Anonymous Full Paper Submission 34

## **ODI** Abstract

Advances in various technologies and machine learn-002 ing (ML) are transforming the field of remote sensing. 003 This study proposes an ML-centered methodology 004 for classifying coastal terrain in tropical coastal re-005 gions using multispectral unmanned aerial vehicle 006 (UAV) image inputs. The objective is to identify 007 suitable ML algorithms for analyzing multispectral 008 images on limited hardware. Multispectral images 009 of the study area were collected using a DJI Mavic 010 3M UAV in March 2023. K-means clustering was im-011 plemented to assist in coastal terrain identification, 012 and the labeled data were used to train pixel-based 013 014 Support Vector Machine (SVM) and Random Forest (RF) models utilizing a 5-fold block cross-validation 015 scheme. The results showed that the optimized RF 016 model outperformed the SVM model across most 017 metrics. Despite this, the SVM model showed po-018 tential for live image classification due to its smaller 019 size and quick classification speed. Additionally, 020 the optimized models effectively classified images 021 from areas set as an independent hold-out test set, 022 demonstrating the applicability of ML in this type 023 of remote sensing problem. 024

## 025 1 Introduction

Climate change has significantly impacted coastal
ecosystems, leading to their degradation through
rising temperatures, ocean acidification, and urban
encroachment [1]. Given the importance of these
ecosystems for biodiversity and biomass production,
urgent measures are needed to mitigate the effects
of anthropogenic climate change.

Traditional environmental assessment methods 033 rely on on-site teams to collect data on species pop-034 ulations, soil and water quality, and human settle-035 ments, but these methods are labor-intensive and 036 time-consuming. Modern approaches use remote 037 sensing technologies like satellite imagery, multi-038 spectral sensors, and LiDAR, allowing for faster 039 and more accurate environmental monitoring. Un-040 manned aerial vehicles (UAVs) have further en-041 hanced data collection by providing high-resolution 042 images that bridge the gap between satellite data 043 and on-site surveys. Processing this data involves 044

advanced computational techniques, including machine learning algorithms, which facilitate rapid and detailed analysis of environmental conditions. 047

Live image segmentation from UAVs is an ex-048 citing and emerging area of research in machine 049 learning. However, several challenges must be ad-050 dressed to make machine learning viable for live 051 or near-live classification. First, models need to 052 be compact enough to run on limited onboard pro-053 cessing power. They must also offer low-latency 054 performance, as faster classification times are prefer-055 able, and be power-efficient to extend flight duration. 056 Additionally, the model may need to share onboard 057 resources with image preprocessing tasks, such as 058 correcting for image warping or other artifacts [2, 059 3]. Suitable hardware options for this task include 060 devices like the Arduino Portenta H7, ESP32-CAM, 061 and Raspberry Pi Zero 2 W, which offer memory 062 capacities of 16 MB, 4 MB, and support for an SD 063 card, along with RAM sizes of 8 MB, 4 MB, and 064 512 MB, respectively [4–6]. 065

In the context of traditional ML approaches to 066 object-based and pixel-based classification, Support 067 Vector Machine (SVMs) and Random Forests (RFs) 068 are among the most popular for use in remote sens-069 ing as powerful machine learning algorithms with 070 distinct strengths and weaknesses [7–9]. SVMs ex-071 cel in high-dimensional spaces where the number of 072 features exceeds the number of samples and robust 073 to overfitting, especially in cases where the data is 074 sparse [10]. However, they can be computationally 075 intensive, particularly with large problem sizes, and 076 their performance relies heavily on the careful tun-077 ing of hyperparameters, which often involves tedious 078 and time-consuming experimentation and iterative 079 adjustments [11]. 080

On the other hand, RFs are versatile and easy 081 to implement, providing good performance across a 082 wide range of datasets without much need for tuning 083 [12]. They handle large datasets efficiently and are 084 capable of capturing complex interactions between 085 features. However, RFs can sometimes struggle with 086 overfitting, particularly if the number of trees is not 087 sufficiently large, and they can be less effective than 088 SVMs in very high-dimensional spaces. Additionally, 089 RFs tend to require more computational resources 090 as the number of trees grows. 091

120

# <sup>092</sup> 2 Methodology

## 093 2.1 Data Collection

The study was conducted in an 8-hectare area, West 094 of the municipality of Lian, Batangas province of 095 the Philippines. The inland region consists of un-096 even ground covered by various mangroves, bushes, 097 and grasses. This transitions into a shallow sandbar 098 that extends about 150 meters westward into the sea. 099 Within this area, there are patches of aquatic vegeta-100 tion and mangroves before the landscape changes to 101 a deeper and rockier region. The dataset analyzed 102 103 in the present study was obtained through a single aerial survey campaign in March 2023 that began 104 at noon. The weather on the day was fair with little 105 cloud coverage. 106

The UAV used for data acquisition was the DJI 107 Mavic 3M, manufactured by SZ DJI Technology Co., 108 Ltd., based in Shenzhen, China. It is equipped with 109 a high-resolution 4K RGB alongside a multispectral 110 camera. The imaging capability of the UAV encom-111 passes a wide spectrum of wavelengths, including 112 Green (560  $\pm$  16 nm), Red (650  $\pm$  16 nm), Red 113 Edge (730  $\pm$  16 nm), and Near-Infrared (860  $\pm$  26 114 nm), enabling the detailed capture of vegetative and 115 geographical features with high spectral resolution 116 [13]. Each pixel within the image corresponds to a 117 spatial resolution of 2 cm, thereby facilitating the 118 extraction of detailed information at a fine scale. 119



Figure 1. Orthomosaic of the region of interest.

## 2.2 Data Processing

The images that were captured were combined to 121 create orthomosaics through the use of onboard soft-122 ware. These orthomosaics encompass various maps 123 such as RGB, Normalized Difference Vegetation In-124 dex (NDVI), Green Normalized Difference Index 125 (GNDVI), Normalized Difference Red Edge (NDRE), 126 and Leaf Chlorophyll Index (LCI). The constructed 127 orthomosaic was just under 50,000,000 pixels large. 128 Subsequent data operations were carried out using 129 the multispectral vegetation index (VI) and the mul-130 tispectral images instead of the RGB images. The 131 unsupervised and supervised algorithms were both 132 implemented using Python. 133

All machine learning model training and testing 134 was conducted using the free tier of Google Colab, 135 which featured 12.7 GB of RAM [14]. This resource 136 limitation played a significant role in determining 137 the final optimized model. In addition to tradi-138 tional metrics such as accuracy, precision, recall, 139 and F1-score, training times also factored into the 140 decision-making process: in cases where two models 141 demonstrated comparable performance, the model 142 with the shorter training time was chosen. 143

### 2.3 Definition of Training Labels 144

Features were identified by implementing k-means 145 clustering on each of the VIs from k = 2 to k = 8. 146 A mini-batch algorithm was chosen to reduce the 147 computation time. Each combination of a VI and 148 the k number of clusters was assessed to determine 149 possible terrain types. This assessment was based on 150 both the cluster's silhouette score and a qualitative 151 comparison to the cluster's corresponding region in 152 the RGB image. These were then associated with 153 a terrain type in the image such as "terrestrial veg-154 etation" or "sublittoral zone". The training labels 155 on pixels were then manually adjusted and reas-156 signed to resolve overlaps between clusters or to 157 align them with the correct terrain type based on 158 domain experts. 159

The silhouette score is a metric used to measure 160 the quality of clusters in a clustering algorithm. It 161 provides an indication of how well each data point 162 lies within its cluster relative to other clusters [15]. 163 The resulting value ranges from -1 to 1, where a value 164 close to 1 indicates that the point is well clustered, 165 with the data point being much closer to points in 166 its own cluster than to points in other clusters. A 167 value close to 0 indicates that the point lies on the 168 boundary between clusters, while negative values 169 suggest that the point may have been assigned to the 170 wrong cluster [16]. By averaging the silhouette coef-171 ficients of all points in a dataset, one can obtain an 172 overall measure of cluster quality, where higher aver-173 age silhouette scores simply better-defined and more 174

 $\mathbf{2.4}$ 

181

175 distinct clusters. It is mathematically expressed as

$$s_i = \frac{b_i - a_i}{\max(a_i, b_i)} \tag{1}$$

where for a data point i,  $a_i$  denotes the distance between a data point and its assigned centroid while  $b_i$  denotes the distance to the closest centroid belonging to a different cluster. Through the unique combinations of k and the VIs, 182 6 terrain classes were identified as seen in Figure 183 3. NDRE clustered with k = 2 was used to identify 184 class 0, the "sublittoral zone". This corresponds to 185 the deeper submerged areas of the image. In these 186 regions, further features are difficult to isolate due 187

**Coastal Terrain Identification** 







**Figure 2.** Graphical representation of feature extraction through implementing k-means clustering on VIs (top) and machine learning pipeline using hold-out test set and a block k-folds cross-validation scheme with grid search hyperparameter optimization (bottom).

246

to the depth of the water.

LCI clustered with k = 5 was then used to identify classes 1 and 2, "shallow water" and "shallow bare zone" respectively. The "shallow water" cluster represents areas with shallow water and some algal content, while the "shallow bare zone" refers to submerged areas without significant photosynthetic activity.

NDVI clustered with k = 4 was used to detect class 3, the "terrestrial vegetation". It consists of trees, bushes, and grasses.

GNDVI clustered with k = 2 was used to isolate class 4, labeled "bare land". This refers to regions on the land with little to no vegetation.

Lastly, GNDVI clustered with k = 5 was used to isolate class 5, "shadows and rocks" cluster. This is a region where labeling is challenging due to shadows cast by tree canopies or the presence of rocks.



**Figure 3.** Identified classes from k-means clustering. These six classes encompass the terrain types found.

## 206 2.5 Implementation

SVM and RF models were trained on the layered 207 multispectral bands. These were chosen as the model 208 inputs as VIs require processing and context of the 209 larger image to effectively normalize values whereas 210 model's trained directly on the multispectral bands 211 will be able to classify immediate instances taken 212 by the multispectral camera. Hyperparameters were 213 optimized using a Grid search approach. Grid search 214 finds the optimized hyperparameters of an algorithm 215 using a specified list of values for each hyperparam-216 eter. A model is then trained for every possible 217 combination of hyperparameters with the optimized 218 model resulting from the combination that yielded 219 the highest F1-Score. This metric was chosen as 220 the primary metric as it accounts for the misclas-221 sification of minority classes that may be under-222 represented due to the proportion of labels in the 223 image. 224

A 5-fold block cross-validation with a separate hold-out test set was used to validate the model. The image was first separated into a training-validation 227 set in the North with the rest being separated as a 228 hold-out test set as can be seen in Figure 2. The 229 training-validation set was then divided into 34 im- 230 age blocks equivalent to a 20x20 meter area each. 231 These blocks are then distributed between an n num-232 ber of subsets or folds. The model is then trained 233 on the n-1 folds of data with the remaining fold 234 being used as a validation set. The process is then 235 repeated, cycling through the various possible val-236 idation folds. These results are then averaged to 237 provide an understanding of the performance of the 238 particular model [17]. In the particular case of a 239 5-fold cross-validation scheme, 80% of blocks at any 240 given time are used as the training data while 20%241 remains for validation. This is then cycled such 242 that all subsets of 20% are used for validation of the 243 model's performance. 244

# 3 Results 245

# 3.1 Machine-Labeled Maps



Figure 4. Comparison of machine-labeled maps. Shallow bare zones are more prevalent in the machine-labeled maps as compared to the training labels.

Displayed in Figure 4 are the terrain type maps 247 generated by the trained SVM and RF models. Upon 248 initial visual inspection, it was seen that both models 249 were able to label the image similar to the training 250 image. As seen in the figure, shallow water rep-251 resents the majority of the image with sublittoral 252 zone, shallow bare zones, terrestrial vegetation, and 253 bare land being smaller classes of similar size. As ex-254 pected, the shadows and rocks is seen as the smallest 255 NLDL

#34

256

However, some immediate differences are obvious 257 between the machine-labeled maps and the training 258 labels. Both machine learning models appear to 259 assign pixels to the shallow bare zone terrain type 260 at a rate higher than the training labels. These 261 manifest as more spread out throughout the image 262 as opposed to the tighter concentrations found in the 263 training labels. A second observation is the spread 264 of the shadows and rocks clusters in the SVM-map 265 being much more prevalent along the coastline as 266 opposed to the training map and RF-labeled map. 267

### Discussion 4 268

#### **Experiments with Forests** 4.1269

For the purposes of minimizing file size and training 270 time in RF models, particularly close attention was 271 given to the number of trees and the maximum 272 depth of trees in the models. Training time was 273 seen to increase linearly with both the number of 274 trees and the maximum depth of the trees. Between 275 these two, the maximum depth of trees was the more 276 important factor in determining model performance. 277 The final hyperparameters chosen for the random 278 forest model reflect a sparse forest of only 20 trees 279

with a depth of 30. Forests with a greater number 280 of trees only a minor amount of improvement in 281 the validation set while extending training by many 282 more minutes. 283

### **Optimized Models** 4.2284

Table 1. SVM classification report on the independent test set. Generally good performance across terrestrial terrain types and the sublittoral zone.

SVM Accuracy: 0.85	Precision	Recall	F1-Score
Sublittoral Zone	0.91	0.98	0.94
Shallow Water	0.90	0.82	0.86
Shallow Bare Zones	0.78	0.77	0.78
Terrestrial Vegetation	0.95	0.97	0.96
Bare Land	0.88	0.92	0.90
Shadows and Rocks	0.20	0.33	0.25
Macro Average	0.77	0.80	0.78
Weighted Average	0.86	0.85	0.85

The SVM model performed relatively well with 285 an accuracy of 0.85. When taking their weighted 286 average (that is the average of each metric weighted 287 by its number of samples) the Precision, Recall, and 288 F1 scores across all classes are 0.86, 0.85, and 0.85 289 respectively. These scores drop when considering 290 the macro average which considers the scores of each 291 class as being of equal weight. Using this method 292 of averaging, the scores drop to 0.77, 0.80, and 0.78 293

suggesting that there is a higher incidence of false 294 negatives with the model. 295

Looking into the individual metrics per class, we 296 see that the model's performance in identifying the 297 sublittoral zone, shallow water, terrestrial vegeta-298 tion, and bare land classes is good. However, there 299 is a high rate of false negatives in the shallow bare 300 zone and shadows and rocks regions with their Recall 301 scores being only 0.77 and 0.33 respectively. 302



Figure 5. SVM confusion matrix on the independent test set. Minor misclassification observed between the "shallow water" and "shallow bare zones" with heavy misclassification in "shadows and rocks".

Referring to the SVM model's confusion matrix 303 in Figure 5., it is seen that the sublittoral zone, ter-304 restrial vegetation, and bare land terrain types are 305 accurately classified. However, the shallow water 306 and shallow bare zones offer a challenge being com-307 monly mistaken for each other resulting in correct 308 predictions only 82.26% and 77.23% of the time and 309 misclassification of shallow water for shallow bare 310 zones at 7.65% with the reverse occurring more often 311 at 16.85%. The most prevalent case of erroneous 312 classification manifests in the shadows and rocks 313 cluster with only 32.96% of the true labels being cor-314 rectly predicted thereby underscoring the challenges 315 in classifying this terrain type. This can be explained 316 by this terrain type's presence in both aquatic and 317 terrestrial portion of the image as reflected by the 318 25.45% misclassification into the shallow bare zones 319 and 32.53% in the bare land. 320

The RF model exhibited superior performance 321 compared to the SVM model, achieving an accu-322 racy of 0.98. Furthermore, it demonstrated strong 323 performance across all metrics in both macro and 324 weighted averages. Upon analyzing its performance 325 within each class, it maintained high accuracy for 326 shallow water, shallow bare zones, terrestrial vege-327 tation, bare land, and shadows and rocks. The only 328 exception was the shallow bare zones and shadows 329 NLDL

#34

and rocks, which exhibited a small amount of mis-

classification, indicated by a Precision score of 0.94.

Nonetheless, the overall performance of the model

remained commendable.

**Table 2.** RF classification report on the independent test set. Minor errors in "shallow water" and "shadows and rocks".

RF Accuracy: 0.98	Precision	Recall	F1-Score
Sublittoral Zone	0.99	0.98	0.99
Shallow Water	0.99	0.97	0.98
Shallow Bare Zones	0.94	0.99	0.96
Terrestrial Vegetation	0.99	0.99	0.99
Bare Land	0.98	0.99	0.98
Shadows and Rocks	0.89	0.99	0.93
Macro Average	0.96	0.98	0.97
Weighted Average	0.98	0.98	0.98

Referring once again to the model's correspond-334 ing confusion, it is observed that in nearly all of 335 the classes, the majority of pixels lies along the di-336 agonal with no misclassification exceeding 2.5% of 337 pixels. The RF model largely prevents the frequent 338 misclassification of shallow bare zones as shallow 339 water, which is observed in the SVM model. This 340 performance may be explained by the depth of the 341 RF model with the large number of splits allowing it 342 to classify well. This along with the smaller number 343 of trees in the forest, this may hurt the RF model's 344 ability to generalize to other data. 345



Figure 6. RF confusion matrix on the independent test set. Excellent performance is observed across all classes.

Some aspects in which the SVM model has clear 346 advantages over the RF in regards to prediction 347 time, and file size which are important factors to 348 consider of live image classification. The training 349 of the SVM model took 20 minutes to train and 350 was able to classify the test set in as fast as 0.51351 seconds. Besides this, its minimal file size of 1.28 352 Kilobytes allows it to be utilized by microcontroller 353

devices such as the Arduino line of microcontrollers 354 which have minimal storage space. This opens up 355 the possibility for live image prediction. In reality, 356 a real-time imaging system would take in images 357 smaller than those used in the test set thus having a 358 quicker effective classification time. In comparison, 359 the RF model trains slower needing nearly an hour 360 to train and falls behind in other metrics with a 361 prediction time 10 times longer than the SVM and a 362 file size three and a half orders of magnitude larger. 363 Though the prediction time of the RF model may 364 still be considered usable in some cases, the model 365 is best suited to accurate post-processing in which 366 file size and prediction time are not much of a con-367 cern. It would be likely of the three microcontrollers 368 mentioned in this work's introduction that the SVM 369 would be usable on all three whereas the RF model 370 would only likely find success when implemented on 371 the Raspberry Pi. Listed in Table 3. is a summary 372 of the major differences between the two models. 373

**Table 3.** Summary of differences between optimized SVM and RF models. RF is suited for post processing, SVM shows potential for live classification tasks.

	$\mathbf{SVM}$	$\mathbf{RF}$
Accuracy	0.85	0.98
Precision (Macro)	0.86	0.92
Recall (Macro)	0.85	0.91
F1-Score (Macro)	0.85	0.91
Training Time $(s)$	1259	3244
Prediction Time (s)	0.51	4.957
File Size (KB)	1.28	1890

# 5 Conclusion

374

This study demonstrates the effectiveness of ML 375 methodologies in classifying coastal terrain using 376 multispectral images captured by a UAV in tropical 377 coastal regions. By implementing K-means clus-378 tering for initial terrain identification and training 379 SVM and RF models, the research identified RF 380 as the superior model for this application, outper-381 forming SVM across most metrics. Despite this, 382 the optimized SVM model showed promise for live 383 classification due to its smaller size and quicker pre-384 diction time. The successful classification of images 385 from areas in the test set underscores the further 386 applicability of ML techniques in remote sensing. 387 These findings reinforce RF models in providing 388 robust ML frameworks for accurate classification. 389 At the same time, SVMs are seen to have poten-390 tial in terrain classification in resource-constrained 391 environments. Future research could explore the 392 application of these methods to other geographic 393 regions and further optimize the models for broader 394

<sup>395</sup> use in remote sensing.

## **References**

- T. Wernberg, S. Bennett, R. C. Babcock, T. [1]397 398 de Bettignies, K. Cure, M. Depczynski, F. Dufois, J. Fromont, C. J. Fulton, R. K. Hovey, 399 E. S. Harvey, T. H. Holmes, G. A. Kendrick, B. 400 Radford, J. Santana-Garcon, B. J. Saunders, 401 D. A. Smale, M. S. Thomsen, C. A. Tuck-402 ett, F. Tuya, M. A. Vanderklift, and S. Wil-403 son. "Climate-driven regime shift of a temper-404 ate marine ecosystem". In: Science 353.6295 405 (2016), pp. 169–172. DOI: 10.1126/science. 406 aad8745. eprint: https://www.science.org/ 407 doi/pdf/10.1126/science.aad8745. URL: 408 409 https://www.science.org/doi/abs/10. 1126/science.aad8745. 410
- H. C. Baykara, E. Bıyık, G. Gül, D. Onural,  $\left|2\right|$ 411 A. S. Oztürk, and I. Yıldız. "Real-Time De-412 tection, Tracking and Classification of Mul-413 tiple Moving Objects in UAV Videos". In: 414 2017 IEEE 29th International Conference 415 on Tools with Artificial Intelligence (ICTAI). 416 2017, pp. 945–950. doi: 10.1109/ICTAI.2017. 417 00145. 418
- [3] Z. Cao, L. Kooistra, W. Wang, L. Guo, and J. Valente. "Real-Time Object Detection Based on UAV Remote Sensing: A Systematic Literature Review". In: *Drones* 7.10 (2023). ISSN: 2504-446X. DOI: 10.3390/drones7100620.
  URL: https://www.mdpi.com/2504-446X/7/ 10/620.
- 426 [4] Arduino Portenta H7. https://www.arduino.
  427 cc/pro/hardware/product/portenta-h7.
  428 Accessed: 2024-10-25. Arduino, 2024.
- 429 [5] ESP32-CAM. https://www.espressif.com/
  430 en/products/devkits/esp32-cam. Accessed:
  431 2024-10-25. Espressif Systems, 2024.
- 432 [6] Raspberry Pi Zero 2 W. https://www.
  433 raspberrypi.com/products/raspberry434 pi-zero-2-w/. Accessed: 2024-10-25. Rasp435 berry Pi Foundation, 2024.
- [7] S. Bhatnagar, L. Gill, and B. Ghosh. "Drone Image Segmentation Using Machine and Deep Learning for Mapping Raised Bog Vegetation Communities". In: *Remote Sensing* 12.16 (2020). ISSN: 2072-4292. DOI: 10.3390 / rs12162602. URL: https://www.mdpi.com/ 2072-4292/12/16/2602.
- [8] L. W. Tait, S. Orchard, and D. R. Schiel.
  "Missing the Forest and the Trees: Utility, Limits and Caveats for Drone Imaging of Coastal Marine Ecosystems". In: *Remote Sensing* 13.16 (2021). DOI: 10.3390/rs13163136.

URL: https://www.mdpi.com/2072-4292/ 448 13/16/3136. 449

- H. G. Olariu, L. Malambo, S. C. Popescu, [9] 450 C. Virgil, and B. P. Wilcox. "Woody Plant 451 Encroachment: Evaluating Methodologies for 452 Semiarid Woody Species Classification from 453 Drone Images". In: Remote Sensing 14.7 454 (2022). DOI: 10.3390 / rs14071665. URL: 455 https://www.mdpi.com/2072-4292/14/ 456 7/1665. 457
- [10] V. Chauhan, K. Dahiya, and A. Sharma. 458
  "Problem formulations and solvers in linear 459
  SVM: a review". In: Artificial Intelligence Re- 460
  view 52 (2019), pp. 803-855. DOI: 10.1007/461
  s10462-018-9614-6. URL: https://doi.462
  org/10.1007/s10462-018-9614-6. 463
- [11] A. Abdiansah and R. Wardoyo. "Time complexity analysis of support vector machines 465 (SVM) in LibSVM". In: Int. J. Comput. Appl 466 128.3 (2015), pp. 28–34. 467
- M. Belgiu and L. Drăguţ. "Random forest in 468 remote sensing: A review of applications and 469 future directions". In: *ISPRS Journal of Pho-* 470 *togrammetry and Remote Sensing* 114 (2016), 471 pp. 24–31. ISSN: 0924-2716. DOI: https://doi. 472 org/10.1016/j.isprsjprs.2016.01.011. 473 URL: https://www.sciencedirect.com/ 474 science/article/pii/S0924271616000265. 475
- SZ DJI Technology Co., Ltd. DJI Mavic 3M 476 Unmanned Aerial Vehicle (UAV). https:// 477 ag.dji.com/mavic-3-m/specs. [Apparatus]. 478 Shenzhen, China, 2023. 479
- [14] Google Research. Google Colaboratory. https: 480
   //colab.research.google.com/. Accessed: 481
   2024-08-30. 2024.
   482
- M. Shutaywi and N. N. Kachouie. "Silhouette Analysis for Performance Evaluation in Machine Learning with Applications to Clustering". In: Entropy 23.6 (2021). ISSN: 1099-4300. DOI: 10.3390/e23060759. URL: https: //www.mdpi.com/1099-4300/23/6/759.
- [16] K. R. Shahapure and C. Nicholas. "Cluster 489 Quality Analysis Using Silhouette Score". In: 490 2020 IEEE 7th International Conference on 491 Data Science and Advanced Analytics (DSAA). 492 2020, pp. 747–748. DOI: 10.1109/DSAA49011. 493 2020.00096. 494
- T.-T. Wong and P.-Y. Yeh. "Reliable Accuracy 495 Estimates from k-Fold Cross Validation". In: 496 *IEEE Transactions on Knowledge and Data* 497 *Engineering* 32.8 (2020), pp. 1586–1594. DOI: 498 10.1109/TKDE.2019.2912815. 499