MATCH: <u>Multi-faceted Adaptive Topo-Consistency</u> for Semi-Supervised <u>Histopathology Segmentation</u>

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Abstract

In semi-supervised segmentation, capturing meaningful semantic structures from unlabeled data is essential. This is particularly challenging in histopathology image analysis, where objects are densely distributed. To address this issue, we propose a semi-supervised segmentation framework designed to robustly identify and preserve relevant topological features. Our method leverages multiple perturbed predictions obtained through stochastic dropouts and temporal training snapshots, enforcing topological consistency across these varied outputs. This consistency mechanism helps distinguish biologically meaningful structures from transient and noisy artifacts. A key challenge in this process is to accurately match the corresponding topological features across the predictions in the absence of ground truth. To overcome this, we introduce a novel matching strategy that integrates spatial overlap with global structural alignment, minimizing discrepancies among predictions. Extensive experiments demonstrate that our approach effectively reduces topological errors, resulting in more robust and accurate segmentations essential for reliable downstream analysis. Code is available at https://github.com/Melon-Xu/MATCH.

1 Introduction

Accurate segmentation of glands and nuclei in histopathology images is critical for digital pathology, significantly influencing diagnosis, prognosis, and treatment planning by enabling precise quantification of morphological and structural tissue features [8, 43, 27]. Numerous fully-supervised segmentation methods [49, 85, 11, 12, 25, 17, 41, 18] have demonstrated substantial success. However, densely distributed cellular structures in histopathology images often induce topological errors, including false merges or splits, severely impacting clinical reliability. Additionally, fully supervised methods demand extensive annotated datasets, which are costly, time-consuming, and not scalable [53, 32]. This limitation motivates exploring semi-supervised learning (SSL) strategies capable of leveraging abundant unlabeled data alongside limited annotations.

Recent SSL approaches have significantly enhanced segmentation accuracy in contexts of limited supervision [79, 55, 37–39, 64, 78, 81, 77, 82, 1, 83, 76, 30, 84, 73, 74, 45]. Nevertheless, these methods typically do not explicitly target topological errors, resulting in seemingly small segmentation errors with consequential significant topological inaccuracies that affect segmentation robustness. To explicitly address topological errors, persistent homology [7] offers a rigorous mathematical framework that captures and characterizes topological features, such as connected components and loops in data across multiple scales. The output, persistence diagram, summarizes these structures as dots in a 2D diagram. For each dot, the coordinate difference (y - x) captures the *persistence* of the

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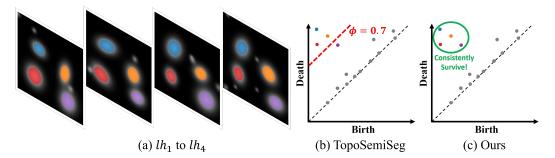


Figure 1: Intuition of the proposed framework. (a) Colored likelihood maps are coming from the MC dropout. Connected components consistently matched in at least three predictions retain identical colors across instances, indicating topological stability; components shown in grey fail to reach this consensus and are therefore treated as topologically transient. (b) Limitation of TopoSemiSeg [69], which relies on a fixed persistence threshold ($\phi=0.7$, red dashed line) and therefore overlooks less-persistent yet meaningful structures (e.g. the violet point). (c) Our method adaptively identifies relevant topological structures without the need for human-selected thresholds.

topological structure across scales. Building upon this mathematical foundation, TopoSemiSeg [69] introduces topology-aware constraints into SSL frameworks, utilizing persistent homology to enforce topological consistency between teacher and student model predictions. Despite its effectiveness, TopoSemiSeg mainly relies on a predefined, hand-picked persistence threshold to identify meaningful topological structures. Such fixed thresholds are not data-driven, potentially biased, and can exclude relevant structures or retain irrelevant ones, as shown in Figure 1.

To address this issue, we investigate how to identify reliable topological structures from model predictions in a robust and adaptive manner, and enforce model consistency over these structures. We first revisit the fundamental principles of semi-supervised learning – robustness against perturbations. For an image without a training label, to identify reliable information, semi-supervised approaches typically add perturbations at the input level (i.e., augmentation) and at the model level (i.e., Monte Carlo Dropout). Pixel-level predictions that persist across these perturbations are considered reliable and used to self-supervise the model.

Our main idea is to tightly couple this SSL robustness-against-perturbation principle with topological reasoning. Moving beyond pixel-level, we identify topological structures that persist across different perturbations. These structures are considered reliable and used to self-supervise the model. This idea avoids a hand-picked threshold to determine reliable topological structures, and adaptively identifies truly relevant structures to enhance the model's topological reasoning power in an SSL setting.

Building on this idea, we propose a novel SSL segmentation framework employing **dual-level topological consistency**. Our method identifies significant topological features by examining predictions generated with different model perturbations. We formulate the structure correspondence task as a contrastive learning problem, distinguishing stable features, i.e., those consistently detected across multiple predictions, from transient or noisy structures. To identify the stable topological structures, we introduce an advanced matching algorithm that integrates spatial overlap, topological persistence, and spatial proximity criteria to associate topological structures across diverse predictions reliably.

As for perturbations, we propose to employ Monte Carlo (MC) dropout perturbations [9]. Meanwhile, we stress the importance of a temporal view of SSL. Previous works, such as [33, 36, 35, 51], demonstrate that evaluating the predictions in different training snapshots can reveal informative signals for robust prediction. Inspired by this, we propose to also compare topological structures across model snapshots at different training epochs. By explicitly optimizing for dual-level topological consistency, our framework enhances structural coherence within the student model without relying on extensive pixel-wise annotations. Our key contributions can be summarized as follows:

- We propose a novel integration of topological reasoning into the semi-supervised segmentation framework to robustly identify and preserve meaningful topological structures.
- We introduce dual-level topological consistency, measuring structural stability from intra-perturbed predictions (MC dropout) and temporal training snapshots, to effectively utilize unlabeled data.

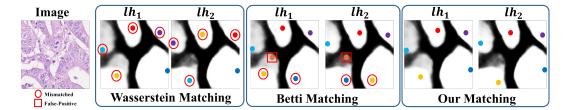


Figure 2: Comparison of our matching with Betti Matching [56] and Wasserstein Matching [21]. We match two likelihood maps obtained from the same input histopathology patch. The birth critical points of the matched pairs are highlighted in the same color. Note that Wasserstein Matching gets most matches wrong, and Betti Matching also gets two matches wrong while pairing biologically unrelated features when lacking the guidance of the ground truth.

• We develop a novel matching algorithm that integrates spatial overlap, topological persistence, and spatial proximity to accurately match topological structures across predictions.

Through extensive experiments on three widely used histopathology image datasets, our method significantly improves the topological accuracy while achieving comparable pixel-wise performance with limited annotations.

2 Related Works

Segmentation with Limited Supervision. Semi-supervised learning enhances medical image segmentation by effectively utilizing limited labeled data together with abundant unlabeled data. Consistency regularization approaches, such as the Mean Teacher model [57], ensure stable segmentation despite input variations [57, 37, 62, 46, 69]. Pseudo-labeling progressively improves accuracy by leveraging confident model predictions on unlabeled data [75, 50, 82]. Adversarial training aligns segmentation outputs from labeled and unlabeled datasets using discriminator networks [24, 34]. Additionally, uncertainty estimation methods such as MC dropout and Bayesian neural networks enhance reliability by effectively handling uncertainty during pseudo-label generation [9, 79, 44, 39, 70], while entropy minimization is used to reduce prediction uncertainty [13, 3, 66]. Contrastive learning strengthens segmentation robustness by training models to differentiate similarities and distinctions among data pairs, thereby boosting overall segmentation quality [78, 1, 77, 76].

Topology-Aware Image Segmentation. Topology-aware methods have been proposed to enforce correct topology, like connectivity or correct counts in segmentation tasks [21, 23, 52, 5, 71, 72, 20, 15, 61, 56, 60, 68, 80, 40]. These methods typically use differentiable loss functions derived from topological data analysis tools, including persistent homology [21, 5, 56], discrete Morse theory [23, 22, 16], topological interactions [15, 2], homotopy warping [20], centerline-based comparisons [52, 61]. These methods generally rely heavily on precisely annotated labels. Xu *et al.* [69] propose TopoSemiSeg to combine SSL with topological constraints. Classical persistent homology-based segmentation methods rely on Wasserstein matching [21, 69], which compares persistence diagrams based solely on feature lifespans. However, this approach may produce ambiguous or incorrect correspondences, as illustrated in Figure 2. To alleviate spatial inconsistencies, several methods were proposed [56, 63]. Betti Matching [56] embeds predictions and ground truth into a shared super-level filtration, ensuring alignment only among overlapping topological features. However, as shown Figure 2, it cannot ensure fully correct matching when the ground truth is missing and is too sensitive to preserve some transient structures. Our proposed MATCH-Pair could achieve almost completely accurate matching without the ground truth.

3 Methodology

The motivation of our proposed framework is to identify meaningful topological structures directly from perturbed predictions without the ground truth. The main challenge is to accurately match corresponding topological structures across multi-facet predictions that often contain substantial noise and variability. To overcome this challenge, we introduce MATCH-Pair, a pairwise matching

algorithm, and MATCH-Global, an extended global matching algorithm, to robustly identify stable structures across multiple predictions. Building upon these matching algorithms, we propose dual-level topological consistency constraints: intra-topological consistency, enforcing consistency across multiple stochastic predictions, and temporal-topological consistency, ensuring stability across consecutive training snapshots. These consistency constraints directly optimize the student model, enabling it to learn robust segmentation representations from limited labeled data.

Our method overview is shown in Figure 3. The proposed MATCH framework leverages labeled data via supervised loss and unlabeled data through pixel-wise and dual-level topological consistency.

In this section, we will start by introducing the preliminaries of classic SSL. Next, we will use 3 subsections to introduce MATCH-Pair, MATCH-Global, and the dual-level topological consistency.

Preliminaries: SSL training. We address the semi-supervised image segmentation problem by leveraging a teacher-student framework, a widely adopted paradigm in semi-supervised learning [57]. Let $\mathcal{D}_L = \{(x_i^L, y_i^L)\}_{i=1}^{N_L}$ denote the labeled dataset, where x_i^L represents the input image and $y_i^L \in \{0,1\}^{H \times W}$ is the corresponding pixel-wise annotation. Let $\mathcal{D}_U = \{x_j^U\}_{j=1}^{N_U}$ denote the unlabeled dataset. In our setting, the number of labeled samples is significantly smaller than the number of unlabeled samples, i.e., $N_L \ll N_U$. Our objective is to train a segmentation model f_θ , parameterized by θ , that accurately predicts segmentation masks using labeled and unlabeled data.

In this framework, the student model f_{θ_s} is trained using both supervised and unsupervised losses, while the teacher model f_{θ_t} provides stable targets for the student by being updated as an exponential moving average (EMA) of the student's parameters: $\theta_t^{(\tau+1)} = \alpha \theta_t^{(\tau)} + (1-\alpha)\theta_s^{(\tau+1)}$, where α controls the update rate. For the supervised loss on labeled data, we employ a combination of Dice loss and cross-entropy loss to capture both overlap and pixel-wise discrepancies, $\mathcal{L}_{\text{sup}} = \mathcal{L}_{\text{Dice}}(f_{\theta_s}(x^L), y^L) + \mathcal{L}_{\text{CE}}(f_{\theta_s}(x^L), y^L)$.

To leverage the unlabeled data, we enforce consistency between the student and teacher predictions. Specifically, the student receives a strongly augmented version of an unlabeled image x^U , while the teacher processes a weakly augmented version. The pixel-wise consistency loss is defined as the cross-entropy between the student and teacher outputs, $\mathcal{L}_{\text{cons}} = \mathcal{L}_{\text{CE}}(f_{\theta_s}(\mathcal{A}_s(x^U)), f_{\theta_t}(\mathcal{A}_w(x^U)))$, where \mathcal{A}_s and \mathcal{A}_w denote strong and weak augmentations, respectively.

3.1 MATCH-Pair: Spatial-Aware Pairwise Matching

Accurate identification of corresponding topological structures between the likelihood maps is crucial for robust histopathology image segmentation. We employ persistent homology with a **super-level set filtration** to extract 0-D topological features from likelihood maps, producing persistence diagrams that characterize each component by its persistence and critical points. To find correspondence between different persistence diagrams, traditional methods based on Wasserstein distance emphasize topological persistence without considering spatial relationships, often leading to incorrect associations between spatially distant yet similarly persistent features. In contrast, approaches based solely on spatial overlap tend to match transient structures of minimal significance incorrectly. To address these limitations, we propose MATCH-Pair, a Hungarian overlap-matching algorithm that integrates spatial overlap, topological persistence, and spatial proximity. The overall pipeline is depicted in Figure 4.

Given two likelihood maps $lh_1, lh_2 \in [0,1]^{H \times W}$, which are the softmax-activated outputs of the final UNet layer, we compute the persistence diagrams: $\mathrm{Dgm}(lh_k) = \{(b_i, d_i), k \in \{1,2\} \text{ with the persistence pers}_i = |d_i - b_i|$. Each persistence pair (b_i, d_i) yields a connected spatial region M_i , defined by flood-fill algorithm [54]. This algorithm generates a binary mask M_i starting from the birth pixel b_i . The region is expanded iteratively to neighboring pixels, provided that their likelihood exceeds the threshold $1 - d_i$.

To compute the relative significance of each structure, the persistence values are normalized to derive a weighting factor: $w_{k,i} = \frac{\operatorname{pers}_{k,i}}{\max \operatorname{pers}_{k,j}}, \quad k \in \{1,2\}.$ Here, i and j index the topological features

from the 1_{st} and 2_{nd} persistence diagrams respectively, where $i \in 1,...,n_1$ and $j \in 1,...,n_2$ with n_1 and n_2 being the number of features in each diagram. k distinguishes between the two likelihood maps being compared. The notation $w_{k,i}$ refers to the normalized persistence weight of the i-th topological feature in the k-th likelihood map.

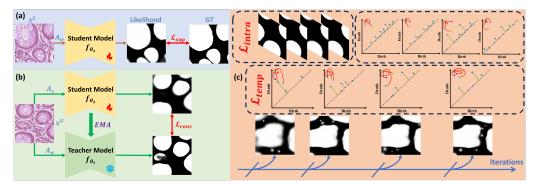


Figure 3: Overview of the proposed MATCH framework with dual-level topological consistency. Note that the \mathcal{L}_{intra} and \mathcal{L}_{temp} are used to directly optimize the parameters of the student model.

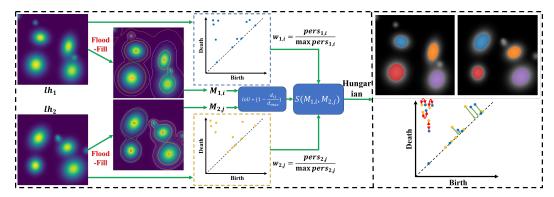


Figure 4: Pipeline of the MATCH-Pair algorithm between two persistence diagrams.

To evaluate the similarity between spatial masks $M_{1,i}$ and $M_{2,j}$, a combined metric that integrates spatial overlap, normalized persistence weights, and spatial proximity is defined as:

$$S_{ij} = w_{1,i} \, w_{2,j} \frac{|M_{1,i} \cap M_{2,j}|}{|M_{1,i} \cup M_{2,j}|} \left(1 - \frac{d_{ij}}{d_{\text{max}}}\right)$$

where d_{ij} is the Euclidean distance between birth critical points of the corresponding masks, and d_{max} denotes the maximum distance among all mask pairs. This similarity metric ensures the prioritization of spatially close, persistent, and well-overlapping structures.

A global one-to-one assignment between features from the two maps is obtained via the Hungarian algorithm [31], minimizing the cost (defined as the complement of similarity):

$$\min_{\pi_{ij}} \sum_{i,j} (1 - S_{ij}) \, \pi_{ij}, \quad \pi_{ij} \in \{0, 1\}$$

Pairs achieving scores above a predefined threshold τ_{primary} constitute valid matches.

3.2 MATCH-Global: Multi-faceted Global Matching

While MATCH-Pair addresses an optimal correspondence between two persistence diagrams, many practical scenarios often involve multiple stochastic predictions (facets). Finding the corresponding topological structures among multiple facets is a challenge. Thus, we extend MATCH-Pair to MATCH-Global, a global multi-facet matching approach to link homologous 0-dimensional components consistently across all facets, assigning global indices to anatomical or topological structures.

Given a series of likelihood maps $\mathcal{L}=\{lh_t\}_{t=1}^T,\, lh_t\in[0,1]^{H\times W}$, each generates a persistence diagram: $\mathrm{Dgm}_t=\{(b_{t,i},d_{t,i})\}_{i=1}^{n_t}$. Each pair $(b_{t,i},d_{t,i})$ corresponds to a spatial mask $M_{t,i}$, the normalized persistence weight $w_{t,i}=\left|d_{t,i}-b_{t,i}\right|/\max_{t',j}\left|d_{t',j}-b_{t',j}\right|$, and birth-critical point $c_{t,i}$.

Matching is performed sequentially across facets. For each adjacent pair of facets (t, t + 1) we form the weighted overlap matrix:

$$S_{ij}^{(t)} = \mathbf{w}_{t,i} \, \mathbf{w}_{t+1,j} \text{IoU}(M_{t,i}, M_{t+1,j}) \left(1 - \frac{\|c_{t,i} - c_{t+1,j}\|_2}{d_{\max}^{(t)}}\right)$$

with $d_{\max}^{(t)} = \max_{i,j} \|c_{t,i} - c_{t+1,j}\|_2$ introduces a soft spatial penalty. Optimal assignments are solved via the proposed MATCH-Pair algorithm.

These matches form an undirected graph $G=(\mathcal{V},\mathcal{E})$ with vertices $\mathcal{V}=\{(t,i)\mid 1\leq t\leq T,\ 1\leq i\leq n_t\}$, representing the structures and edges $\mathcal{E}=\bigcup_{t=1}^{T-1}\mathcal{E}^{(t)}$ indicating matches. Connected components $\{\mathcal{C}_k\}_{k=1}^K$ of G are identified by breadth-first search, providing globally consistent identities: $\mathcal{C}_k=\{(t,i)\mid \text{mask }M_{t,i}\text{ belongs to identity }k\}$.

Thus, the global multi-facet matching framework integrates pairwise correspondences into globally coherent tracks, robustly accommodating missing detections, splits, and merges, thereby ensuring topological consistency across multiple facets.

3.3 Dual-Level Topological Consistency

After identifying consistent topological structures across multiple facets, we propose dual-level topological consistency losses to enhance segmentation reliability and coherence. Specifically, we introduce two complementary loss terms: *intra-topological consistency*, which ensures consistency among stochastic predictions from MC dropout realizations [9], and *temporal-topological consistency*, which maintains consistency across consecutive training iterations.

In both scenarios, topological features are extracted from multiple prediction facets. We then apply our proposed MATCH-Global algorithm (see Section 3.2) to classify these topological structures into two distinct categories: **matched** ($\mathcal{C}_{intra}^{match}$, $\mathcal{C}_{temp}^{match}$), representing features consistently identified across multiple predictions, and **unmatched** ($\mathcal{C}_{intra}^{unmatch}$, $\mathcal{C}_{temp}^{unmatch}$), denoting features that are inconsistent or unstable across predictions. Specifically, matched structures are encouraged toward optimal probability distributions at their birth and death critical points, whereas unmatched structures, indicative of prediction uncertainty or instability, are driven toward shorter topological lifespans. Formally, we define the associated losses as:

$$\mathcal{L}_{\text{match}}(t,i) = \left(P_{b_{t,i}}^{(t)}\right)^2 + \left(1 - P_{d_{t,i}}^{(t)}\right)^2, \quad \mathcal{L}_{\text{diag}}(t,i) = \left(P_{b_{t,i}}^{(t)} - P_{d_{t,i}}^{(t)}\right)^2.$$

where $P_{b_{t,i}}^{(t)}$ and $P_{d_{t,i}}^{(t)}$ represent the predicted probability values at the birth $(b_{t,i})$ and death $(d_{t,i})$ critical points, respectively, of the i-th topological feature extracted from the t-th prediction.

The intra-topological consistency loss aggregates these penalties over multiple stochastic predictions through MC dropout within each iteration:

$$\mathcal{L}_{\text{intra}} = \frac{1}{B_{\text{intra}}} \sum_{b=1}^{B_{\text{intra}}} \left[\frac{1}{|\mathcal{C}_{\text{intra}}^{\text{match},(b)}|} \sum_{(t,i) \in \mathcal{C}_{\text{intra}}^{\text{match},(b)}} \mathcal{L}_{\text{match}}(t,i) + \frac{1}{|\mathcal{C}_{\text{intra}}^{\text{unmatch},(b)}|} \sum_{(t,i) \in \mathcal{C}_{\text{intra}}^{\text{unmatch},(b)}} \mathcal{L}_{\text{diag}}(t,i) \right]$$

where B_{intra} indicates the number of MC dropout predictions within each iteration. Similarly, the temporal-topological consistency enforces the constraints across predictions from consecutive training snapshots:

$$\mathcal{L}_{\text{temp}} = \frac{1}{B_{\text{temp}}} \sum_{b=1}^{B_{\text{temp}}} \left[\frac{1}{|\mathcal{C}_{\text{temp}}^{\text{match},(b)}|} \sum_{(t,i) \in \mathcal{C}_{\text{temp}}^{\text{match},(b)}} \mathcal{L}_{\text{match}}(t,i) + \frac{1}{|\mathcal{C}_{\text{temp}}^{\text{unmatch},(b)}|} \sum_{(t,i) \in \mathcal{C}_{\text{temp}}^{\text{unmatch},(b)}} \mathcal{L}_{\text{diag}}(t,i) \right]$$

where B_{temp} presents the number of temporal training snapshots. Finally, our dual-level topological consistency losses are integrated into the overall training objective alongside the supervised and pixel-wise consistency terms:

$$\mathcal{L}_{total} = \mathcal{L}_{sup} + \lambda_{cons} \mathcal{L}_{cons} + \lambda_{intra} \mathcal{L}_{intra} + \lambda_{temp} \mathcal{L}_{temp}$$

where hyperparameters λ_{cons} , λ_{intra} , and λ_{temp} balance their respective contributions, ensuring the model jointly meets pixel-level accuracy and robust topological coherence.

Table 1: Quantitative results on three histopathology image datasets. We compare our method with several state-of-the-art semi-supervised medical image segmentation methods on two settings of 10% and 20% labeled data. The statistically significant best results are highlighted in **bold**, while the second-best are marked with underline.

MoNuSeg $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Dataset	Label Ratio (%)	Method	Pixel-wise		Topology-wise	
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Heat Fig.		100 (Full)	Fully-Supervised	0.928 ± 0.002	0.149 ± 0.015	5.650 ± 0.223	29.425 ± 1.782
Heat Fig.			MT [57]	0.790 ± 0.005	2.392 ± 0.162	31.125 ± 3.274	76.130 ± 2.965
TopoSemiSeg [69] 0.849 ± 0.004 1.155 ± 0.123 19.588 ± 3.408 54.832 ± 3.017 14.238 ± 1.154 40.912 ± 2.422 40.904 40.912 ± 2.422 40.905						19.188 ± 3.846	
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GlaS TopoSemiSeg [69] 0.878 ± 0.003 0.551 ± 0.014 8.300 ± 0.478 35.845 ± 1.965			XNet [83]	0.874 ± 0.003	0.843 ± 0.051	14.238 ± 1.154	40.912 ± 2.422
GlaS MT [57] 0.863 ± 0.005 2.126 ± 0.171 29.963 ± 3.987 64.275 ± 3.496 EM [59] 0.865 ± 0.006 1.255 ± 0.138 17.275 ± 3.783 58.673 ± 3.255 UA-MT [79] 0.866 ± 0.005 1.123 ± 0.132 18.038 ± 3.599 53.014 ± 3.069 URPC [39] 0.878 ± 0.004 0.759 ± 0.067 14.350 ± 1.212 42.587 ± 2.601 XNet [83] 0.887 ± 0.003 0.510 ± 0.065 10.188 ± 1.154 35.298 ± 2.328 PMT [10] 0.895 ± 0.003 0.510 ± 0.053 9.825 ± 0.813 30.462 ± 1.978 Ours 0.894 ± 0.004 0.273 ± 0.026 6.875 ± 0.276 19.620 ± 0.712 MT [57] 0.748 ± 0.006 10.210 ± 0.486 292.857 ± 6.542 1526.079 ± 35.84 EM [59] 0.757 ± 0.006 10.339 ± 0.503 257.071 ± 5.445 1319.815 ± 31.78 UA-MT [79] 0.774 ± 0.004 6.829 ± 0.319 214.428 ± 5.327 1098.372 ± 24.39 XNet [83] 0.762 ± 0.005 7.152 ± 0.338 220.405 ± 4.611 1122.799 ± 25.11 PMT [10] 0.785 ± 0.003 6.661 ± 0.376 196.357 ± 3.067 1068.401 ± 17.50 Ours 0.785 ± 0.003 5.594 ± 0.361 192.863 ± 1.137 1011.857 ± 12.64 MoNuSeg MT [57] 0.767 ± 0.005 12.522 ± 0.547 246.786 ± 8.018 1350.751 ± 32.40 URPC [39] 0.777 ± 0.006 1.252 ± 0.547 246.786 ± 8.018 1350.751 ± 32.40 UA-MT [79] 0.778 ± 0.005 12.522 ± 0.547 246.786 ± 8.018 1350.751 ± 32.40 UA-MT [79] 0.777 ± 0.006 0.751 ± 0.035 198.571 ± 6.731 1011.857 ± 12.64 MoNuSeg MT [57] 0.767 ± 0.005 12.522 ± 0.547 246.786 ± 8.018 1350.751 ± 32.40 URPC [39] 0.779 ± 0.006 5.325 ± 0.254 193.429 ± 6.105 1025.431 ± 23.79 URPC [39] 0.779 ± 0.006 5.305 ± 0.316 198.525 ± 5.421 1174.066 ± 26.01 PMT [10] 0.778 ± 0.006 6.500 ± 0.308 195.125 ± 6.289 1080.462 ± 25.11 TopoSemiSeg [69] 0.793 ± 0.004 5.150 ± 0.145 188.642 ± 3.215 1105.946 ± 18.48 Ours 0.790 ± 0.006 4.930 ± 0.156 179.225 ± 2.383 982.286 ± 14.955 Ours 0.790 ± 0.006 5.005 ± 0.156 179.225 ± 2.383 982.286 ± 14.955 Ours 0.790 ± 0.006 5.005 ± 0.156 179.225 ± 2.383 982.286 ±			PMT [10]				
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Ours 0.790 ± 0.006 $\overline{4.930 \pm 0.156}$ $\overline{179.225 \pm 2.383}$ $\overline{982.286 \pm 14.953}$							1080.476 ± 25.145
							1105.946 ± 18.486
100 (Full) Fully-Supervised 0.817 ± 0.010 2.491 ± 0.460 142.429 ± 4.674 729.017 ± 17.662							
		100 (Full)	Fully-Supervised	0.817 ± 0.010	2.491 ± 0.460	142.429 ± 4.674	729.017 ± 17.662

4 Experiments

We conduct comprehensive evaluations on three publicly available histopathology image datasets on both pixel-wise and topology-wise metrics. We benchmark our method against classic and recent state-of-the-art semi-supervised segmentation methods, including MT [57], EM [59], UA-MT [79], URPC [39], XNet [83], PMT [10], and TopoSemiSeg [69].

Implementation Details. The implementation details will be provided in the Supplementary.

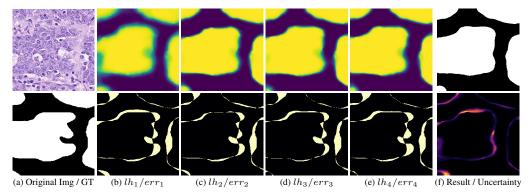


Figure 5: Qualitative illustration of MC dropout predictions (after the model convergence). **Top row:** original patch, the four likelihood maps, and the final segmentation. **Bottom row:** ground-truth mask, corresponding error maps, and the pixel-wise variance (uncertainty) map.

Datasets. We evaluate our proposed method on Colorectal Adenocarcinoma Gland (CRAG) [11], Gland Segmentation in Colon Histology Images Challenge (GlaS) [53], and Multi-Organ Nuclei Segmentation (MoNuSeg) [32]. More details are provided in the Supplementary.

Evaluation Metrics. To better evaluate our proposed method, we use pixel-wise metrics including **Object-level Dice Score (Dice_obj)** [67]; topology-wise metrics including **Betti Error** [21], **Betti Matching Error** [56], and **Discrepancy between Intersection and Union (DIU)** [40]. More details are provided in the Supplementary.

4.1 Results

Uncertainty Throughout the Topological Consistency. As illustrated in Figure 5, our proposed MATCH not only produces a robust segmentation result (top, (f)) but also furnishes an informative pixel-wise uncertainty map without any uncertainty-specific training objective or doing post hoc calibration. Visually, the variance map (bottom, (f)) concentrates along the gland boundaries where the four likelihood maps disagree, and these regions coincide almost perfectly with the binary error maps (bottom, (b) - (e)). Quantitatively, the Pearson correlation coefficients (PCC) [48] between the uncertainty and the error maps are 0.768, 0.728, 0.757, and 0.753 for the four facets, respectively. This confirms that the uncertainty is tightly coupled with prediction errors. Hence, reliable uncertainty estimation and the attendant suppression of spurious structures emerge naturally as a by-product of the proposed consistency mechanism, with no additional supervision or model modification required.

Quantitative Results. As shown in Table 1, across the three histopathology image datasets, our proposed method consistently achieves superior performance compared to state-of-the-art semi-supervised segmentation methods, under both 10% and 20% labeled data settings. Specifically, our method yields higher topology-wise accuracy with comparable pixel-wise performance. These results collectively illustrate that our framework effectively leverages limited annotations to achieve robust segmentation accuracy and enhanced topological fidelity.

Qualitative Results. We provide the qualitative results in Figure 6. The qualitative comparison highlights that our proposed method consistently outperforms other semi-supervised methods in preserving accurate glandular structures and topology across various histopathology samples. The comparative methods exhibit notable topological errors, including fragmentation, merging, and boundary leakage, as indicated by the red boxes. In contrast, our method effectively mitigates these errors, demonstrating superior robustness in maintaining topological integrity and accurate boundary delineation, thereby underscoring its effectiveness for precise medical image analysis tasks.

4.2 Ablation Study

To comprehensively explore the robustness and efficacy of our proposed strategy, hyperparameterselection, and experimental settings, we conduct the ablation experiments on the CRAG dataset using 20% labeled data.

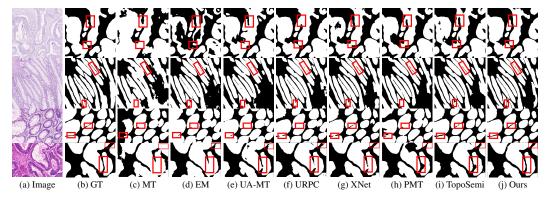


Figure 6: Qualitative results for semi-supervised methods on 10% and 20% labeled data. Rows 1-2 correspond to CRAG dataset, rows 3-4 correspond to the GlaS dataset. From left to right: (a) raw image, (b) ground-truth mask, (c) to (i) present the 7 baselines. (j) indicates the results of our method. The regions prone to topological errors are highlighted in red boxes.

Table 2: Ablation study on matching algorithms. Table 3: Effect of IoU & spatial-proximity (SP).

Matching	Pixel-wise		Topology-wise			
	Dice_obj ↑	BE ↓	BME ↓	DIU ↓		
Betti [56]	0.864 ± 0.007 0.889 ± 0.005	0.237 ± 0.021	8.216 ± 0.717	58.592 ± 2.574 44.157 ± 2.146		
Ours	0.909 ± 0.005	0.188 ± 0.018	7.425 ± 0.570	40.250 ± 1.720		

IoU SP		Pixel-wise	Topology-wise			
		Dice_obj ↑	BE ↓	BE↓ BME↓		
1	х	0.890 ± 0.005	0.233 ± 0.020	8.300 ± 0.650	43.750 ± 2.100	
Х	1	0.882 ± 0.006	0.247 ± 0.022	9.600 ± 0.680	46.200 ± 2.250	
1	✓	$\textbf{0.909} \pm \textbf{0.005}$	$\textbf{0.188} \pm \textbf{0.018}$	$\textbf{7.425} \pm \textbf{0.570}$	40.250 ± 1.720	

Ablation Study on Matching Algorithm. To validate the effectiveness of our proposed matching algorithm, we compare it against established alternatives, including Wasserstein Matching [21] and Betti-Matching [56]. As shown in Table 2, our algorithm consistently achieves superior performance in both pixel- and topology-wise metrics. Specifically, Wasserstein Matching, relying exclusively on persistence values without spatial information, exhibits the worst results. Although Betti-Matching incorporates spatial context, it still performs suboptimally compared to our method.

Ablation Study on IoU and Spatial Proximity (SP). To validate the effectiveness of the individual items of our matching cost, we conduct an ablation study on IoU and spatial proximity. The results in Table 3 quantitatively substantiate the complementary roles of the IoU and the spatial proximity factor in our Hungarian assignment cost. Removing either the proximity or the overlap item could degrade the performance. The overlap itself cannot fully distinguish spatially adjacent structures. These results demonstrate that both items are necessary to achieve topologically accurate matching.

Sensitivity Analysis on B_{intra} and B_{temp} . We further analyzed the sensitivity of our method to the number of MC dropout samples B_{intra} and temporal training snapshots B_{temp} . Table 4 shows that employing too few facets yields unreliable estimation of topological consistency, resulting in suboptimal segmentation performance. Conversely, increasing the number of facets beyond an optimal point introduces redundant information and additional variability, degrading model performance. Therefore, 4 is the optimal number that strikes a practical balance, ensuring the best performance while remaining computationally efficient.

Table 4: Influence of B_{intra} and B_{temp} .

Table 5: Efficacy of \mathcal{L}_{intra} and \mathcal{L}_{temp} .

B _{intra} B _{temp}		Pixel-wise		$\mathcal{L}_{\mathrm{intra}}$ \mathcal{L}		
mua	temp	Dice_obj ↑	BE ↓	BME ↓	DIU ↓	- mua
2	2	0.878 ± 0.010	0.255 ± 0.025	9.350 ± 0.620	48.600 ± 2.300	×
3	3	0.892 ± 0.007	0.214 ± 0.020	8.105 ± 0.600	44.105 ± 2.050	1
5	5	0.872 ± 0.011	0.275 ± 0.023	10.050 ± 0.630	54.250 ± 2.253	X
4	4	$\textbf{0.909} \pm \textbf{0.005}$	$\textbf{0.188} \pm \textbf{0.018}$	7.425 ± 0.570	40.250 ± 1.720	✓

\mathcal{L}_{intra} \mathcal{L}_{temp}		Pixel-wise	Topology-wise			
		Dice_obj ↑	BE ↓	BME ↓	DIU ↓	
x	Х	0.862 ± 0.011	0.460 ± 0.022	11.680 ± 0.610	59.930 ± 2.150	
/	Х	0.898 ± 0.006	0.215 ± 0.020	7.920 ± 0.590	44.750 ± 1.970	
Х	/	0.882 ± 0.008	0.238 ± 0.031	8.540 ± 0.450	45.310 ± 2.040	
/	/	$\textbf{0.909} \pm \textbf{0.005}$	$\textbf{0.188} \pm \textbf{0.018}$	$\textbf{7.425} \pm \textbf{0.570}$	40.250 ± 1.720	

Ablation Study on Loss Components. To evaluate the contributions of individual loss terms in our dual-level topological consistency framework, we conduct experiments selectively enabling or disabling the \mathcal{L}_{intra} and \mathcal{L}_{temp} . As presented in Table 5, each loss individually improves the pixel- and

Table 6: The results on the Roads dataset.

Table 7: Density-aware quantitative results.

Labeled Ratio	Method	BE↓	BME↓	DIU↓
10%	TopoSemiSeg Ours			10.952 ± 0.671 9.376 ± 0.583
20%	TopoSemiSeg Ours			9.387 ± 0.538 8.149 \pm 0.492

Setting	Dice_obj↑	BE \downarrow	BME↓
Sparse (Ours, ≤ 30 cells) Crowded ([69], ≥ 100 cells) Crowded (Ours, ≥ 100 cells)	0.756 ± 0.009	6.890 ± 0.240	
Ours (whole test image)	0.790 ± 0.006	4.930 ± 0.156	179.225 ± 2.383

topology-wise performance compared to the baseline without these constraints. Combining both losses achieves the strongest overall performance, confirming that \mathcal{L}_{intra} and \mathcal{L}_{temp} complement each other by addressing different sources of topological inaccuracies—stochastic noise within single facets and structural inconsistencies across training iterations.

Ablation Study on 1-D Topological Features. We mainly focus on 0-D topological features due to the following factors: For the primary application in our study (gland and nuclei segmentation), the most critical topological errors involve incorrect splitting or merging of individual structures, which are well-captured by 0-D persistent homology. For the validation on 1-dimensional structures, we conducted additional experiments on the Roads dataset [42]. The results are shown in Table 6. It verifies that our method could learn good topological representations from unlabeled data on 1-dimensional topological features.

Crowding-Aware Ablation Study. To quantify the influence of nuclei density on model performance, we randomly cut the test images into patches of size 256×256 . For every patch, we count nuclei in the ground-truth instance map. Patches with <= 30 nuclei are labeled Sparse; those with >=100 nuclei are labeled Crowded. We sampled 14 samples for a fair comparison and show the results below in Table 7. The experiments above verify that our approach is density-aware. It achieves state-of-the-art performance on typical tissue, excels in sparse fields, and maintains a clear advantage over the strongest baseline under extreme nuclear crowding.

Ablation Study on the Alternatives of MC-dropout. We choose two alternative perturbation methods: Variational Inference (VI) [26], which generates multiple predictions by sampling from the learned variational posterior distribution, and Temperature Scaling [14], which produces diverse predictions through multiple sampling from temperature-modulated probability distributions. The experiments are conducted on CRAG 20% labeled data, and the results are shown in Table 8.

Table 8: Ablation of perturbation methods.

Table 9: Comparison with foundation models.

 ± 0.042

+0.025

BME↓

 27.300 ± 2.937

 11.275 ± 1.899

Method	Dice_obj↑	BE↓	BME↓	Method	Dice_obj↑	BE↓
Variational Inference	0.895 ± 0.006	0.242 ± 0.022 0.258 ± 0.025 $\textbf{0.188} \pm \textbf{0.018}$	9.125 ± 0.685	LoRA–SAM	0.882 ± 0.006	0.440 ± 0.0
Temperature Scaling	0.891 ± 0.007		9.850 ± 0.795	LoRA–MedSAM	0.898 ± 0.005	0.268 ± 0.0
MC-Dropout	0.909 ± 0.005		7.425 ± 0.570	Ours	0.909 ± 0.005	0.188 ± 0.0

Comparison with Self-Supervised Methods Finetuned on Limited Labeled Data. To comprehensively evaluate the effectiveness of our method, we compare our method against some foundation models, like SAM [29] and MedSAM [41]. We use LoRA [19] to finetune these two models using 20% labeled data on the CRAG dataset and report the performance in Table 9. The results show that even with powerful foundation models, like SAM or MedSAM, topological errors can still exist without explicit topological modeling.

5 Conclusion

We present a semi-supervised segmentation framework that preserves significant topological structures in histopathology with limited annotations. Dual-level topological consistency across Monte Carlo dropout predictions and temporal training snapshots separates stable biological patterns from noise. For alignment, MATCH-Pair achieves spatially accurate matching between noisy persistence diagrams by combining spatial overlap, persistence, and proximity, and MATCH-Global scales to multiple facets. Experiments show consistent gains in robustness and substantial reductions in topological errors, enabling more reliable downstream analyses in digital pathology.

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MATCH: <u>Multi-faceted Adaptive Topo-Consistency</u> for Semi-Supervised Histopathology Segmentation

-Supplementary Material-

6 Overview

In the supplementary, we begin with a brief introduction to the persistent homology in Section 7, followed by detailed introductions of the datasets in Section 8 and the evaluation metrics in Section 9. Then, we provide the implementation details in Section 10, followed by the references of our baselines in Section 11. We also provide additional ablation studies in Section 12 to further illustrate the efficacy and robustness of our method and hyper-parameter selections. The limitations are provided in Section 13, followed by an analysis on the broader impact in Section 14.

7 Brief Introduction to Persistent Homology

Persistent homology [6, 7], a fundamental concept in topological data analysis (TDA), offers a robust framework for capturing and quantifying the topological features of data across multiple scales. In the context of image segmentation, particularly when dealing with likelihood maps that represent the probability of each pixel belonging to a specific class, persistent homology provides a means to analyze the underlying topological structures inherent in these probabilistic representations.

Given a likelihood map $f: \Omega \to [0,1]$, where $\Omega \subset \mathbb{R}^2$ represents the image domain, we construct a filtration of super-level sets:

$$\mathcal{F}_{\alpha} = \{ x \in \Omega \mid f(x) \ge \alpha \}, \quad \alpha \in [0, 1].$$

As α decreases from 1 to 0, the super-level set \mathcal{F}_{α} transitions from empty regions to encompass the entire domain Ω , revealing the sequential emergence, merging, and disappearance of connected components and loops. Persistent homology tracks these topological changes across the filtration, recording the corresponding birth and death thresholds of each feature in a persistence diagram.

A persistence diagram is a multiset of points $\{(b_i, d_i)\}$ in the extended plane \mathbb{R}^2 , where each point corresponds to a topological feature that appears (birth b_i) and disappears (death d_i) during the filtration process. Features that persist across a wide range of α values (i.e., with large $|d_i - b_i|$) are considered topologically significant, while those with short lifespans are often attributed to noise.

8 Dataset Details

Colorectal Adenocarcinoma Gland (CRAG) [11] consists of 213 hematoxylin and eosin (H&E)-stained colorectal adenocarcinoma image tiles acquired at $20\times$ magnification, each with detailed annotations at the instance level. Most images are in approximately 1512×1516 pixels. Officially, the dataset is partitioned into 173 training samples and 40 testing samples. For our experiments, the training subset is further divided into 153 images for model training and 20 images for validation. For semi-supervised scenarios with 10% and 20% labeled data, we randomly select 16 and 31 labeled images, respectively, for training.

Gland Segmentation in Colon Histology Images Challenge (GlaS) [53] comprises 165 images sourced from 16 H&E-stained histological slides of colorectal adenocarcinoma at stages T3 or T4. The official split includes 85 training images and 80 testing images. In our experimental setup, the training set is divided into 68 images for model training and 17 for validation. We randomly select 7 and 14 labeled images to represent 10% and 20% of labeled training data scenarios, respectively.

Multi-Organ Nuclei Segmentation (MoNuSeg) [32] dataset contains 44 H&E-stained histology images of dimensions 1000×1000 pixels, encompassing nuclei annotations from seven distinct organs. Officially, it consists of 30 training images with a total of 21,623 annotated nuclei and 14 images designated for testing. For our experiments, we reserve 20% (6 images) of the training set for validation. In experiments involving 10% and 20% labeled data splits, we randomly select 3 and 5 labeled images, respectively, for training.

9 Evaluation Metrics

We evaluate the segmentation quality from both pixel- and topology-wise. **Object-level Dice coefficient (Dice_Obj)** [67] is selected to measure pixel-wise performance, which measures instance-wise overlap between predicted and ground-truth masks and is thus well suited to the precise delineation of individual structures required in digital pathology.

To evaluate the topological accuracy, we select three topological evaluation metrics, **Betti Error** [21], **Betti Matching Error** [56], and **Discrepancy between Intersection and Union (DIU)** [40]. Betti Error (BE) mainly computes the mean absolute difference in 0-dimensional Betti numbers over 256×256 sliding-window patches. Betti Matching Error (BME), which extends BE by enforcing spatial correspondence when pairing topological features, thereby penalizing misplaced components even when counts are preserved. Introduced in [40], DIU quantifies how faithfully the topology of the common and combined foreground regions agrees.

10 Implementation Details

Our model is trained in two distinct stages. In the initial stage, we perform pretraining using only supervised loss and pixel-wise consistency loss. For all three datasets, the pretraining stage proceeds for 12,000 iterations. The second stage involves fine-tuning the model by integrating our proposed dual-level topological consistency constraints, which last for an additional 1,000 iterations. We use UNet [49] as the backbone for both the student and teacher models.

All training is implemented using PyTorch [47] and optimized using the Adam optimizer [28]. Training hyperparameters are set as follows: the batch size is 16 and the learning rate is 5×10^{-4} . Both labeled and unlabeled data undergo pre-processing through random cropping (with cropping size of 256×256), followed by data augmentation procedures including random rotation and flipping as weak augmentations, and color adjustments and morphological shifts for stronger augmentations.

In particular, we adopt a random cropping strategy for enforcing intra-topological consistency, while a fixed patch cropping strategy is used for temporal-topological consistency. The inputs to the student model to estimate the intra- and temporal-topological consistency are all original patches, without any transformations. The EMA decay rate α is set to 0.999. Within the supervised loss, the weights assigned to the cross-entropy loss and Dice loss are equally set to 0.5. The weight of the pixel-wise consistency loss is calculated by the Gaussian ramp-up function $\lambda_{\rm cons} = k*e^{-5*(1-\frac{\tau}{T})^2}$, where k=0.1 and T is the total number of iterations.

Additionally, λ_{intra} and λ_{temp} are both set to 0.001. This balanced configuration ensures effective integration of topological constraints while maintaining stable training dynamics. Note that dual-level topological consistency is used to optimize the student model directly, and we use the student model to do the inference. The experiments are conducted on an NVIDIA RTX A6000 GPU (48 GB), using a 24-core Intel® Xeon® Gold 6248R CPU @ 3.00 GHz and 192 GB RAM. The training time of one iteration is 1020.04 ms, and GPU memory consumption is 25.726 GB using UNet with batch size 16. The training time of TopoSemiSeg for one iteration is 610.80 ms, and the GPU memory consumption is 15.235 GB. For the non-PH baseline, like PMT [10], the training time per iteration is 582.34 ms,

11 Baseline Reference

We select 7 classical and recent state-of-the-art methods as comparatives. The implementations of some of them are based on publicly available repositories. Here, we provide the source of our baselines for reference and greatly appreciate their efforts in building the open-source community:

MT [57], EM [59], UA-MT [79] and URPC [39] are based on the implementations from: https://github.com/HiLab-git/SSL4MIS.

XNet [83] is based on the implementations from:

https://github.com/guspan-tanadi/XNetfromYanfeng-Zhou.

PMT [10] is based on the implementations from: http://github.com/Axi404/PMT.

TopoSemiSeg [69] is based on the implementations from: https://github.com/Melon-Xu/TopoSemiSeg.

12 Additional Ablation Study

Here, we provide additional ablation studies to illustrate the efficacy and robustness of our selected backbone and hyperparameters.

Ablation Study on λ_{intra} and λ_{temp} . The results shown in Table 10 demonstrate the impact of varing weights of intra- and temporal-topological consistency (λ_{intra} and λ_{temp}). When two weights are both 0.001, the performance is the best across both pixel-wise and topology-wise metrics. As these weights increase from 0.001 to 0.01, there's a clear degradation in performance, indicating that excessively large consistency constraints may introduce unnecessary regularization, thus impairing the segmentation quality. When both weights are reduced to 0.0005, the dual-level consistency regularization becomes too weak to meaningfully optimize the student model, leading to diminished topological guidance and a corresponding drop in both pixel-wise and topology-wise performance.

Ablation Study on EMA Decay α . Table 11 investigates the influence of the EMA decay parameter α . $\alpha=0.999$ yields the best performance. When decreasing α from 0.999 to 0.996, the results remain competitive but slightly deteriorate, highlighting that a higher EMA decay value effectively leverages historical model parameters for improved topological and segmentation robustness. In contrast, very high values (e.g. $\alpha=0.9999$) excessively rely on historical information, marginally weakening the adaptability and performance of the model.

Table 10: Influence of λ_{intra} and λ_{temp} .

Table 11: Impact of the EMA decay α .

$\lambda_{ ext{intra}}$	$\lambda_{ ext{temp}}$	Pixel-wise		Topology-wise		
mua	temp	Dice_obj ↑	BE ↓	BME ↓	DIU ↓	
0.01 0.005 <u>0.001</u> 0.0005	0.001	0.892 ± 0.007 0.909 ± 0.005	0.214 ± 0.020 0.188 ± 0.018	$\textbf{7.425} \pm \textbf{0.570}$	53.500 ± 2.300 44.105 ± 2.050 40.250 ± 1.720 44.225 ± 1.850	

α	Pixel-wise	Topology-wise				
	Dice_obj ↑	BE ↓	BME ↓	DIU ↓		
0.999	$\begin{array}{c} \textbf{0.909} \pm \textbf{0.005} \\ 0.902 \pm 0.006 \end{array}$	$\begin{array}{c} \textbf{0.188} \pm \textbf{0.018} \\ 0.205 \pm 0.020 \end{array}$	$\begin{array}{c} \textbf{7.425} \pm \textbf{0.570} \\ 8.250 \pm 0.610 \end{array}$	46.000 ± 2.100 40.250 ± 1.720 42.500 ± 1.900 50.000 ± 2.300		

Ablation Study on Different Backbones. To further verify the robustness of our proposed method, we conduct ablation experiments on different backbones. The results are shown in Table 12. Specifically, DeepLabV3+ [4] and UNet++ [85] show modest but clear improvements in both pixel-wise and topology-wise metrics. The UNet [49] backbone achieves the most substantial gains, particularly in topology-wise metrics. These results demonstrate that integrating our MATCH framework consistently improves performance across multiple backbones.

Table 12: Performance comparison of different backbones w or w/o our MATCH.

Backbone	Pixel-Wise	Topology-Wise			
	Dice_Obj ↑	BE ↓	BME ↓	VOI ↓	
DeepLabV3+ [4] DeepLabV3+ [4]+Ours	0.889 ± 0.010 0.892 ± 0.008	0.272 ± 0.023 0.245 ± 0.022	$\begin{array}{c} 11.782 \pm 0.690 \\ 10.129 \pm 0.638 \end{array}$	50.867 ± 2.221 47.412 ± 2.047	
UNet++ [85] UNet++ [85]+Ours	$0.886 \pm 0.008 \\ 0.890 \pm 0.006$	$\begin{array}{c} 0.245 \pm 0.023 \\ 0.238 \pm 0.020 \end{array}$	$\begin{array}{c} 9.210 \pm 0.603 \\ 9.021 \pm 0.580 \end{array}$	$\begin{array}{c} 45.517 \pm 2.041 \\ 45.073 \pm 1.995 \end{array}$	
UNet [49] UNet [49]+Ours	0.894 ± 0.006 0.909 ± 0.005	0.232 ± 0.019 0.188 ± 0.018	8.872 ± 0.579 7.425 \pm 0.570	44.281 ± 1.881 40.250 ± 1.720	

Ablation Study on Applying Dual-Level Topo-Consistency between Teacher and Student Models.

We conduct an ablation study to assess the impact of enforcing dual-level topological consistency in a teacher-student framework. Specifically, the dual-level topological consistency is estimated from the teacher model's multiple predictions, and consistency constraints are applied between the student output and the most recent prediction from the teacher. We compare this teacher-student configuration with a student-only model, both trained under identical consistency constraints. The results in Table 13 reveal that the student-only model consistently achieves superior performance. The relatively poorer performance of the teacher-student configuration suggests that leveraging the

teacher's predictions, potentially noisy or outdated, introduces additional uncertainty and adversely affects the student's ability to effectively capture stable topological structures.

Table 13: Ablation study on applying dual-level topo-consistency between teacher and student models.

Mode	Pixel-wise	Topology-wise			
	Dice_Obj ↑	BE \downarrow	$BME\downarrow$	DIU \downarrow	
Teacher–Student Student Only	0.885 ± 0.007 0.909 ± 0.005	0.217 ± 0.021 0.188 ± 0.018	8.102 ± 0.620 7.425 \pm 0.570	42.520 ± 1.880 40.250 ± 1.720	

Extension from Binary to Multi-Class Segmentation. To extend our method to the multi-class setting, we choose a multi-class nuclei segmentation dataset, MoNuSAC [58], to conduct experiments. This dataset contains four cell types: Epithelial, Lymphocyte, Macrophage, and Neutrophil. We conducted experiments using 20% labeled data and report the class-wise performance of TopoSemiSeg and our method in Table 14. As demonstrated in our class-specific results on MoNuSAC (Epithelial, Lymphocyte, Macrophage, and Neutrophil), our approach consistently outperforms TopoSemiSeg across all cell types, with particularly notable improvements in topological metrics (BE and BME) that are crucial for distinguishing overlapping structures.

Table 14: The multi-class segmentation results on the MoNuSAC dataset.

Class	Method	Dice_obj↑	BE \downarrow	$BME \!\downarrow$
Epithelial	TopoSemiSeg Ours	0.778 ± 0.009 0.781 ± 0.008	5.342 ± 0.187 5.128 ± 0.189	195.158 ± 4.627 186.847 ± 3.958
Lymphocyte	TopoSemiSeg Ours	0.751 ± 0.013 0.756 ± 0.012	6.089 ± 0.223 5.794 ± 0.235	218.394 ± 5.841 207.693 \pm 4.672
Macrophage	TopoSemiSeg Ours	0.765 ± 0.011 0.769 ± 0.010	5.687 ± 0.201 5.423 ± 0.208	206.732 ± 4.985 195.381 ± 4.127
Neutrophil	TopoSemiSeg Ours	0.738 ± 0.016 0.742 ± 0.015	6.521 ± 0.267 6.187 ± 0.281	234.576 ± 6.123 221.459 \pm 5.894

Ablation Study on the Sensitivity of $\tau_{primary}$. We provide the ablation study on the sensitivity of $\tau_{primary}$ in Table 15. The results have shown that our method is robust to selecting $\tau_{primary}$. Moreover, the low threshold of 0.1 was chosen to be inclusive rather than restrictive: it allows more potential matches to be considered valid while letting the Hungarian algorithm determine optimal assignments based on our comprehensive similarity metric (combining spatial overlap, persistence weights, and proximity).

Table 15: Effect of $\tau_{primary}$.

$ au_{ ext{primary}}$	Dice_obj ↑	BE ↓	BME ↓	DIU ↓
0.05	0.906 ± 0.0060	0.195 ± 0.019	7.850 ± 0.620	41.750 ± 1.850
0.1 (current)	0.909 ± 0.0050	0.188 ± 0.018	7.425 ± 0.570	40.250 ± 1.720
0.2	0.908 ± 0.0050	0.191 ± 0.020	7.680 ± 0.590	41.100 ± 1.780
0.3	0.905 ± 0.0060	0.201 ± 0.021	8.150 ± 0.650	42.850 ± 1.920

Table 16: Effect of dropout rates.

Dropout Ra	te Dice_obj↑	$\mathbf{BE}\downarrow$	$\mathbf{BME}\downarrow$
10%	0.898 ± 0.0060	0.210 ± 0.020	08.200 ± 0.650
20% (current	0.909 ± 0.0050	$.188 \pm 0.013$	87.425 ± 0.570
30%	0.910 ± 0.0050	0.185 ± 0.01	77.350 ± 0.560
50%	0.890 ± 0.0070	0.020 ± 0.022	28.800 ± 0.720

The Impact of Different Dropout Rates. We also add complementary ablation studies on the dropout rate of the MC-dropout. Other settings are kept unchanged. We conduct the ablation experiments on CRAG 20% labeled data and report the performance in Table 16. The results reveal an optimal dropout rate range of 20%-30% for our framework, where performance plateaus with minimal differences between these rates. Lower dropout rates provide insufficient perturbation diversity for reliable topological matching. In contrast, excessive dropout introduces detrimental noise that degrades both pixel- and topology-wise performance, confirming that moderate stochasticity is essential for effective topological consistency estimation.

Ablation Study on \mathcal{L}_{cons} . We conducted the ablation study on the \mathcal{L}_{cons} and the results are shown in Table 17. Based on the results of the ablation study and the principles of semi-supervised learning, removing the pixel-wise consistency term in the training stages would result in significant performance degradation across all metrics.

Table 17: Ablation Study on \mathcal{L}_{cons} .

Method	Dice_obj ↑	BE ↓	BME ↓
w/o \mathcal{L}_{cons}	0.875 ± 0.008	0.285 ± 0.025	9.850 ± 0.680
Ours	0.909 ± 0.005	0.188 ± 0.018	7.425 \pm 0.570

Downstream Analysis: Cell counting To further analyze the impact of our method on downstream analysis, we conducted a cell counting study on the same MoNuSeg test cohort. We used the connected component analysis [65] to identify the cells and calculate the total cell count, the predicted total cell count, and the absolute counting error (mean \pm std). The results are shown in Table 18. Note that the Total GT cell count and the predicted cell count are reported for the entire test cohort, while the absolute count error is reported per image (with a total of 14 test images).

We observed that our method yields noticeably smaller counting errors than both baseline approaches (one topo method and one non-topo method). This confirms that although the pixel-wise segmentation performances are comparable, fixing the topological errors on a few pixels leads to more accurate biological readouts.

Table 18: Downstream Analysis on Cell Counting.

Method	Total GT Cell Count	Predicted Cell Count	Absolute Counting Error (Mean \pm Std)	Dice_obj
PMT [8] TopoSemiSeg [57]	6024 6024	8106 7877	$148.71 \pm 99.41 \\ 132.36 \pm 56.09$	0.778 ± 0.006 0.793 ± 0.004
MATCH	6024	7511	106.21 ± 49.30	0.790 ± 0.006

13 Limitations

A potential limitation of our MATCH framework arises from its reliance on stable feature extraction from persistence diagrams, which can be challenged when predictions exhibit extreme noise or minimal structural differences. In addition, the framework introduces nontrivial computational overhead: computing persistence diagrams and performing MATCH-Global/MATCH-Pair alignments across Monte Carlo dropout samples and temporal snapshots require multiple forward passes and matching steps, resulting in longer training times and increased memory usage.

14 Broader Impact

Our method significantly contributes to enhancing segmentation robustness by effectively leveraging unlabeled data, reducing reliance on extensive annotations, and ensuring topological accuracy crucial for clinical and biomedical analysis. This approach not only facilitates efficient utilization of limited labeled data but also provides insightful uncertainty estimates beneficial for downstream diagnostic applications.

A negative broader impact could include inadvertent propagation of segmentation inaccuracies if poorly matched topological structures influence model learning, potentially affecting reliability in critical medical decisions.