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# Modeling variable guide efficiency in pooled CRISPR screens with ContrastiveVI+

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## Abstract

1 Genetic screens mediated via CRISPR-Cas9 combined with high-content readouts  
2 have emerged as powerful tools for biological discovery. However, computational  
3 analyses of these screens come with additional challenges beyond those found with  
4 standard scRNA-seq analyses. For example, perturbation-induced variations of  
5 interest may be subtle and masked by other dominant source of variation shared with  
6 controls, and variable guide efficiency results in some cells not undergoing genetic  
7 perturbation despite expressing a guide RNA. While a number of methods have been  
8 developed to address the former problem by explicitly disentangling perturbation-  
9 induced variations from those shared with controls, less attention has been paid  
10 to the latter problem of noisy perturbation labels. To address this issue, here we  
11 propose ContrastiveVI+, a generative modeling framework that both disentangles  
12 perturbation-induced from non-perturbation-related variations while also inferring  
13 whether cells truly underwent genomic edits. Applied to three large-scale Perturb-  
14 seq datasets, we find that ContrastiveVI+ better recovers known perturbation-  
15 induced variations compared to previous methods while successfully identifying  
16 cells that escaped the functional consequences of guide RNA expression.

## 17 1 Introduction

18 Advances in single-cell genomics technologies have enabled the profiling of molecular modalities  
19 across the central dogma at an unprecedented resolution. Moreover, recently developed genetic  
20 screening protocols combining CRISPR-Cas9-mediated genome editing with high-content single-cell  
21 readouts, such as Perturb-seq [1], hold major promise for identifying the genetic bases of functional  
22 phenotypes. Such screens are often conducted in a pooled fashion [2], in which a CRISPR guide  
23 RNA (gRNA) library is introduced in bulk to a cell population. Individual cells subsequently receive  
24 different gRNAs corresponding to different gene perturbations, and the specific perturbation induced  
25 in a cell can be determined by recovering the barcode sequence corresponding to an individual gRNA.

26 Despite the enormous potential of high-content genetic screens, computational analyses of these  
27 datasets are unfortunately beset by numerous challenges. Beyond confounding technical sources  
28 of noise present in scRNA-seq data generally, such as differences in sequencing depth and over-  
29 dispersion in RNA counts, analyses of pooled CRISPR datasets present an additional unique set  
30 of difficulties. For example, perturbation-induced variations in the data may be relatively subtle  
31 compared to those due to other biological processes, such as cell-cycle-related variations or those  
32 due to cellular stress responses [3]. Thus, standard single-cell analysis techniques, such as principal  
33 component analysis or generative modeling approaches (e.g. scVI [4]) may fail to capture perturbation  
34 effects, as these methods prioritize capturing factors with the highest variance across an entire dataset.

35 To work around this issue, a line of recent work [5, 6, 7, 8] has developed so-called contrastive latent  
36 variable models (cLVMs) based on the principle of contrastive analysis [9]. Such models explicitly

37 disentangle perturbation-induced variations into a set of *salient* latent variables while factors of  
 38 variation present in both control and perturbed samples are segregated into a second set of *background*  
 39 variables. While cLVMs have shown promise for analyzing pooled CRISPR datasets [5, 6], their  
 40 assumed generative processes disagree with the structure of pooled genetic screens in two important  
 41 ways. First, while pooled screens measure the effects of many perturbations in a single experiment,  
 42 standard cLVM models assume a single prior distribution over the salient variables for all perturbed  
 43 samples. Such models thus may fail to discern perturbations with small effect sizes due to shrinkage  
 44 toward the shared prior. Second, variable guide efficiency results in a subset of cells escaping the  
 45 effects of perturbation and acting as control cells despite being labeled with a perturbation [3]. Thus,  
 46 even when restricted to a single perturbation, the assumption of a single unimodal prior leads to  
 47 nontrivial model misspecification.

48 To resolve these issues, here we introduce ContrastiveVI+, an extension of ContrastiveVI, a previously  
 49 proposed cLVM for scRNA-seq data, that explicitly accounts for the additional structure in pooled  
 50 genetic screening datasets. The remainder of this work proceeds as follows. In Section 2 we review  
 51 cLVMs and related work. We then proceed to describe our proposed generative process (Section 3)  
 52 and our corresponding inference procedure (Section 4). In Section 5 we apply our method to three  
 53 pooled genetic screening datasets with scRNA-seq readouts, and we find that ContrastiveVI+ learns  
 54 representations that exhibit better agreement with prior biological knowledge compared to baseline  
 55 methods while also successfully identifying cells that escaped perturbation.

## 56 2 Background: Contrastive Latent Variable Models

57 Recall that the goal of CA is to disentangle novel perturbation-induced factors of variation from  
 58 those shared with control samples. To formalize this idea, a number of recent works [7, 8, 6, 5]  
 59 have developed contrastive latent variable models (cLVMs) using the following framework. Letting  
 60  $x_i$  denote a perturbed sample (e.g. a cell infected with a non-control gRNA), we assume that  $x_i$  is  
 61 generated from a random process parameterized by  $\theta$  and conditioned on two sets of latent variables  
 62  $z_i$  and  $t_i$ , i.e.,

$$x_i \sim p_\theta(x_i | z_i, t_i)$$

63 Here  $t_i$  denotes a set of salient latent variables capturing novel perturbation-induced variations,  
 64 while  $z_i$  denotes a set of background latent variables capturing variations shared across control and  
 65 perturbed samples and which are irrelevant our analysis. Without additional constraints, standard  
 66 latent variable inference procedures are unlikely to naturally disentangle these two sets of latent  
 67 variables. To address this issue, we leverage our control samples to impose an inductive bias on our  
 68 model that implicitly encourages disentanglement. In particular, for a control sample  $x_j^\emptyset$  we assume

$$x_j^\emptyset \sim p_\theta(x_j^\emptyset | z_j, 0).$$

69 In words, we assume that control samples are generated from the same process  $p_\theta$ , but with the  
 70 salient variables fixed at 0 to represent their absence. Equipped with this inductive bias, we may then  
 71 apply standard inference techniques with appropriate modifications to learn these disentangled sets  
 72 of variables, and previous works have leveraged this idea to explore high-content pooled CRISPR  
 73 screening data with linear cLVMs [5] and non-linear cLVMs based on deep neural networks [6]. Yet,  
 74 as discussed previously, standard cLVMs may not be ideal for modeling pooled CRISPR screens  
 75 due to the assumption of a single unimodal prior over the salient latent variables shared across all  
 76 perturbations. To resolve this issue, in the next section we propose a new generative model that  
 77 extends the standard cLVM framework with a richer prior over the salient variables to reflect the  
 78 additional structure present in pooled genetic screening datasets.

## 79 3 The ContrastiveVI+ Probabilistic Model

80 For a given cell  $i$  labelled with a non-control guide RNA  $c_i$ , let

$$z_i \sim \mathcal{N}(0, I_p)$$

81 denote a low-dimensional set of latent variables capturing factors of variation found in both perturbed  
 82 cells as well as controls. Next, let

$$y_i \sim \text{Bern}(\alpha)$$

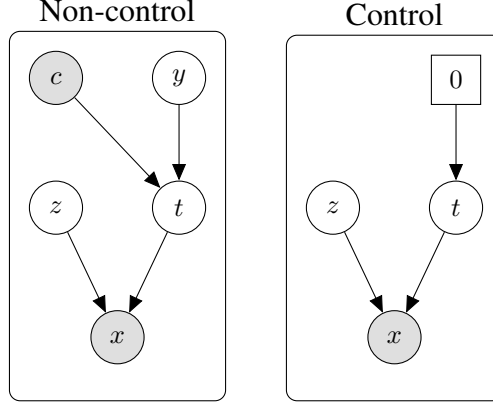


Figure 1: Graphical representation of the ContrastiveVI+ generative process for cells with non-control guides (left) and control guides (right).

83 denote a binary value indicating whether a cell expressing a gRNA successfully underwent a cor-  
 84 responding genetic perturbation ( $y_i = 1$ ) or failed to do so ( $y_i = 0$ ). For all of the experiments  
 85 presented in this work we placed an uninformative prior on  $y_i$  with  $\alpha = 0.5$ . Conditioned on this  
 86 value and the perturbation label  $c_i$ , we then draw

$$t_i \mid y_i, c_i \sim y_i \cdot \mathcal{N}(\mu_c, I_q) + (1 - y_i) \cdot \mathcal{N}(\mu_\emptyset, I_q).$$

87 That is, if a cell successfully underwent a genetic perturbation, we assume that its salient latent  
 88 representation is drawn from a Gaussian centered at a perturbation-specific mean  $\mu_c$ . For all results  
 89 presented in this manuscript, we set our perturbation labels  $c_i$  as the gene targeted by the guide in cell  
 90  $i$ ; however, in principle other labeling schemes to be used (e.g.  $c_i$  could denote the specific species of  
 91 gRNA when multiple gRNAs targeting the same gene are used in an experiment). On the other hand,  
 92 if the cell was not perturbed, we assume that its salient representation was drawn from a Gaussian  
 93 with mean  $\mu_\emptyset$  shared across all perturbations.

94 Letting  $f^\eta$  denote a neural network with a softmax non-linearity as the final layer, we then compute

$$\rho_i = f^\eta(z_i, t_i).$$

95 Analogous to scVI [4], this vector on the probability simplex represents the expected normalized  
 96 expression frequency of each gene  $g$ . For a gene  $g$  we then assume that the observed gene expression  
 97  $x_{ig}$  in cell  $i$  is drawn

$$x_{ig} \sim \text{ZINB}(\ell_i \rho_{ig}, \theta_g, f^\nu(z_i, t_i)),$$

98 where ZINB denotes the zero-inflated negative binomial distribution,  $\ell_i$  is the observed library size  
 99 for cell  $i$ ,  $\theta_g$  is a gene-specific inverse dispersion parameter, and  $f^\nu$  is a neural network whose outputs  
 100 are interpreted as dropout probabilities.

101 For a cell  $j$  infected with a control gRNA, we assume the same generative process but with  $y_j$  fixed at  
 102 0. Thus, cell  $j$ 's salient variables  $t_j$  are always drawn from a Gaussian centered at  $\mu_\emptyset$ , and the region  
 103 of the salient latent space around  $\mu_\emptyset$  thus semantically represents the absence of perturbation-induced  
 104 variations. We depict our generative processes for cells with control and non-control gRNAs in  
 105 graphical model form in **Fig. 1**.

## 106 4 Inference

107 Exact posterior inference for our model is intractable, so we instead resort to variational inference  
 108 [10] via auto-encoding variational Bayes [11]. For cells with non-control guides, we assume that our  
 109 variational distribution with parameters  $\phi$  factorizes as follows

$$q_\phi(z_i, t_i, y_i, \mid x_i, c_i) = q_{\phi_z}(z_i \mid x_i) q_{\phi_t}(t_i \mid x_i) q_{\phi_y}(y_i \mid t_i),$$

110 where  $\phi_z$ ,  $\phi_t$ , and  $\phi_y$  denote parameters of inference networks for  $z$ ,  $t$ , and  $y$  respectively. Here  
 111  $q(z | x)$  and  $q(t | x)$  take the form of Gaussian distributions, while  $q(y | t)$  is a Bernoulli distribution.  
 112 Our corresponding variational bound is then (derivation in Appendix A):

$$\begin{aligned} \mathcal{L}(x_i) &= \mathbb{E}_{q_{\phi_z}(z_i|x_i)q_{\phi_t}(t_i|x_i)} [p_\theta(x_i | z_i, t_i)] - D_{KL}(q_{\phi_z}(z_i | x_i) \| p(z_i)) \\ &\quad - \mathbb{E}_{q_{\phi_t}(t_i|x_i)} [D_{KL}(q_{\phi_y}(y_i | t_i) \| p(y_i))] \\ &\quad + \mathbb{E}_{q_{\phi_t}(t_i|x_i)} \left[ \left( \sum_{y' \in \{0,1\}} q_{\phi_y}(y' | t_i) (\log p(t_i | y', c_i)) \right) - \log q_{\phi_t}(t_i | x_i) \right]. \end{aligned} \quad (1)$$

113 For cells with non-targeting control (NTC) guides, we assume an alternative variational distribution  
 114 incorporating our prior knowledge that factorizes as

$$q_{\phi_{NTC}}(z_j, t_j, y_j, | x_j) = q_{\phi_z}(z_j | x_j) \delta\{t_j = \mu_\emptyset\} \delta\{y_j = 0\},$$

115 That is, for control cells we assume that  $t_j$  and  $y_j$  are fixed at  $\mu_\emptyset$  and 0, respectively to reflect the  
 116 fact that cells with NTC guides are known to be unperturbed ( $y_j = 0$ ) and that the salient variables  
 117  $t_j$  should not capture variations in the observed data for control cells. We also note that the same  
 118 inference parameters  $\phi_z$  are used as in the non-NTC case. We then derive a corresponding bound

$$\mathcal{L}_{NTC}(x_j^\emptyset) = \mathbb{E}_{q_{\phi_z}(z_j, | x_j^\emptyset)} [p_\theta(x_j^\emptyset, | z_j, t_j = \mu_\emptyset)] - D_{KL}(q_{\phi_z}(z_j | x_j^\emptyset) \| p(z_j)). \quad (2)$$

119 By fixing  $t_j = \mu_\emptyset$  for NTC cells during the inference procedure, we ensure that the salient variables  
 120  $t_j$  do not capture any sources of variation for cells with NTC guides. Thus, as the recognition network  
 121 parameters  $\phi_z$  are shared across NTC and non-NTC guide cells, the background variables  $z$  are  
 122 implicitly encouraged to recover sources of variation shared across cells from both groups, while  
 123 the salient variables  $t$  are then free to recover the additional variations only present in perturbed  
 124 cells. As all cells are assumed to be generated independently, we may then perform inference by  
 125 maximizing the sums of Equations 1 and 2 across all cells via minibatch gradient ascent similar  
 126 to standard cLVMS [7, 5, 6, 8]. Perturbation-specific means  $\mu_c$  along with  $\mu_\emptyset$  are learned as point  
 127 estimates and optimized along with our model’s other parameters.

128 While similar implicit schemes have been successfully employed to encourage disentanglement in  
 129 standard cLVMS, in initial experiments we found that additional regularization was required to ensure  
 130 that our inference procedure respected the intended semantics of our more structured generative  
 131 process. First, as the salient space recognition network  $q_{\phi_t}$  does not learn from cells with NTC guides  
 132 when optimizing Equation 2, we found that  $q_{\phi_y}$  did not reliably associate nonperturbed cells to the  
 133 region of the salient latent space around  $\mu_\emptyset$ . To remedy this issue, we added an additional KL penalty  
 134 to  $\mathcal{L}_{NTC}$  encouraging NTC cells to map to the null region of the salient space, yielding

$$\mathcal{L}_{NTC}^*(x_j^\emptyset) = \mathcal{L}_{NTC} - D_{KL}(q(t_j | x_j^\emptyset) \| \mathcal{N}(\mu_\emptyset, I_q)). \quad (3)$$

135 Second, for datasets with larger numbers of perturbations, we observed that perturbation-induced  
 136 variations were sometimes undesirably captured in the model’s background latent space. To discour-  
 137 age this behavior, we leveraged the maximum mean discrepancy (MMD) [12], a kernel-based test  
 138 statistic for determining whether two groups of samples were drawn from the same distribution. In  
 139 particular, letting  $Z^b$  denote a minibatch of posterior background latent space samples for cells with  
 140 non-NTC guides and defining  $Z_{NTC}^b$  analogously for cells with control guides, we add the penalty

$$-\lambda \cdot \ell_{\text{MMD}}(Z^b, Z_{NTC}^b), \quad (4)$$

141 where  $\ell_{\text{MMD}}$  denotes the empirical estimate of the MMD of Gretton et al. [12] and  $\lambda$  controls the  
 142 regularization strength. For all experiments presented in this work, we tuned  $\lambda$  such that the MMD  
 143 penalty was of similar magnitude to the KL regularization terms in our ELBOs, a strategy successfully  
 144 employed in previous work [6]. With this penalty, ContrastiveVI+’s background latent space was  
 145 thus explicitly encouraged to capture variations shared across cells with NTC and non-NTC guides.

146 Combined with our more structured generative process, ContrastiveVI+’s inference procedure pro-  
 147 vides two major advantages over that of the original ContrastiveVI model. First, our richer prior on  
 148 the salient latent space with perturbation-specific means may allow ContrastiveVI+ to recover subtle  
 149 perturbation-induced effects in the salient latent space that would be shrunk to the shared unimodal  
 150 prior in the standard cLVM setup. Second, post-training our approximate posterior  $q_{\phi_y}(y_i | t_i)$  can  
 151 be used to classify cells that escaped perturbation versus those that were successfully perturbed.

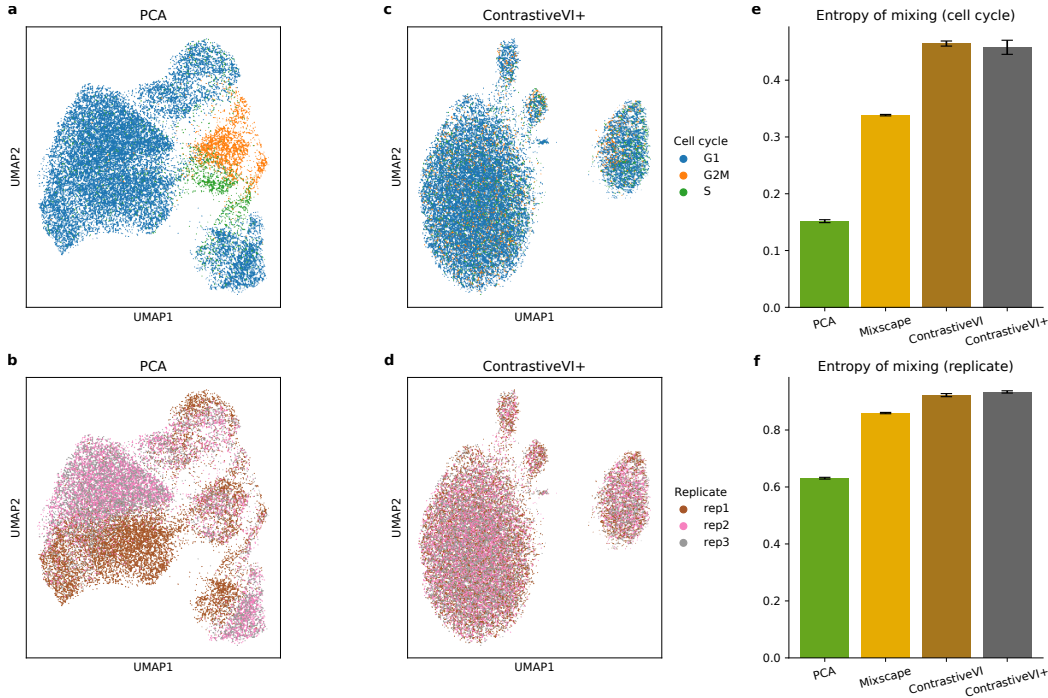


Figure 2: **a-b**, UMAP visualizations of PCA (**a**) applied to data from Papalexi et al. [3] colored by cell cycle (**a**) and replicate (**b**). **c-d** UMAP visualizations of ContrastiveVI+’s salient latent space colored by cell cycle (**c**) and replicate (**d**). **e-f**, Entropy of mixing for ContrastiveVI+ and baseline methods’ representations with respect to cell cycle phase (**e**) and replicate identity (**f**).

## 152 5 Experiments

153 **Overview.** To evaluate our method, we applied it to three publicly available pooled genetic screening  
 154 datasets [3, 13, 14]. Based on previous analyses, for each of these datasets we have known con-  
 155 founding sources of variation (e.g. cell cycle) and/or known perturbation-induced variations (e.g.  
 156 common gene programs induced by groups of perturbations) that allowed us to assess the quality  
 157 of ContrastiveVI+’s learned representations. Moreover, we also used these datasets to assess the  
 158 quality of ContrastiveVI+’s predictions of escaping versus perturbed cells. Details regarding the  
 159 preprocessing of these datasets can be found in Appendix B.

160 **Baselines.** For each dataset we benchmarked ContrastiveVI+ against two previously proposed  
 161 methods for exploring perturbation-induced variations in pooled genetic screens. First, we considered  
 162 the original ContrastiveVI model of Weinberger et al. [6] to assess whether our more structured  
 163 generative process could better recover subtle perturbation-induced variations. Second, we considered  
 164 the Mixscape method proposed in Papalexi et al. [3]. Mixscape provides both a procedure for isolating  
 165 perturbation-induced variations, via a nearest-neighbors-based approach for computing so-called  
 166 “perturbation signatures” for each cell, and a procedure for identifying escaping cells. Finally, as a  
 167 naive baseline we also include results from simply applying principal component analysis (PCA) to  
 168 normalized expression levels. Further details on our implementation of ContrastiveVI+ and baseline  
 169 methods can be found in Appendix C.

### 170 5.1 Initial validation of ContrastiveVI+ on a small-scale ECCITE-seq dataset

171 We first applied ContrastiveVI+ to data originally presented in Papalexi et al. [3] collected using  
 172 ECCITE-seq [15], a protocol that combines pooled CRISPR screening with single-cell transcriptomic  
 173 as well as surface protein measurements. This dataset was collected from a human leukemia  
 174 monocytic cell line (THP-1) after stimulation with interferon gamma (IFN- $\gamma$ ), with the goal of  
 175 identifying immune checkpoint regulators. In this dataset a total of 25 genes were targeted for  
 176 CRISPR knockout.

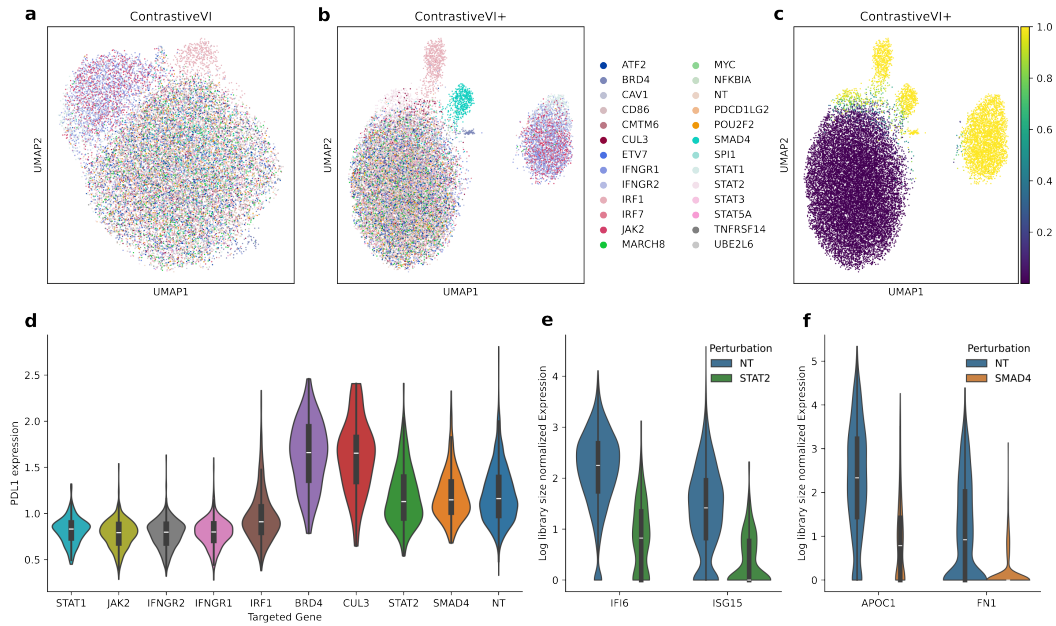


Figure 3: **a-b**, UMAP plots of ContrastiveVI and ContrastiveVI+’s salient latent representations colored by gene target. **c**, UMAP plot of ContrastiveVI+’s salient latent representations colored by inferred probability of perturbation. **d**, *PDL1* protein expression for gene perturbations highlighted in ContrastiveVI+’s salient latent space compared to control cells. **e-f**, Subset of transcriptomic changes for *STAT2*- and *SMAD4*-perturbed cells identified by ContrastiveVI+.

177 Beyond variations due to novel perturbation-induced phenotypes, in their original analyses Papalexi  
 178 et al. [3] identified substantial confounding sources of variation shared with control cells due to cell  
 179 cycle phase and batch effects (Fig. 2a-b). We thus began our experiments by assessing ContrastiveVI+  
 180 ’s ability to remove these confounding sources of variation in its salient latent space. Qualitatively,  
 181 we found that ContrastiveVI+ ’s salient latent space was indeed invariant to these confounding  
 182 variations (Fig. 2c-d). To quantify ContrastiveVI+ and baseline methods’ performance on this task,  
 183 we computed the entropy of mixing (Appendix D.1) for each method’s representations with respect  
 184 to cell cycle phase and replicate identity. While all methods resulted in better mixing compared to the  
 185 naive PCA baseline, we found that ContrastiveVI and ContrastiveVI+ achieved stronger performance  
 186 on this task for both confounding sources of variation (Fig. 2e-f) compared to Mixscape’s perturbation  
 187 signatures. This result suggests that the nearest-neighbors based approach employed by Mixscape is  
 188 less effective at isolating perturbation-induced variations compared to deep generative models.

189 We next investigated whether ContrastiveVI+ ’s richer model could highlight further trends compared  
 190 to ContrastiveVI. We found that both methods (Fig. 3a-b) highlighted a cluster of cells with gRNA’s  
 191 corresponding to known upstream components of the IFN- $\gamma$  pathway (*IFNGR1*, *IFNGR2*, *JAK2* and  
 192 *STAT1*), a cluster of cells with gRNAs corresponding to the downstream IFN- $\gamma$  mediator *IRF1*, and  
 193 a third cluster containing containing cells from all perturbations (including non-targeting gRNAs).  
 194 Beyond these clusters, ContrastiveVI+ additionally highlighted clusters of cells expressing gRNAs  
 195 targeting *SMAD4*, *BRD4*, and *STAT2*. Moreover, when inspecting ContrastiveVI+ ’s inferred values of  
 196  $y$  (Fig. 3c), we found that cells in mixed cluster shared with controls were assigned as non-perturbed  
 197 ( $y \approx 0$ ) while cells in the non-control clusters were classified as perturbed ( $y \approx 1$ ), suggesting that  
 198 ContrastiveVI+ successfully distinguished perturbed versus escaping cells.

199 We verified that these clusterings corresponded to meaningful perturbation effects by first inspecting  
 200 *PDL1* surface protein expression levels (Fig. 3d) for cells predicted by ContrastiveVI+ as perturbed.  
 201 For most genes, we found corresponding decreases (*IFNGR1*, *IFNGR2*, *JAK2*, *STAT1*, and *IRF1*)  
 202 or increases (*BRD4*, *CUL3*) in *PDL1* expression compared to control cells. Moreover, while *STAT2*  
 203 and *SMAD4* did not affect *PDL1* expression, we nevertheless found clear transcriptomic changes  
 204 in cells predicted by ContrastiveVI+ as perturbed compared to controls (Fig. 3e-f). In particular,  
 205 *STAT2*-perturbed cells exhibited strong downregulation of interferon-induced genes (e.g. *IFI6*, *ISG15*)

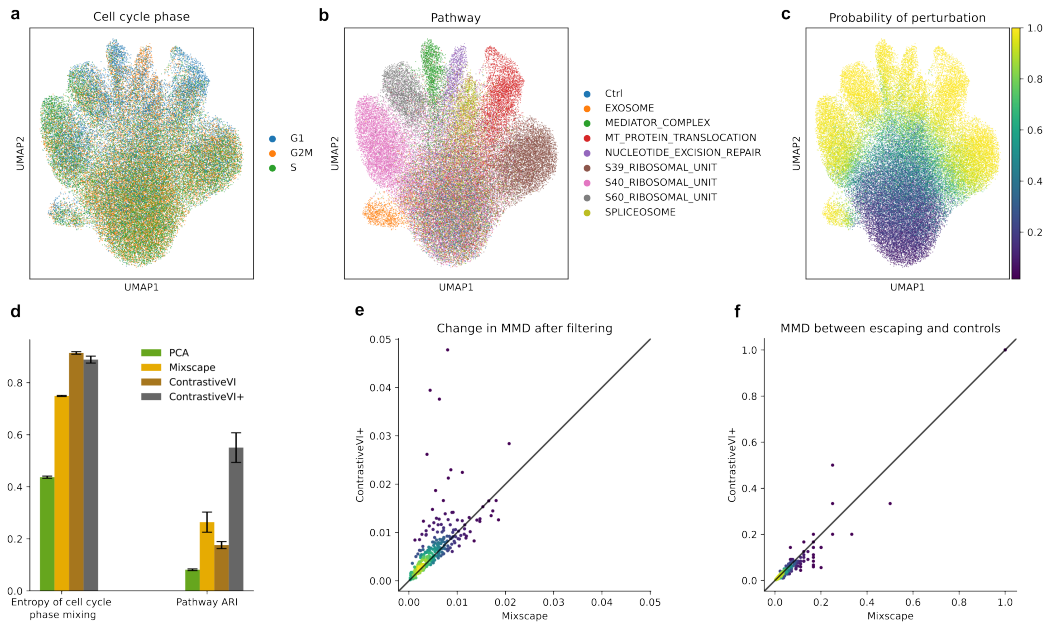


Figure 4: **a-c**, UMAP plots of ContrastiveVI+’s salient latent space for data from Replogle et al. [13] colored by cell cycle phase (**a**), pathway annotations (**b**) and inferred probability of perturbation (**c**). **d**, Quantitative assessments of invariance with respect to cell cycle phase (entropy of cell cycle phase mixing) and capturing of known perturbation-induced variations (pathway ARI) for ContrastiveVI+ and baseline method’s salient representations. **e**, Change in MMD between cells labeled with gRNAs targeting a given gene versus cells with non-targeting control guides after filtering with ContrastiveVI+ (*y*-axis) or Mixscape (*x*-axis) compared to the MMD without filtering. **f**, MMD between cells labeled as escaping by ContrastiveVI+ (*y*-axis) or Mixscape (*x*-axis) versus control cells.

206 while *SMAD4*-perturbed cells demonstrated downregulation in inflammatory response genes (e.g.  
 207 *APOC1*, *FNI*).

208 Taken together, these results illustrate that ContrastiveVI+ indeed may highlight additional structure  
 209 in the model’s salient latent space compared to standard cLVMs. Moreover, these results demonstrate  
 210 that our inference procedure can identify cells exhibiting perturbation effects versus escaping cells.

## 211 5.2 Further validation on a larger-scale CRISPRi screen

212 We next applied ContrastiveVI+ to analyze data from a CRISPR interference (CRISPRi) Perturb-seq  
 213 dataset presented in Replogle et al. [13]. Following previous work [16, 17], in our experiments  
 214 we considered a subset of perturbations identified as having nontrivial effect sizes and which were  
 215 labeled by the original authors of Replogle et al. [13] as affecting specific biological pathways. In  
 216 total, we retained data from cells with guides targeting 336 genes as well as cells with NTC guides.

217 We began our analysis by assessing the quality of ContrastiveVI+’s salient representations. Previous  
 218 analyses of this data [18] have identified cell cycle as a major confounding source of variation in this  
 219 dataset shared with control cells. Thus, we would expect ContrastiveVI+’s salient latent space to  
 220 be invariant with respect to cell cycle phase. Moreover, we would expect cells to cluster based on  
 221 the pathway labels assigned to perturbations by [13]. We found that ContrastiveVI+’s salient space  
 222 was indeed invariant to cell cycle (**Fig. 4a**), with clear clusters separating by pathway label (**Fig. 4b**).  
 223 Moreover, cells from these distinct pathway clusters were inferred as truly perturbed, while cells in  
 224 the remaining cluster mixed across pathways and control cells were inferred as escaping (**Fig. 4c**).

225 To compare ContrastiveVI+ and baselines’ performance on this task, we employed the entropy of  
 226 mixing to measure invariance with respect to cell cycle and used the adjusted rand index (ARI;  
 227 Appendix D.2) to quantify separation based on pathway labels. When computing pathway ARI, for  
 228 ContrastiveVI+ and Mixscape we restricted our attention to cells labeled by these methods as truly  
 229 perturbed to mitigate the impact of escaping cells; for ContrastiveVI we used all cells as this method



230 does not predict perturbed versus escaping cells. We found that ContrastiveVI+ and ContrastiveVI had  
231 the strongest performance on cell cycle mixing, while ContrastiveVI+ achieved substantially stronger  
232 performance on the pathway ARI metric compared to baselines. These results further demonstrate  
233 ContrastiveVI+’s superior ability to isolate perturbation-induced variations.

234 Given its large number of distinct perturbations, we further used this dataset to benchmark Con-  
235 trastiveVI+ and Mixscape’s procedures for identifying perturbed versus escaping cells. Intuitively,  
236 cells classified as perturbed should have substantially different gene expression profiles compared  
237 to cells with NTC guides. To capture this idea, we used the MMD to measure the distance between  
238 populations of cells. Specifically, for each gene perturbation we computed the MMD between  
239 cells labeled with a gRNA targeting that gene versus cells with NTC guides. We then recalculated  
240 the MMD after filtering to cells labeled by ContrastiveVI+ or Mixscape as perturbed, and finally  
241 computed the change in MMD with filtering versus without filtering. We present our results for this  
242 experiment in **Fig. 4e**. Here a *higher* change in MMD indicates that cells classified as perturbed  
243 exhibit stronger differences from control cells and thus represents better performance. We found that  
244 for a majority of genes ContrastiveVI+ led to larger changes in MMD compared to Mixscape, with  
245 statistical significance confirmed with a binomial test assuming a null hypothesis of equal chance of  
246 either method achieving better performance for each gene ( $p < 1 \cdot 10^{-5}$ ).

247 In isolation, such a metric could be maximized by only retaining cells with the most extreme changes  
248 compared to controls and erroneously labeling many truly-perturbed cells as escaping. To counteract  
249 this potential pathology, we thus also assessed whether cells labeled as escaping perturbation by each  
250 method were indeed similar to cells with NTC guides. To do so, we computed the MMD between  
251 cells labeled as escaping by each method versus cells with NTC guides, and we present our results in  
252 **Fig. 4f**. Here lower MMD values indicate that the cells flagged by a method as escaping are closer to  
253 true controls and thus represent better performance. We found that cells predicted as escaping by  
254 ContrastiveVI+ largely had lower MMDs compared to Mixscape ( $p < 1 \cdot 10^{-5}$ , binomial test).

255 Taken together, these results suggest ContrastiveVI+’s more expressive modeling procedure facilitates  
256 superior prediction of perturbed versus escaping cells compared to Mixscape.

### 257 **5.3 Exploring the diversity in perturbation responses in a CRISPRa screen**

258 As a final demonstration of ContrastiveVI+’s capabilities, we applied it to explore a Perturb-  
259 seq dataset from Norman et al. [14]. In this dataset the authors assessed the effects of CRISPR  
260 activation (CRISPRa) perturbations on K562 cells. For our analysis, we focused on a subset of these  
261 perturbations labeled in Norman et al. [14] as inducing specific gene programs.

262 We began by confirming that ContrastiveVI+ successfully isolated perturbation-induced variations in  
263 its salient latent space. Based on the analysis of Norman et al. [14], we would expect cells to separate  
264 by gene program labels. Moreover, we would expect cells to mix across cell cycle phase, a known  
265 confounding source of variation shared with control cells in this dataset [6]. We found that cells  
266 indeed mixed across cell cycle phase (**Fig. 5a**), while separating by gene program labels (**Fig. 5b**),  
267 with cells in the separated gene program clusters being predicted by ContrastiveVI+ as perturbed (**Fig.**  
268 **5c**). Moreover, ContrastiveVI+ achieved significantly better separation of gene programs compared  
269 to baseline methods as measured by ARI while also achieving strong performance at removing cell  
270 cycle effects as measured by entropy of mixing (**Fig. 5d**).

271 In addition to separation between the gene program clusters, in our analysis we also observed  
272 separation between substructures within these clusters. To highlight ContrastiveVI+’s potential  
273 to facilitate additional insights, we thus further inspected the cells with perturbations labeled as  
274 “granulocyte/apoptosis” and which were predicted by ContrastiveVI+ as perturbed (**Fig. 5e**). Notably,  
275 in Norman et al. [14], the authors of that work largely analyzed the relationships between perturbations  
276 at the pseudobulk level (i.e., by considering the mean expression profile for each perturbation). Thus,  
277 a particular focus of our analysis was to see if our single-cell-level model could uncover further  
278 relationships between perturbations beyond those discussed in Norman et al. [14].

279 First, to understand the genes driving separation in ContrastiveVI+’s latent space, we employed  
280 Hotspot [19], a tool for identifying informative genes in single-cell data by ranking genes in terms of  
281 spatial autocorrelation with respect to a given metric of cell–cell similarity (e.g., the latent space of a  
282 VAE). From the top genes returned by Hotspot, we found that separation in ContrastiveVI+’s salient  
283 space was strongly correlated with canonical granulocyte marker genes, such as *LST1*, *CSF3R*, and



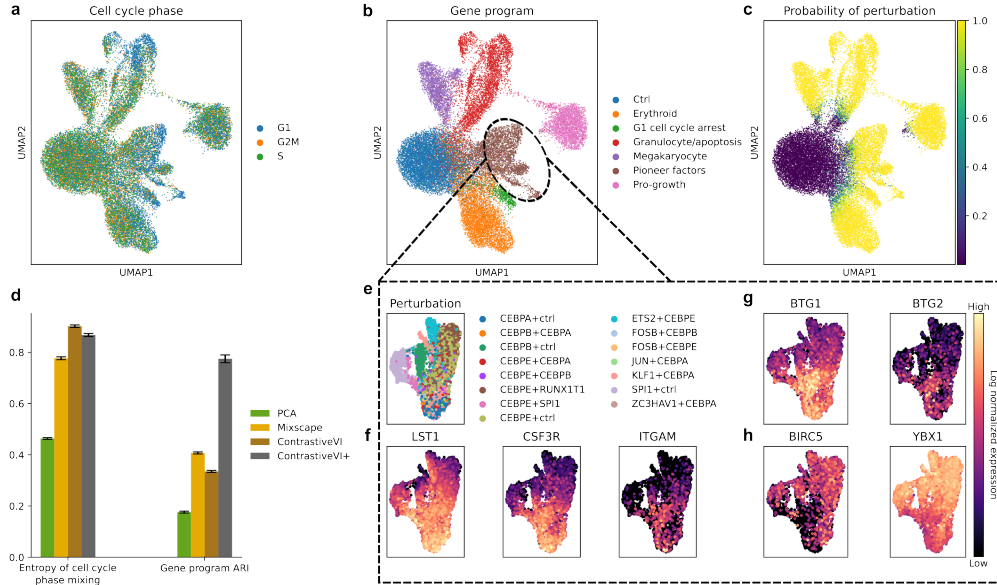


Figure 5: **a-c**, UMAP visualizations of ContrastiveVI+’s salient latent space for Norman et al. [14] colored by cell cycle phase (**a**), gene program labels provided by Norman et al. [14] (**b**), and inferred probability of perturbation (**c**). **d**, Quantitative assessments of ContrastiveVI+ and baseline method’s salient representations. **e-h**, ContrastiveVI+’s salient latent representations for cells with perturbations labeled as “granulocyte/apoptosis” by Norman et al. [14]. Plots colored by perturbation labels (**e**), canonical granulocyte marker genes (**f**), the pro-apoptotic anti-proliferation factors *BTG1* and *BTG2* (**g**), and anti-apoptotic genes *BIRC5* (survivin) and *YBX1* (**h**).

284 *ITGAM* (**Fig. 5f**). Moreover, expression of the granulocyte markers was correlated with expression of  
 285 the pro-apoptotic anti-proliferation factors *BTG1* and *BTG2* (**Fig. 5g**), and inversely correlated with  
 286 the anti-apoptotic genes *BIRC5*, also known as survivin, and *YBX1* (**Fig. 5h**).

287 Furthermore, we observed clear heterogeneity in the responses induced by individual perturbations.  
 288 For example, while some perturbations induced consistently strong upregulation of granulocyte  
 289 markers (e.g. *CEBPA+ctrl*), other perturbations (e.g. *CEBPE+ctrl*) resulted in more variable re-  
 290 sponses. Notably, we often observed strong mixing between cells perturbed solely to activate  
 291 *CEBPE* (i.e., *CEBPE+ctrl*) and cells perturbed to activate *CEBPE* along with a second gene (e.g.  
 292 *CEBPE+RUNX1T1*, *CEBPE+CEBPA*, and *FOSB+CEBPE*). This phenomenon suggests that activa-  
 293 tion of *CEBPE* is sufficient to achieve a certain cellular state, with other perturbations not having an  
 294 observable impact. Moreover, this behavior is consistent with *CEBPE*’s known function of strongly  
 295 driving terminal differentiation for granulocytes [20]; in other words, due to *CEBPE* activation  
 296 inducing cells to differentiate into granulocytes, the effects of additional perturbations may be muted.

297 Notably, these phenomena were not discussed in Norman et al. [14], and these results illustrate  
 298 how the higher resolution of our single-cell-level modeling approach may facilitate insights into the  
 299 diversity of perturbation responses beyond those possible from previous workflows.

## 300 6 Conclusion

301 Here we introduced ContrastiveVI+, a deep generative modeling framework for exploring  
 302 perturbation-induced variations in pooled genetic screening datasets while explicitly accounting  
 303 for variable guide efficiency and the diversity of responses induced by different perturbations. In  
 304 experiments on three datasets with scRNA-seq readouts, we found that our model’s additional struc-  
 305 ture resulted in substantially better recovery of known biological relationships compared to baseline  
 306 methods while also successfully predicting truly perturbed versus escaping cells. Moreover, we found  
 307 that our more structured modeling approach could reveal further biological insights beyond those  
 308 provided by other analysis workflows. Future work will involve assessing ContrastiveVI+’s abilities  
 309 on larger scale datasets and additional high-content screening modalities beyond scRNA-seq.

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## 387 A Derivation of variational bounds for ContrastiveVI+

388 Here we present a full derivation of the variational bound for cells with non-NTC guides presented in  
389 Section 4. We begin by assuming that our variational distribution factorizes as

$$q_\phi(z_i, t_i, y_i, | x_i, c_i) = q_{\phi_z}(z_i | x_i)q_{\phi_t}(t_i | x_i)q_{\phi_y}(y_i | t_i),$$

390 where  $\phi_z$ ,  $\phi_t$ , and  $\phi_y$  denote parameters of inference networks for  $z$ ,  $t$ , and  $y$  respectively. Leveraging  
391 our variational distribution as well as the generative process proposed in Section 3, we then proceed  
392 to derive a corresponding ELBO:

$$\begin{aligned} \mathcal{L}(x_i) &= \mathbb{E}_{q_\phi(z_i, t_i, y_i | x_i)} \left[ \log \frac{p(z_i, t_i, y_i, x_i | c_i)}{q_\phi(z_i, t_i, y_i | x_i)} \right] \\ &= \mathbb{E}_{q_{\phi_z}(z_i | x_i)q_{\phi_t}(t_i | x_i)q_{\phi_y}(y_i | t_i)} \left[ \log \frac{p(z_i)p(t_i | y_i, c_i)p(y_i)p(x_i | z_i, t_i)}{q_{\phi_z}(z_i | x_i)q_{\phi_t}(t_i | x_i)q_{\phi_y}(y_i | t_i)} \right] \\ &= \mathbb{E}_{q_{\phi_z}(z_i | x_i)q_{\phi_t}(t_i | x_i)q_{\phi_y}(y_i | t_i)} \left[ \log \frac{p(z_i)}{q_{\phi_z}(z_i | x_i)} + \log \frac{p(t_i | y_i, c_i)}{q_{\phi_t}(t_i | x_i)} + \log \frac{p(y_i)}{q_{\phi_y}(y_i | t_i)} + \right. \\ &\quad \left. \log p(x_i | z_i, t_i) \right] \\ &= \mathbb{E}_{q_{\phi_z}(z_i | x_i)q_{\phi_t}(t_i | x_i)} [p(x_i | z_i, t_i)] + \mathbb{E}_{q_{\phi_z}(z_i | x_i)} \left[ \log \frac{p(z_i)}{q_{\phi_z}(z_i | x_i)} \right] + \\ &\quad \mathbb{E}_{q_{\phi_t}(t_i | x_i)q_{\phi_y}(y_i | t_i)} \left[ \log \frac{p(t_i | y_i, c_i)}{q_{\phi_t}(t_i | x_i)} \right] + \mathbb{E}_{q_{\phi_t}(t_i | x_i)q_{\phi_y}(y_i | t_i)} \left[ \log \frac{p(y_i)}{q_{\phi_y}(y_i | t_i)} \right] \\ &= \mathbb{E}_{q_{\phi_z}(z_i | x_i)q_{\phi_t}(t_i | x_i)} [p(x_i | z_i, t_i)] - D_{KL}(q_{\phi_z}(z_i | x_i) \| p(z_i)) \\ &\quad - \mathbb{E}_{q_{\phi_t}(t_i | x_i)} [D_{KL}(q_{\phi_y}(y_i | t_i) \| p(y_i))] \\ &\quad + \mathbb{E}_{q_{\phi_t}(t_i | x_i)} \left[ \left( \sum_{y' \in \{0,1\}} q_{\phi_y}(y' | t_i) (\log p(t_i | y', c_i)) \right) - \log q_{\phi_t}(t_i | x_i) \right] \end{aligned}$$

393 For control cells infected with non-targeting control (NTC) guides we assume the following variational  
394 distribution:

$$q_{NTC}(z_j, t_j, y_j, | x_j^\emptyset) = q_{\phi_z}(z_j | x_j^\emptyset)\delta\{t_j = \mu_\emptyset\}\delta\{y_j = 0\}.$$

395 Our corresponding ELBO is then:

$$\begin{aligned} \mathcal{L}_{NTC}(x_j^\emptyset) &= \mathbb{E}_{q(z_j, | x_j^\emptyset)} \left[ \log \frac{p(z_j, x_j | t_j = \mu_\emptyset, y_j = 0)}{q(z_j | x_j^\emptyset)} \right] \\ &= \mathbb{E}_{q(z_j, | x_j^\emptyset)} \left[ \log \frac{p(x_j^\emptyset, | z_j, t_j = \mu_\emptyset)p(z_j)}{q(z_j | x_j^\emptyset)} \right] \\ &= \mathbb{E}_{q(z_j, | x_j^\emptyset)} [p(x_j^\emptyset, | z_j, t_j = \mu_\emptyset)p(z_j)] - D_{KL}(q(z_j | x_j^\emptyset) \| p(z_j)). \end{aligned}$$

## 396 B Dataset preprocessing

397 Here we provide descriptions of any preprocessing steps for the datasets considered in this work.

398 **Papalexi et al. [3].** The cell by gene count matrix along with corresponding metadata for this  
399 dataset was obtained from the NIH gene expression omnibus entry GSE153056. For our analysis we  
400 considered the top 2,000 highly variable genes returned from the Scanpy `highly_variable_genes`  
401 function with `flavor=seurat_v3`. For the analysis presented in Section 5, normalized protein  
402 counts were computed using the centered log ratio transform as implemented in `muon` [21] with  
403 `axis=1` to match the original analysis of Papalexi et al. [3]. Based on the original analysis of Papalexi  
404 et al. [3], cells with perturbations identified as having trivial effects were all labeled as nonperturbed  
405 and considered as control cells.

406 **Norman et al. [14].** The cell by gene count matrix for this dataset along with corresponding metadata  
 407 was obtained from the NIH gene expression omnibus entry GSE133344. As done in the analysis of  
 408 Norman et al. [14], cells with the perturbation label `NegCtrl1_NegCtrl0__NegCtrl1_NegCtrl0`  
 409 were excluded from our analysis. Cells marked as doublets (i.e., a `number_of_cells` metadata value  
 410 greater than 1.0) by Norman et al. [14] were also excluded from our analysis. For our experiments  
 411 we retained all cells with control guides along with cells infected with non-control guides that were  
 412 annotated with gene program labels by Norman et al. [14]. For our analysis we considered the  
 413 top 2,000 highly variable genes returned from the Scanpy `highly_variable_genes` function with  
 414 `flavor=seurat_v3`.

415 **Replogle et al. [13].** For the analysis presented in this work we considered a filtered version of the  
 416 original genome-wide data presented in Replogle et al. [13] provided by Bereket and Karaletsos [16]  
 417 that retained data from perturbations with non-trivial effect sizes. Among this set of perturbations,  
 418 for our experiments we considered the perturbations that had corresponding pathway labels provided  
 419 by Replogle et al. [13], and we used the same set of highly variable genes considered in Bereket and  
 420 Karaletsos [16].

## 421 C ContrastiveVI+ and baseline method implementation details

422 In the experiments presented in Section 5, we compared our proposed ContrastiveVI+ against two  
 423 baselines: the original ContrastiveVI model of Weinberger et al. [6] and the Mixscape method of  
 424 Papalexi et al. [3]. Here we provide a brief overview of these methods and their corresponding  
 425 implementations used in this work.

### 426 C.1 ContrastiveVI+

427 Our implementation of ContrastiveVI+ was performed using the `scvi-tools` library [22]. Our  
 428 variational distributions  $q_{\phi_z}$  and  $q_{\phi_t}$  were implemented as multilayer perceptrons with a single hidden  
 429 layer of 128 units and ReLU activation functions [23]. For all experiments we set the dimensionality  
 430 of both the background and salient latent spaces (i.e.,  $z$ , and  $t$ ) to 10. For  $q_{\phi_y}$ , we found that using  
 431 additional hidden layers led to more consistent performance across random initialization, with good  
 432 stability achieved with three hidden layers. Thus, for all results presented in this manuscript we  
 433 implemented  $q_{\phi_y}$  as an MLP with three hidden layers with 128 units each. For our decoder network  
 434 we used an MLP with a single hidden layer of 128 units. All ContrastiveVI+ models were optimized  
 435 using Adam [24] with the default parameters in `scvi-tools`.

### 436 C.2 ContrastiveVI

437 The original ContrastiveVI model of Weinberger et al. [6] extends the scVI model of Lopez et al. [4]  
 438 via the contrastive latent variable modeling framework described in Section 2. Specifically, for a cell  
 439  $i$  labelled with a non-control gRNA, ContrastiveVI assumes the following generative process. Let

$$z_i \sim \mathcal{N}(0, I)$$

440 denote a low-dimensional set of *background* latent variables capturing factors of variation found in  
 441 both perturbed cells as well as controls. Next, let

$$t_i \sim \mathcal{N}(0, I)$$

442 denote a low-dimensional set of *salient* latent variables capturing novel perturbation-induced varia-  
 443 tions in cells labeled with non-NTC guides.

444 Letting  $f^\eta$  denote a neural network with a softmax non-linearity as the final layer, we then compute

$$\rho_i = f^\eta(z_i, t_i).$$

445 Analogous to scVI, this vector on the probability simplex represents the expected normalized expres-  
 446 sion frequency of each gene  $g$ . For a gene  $g$  we then assume that the observed gene expression  $x_{ig}$  in  
 447 cell  $i$  is drawn

$$x_{ig} \sim \text{ZINB}(\ell_i \rho_{ig}, \theta_g, f^\nu(z_i, t_i)),$$

448 where ZINB denotes the zero-inflated negative binomial distribution,  $\ell_i$  is the observed library size  
 449 for cell  $i$ ,  $\theta_g$  is a gene-specific inverse dispersion parameter, and  $f^\nu$  is a neural network whose outputs

450 are interpreted as dropout probabilities. For cells with NTC guides, ContrastiveVI assumes the same  
451 generative process but with the salient latent variables fixed at a constant zero vector.

452 For inference, ContrastiveVI posits a variational distribution with parameters  $\phi$  that factorizes as

$$q_{\phi}(z_i, t_i, | x_i) = q_{\phi_z}(z_i | x_i)q_{\phi_t}(t_i | x_i)$$

453 for cells with non-NTC guides. For cells with control guides, the above variational distribution is  
454 modified to account for the assumption that the salient variables do not contribute to the generative  
455 process, yielding

$$q_{\phi}(z_i, t_i, | x_i) = q_{\phi_z}(z_i | x_i)\delta\{t_i = 0\}.$$

456 In other words, the salient variables  $t_n$  are simply fixed at 0 during inference for cells with control  
457 guides. We refer to Weinberger et al. [6] for derivation of corresponding evidence lower bounds.

458 In our experiments we used the scverse [25] compatible implementation of ContrastiveVI available  
459 in the `scvi-tools` [22] package. For our experiments we used the same model architecture and  
460 optimization hyperparameters as described in the ContrastiveVI paper [6].

### 461 C.3 Mixscape

462 The Mixscape procedure proposed in Papalexi et al. [3] begins by computing a so-called perturbation  
463 signature for each cell infected with a non-NTC guide. To do so, for a given cell with a non-NTC  
464 guide, that cell’s nearest neighbors in the control population are identified. The gene expression  
465 profiles of these nearest control neighbors are then averaged together and subtracted from the gene  
466 expression profile of the original given non-NTC guide cell. The result of this procedure is then  
467 defined as a cell’s perturbation signature.

468 After computing cells’ perturbation signature, Mixscape then classifies cells with non-NTC guides  
469 as perturbed or escaping perturbation. To do so, for each targeted gene Mixscape fits a mixture  
470 of Gaussian models with two components on the corresponding cells’ perturbation signatures. As  
471 escaping cells’ signatures are assumed to be similar to those of control cells, one component of each  
472 of these mixtures is constrained to be equal to of a unimodal Gaussian fit to control cells.

473 For all results presented in this work, we used the R implementation of Mixscape in the Seurat  
474 package with default parameters. When computing UMAP embeddings and metrics on representation  
475 quality (e.g. mixing across cell cycle phases), we used the principal components of cells’ perturbation  
476 signatures as done in Papalexi et al. [3].

## 477 D Metrics

478 Here we provide details on the quantitative metrics used in this work to compare ContrastiveVI+  
479 against baseline methods.

### 480 D.1 Entropy of mixing

481 For  $c$  groups (e.g. cell cycle phases.) the entropy of mixing [26] is defined as

$$\sum_{i=1}^c p_i \log p_i,$$

482 where  $p_i$  denotes the proportion of cells from group  $i$  in a given region, such that  $\sum_{i=1}^c p_i = 1$ .  
483 Next, let  $U$  denote a uniform random variable over the population of cells. Let  $B_U$  then denote the  
484 empirical proportions of cells’ groups in the 50 nearest neighbors of cell  $U$ . We report the entropy  
485 of this variables averaged over 100 random cells  $U$ . Higher values of this metric indicate stronger  
486 mixing of the  $c$  groups.

### 487 D.2 Adjusted Rand index

488 The adjusted Rand index (ARI) measures agreement between reference clustering labels and labels  
489 assigned by a clustering algorithm. Given a set of  $n$  samples and two sets of clustering labels

490 describing those cells, the overlap between clustering labels can be described using a contingency  
491 table, where each entry indicates the number of cells in common between the two sets of labels.  
492 Mathematically, the ARI is calculated as

$$\text{ARI} = \frac{\sum_{ij} \binom{n_{ij}}{2} - \left[ \sum_i \binom{a_i}{2} \sum_j \binom{b_j}{2} \right] / \binom{n}{2}}{\frac{1}{2} \left[ \sum_i \binom{a_i}{2} + \sum_j \binom{b_j}{2} \right] - \left[ \sum_i \binom{a_i}{2} \sum_j \binom{b_j}{2} \right] / \binom{n}{2}},$$

493 where  $n_{ij}$  is the number of cells assigned to cluster  $i$  based on the reference labels and cluster  $j$  based  
494 on a clustering algorithm,  $a_i$  is the number of cells assigned to cluster  $i$  in the reference set, and  $b_j$  is  
495 the number of cells assigned to cluster  $j$  by the clustering algorithm. ARI values closer to 1 indicate  
496 stronger agreement between the reference labels and labels assigned by a clustering algorithm. In our  
497 experiments we used the  $k$  means clustering algorithm to assign cluster labels to cells with  $k$  equal to  
498 the true number of clusters.