WHALE-X: LEARNING SCALABLE EMBODIED WORLD MODELS WITH ENHANCED GENERALIZABILITY

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Abstract

World models play a crucial role in decision-making within embodied environments, enabling cost-free explorations that would otherwise be expensive in the real world. However, to support faithful imagination in out-of-distribution (OOD) regions, world models must possess significant generalizability, which poses substantial challenges for previous scalable approaches. This paper addresses two primary sources of the world model generalization error: the *policy distribution shift* caused by the divergence between test and data-collection policies, and the compounding error arising from long-horizon autoregressive rollout. To tackle these issues, we introduce the *policy-conditioning* and the *retracing-rollout* techniques, respectively. Incorporating these two techniques, we present Whale, a scalable spatial-temporal transformer-based world model with enhanced generalizability. We first demonstrate the effectiveness of the two techniques, showcasing their consistent superiority over previous baselines in both trajectory generation quality and value estimation accuracy. Furthermore, we propose Whale-X, a 414M parameter world model trained on 970K trajectories from Open X-Embodiment datasets. We show that Whale-X exhibits promising scalability and strong generalizability in real-world manipulation scenarios using minimal demonstrations.

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1 INTRODUCTION

Human beings have the capability to envision an imagined world in their minds, predicting how different actions might lead to different outcomes (Maus et al., 2013; Nortmann et al., 2015). Inspired by this aspect of human intelligence, world models (Ha & Schmidhuber, 2018) are designed to abstract real-world dynamics and provide such "what if" prediction. As a result, embodied agents can interact with world models instead of real-world environments to generate simulation data, which can be used for various downstream tasks, including counterfactual prediction (Chen et al., 2023), off-value estimation (Fu et al., 2021), and offline reinforcement learning (Levine et al., 2020). However, the requirement for accurate out-of-distribution (OOD) predictions for reliable model imagination poses significant challenges to the generalizability of world models, which has not been well addressed by previous approaches (Schubert et al., 2023).

In this work, we investigate the sources of the generalization error in world models, identifying two
 primary factors: 1) *policy distribution shift* (Janner et al., 2019), stemming from the divergence
 between the test policy and data-collection policies, and 2) *error compounding* (Xu et al., 2020),
 resulting from long-horizon autoregressive rollouts. The interplay of these two factors intensifies the
 challenge of generalization in world models.

To mitigate the generalization error caused by policy distribution shift, we introduce the **policy conditioning**, building upon the concept of policy-conditioned model learning (Chen et al., 2024a), aims to embed the policy information into the dynamics model learning, allowing the model to adapt to different policies actively to mitigate the extrapolation error caused by distribution shift. Furthermore, we propose a simple yet effective technique called **retracing rollout**, to reduce the long-horizon compounding error during test time. This approach fixes the first frame of the moving contexts to be the initial real observation and relabels the corresponding action by retracing the effects of the original actions at the history timesteps. As a plug-and-play solution, retracing rollout can be efficiently applied to end-effector pose control in various embodiment tasks without necessitating any changes to the training process. 054 Incorporating these two techniques, we present Whale, a scalable embodied world model based on 055 the spatial-temporal transformer (Ma et al., 2024; Bruce et al., 2024), designed to enable faithful long-056 horizon imagination for real-world visual control tasks. To substantiate the effectiveness of Whale, we conduct extensive experiments on both simulated Meta-World (Yu et al., 2019) benchmark and a 058 physical robot platform, encompassing a variety of pixel-based manipulation tasks. Experimental results on the simulated tasks show that Whale outperforms existing world model learning methods in both video fidelity and value estimation accuracy. Moreover, we also validate the effectiveness 060 of policy-conditioning and retracing-rollout techniques in reducing the generalization error. As a 061 further step, we introduce Whale-X, a 414M parameter world model trained on 970k real-world 062 demonstrations from Open X-Embodiment datasets (Collaboration et al., 2023). Whale-X serves as 063 a foundational embodied world model for evaluating real-world behaviors. With fine-tuning on a 064 few demonstrations in completely unseen environments and robots, Whale-X demonstrates strong 065 OOD generalizability across visual, motion, and task perspectives. Furthermore, by scaling up the 066 pre-training dataset or model parameters, Whale-X shows impressive scalability during both the 067 pre-training and fine-tuning phases. 068

- The primary contributions of this work are outlined as follows:
 - We introduce two key techniques: **policy conditioning** and **retracing rollout**, to tackle two main challenges of world model generalization: *policy distribution shift* and *long-horizon error compounding*;
 - By incorporating these two techniques, we propose **Whale**, a scalable embodied world model with enhanced generalizability, and further present a 414M parameter **Whale-X** pre-trained on 970K robot demonstrations;
 - We conduct extensive experiments to showcase the effectiveness of two techniques while highlighting Whale's remarkable scalability and generalization across both simulated and real-world tasks.
 - 2 BACKGROUNDS
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2.1 SEQUENTIAL DECISION-MAKING

A typical formulation of sequential decision tasks is the Markov decision process (MDP) (Puterman, 1990) specified by the tuple $\mathcal{M} = (S, \mathcal{A}, r, T^*, \gamma, H, \rho_0)$, where S is the state space, \mathcal{A} is the action space, r(s, a) is the reward function, $T^*(s'|s, a)$ is the real transition probability, $\gamma \in (0, 1]$ is the discount factor, H is the decision horizon, and $\rho_0(s)$ is the initial state distribution. In this work, we simply consider the case where $\gamma = 1$ and $H < \infty$. In reinforcement learning (Sutton & Barto, 2018), the objective is to learn a policy that maximizes the expected return in the MDP, which involves estimating the value of different policies. Specifically, the value of policy π is defined as:

$$V_{T^*}^{\pi} = \mathbb{E}_{\tau_H \sim (\pi, T^*)} \Big[\sum_{t=1}^{H} r(s_t, a_t) \Big], \tag{1}$$

where the state-action trajectory $\tau_H = (s_1, a_1, \dots, s_H, a_H)$ and rewards are generated by the rollouts of policy π within the dynamics T^* . Therefore, an unbiased estimation of policy values requires online interactions with the real environment.

100 A common scenario involves abundant pre-collected experience data, but direct interaction with 101 the environment is either prohibited or costly, necessitating value estimation and optimization to be 102 performed offline. In this scenario, an environment model T can be explicitly learned from the offline 103 data and used to generate a simulated experience for value estimation and optimization. Assume 104 that V_T^{π} is the value estimated within the model T, the environment model error induces a value 105 gap $|V_{T_*}^{\pi} - V_T^{\pi}|$ for the policy π . If the model is globally accurate, the value gap will diminish for any policy. However, offline experiences are often collected by a narrow range of policies (e.g., 106 near-expert policies), and the learned environment models have to generalize beyond the training 107 experiences to evaluate diverse policies.

108 2.2 WORLD MODELS FOR VISUAL CONTROL 109

110 Real-world control tasks often involve high-dimensional visual observations and a partially observable nature. These visual control environments can be further described by a partially observable Markov 111 decision process (POMDP) (Åström, 1965) specified by tuple $(S, \mathcal{O}, \phi, \mathcal{A}, r, T^*, \gamma, H, \rho_0)$, where 112 the agent receives visual observation $o_t = \phi(s_t)$ at each step, only containing incomplete information 113 of s_t , and executes an action based on history observations $a_t \sim \pi(\cdot | o_{1:t})$. The environment 114 then transitions into the next state s_{t+1} according to $T^*(\cdot|s_t, a_t)$ and provides the agent the next 115 observation $o_{t+1} = \phi(s_{t+1})$ and a reward signal $r(s_t, a_t)$. The agent must predict future outcomes 116 and make decisions based on historical observations due to incomplete information, making the 117 learning of general environment models in visual domains a significant challenge. 118

World models (Ha & Schmidhuber, 2018) are proposed as a general framework of learning visual 119 dynamics. A vision module learns an abstract, compressed representation of high-dimensional 120 image observations $z_t = E_{\theta}(o_t)$, a memory model tries to predict the future representations based 121 on the history $P_{\theta}(z_{t+1}|z_{1:t}, a_{1:t})$, compressing what happens over time, and a decoder recovers 122 the observation and reward predictions from the predicted representation $\hat{o}_{t+1}, \hat{r}_{t+1} = D_{\theta}(z_{t+1})$. 123 The combination of vision and memory modules enables efficient autoregressive future predictions, 124 allowing agents to plan or learn policies through model imaginations for visual control. Advanced 125 approaches (Hafner et al., 2020; 2023; Babaeizadeh et al., 2021; Gupta et al., 2023; Wu et al., 126 2024) largely retain this architecture, but replace the encoder, decoder, and latent dynamics with 127 different model architectures (e.g. transformer with video tokenizer and detokenizer). However, these 128 works have not emphasized the generalizability of world models, which is crucial for sequential decision-making but has not been well addressed by previous approaches (Schubert et al., 2023). 129

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3 SCALABLE WORLD MODEL WITH ENHANCED GENERALIZABILITY

133 The common learning methods for autoregressive world models regard the transition learning as a 134 standard supervised learning problem, minimizing the negative log-likelihood (NLL) of the single-step 135 transition probabilities over the pre-collected trajectories in a teacher-forcing manner, i.e.,

$$\min_{T} \mathbb{E}_{\mu \sim \Pi} \mathbb{E}_{\tau_{H} \sim (\mu, T^{*})} \frac{1}{H} \sum_{h=1}^{H} -\log T(o_{h} | \tau_{h-1}) \iff \min_{T} l_{\mathrm{KL}}(T; \Pi),$$

139 where (sub-)trajectory $\tau_h = (o_1, a_1, o_2, \dots, o_h, a_h), 1 \le h \le H$ is generated by interaction of a 140 behavior policy μ with the real dynamics T^* , and behavior μ is assumed to be sampled from a 141 behavior policy distribution Π . Minimizing the NLL equals to minimizing the KL divergence loss 142

$$l_{\mathrm{KL}}(T;\Pi) = \mathbb{E}_{\mu \sim \Pi} \mathbb{E}_{\tau_H \sim (\mu, T^*)} \frac{1}{H} \sum_{h=1}^{\infty} D_{\mathrm{KL}}(T^*(\cdot | \tau_{h-1}), T(\cdot | \tau_{h-1})).$$
 The learned world models are

usually utilized to evaluate any target policy π by simulating trajectories in an autoregressive manner:

$$V_T^{\pi} = \mathbb{E}_{\tau_H \sim (\pi, T)} \Big[\sum_{t=1}^H r(o_t, a_t) \Big],$$

where the trajectory simulation distribution deviates from the training distribution. In classical 149 sequential modeling tasks like sentence generation and translation, the distribution shift from teacher-150 forcing training to autoregressive generation diminishes as the model accuracy improves, which 151 therefore does not lead to significant negative impacts. In the world model learning, however, the 152 distribution shift results from both the model inaccuracy and the policy divergence, exacerbating the 153 evaluation inaccuracy: 154

$$\left| V_T^{\pi} - V_{T^*}^{\pi} \right| \le 2R_{\max} \underbrace{\mathcal{H}^2}_{\text{AutoReg}} \left(\underbrace{\sqrt{2 \, l_{\text{KL}}(T;\Pi)}}_{\text{Train Error}} + \underbrace{L \cdot W_1(d^{\pi}, d^{\Pi})}_{\text{Policy Divergence}} \right), \tag{2}$$

157 where a distribution shift term induced by the policy divergence ¹ occurs in addition to the KL training 158 loss, further amplified by an H^2 factor caused by the autoregressive generation. Even if the world 159

¹Here $W_1(d^{\pi}, d^{\Pi})$ is the Wasserstein-1 distance between the π -induced trajectory distribution $d^{\pi}(\tau)$ and 160 the behavior trajectory distribution $d^{\Pi}(\tau) = \mathbb{E}_{\mu \sim \Pi}[d^{\mu}(\tau)]$, and L is the Lipschitz constant of model loss w.r.t. 161 the trajectory, adapted from Chen et al. (2024a).



Figure 1: The overall architecture of Whale. The policy embedding model encodes the observation and action subsequences into policy embeddings z_i , which are then passed to the dynamics model along with observation tokens and actions to generate the next token predictions \hat{x}_{i+1} . The predicted observation tokens are subsequently fed into the dynamics model for further predictions autoregressively and decoded into observation predictions to obtain later policy embeddings.

model perfectly fits the training transitions, i.e. $l_{\text{KL}}(T;\Pi) = 0$, the variation of the policies could also significantly shift the trajectory distribution to those large error areas, resulting in degenerative generalizability.

One possible solution to this policy generalization issue is to embed the policy information into the world model, allowing the model to actively recognize and adapt to the policy-induced distribution shift (Chen et al., 2024a). This adaptation effect has been shown to reduce model generalization error caused by policy divergence, i.e. the last term in Eq (2). For further analysis, please refer to Appendix A. Furthermore, we devise a simple trick to facilitate long-horizon model rollout for embodiment tasks, effectively alleviating the autoregressive error amplification. Building on these concepts, we propose Whale, a scalable embodied world model with enhanced generalizability.

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189 3.1 OVERALL MODEL ARCHITECTURE190

191 In Figure 1, we illustrate the architecture of the Whale. Specifically, Whale comprises three main 192 components: policy embedding model, video tokenizer, and dynamics model. Inspired by previous works (Bruce et al., 2024), these modules utilize a spatial-temporal transformer (ST-transformer) 193 architecture. Within this framework, each token is designed to attend only to other tokens in the 194 current frame and those at corresponding positions in prior frames. Additionally, Whale is capable of 195 generating all tokens for the next frame in parallel at one time. These designs significantly simplify 196 the computational demands from a quadratic to a linear dependency relative to sequence length, 197 reducing both the memory usage and computational costs of the model training while increasing model inference speed. 199

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3.2 POLICY EMBEDDING LEARNING

We would like to extract the decision patterns within training trajectories τ_H into a policy embedding, reminiscent of the maximization of the evidence lower bound (ELBO) of the trajectory likelihood conditioned on the history τ_h (Venkatraman et al., 2024; Yang et al., 2023; Ajay et al., 2021):

$$\log P(\tau_H | \tau_h) \ge \mathbb{E}_{q_\phi(z | \tau_H)} \sum_{t=h}^{H} \log \pi_w(a_t | o_t, \tau_{t-1}, z) - D_{\mathrm{KL}}(q_\phi(z | \tau_H) | | p_\psi(z | \tau_h)) + Const, \quad (3)$$

where $q_{\phi}(z|\tau_H)$ denotes the posterior encoder, encoding the whole trajectory τ_H into a latent variable $z; \pi_w(a_h|o_h, \tau_{h-1}, z)$ denotes the decoder, which recovers the decision action from the latent variable z and the up-to-date history $(\tau_{h-1}, o_h); p_{\psi}(z|\tau_h)$ denotes the prior predictor, which allows the prediction of z based on the history τ_h . The information bottleneck requires the learned variable z to effectively capture the decision pattern within the trajectory, embedding the information about the corresponding behavior policy. Following this argument, we propose to learn the policy embedding by maximizing the ELBOs over H decision steps and adjusting the amount of KL constraints similar



Figure 2: The illustration of the retracing rollout. Here, the retrace action \hat{a}_1 can produce an equal effect of the robot's arm as executing a_1, \dots, a_{t-3} sequentially from o_1 , thus effectively reducing the compounding error of the robot's arm generated by world models.

to β -VAE (Higgins et al., 2017):

$$\mathcal{L}(w,\phi,\psi) = \mathbb{E}_{\tau_H \sim \mathcal{D}} \Big[\mathbb{E}_{q_\phi(z|\tau_H)} \Big[-\sum_{h=1}^H \log \pi_w(a_h|o_h,\tau_{h-1},z) \Big] + \beta \sum_{h=1}^H D_{\mathrm{KL}}(q_\phi(z|\tau_H)||p_\psi(z|\tau_h)) \Big],$$
(4)

here the KL terms constrain the embedding predictions from sub-trajectories up to each time step h, encouraging them to approximate the posterior encoding. This ensures that the representation remains policy-consistent, meaning that trajectories generated by the same policy should have similar representations, as suggested in the previous analysis.

3.3 WORLD MODEL LEARNING

World models typically consist of an observation encoder that encodes the raw observation into a compact representation and a dynamics model that predicts future transitions within this representation space (Ha & Schmidhuber, 2018). In this work, we adopt a tokenizer based on VQ-VAE (Van Den Oord et al., 2017) as the encoder to discretize observations into tokens and train a dynamics model at the token level.

Specifically, the video tokenizer e_{θ} is composed of an encoder E_{θ} and a decoder D_{θ} , where the encoder E_{θ} compresses video input into a sequence of tokens, while the decoder D_{θ} is capable of reconstructing the original video from these tokens. This tokenizer is trained with the standard VQ-VAE loss $\mathcal{L}_{tok}(\theta)$, which is a combination of a L_1 reconstruction loss, a codebook loss, and a commitment loss.

After training the tokenizer, we embed the policy information into the dynamics model learning process. The key distinction from standard dynamics model learning is that Whale additionally incorporates a policy embedding z_h inferred by the prior predictor p_{ψ} . In this phase, for each input trajectory segment τ_H , the video tokenizer first converts it into a sequence of tokens $x_H =$ $((x_1^{(1)}, \dots, x_1^{(N)}), (x_2^{(1)}, \dots, x_2^{(N)}), \dots, (x_H^{(1)}, \dots, x_H^{(N)}))$, where $x_i^{(j)}$ represents the *j*-th token of the *i*-th frame. Consequently, the training objective of the dynamics model is to maximize the log-likelihood of the tokens x_{h+1} for the next frame s_{h+1} , conditioned on the history tokens $x_{0:h}$, history actions $a_{0:h}$ and the policy embedding $z_h = p_{\psi}(\tau_h)$:

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$$\mathcal{L}_{dyn}(\theta) = \mathbb{E}_{\tau_H \sim \mathcal{D}} \Big[-\sum_{h=1}^{H} \log P_{\theta}(x_{h+1} | x_{1:h}, a_{1:h}, z_h) \Big],$$
(5)

Intuitively speaking, Whale does not only accept history as a direct feature to predict transitions but
 also infers the latent decision intention from the history to enable test-time adaptation to the induced
 distribution shift.

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3.4 RETRACING ROLLOUT FOR COMPOUNDING ERROR REDUCTION

269 Model imagination involves rolling out a policy or executing an action sequence step-by-step within the world model. As highlighted in Eq (2), this process suffers from error compounding during test



Figure 3: Qualitative evaluation: long-horizon video generation results of Whale on Meta-World, Open X-Embodiment, and our Real-world tasks.

287 time due to the shift from teacher-forcing training objective to autoregressive generation, resulting 288 in a quadratic increase in model error as the decision horizon H extends. To mitigate this issue, 289 we propose a simple but effective technique, termed **retracing rollout**, as depicted in Figure 2. 290 Specifically, if the model imagination begins from a real initial observation o_1 with a context 291 length assumed to be 4, the context for standard autoregressive rollout to predict \hat{o}_{t+1} at timestep t is 292 $(\hat{o}_{t-3}, a_{t-3}, \hat{o}_{t-2}, a_{t-2}, \hat{o}_{t-1}, a_{t-1}, \hat{o}_t, a_t)$. Nevertheless, if the decision horizon significantly exceeds 293 the context length, the prediction context for later observations will consist entirely of model-generated images and actions. This causes early prediction errors to accumulate, leading to increasingly inaccurate subsequent predictions, a phenomenon commonly referred to as *compounding error*. To 295 mitigate this issue, our retracing rollout instead use the context $(o_1, \hat{a}_1, \hat{o}_{t-2}, a_{t-2}, \hat{o}_{t-1}, a_{t-1}, \hat{o}_t, a_t)$, 296 which fixes the first frame to be the initial real observation o_1 , and relabel the corresponding action 297 \hat{a}_1 to produces an equivalent effect on the robot's end-effector as executing the skipped actions 298 a_1, \ldots, a_{t-3} sequentially, starting from o_1 . 299

Benefiting from the semantic structure of the action space in embodied control, the action-retracing operation is computationally feasible for end-effector pose control. For instance, in the Open Xembodied dataset, the action space is defined by a 7-dimensional vector that controls the end-effector. The first three dimensions represent the changes in the gripper position (Δx , Δy , Δz), the next three represent the changes in wrist orientation (Δ roll, Δ pitch, Δ yaw), and the final dimension determines whether the gripper opens or closes. Therefore, the retrace action can be directly computed using Eq (6), where $a_i^{(j)}$ represents the value of the *j*-th dimension of the action a_i .

$$retrace(a_1, \cdots, a_t) = \left(\sum_{i=1}^t a_i^{(0)}, \sum_{i=1}^t a_i^{(1)}, \sum_{i=1}^t a_i^{(2)}, \sum_{i=1}^t a_i^{(3)}, \sum_{i=1}^t a_i^{(4)}, \sum_{i=1}^t a_i^{(5)}, a_t^{(6)}\right).$$
 (6)

The retracing rollout intuitively offers two key advantages. First, in long-horizon rollouts, it acts as a "fast track" connecting the initial observation to the predicted target, reducing the prediction error in the pose of the robot's arm. Second, by consistently incorporating the real initial observation o_1 into the model's context, the retracing rollout significantly improves the coherence and consistency of the generated trajectories. Notably, the retracing rollout operates without any modifications to the training process, making it a plug-and-play solution, offering both flexibility and ease of implementation.

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4 EXPERIMENT

We conduct extensive experiments on both simulated tasks and real-world tasks. The experimental design is primarily designed to answer the following key questions:

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- How does Whale perform compared with other baselines on simulated tasks? Are policyconditioning and retracing-rollout techniques effective? (Section 4.1)

- How does Whale perform on real-world tasks? Can Whale benefit from pre-training on internetscale data? (Section 4.2)
- How is Whale's scalability? Does increasing the model capacity or pre-training data improve performance on real-world tasks? (Section 4.3)

4.1 SIMULATION EVALUATION

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Experiment Setups We conduct our simulated task experiments on the Meta-World (Yu et al., 2019) benchmark, which offers a diverse set of vision-based manipulation tasks. In this experiment, we construct a training dataset with 60k trajectories collected from 20 tasks. The model learning algorithms are required to use all the data for training from scratch. During evaluation, given an initial observation and a sequence of actions, the world model should reconstruct the corresponding video trajectories. More detailed information about data collection can be found in Appendix D.1.

338 **Baselines** We compare Whale against several world model learning baselines, including 339 (1) FitVid (Babaeizadeh et al., 2021), a variational-based world model that can fit large diverse video datasets. (2) MCVD (Voleti et al., 2022), a diffusion-based world model that can perform video 340 generation conditioning on different subsets of video frames and actions. (3) DreamerV3 (Hafner 341 et al., 2023), a recurrent world model that outperforms specialized methods across diverse control 342 tasks. (4) iVideoGPT (Wu et al., 2024), a scalable transformer-based world model that achieved 343 state-of-the-art results in video generation and embodied control tasks. Complete descriptions and 344 implementation details are provided in Appendix B.2. 345

Evaluation Metrics The evaluation scenarios are divided into two categories: seen policies and 346 unseen policies. Specifically, seen policies involve tasks and action sequences that both appear in the 347 training set, *unseen policies* refer to tasks from the training set with action sequences generated by 348 unseen policies. Moreover, we assess the performance of world models from two perspectives: 1) 349 Video fidelity. Measures the quality of video trajectory generation, in terms of Fréchet Video Distance 350 (FVD) (Unterthiner et al., 2018), Peak Signal-to-noise Ratio (PSNR) (Huynh-Thu & Ghanbari, 2008), 351 Learned Perceptual Image Patch Similarity (LPIPS) (Zhang et al., 2018), and Structural Similarity 352 Index Measure (SSIM) (Wang et al., 2004). 2) Value estimation accuracy. Verifies whether the model 353 can correctly estimate the value of a given action sequence, in terms of Value Gap. 354

Comparison Results Table 1 presents the results for video fidelity and value estimation in the unseen policies setting. Our analysis shows that Whale outperforms all other methods across every metric related to video fidelity, with a notable advantage in FVD. ² Furthermore, the value estimation results demonstrate that Whale consistently matches or surpasses the baselines in minimizing the value gap for both seen and unseen policies, emphasizing its superior accuracy in value estimation. The remaining evaluation and visualization results can be found in Appendix C and F.1.

Meta-World	#Params	FVD↓	PSNR↑	SSIM↑	LPIPS↓	Value Gap \downarrow
		unseen polic	ries & 64×64	4 resolution		
FitVid	143M	154.6	23.7	90.3	6.5	11.1
MCVD	53M	272.8	29.7	92.3	4.0	15.9
DreamerV3	44M	142.7	27.6	92.1	4.3	5.3
iVideoGPT	63M	115.7	28.5	92.8	4.5	6.4
Whale (ours)	51M	33.0±1.4	29.8±0.0	94.4±0.0	3.2±0.0	5.6±0.3
unseen policies & 256×256 resolution						
DreamerV3	61M	112.4	26.2	91.7	8.5	7.5
Whale (ours)	63M	$\textbf{28.2}{\pm\textbf{3.6}}$	$\textbf{29.2}{\pm 0.2}$	$95.0{\pm}0.1$	4.3±0.1	5.0±0.2

Table 1: Performance comparison on Meta-World benchmark with various models.

²In the 64×64 resolution, retracing rollout was omitted due to inconsistencies in object appearance within the real videos, offering no added benefit in this context. However, at higher resolutions, retracing rollout led to a marked improvement, as demonstrated in Table 2 and Table 3.

378 Ablation Study To validate the effectiveness of policy-conditioned and retracing rollout techniques, 379 we conduct comprehensive ablation experiments under the unseen policies setting at a resolution of 380 256x256, as presented in Table 4 and Figure 4. The results show that the policy-conditioned method 381 effectively identifies and represents test policies, generating more realistic video trajectories and 382 reducing the value gap by 37%. Additionally, we find that retracing rollout provides significant improvements: without altering the training process, the FVD of trajectories generated by retracing rollout is only 33% of that produced by standard autoregressive rollout, while the value gap is reduced 384 to 50% of the original. These findings demonstrate that the policy-conditioning and retracing-rollout 385 mechanisms significantly enhance the generalizability of world models. For more results, please refer 386 to Appendix C. 387

Meta-World	FVD↓	PSNR↑	SSIM↑	LPIPS↓	Value Gap \downarrow
unsee	en policies &	256×256 r	esolution		
Whale (w/o retracing-rollout)	84.2±5.7	24.3±0.3	92.0±0.2	6.9±0.3	$10.0 {\pm} 0.6$
Whale (w/o policy-conditioning)	$32.0{\pm}0.4$	$28.9{\pm}0.2$	$94.6{\pm}~0.1$	$4.6 {\pm} 0.1$	$7.9{\pm}0.2$
Whale (ours)	$\textbf{28.2}{\pm\textbf{3.6}}$	$\textbf{29.2}{\pm 0.2}$	95.0±0.1	4.3±0.1	5.0±0.2

Table 2: Ablation Study of Whale on Meta-World benchmark.

4.2 Physical Robot Evaluation

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Pre-training. We present Whale-X, a 414M parameter world model pre-trained on 970K real-world
robot demonstrations from Open X-Embodiment datasets. We use the entire dataset to pre-train
both the policy embedding model and the video tokenizer, selectively using a subset of the data
to pre-train the dynamics model. Whale-X serves as a foundational embodied world model for
evaluating real-world behaviors, capable of generating realistic and controllable video trajectories
that align with the given actions, as shown in Figure 3. Additional details on the pre-training process
and the generated results can be found in Appendix D.2 and Appendix F.3, respectively.

Experiment Setups. To evaluate the out-of-distribution generalizability of Whale-X in the physical
 world, we conduct comprehensive real-world experiments on ARX5 robotic platform. The evaluation
 tasks differ significantly from the pre-training data, in terms of the robotic platform, camera angles,
 and background visual information, posing considerable challenges for world models.

We carefully collect a limited dataset for fine-tuning, consisting of 60 trajectories for each of the four tasks: *open bin, push plate, throw ball,* and *move bottle.* Following this, we designed several challenging unseen tasks for testing, with a focus on evaluating the model from the perspectives of *visual generalization, motion generalization,* and *task generalization* perspectives. Further details on the data collection process can be found in Appendix E.

416 **Evaluation Metrics.** Given an initial frame and a sequence of subsequent actions, world models 417 should autoregressively generate future video trajectories. For a visual world model to be effective 418 in decision-making, it needs to focus more on reasoning about the consequences of actions than on 419 reconstructing irrelevant visual information like backgrounds. Thus we introduce the consistency 420 rate to assess whether the differences in reconstructed object positions, interactive object states, 421 and robot arm positions fall within an acceptable range compared to the ground truth. We use the 422 multimodal large model GPT-40 (Achiam et al., 2023) for this evaluation through multiple rounds 423 of Q&A. Details of the prompts and the evaluation process can be found in the Appendix H, with results presented in Figure 4. In addition, we employ several video fidelity metrics, similar to those 424 in Section 4.1, to assess the quality of video generation by the world models. 425

Task Results Whale-X model shows a clear advantage in our real-world experiments. Specifically, as shown in Figure 4, the quantitative results indicate that: 1) Whale-X improves consistency by
63% and 30% compared to models without policy-conditioning and retracing-rollout respectively, demonstrating that these mechanisms significantly enhance the OOD generalizability; and 2) Whale-X, pre-trained on 970k samples, achieved much higher consistency rate than models trained from scratch, highlighting the benefits of pre-training on large-scale internet data. Furthermore, the evaluation of video generation quality aligns with these consistency rate findings as illustrated in



Figure 4: The results of physical robot evaluation on unseen scenarios. The row above shows the bar chart of the consistency rate, and the row below represents the tasks used for testing. The experiments demonstrate that Whale-X exhibits good generalization performance in unseen scenarios, and both the proposed policy-conditioning and retracing-rollout can enhance the model's performance.

Real-world Tasks	PSNR ↑	SSIM↑	LPIPS↓
unseen tasks & $256 \times$	256 resolu	tion	
Whale-X (training from scratch)	20.0	74.9	37.0
Whale-X (w/o retracing-rollout)	21.9	79.6	30.3
Whale-X (w/o policy-conditioning)	21.4	79.0	31.2
Whale-X (ours)	22.3	80.5	29.6

Table 3: Video Fidelity of Whale-X on real-world tasks.



Figure 5: Scaling Experiment Results of Whale-X. The leftmost plot shows the training loss curves for models with varying parameter sizes during the pre-training phase. The second plot presents the final training loss for all models after 300k pre-training steps. The third plot displays the test loss after fine-tuning. The legend in the figure indicates the parameter number of the dynamics model.

Table 3: both policy-conditioning and retracing-rollout techniques boost OOD generalizability and significantly outperform models lacking pre-training.

4.3 SCALING EXPERIMENTS

In this section, we aim to investigate the scaling behavior of Whale-X. Specifically, We freeze the video tokenizer and policy embedding model, adjusting only the model size and pre-training data size of dynamics models, considering the impact of model size and data size for the pre-training and fine-tuning phases.

Pre-training Scaling Experiments. With a freezed video tokenizer and policy embedding model, we train four dynamics models ranging from 39M to 456M parameters during the pre-training phase, with results shown in the first two plots of Figure 5. These results demonstrate that Whale-X exhibits strong scalability, as increasing either the pre-training data or the number of parameters reduces the training loss. Notably, the training loss of Whale-X follows a log-linear relationship with FLOPs, which can guide the design of larger models and appropriate data ratios for future experiments.

Fine-tuning Scaling Experiments. Apart from the scalability in the pre-training stage, it is also worth verifying whether a larger model can exhibit better performance during the fine-tuning phase. To this end, we fine-tune a series of dynamics models and show the test mean-squared-error losses in the leftmost plot in Figure 5. The results indicate that after fine-tuning, the larger model demonstrates lower loss on test data, highlighting promising scalability of Whale-X for real-world tasks.

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5 RELATED WORKS

500 Learning accurate dynamics models has been a long-standing challenge in sequential decision-making. 501 Many works focused primarily on learning transition models in lower-dimensional proprioceptive 502 state spaces from the perspective of model architecture (Chua et al., 2018; Zhang et al., 2021; Janner et al., 2021; Chen et al., 2024b) or learning objective (Xu et al., 2020; Chen et al., 2023; Luo et al., 504 2024a; Lin et al., 2024). The environment model learning provides benefits for downstream tasks, 505 especially model-based reinforcement learning (Janner et al., 2019; Yu et al., 2020; 2021; Sun et al., 2023). Recent research interest has shifted towards learning environment models for high-dimensional 506 image-based tasks (Hafner et al., 2020; Babaeizadeh et al., 2021; Yang et al., 2024), commonly 507 referred to as world models (Ha & Schmidhuber, 2018). 508

509 Some recent model-based RL algorithms leverage latent imagination for more efficient and accurate 510 rollouts (Hafner et al., 2020; 2021; 2023; Hansen et al., 2022; Schrittwieser et al., 2020), but they become more complex by tightly coupling model and policy learning. Advanced methods leverage 511 modern action-conditioned video prediction models (Oh et al., 2015; Kaiser et al., 2020) to model 512 the visual dynamics and pre-train from large-scale video experience data (Mendonca et al., 2023b; 513 Wu et al., 2023). Various models have been adopted in these methods, including RNNs (Villegas 514 et al., 2019; Hafner et al., 2020; Babaeizadeh et al., 2021), diffusion models (Voleti et al., 2022), 515 and transformers (Gupta et al., 2023; Wu et al., 2024). These interactive models generate videos 516 under the control of the executed actions, with the goal of capturing real visual dynamics for 517 various decision strategies. However, these works have not emphasized the generalizability of world 518 models, which is crucial for sequential decision-making but has not been well addressed by previous 519 approaches (Schubert et al., 2023). In contrast, our work focuses on the world model generalizability 520 from a perspective of evaluation accuracy and utilizing model adaptation to policies and retracing 521 rollout to mitigate the generalization error in scalable world models.

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6 DISCUSSIONS AND LIMITATIONS

 We introduce Whale, a scalable and generalizable embodied world model that incorporates the policyconditioning mechanism and retracing-rollout technique to enhance out-of-distribution generalization, and pre-train a 414M-parameter Whale-X on large-scale real-world robot data to assist physical robot manipulation. As a powerful world model with strong generalizability and promising scalability, Whale enables high-fidelity imagination and accurate value estimation, even in novel scenarios, thereby facilitating downstream control tasks.

531 **Limitations and future work.** Although Whale-X marks significant progress, there remains 532 substantial room for further improvement in future work. One limitation is the lack of diversity in 533 real-world robotic data, typically collected by a narrow range of policies (e.g. near-optimal policies). 534 This poses significant challenges to the generalization of world models. Additionally, we found that the quality of reward models with visual input plays a crucial role in accurate value estimation, which 536 remains an unsolved challenge for future research. Lastly, we have to mention that although Whale's 537 generalization capability has significantly improved compared with previous methods, it remains limited for zero-shot transfer in the face of the diversity and complexity of unseen real-world tasks. 538 Integrating existing prior knowledge into the data-driven world model learning process could enable broader generalization, presenting a valuable avenue for long-term research.

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864 А ANALYSIS OF POLICY CONDITIONING 865

In this section, we provide some theoretical explanations about why policy-conditioning mechanism helps mitigate the generalization error caused by the policy divergence. The analysis is mainly adapted from Chen et al. (2024a).

First, we introduce an assumption on the smoothness of a well-trained dynamics model:

Assumption A.1 For the learned dynamics model T, the point-wise total-variation model error $D_{\rm TV}[T^*(\cdot|\tau_h), T(\cdot|\tau_h)]$ is L-Lipschitz with respect to the trajectory inputs, i.e.,

 $\left| D_{\mathrm{TV}}[T^*(\cdot|\tau_h^1), T(\cdot|\tau_h^1)] - D_{\mathrm{TV}}[T^*(\cdot|\tau_h^2), T(\cdot|\tau_h^2)] \right| \le L \cdot D(\tau_h^1, \tau_h^2),$

where $D(\cdot, \cdot)$ is some kind of distance defined on the trajectory space.

Assumption A.1 measures the local extrapolation ability of a world model. Based on this assumption, the value gaps of common dynamics model T without a policy-conditioning mechanism can be controlled:

Proposition A.2 Under Assumption A.1, for any policy π , the value gap of common dynamics model T without policy conditioning has an upper bound:

$$\left| V_T^{\pi} - V_{T^*}^{\pi} \right| \le 2R_{\max} H^2 \left(\underbrace{\sqrt{2 \, l_{\mathrm{KL}}(T;\Pi)}}_{\text{Train Error}} + \underbrace{L \cdot W_1(d^{\pi}, d^{\Pi})}_{\text{Policy Divergence Error}} \right)$$

where $W_1(d^{\pi}, d^{\Pi})$ is the Wasserstein-1 distance between the π -induced trajectory distribution $d^{\pi}(\tau)$ and the behavior trajectory distribution $d^{\Pi}(\tau) = \mathbb{E}_{\mu \sim \Pi}[d^{\mu}(\tau)].$

889 Proposition A.2 shows that the generalization of common dynamics model T solely relies on its point-890 level smoothness over the trajectory inputs, resulting in an inevitable extrapolation error of the policy distribution. In contrast, a policy-conditioned dynamics model $T(\cdot)$, which yields adapted dynamics 892 model $T(\pi)$ for some policy π , takes a further step to reduce the policy distribution extrapolation 893 error: 894

Proposition A.3 Under Assumption A.1, for any policy π , the value gap of policy-conditioned dynamics model $T(\cdot)$ has an upper bound:

$$\left|V_{T(\pi)}^{\pi} - V_{T^*}^{\pi}\right| \leq 2R_{\max}H^2\Big(\underbrace{\sqrt{2\,l_{\mathrm{KL}}(T;\Pi)}}_{\text{Train Error}} + \underbrace{L \cdot W_1(d^{\pi}, d^{\Pi}) - C(\pi, \Pi)}_{\text{Reduced Policy Divergence Error}}\Big),$$

where the adaptation gain $C(\pi, \Pi) := \mathbb{E}_{\mu \sim \Pi} \mathbb{E}_{\tau \sim d^{\pi}} D_{\mathrm{TV}}[T^*, T(\mu)](\tau) - \mathbb{E}_{\tau \sim d^{\pi}} D_{\mathrm{TV}}[T^*, T(\pi)](\tau)$ summarizes the policy adaptation effect. 902

903 Proposition A.3 explains the benefit brought by policy-conditioning: a positive adaptation gain 904 $C(\pi, \Pi)$, which quantifies the advantage of the policy adaptation effect. The key insight is that when 905 testing on an unseen policy π within some effective region, the model $T(\pi)$, customized for π , should 906 exhibit a smaller model error under the target trajectory distribution d^{π} compared to models $T(\mu)$ 907 trained on behavior policies $\mu \in \Pi$, which mitigates the generalization error caused by the policy extrapolation. Although it is challenging to rigorously analyze the adaptation gain $C(\pi, \Pi)$ due to the 908 complexity of neural networks and the optimization process, qualitative discussions and empirical 909 evidence, as shown in Chen et al. (2024a), justify the underlying rationale. 910

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В **IMPLEMENTATION DETAILS**

914 IMPLEMENTATION DETAILS OF WHALE **B**.1

Video Tokenizer. Here we show the architecture and training hyperparameter of the video tokenizer 916 as shown in Table 4. We train three different video tokenizers in total, and our model architecture and 917 training parameter selection are based on the design of Bruce et al. (2024).

Component	Parameter	Meta-World $_{(64 \times 64)}$	Meta-World $_{(256 \times 256)}$	Whale- $X_{(256 \times 256)}$
	num_layers	4	12	12
Encoder	d_model	512	512	512
	num_heads	8	8	8
	num_layers	8	16	20
Decoder	d_model	512	512	1024
	num_heads	8	8	16
	num_codes	1024	1024	2048
Cadabaalt	patch_size	4	16	16
Decoder Codebook	latent_dim	32	32	32
	beta	0.25	0.25	0.25
	type	AdamW	AdamW	AdamW
	max lr	3e-4	3e-4	3e-4
	min_lr	3e-4	3e-4	3e-5
	β_1^-	0.9	0.9	0.9
Optimizer	β_2	0.9	0.9	0.9
	weight_decay	1e-4	1e-4	0
	warmup_steps	10k	10k	5k
	batch_size	32	32	64
	training_steps	100k	150k	300k

Table 4: Hyperparameter of video tokenizers.

Policy Embedding Model. The model architecture and training hyperparameters of the policy embedding model are shown in Table 5. We also train three different policy embedding models. We use two-hot encoding for the practical implementation of our policy embedding similar in Hafner et al. (2020). Additionally, We also observe overfitting in the policy embedding model during pre-training, prompting the use of the early-stop technique. As a result, the checkpoint at 50k is selected as the final model for Whale-X.

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950 **Dynamics model** Table 6 and Table 7 present the hyperparameters of the dynamics model. We train a total of 6 different dynamics models. The architecture design and training hyperparameters of our dynamics model are also referred to Bruce et al. (2024). 952

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B.2 IMPLEMENTATION DETAILS OF BASELINES

We use the official implementation of VP2 (Tian et al., 2023) for both FitVid and MCVD. For DreamerV3, we retain only the world model learning component. Additionally, we use the official implementation of iVideoGPT as described in their original paper, but with a reduced number of parameters. The detailed hyperparameters for DreamerV3 and iVideoGPT are provided in Table 8 and Table 9, respectively.

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С ADDITIONAL EXPERIMENTS RESULTS

Benchmark results. The omitted benchmark results on simulated tasks are shown in Table 10. This table presents the evaluation results of trajectories generated by the world model, conditioned on action sequences produced by policies seen in the training dataset.

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Ablation studies. The omitted ablation studies results on simulated tasks are shown in Table 11, 970 showcasing both retracing rollout and policy conditioning consistently effective in seen policies 971 setting.

Component	Parameter	$\textbf{Meta-World}_{(64\times 64)}$	$\textbf{Meta-World}_{(256\times 256)}$	Whale- $X_{(256 \times 256)}$
	num_layers	8	8	12
Destarior	d_model	512	512	768
FOSTELLOI	num_heads	8	8	12
	patch_size	8	32	32
	num_layers	4	4	8
Prior	d_model	512	512	512
1 1101	num_heads	4	4	8
	patch_size	8	32	32
	num_layers	8	8	12
Policy	d_model	512	512	768
Toncy	num_heads	8	8	12
	log_std	[-2, 5]	[-2, 5]	[-2, 5]
	patch_size	8	32	32
Embedding	category_size	16	16	16
Embedding	class_size	16	16	16
	type	AdamW	AdamW	AdamW
	max_lr	3e-4	3e-4	3e-4
	min_lr	3e-5	3e-5	3e-5
	β_1	0.9	0.9	0.9
Ontimizer	β_2	0.9	0.9	0.9
Optimizer	weight_decay	1e-4	1e-4	1e-4
	warmup_steps	5k	5k	5k
	batch_size	64	64	64
	training_steps	100k	100k	50k

Table 5: Hyperparameter of policy embedding models.

Model	#Parameters (dynamics only)	num_layers	num_heads	d_mode
Whale-Meta64	26M	12	8	512
Whale-Meta256	26M	12	8	512
Whale-X-small	39M	18	8	512
Whale-X-medium	77M	16	16	768
Whale-X-base	204M	24	16	1024
Whale-X-large	456M	24	12	1536

Table 6: Model hyperparameter of dynamics models.

Parameter	Value
max_lr	3e-5
min_lr	3e-6
β_1	0.9
β_2	0.9
weight_decay	0
warmup_steps	5k
batch_size	64
training_steps	300k

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Table 7: Trainig hyperparameter of dynamics models.

		Hyperparameters	Values
Hyperparameters	Values	# Parameters	63M
# Parameters	44M	Down blocks	3
Dynamics hidden	1024	Down layers per block	2
Dynamics deterministic	1024	Down channels	[64, 128, 256]
Dynamics stochastic	32	Up blocks	3
Dynamics discrete	32	Up layers per block	3
CNN depth	64	Up channels	[256, 128, 64]
CNN kernel size	4	Embedding dim	64
MLP layers	5	Codebook size	8192
MLP units	1024	Actionvation	SiLU
Actionvation	SiLU	Transformer hidden dim	512
Train batch size	32	Transformer hidden layers	6
Train batch length	8	Attention Heads	8
		Feedforward dim	1024

Table 9: Hyperparameters for iVideoGPT.

Meta-World	$FVD\downarrow$	PSNR↑	SSIM↑	LPIPS↓	Value Gap \downarrow			
	seen policies & 64×64 resolution							
FitVid	193.2	23.7	90.3	6.4	9.7			
MCVD	271.7	30.1	92.8	3.8	12.2			
DreamerV3	145.8	28.3	92.8	4.0	4.4			
iVideoGPT	122.0	30.4	93.3	4.4	4.5			
Whale (ours)	28.4±1.1	$31.3{\pm}0.01$	95.3±0.03	$2.9{\pm}0.05$	$\textbf{4.7} \pm \textbf{0.47}$			
seen policies & 256×256 resolution								
DreamerV3	105.1	26.8	92.1	8.2	6.2			
Whale (ours)	$\textbf{25.2}{\pm}\textbf{ 3.0}$	30.1±0.2	95.4±0.1	4.0±0.1	$\textbf{3.9} \pm \textbf{0.3}$			

Table 10: Benchmark results in seen policies setting.

D DATA PREPARATION

1062 D.1 SIMULATED DATA

We select a total of 20 tasks from the MetaWorld benchmark. Each task includes a training set of 3,000 trajectories and a test set of 1,500 trajectories. Specifically, for each task, we use six different policies to collect the training set: expert policy, random policy, two suboptimal policies with different levels of Gaussian noise, and two cross-environment policies. Additionally, three unseen policies are used to gather the testing data. The world models are trained on the full training dataset, followed by a thorough evaluation using the testing data.

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1071 D.2 PRE-TRAINING DATA

We pretrain our Whale-X model on the Open X-Embodiment dataset (Collaboration et al., 2023) (OpenX). The full OpenX dataset consists of more than 70 individual robot datasets, with more than 2M robot trajetories, that were pooled into a coherent and easy-to-use data format in a large community effort. We list our used data mixture in Table 12, mostly following OpenVLA (Kim et al., 2024) and Octo (Octo Model Team et al., 2023).

To train a world model focused on tabletop tasks, we extract data related to tabletop tasks from the
 dataset that features similar camera positions (the bolded tasks in Table 12) to train the dynamics
 model, while the video tokenizer and policy condition model are trained on the full OpenX dataset.

Meta-World	FVD↓	PSNR ↑	SSIM↑	LPIPS↓	Value Gap \downarrow
se	en policies &	256×256 res	solution		
Whale (wo retracing rollout) Whale (wo policy-conditioned)	$63.4{\pm}23.6$ 28.4 ${\pm}1.1$	25.5 ± 0.7 29.5 ± 0.2	$92.8 {\pm} 0.5$ $95.0 {\pm} 0.1$	$_{4.5\pm0.1}^{6.2\pm0.6}$	$7.5{\pm}1.0$ $4.9{\pm}0.1$
Whale	25.2±3.0	30.1±0.2	95.4±0.1	4.0±0.1	3.9±0.3
Table 11: Abl	lation Study of	f Whale in se	en policies	setting.	
Whole Y Pro trai	ning Datasat	Mixturo		Dorcontago	
Fractal (Broban et		wiixtuie		12.7%	
Kuka (Kalashnikov	v et al (2022)			12.7%	
Bridge (Ebert et al.	. 2021: Walke	et al., 2023)		13.3%	
Taco Play (Rosete-	Beas et al., 20	022; Mees et	al., 2023)	3.0%	
Jaco Play (Dass et	t al., 2023)	,	, ,	0.4%	
Berkeley Cable Ro	outing (Luo et	al., 2023)		0.2%	
Roboturk (Mandle	ekar et al., 201	18)		2.3%	
Viola (Zhu et al., 2	2023b)			0.9%	
Berkeley Autolab	UR5 (Chen et	al.)		1.2%	
Toto (Zhou et al., 2	2023)			2.0%	
Language Table (Lynch et al., 2	2023)	22)	4.4%	
Stanford Hydra L	Jataset (Belkh	ale et al., 20	23)	4.4%	
Austin Buds Datas	Deteget (Cui et al.,	2022)		0.2%	
NYU Franka Play Furnitura Banch D	Dalasel (Cui e	a1, 2022)		0.8%	
UCSD Kitchen Da	taset (Yan et a	1, 2023		2.4%	
Austin Sailor Data	set (Nasirianv	et al 2023)		2.2%	
Austin Sirius Data	set (Liu et al	2023)		1.7%	
DLR EDAN Share	d Control (Ou	ere et al., 20	20)	< 0.1%	
IAMLab CMU Pic	kup Insert (Sa	xena et al., 2	2023)	0.9%	
UTAustin Mutex	(Shah et al., 20	023)	,	2.2%	
Berkeley Fanuc M	anipulation (Z	hu et al., 202	23a)	0.7%	
CMU Stretch (Mer	ndonca et al., 2	2023a)		0.2%	
BC-Z (Jang et al.,	2022)			7.5%	
FMB Dataset (Luc	et al., 2024b)	1		7.1%	
DobbE (Shafiullah	et al., 2023)			1.4%	
DROID (Khazatsk	y et al., 2024)			10.0%	
Table 12	· Whale-X Pro	e-training Da	taset Mixtu	re	
14010-12	. ,, in nuite=2x 1 10	c training Da			
E REAL-WORLD TASK D	ESIGN				
E.1 HARDWARE SETUP					
Dur hardware setup is shown in F	Figure 6. For t	he embodim	ent, we use	the ARX5 ro	botic platform
which is similar to Aloha (Fu et a	1., 2024) and in	ncludes two	master arms	and two pup	pet arms. Data
Realsense D435i camera is mo	we only use the	the left side	of the platfo	ment. FOF th	re RGR image
bservations		ine fert slue	or the platte	mi to captu	it KOD illiage
E.1.1 DETAILS OF TASKS					
The training data set used for find not	etuning consis	sts of 4 tasks	: Move Bot	tle, Open B	in, Push Plate,







specific task from pushing left to right in the fine-tuning data to pushing right to left. This task is designed to evaluate the model's ability to generalize environment transition modeling when facing an unseen action distribution, or even a completely reversed action distribution.
 Task Generalization: In this unseen scenario, we combined two tasks from the fine tuning

Task Generalization: In this unseen scenario, we combined two tasks from the fine-tuning phase—Open Bin and Throw Ball—into a new two-stage task. In this task, the robot arm must first open the bin and then place the ball inside. This task is designed to test the model's generalization ability to new tasks, as well as its capability to model long-horizon actions.

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E.2 DATA OVERVIEW

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1210	Entry	Value			
1220	# Episodes	300(240 for fine-tuning, 60 for testing)			
1221	Average horizon	30			
1222	Data Collect Method	Human teleoperation using the master arm			
1223	Scene Type	Table top			
1004	Robot Morphology	Single arm			
1224	Camera resolution	640x480			
1225	# Cameras	1			
1226	Action dimension	7			
1227	Action space	EEF position			
1228	Action semantics	$(\Delta x, \Delta y, \Delta z, \Delta roll, \Delta pitch, \Delta yaw, the gripper state)$			
1229	Control frequency	5Hz			
1230	Has suboptimal?	Yes(some failure data for fine-tuning)			
1231	Has camera calibration?	No			

Table 13: The meta Information of data used in physical robot evaluation.

1236 F QUALITATIVE EVALUATION

1238 F.1 QUALITATIVE EVALUATION ON SIMULATED TASK

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Figure 9 shows the results of Whale and baselines after rolling out 64 steps in two different tasks.
 Notably, this qualitative evaluation is highly challenging and presents significant complexities. First, the evaluation rollout horizon is set to 64, exceeding that used in prior works, which imposes

1242 substantial demands on the generalizability and robustness of world models. Moreover, the variations 1243 between adjacent frames are subtle in the Meta-World environment, requiring world models to learn 1244 the semantics of actions from these minimal changes. In each image, the first row represents the real 1245 trajectory, while the others show the generated trajectories. It can be observed that Whale not only 1246 generates high-fidelity videos but also accurately restores the robot arm's pose. DreamerV3 is the baseline closest to Whale, but its generated trajectory still loses key information, such as the blue 1247 marker representing the target point. The other baselines fail to accurately model the robot arm's 1248 pose changes from the subtle variations between adjacent frames. 1249



Figure 9: Additional qualitative evaluation on the Meta-World dataset.

1281 F.2 QUALITATIVE EVALUATION ON OPEN X-EMBODIMENT DATASET 1282

Figure 10 shows the qualitative evaluation results of Whale-X on Open X-Embodiment dataset. 1283 Whale-X demonstrates a remarkable ability to generate high-fidelity, action-conditioned trajectories. 1284 Moreover, with the aid of retracing-rollout and policy-conditioning techniques, Whale-X consistently 1285 delivers highly accurate predictions of the robotic arm's pose. 1286

1287 F.3 QUALITATIVE EVALUATION ON REAL-WORLD TASK 1288

Figure 11 shows the qualitative evaluation results of Whale-X on Real-world Tasks. Whale-X demonstrates strong generalizability in terms of motion, visualization, and task combination.

POLICY EMBEDDING ANALYSIS G

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In this section, we conduct experiments to visualize the policy embeddings via t-SNE (Van der 1295 Maaten & Hinton, 2008) in order to verify whether our method can learn reasonable representations.





Figure 12: The policy embedding visualization via t-SNE (Van der Maaten & Hinton, 2008). The different colors denotes different policies in the same task (12a) and different tasks' expert policies (12b) or random policies (12c). The separability validates the ability of the embeddings learned by our method to represent different policies.

1404 H GPT-40 EVALUATION DETAILS

1406 1407 H.1 Q&A EXAMPLE

We use the large vision language model GPT-40 for evaluation in the physical robot experiment. Generally, we input the real final frame and the model-generated final frame to GPT-40, using natural language dialogue to enable GPT-40 to assess whether the generated errors in key information such as the robot arm's position and the status of interactive objects fall within an acceptable range, thus determining whether the generated results are consistent with reality. Figure 13 shows one of our dialogue examples with GPT-40. We use multi-turn dialogue to enable the model to easily process and infer information from images.

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1416 H.2 ALL GPT-40 PROMPTS

Table 14 contains all the prompts we used with GPT-40 for evaluation in unseen scenarios. The prompts evaluate various criteria by listing factors such as the robotic arm's position and the status of interactive objects.

Visual GeneralizationHere are two images. The first image is the last frame of a real scene, and I will pr you with another image predicted by a model. The task is to open the trash bin t an unseen background. The trash bin is on the left side of the desk and is clos the beginning. You need to determine if the two images are consistent based of following criteria: 1) You can see the inside of the trash bin. 2) Is the predicted i clear? When all these criteria are satisfied, we call the predicted image is consistent based on the real one. Now I will show you the real image.MotionGeneraliza- tionHere are two images. The first image is the last frame of a real scene, and I will pr you with another image predicted by a model. You need to determine if the two in are consistent based on the following criteria: 1) Is the plate's position on the left of the image? 2) Does the plate disappear in the predicted image? 3) Is the predi- image clear? 4) Is the robot arm sill present in the predicted image? 5) Doo position of the robot arm in the predicted image is consistent with the one. Now I will show you the real image.Task GeneralizationHere are two images. The first image is the last frame of a real scene, and I will pr you with another image predicted by a model. You can see the inside of the image clear? 4) Is the robot arm in the predicted image is consistent with the one. Now I will show you the real image.Task GeneralizationHere are two images. The first image is the last frame of a real scene, and I will pr you with another image predicted by a model. You can see the inside of the bin. 2) The ball should be simply missing and not on the desk. 3) Is there any s distortion in the predicted image? 4) Is the position of the robot arm in the predi- image not far away from that of the real image? When all these criteri	Task	Prompt
Motion tionGeneraliza- tionHere are two images. The first image is the last frame of a real scene, and I will pr you with another image predicted by a model. You need to determine if the two in are consistent based on the following criteria: 1) Is the plate's position on the lef of the image? 2) Does the plate disappear in the predicted image? 3) Is the predi- image clear? 4) Is the robot arm still present in the predicted image? 5) Doe position of the robot arm in the predicted image match that of the real image? V all these criteria are satisfied, we call the predicted image is consistent with the one. Now I will show you the real image.Task GeneralizationHere are two images. The first image is the last frame of a real scene, and I will pr you with another image predicted by a model. You need to determine if the two in are consistent based on the following criteria: 1) You can see the inside of the bin. 2) The ball should be simply missing and not on the desk. 3) Is there any s distortion in the predicted image? When all these criteria are sati we call the predicted image? When all these criteria are sati we call the predicted image is consistent with the real one. Now I will show you real image.Table 14: The prompt used for 3 unseen tasks.	Visual Generalization	Here are two images. The first image is the last frame of a real scene, and I will provi you with another image predicted by a model. The task is to open the trash bin und an unseen background. The trash bin is on the left side of the desk and is closed the beginning. You need to determine if the two images are consistent based on t following criteria: 1) You can see the inside of the trash bin. 2) Is the predicted image clear? When all these criteria are satisfied, we call the predicted image is consistent with the real one. Now I will show you the real image.
Task GeneralizationHere are two images. The first image is the last frame of a real scene, and I will pr you with another image predicted by a model. You need to determine if the two in are consistent based on the following criteria: 1) You can see the inside of the bin. 2) The ball should be simply missing and not on the desk. 3) Is there any s distortion in the predicted image? 4) Is the position of the robot arm in the predi image not far away from that of the real image? When all these criteria are sati we call the predicted image is consistent with the real one. Now I will show yo real image.Table 14: The prompt used for 3 unseen tasks.	Motion Generaliza- tion	Here are two images. The first image is the last frame of a real scene, and I will provi you with another image predicted by a model. You need to determine if the two image are consistent based on the following criteria: 1) Is the plate's position on the left si of the image? 2) Does the plate disappear in the predicted image? 3) Is the predict image clear? 4) Is the robot arm still present in the predicted image? 5) Does the position of the robot arm in the predicted image match that of the real image? Wha all these criteria are satisfied, we call the predicted image is consistent with the re- one. Now I will show you the real image.
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		Table 14: The prompt used for 3 unseen tasks.
I.3 MORE EVALUATION RESULTS	I.3 MORE EVALUATI	on Results

1455 Whale-X (w/o retracing-rollout), and Whale-X (training from scratch) on the Motion Generalization

task. Figure 22 23 24 25 show the evaluation results for Whale-X, Whale-X (w/o policy conditioning),

1457 Whale-X (w/o retracing-rollout), and Whale-X (training from scratch) on the Task Generalization task.











Figure 19: The example of GPT-40 evaluation for Whale-X(w/o policy-conditioning) on the Motion Generalization Task.











Figure 22: The example of GPT-40 evaluation for Whale-X on the Task Generalization Task.

