AirRAG: Autonomous Strategic Planning and Reasoning Steer Retrieval Augmented Generation

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Abstract

Leveraging the autonomous decision-making capabilities of large language models (LLMs) has demonstrated superior performance in reasoning tasks. However, despite the success of 004 iterative or agentic retrieval-augmented generation (RAG) techniques, these methods are often constrained to a single solution space when confronted with complex problems. In this paper, we propose a novel thinking pattern in RAG that integrates autonomous strategic planning with efficient reasoning actions, significantly activating intrinsic reasoning capabilities and 012 expanding the solution space of specific tasks via Monte Carlo Tree Search (MCTS), which we refer to as AirRAG. Specifically, our approach designs five fundamental reasoning ac-016 tions, which are expanded to a broad tree-based 017 reasoning space using MCTS. The approach also incorporates self-consistency verification to explore potential reasoning paths and inference scaling law. Additionally, computationally optimal strategies are employed to allocate more inference resources to key actions, thereby enhancing overall performance. Experimental results demonstrate the effectiveness of AirRAG, showing significant performance gains on complex question-answering 027 datasets. Furthermore, AirRAG is flexible and lightweight, making it easy to integrate with other advanced technologies and models.

1 Introduction

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Retrieval-Augmented Generation (RAG) has shown great potential in addressing the issue of generating factually incorrect content, especially in domain-specific or knowledge-intensive tasks (Kandpal et al., 2023). However, as task complexity increases, several new challenges emerge, such as the inability to retrieve sufficient knowledge with a single query and the difficulty of understanding the intricate reasoning logic inherent



Figure 1: Comparison of average performance across three datasets with varying numbers of output sequences. L_{total} represents the total number of tokens consumed during the reasoning process. AirRAG leverages generation diversity and self-consistency to explore the potential solution space, significantly enhancing overall performance by scaling inference computation.

in the question. To tackle these challenges, it is crucial to harness the reasoning capabilities of large language models (LLMs) to improve RAG performance (Jiang et al., 2023; Jeong et al., 2024; Asai et al., 2024; Yu et al., 2024). 041

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Previous research on complex query scenarios has primarily focused on optimizing the query and retrieval processes to obtain relevant information (Shi et al., 2023; Zhou et al., 2023; Gao et al., 2023; Jiang et al., 2023; Zheng et al., 2024; Asai et al., 2024; Yan et al., 2024). Iterative retrieval is frequently used to improve the depth and relevance of search results in information retrieval tasks. This process continuously updates intermediate queries and results to satisfy dynamic information needs during the complex task-solving process (Jeong et al., 2024; Yue et al., 2024). In addition, Li et al. (2025) integrates an agentic search workflow into the reasoning process, enabling dynamic retrieval when LLMs encounter uncertain knowledge points. The agentic LLMs are trained to learn step-by-step

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reasoning with search through reinforcement learning (Chen et al., 2025; Zheng et al., 2025).

However, these approaches face two significant issues. First, the single reasoning paradigm and the chain-like reasoning process often fail to effectively explore the solution space, particularly when reasoning relies on self-exploration. This process is vulnerable to low-quality intermediate reasoning steps and is easily trapped in a narrow solution space. Second, the agentic search workflow and guiding self-exploration become challenging when using relatively smaller language models (e.g., *Qwen2.5-7B-Instruct* (Yang et al., 2024)). Furthermore, trainable agentic LLMs require efficient reinforcement learning training data and are difficult to apply to models with hundreds of billions of parameters.

In response to these challenges, we propose

AirRAG, a method that leverages autonomous

strategic planning and reasoning capabilities and

expands the solution space using Monte Carlo

Tree Search (MCTS). We design five fundamen-

tal reasoning actions: system analysis, direct an-

swer, retrieval-answer, query transformation, and

summary-answer. These actions are the core and

frequently used ones in the deep search scenar-

ios, which can effectively address a wide range

of problems in various scenarios, including those

that require progressive or parallel queries. Impor-

tantly, these actions can be executed efficiently on

LLMs of different scales. Additionally, we intro-

duce MCTS and self-consistency to enable con-

trollable reasoning path generation and efficient

inference scaling. To accurately select the answer

from multiple reasoning paths, we combine a vot-

ing mechanism with a process-supervised reward

model. As inference computation increases, our

approach demonstrates significant performance im-

provements as shown in Figure 1. Moreover, Air-

RAG features a flexible architecture that can easily

integrate other advanced methods into the approach

as additional action branches. In summary, our

• We design five fundamental reasoning actions

that can address most problem types in deep

search scenarios, ensuring controllable reason-

• We introduce MCTS and self-consistency to

effectively expand the solution space for com-

plex tasks. Our approach improves generaliza-

tion and performance through comprehensive

main contributions are as follows:

ing processes.

Retrieval-Augmented Generation (RAG). RAG has demonstrated significant improvements in the performance of LLMs in knowledge-intensive

tasks. Compared to vanilla RAG, optimizing the query and retrieval process enhances knowledge correlation and, consequently, improves reasoning

performance. Several methods, such as query expansion and transformation, have been proposed to achieve better retrieval results (Zhou et al., 2023; Ma et al., 2023; Gao et al., 2023). However, as task complexity increases, retrieving sufficient knowledge in a single query becomes increasingly difficult. To address this, iterative retrieval techniques have been proposed to gather additional contextual references. For instance, IR-CoT (Trivedi et al., 2023) utilizes chain-of-thought (CoT) to guide the retrieval process, refining the CoT with the retrieved information. Similarly, ITER-RETGEN (Shao et al., 2023) combines retrieval and generation modules to promote a deeper understanding of specific tasks.

Autonomous Planning and Reasoning in RAG. In addition to optimizing retrieval, activating the planning and reasoning capabilities of LLMs can significantly improve the efficiency and relevance of the retrieved information. Self-RAG and its variants (Asai et al., 2024; Yan et al., 2024; Jeong et al., 2024) adopt a self-reflection mechanism that iteratively predicts reflection tokens during training, enabling better control during inference. Auto-RAG (Yu et al., 2024) systematically plans retrievals and refines queries to acquire valuable knowledge through multi-turn iterations. Iter-DRAG (Yue et al., 2024) explores inference scaling strategies in RAG, improving LLMs' ability to effectively acquire and utilize contextual information. Search-o1 (Li et al., 2025) designs an agentic search workflow to dynamically obtain effective knowledge. ReSearch (Chen et al., 2025) and Deep-Researcher (Zheng et al., 2025) train agentic LLMs to reason with search using reinforcement learning. Despite the progress made in these methods, they often struggle to explore the solution space

inference scaling and a pluggable architecture.

• We show thorough experimental results that AirRAG outperforms current iterative or agentic methods, effectively activating the planning and reasoning capabilities of LLMs and flexibly expanding the solution space.

2 **Related Work**

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effectively during reasoning. Self-exploration frequently leads to being trapped in a limited solution space, hindered by low-quality reasoning steps
even after multiple iterations. This issue is often attributed to the chain reasoning pattern and the difficulty small-scale LLMs face when handling overly complex tasks in a single iteration.

Monte Carlo Tree Search (MCTS). To address these challenges, tree-based search algorithms, par-171 ticularly Monte Carlo Tree Search (MCTS), have 172 emerged as effective tools to expand search spaces 173 and enhance reasoning capabilities (Silver et al., 174 2017; Chen et al., 2024; Qi et al., 2024; Zhang et al., 2024). MCTS has been shown to extend 176 reasoning by exploring multiple branching queries, 177 thus enabling the exploration of diverse reasoning 178 paths (Yao et al., 2023; Besta et al., 2024). In 179 the mathematical reasoning scenario, Zhang et al. 180 (2024) and Chen et al. (2024) leverage MCTS 181 to achieve more efficient exploration of solution 182 spaces, while Qi et al. (2024) designs rich human-183 like reasoning actions to improve reasoning tra-184 jectories. Furthermore, recent research indicates 185 that inference scaling (Yue et al., 2024) and selfconsistency (Wang et al., 2023) can lead to substantial improvements. In this context, our approach samples diverse reasoning paths to achieve both 189 inference scaling and self-consistency verification 190 during the next expansion of the action space.

> Unlike existing methods that focus on optimizing query and retrieval processes or leveraging LLMs' reasoning capabilities through iterative retrieval, AirRAG uniquely integrates MCTS and self-consistency to systematically expand the solution space and ensure the controllability of the reasoning process. Simultaneously, we design five fundamental reasoning actions that effectively address a broader range of question types, particularly in complex tasks. In the experiment, we thoroughly verify the performance gains brought by the inference scaling law and investigate how to rationally allocate inference resources.

3 Methodology

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In order to effectively explore the solution space during reasoning, we propose a controllable treebased framework of RAG. This framework combines Monte Carlo Tree Search (MCTS) with five distinct reasoning actions, enabling efficient and controlled expansion of the solution space. Meanwhile, we further implement more comprehensive inference scaling strategies based on Yue et al. (2024) and employ pruning techniques along with computationally optimal strategies to strike a balance between effectiveness and efficiency. The whole process is illustrated in Figure 2.

3.1 Define Fundamental Reasoning Actions

Relying solely on the autonomy of LLMs for iterative self-exploration often results in getting trapped in a solution space that is difficult to navigate, especially when dealing with different types of complex questions. IterDRAG (Yue et al., 2024) uses a single action type to generate the next reasoning step, which can lead to ineffective space exploration. The core of MCTS generation lies in the action space, which defines the scope of tree exploration. Based on advanced methods and reasoning language models, we summarize the most common actions in RAG, such as query transformation and retrieval answering. Meanwhile, the chain-ofthought in reasoning models has demonstrated superior performance in complex open-domain question answering. Therefore, simplifying human cognitive processes in complex reasoning is essential (Jaffe et al., 2023). Inspired by this, we introduce five fundamental human-like reasoning actions to bridge the gap between LLM reasoning and human cognition in RAG scenarios.

- *A*₁: *System Analysis* (SAY). This action analyzes the overall structure of the problem, followed by its decomposition or planning. It represents systematic and global thinking before problem-solving.
- A₂: *Direct Answer* (DA). This action leverages parametric knowledge of LLMs to answer questions directly, without relying on any external knowledge.
- *A*₃: *Retrieval-Answer* (RA). This action retrieves related knowledge from the external knowledge base to support subsequent reasoning.
- A_4 : Query Transformation (QT). This action transforms human questions in order to improve retrieval performance. It supports various transformations, such as rewriting, step back prompting, follow-up questions and multi-query retrieval.
- *A*₅: *Summary-Answer* (SA). This action combines intermediate reasoning steps, answers and the initial questions to generate the final answer.



Figure 2: The schematic diagram of our proposed AirRAG. AirRAG implements a paradigm that combines system thinking with step-by-step reasoning. In the inference phase, we introduce MCTS and self-consistency to scaling computation, which significantly outperforms other strong baselines.

The above five actions define a highly diverse action space $\{A_1, A_2, A_3, A_4, A_5\}$. In the first step, the initial state is denoted as s_0 and then MCTS selects the action a_1 and a_2 to prompt the LLM to generate the next reasoning steps in parallel. Subsequent actions are performed sequentially to expand the reasoning path. It is important to note that there are sequential dependencies between different actions. For example, A_1 and A_2 can only be executed after the root question. Additionally, we incorporate the diverse sampling of self-consistency (Wang et al., 2023) for each action to expand the reasoning paths. Specifically, an action is more likely to generate the correct reasoning step if we sample multiple times in the current state. Finally, we can obtain multiple generated reasoning trajectories, such as $[s_0 \oplus s_{1:n}]$. To further improve inference efficiency, we choose the action $\{A_3, A_4, A_5\}$ as a simplified action space, referred to as AirRAG-Lite, which achieves a better balance between efficiency and effectiveness.

3.2 Perform Reasoning Processes via MCTS

3.2.1 Solution Generation

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Based on the action space defined above, we introduce MCTS to generate candidate reasoning trajectories. The initial root node, s_0 , represents the question without any reasoning steps. The policy is directly modeled by a language model as $\pi(a|s) = LM(a|s)$, and the state transition function combines preceding reasoning steps with current actions, i.e., $s_i = \text{Concat}(s_{0:i-1}, a_j)$. During each MCTS rollout, we execute multiple steps, including *selection*, *expansion*, *simulations*, and *backpropagation*. Multiple rollouts are performed to expand the solution space. To balance the exploration and exploitation, we adopt the wellknown Upper Confidence Bounds applied to Trees (UCT) (Kocsis and Szepesvári, 2006) for node selection as follows: 290

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$$\operatorname{UCT}(s,p) = \frac{Q(s,a)}{N(s)} + w \sqrt{\frac{\log N_p(s)}{N(s)}}, \quad (1)$$

where Q(s, a) is the reward value for node s and is updated through backpropagation. N(s) denotes the number of visits to s, p is the parent node of s, and w is the weight to balance exploration and exploitation.

When the search reaches a terminal node, defined either by a terminal state or a predetermined maximum tree depth d, we obtain a trajectory from the root to the terminal node. All trajectories from the rollout iterations are collected as candidate solutions. Section 3.3 explains how we select the optimal answer node from these trajectories.

3.2.2 Inference Scaling

Numerous studies have demonstrated that scaling inference computation can significantly improve the performance of LLMs without additional training (Snell et al., 2024; Yue et al., 2024). Based on

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the above methods, we explore strategies to lever-318 age inference computation scaling in AirRAG. One 319 straightforward strategy is extending the *effective* context length (short for L_{max}) during the document retrieval phase, allowing more related documents to supplement the knowledge base. Addi-323 tionally, we perform multiple *rollouts* to thoroughly 324 explore the solution space relying on the tree-based search. Adjusting the number of output sequences (n) generated during certain actions enables self-327 consistency verification and further inference scaling. These strategies provide flexibility for scaling 329 inference computation in RAG, empowering LLMs 330 to address complex knowledge-intensive queries more effectively.

> To improve efficiency and minimize redundant computations, we implement an early pruning strategy for state nodes and reasoning paths. Deduplication is applied to the output sequence states generated by each action, ensuring the diversity of the subsequent path. Furthermore, if multiple rollouts select the same state sequence, only one valid reasoning path is retained.

3.2.3 Flexible Architecture

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Our tree-based architecture provides the flexibility to integrate other advanced approaches. We reproduce the IterDRAG method based on the prompt design by Yue et al. (2024). Meanwhile, inspired by its iterative implementation, we simplify the fundamental action space to $\{A_3, A_4, A_5\}$, enabling a faster implementation while still achieving relatively good results. These methods serve as an exploratory extension of our approach and can be activated or deactivated as needed. Due to the training-free nature of our method, its generator LLM can be arbitrarily replaced with the strongest existing models for performance improvement.

3.3 Select the Optimal Answer Node

For common mathematical reasoning tasks, a simple consistency-based method can efficiently select the most precise reasoning path. For example, the most frequent number extracted from multiple candidate solutions in MATH (Hendrycks et al., 2021) can be chosen as the final answer. However, extracting precise answers and performing effective aggregation becomes more challenging for knowledge-intensive tasks. To address this, we design two self-consistency verification methods for such problems. *Jaccard similarity* and *text embeddings* are two different approaches used in natural language processing to measure the similarity between texts. We apply these methods to cluster text answers and compute answer scores as follows:

$$jcdScore_{i} = \frac{1}{N} \sum_{j=1}^{N} \frac{|A_{i} \cap A_{j}|}{|A_{i} \cup A_{j}|},$$
 (2) 371

$$embScore_i = \frac{1}{N} \sum_{j=1}^{N} \cos(E_i, E_j), \qquad (3)$$

where N is the number of valid answer nodes, A_i is the word-level set of answer text i, and E_i denotes the embedding vector of answer text i.

In addition, we further investigate the *self-refine* and process-supervision *reward model* to identify the most accurate reasoning trajectory. Selfrefinement uses the A_5 (Summary-Answer) action to refine the final answer from all candidate answer nodes. The reward modeling process consists of two steps: data synthesis and instruction tuning.

- Data synthesis: We leverage MCTS to perform multiple rollouts on partial training sets. Based on known ground truth, we sample positive and negative reasoning trajectories and use Monte Carlo estimation to evaluate intermediate state scores.
- Instruction tuning: Synthetic samples are used to fine-tune a relatively small LLM, such as *Qwen2.5-14B-Instruct*.

4 **Experiments**

In this section, we conducted experiments on complex QA benchmarks by answering the following research questions.

- **RQ1**: Does AirRAG outperform state-of-theart baselines?
- **RQ2**: How does AirRAG perform when it comes to comprehensive inference scaling?
- **RQ3**: What is the performance benefit of Air-RAG in optimizing the allocation of inference computation?
- **RQ4**: How does AirRAG perform for various verification methods for multiple candidate rollouts?
- **RQ5**: What is the intuitive performance of 406 AirRAG in the reasoning process? 407

4.1 **Experimental Settings**

4.1.1 Datasets

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To evaluate the effectiveness of AirRAG, we conduct experiments on various question-answering (QA) tasks, including both open-domain QA and multi-hop QA. The complex multi-hop QA datasets consist of HotpotQA (Yang et al., 2018), MuSiQue (Trivedi et al., 2022) and 2WikiMultiHopQA (2Wiki) (Ho et al., 2020). Other single-hop QA datasets include Natural Questions (NQ) (Kwiatkowski et al., 2019), TriviaQA (Joshi et al., 2017), PopQA (Mallen et al., 2023) and WebQA (Berant et al., 2013).

4.1.2 Implementation Details

We use the hyperparameters reported for the existing models whenever available. Implementation details are available in the Appendix A.

4.1.3 **Baselines and Metrics**

426 To investigate the enhancement effects of thinking and planning on complex RAG tasks, we compare it with vanilla RAG, which performs only a 428 single retrieval and generation process. We evalu-429 ate the naive generators of Qwen2.5 (Yang et al., 430 2024) series instruction models and *Llama3-8B*-Instruct (Grattafiori et al., 2024). In the retrieval phase, we employ *multilingual-e5-base* (Wang 433 et al., 2024) as the retriever. The prompt of 434 vanilla RAG are shown in the Appendix D. For 435 iterative retrieval, we compare AirRAG with Iter-436 RetGen (Shao et al., 2023), Self-RAG (Asai et al., 2024), Auto-RAG (Yu et al., 2024), and Iter-438 DRAG (Yue et al., 2024). For agentic retrieval, 439 we compare AirRAG with Search-o1 (Li et al., 440 2025), ReSearch (Chen et al., 2025), and Deep-Researcher (Zheng et al., 2025). To further explore 442 RAG performance and inference computation scal-443 ing, we focus on a comparison with IterDRAG for a given budget on inference computation. For eval-445 uation metrics, we report Exact Match (EM), F1 446 score (F1) and Accuracy (Acc) between the generated summary and gold answer, where accuracy 448 measures whether the gold answer is covered in the 449 generated answer. 450

4.2 Main Results (RQ1)

We first evaluate the performance of AirRAG on various complex QA datasets. Table 1 compares its accuracy and F1 scores with strong baselines based on LLMs of different scales. The optimal performance exhibits consistent gains as the LLMs scale up. For the *Qwen2.5-7b-instruct* model, our approach achieves the best performance, even surpassing the trainable approaches. To further validate its effectiveness on large-scale reasoning models, we also conduct experiments on Qwen3-235B in both the thinking mode and non-thinking mode. In thinking mode, our approach achieves state-ofthe-art performance among all datasets.

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4.3 Inference Scaling for RAG (RQ2)

Inference computation scaling can enable LLMs to improve their output performance (Snell et al., 2024). Self-consistency can also improve the robustness of the reasoning process (Wang et al., 2023). Therefore, we carry out a comprehensive experimental analysis on the inference computation scaling. Specifically, we can adjust both the number of retrieved documents in a single retrieval and the effective context length in all iterations. The average performance of three datasets exhibits consistent gains in Figure 3. In subsequent experiments, unless otherwise specified, the data presented represent the average performance across the HotpotQA, MuSiQue, and 2Wiki datasets. As shown in Figure 1, the average performance increases with the number of output sequences per action, demonstrating the effectiveness of self-consistency. We also investigate the number of effective reasoning paths under different rollouts in Figure 4. The performance improvement caused by the increase of effective reasoning paths in the early stage is relatively high. We provide additional dataset-specific results in Appendix B.

4.4 Ablation Studies

Effect of Computationally Optimal Strategies (**RQ3**). Extensive experiments show that the outputs of certain actions (e.g., RA, DA and SA) are almost consistent when performing multiple generations. Therefore, we only increase the number of output sequences (short for n) for the remaining actions (e.g., SAY and QT), which reduces invalid inference computation while maintaining good results. This also reflects that this kind of reasoning action, which effectively activates the creativity of LLMs, requires more diversified sampling strategies. We adjust the sampling parameters (top-p=1.0and temperature=1.0) to improve the diversity of the model output. The complete experimental results in Table 2 show that the diversity of key actions can significantly improve performance.

From the aforementioned experiments, it is ob-

Method	NQ		TriviaQA		HotpotQA		MuSiQue		2Wiki		Average	
	F1	Acc	F1	Acc	F1	Acc	F1	Acc	F1	Acc	F1	Acc
Qwen2.5-7B												
ŽeroShot QA	38.4	37.4	57.7	56.3	36.1	34.8	9.1	7.5	45.0	44.1	37.3	36.0
Vanilla RAG	57.8	53.9	70.1	66.3	61.3	56.9	13.5	8.3	45.9	42.8	49.7	45.6
IterDRAG*	58.3	54.1	73.5	69.1	65.3	60.7	18.3	13.0	51.8	47.0	53.4	48.8
Search-o1*	57.8	54.3	72.6	69.8	57.3	54.2	20.2	18.5	56.9	53.6	53.0	50.
ReSearch*	61.3	59.6	76.2	73.4	70.3	68.1	30.9	27.4	62.5	61.0	60.2	57.9
DeepResearcher	62.4	59.8	75.9	73.2	67.6	63.9	33.9	27.8	65.4	62.3	61.0	57.4
AirRAG-Lite	60.8	57.3	74.1	70.0	68.2	63.2	23.4	17.3	51.1	48.0	55.5	51.2
AirRAG	60.4	56.2	74.3	70.1	74.9	70.0	30.3	23.6	65.7	63.2	61.1	56.6
Qwen2.5-14B												
ZeroShot QA	47.1	46.3	70.7	69.5	42.5	41.3	13.5	12.1	48.2	47.3	44.4	43.
Vanilla RAG	62.0	58.2	75.2	71.2	67.0	62.0	20.0	14.4	52.0	49.4	55.2	51.0
IterDRAG*	58.5	53.9	76.4	72.3	71.8	66.2	23.9	17.2	57.4	54.1	57.6	52.7
Search-o1*	61.2	59.7	74.3	72.6	71.4	67.4	23.2	20.4	58.1	55.8	57.6	55.2
AirRAG-Lite	64.8	60.9	78.9	75.0	77.2	72.5	30.3	24.3	70.3	68.0	64.3	60.
AirRAG	66.2	62.1	78.1	73.8	79.9	75.3	36.0	31.9	70.4	68. 7	66.1	62.4
Qwen2.5-32B												
ZeroShot QA	46.8	45.9	69.8	68.8	42.9	41.8	11.1	9.6	48.1	47.2	43.7	42.'
Vanilla RAG	60.6	56.7	75.4	71.6	66.5	62.5	19.5	13.8	51.8	49.6	54.7	50.
IterDRAG*	61.1	56.7	76.9	73.0	72.0	67.3	23.3	17.9	58.2	55.4	58.3	54.
Search-o1*	63.5	61.6	75.6	72.8	72.8	68.4	30.2	27.3	60.5	58.9	60.5	57.
ReSearch*	63.8	61.2	74.6	72.3	76.2	72.6	38.3	33.4	66.8	62.8	63.9	60.5
AirRAG-Lite	65.6	61.9	75.8	71.6	79.3	74.8	33.3	32.5	72.0	70.8	65.2	62.3
AirRAG	66.5	62.7	78.9	74.6	81.1	76.1	36.5	32.7	71.9	70.6	67.0	63.
Qwen3-235B (non-thinking)												
ZeroShot QA	64.1	63.7	77.1	76.3	53.9	52.9	17.1	15.7	56.8	56.1	53.8	52.9
Vanilla RAG	66.0	65.3	78.0	76.2	69.2	67.7	20.8	19.1	53.3	52.2	57.4	56.
IterDRAG*	65.7	63.3	78.8	76.9	75.5	69.7	32.2	25.2	64.8	60.8	63.4	59.2
Search-o1*	67.3	66.2	77.3	76.4	75.9	73.8	36.7	34.2	71.3	68.2	65.7	63.
AirRAG-Lite	67.7	66.9	77.6	75.8	78.3	76.8	43.7	36.5	74.9	74.1	68.4	65.
AirRAG	66.4	65.6	79.1	77.3	79.6	78.1	47.2	40.0	76.2	75.5	69.7	67.
Qwen3-235B (thinking)	(()	(5.6	70.0	70.6	54.0	50.5	01.0	10.0	56.6	56.0		644
ZeroShot QA	66.1	65.6	79.3	78.6	54.2	53.5	21.3	19.9	56.6	56.3	55.5	54.
Vanilla RAG	67.6	67.1	77.9	76.9	72.5	71.9	18.2	16.4	57.5	56.6	58.7	57.
IterDRAG*	68.8	67.1	80.9	78.7	76.3	71.1	30.0	23.1	67.1	64.5	64.6	60.
Search-o1*	67.2	66.4	78.1	77.5	75.2	72.4	33.4	28.9	69.2	66.3	64.6	62.
AirRAG-Lite	73.2	72.7	81.1	80.1	86.2	85.6	44.2	37.8	76.4	75.6	72.2	70.
AirRAG	74.3	72.8	81.4	80.1	84.7	84.0	47.5	40.3	76.8	76.2	72.9	70.'

Table 1: Overall evaluation results on the test sets of five datasets. * indicates the results reproduced by us. The best results for each model are in **bold**. The number of both rollouts and output sequences is set to 1. The number of documents for a single retrieval is set to 5.

served that the recall and accuracy of model are linearly correlated. Intuitively, the size of document database is also related to the recall score. By reducing the scale of the document database, we find a gradual improvement in model performance (shown in Figure 4). This observation provides experimental evidence for effective database partitioning in practical application.

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515Effect of Verification Methods (RQ4). The larger516search space also generates more candidate reason-517ing trajectories. Therefore, how to select the opti-518mal trajectory is crucial for the final performance.

We compare multiple verification methods with the average scores of all candidates in Figure 5. These two self-consistency verification methods are always slightly better than the average score, but they are not nearly as good as the SA and QwenRM methods. The SA method uses the LLM to further refine the final answer from all candidate rollouts, which is simple and effective. Finally, the reward model achieves the most competitive results due to the introduction of supervised information on key intermediate reasoning steps in the training process. However, collecting process-supervised train-

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Figure 3: Impact of the retrieved document number scaling (Left) and the maximum context length scaling (Right) on model performance (averaged Accuracy and Recall of three datasets). All methods show consistent performance improvements as the effective inference computation scales.

Method	Average		
	F1	Acc	
Vanilla RAG	47.0	43.2	
IterDRAG	49.8	45.9	
AirRAG			
$+ n_{\text{all}} = 1$	62.9	58.8	
$+ n_{\text{all}} = 3$	<u>63.4</u>	<u>62.1</u>	
$+ n_{a_1,a_4} = 3, n_{a_2,a_3,a_5} = 1$	63.2	62.0	
$+ n_{a_1,a_4} = 3, n_{a_2,a_3,a_5} = 1, q_{div} = 1.0$	65.1	63.9	

Table 2: Performance comparison with different computationally optimal strategies on the HotpotQA, MuSiQue and 2Wiki datasets. n_{a_i} denotes the number of output sequences of the action a_i in a single extension. q_{div} indicates that setting top-p to 1.0 and temperature to 1.0 for query-related actions, i.e. SAY and QT, increases the diversity of reasoning. The default sampling parameters top-p, top-k and temperature are set to 0.8, 50 and 0.7 respectively. Rational sampling strategies further improve performance across multiple datasets.

ing samples requires high computational costs and high-quality raw data. In the practical application scenario, we can choose the appropriate method while balancing efficiency and effectiveness.

Qualitative Analysis (RQ5) 4.5

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To make it easier to understand why our proposed AirRAG works, we present a qualitative analysis in MuSiQue. Existing iterative methods are often 538 trapped in a single solution space when confronted 539 with complex tasks. As illustrated in Figure 13, these iterative methods exhibit a key limitation that insufficient or ambiguous retrieval context can lead to repetitive follow-up queries until it reaches the predefined maximum depth of iterations. This inefficient iteration results in high computational cost and incorrect answer. In contrast, our proposed Air-546 RAG designs efficient reasoning actions to achieve autonomous planning and reasoning. As shown in Figure 14, the SAY action decomposes the original 549



Figure 4: Left: Performance comparison under different size of document database. A streamlined database can maintain a better performance. Right: Performance comparison in increasing the number of valid rollouts. Sampling a higher number of diverse reasoning paths consistently improves accuracy.

query into a more rational sequence of sub-queries, and then the combination of RA and QT ensures the accuracy of the intermediate reasoning step. We eventually leverage the efficient reasoning trajectory to obtain the correct answer.

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5 Conclusions

In this paper, we propose AirRAG, a novel RAG approach to fully leverage the planning and reasoning capabilities of LLMs. AirRAG designs an efficient action space for the controllable reasoning generation. We also introduce Monte Carlo Tree Search to expand the solution space. Meanwhile, by employing the tree-based search and selfconsistency verification, we explore potential reasoning paths and achieve comprehensive inference computation scaling. In addition, computationally optimal strategies are used to apply more computation to key actions, leading to further performance improvements. Experimental results on diverse QA datasets demonstrate the significant superiority of AirRAG over other methods designed for complex deep search scenarios.

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572 Limitations

Although our model achieves competitive perfor-573 mance in various RAG tasks, there are some meth-574 ods and limitations that can be improved. The 575 current optimal computation allocation strategy is derived from sufficient experiments. We can consider designing an automated policy model to im-578 plement the trade-off between computational cost 579 and performance. Despite great efforts in the inference scaling of RAG, the experimental analysis may be limited due to the massive computational cost of tree-based search approaches. We will explore more complex reasoning tasks to verify the 584 robustness and effectiveness of our approach. In 586 addition, the large search space also brings more noise information, so we will further investigate the reward model or strategy to explore a better 589 reasoning path.

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A Implementation Details

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For evaluation, we randomly select 1,000 samples from the whole validation sets of each dataset as our final test set, with a fixed random seed 0. To better understand the complexity of multi-hop reasoning in these datasets, we analyze the hop distribution of the HotpotQA, MuSiQue, and 2Wiki-MultiHopQA test sets in Figure 6. The statistics show that there is a high proportion of complex reasoning queries with 3 hops or more (aboout 30%, 50%, 25%). HotpotQA lacks explicit hop annotations, so we instead count the number of supporting facts. MuSiQue has a significantly higher proportion of 3-hop and 4-hop queries compared to the other datasets, indicating great reasoning complexity. This observation is further corroborated by our experimental results in Table 1 and Figure 7. The performance of our approach on MuSiQue is much lower than those of the other two datasets.

In the retrieval process, we employ the multilingual-e5-base (Wang et al., 2024) as the retriever and use the widely used Wikipedia dump from December 2018 as the retrieval corpus (Karpukhin et al., 2020) which comprises over 21 million passages. For generation, the default sampling parameters top-p, top-k and temperature are set to 0.8, 50 and 0.7 respectively. Evaluation metrics include Exact Match (EM), F1 score (F1), and Accuracy (Acc), where accuracy indicates whether the ground truth is a substring of the final generated answer. For reward model training, we sample 8,000 question-answer pairs from each dataset and generate more than 156,000 reasoning paths using our proposed AirRAG (rollouts=32, n=4, $q_{div}=1.0$). In inference scaling experiments, we sample maximum computation budgets L_{max} (e.g., 8k, 16k, 32k, 64k and 128k tokens). The $L_{\rm max}$ (maximum effective context length) denotes the maximum number of input tokens across all rollouts following (Yue et al., 2024). The predetermined maximum tree depth d is set to 10, specifically indicating that the SAY and SA actions are executed once, while the RA-QT or QT-RA actions have a maximum of 4 iterations.

B Additional Experiment Results

We evaluate the performance of AirRAG on various complex QA datasets. Table 3 compares its accuracy and F1 with strong baselines under the given inference computation budget, which is implemented based on *Qwen2.5-14B-Instruct* and one million document database. The optimal performance exhibits consistent gains as L_{max} expands, which is termed as the *inference scaling laws* for RAG (Yue et al., 2024). We integrate the remaining methods for a given maximum computational budget into our approach, dubbed as AirRAG-Blender. The best results are obtained by using only the SA action to refine the final answer from all candidates, as shown in Table 3. This also demonstrates the flexibility of our approach architecture. In addition, to verify the robustness and generalization of AirRAG, Table 4 shows the performance on more diverse LLMs and datasets. For a fair comparison, we utilize the widely used Wikipedia dump from December 2018 (Karpukhin et al., 2020) as the retrieval corpus. We observe consistent improvements over vanilla RAG and existing iterative methods (more than 10% on average). The significant boost over IterDRAG and Auto-RAG suggests that AirRAG explores more effective reasoning paths through the human-like thinking paradigm and treebased search. Furthermore, we present detailed inference scaling results for each dataset individually, as shown in Figure 7 and Figure 8.

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C Inference Efficiency Analysis

Given the inherently large search space of treebased search, we design computational optimization strategies for different actions to avoid inefficient and redundant expansions, as shown in Table 2. Furthermore, in Section 3.2.2, we propose pruning strategies for state nodes and reasoning paths. These optimizations significantly reduce inefficient LLM inference and repetitive path exploration. In practical applications, we can select appropriate configuration parameters such as rollout, n, and L_{\max} based on computational resource budgets and time constraints, ensuring effectiveness while achieving inference efficiency comparable to current mainstream iterative RAG approaches. We analyze the average inference efficiency per sample on the HotpotQA dataset in Table 5.

D Prompt Examples

Given a user input query, our proposed AirRAG, as shown in Figure 2, first attempts the *direct answer* (DA) action without prompts and performs *system analysis* (SAY) using the prompt in Figure 9. Subsequently, AirRAG performs *retrieval and answer* (RA) with the prompt in Figure 11, or *query transformation* (QT) to generate refined queries for

L_{\max}	Method	HotpotQA		MuSiQue		2Wiki		Average	
		F1	Acc	F1	Acc	F1	Acc	F1	Acc
	ZeroShot QA	42.5	41.3	13.5	12.1	48.2	47.3	34.7	33.6
8k	Vanilla RAG	70.3	65.4	23.0	17.7	55.8	53.4	49.7	45.5
ðĸ	IterDRAG*	74.3	69.1	26.7	19.4	60.5	57.6	53.8	48.7
	AirRAG-Lite	80.6	75.4	35.4	28.9	75.3	73.1	63.8	59.1
	AirRAG	79.6	75.2	41.0	35.0	76.0	74.2	65.6	61.5
	AirRAG-Blender	81.1	79.8	41.6	36.4	82.2	81.7	68.3	66.0
	Vanilla RAG	77.1	72.0	29.0	22.9	60.9	58.1	55.7	51.0
32k	IterDRAG*	77.7	71.6	30.8	22.3	63.0	60.2	57.1	51.4
32K	AirRAG-Lite	82.4	76.9	36.7	30.1	78.8	76.8	66.0	61.3
	AirRAG	82.5	77.4	43.2	36.3	80.4	78.9	68.7	64.2
	AirRAG-Blender	82.9	80.6	43.3	37.6	83.4	83.0	69.9	67.1
	IterDRAG*	76.8	71.0	31.7	24.8	65.5	62.4	58.0	52.7
128k	AirRAG-Lite	82.5	77.1	35.7	30.4	78.3	76.0	65.5	62.2
	AirRAG	83.3	78.0	43.5	36.5	82.3	80.5	69.7	65.0
	AirRAG-Blender	83.7	81.4	43.9	38.5	84.4	84.2	70.6	68.0

Table 3: Overall evaluation results under different computational resource budgets, where *Qwen2.5-14B-Instruct* is used as the generator LLM. * indicates the results reproduced by us. L_{max} denotes the maximum number of input tokens across all rollouts. The best results for each L_{max} are in **bold**. The number of both rollouts and output sequences is set to 1 for our proposed AirRAG methods.

Method	NQ	TriviaQA	PopQA	WebQA	HotpotQA	2Wiki
	EM	EM	F1	EM	F1	F1
Vanilla RAG	35.1	58.8	36.7	15.7	35.3	21.0
Self-RAG	36.4	38.2	32.7	21.9	29.6	25.1
Iter-RetGen	36.8	60.1	37.9	18.2	38.3	21.6
Auto-RAG	37.9	60.9	47.8	25.1	44.9	48.9
AirRAG	53.6	63.2	51.8	52.6	67.6	66.3

Table 4: Performance comparison on six benchmarks, where *Llama3-8B-Instruct* is used as the generator LLM. Partial experimental results are quoted from Jin et al. (2024) and Yu et al. (2024). The best results are in **bold**. The number of both rollouts and output sequences is set to 1. The number of documents for a single retrieval is set to 5. Our proposed AirRAG significantly outperform the others.

L_{\max}	Method	database_size	retrieval_time	retrieval_number	e2e
8k	Vanilla RAG	100w	0.900	1.00	3.828
	IterDRAG	100w	1.833	2.04	6.703
	AirRAG-Lite	100w	2.205	2.25	8.482
	AirRAG	100w	3.453	3.84	12.752

Table 5: Performance analysis of inference efficiency. L_{max} denotes the maximum number of input tokens across all rollouts. The retrieved database contains approximately one million documents. e2e and retrieval_time denote the average total time for a single question-answering process and the time spent on retrieval respectively, measured in seconds. Other inference configurations remain consistent with those in Table 3.



Figure 5: Performance comparison of different verification methods. "QwenRM" is short for reward model trained on the Qwen model. "SA" is the reasoning action of summary and answer. "SC-emb/jcd" are two self-consistency verification methods based on text embeddings and jaccard similarity. "Average" is the average score over all candidate rollouts. The single retrieval process is set to retrieve three documents or fixed 8k context.



Figure 6: Overview of the distribution of query complexity over three multi-hop QA datasets.

better retrieval and answer. This process of RA-QT
or QT-RA can continuously iterate until no new
sub-queries arise or the maximum iteration depth is
reached. Finally, the *summary answer* (SA) in Figure 11 utilizes all the information and conclusions
from intermediate steps to refine the final answer.

E Case Study

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We select a sample from the complex multi-hop
dataset MuSiQue to analyse in detail, as shown in
Figures 13 and 14.



Figure 7: Impact of the retrieved document number scaling and the maximum context length scaling over three datasets.



Figure 8: Performance comparison on the number of different effective rollouts over three datasets. Sampling more diverse reasoning paths consistently improves accuracy.

Example prompt for SAY reasoning action

Given the user query, you may rephrase it for better clarity, summarize it at a higher level, or decompose it into multiple sub-queries to facilitate more effective information retrieval and response generation. If no modification is necessary, return "None". Otherwise, list sub-queries, each on a new line.

<Here are some examples.> Query: {question} Output:

Figure 9: Example prompt for SAY reasoning action.

Example prompt for QT reasoning action

Given the context provided, please determine whether rephrasing, summarization, or decomposition into sub-queries is necessary to enhance the accuracy and efficiency of information retrieval and response generation. If no modification is required, return "None". Subsequent queries should be listed individually.

<Here are some examples.> Main Query: {question} History: {history} This Query: {this_question}

Figure 10: Example prompt for QT reasoning action.

Example Prompt for RA actions

You are an expert in question answering. I am going to give you some contexts with may or may not be relevant to the question. Answer the question according to the contexts. {contexts} Question: {question}

Figure 11: Example Prompt for RA actions.

Example prompt for SA reasoning action

You are an expert in question answering. Given the context, sub-queries and responses, output a correct and concise answer to User Query.

<Here are some examples.> User Query: {question} {history} Contexts: {contexts} Final Answer:

Figure 12: Example prompt for SA reasoning action.

The iterative methods often traps in a solution space

Context: <Retrieved documents>

Question: What is the mouth of watercourse for the body of water where Bartram's Covered Bridge is located? Follow up: Which body of water is Bartram's Covered Bridge located on? Follow up: | Intermediate answer: | So the final answer is:

Output: Follow up: Which body of water is Bartram's Covered Bridge located on?

(Note: The context does not specify which body of water Bartram's Covered Bridge is located on, but it does mention that the bridge carries Goshen Road over Crum Creek. Therefore, we **need to confirm that Crum Creek is the body of water in question before proceeding to find the mouth of the watercourse.**)

• • •

··· (It enters an endless cycle of iteration until it reaches predefined maximum depth.)

Gold Answer: Delaware River

Process Annotation: Q1: Bartram's Covered Bridge » crosses

A1: Crum Creek

Q2: Q1 » mouth of the watercourse

A2: Delaware River

The iterative self-exploration often traps in a solution space with low-quality reasoning steps even after many attempts.

Figure 13: Incorrect reasoning path of iterative RAG methods. Ambiguity or missing information in the intermediate steps leads in duplicate sub-query.

The simple and effective action space of AirRAG leads to the correct reasoning trajectory

Question: What is the mouth of watercourse for the body of water where Bartram's Covered Bridge is located?

Action1: SAY

Input: What is the mouth of watercourse for the body of water where Bartram's Covered Bridge is located? Output: Where is Bartram's Covered Bridge located? What is the mouth of the watercourse for the body of water near Bartram's Covered Bridge?

Action2: RA

Input: <Retrieved documents> Where is Bartram's Covered Bridge located? Output: Bartram's Covered Bridge is located on the border between Delaware County and Chester County, Pennsylvania, carrying Goshen Road over Crum Creek.

Action3: QT

Input: What is the mouth of the watercourse for the body of water near Bartram's Covered Bridge? Output: What is the mouth of Crum Creek?

Action4: RA

Input: <Retrieved documents> What is the mouth of Crum Creek?

Output: Based on the provided contexts, there are two different locations referred to as Crum Creek, and they flow into different bodies of water:

1. The Crum Creek in Delaware County and Chester County, Pennsylvania, flows into the Delaware River in Eddystone, Pennsylvania.

2. The Crum Creek (also called Cathatachua Creek) in East Creek, New York, flows into the Mohawk River. Since the question does not specify which Crum Creek is being referred to, both answers are possible. However, if we consider the first context as the primary reference, the mouth of Crum Creek is the Delaware River in Eddystone, Pennsylvania.

Action5: SA

Input: <Retrieved documents> <Sub-queries with answers> Output: The mouth of the watercourse for the body of water where Bartram's Covered Bridge is located, **Crum Creek**, is the **Delaware River** in Eddystone, Pennsylvania.

Gold Answer: Delaware River.

AirRAG obtains the correct answer by performing five reasoning actions efficiently.

Figure 14: Effective reasoning rollout of AirRAG. The fundamental action space and tree-based search provides greater compatibility and flexibility, which avoids being trapped in a single solution space by a low-quality intermediate step for chain-like reasoning paradigm.