
| <i>KV Cache Size = 256</i>  |                    |        |       |          |                   |         |           |       |               |       |          |                   |        |        |           |       |       |  |
| StreamingLLM                | 25.96              | 24.08  | 33.73 | 50.56    | 42.61             | 23.49   | 20.86     | 21.60 | 20.64         | 46.00 | 87.50    | 41.09             | 7.50   | 99.50  | 61.19     | 51.53 | 41.12 |  |
| SnapKV                      | 27.96              | 34.49  | 55.07 | 57.40    | 46.57             | 29.50   | 22.49     | 23.51 | 22.42         | 54.00 | 91.10    | 40.61             | 7.33   | 99.50  | 62.48     | 55.36 | 45.61 |  |
| PyramidKV                   | 28.09              | 36.64  | 55.86 | 57.68    | 46.28             | 29.56   | 22.23     | 23.86 | 22.53         | 56.50 | 91.56    | 41.23             | 7.33   | 99.50  | 62.47     | 53.92 | 45.95 |  |
| LAQ                         | 31.03              | 43.97  | 55.93 | 57.78    | 49.42             | 30.42   | 24.48     | 24.60 | 23.29         | 68.00 | 92.20    | 42.61             | 7.08   | 100.00 | 62.70     | 58.09 | 48.23 |  |
| SpeckV                      | 28.66              | 36.19  | 57.26 | 58.17    | 48.51             | 30.85   | 24.83     | 24.60 | 23.32         | 61.00 | 91.16    | 42.46             | 8.33   | 99.50  | 64.21     | 63.18 | 47.64 |  |
| LookaheadKV                 | 31.96              | 44.01  | 56.80 | 57.99    | 47.41             | 31.46   | 27.26     | 24.56 | 24.59         | 69.00 | 92.55    | 42.93             | 7.33   | 100.00 | 62.81     | 57.02 | 48.61 |  |
| <i>KV Cache Size = 512</i>  |                    |        |       |          |                   |         |           |       |               |       |          |                   |        |        |           |       |       |  |
| StreamingLLM                | 27.20              | 26.66  | 34.51 | 50.04    | 42.70             | 23.35   | 23.33     | 21.35 | 23.51         | 57.50 | 87.68    | 41.87             | 7.50   | 97.50  | 62.34     | 53.63 | 42.54 |  |
| SnapKV                      | 30.08              | 41.24  | 56.84 | 57.62    | 47.75             | 29.67   | 24.58     | 24.47 | 24.23         | 64.00 | 92.35    | 41.38             | 7.17   | 99.50  | 64.72     | 57.12 | 47.63 |  |
| PyramidKV                   | 29.50              | 40.46  | 56.47 | 57.30    | 47.55             | 30.34   | 24.26     | 24.46 | 24.00         | 66.50 | 91.32    | 41.64             | 7.20   | 99.50  | 63.65     | 55.49 | 47.48 |  |
| LAQ                         | 31.64              | 45.55  | 55.21 | 57.73    | 49.60             | 30.99   | 26.67     | 24.79 | 24.85         | 71.00 | 92.33    | 43.06             | 6.92   | 100.00 | 62.16     | 58.45 | 48.81 |  |
| SpeckV                      | 31.12              | 43.77  | 57.22 | 57.51    | 49.32             | 31.06   | 26.34     | 24.61 | 24.90         | 65.00 | 92.13    | 43.32             | 7.00   | 100.00 | 65.31     | 61.89 | 48.78 |  |
| LookaheadKV                 | 31.39              | 44.92  | 57.56 | 58.56    | 47.72             | 30.82   | 29.24     | 24.82 | 25.83         | 72.50 | 91.92    | 43.39             | 7.08   | 100.00 | 64.87     | 58.36 | 49.31 |  |
| <i>KV Cache Size = 1024</i> |                    |        |       |          |                   |         |           |       |               |       |          |                   |        |        |           |       |       |  |
| StreamingLLM                | 27.23              | 30.80  | 36.64 | 50.59    | 43.26             | 23.45   | 25.73     | 21.67 | 25.49         | 63.50 | 88.84    | 42.56             | 7.50   | 93.50  | 63.15     | 55.73 | 43.73 |  |
| SnapKV                      | 29.64              | 44.60  | 57.30 | 57.62    | 48.31             | 31.18   | 27.57     | 24.17 | 25.84         | 69.50 | 92.04    | 42.78             | 7.08   | 99.50  | 64.57     | 58.46 | 48.76 |  |
| PyramidKV                   | 30.79              | 44.91  | 56.65 | 58.13    | 48.17             | 30.56   | 26.65     | 24.53 | 25.88         | 68.00 | 91.78    | 42.20             | 6.83   | 99.50  | 64.41     | 57.77 | 48.55 |  |
| LAQ                         | 31.63              | 45.63  | 55.02 | 57.70    | 50.27             | 31.28   | 28.82     | 25.10 | 26.18         | 72.50 | 92.33    | 43.31             | 6.50   | 100.00 | 62.75     | 59.04 | 49.25 |  |
| SpeckV                      | 31.59              | 45.44  | 57.98 | 57.51    | 49.16             | 31.95   | 28.67     | 24.95 | 25.77         | 67.50 | 92.23    | 43.94             | 6.00   | 99.50  | 65.21     | 62.30 | 49.36 |  |
| LookaheadKV                 | 31.14              | 46.04  | 57.77 | 58.22    | 48.43             | 30.72   | 30.75     | 25.31 | 26.66         | 72.50 | 91.92    | 43.39             | 7.08   | 100.00 | 64.87     | 58.36 | 49.57 |  |
| <i>KV Cache Size = 2048</i> |                    |        |       |          |                   |         |           |       |               |       |          |                   |        |        |           |       |       |  |
| StreamingLLM                | 28.53              | 37.02  | 39.90 | 51.22    | 45.83             | 23.69   | 28.41     | 21.91 | 26.50         | 67.50 | 90.98    | 42.53             | 7.25   | 90.50  | 64.88     | 57.52 | 45.26 |  |
| SnapKV                      | 31.22              | 46.14  | 56.94 | 58.12    | 48.21             | 31.74   | 27.57     | 24.17 | 27.57         | 64.50 | 92.04    | 42.78             | 6.38   | 99.50  | 64.98     | 58.80 | 49.38 |  |
| PyramidKV                   | 31.37              | 46.01  | 56.61 | 58.02    | 48.21             | 31.50   | 29.73     | 24.70 | 26.57         | 71.50 | 91.65    | 42.83             | 6.64   | 99.50  | 64.94     | 58.32 | 49.26 |  |
| LAQ                         | 31.30              | 45.69  | 55.62 | 57.61    | 49.91             | 31.33   | 30.96     | 25.51 | 26.77         | 72.50 | 92.33    | 43.54             | 6.83   | 100.00 | 63.77     | 59.28 | 49.56 |  |
| SpeckV                      | 31.88              | 46.64  | 57.39 | 57.97    | 48.80             | 32.72   | 30.96     | 25.38 | 26.82         | 71.00 | 91.48    | 43.65             | 5.88   | 99.50  | 65.79     | 61.16 | 49.81 |  |
| LookaheadKV                 | 31.01              | 46.37  | 57.24 | 58.15    | 48.31             | 31.12   | 32.56     | 25.22 | 27.07         | 72.50 | 91.48    | 43.56             | 6.38   | 99.50  | 64.96     | 59.13 | 49.66 |  |
| <i>KV Cache Size = 512</i>  |                    |        |       |          |                   |         |           |       |               |       |          |                   |        |        |           |       |       |  |
| StreamingLLM                | 17.65              | 26.69  | 28.40 | 41.05    | 33.46             | 20.82   | 15.72     | 19.15 | 15.14         | 43.00 | 82.57    | 38.44             | 1.50   | 70.00  | 62.84     | 56.69 | 35.82 |  |
| SnapKV                      | 19.14              | 32.65  | 45.99 | 54.81    | 38.95             | 26.59   | 17.66     | 20.83 | 16.04         | 49.50 | 87.10    | 38.90             | 3.50   | 99.50  | 64.62     | 58.29 | 42.13 |  |
| PyramidKV                   | 15.57              | 30.19  | 41.84 | 46.01    | 35.73             | 19.57   | 16.51     | 19.67 | 14.86         | 47.00 | 80.62    | 35.56             | 2.50   | 92.00  | 62.14     | 53.07 | 38.48 |  |
| LAQ                         | 22.74              | 42.15  | 53.55 | 57.89    | 42.84             | 36.74   | 21.33     | 22.25 | 18.34         | 64.50 | 89.55    | 40.93             | 3.00   | 100.00 | 66.74     | 61.70 | 46.52 |  |
| SpeckV                      | 23.03              | 37.14  | 53.58 | 56.77    | 42.24             | 31.82   | 21.33     | 22.86 |               |       |          |                   |        |        |           |       |       |  |

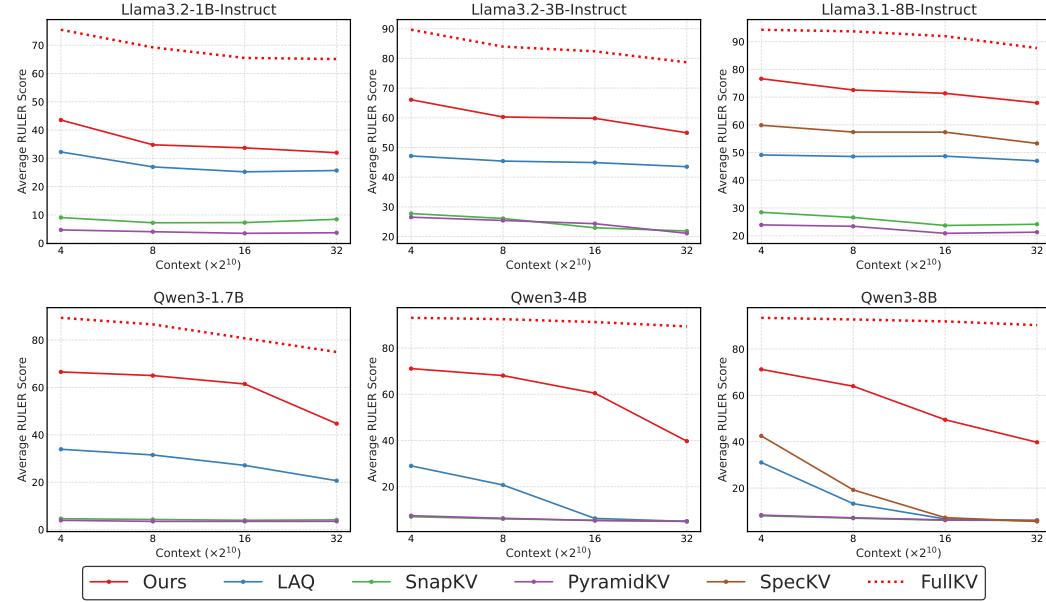
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## E.5 RESULTS ON RULER

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1191We report the RULER results across all six models tested, with cache budget settings at 64 (Figure 9)  
and 128 (Figure 10).

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Figure 9: Full RULER results across context lengths (budget = 64)

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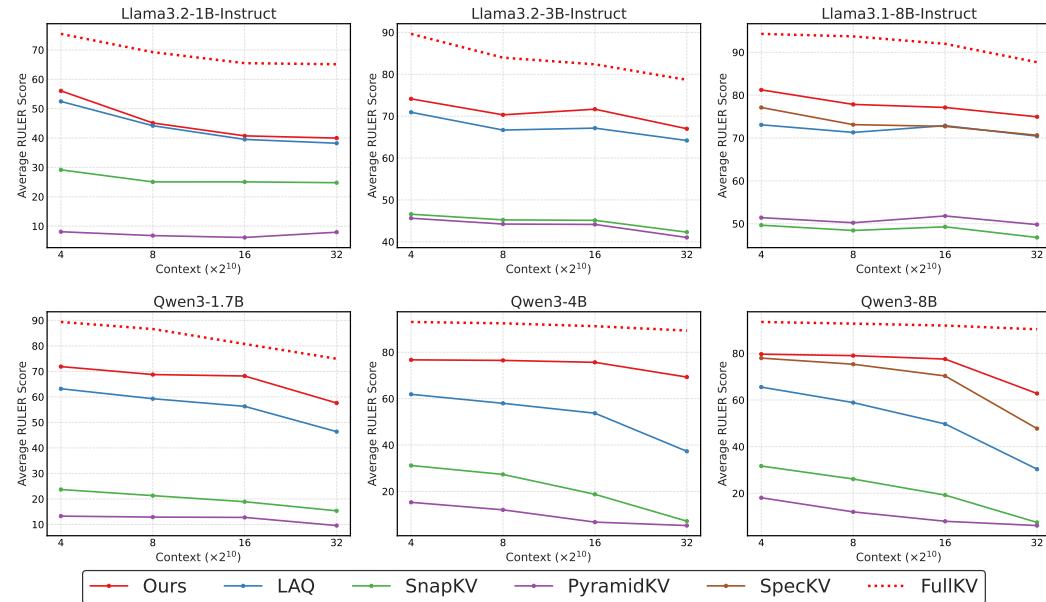


Figure 10: Full RULER results across context lengths (budget = 128)

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## E.6 ADDITIONAL EFFICIENCY ANALYSIS

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We show the full results of the latency analysis that were omitted in the main paper due to space limitation in this section. Note that the empirical TTFT overheads for some methods can be larger than theoretical estimations. These are probably due to a combination of measurement noise and inefficient implementation of these methods in KVCache-Factory or their official implementation. Better implementations may reduce these overheads significantly, more in line with the theoretical cost.

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Table 15: Theoretical and Practical Analysis across various context lengths and methods.

| Context Length | Method             | Theoretical Cost |                     |           | Empirical Cost     |           |
|----------------|--------------------|------------------|---------------------|-----------|--------------------|-----------|
|                |                    | Compute (TFLOPs) | Memory Traffic (GB) | TTFT (ms) | TTFT Overhead (ms) | TTFT (ms) |
| 4096           | Forward Pass Only  | 60               | 13                  | 113       | N/A                | 130       |
|                | LookaheadKV (ours) | 60               | 13                  | 114       | 0.92               | 141       |
|                | SnapKV             | 60               | 13                  | 113       | 0.01               | 143       |
|                | SpecKV             | 70               | 77                  | 165       | 52.10              | 223       |
|                | LAQ                | 61               | 444                 | 347       | 233.81             | 637       |
| 8192           | Forward Pass Only  | 136              | 13                  | 257       | N/A                | 291       |
|                | LookaheadKV (ours) | 137              | 13                  | 258       | 1.03               | 302       |
|                | SnapKV             | 136              | 13                  | 257       | 0.01               | 311       |
|                | SpecKV             | 159              | 81                  | 337       | 79.53              | 411       |
|                | LAQ                | 137              | 445                 | 492       | 234.59             | 800       |
| 16384          | Forward Pass Only  | 336              | 13                  | 635       | N/A                | 658       |
|                | LookaheadKV (ours) | 337              | 13                  | 636       | 1.27               | 677       |
|                | SnapKV             | 336              | 13                  | 635       | 0.01               | 695       |
|                | SpecKV             | 398              | 89                  | 792       | 157.05             | 866       |
|                | LAQ                | 337              | 447                 | 871       | 236.15             | 1182      |
| 32768          | Forward Pass Only  | 928              | 13                  | 1754      | N/A                | 1760      |
|                | LookaheadKV (ours) | 929              | 13                  | 1755      | 1.74               | 1798      |
|                | SnapKV             | 928              | 13                  | 1754      | 0.01               | 1838      |
|                | SpecKV             | 1115             | 106                 | 2156      | 402.80             | 2263      |
|                | LAQ                | 930              | 451                 | 1993      | 239.26             | 2314      |

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1296 **F HYPER-PARAMETERS**  
12971298 **Training hyper-parameters.** Learning rate was searched for Llama and Qwen model family  
1299 among  $[5 \times 10^{-5}, 1 \times 10^{-4}, 2 \times 10^{-4}, 1 \times 10^{-3}]$ . The final hyper-parameters for all experiments  
1300 are shown in Table 16.  
13011302 Table 16: Training hyperparameters.  
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| 1304 <b>Parameters</b>    | 1305 <b>Values</b>   |
|---------------------------|--|
| 1305 Optimizer            | 1306 Adam  |
| 1306 $\beta_1, \beta_2$   | 1307 0.9, 0.95   |
| 1307 Effective Batch Size | 1308 32  |
| 1308 Drop-out ( $p$ )     | 1309 0.0   |
| 1309 Max Sequence Length  | 1310 16384 (prompt length) + 512 (response length)                 |
| 1310 Train Iters          | 1311 7600  |
| 1311 Learning rate        | 1312 $1 \times 10^{-3}$ (for Llama), $2 \times 10^{-4}$ (for Qwen) |
| 1312 Schedule             | 1313 Cosine  |
| 1313 Warmup steps         | 1314 2%  |
| 1314 Min LR               | 1315 0.0   |
| 1315 Gradient clipping    | 1316 1.0   |

1317 **Eviction hyper-parameters.** We use the implementations in KVCache-Factory or their official  
1318 implementations (SpecKV) for all baseline methods, except for LAQ which we re-implement our-  
1319 selves. Following prior works (Li et al., 2024; Cai et al., 2024; Galim et al., 2025), we use stan-  
1320 dard configuration settings for all baseline methods, including an observation window size of 32,  
1321 maxpooling kernel size of 7, and mean reduction for GQA compatibility (Feng et al., 2024). For  
1322 LookaheadKV we use the same settings, except we do not use window size, as our method does  
1323 not train with the suffix window for prediction. Further, since our lookahead size  $n_{\text{lookahead}}$  is 32,  
1324 we set the maximum generation limit of LAQ and SpecKV to 32 tokens so that the methods can be  
1325 compared using the same number of draft tokens.  
13261327 **G DATASETS, BENCHMARKS, AND SOFTWARE**  
13281329 **Software** Our source code is available in the supplementary, and our implementation is built on  
1330 KVCache-Factory.1331 **Training Dataset** Our training dataset mixture consist of random samples from publicly available  
1332 datasets: 50K long\_sft subset of ChatQA2-Long-SFT-data, 20K subset of tulu-3-sft-olmo-2-mixture,  
1333 7K samples from The Stack, and 3K samples from MetaMathFewshot, HellaSwag\_DPO\_Fewshot,  
1334 and ARC\_DPO\_Fewshot, respectively.1335 **Evaluation Benchmarks** We used LongBench dataset as fetched and processed by KVCache-  
1336 Factory, see HF Dataset for the official source. For RULER, we used RULER Github. For LongProc,  
1337 we used LongProc Github.  
13381339 **H LLM USAGE**  
13401341 LLM assistants were used to refine the wording of selected sentences, while the majority of the text  
1342 was written by human. All LLM-generated text was carefully inspected to ensure that it contained  
1343 no harmful or controversial content. Additionally, we used LLMs to help in finding some of the  
1344 related literature discussed in the paper.  
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