Continual Gradient Low-Rank Projection Fine-Tuning for LLMs

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Abstract

Continual fine-tuning of Large Language Models (LLMs) is hampered by the trade-off between efficiency and expressiveness. Low-Rank Adaptation (LoRA) offers efficiency but constrains the model's ability to learn new tasks and transfer knowledge due to its lowrank nature and reliance on explicit parameter constraints. We propose GORP (Gradient LOw Rank Projection for Continual Learning), a novel training strategy that overcomes these limitations by synergistically combining full and low-rank parameters and jointly updating within a unified low-rank gradient subspace. GORP expands the optimization space while preserving efficiency and mitigating catastrophic forgetting. Extensive experiments on continual learning benchmarks demonstrate GORP's superior performance compared to existing state-of-the-art approaches.

1 Introduction

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Large Language Models (LLMs) have demonstrated remarkable capabilities in areas like incontext learning (Hendel et al., 2023; Liu et al., 2024b) and instruction following (Wei et al., 2022b,a). To adapt these large models to specific downstream tasks, traditional full fine-tuning imposes prohibitive computational costs and memory requirements, which has driven extensive research into parameter-efficient fine-tuning (PEFT) approaches (Houlsby et al., 2019; Hu et al., 2022; Ben Zaken et al., 2022). Low-Rank Adaptation (LoRA) (Hu et al., 2022), in particular, has become a popular PEFT technique, especially in continual learning scenarios (Chitale et al., 2023; Wistuba et al., 2024), due to its efficiency and ability to mitigate catastrophic forgetting (Biderman et al., 2024).

While LoRA significantly reduces training complexity and storage, the low-rank matrices inherently constrain the parameter space and, consequently, the model's expressiveness during optimization (Zhao et al., 2024). This restriction to a low-rank subspace can lead to suboptimal performance compared to full fine-tuning, a gap that often widens in continual learning settings (Xia et al., 2024; Mahla et al., 2025). Furthermore, LoRA updates are intertwined with shared parameter updates, potentially causing collisions in the parameter spaces of different tasks (Wang et al., 2023; Lu et al., 2024). Gradient projection has emerged as a promising mitigation strategy (Saha et al., 2021; Wang et al., 2021; Kong et al., 2022; Saha and Roy, 2023). Common approaches involve calculating the hidden feature space and projecting it onto the orthogonal gradient space of the old task. However, gradient spaces for different tasks are heterogeneous and dynamically evolving. Existing methods that impose explicit constraints (e.g., parameter regularization) on LoRA's low-rank parameters (Wang et al., 2023; Du et al., 2024; Yang et al., 2025) can only approximate the ideal parameter space and fail to adapt dynamically to the changing gradient space of new tasks (Liu et al., 2024a). Moreover, these explicit constraints often struggle to capture shared features across tasks, hindering knowledge transfer.

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To address these limitations, we introduce $GORP(\underline{G}radient \ L\underline{O}w \ \underline{R}ank \ \underline{P}rojection for Continual Learning), a novel training strategy for continual fine-tuning of LLMs that synergistically integrates full and low-rank parameter updates within a low-rank gradient subspace. GORP effectively balances the$ *stability-plasticity dilemma*inherent in continual learning (see Table 1 for a comparison with other methods). From a*plasticity*perspective, GORP enhances LoRA by incorporating learnable full-rank parameters for the current task. Crucially, we exploit the observation that gradients tend to adopt a low-rank structure during training (Zhao et al., 2024). Therefore, we project the gradients of these full-rank parameters into a low-rank

	Parameters		Parameter Constraints		Gradient Space	
Method	Full-rank	Low-rank	Explicit	Implicit	Low-rank	Adaptability
O-LoRA (Wang et al., 2023)	×	\checkmark	\checkmark	×	×	Static
MIGU (Du et al., 2024)	×	\checkmark	X	\checkmark	×	Static
N-LoRA (Yang et al., 2025)	×	\checkmark	\checkmark	×	×	Static
GORP(Ours)	\checkmark	\checkmark	×	\checkmark	\checkmark	Dynamic

Table 1: Comparison of continual fine-tuning methods on training parameters, parameter constraints and Gradient Space Adaptability.

space, maintaining fine-tuning efficiency while significantly expanding the search space for optimal solutions. From a stability perspective, GORP de-084 parts from prior methods that rely on explicit constraints. Recognizing the limitations of directly sampling subspaces from large-scale models, we 087 leverage the first-order moment of gradients to implicitly capture the dynamic properties of the gradient space. This approach provides a more robust 090 and comprehensive representation of the gradient, reducing computational complexity compared to methods that directly manipulate the hidden feature space (Saha et al., 2021; Zheng et al., 2024a; Qiao et al., 2024). We evaluate GORP on several continual fine-tuning evaluations, demonstrating its 096 superior performance compared to existing stateof-the-art methods. Our results confirm that GORP 098 provides a more effective approach for continual fine-tuning of LLMs. 100

> Our main contributions are summarized as follows:

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• We leverage the complementary strengths of full and low-rank parameters by jointly updating them within a unified low-rank gradient subspace. This expands the search space for optimal solutions while retaining the efficiency of low-rank adaptation.

• We utilize the first-order moment of gradients to approximate the hidden feature space, providing a more robust and efficient way to construct a gradient subspace. This mitigates catastrophic forgetting and minimizes computational overhead.

We introduce GORP, a novel training strategy that effectively balances stability and plasticity in continual learning, outperforming existing methods while maintaining fine-tuning efficiency.

2 Related Works

2.1 Parameter-efficient Fine Tuning of LLMs

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Various efficient parameter fine-tuning methods include adapters (Houlsby et al., 2019), Low-Rank Adaptation (LoRA) (Hu et al., 2022), and parameter subset techniques (Ben Zaken et al., 2022). These methods have tackled the challenges including large number of parameters and substantial memory requirements by fine-tuning selective model parameters rather than the entire model. Among these, LoRA has become one of the most widely used methods, which is achieved by freezing pre-trained weights and introducing low-rank trainable matrices, effectively reducing the computational burden. Building on LoRA, Lialin et al. (2023) proposed a series of low-rank aggregation updates for learning network parameters. Xia et al. (2024) employed a residual LoRA module at each fixed step, and eventually merging it with the pretrained model parameters for chained updates. Hao et al. (2024) used random projection sampling to approximate LoRA, enabling high-rank weight updates, and optimizing memory usage.

2.2 Continual Fine Tuning for LLMs

Three widely used continual learning paradigms (Shi et al., 2024; Lu et al., 2024; Zheng et al., 2024b) for parameter fine-tuning are Replay-based methods (Zhao et al., 2022; Huang et al., 2024), Architecture-based methods (Badola et al., 2023; Song et al., 2023), and Learning-based methods (Farajtabar et al., 2020; Smith et al., 2024), which employ specific optimization strategies or introduce regularization penalties based on the original loss function to balance the trade-off between old and new knowledge. Many studies have demonstrated improved performance through learningbased methods. Qiao et al. (2024) proposed an overarching framework for continual fine-tuning, establishing diverse paradigms for efficient fine-tuning. However, due to the challenges in obtaining gradi-

ent spaces and the impracticality of using implicit 158 feature spaces, Wang et al. (2023) suggested lever-159 aging LoRA itself to represent the gradient space, 160 ensuring orthogonality between gradient spaces of 161 different tasks to mitigate forgetting. Subsequently, Du et al. (2024) focused on screening the normal-163 ized gradients of the hidden linear layer outputs 164 and updating the selected parameters to minimize 165 gradient conflicts. Yang et al. (2025) introduced parameter sparsification constraints, addressing pa-167 rameter conflicts between tasks and ensuring that each task's vector space remains independent. Ad-169 ditionally, Lu et al. (2024) and Chen and Garner 170 (2024) employed regularization matrices and intro-171 duced further constraints to enhance the ability of 172 LLMs to learn new tasks. 173

2.3 Continual learning with Gradient Projection

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Gradient projection methods in continual learning project the gradient into a subspace of the input's implicit feature space to mitigate catastrophic forgetting when learning new tasks. The Gradient Projection Memory proposed by Saha et al. (2021) leverages the relationship between the input and gradient spaces to form a gradient subspace for each layer, thereby retaining prior knowledge while accommodating new information. However, the gradient space can impose restrictive constraints on the optimization space for new tasks, potentially limiting their learning performance. To facilitate both forward and backward knowledge transfer, Lin et al. (2022c)(2022b) proposed a scaling matrix based on the similarity between new and previous tasks, using the frozen weights from the old task to scale and update the current task's weights. In response to the continuous expansion of the gradient subspace, Liang and Li (2023) introduced the dual gradient projection memory method, which reduces memory consumption and adaptively expands the dimensionality of the layer, enhancing the model's plasticity for new tasks. Other studies (Kong et al., 2022; Wang et al., 2021; Lin et al., 2022a) also improved continual learning performance by refining the gradient space.

3 Gradient Low Rank Projection

We introduce GORP, a novel training strategy that combines full and low-rank parameters with lowrank gradient updates to strike a balance between plasticity and stability. The framework, illustrated

Algorithm 1: Algorithm for GORP **Input** :Old task weight W, gradient G_t , step t, rank r, scale factor α , decay rates β_1, β_2 , learning rate η , subspace change frequency T, num steps N. **Output :** New task weight W 1 Initialize gradient subspace $\mathcal{S} \leftarrow [$] 2 Initialize first-order moment $M_t \leftarrow 0$ 3 Initialize second-order moment $V_t \leftarrow 0$ 4 Initialize step $t \leftarrow 1$ 5 while $t \leq N$ do 6 if Full-rank Parameters then if $t \mod T = 0$ then // via 7 Equation 6 $USV \leftarrow SVD(G_t)$ 8 $G'_t \leftarrow U_r^\top G_t$ 9 else 10 $G'_t \to G'_{t-1}$ 11 end 12 end 13 if LoRA Parameters then 14 $G'_t \leftarrow G_t$ 15 end 16 $P_t \leftarrow \mathsf{Project}(G'_t) / / \mathsf{via}$ 17 Equation 7 $M_t \leftarrow \beta_1 M_{t-1} + (1 - \beta_1) P_t$ 18 $V_t \leftarrow \beta_2 V_{t-1} + (1 - \beta_2) P_t^2$ 19 $P'_t \leftarrow M_t / \sqrt{V_t + \epsilon}$ 20 $W_t \leftarrow W_{t-1} + \eta \cdot \alpha U_r P'_t$ 21 22 end 23 Update S with $M_t//$ via Equation 2,3,4 24 return New task weight W

in Figure 1, consists of two main components: (1) the Gradient Shared Space Construction, which employs low-rank moment with distinct parameters to construct a shared gradient space, and (2) the Low-Rank Projection Optimization, which projects the gradient space of both full and low-rank parameters. The pseudo-code of our method is provided in Algorithm 1.

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3.1 Gradient Shared Space Construction

In this section, we construct a gradient shared space. A common approach for building gradient spaces in continual learning is to randomly sample from hidden layer input features. However, for LLMs trained on vast amounts of data, the limited number



Figure 1: The framework of our Gradient Low Rank Projection (GORP) method. During k-th task training, we reduce the dimensions of full-rank parameters and project both full and low-rank parameters into the space S_{k-1} . Then, we use the first-order moment M_k and a k-rank approximation to construct the Gradient Shared Space S_k .

of sampled features may fail to accurately represent the overall data distribution. Consequently, the resulting gradients may not align with the overall gradient direction during gradient space computation.

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To address this issue, we employ low rank moment to more accurately represent the overall gradient space. Specifically, using Adam as an example, for the parameter gradient $G_t \in \mathbb{R}^{m \times n}$, there exists a first-order moment $M_t \in \mathbb{R}^{m \times n}$. Since Adam incorporates historical gradient information at each iteration, its moment term can theoretically help the optimization algorithm better approximate the optimal gradient direction for the overall task, particularly when the task's loss function exhibits a flat or irregular landscape. Thus, after training, we can leverage first-order moment information to capture the gradient direction of the current task and calculate the gradient sharing space. Let L denote the number of parameter layers to be trained.

For the first task, we utilize first-order moments of each layer's parameters, denoted as $M_1 = \{M_1^1, M_1^2, \ldots, M_1^l, \ldots, M_1^L\}$. We then perform singular value decomposition (SVD) on each layer, yielding $M_1^l = U_1^l \sum_{1}^l V_1^{l^{\top}}$. Finally we execute a k-rank approximation under the specified constraints:

$$\|(M_1^l)_k\|_F^2 > \epsilon_t^l \|M_1^l\|_F^2 \tag{1}$$

where ϵ_t^l is an approximation threshold. We select the first k vectors from U_1^l to form layer gradient space, denoted as $S_1^l = [u_{1,1}^l, u_{1,2}^l, \dots, u_{1,k}^l]$, and aggregate the layer-wise gradient spaces to obtain overall gradient space $S = \{\{S_1^l\}_{l=1}^L\}$ for the current task.

For task 2 to T, we use the second task as an

example to illustrate our method. After completing training, we use the first-order moment $M_2 = \{M_2^1, M_2^2, \ldots, M_2^l, \ldots, M_2^L\}$ obtained from the second task to calculate the component that is orthogonal to the previously gradient space:

$$\hat{M}_{2}^{l} = M_{2}^{l} - \mathcal{S}^{l}(\mathcal{S}^{l})^{\top} M_{2}^{l} = M_{2}^{l} - M_{2,Proj}^{l} \quad (2)$$

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We perform SVD decomposition on the first-order moment of each layer, obtaining $\hat{M}_2^l = U_2^l \Sigma_2^l V_2^{l^{\top}}$. Then we apply the updated constraints and the approximation threshold ϵ_t^l to perform a k-rank approximation:

$$\|(\hat{M}_{2}^{l})_{k}\|_{F}^{2} + \|\hat{M}_{2,Proj}^{l}\|_{F}^{2} \ge \epsilon_{t}^{l}\|\hat{M}_{2}^{l}\|_{F}^{2} \quad (3)$$

Finally, we update the gradient space as follows:

$$\mathcal{S} = [\mathcal{S}, u_{2,1}^l, u_{2,2}^l, \dots, u_{2,k}^l]$$
(4)

As the number of tasks increases, the gradient space will gradually expand. Therefore, it is necessary to constrain the gradient space and control its size by filtering the singular values to maintain a fixed dimension.

3.2 Low Rank Projection Optimization

In this section, we leverage the gradient shared space to project the training parameters effectively. Our training parameters consist of both LoRA and the full-rank parameters. The core idea behind low-rank projection is to reduce redundant information by constraining updates within the low-rank gradient space, ensuring learning focuses on critical direction updates. This approach mitigates overfitting and improves the model's generalization ability in high-dimensional data, resulting in

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a more stable training process, while maintaining fine-tuning efficiency.

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Specifically, for LoRA parameters, the projection is applied to parameter A, which is projected into the gradient shared space. Given the gradient $G_{A,l} \in \mathbb{R}^{m \times n}$ of parameter A and the gradient space $S_{t-1}^{A,l}$:

$$G'_{A,l} = G_{A,l} - \mathcal{S}^{A,l}_{t-1} (\mathcal{S}^{A,l}_{t-1})^\top G_{A,l}$$
(5)

For full-rank parameters, following Zhao et al. (2024), we apply low-rank updates during Adam optimization rather than full-rank updates. Since full-parameter training introduces additional memory overhead and given that parameter gradients tend to exhibit a low-rank structure over the course of training, it is essential to preserve their lowrank nature as much as possible throughout the optimization. Given a full-rank parameter gradient $G_{t,l} \in \mathbb{R}^{m \times n}$, we decompose it into a low-rank structure using $G_{t,l} = U_l \sum_l V_l^{\top}$, then we select first k vectors $U_{l,k}$ and $V_{l,k}$, and project them into $G_{t,l}$ as follows:

$$G'_{t,l} = U_{l,k}^{\top} G_{t,l} V_{l,k}$$
(6)

The original gradient information is compressed by projecting $G_{t,l}$ into a low-rank representation $G'_{t,l}$. This reduces the dimensionality of the data while preserving its most significant features. Then $G'_{t,l}$ is projected into gradient space S^l_{t-1} as follows:

$$P_{t,l} = G'_{t,l} - \mathcal{S}^{l}_{t-1} (\mathcal{S}^{l}_{t-1})^{\top} G'_{t,l}$$
(7)

The projected gradient $G'_{t,l}$ of LoRA and the lowrank projected gradient $P_{t,l}$ are then optimized by Adam:

$$M_{t,l} = \beta_1 M_{t-1,l} + (1 - \beta_1) P_{t,l} \tag{8}$$

$$V_{t,l} = \beta_2 V_{t-1,l} + (1 - \beta_2) P_{t,l}^2$$
(9)

$$P_{t,l}^{\prime} = M_{t,l} / \sqrt{V_{t,l} + \epsilon} \tag{10}$$

Finally, the low-rank projected gradient is scaled back to the original gradient dimension:

$$\hat{G}_{t,l} = \alpha U_{l,k} P_{t,l}^{\prime} V_{l,k}^{\top} \tag{11}$$

$$W_{t,l} \leftarrow W_{t-1,l} + \eta \hat{G_{t,l}} \tag{12}$$

where α is the scaling factor and η is the learning rate. LoRA gradients do not require dimensional expansion and directly update the weights with Equation 12. However, frequent low-rank operations can introduce additional computational overhead. Therefore, we minimize the low-rank operations for full-rank parameters by updating them at fixed intervals. Simultaneously, the projection process in Equation 6 is simplified by projecting the gradients into a subspace, denoted as $G'_{t,l} = U_{l,k}^{\top} G_{t,l}$.

4 Experiments

In this section, we present the experimental setup and evaluate the performance of the proposed GORP method across multiple tasks. The focus is on assessing the advantages of GORP in terms of model performance and adaptability, while also comparing it with existing mainstream methods.

4.1 Experimental Setups

Models and Datasets. To evaluate the proposed method, we employ two widely adopted language models: the encoder-decoder T5-large model (Raffel et al., 2020) with 770M parameters and the decoder-only Llama2 model (Touvron et al., 2023) with 7B parameters. For datasets, we utilize the standard CL benchmarks (Zhang et al., 2015) and the large number of tasks (Razdaibiedina et al., 2023) as our experimental datasets. The standard CL benchmarks consist of classification datasets with 4 tasks and 5 categories, while the large number of tasks dataset includes a long-sequence CL dataset with 15 tasks, comprising the GLUE benchmark (Wang et al., 2018), SuperGLUE benchmark (Wang et al., 2019), and the IMDB movie reviews dataset (Maas et al., 2011). Following the experimental setup of Qin and Joty (2022) and Wang et al. (2023), we shuffle the tasks in the datasets and establish three different task orders. Detailed information is provided in Appendix B.

Evaluation Metrics. We evaluate the effectiveness of our GORP method from multiple perspectives using various evaluation metrics, including Average Accuracy, Backward Transfer (BWT), Parameter Orthogonality, and Gradient Orthogonality. The detailed calculation methods are provided in Appendix C.

Baselines. To demonstrate the effectiveness of our method, we compare it with various CL baseline approaches, including both non-continual learning methods and non-continual learning methods.

	Standard CL Benchmark			Large Number of Tasks				
	Order-1	Order-2	Order-3	Avg	Order-4	Order-5	Order-6	Avg
ProgPrompt	75.2	75.1	75.1	75.1	78.3	77.9	77.9	78.0
PerTaskFT	70.0	70.0	70.0	70.0	78.1	78.1	78.1	78.1
MTL	80.0	80.0	80.0	80.0	76.5	76.5	76.5	76.5
SeqFT	18.9	24.9	41.7	28.5	7.5	7.4	7.5	7.4
SeqLoRA	44.6	32.7	53.7	43.7	2.0	1.9	1.6	1.8
IncLoRA	66.0	64.9	68.3	66.4	54.7	53.2	62.2	56.7
Replay	55.2	56.9	61.3	57.8	44.5	46.5	45.1	45.4
EWC	48.7	47.7	54.5	50.3	46.9	45.6	45.6	46.0
LwF	50.2	52.0	64.3	55.5	49.9	50.5	49.5	49.9
L2P	60.3	61.7	61.1	61.0	56.9	56.9	56.1	56.6
LFPT5	65.3	68.0	71.5	68.3	70.0	73.0	73.8	72.3
O-LoRA	75.4	75.7	76.3	75.8	72.3	64.8	71.6	69.6
MIGU	77.1	77.0	75.6	76.6	67.3	68.5	74.2	70.0
N-LoRA	79.2	78.4	78.8	78.8	73.6	70.3	73.2	72.4
GORP	79.7	79.9	79.7	79.8	76.1	76.2	75.6	76.0

Table 2: Performance comparison across different methods on Standard CL Benchmark and Large Number of Tasks. The average accuracy after training on the final task is reported.

- Non-Continual Learning Methods: MTL (Multi Task Learning), which involves jointly training on multiple task datasets, typically represents the upper bound of continual learning. Per-TaskFT trains an independent model for each task, SeqFT (d'Autume et al., 2019) entails continual training of all parameters, SeqLoRA focuses on training only one LoRA, and IncLoRA involves training a new LoRA for each task.
- Continual Learning Methods: Replay involves merging old task data to train new tasks, while EWC (Kirkpatrick et al., 2017) and LwF (Li and Hoiem, 2018) adjust model parameters using regularization losses. L2P (Wang et al., 2022) and LFPT5 (Qin and Joty, 2022) dynamically design prompts to adapt to new tasks, and O-LoRA (Wang et al., 2023) constrains LoRA parameters to be orthogonal in a subspace to learn new tasks. MIGU (Du et al., 2024) considers output gradient normalization distributions to filter parameter updates, and N-LoRA (Yang et al., 2025) reduces collisions by sparsifying parameter updates.

4.2 Main Results

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We compare the performance of GORP with baseline methods on two types of CL benchmarks. The experimental results across different task orders are summarized in Table 2.

	Order-1	Order-2	Order-3	Avg
O-LoRA	76.8	75.7	75.7	76.1
N-LoRA	77.2	77.3	78.4	77.6
GORP	78.7	78.8	78.2	78.6

Table 3: Performance comparison of various methods implemented on the Llama2-7B model, reporting average accuracy across all task orders and evaluated across multiple task orders within the Standard CL Benchmark.

Performance on standard CL benchmarks. On T5 model, GORP demonstrates consistent superiority over all prior methods across various task sequences, achieving significant improvements on standard continual learning benchmarks. Specifically, GORP improves performance by 4% over baseline methods while closely approaching MTL performance. As shown in Table 3, GORP also significantly outperforms baseline methods on LLaMA2-7B, achieving a 2.5% performance gain. These results highlight the effectiveness of our approach, even with larger model parameters.

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Performance on a Large Number of Tasks. Continual learning tasks with long sequences are generally more challenging. As shown in Table 2, GORP consistently outperforms the baseline methods, achieving a 6.1% performance improvement. It also surpasses other state-of-the-art methods, with GORP's performance approaching that of MTL. Additionally, GORP performs more simi-

Baseline Gradient Orthogonality



Figure 2: The visualization comparison of gradient orthogonality between Baseline and our method. Although the first two tasks maintain orthogonality, gradient interference between parameters gradually increases as more tasks are added, while our method consistently preserves orthogonality.



Figure 3: Performance comparison of generalization on unseen tasks. GORP consistently outperforms other methods across all task orders.

larly to PerTaskFT than other methods, suggesting that combining low-rank parameters with full parameters helps narrow the performance gap.

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Generalization of LLMs. This part explores the generalization ability of our proposed GORP. We train on the first T-1 tasks, and test on the unseen t-th task, evaluating directly on the unseen task for comparison. As shown in Figure 3, the generative capability of pre-trained LLMs on unseen tasks is nearly zero. Although O-LoRA and its improved version, N-LoRA, outperform the pre-

	BWT (%)		
	Avg Order 1-3	Avg Order 4-6	
O-LoRA	-7.8	-16.4	
GORP	-0.8	-4.3	

Table 4: The forgetting rate comparison between the baseline and our proposed method, quantified using Backward Transfer (BWT) as the evaluation metric. As evidenced by the comparative results presented in the table, our method demonstrates a 7% and 12.1% reduction in forgetting rate compared to the baseline.

trained model on unseen tasks, the GORP method surpasses these comparative methods in generative ability. Across all task order configurations, GORP surpasses N-LoRA and O-LoRA, achieving average performance improvements of 7.0% and 26.2%, respectively. The results demonstrate the superior generative capability of GORP on unseen tasks. 433

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4.3 Ablation Study

In this section, we conduct ablation experiments to assess the contribution of each component to GORP. As shown in Figure 4, adding low-rank projections to LoRA improves performance by an average of 0.7% compared to the baseline. Combining LoRA with full-rank parameters and low-rank projection results in an average improvement of 2.0%, while the overall improvement reaches 3.9%. The results

		Method	
	O-LoRA	N-LoRA	GORP
FLOPs	68.4	84.3	0.125
$(\times 10^{12})$	$1 \times$	$1.23 \times$	$1.8e-3 \times$
Time/task	128.5	97.7	128.1
	$1 \times$	$0.76 \times$	$0.99 \times$

Table 5: Time complexity comparison of different methods on Standard CL Benchmark.



Figure 4: Ablation study of our method. B refers to the baseline method, L refers to low-rank projection for full-rank parameters, S refers to projection for LoRA, and G refers to our GORP method, which outperforms other components.

suggest that the incorporating both full-rank and low-rank parameters produces a complementary effect. The full-rank parameters enhance model flexibility and enable finer-grained adjustments, leading to improved performance. The ablation results confirm the effectiveness of each component.

4.4 Model Forgetting

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Forgetting is a critical challenge in continual learning. To address this, we compare the forgetting rate of GORP with baseline methods. As shown in Table 4, GORP achieves a forgetting rate of just 0.8%, while baseline methods exhibit a rate of 7.8%, representing a 7.0% reduction. This result highlights the strong anti-forgetting capability of GORP.

Gradient space plays a crucial role in mitigating forgetting. While O-LoRA explicitly enforces orthogonality constraints on LoRA weights, GORP applies implicit constraints to regulate gradients. We compare the updates of parameter A in GORP and O-LoRA from both parameter and gradient perspectives, visualizing the weight distribution of A and the orthogonality of gradient distributions. As shown in Figure 5, the baseline method maintains parameter orthogonality throughout. Although GORP exhibits slightly weaker parameter



Figure 5: The visualization comparison of parameter orthogonality between baseline and our method. Although the parameter orthogonality of our method is higher compared to the baseline, the difference is not significant.

orthogonality, the difference is minimal. However, GORP demonstrates highly stable gradient orthogonality in Figure 2, enabling better gradient direction control while allowing parameters to update within a larger space, thereby increasing their degrees of freedom. 474

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4.5 Time complexity Analysis

We present in Table 5 the floating point operations per second (FLOPs) and total running times (in seconds) of different methods on the standard CL benchmarks. Compared to O-LORA, our proposed GORP method requires nearly the same amount of time but significantly reduces computational cost. In contrast, N-LoRA reduces training time but increases computational demand. This indicates that our GORP method does not introduce significant computational delays and optimizes efficiency, making it a more resource-efficient alternative to O-LORA. While N-LoRA offers desirable speedup, it may result in higher computational burden. Therefore, GORP may be more suitable for scenarios where both time and computational resources are critical.

5 Conclusion

In this work, we propose GORP, a novel training strategy that overcomes these limitations by synergistically combining full and low-rank parameters and jointly updating within a unified lowrank gradient subspace. GORP is enable to expand the search space for optimal solutions while preserving the essential properties of continual fine-tuning. Through extensive empirical evaluations, we show that GORP effectively addresses the stability-plasticity dilemma in continual learning, all while maintaining computational efficiency during the fine-tuning.

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510 Limitations

While GORP outperforms existing methods on 511 continual learning benchmarks, several limitations 512 should be considered. First, as task sequences ex-513 pand, continuously updating task vectors within 514 the gradient subspace becomes necessary. There-515 fore, effectively capturing increasing task diversity 516 within constrained dimensional boundaries is a key 517 challenge. Additionally, while GORP has shown 518 strong performance in known continual data envi-519 ronments, its effectiveness in more complex realworld scenarios remains to be further validated. 521

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Preliminary Knowledge Α

Continual learning setups A.1

For consecutive tasks $\{T_1, T_2, \ldots, T_n\}$, each task T_t contains N_t samples $\{x_t, y_t\}_{t=1}^{N_t}$. In the t-th task, each step will sample n training samples \mathcal{B}_n from the task for training, obtain parameter weights W_s^t , and then accumulate the weights to obtain the weight of the current task $W_t = \sum_s W_s^t$, and integrate with the previous task weight to get $W_t' = \tilde{W}_{t-1}' + W_t$. The model is able to retain its performance on previous tasks while progressively learning new ones, thereby minimizing the forgetting of earlier tasks.

A.2 Low Rank Adaptation

For a pre-trained weight $W_p \in \mathbb{R}^{m \times n}$, LoRA freezes the pretrained parameters and updates $W_{new} = W_p + \Delta W = W_p + AB$ by training low rank parameters, where $A \in \mathbb{R}^{m \times k}$ and $B \in \mathbb{R}^{k \times n}$, and rank $k \ll min(m, n)$. For a linear layer, the output can be written by Equation 13:

$$y = (W_p + \Delta W)x = W_p x + ABx$$
(13)

Through low rank updates, W_{new} retains the capabilities of pretrained models and also improves the generalization ability on downstream tasks.

Datasets and Task Details B

This part presents the datasets used in the experiments, along with the data categories and their

corresponding tasks. The detailed information is
provided in Table 6. CL benchmark includes Yelp,
Amazon, Dbpedia, Yahoo and Agnews, GLUE
dataset includes MNLI, QQP, RTE and SST-2, and
SuperGLUE includes WiC, CB, COPA, BoolQA,
MultiRC and IMDB. For the large number of tasks,
we select 1000 random samples for training each
task and 500 samples per class for validation and
testing.

We report the task sequences used for CL experiments on the T5 and LLAMA2 models in Table 7. These datasets span diverse categories, including natural language inference (NLI), sentiment classification (SC), and topic classification (TC), ensuring diverse abilities of the model's generalization across multiple tasks. And the task instructions for different categories are shown in Table 8.

C Evaluation Metrics

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Let $a_{i,j}$ be the test accuracy of the *i*-th task after training on the *j*-th task. A_i denotes the A matrix of LoRA, and $G_{A,i}$ denotes the gradient of A matrix on the *i*-th task. We evaluate the model using the following metrics:

• Average Accuracy (ACC): The average accuracy of all tasks after training on the last task:

$$ACC = \frac{1}{T} \sum_{i=1}^{T} a_i, T \tag{14}$$

• **Backward Transfer (BWT)**: The average forgetting of all tasks after training on the last tasks:

$$BWT = \frac{1}{T-1} \sum_{i=1}^{T-1} a_{i,T} - a_{i,i} \qquad (15)$$

• **Parameter Orthogonality (PO)**: We use this metric to quantify the orthogonal overlap between A_i and A_j , for the reason that O-LoRA use A to capture gradient subspaces of previous tasks. The metric is calculated as:

$$PO_{i,j} = \|A_i^{\top} A_j\|^2 \tag{16}$$

• Gradient Orthogonality (GO): We use this metric to quantify the orthogonal overlap between $G_{A,i}$ and $G_{A,j}$, showing the difference between the gradient space and the parameter space, calculated as:

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We adapted the code-base from O-LoRA (Wang et al., 2023). And our improved version of the code is available in the supplementary meterial and will be released upon acceptance. All experiments were conducted on the machine with 8 NVIDIA L20 and were implemented with Deepspeed. 880

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Implementation Details

For T5 model, we employed LoRA to replace the SelfAttention layers and full-rank parameter trainings for the EncDecAttention layers. For all orders, we trained the models with one epoch, a constant learning rate 1e-03 for LoRA and 1e-05 for full-rank parameters, a training batch size of 8 per device, a evaluation batch size of 64 per device, and a weight decay rate of 0, a value 0.05 of λ . We set different scale factors for order 1 to 6. For order 1 to 3, we set scale factor 1 and 0.25 for order 4 to 6. In our method, the low-rank updates are interval, and we set the update gap 10.

For LLaMA2 model, we employed LoRA to replace the Self-atten layers and full-rank parameter trainings for the MLP Gate layers. For order 1 to 3, we trained the models with one epoch, a constant learning rate 2e-04 for LoRA and 1e-06 for full-rank parameters, a training batch size of 1 per device, a evaluation batch size of 4 per device, and a weight decay rate of 0, a value 0 of λ . We set scale factor 0.25 for order 1 to 3 and the value 20 of the interval gap for low-rank updates.

- $GO_{i,j} = \|G_{A,i}^{\top}G_{A,j}\|^2 \tag{17}$
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Dataset Name	Category	Task	Domain	Metric
Yelp	CL Benchmark	Sentiment analysis	Yelp reviews	Accuracy
Amazon	CL Benchmark	Sentiment analysis	Amazon reviews	Accuracy
Dbpedia	CL Benchmark	Topic classification	Wikipedia	Accuracy
Yahoo	CL Benchmark	Topic classification	Yahoo Q&A	Accuracy
AG News	CL Benchmark	Topic classification	News	Accuracy
MNLI	GLUE	NLI	Various	Accuracy
QQP	GLUE	Paragraph detection	Quora	Accuracy
RTE	GLUE	NLI	News, Wikipedia	Accuracy
SST-2	GLUE	Sentiment analysis	Movie reviews	Accuracy
WiC	SuperGLUE	Word sense disambiguation	Lexical databases	Accuracy
CB	SuperGLUE	NLI	Various	Accuracy
COPA	SuperGLUE	QA	Blogs, encyclopedia	Accuracy
BoolQA	SuperGLUE	Boolean QA	Wikipedia	Accuracy
MultiRC	SuperGLUE	QA	Various	Accuracy
IMDB	SuperGLUE	Sentiment analysis	Movie reviews	Accuracy

Table 6: Datasets, Categories, Domians and evaluation Metrics.

Model	Order	Task Sequence
T5-large, Llama2	1	dbpedia \rightarrow amazon \rightarrow yahoo \rightarrow ag
T5-large, Llama2	2	dbpedia \rightarrow amazon \rightarrow ag \rightarrow yahoo
T5-large, Llama2	3	yahoo \rightarrow amazon \rightarrow ag \rightarrow dbpedia
T5-large	4	$mnli \rightarrow cb \rightarrow wic \rightarrow copa \rightarrow qqp \rightarrow boolqa \rightarrow rte \rightarrow imdb \rightarrow$
		$yelp \rightarrow amazon \rightarrow sst-2 \rightarrow dbpedia \rightarrow ag \rightarrow multirc \rightarrow yahoo$
T5-large	5	$multirc \rightarrow boolqa \rightarrow wic \rightarrow mnli \rightarrow cb \rightarrow copa \rightarrow qqp \rightarrow rte \rightarrow$
	5	imdb \rightarrow sst-2 \rightarrow dbpedia \rightarrow ag \rightarrow yelp \rightarrow amazon \rightarrow yahoo
T5-large	6	$yelp \rightarrow amazon \rightarrow mnli \rightarrow cb \rightarrow copa \rightarrow qqp \rightarrow rte \rightarrow imdb \rightarrow$
	U	sst-2 \rightarrow dbpedia \rightarrow ag \rightarrow yahoo \rightarrow multirc \rightarrow boolqa \rightarrow wic

Table 7: Task sequences used for CL experiments on the T5 and LLAMA2 models.

Task	Instructions
NLI	What is the logical relationship between the "sentence 1" and the
	"sentence 2"? Choose one from the option.
QQP	Whether the "first sentence" and the "second sentence" have the same
	meaning? Choose one from the option.
SC	What is the sentiment of the following paragraph? Choose one from
	the option.
TC	What is the topic of the following paragraph? Choose one from the
	option.
BoolQA	According to the following passage, is the question true or false?
	Choose one from the option.
MultiRC	According to the following passage and question, is the candidate
	answer true or false? Choose one from the option.
WiC	Given a word and two sentences, whether the word is used with the
	same sense in both sentences? Choose one from the option.

Table 8: Instructions for different tasks.