Predicting Motion of Vulnerable Road Users using High-Definition Maps and Efficient ConvNets

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Abstract

Following detection and tracking of traffic actors, prediction of their future motion is the next critical component of a self-driving vehicle (SDV), allowing the SDV to move safely and efficiently in its environment. This is particularly important when it comes to vulnerable road users (VRUs), such as pedestrians and bicyclists. We present a deep learning method for predicting VRU movement where we rasterize high-definition maps and actor's surroundings into bird's-eye view image used as input to convolutional networks. In addition, we propose a fast architecture suitable for real-time inference, and present an ablation study of rasterization choices.

1 Introduction

Recent advances in high-performance hardware and software led to unprecedented breakthroughs in AI applications. Computers have surpassed human performance in centuries old games such as go [29], understand health conditions and suggest medical treatment [35], and can even reason about complex relationships conveyed through images [39]. This progress also prompted renewed enthusiasm and work on self-driving vehicles (SDVs), a nascent technology holding a potential to transform the way we live and work. While interest in SDVs goes as far back as the 1980s [24], only in the last decade government agencies and large industry players turned their focus towards the field, leading to a new era of research that caused leaps in real-world performance of SDVs [36].

Predicting actor movement is a critical part of the autonomous technology. Once a self-driving vehicle successfully detects and tracks a traffic actor in its vicinity, it needs to understand how they will move in the near future for both actors and SDV to be safe during operation [6]. This particularly holds true for vulnerable road users (VRUs), defined as traffic actors with increased risk of injury, unprotected by an outside shield [21]. Road planners and policy makers have recognized this problem many decades ago, and attempted to mitigate it through several means. This included legal frameworks, designing new road types (e.g., segregating VRUs from motorized actors), educating both drivers and VRUs with particular focus on children and elderly that are at an even greater risk than others [5, 21], to name a few. These efforts however have given limited results, and in the US proportion of VRUs within overall traffic deaths actually increased between 2008 and 2017 from 14% to 19% [19].

In the current study we address a critical aspect of SDV technology, and focus on predicting motion for VRUs, namely pedestrians and bicyclists. The main contributions are summarized below:

- We present a system for motion prediction of VRU traffic actors, relying on recently proposed context rasterization techniques [6];
- We propose a fast convolutional neural network (CNN) architecture suitable for running in real-time onboard the SDV;
- We present an ablation study of various rasterization settings.

2 Related work

Efficient and accurate detection, tracking and motion prediction of VRUs are one of the key factors for autonomous vehicles to be safely deployed in complex urban environments. With greatly improved detection and tracking of VRUs [22], research on motion prediction of VRUs has been gaining lot of traction recently. Although most of the studies on VRU motion prediction focuses on pedestrians with only a very few focusing on bicyclists, recent work showed importance of predicting bicyclists at crossings [3] and signalized intersections [32]. In this section we provide an overview of motion prediction of pedestrians and bicyclists with respect to autonomous driving, while more comprehensive review that includes research on motion prediction of vehicles can be found in [6].

Motion prediction. A common approach for prediction of VRUs' motion in autonomous driving systems is to use motion model from tracking component to predict their future states. Most of the autonomous system's pedestrian tracking components use either the Brownian or the constant velocity motion models [31]. Those models don't take into account scene context and therefore fail in long-term prediction tasks as VRU motion follows complex patterns constrained by static and dynamic obstacles along the path. Traditionally, hand-crafted features were used for motion prediction of VRUs with respect to a surrounding context. The social force model for pedestrian motion prediction incorporated interactive forces that guide pedestrians towards their goals and enforce collision avoidance among pedestrians, as well as between pedestrians and static obstacles [10, 41]. Similar approach was applied for bicyclist motion prediction [13]. [25] introduced a motion model for bicyclist motion prediction that incorporates knowledge of the road topology. The authors were able to improve prediction accuracy by using specific motion models for a pre-specified set of canonical directions. [8] obtained more accurate predictions of pedestrian trajectories by incorporating semantic features from a scene such as relative distance to curbside and status of pedestrian traffic lights in the Gaussian Process (GP) model. A significant number of studies has been devoted to modeling pedestrian motion using maximum entropy Inverse Reinforcement Learning (IRL) [43]. [44] introduced an IRL model based on a set of manually designed feature functions that capture interaction and collision avoidance behavior of pedestrians. While all of these approaches are capable of predicting the pedestrian and bicyclist motions in many scenarios, the need for manual design of features makes them hard to scale in complex driving environments [37].

Deep learning motion prediction. Inspired by the success in the various areas of computer vision and robotics, many deep learning-based approaches have been proposed recently for the motion prediction task in order to model object-object and object-scene interactions which may not have been straightforward to represent manually. Most of deep learning approaches are based on Long Short-Term Memory (LSTM) variant of recurrent neural networks (RNNs) [11]. [33] used a sequenceto-sequence LSTM encoder-decoder architecture to predict the pedestrian position and angle of direction. Incorporating the angular information in addition to the temporal information led to a significant improvement in the prediction accuracy. With respect to modeling of dynamic context, [2] proposed an approach for pedestrian motion prediction based on LSTM architecture and a "social pooling layer" that uses spatial information of nearby pedestrians to implicitly model interactions among them. [38] proposed "social attention" method to predict future motion based on estimation of the relative importance of pedestrians through an attention layer. Recently, [7] proposed an LSTM-based Generative Adversarial Network (GAN) to generate and predict socially feasible motions. With respect to modeling of static context, [23] proposed an LSTM-based model for pedestrian's motion prediction that incorporates the map of static obstacles and position of surrounding pedestrians. [26] presented SoPhie, an LSTM-based GAN system for predicting physically and socially acceptable pedestrian trajectories using an RGB image from the scene and the trajectory information of surrounding pedestrians. [18, 37] incorporated scene information as well as human movement trajectories in the pedestrian motion prediction process. In addition to LSTM-based approaches, [20] proposed CNN-based approach where convolutional layers are utilized to handle temporal dependencies. Authors of [16] use CNNs for joint detection, tracking, and prediction. However, these models do not take into account scene context information. Authors of [4] include map information to predict high-level intent of vehicle actors, unlike our model that predicts trajectories.

Efficient CNN architectures. Since the introduction of AlexNet [15], researchers made significant progress in improving CNN architectures to make them more accurate and efficient. State-of-the-art architectures, such as VGG [30] or ResNet [9], tend to have a large number of layers running expensive computations, making them unsuitable for real-time inference. Recent proposals such as MobileNet

[12] and ShuffleNet [42] replace regular convolutional operator with more efficient depthwise separable or group convolutions, making them small and fast for mobile applications. MobileNet-v2 (MNv2) [27] further improves the original MobileNet by combining depthwise convolution with residual connections and bottleneck layers proposed in ResNet. One problem of this prior work is their focus on reducing computational FLOPs instead of optimizing for inference latency on devices. More recently, MnasNet [34] applied network architecture search algorithms [45] to optimize MNv2 for both accuracy and inference latency on mobile devices, and is able to improve both while maintaining similar FLOPs. ShuffleNet v2 [17] proposed several guidelines for designing fast networks beyond counting FLOPs, and applied these guidelines to design architectures that are both fast and accurate on GPUs and mobile CPUs. In this paper we propose modifications to MNv2 that make it much faster on GPU without compromising accuracy.

3 Proposed approach

In this section we discuss our approach to trajectory prediction of VRU actors. Note that we followed the same setup used in the previous work [6] (originally applied to vehicle actors), where the same loss functions are used to train the CNN models. However, in this paper we demonstrate that the methodology can be successfully applied to VRU actors, and explore two aspects of the existing approach that are critical to model's accuracy and inference speed. First, we experimented with different variations of the CNN architectures, and proposed a novel architecture that reduces inference latency without affecting accuracy. Second, we performed ablation study of different rasterization configurations, and measured their impact on the prediction accuracy for VRU actors.

Let us assume that we have access to real-time data streams coming from sensors such as lidar, radar, or camera, installed aboard a self-driving vehicle. In addition, assume that these inputs are used by an existing detection and tracking system, outputting state estimates S for all surrounding actors (state comprises the bounding box, position, velocity, acceleration, heading, and heading change rate). Denote a set of discrete times at which tracker outputs state estimates as $T = \{t_1, t_2, \ldots, t_T\}$, where time gap between consecutive time steps is constant (e.g., the gap is equal to 0.1s for tracker running at a frequency of 10Hz). Then, we denote state output of a tracker for the *i*-th actor at time t_j as s_{ij} , where $i = 1, \ldots, N_j$ with N_j being a number of unique actors tracked at t_j . Moreover, we assume access to detailed, high-definition map information \mathcal{M} of the SDV's operating area, including road and crosswalk locations, lane directions, and other relevant map information.

Using the state estimates and high-definition map, we rasterize an actor-specific bird's-eye view raster image encoding the actor's surrounding map and traffic actors for each actor of interest (see Figure 2 for examples). Then, given *i*-th actor's raster image and state estimate s_{ij} at time step t_j , we use a CNN model to predict its future state sequences up to H steps of horizon $[s_{i(j+1)}, \ldots, s_{i(j+H)}]$. Without the loss of generality, in this work we simplify the task to infer *i*-th actor's future x- and y-positions instead of full state estimates, while the remaining states can be derived by considering s_{ij} and the future position estimates. Both past and future positions at time t_j are represented in the actor-centric coordinate system derived from actor's state at time t_j , where forward direction is x-axis, left-hand direction is y-axis, and actor's bounding box centroid is the origin.

Following the approach in [6] we use a MNv2 model architecture to compute future positions from the input raster image. Below we describe improvements to this model architecture, followed by discussion of variations in the rasterization process that were considered during the ablation study.

3.1 Improved MobileNet-v2 architecture for fast inference

In this section we propose simple modifications to the MNv2 architecture that significantly speed up GPU inference. MNv2 is based on the inverted bottleneck block illustrated in Figure 1a. In each block, the input feature map is first upsampled to k times more channels (k is set to 6 in the original MNv2) with 1×1 convolution, followed by 3×3 depthwise convolution (DwConv) applied to the upsampled feature map. Then, the feature map is compressed back to the original channel size using 1×1 convolution, and summed with the initial input through residual connection. Non-linearity (e.g., ReLU) is applied only in the upsampled phase, as non-linearity in the bottlenecked phase (before the upsampling or after the compression) causes too much information loss and hurts model performance. Batch-norm (BN) is used in all 3 layers. While the majority of the FLOPs are in the 1×1 convolutions (i.e., 87%), the other operations are still non-negligible. As discussed in [17],



Figure 1: Building blocks of MobileNet-v2 and FastMobileNet

Table 1: Base CNN architecture of FastMobileNet (upsample=6 for all FMNet blocks)

Layer	Output	Stride	Repeats	
Raster image	$300 \times 300 \times 3$	_	_	
$\boxed{ \text{Conv } 3 \times 3}$	$150 \times 150 \times 24$	2	1	
\square DwConv 3 \times 3	$75 \times 75 \times 24$	2	1	
FMNet block 1	$75 \times 75 \times 12$	1	2	
FMNet block 2	$38 \times 38 \times 16$	2	3	
FMNet block 3	$19 \times 19 \times 32$	2	4	
FMNet block 4	$19 \times 19 \times 48$	1	3	
FMNet block 5	$10 \times 10 \times 80$	2	3	
FMNet block 6	$10 \times 10 \times 160$	1	1	
Conv 1×1	$10 \times 10 \times 640$	1	1	
Global average pooling	$1 \times 1 \times 640$	1	1	

FLOPs itself is not an accurate estimator of actual latency, and another important factor is the number of memory access operations (MAC). Operations such as DwConv, BatchNorm, ReLU, and BiasAdd, while having small FLOPs, typically incur heavy MAC. Especially in MNv2, the operations in the upsampled phase have k times more MAC than the same operations in the bottlenecked phase.

Compared to MNv2, in the proposed novel architecture called FastMobileNet (FMNet) we move most of the operations originally in the upsampled phase into the bottlenecked phase, reducing their FLOPs and MAC k times, see Figure 1b. The only remaining operation in the upsampled phase is a ReLU. Similarly to MNv2, no ReLU is applied in the bottlenecked phase. As the layers are linear in the bottlenecked phase we only apply one BiasAdd at the end of the block, as applying multiple BiasAdd in consecutive linear layers does not increase model expressiveness. Note that we do not use batch-norm in FMNet as we found the model converges well during training without it, and excessive batch-norm operations cost additional computation time. The stride=2 block of FMNet is similar to the regular block (see Figure 1c), except the original input is downsampled to the correct output size for residual connection. The FMNet architecture before fully-connected and output layers (see [6] for more details) used in this work is shown in Table 1, where the layer sizes and block repeats of the model are based on MNv2-0.5 (i.e., MNv2 with halved channel sizes in all layers).

3.2 Rasterization

To describe rasterization, let us first introduce a concept of a *vector layer*, formed by a collection of polygons and lines that belong to a common type. For example, in the case of map elements we have vector layer of roads, of crosswalks, and so on. To rasterize vector layer into an RGB space, each vector layer is manually assigned a color from a set of distinct RGB colors that make a difference among layers more prominent. Once the colors are defined, vector layers are rasterized one by one on top of each other, in the order from layers that represent larger areas such as road polygons towards layers that represent finer structures such as lanes or actor bounding boxes. To represent context around the *i*-th actor tracked at time step t_j we create a rasterized image I_{ij} of size $n \times n$ such that the actor is positioned at pixel (w, h) within I_{ij} , where *w* represents width and *h* height



Figure 2: Raster images for bicyclist actor (colored red) using resolution of 0.1m, 0.2m, and 0.3m



Figure 3: Different rasterization settings with 0.2m resolution for bicyclist example: (a) no rotation, (b) no lane heading, (c) no traffic light, (d) learned colors

measured from the bottom-left corner of the image. We color the actor of interest differently so that it is distinguishable from other actors.

In this study we tested several different choices of rasterization for the prediction of VRU actors. For all rasterization methods, we maintain a constant RGB raster dimension of 300×300 pixels (i.e., n = 300). The details of each rasterization choice are discussed below.

Raster frame rotation. In the previous work [6] the raster was rotated separately for each actor, such that the heading of each actor points up and the target actor is placed at w = 150, h = 50 (see Fig. 2). In this way heading of the actor is encoded directly into the input, and the raster encodes more context in front of the actor. We tested an alternative scheme where the raster frame is unrotated so that north direction points up, and the actor is placed in the center (w = 150, h = 150, see Fig. 3a).

Raster pixel resolution. The resolution governs the extent of surrounding context seen by the model. At 0.1m resolution, the model sees 25m in front and 5m behind the actor (assuming the rotated raster discussed above). Larger resolution allows for larger context around the actor, however the raster loses finer details which may be critical for accuracy. Thus, we experimented with resolutions of 0.1m, 0.2m and 0.3m, illustrated in Figure 2.

Lane direction. In the previous work [6] the direction of each lane segment was encoded as a hue value in HSV color space with saturation and value set to maximum, followed by conversion of HSV to RGB color space. Alternatively we can encode all lanes with a constant color, such that the raster does not contain lane direction information (see Figure 3b without using HSV approach, as opposed to Figure 2b where lane color indicates its heading).

Traffic lights. We use an existing traffic light classification algorithm to extract current traffic light states from sensor inputs. To encode this info in the input raster, we plot traffic light states as a colored circle at location where lane meets a traffic-light controlled intersection. Furthermore, we identify inactive crosswalks and paint them green (see Figure 3c without traffic light info, as opposed to Figure 2b). We tested if traffic light information impacts model accuracy.

Learning raster colors. In the previous work colors for each raster layer type were picked manually [6]. An alternative approach is to have the DNN learn the colors by itself. In this study, we provided all raster layers (e.g., road and vehicle polygons, tracked objects) to the network as separate binary-valued channels, and added a 1×1 convolution layer with 3 output channels and linear activation to generate the RGB raster image (see Figure 3d for example of a learned raster). The generated RGB image is then passed to the rest of the network as before.

Architecture	Pred. error [m]	Latency [ms]	FLOPs	Num. parameters
AlexNet	1.36	15.8	2.84G	70.3M
ResNet18	1.29	36.2	6.80G	11.7M
MNv2-0.5	1.27	21.3	322M	581k
MnasNet-0.5	1.28	18.3	335M	825k
FMNet	1.28	12.1	363M	564k

Table 2: Comparison of various CNN architectures

Model pre-training. We also tested one modification not related to rasterization. As the majority of road actors are vehicles, our training dataset has a much larger number of such actors. We can thus initialize our VRU models with a pre-trained vehicle model trained using more examples. The model is then fine-tuned with VRU training examples until convergence.

4 Experiments

We collected 240 hours of data by manually driving SDV in various traffic conditions (e.g., varying times of day, days of the week). The data contains significantly different number of examples for various actor types, namely 7.8 million vehicles, 2.4 million pedestrians, and 520 thousand bicyclists. Traffic actors were tracked using Unscented Kalman filter (UKF) [40], taking raw sensor data from the camera, lidar, and radar, and outputting state estimates for each object at 10Hz. We considered prediction horizon of 6s (i.e., H = 60) for VRU actors. For the default rasterization scheme (used in the architecture experiments and as a base setting in the ablation study), we rotated raster to actor frame with resolution of 0.2m, including both lane heading and traffic light raster layers.

We implemented models in TensorFlow [1] and trained on 16 Nvidia Titan X GPU cards. We used open-source distributed framework Horovod [28] for training, completing in around 24 hours. We used a per-GPU batch size of 64 and Adam optimizer [14], setting initial learning rate to 10^{-4} further decreased by a factor of 0.9 every 20,000 iterations. Models were trained end-to-end from scratch.

4.1 Comparison of CNN architectures

In the first set of experiments we compared a number of CNN architectures, summarizing results in Table 2. We trained the models on vehicle actors and set the prediction horizon to 6*s*. Average prediction error and latency are reported in the table. The inference latency is measured at a batch of 32 actors on a GTX 1080Ti GPU. As our prediction algorithm performs inference for each actor in the scene, having such a large batch size is not uncommon when SDV is driving on crowded roads.

We compared the prediction accuracy and inference latency on several base CNN architectures. We found that our FMNet gives similar prediction accuracy as other modern architectures such as ResNet, MNv2 and MnasNet, while being much faster in inference. In terms of the number of FLOPs and parameters, FMNet is similar to MNv2-0.5 (which it is based on) and MnasNet-0.5, while AlexNet and ResNet18 have much more FLOPs and parameters. It is interesting to note that AlexNet is the second fastest CNN in our experiment while having large FLOPs (possibly because it has much fewer layers than other considered CNNs), although its accuracy is not on par with the competing networks. Following these results in the rasterization ablation studies we use FMNet as the model architecture.

4.2 Ablation studies on rasterization

We conducted ablation study regarding the rasterization setup, modifying various parameters of the rasterization configuration of the base setup. Empirical results in terms of average prediction error, as well as short- and long-term errors are given in Table 3. We see that the all variants of the proposed CNN approach (referred to as RasterNet) significantly outperform UKF, especially at longer horizons.

First, we analyzed accuracy of the base 0.2m resolution, as compared to other resolution choices. Resolution of 0.1m has smaller coverage, and is expected to benefit slow-moving objects such as pedestrians. On the other hand, 0.3m resolution may benefit fast-moving objects requiring larger coverage. For pedestrians 0.1m-resolution indeed resulted in lower error, while setting 0.3m gave the worst performance. We observed that 0.1m showed no significant difference for bicyclists, while

		Bicyclists			Pedestrians		
Approach	Resolution	Average	@1s	@5s	Average	@1s	@5s
UKF	_	2.89	0.80	6.60	0.67	0.22	1.22
RasterNet	0.1m	1.07	0.43	2.73	0.51	0.17	0.90
RasterNet	0.2m	1.07	0.44	2.72	0.52	0.18	0.93
RasterNet	0.3m	1.09	0.45	2.80	0.53	0.18	0.95
RasterNet w/o rotation	0.2m	1.29	0.49	3.30	0.58	0.20	1.02
RasterNet w/o traffic lights	0.2m	1.11	0.44	2.86	0.55	0.20	0.96
RasterNet w/o lane headings	0.2m	1.07	0.43	2.72	0.52	0.18	0.93
RasterNet with learned colors	0.2m	1.05	0.42	2.70	0.53	0.18	0.93
RasterNet with car pretraining	0.2m	1.05	0.42	2.70	0.59	0.20	1.05

Table 3: Comparison of prediction errors (in meters) for various experimental settings

0.3m resulted in slightly higher error. This may be attributed to the fact that bicyclists are not fast enough to benefit from larger context.

Next, we evaluated the impact of not rotating raster such that actor heading points up, as discussed in Section 3.2, which resulted in a significant drop of accuracy for both actor types. This can be explained by the fact that, when raster is not rotated such that actor heading points up, there is a large number of input data variations that network needs to observe to learn how actors move. In other words, for such setup actors may move in any direction, which is not the case for rotated raster where actors initially always move upwards, resulting in a simplified prediction problem.

We further investigated the affect of encoding traffic light info. The traffic light is important for predicting longitudinal movement, as it can provide info about whether an actor may or may not pass through an intersection. We observed error increase without traffic light rasterization for both actor types, matching this intuition. Furthermore, we removed lane heading information provided in raster images, encoded by using different colors to indicate different directions. Without lane heading bicyclist model degraded slightly in performance, while pedestrian model was unaffected. This again matches intuition, as bicyclists may behave as vehicles and follow lane direction, while pedestrians do not normally use lanes. Finally, we tried learning raster colors instead of setting them manually. The results show that learned colors slightly improved accuracy for bicyclists, whereas the pedestrian model slightly degraded compared to the baseline. This indicates that our manual rasterization setup captured sufficient signal when it comes to pedestrians, while for bicyclists it can be further improved.

Lastly, due to larger amount of vehicle data as compared to VRUs, instead of training from scratch we finetuned VRU models using preloaded weights from the vehicle model. The results show that bicyclist performance improved over the baseline, indicating that bicyclists may exhibit similar behavior to vehicles. On the other hand the pedestrian model regressed, explained by the fact that pedestrian motion is very different from vehicle motion making vehicle pretraining ineffective.

5 Conclusion

We presented an efficient and effective solution to motion prediction of VRU actors. This is a critical problem in autonomous driving, as such actors have higher risk of injury and are less predictable since they may change behavior faster than vehicles. We applied recently proposed rasterization technique to generate raster images of actors' surroundings encoding their context, used as input to deep CNN trained to predict actor trajectory. Moreover, we proposed a fast architecture suitable for real-time operations, and finally presented a detailed ablation study of various rasterization choices.

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