SUPERMARK: ROBUST AND TRAINING-FREE IM AGE WATERMARKING VIA DIFFUSION-BASED SUPER RESOLUTION

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ABSTRACT

In today's digital landscape, the intermingling of AI-generated and authentic content has heightened the importance of copyright protection and content authentication. Watermarking has emerged as a crucial technology to address these challenges, offering a general approach to safeguard both generated and real content. To be effective, watermarking methods must withstand various distortions and attacks. While current deep watermarking techniques typically employ an encoder-noise layer-decoder architecture and incorporate various distortions to enhance robustness, they often struggle to balance robustness and fidelity, and remain vulnerable to adaptive attacks, despite extensive training. To overcome these limitations, we propose SuperMark, a novel robust and training-free watermarking framework. Our approach draws inspiration from the parallels between watermark embedding/extraction in watermarking models and the denoising/noising processes in diffusion models. Specifically, SuperMark embeds the watermark into initial Gaussian noise using existing techniques and then applies pretrained Super-Resolution (SR) models to denoise the watermarked noise, producing the final watermarked image. For extraction, the process is reversed: the watermarked image is converted back to the initial watermarked noise via DDIM Inversion, from which the embedded watermark is then extracted. This flexible framework supports various noise injection methods and diffusion-based SR models, allowing for enhanced performance customization. The inherent robustness of the DDIM Inversion process against various perturbations enables SuperMark to demonstrate strong resilience to many distortions while maintaining high fidelity. Extensive experiments demonstrate SuperMark's effectiveness, achieving fidelity comparable to existing methods while significantly surpassing most in terms of robustness. Under normal distortions, SuperMark achieves an average watermark extraction bit accuracy of 99.46%, and 89.29% under adaptive attacks. Furthermore, Super-Mark exhibits strong transferability across different datasets, SR models, watermark embedding methods, and resolutions.

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040 1 INTRODUCTION

042 With the rapid advancement of text-to-image (T2I) models (Saharia et al., 2022; Rombach et al., 043 2022) and image-to-image (I2I) models (Brooks et al., 2023; Mokady et al., 2023), AI-generated 044 content (AIGC) has been increasingly prevalent and harder to be distinguished from real images. To mitigate the challenges posed by this trend, various regulations (European Parliament, 2023; PBS NewsHour, 2024; Reuters, 2024) have emerged that mandate the embedding of watermarks into 046 AI-generated images. These watermarks serve as a proactive measure for ensuring transparency, 047 traceability, and copyright verification. There are two emerging approaches for watermarking: em-048 bedding watermarks during the image generation process (Fernandez et al., 2023; Wen et al., 2024; Yang et al., 2024) and applying watermarks to the generated images via post-processing (Rahman, 2013; Zhang et al., 2019; Jia et al., 2021). The latter approach is more flexible and general, as it can 051 be applied to both AIGC and real images, which is the focus of this paper. 052

053 The performance of general watermarking is evaluated along two key dimensions: robustness and fidelity. Robustness refers to the watermark's ability to remain detectable and intact even when



Figure 1: (a) The pipeline of traditional watermarking methods, which are trained in an encodernoise layer-decoder manner. (b) The pipeline of our proposed training-free SuperMark. Here, *m* represents for the watermark information.

subjected to various distortions or attacks on the watermarked image, while fidelity means the vi-067 sual consistency between the watermarked image and the cover image. Deep learning-based wa-068 termarking methods typically adopt an encoder-noise layer-decoder framework, introducing various 069 distortions during training to enhance robustness. However, achieving a balance between strong robustness and high fidelity remains a significant challenge for these models. Furthermore, adap-071 tive attacks (Zhao et al., 2023) based on VAE (Ballé et al., 2018; Cheng et al., 2020) and diffusion 072 models (Brooks et al., 2023) can easily circumvent most existing watermarking methods. Although 073 some works have attempted to enhance robustness against such attacks, they often require extensive 074 training with carefully designed differentiable distortions (e.g., StegaStamp (Tancik et al., 2020), 075 RoSteALS (Bui et al., 2023), and Robust-Wide (Hu et al., 2024)) or they compromise fidelity (e.g., StegaStamp (Tancik et al., 2020) and RoSteALS (Bui et al., 2023)). 076

077 We reveal that their limitations are mostly stemmed from the disentanglement between robustness and fidelity due to the the encoder-noise layer-decoder architecture and the joint training strat-079 egy. Moreover, we have two interesting observations: 1) there exists an inherent symmetry between the embedding/extraction of watermarks and the denoising/noising processes in diffusion models, 081 and 2) diffusion process holds inherent robustness against different distortions. Based on these, we propose SuperMark to design a novel diffusion-based general watermarking framework, which can 083 inherently achieve robustness and fidelity in a unified manner. Briefly, the embedding and extraction of a watermark essentially involve a reversible transformation between the watermark information 084 and watermarked image. Similarly, in diffusion models, the processes of denoising and noising 085 represent transformations between the Gaussian noise and sampled image. Leveraging this insight, 086 SuperMark injects the watermark information into the initial Gaussian noise, and defaultly employs 087 the Denoising Diffusion Implicit Model (DDIM) as the sampling method for watermark embed-088 ding, this process is deterministic and exhibits strong reversibility with the denoising process. Most importantly, its corresponding reversible process, known as DDIM Inversion, has demonstrated re-090 markable robustness against various perturbations (Wen et al., 2024; Yang et al., 2024). Thus, Super-091 Mark applies DDIM Inversion to cover the sampled image back into the initial watermarked noise 092 for inherent roboust extraction. To satisfy the fidelity requirement, we feed both the watermarked 093 noise and the cover image into a pretrained diffusion-based Super-Resolution (SR) model to generate the watermarked image. Moreover, this entire process can be executed without any fine-tuning of 094 the SR model. Figure 1 shows a comparison between SuperMark and the traditional watermarking 095 framework. 096

Extensive experimental results demonstrate that SuperMark achieves strong robustness against both normal distortions (e.g., JPEG compression and Gaussian noise) and adaptive attacks (e.g., VAE-based and diffusion-based attacks). It achieves high watermark extraction accuracy, with 99.46% accuracy under normal distortions and 89.29% accuracy even under adaptive attacks on the MS-COCO dataset. Additionally, SuperMark maintains high fidelity, with a PSNR of 32.49 and an SSIM of 0.93. We also evaluate its transferability across different datasets, SR models, watermark injection methods, and image resolutions.

- 104 In summary, our key contributions are as follows:
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In summary, our key contributions are as follows.

Our research uncovers a critical insight into current deep watermarking techniques: the encoder-noise layer-decoder architecture and joint training strategy create a trade-off between robustness and fidelity.

- We introduce SuperMark, a novel and training-free watermarking framework based on diffusion-based super-resolution models. SuperMark's simplicity and effectiveness allow it to seamlessly integrate with various watermark injection methods and pre-trained diffusionbased SR models.
 - Extensive experiments demonstrate that SuperMark offers superior robustness against both normal distortions and adaptive attacks compared to most existing watermarking methods, while maintaining high fidelity.

117 2 BACKGROUND

119 2.1 DIFFUSION MODELS

121 Diffusion Models (DMs) are designed to predict and gradually remove varying levels of noise added 122 to images during training. During inference, they iteratively denoise randomly sampled Gaussian 123 noise $x_T \sim \mathcal{N}(0,1)$, progressively generating high-quality images x_0 . Denoising Diffusion Prob-124 abilistic Models (DDPMs (Ho et al., 2020)) are a widely-used implementation of DMs, but they 125 typically require thousands of denoising steps to produce high-quality samples. To accelerate the sampling process, Denoising Diffusion Implicit Models (DDIMs (Song et al., 2021)) are proposed 126 to improve DDPMs by introducing *a deterministic sampling process* that reduces the number of re-127 quired steps while maintaining the quality of the generated data. Besides, DDIMs can encode from 128 x_0 to x_T and reconstruct x_T from the resulting x_0 with low reconstruction error, a capability that 129 DDPMs lack due to their stochastic nature. In other words, the transformation between x_0 and x_T is 130 reversible. The reverse process $x_T \to x_0$ is known as DDIM Inversion, which enables a wide range 131 of applications, such as image editing (Mokady et al., 2023). 132

Despite these improvements in the sampling speed and efficiency, generating images directly in the 133 pixel space remains computationally expensive in terms of both time and memory. To address it, 134 Latent Diffusion Models (LDMs (Rombach et al., 2022)) are designed to operate in a compressed, 135 lower-dimensional latent space, facilitated by the Variational Autoencoder (VAE) which could sig-136 nificantly reduce the costs. Super-Resolution (SR) models, an important application within Image-137 to-Image (I2I) tasks, can be also implemented using LDMs. The core idea is to concatenate a 138 low-resolution image with a latent variable of the same resolution for denoising. The denoised la-139 tent variable is then decoded using a VAE decoder \mathcal{D} to obtain the corresponding high-resolution 140 image.

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2.2 IMAGE SUPER-RESOLUTION WITH LATENT DIFFUSION

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In this section, we provide a detailed explanation of how the latent diffusion-based super-resolution (SR) model \mathcal{M} achieves image super-resolution. In general, \mathcal{M} employs a Variational Autoencoder (VAE) to realize image resolution, using a scaling factor f_{vae} defined as: $f_{vae} = \frac{S_I}{S_Z}$, where S_I and S_Z represent the size of the input image and its corresponding latent variable produced by the VAE encoder \mathcal{E} . The magnification factor f_{sr} of \mathcal{M} indicates the ratio by which the model increases the input image's resolution, which is equal to f_{vae} .

Specifically, given a low-resolution input image I_{low} with dimensions $(C_{pixel}, H_{low}, W_{low})$, \mathcal{M} performs iterative denoising as follows:

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$$D^{0} = \text{Denoise}(\mathcal{M}(Z_{concat} = I_{low} \oplus Z^{T})), \qquad (1$$

where Z^0 is the denoised latent variable with dimensions $(C_{latent}, H_{low}, W_{low})$, and $Z^T \sim \mathcal{N}(0, 1)$ is randomly sampled Gaussian noise of shape $(C_{latent}, H_{low}, W_{low})$. The input to the SR model, Z_{concat} , is formed by concatenating I_{low} and Z^T , resulting in a shape of $(C_{pixel} + C_{latent}, H_{low}, W_{low})$. Here, C_{pixel} refers to the number of pixel channels (typically 3 for RGB images), C_{latent} is the number of latent channels in the VAE (e.g., 4 for SD-Upscaler), and H_{low} and W_{low} represent the height and width of I_{low} . The super-resolved image I_{sr} , with dimensions $(C_{pixel}, H_{high}, W_{high})$, is then produced by the VAE decoder \mathcal{D} : $I_{sr} = \mathcal{D}(Z^0)$. Since $H_{high} = f_{vae} \times H_{low}$, the magnification factor is given by $f_{sr} = \frac{H_{high}}{H_{low}} = f_{vae}$.

162 2.3 IMAGE WATERMARKING

164 Current image watermarking methods can mainly be divided into two categories: in-generation 165 watermarking and *post-processing* watermarking. In-generation watermarking involves embedding watermarks during the image generation process of a target generative model and has emerged as 166 a key approach alongside the rise of AI-generated content (AIGC). Two notable techniques in this 167 field are Tree-Ring (Wen et al., 2024) and Gaussian Shading (Yang et al., 2024), both designed for 168 diffusion-based text-to-image (T2I) models. These methods embed watermarks into the initial Gaussian noise and utilize inverted noise, obtained through DDIM Inversion, for watermark extraction. 170 Specifically, Tree-Ring embeds multiple rings in the frequency domain center of the Gaussian noise 171 and extracts the watermark from the same positions in the inverted noise's frequency domain. In 172 contrast, Gaussian Shading samples Gaussian noise based on the watermark bit string and extracts 173 the watermark by inverse sampling of the inverted noise. Both techniques have demonstrated strong 174 robustness.

175 However, the aforementioned in-generation watermarking methods are limited to AI-generated im-176 ages and are not the focus of this paper. Instead, we focus on post-processing watermarking methods, 177 which can be applied to both real and generated images. Traditional robust post-processing meth-178 ods, such as DwtDct (Rahman, 2013) and DwtDctSvd (Rahman, 2013), embed watermark messages 179 into transformed domains, offering only limited robustness. With the rise of deep learning, new post-processing watermarking methods based on deep models have emerged to improve robustness. 181 Most follow the encoder-noise layer-decoder framework, where the encoder embeds watermarks, and the decoder extracts them in the pixel space. Different methods use customized noise layers for 182 specific robustness. For example, MBRS (Jia et al., 2021) enhances robustness against JPEG com-183 pression, while StegaStamp (Tancik et al., 2020) and PIMoG (Fang & et al., 2022) target robustness 184 against physical distortions. SepMark (Wu et al., 2023) focuses on inpainting, and Robust-Wide 185 (Hu et al., 2024) addresses instruction-driven image editing. Recently, RoSteALS (Bui et al., 2023) showed that embedding watermarks in the latent space of a VAE significantly boosts semantic ro-187 bustness. Beyond the encoder-noise layer-decoder framework, ZoDiac (Zhang et al., 2024), similar 188 to our approach, embeds watermarks in Gaussian noise for general robustness. However, ZoDiac 189 requires optimizing the initial Gaussian noise for each image to ensure the denoised result closely 190 matches the original. It then adds ring-shaped watermarks using the Tree-Ring method before gener-191 ating the watermarked image with an unconditional diffusion model. This process adds optimization 192 overhead and results in lower fidelity, distinguishing it from our approach.

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3 Methodology

196 197 3.1 DESIGN PRINCIPLES

As illustrated in Figure 1, we compare the design principles of our proposed SuperMark with traditional watermarking methods. Traditional watermarking models typically rely on an encoder and decoder, both of which require extensive training to embed and extract watermarks. In contrast, the core component of our framework is a pre-trained diffusion model, which performs these tasks without additional fine-tuning. Furthermore, while traditional methods require an extra noise layer during training to enhance robustness, our approach leverages the inherent robustness of the diffusion process itself. Below, we discuss the considerations for selecting this diffusion model and how our framework effectively achieves watermark embedding and extraction.

206 Watermark embedding stage: In the traditional pipeline, the encoder takes the original image along with the watermark information and generates a watermarked image that closely resembles the 207 original. For SuperMark, the diffusion model must be image-conditioned so that the denoised output 208 closely matches the conditioned image. Our research indicates that diffusion-based super-resolution 209 (SR) models, which generate higher-resolution versions of conditioned images, effectively meet this 210 requirement. The Gaussian noise added to the conditioned image corresponds to the watermark in-211 formation, allowing the watermark to be injected seamlessly. Techniques such as Gaussian Shading 212 (Yang et al., 2024) and Tree-Ring (Wen et al., 2024) have already been developed to achieve this. 213

Watermark extraction stage: For traditional watermarking methods, the decoder is trained jointly
 with the encoder to extract the embedded watermark from the watermarked image. In contrast,
 SuperMark achieves this using the same SR model employed during watermark embedding. The



Figure 2: The end-to-end inference pipeline of SuperMark.

watermarked image is fed into the model, which performs DDIM Inversion to reconstruct the initial watermarked noise. From this reconstructed noise, the watermark can be extracted effectively, without requiring any additional training.

The flexibility of watermark injection into Gaussian noise and the choice of SR models are key strengths of SuperMark. These components can be interchanged and optimized, presenting exciting opportunities for future research and development.

3.2 OVERVIEW

The complete inference pipeline of SuperMark is illustrated in Figure 2, comprising two stages: 241 watermark embedding and watermark extraction. Both the SR model \mathcal{M} and the VAE operate with 242 frozen parameters, meaning no additional training is required. In the watermark embedding stage, 243 various techniques can be used to inject the watermark into the latent Gaussian noise, resulting 244 in the watermarked noise Z_{wm}^{T} . This noise is then denoised to produce the watermarked image 245 I_{wm} . In the watermark extraction stage, the distorted watermarked image $I_{wm}^{'}$ is processed using 246 DDIM inversion to reconstruct the initial watermarked noise Z'_{wm}^T . From this reconstructed noise, 247 the embedded watermark can be extracted. Below, we first present some preliminaries, followed by 248 a detailed description of our method. 249

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3.3 WATERMARK EMBEDDING

We adopt an off-the-shelf strategy for watermark embedding, as used in *Gaussian Shading* (Yang et al., 2024), with details provided in Appendix A.1. In general, the primary challenge of the watermark embedding process is to address the size discrepancy between the original image and the super-resolved image, while also balancing watermark robustness and image fidelity.

Due to the change in the size of the original image I_{ori} , caused by the SR model \mathcal{M} , the super-257 resolved image I_{sr} cannot be directly used as the watermarked image. A straightforward solution 258 would be to downscale I_{sr} through interpolation to match the size of I_{ori} , using it as the water-259 marked image I_{wm} . However, this resizing process (e.g., downscaling by a factor of 1/4) results 260 in the loss of a significant portion of watermarked pixels, greatly diminishing the robustness of the 261 watermark. To address this issue, we downscale I_{ori} to a smaller size before passing it through \mathcal{M} 262 for upscaling. This reduces the size discrepancy between I_{sr} and I_{ori} , minimizing the loss of wa-263 termarked pixels during resizing and enhancing watermark robustness. However, downscaling I_{ori} 264 before inputting it into the model results in the loss of some original image details, which are then regenerated by the SR model. This leads to a trade-off between the robustness and fidelity, which 265 we will explore in detail in Sec. 4.4. 266

The watermark embedding process is depicted in the upper half of Figure 2. We initially down resize I_{ori} , with a resolution of $H_{ori} \times W_{ori}$, to the image I_{low} with a low resolution of $H_{low} \times W_{low}$. Subsequently, the watermark message s can be injected into the Gaussian noise in various ways to obtain the watermarked Gaussian noise Z_{wm}^T . Then I_{low} and Z_{wm}^T are concatenated to a tensor as 270 \mathcal{M} 's input for iterative denoising to obtain the denoised watermarked latent Z_{wm}^0 which is converted 271 to the super-resolved image I_{sr} by the VAE decoder \mathcal{D} : $I_{sr} = \mathcal{D}(Z_{wm}^0)$. Afterwards, I_{sr} with the 272 resolution of $H_{high} \times W_{high}$ is down resized to acquire I_{sr}^{\downarrow} with the resolution of $H_{ori} \times W_{ori}$. 273 Now I_{sr}^{\downarrow} and I_{ori} have the same size, and we subtract them to get the residual image I_{res} :

$$I_{res} = I_{sr}^{\downarrow} - I_{ori}, \tag{2}$$

Finally, the watermarked image I_{wm} is acquired by:

$$wm = I_{ori} + f_s \times I_{res},\tag{3}$$

where f_s is the strength factor used to balance the fidelity and robustness.

281 3.4 WATERMARK EXTRACTION282

The watermark extraction process is illustrated in the lower part of Figure 2. In this process, I'_{wm} represents a distorted or attacked version of the original watermarked image I_{wm} . We explain how the watermark is extracted from I'_{wm} using DDIM Inversion below.

286 To perform DDIM Inversion using the model \mathcal{M} , the resolution of $I_{wm}^{'}$ must match the resolution 287 used during the model's inference phase. To achieve this, we first upscale I'_{wm} to I'^{\uparrow}_{wm} , ensuring it 288 matches the resolution of the super-resolved image, I_{sr} . The upscaled image is then encoded into the 289 latent space using the VAE encoder \mathcal{E} , resulting in the latent representation $Z_{wm}^{'0}$: $Z_{wm}^{'0} = \mathcal{E}(I_{wm}^{'\uparrow})$. 290 Additionally, we downscale I'_{wm} to I'_{wm} , matching the resolution of the original low-resolution image, I_{low} . Next, the super-resolution model \mathcal{M} takes the concatenated tensor of the latent rep-291 292 resentation Z'^{0}_{wm} and the downscaled image I'^{\downarrow}_{wm} as input. It then performs DDIM Inversion to 293 generate the reverted latent representation of the watermarked image, Z'^{T}_{wm} . Finally, depending on 294 the specific watermark injection method used, the watermark is extracted from Z'_{wm}^T through various 295 extraction techniques.

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3.5 EXTENSION POTENTIAL OF SUPERMARK

Other image-conditioned models. Since the SR model is a core component of our framework and can be easily swapped out, future improvements can leverage more advanced SR models to enhance performance. In Sec. 4.3, we will discuss how enhancing the SR model directly improves both the robustness and fidelity of SuperMark. Beyond super-resolution models, other image-conditioned diffusion models could also be explored, as long as the denoised and conditional images can be closely aligned. This opens up opportunities for further enhancing the framework's flexibility and performance.

Different watermark injection methods. Several existing works have focused on enhancing
 Gaussian Shading and Tree-Ring methods, or introducing novel techniques for watermark injection into Gaussian noise, such as Ring-ID (Ci et al., 2024) and DiffuseTrace (Lei et al., 2024). The
 robustness of SuperMark is significantly influenced by the watermark injection technique employed.
 In Sec. 4.3, we will explore how the watermark injection method utilized in Tree-Ring (Wen et al., 2024) enables SuperMark to exhibit exceptional resistance to geometric distortions, such as rotations. Therefore, these methods can be seamlessly integrated into our framework, leveraging their advantages to enhance the corresponding robustness of SuperMark.

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Inversion accuracy. The robustness of SuperMark is closely tied to the accuracy of the Inversion process: improving Inversion accuracy can reduce the reconstruction error of the initial watermarked noise, thereby enhance the watermark extraction accuracy. Several existing works are exploring more precise Inversion techniques beyond the basic DDIM Inversion, such as those proposed in Hong et al. (2024) and Meiri et al. (2023). Integrating these advanced methods could further bolster the robustness of SuperMark.

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Inference overhead. Since SuperMark requires multiple iterative steps of inference and inversion
 to achieve watermark embedding and extraction, it results in significant inference overhead. However, numerous efforts have been made to accelerate diffusion models, such as using more efficient

sampling methods (Salimans & Ho, 2022), model distillation (Meng et al., 2023), and consistency models (Song et al., 2023). These approaches can reduce the number of sampling steps to just a few, or even a single step, while maintaining image generation quality. For example, SinSR (Wang et al., 2024) is proposed recently to achieve single-step SR generation with a student model obtained by distillation. Additionally, SinSR has demonstrated improved Inversion accuracy, positioning it as another effective approach for enhancing the robustness of SuperMark. In the future, SuperMark can flexibly integrate these acceleration techniques to reduce time costs and enhance practicality.

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- 4 EXPERIMENTS
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4.1 EXPERIMENTAL SETTING

336 Datasets. For our evaluation, we use a default dataset consisting of 500 randomly selected images 337 from the MS-COCO dataset (Lin et al., 2014), a large-scale real-world dataset containing 328K 338 images. Since InstructPixPix requires paired instruction-image data, we extract 500 pairs from the official dataset ¹ to assess robustness. Additionally, to further validate the effectiveness of Super-339 Mark, we conduct tests on several other datasets: DiffusionDB (Wang et al., 2023), WikiArt (Phillips 340 & Mackintosh, 2011), CLIC (Toderici et al., 2020), and MetFACE (Karras et al., 2020), which are 341 commonly used in RoSteALS (Bui et al., 2023) and ZoDiac Zhang et al. (2024) benchmarks. Specif-342 ically, we randomly select 500 images from DiffusionDB, WikiArt, and MetFACE, and use the entire 343 test set of 428 images from CLIC. All images are resized and center-cropped to a resolution of 512 344 × 512. 345

346 **Implementation details.** We use the SD-Upscaler 2 as our default super-resolution (SR) model. 347 For both sampling and inversion, the following configurations are applied: prompt = Null, guidance 348 scale = 1.0, noise level = 0, and steps = 25. The low-resolution image size, S_{low} , is set to 128, and the 349 strength factor, f_s , is set to 0.4. For watermark injection, we configure Gaussian Shading to embed 350 32 bits. To evaluate robustness, we consider the following normal distortions: JPEG compression, 351 random cropping, Gaussian blur, Gaussian noise, and brightness adjustments. Additionally, we 352 examine adaptive attacks, including VAE-based methods such as Bmshi18 (Ballé et al., 2018) and 353 Cheng20 (Cheng et al., 2020), as well as diffusion-based attacks like Zhao23 (Zhao et al., 2023) and InstructPix2Pix (InsP2P) (Brooks et al., 2023). Detailed configurations are provided in Appendix 354 A.2. 355

Metrics. For assessing the fidelity of watermarked images, we utilize Peak Signal-to-Noise Ratio
 (*PSNR*) and Structural Similarity Index Measure (*SSIM*). To measure the robustness and accuracy of
 watermark extraction, we use *Bit Accuracy*. This metric indicates the proportion of watermark bits
 correctly recovered during the extraction process, providing a direct measure of the watermarking
 method's effectiveness in preserving and retrieving the embedded information.

4.2 MAIN RESULTS

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Table 1: Comparison results of SuperMark and baseline methods in terms of fidelity and watermark extraction ability. The **best** and the <u>second</u> best results are highlighted in bold and underlined, respectively.

	Fide	elity	Watermark Extraction Ability (Accuracy ↑)											
Method	PSNR ↑	SSIM↑	Identity			Norm	al Distortic	ns			Ada	ptive Attac	:ks	
	101111	001111	lucinity	JPEG	Crop	G Blur	G Noise	Brightness	Average	Bmshj18	Cheng20	Zhao23	InsP2P	Average
DwtDct	38.0227	0.9652	0.9214	0.5096	0.7881	0.5227	0.7022	0.5635	0.6172	0.5026	0.5027	0.5031	0.5011	0.5024
DwtDctSvd	38.1125	0.9730	0.9988	0.9623	0.8040	0.9917	0.8368	0.5691	0.8328	0.5060	0.5034	0.5006	0.4950	0.5013
RivaGAN	40.5255	0.9788	0.9988	0.9624	0.9967	0.9963	0.9088	0.9490	0.9626	0.5669	0.5618	0.6399	0.5905	0.5898
StegaStamp	28.6922	0.8957	0.9987	0.9981	0.9753	0.9958	0.9236	0.9657	0.9717	0.9979	0.9981	0.9260	0.9209	0.9607
MBRS	43.2538	0.9874	1.0000	0.9965	0.8605	0.7104	0.8035	0.9316	0.8605	0.5607	0.5547	0.5291	0.5296	0.5435
CIN	41.7388	0.9789	1.0000	0.6274	1.0000	0.9130	0.9178	0.9966	0.8910	0.5084	0.5128	0.5026	0.5020	0.5065
PIMoG	37.4647	0.9772	0.9989	0.7804	0.9918	0.9871	0.7078	0.9191	0.8772	0.6336	0.6015	0.5483	0.5191	0.5756
SepMark	35.9085	0.9520	0.9997	0.9985	0.9932	0.9889	0.9667	0.9760	0.9847	0.8312	0.8511	0.7466	0.7394	0.7921
RoŜteALS	28.3445	0.8396	0.9947	0.9745	0.8500	0.9908	0.9231	0.9412	0.9359	0.9074	0.9034	0.8469	0.8412	0.8747
SuperMark	32.4978	0.9322	1.0000	0.9976	1.0000	1.0000	0.9810	0.9946	0.9946	0.9293	0.9310	0.8718	0.8396	0.8929

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¹https://huggingface.co/datasets/timbrooks/instructpix2pix-clip-filtered ²https://huggingface.co/stabilityai/stable-diffusion-x4-upscaler 378 We compare SuperMark with nine open-source baselines, and the results are presented in Table 1. 379 The watermarked images generated by SuperMark exhibit relatively high fidelity, comparable to 380 other baselines. Notably, SuperMark demonstrates significantly stronger robustness than most of 381 the watermarking methods tested. Against normal distortions, SuperMark achieves the highest av-382 erage watermark extraction accuracy of 99.46%. Even in the face of adaptive attacks, which render most watermarking methods ineffective, SuperMark maintains a high robustness with an accuracy of 89.29%. Although this accuracy is slightly lower than StegaStamp, which may have state-of-the-art 384 robustness, SuperMark outperforms in terms of fidelity, with visual results and analyses provided in 385 Appendix A.3. 386

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4.3 TRANSFERABILITY

389 Transfer to different datasets. To evaluate 390 the universality of SuperMark across data with 391 different distributions, we conduct additional 392 experiments on four datasets: DiffusionDB, 393 WikiArt, CLIC, and MetFACE. As shown in 394 Table 2, SuperMark performs effectively across 395 these diverse data distributions. Notably, in the 396 MetFACE dataset, watermarked images exhibit 397 superior fidelity, particularly in terms of PSNR. This may be due to the SR model's proficiency 398 in enhancing details for facial images, allowing 399

Table 2: Test results of SuperMark on different datasets. The gray cell denotes the default setting.

	Fide	elity	Watermark Extraction Ability↑				
Dataset	PSNR ↑	SSIM ↑	Identity	Normal Distortions	Adaptive Attacks		
DiffusionDB	32.5958	0.9318	1.0000	0.9942	0.8751		
WikiArt	32.1425	0.9126	1.0000	0.9950	0.9064		
CLIC	33.0314	0.9387	1.0000	0.9939	0.8870		
MetFACE	37.2351	0.9363	1.0000	0.9952	0.8330		
COCO	32.4978	0.9322	1.0000	0.9946	0.8929		

the generated images to closely approximate the originals. These results further support the idea that
 the stronger the SR model, the higher the fidelity achieved. Visualizations of the results for different
 datasets are provided in Appendix A.3.

LDM-SR as the SR model. Given the flexible selection of the SR model in SuperMark, we also 404 test it with another SR model, LDM-SR³ for transferability assessment, to demonstrate SuperMark's 405 versatility. As the VAE used in LDM-SR has 3 latent channels, it is not possible to configure a 32-406 bit watermark. To ensure a fair comparison, we use 16 embedding bits for both super-resolution 407 models ($f_c = 3$ for LDM-SR and $f_c = 4$ for SD-Upscaler). As shown in Table 3, SuperMark 408 with LDM-SR achieves comparable performance in both fidelity and robustness against normal 409 distortions. However, SD-Upscaler, an SR model with superior performance compared to LDM-410 SR, may provide SuperMark with greater robustness against adaptive attacks. This confirms that 411 improving the capabilities of the SR model used in SuperMark can enhance its overall robustness. 412 We also provide some visual examples in Appendix A.3.

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Table 3: Test results of SuperMark using different SR models.

	Fide	elity					V	Vatermark Ex	straction A	bility↑				
SR Model	PSNR ↑	SSIM↑	Identity			Norm	al Distortio	ons			Ada	ptive Attac	ks	
				JPEG	Crop	G Blur	G Noise	Brightness	Average	Bmshj18	Cheng20	Zhao23	InsP2P	Average
LDM-SR	32.3906	0.9332	1.0000	0.9972	1.0000	1.0000	0.9632	0.9930	0.9907	0.9300	0.9297	0.9411	0.8716	0.9181
SD-Upscaler	32.4747	0.9306	1.0000	0.9998	1.0000	1.0000	0.9883	0.9945	0.9965	0.9626	0.9628	0.9511	0.9066	0.9458

420 Adoption of Tree-Ring's watermark injection method. We also utilize the watermark injection 421 method employed in Tree-Ring (Wen et al., 2024) to further assess the transferability of SuperMark. 422 The configurations of Tree-Ring are: the watermark ring radius r is set to 30 and the threshold τ 423 is set to 0.9, which means the watermark is detected if p falls below this value. As ZoDiac is not 424 open source, we apply the same distortions and attack configurations as described in their paper for 425 comparison (see Appendix A.2 for details). Since Tree-Ring is a 0-bit watermark method, we use 426 the Watermark Detection Rate (WDR) to evaluate the performance aligned with ZoDiac.

The test results of applying Tree-Ring to SuperMark are presented in Table 4 and we also provide some visual results in Appendix A.3. Due to the ring-shaped watermark embedded with the Tree-Ring method, SuperMark demonstrates superior robustness against spatial distortions, such as rotation. Furthermore, compared to ZoDiac, SuperMark maintains better fidelity and exhibits sig-

³https://huggingface.co/CompVis/ldm-super-resolution-4x-openimages

nificantly stronger robustness against rotation, while offering comparable robustness against other
 distortions and attacks.

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Table 4: Comparison results of ZoDiac and SuperMark adopting Tree-Ring's watermark injection method. The corresponding results of ZoDiac are those presented in their paper.

	Fide	elity		Watermark Extraction Ability↑										
Method	PSNR ↑	↑ SSIM↑	SSIM↑	Identity			Norm	al Distortions	Adaptive Attacks					
				JPEG	G Blur	G Noise	Brightness	Rotation	Average	Bmshj18	Cheng20	Zhao23	Average	
ZoDiac	29.41	0.92	0.998	0.992	0.996	0.996	0.998	0.538	0.904	0.992	0.986	0.988	0.989	
SuperMark	32.65	0.94	1.000	0.998	1.000	0.962	0.998	0.978	0.987	0.968	0.990	0.952	0.970	

Transfer to different resolutions. Water-442 marks can be injected into Gaussian noise of 443 varying sizes, enabling SuperMark to embed 444 and extract watermarks for images of different 445 resolutions. As higher-resolution images offer 446 more capacity for watermark embedding, it be-447 comes feasible to embed more bits. To maintain 448 consistency, we keep f_c and f_{hw} constant, en-449 suring the same copy count of each bit, which will also change the length of the embedded 450 bits. Besides, we maintain f_s unchanged to 451

Table 5: SuperMark's test results	on images of dif-
ferent resolutions.	

		Fide	elity	Watermark Extraction Ability↑					
Resolution	Bits	PSNR ↑	SSIM↑	Identity	Normal Distortions	Adaptive Attacks			
256	8	29.5828	0.8929	1.0000	0.9963	0.9091			
384	18	31.5776	0.9239	1.0000	0.9957	0.9014			
512	32	32.4978	0.9322	1.0000	0.9946	0.8929			
640	50	33.6769	0.9392	1.0000	0.9936	0.9002			
768	72	34.5080	0.9408	1.0000	0.9938	0.9012			

452 control the watermark strength added to the original image. This setup allows us to evaluate the
 453 impact of resolution on SuperMark's performance.

The results, shown in Table 5, indicate that SuperMark improves fidelity as image resolution increases while maintaining robustness against both normal distortions and adaptive attacks with more bits embeded. This improvement is due to SR models being more effective at upscaling higherresolution images, whereas upscaling lower-resolution images requires adding more details and involves a larger generative space, which is more challenging. As a result, the generated highresolution image differs more significantly from the corresponding watermarked image, leading to lower fidelity. This also suggests that enhancing the SR model's capabilities can improve the fidelity.

462 4.4 ABLATION STUDY

463 Impact of low image size S_{low} and strength factor f_s . Two important hyperparameters, S_{low} and 464 f_s , play a key role in balancing the fidelity of watermarked images and the bit accuracy of watermark 465 extraction. We conduct a series of comprehensive experiments to explore different combinations of 466 these parameters, and the results are displayed in Figure 3. When f_s is fixed, increasing S_{low} 467 enhances the fidelity but reduces robustness. This is consistent with our previous analysis: larger 468 S_{low} leads to fewer pixel losses in the original image during watermark embedding, but more pixel losses in the watermarked image during extraction. Moreover, for a given S_{low} , increasing f_s , which 469 amplifies the strength of the added watermark residual, improves the robustness of the watermark. It 470 is also worth noting that smaller S_{low} values reduce the memory and time overhead required for both 471 inference and inversion. In practical use, we can configure S_{low} and f_s to maintain both fidelity and 472 robustneelatively high levels. By default, we set $S_{low} = 128$ and $f_s = 0.4$, as this reduces memory 473 usage during inference and improves inference speed. 474

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Impact of inference and inversion steps. We evaluate SuperMark's performance under varying 476 inference and inversion steps, with results presented in Figure 4. Our observations show that differ-477 ent inversion steps have minimal impact on both the fidelity and robustness of SuperMark. However, 478 increasing the number of inference steps results in a slight decrease in fidelity while significantly 479 improving robustness, especially in scenarios involving adaptive attacks. We hypothesize that more 480 inference steps prompt the SR model to generate more detailed features, which increases the dis-481 crepancy between the watermarked and original images, leading to a decline in fidelity. Conversely, these generated details provide more reversible pixels during the inversion process, thereby enhanc-482 ing watermark extraction accuracy. 483

- 484
- **Impact of watermark bits length.** We can embed bits of varying lengths by adjusting different values of f_c and f_{hw} and the results are shown in Figure 5. The fidelity of the watermarked image is



Figure 3: The impact of varying the low image size S_{low} and strength factor f_s on the fidelity and robustness. Robustness is measured by the watermark extraction accuracy on watermarked images subjected to normal distortions and adaptive attacks. Lines of different colors represent different values of S_{low} .



509 Figure 4: Effects of SuperMark on fidelity and robustness with varying inference and inversion 510 steps.

maintained across different bit lengths, as it has been shown that in Gaussian Shading, the sampling of Gaussian noise based on bits does not affect the model's denoising performance. Consequently, the SR model generates images with consistent fidelity, irrespective of the bit length employed. However, embedding more bits leads to a corresponding decrease in SuperMark's robustness, par-ticularly when faced with adaptive attacks. This is expected, as embedding more bits requires a larger number of successfully inverted pixels for extraction, while the proportion of invertible pixels in a corrupted image remains fixed. Consequently, the accuracy of watermark extraction diminishes as the bit length increases.



Figure 5: Fidelity and robustness when embedding watermark bits of different lengths.

5 CONCLUSION

In this paper, we propose a training-free and robust image watermarking framework, named SuperMark, which leverages a diffusion-based SR model to achieve effective watermark embedding
and extraction. Thanks to the inherent resilience of DDIM Inversion to various distortions, SuperMark demonstrates superior robustness compared to nearly all existing watermarking methods
while maintaining high fidelity. Extensive experiments highlight its outstanding performance across different datasets, watermark injection methods, SR models, and image resolutions.

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A APPENDIX

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A.1.1 GAUSSIAN SHADING

The watermark is a bit string s consisting of 0s and 1s, with a length defined as $\frac{c}{f_c} \cdot \frac{h}{f_{hw}} \cdot \frac{w}{f_{hw}}$, where c, h, and w represent the channels, height, and width of the Gaussian noise used for watermark injection, and f_c , f_{hw} are scaling factors for expansion. The string s is then replicated $f_c \cdot f_{hw}^2$ times and reshaped into its diffused version s^d with the shape (c, h, w). To preserve the distribution and obtain the corresponding watermarked Gaussian noise Z_{wm}^T , s^d is transformed into a uniformly distributed randomized watermark m through encryption (e.g., ChaCha20 (Bernstein et al., 2008)) using a stream key K. The watermarked Gaussian noise Z_{wm}^T is sampled as follows:

$$p(Z_{wm}^T|y=i) = \begin{cases} 2 \cdot f(Z_{wm}^T) & ppf\left(\frac{i}{2}\right) < Z_{wm}^T \le ppf\left(\frac{i+1}{2}\right) \\ 0 & \text{otherwise} \end{cases}$$

where $y \in \{0, 1\}$ is the bit in s^d . Since *m* follows a uniform distribution, it can be shown that Z_{wm}^T preserves the Gaussian distribution, ensuring that the fidelity of the image denoised from Z_{wm}^T is not affected.

After performing DDIM inversion, the inverted Gaussian noise Z'^T_{wm} is obtained, and the diffused watermark s'^d is extracted by:

$$i' = |2 \cdot cdf(Z_{wm}'^T)|,$$

where i' is the extracted bit in m'. The decrypted version of m' using K yields s'^d , which consists of $f_c \cdot f_{hw}^2$ copies of the watermark. The extracted watermark s' is then reconstructed using a voting mechanism: if a bit is set to 1 in more than half of the copies, the corresponding bit in s' is set to 1; otherwise, it is set to 0.

702 A.1.2 TREE-RING

The watermark is a key k^* composed of multiple rings, with a constant value along each ring. The key k^* is injected into the Fourier transform of the initial Gaussian noise Z^T to obtain the watermarked Gaussian noise Z_{wm}^T . Specifically, a circular mask M with radius r centered on the low-frequency modes is chosen, and the injection process is described as:

$$\mathcal{F}(Z_{wm}^T) \sim \begin{cases} k_i^* & i \in M\\ \mathcal{N}(0,1) & \text{otherwise} \end{cases}$$

For watermark extraction, let $y = \mathcal{F}(Z'^T_{wm})$, and the score μ is defined as:

$$\mu = \frac{1}{\sigma^2} \sum_{i \in M} |k_i^* - y|^2,$$

where $\sigma^2 = \frac{1}{M} \sum_{i \in M} |y_i|^2$. An interpretable P-value p is computed as:

 $p = \Pr(\chi^2_{|M|,\lambda} \le \mu \mid H_0) = \Phi_{\chi^2}(z),$

where $\Phi_{\chi^2}(z)$ is a standard statistical function. The watermark is "detected" when p falls below a chosen threshold α .

724 A.2 More implementation details 725

Configurations of normal distortions. The default configurations of different normal distortions are: JPEG (Q=50), Random Crop (ratio=0.8), Gaussian Blur (r=2), Gaussian Noise (std=0.05), Brightness (factor=2). When testing on Tree-Ring, the configurations are: JPEG (Q=50), Gaussian Blur (r=5), Gaussian Noise (std=0.05), Brightness (factor=0.5), Rotation (degrees=90).

Configurations of adaptive attacks. For Bmshj18 and Cheng20, we use the models from CompressAI⁴ (bmshj2018_hyperprior and cheng2020_anchor) with compression factor=3. For Zhao23, we use the model ⁵ with noise&denoise steps=20 by default and steps=60 when testing on Tree-Ring. For InstructPix2Pix, we use the model ⁶ with text guidance=7.5, image guidance=1.5 and inference steps=25.

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A.3 VISUAL RESULTS

738 Fidelity comparison with StegaStamp, RoSteALS and SuperMark. Figure 7 compares the fi-739 delity distribution of StegaStamp, RoSteALS and SuperMark, which have comparable robustness. SuperMark demonstrates the best performance in both PSNR and SSIM, with stability only slightly 740 behind StegaStamp. While StegaStamp shows relatively consistent results, its fidelity lags behind 741 SuperMark. On the other hand, RoSteALS exhibits significant variability in both PSNR and SSIM, 742 resulting in lower and less stable fidelity. Figure 8 showcases some examples where SuperMark 743 produces relatively low fidelity, primarily due to the complex composition and detailed content of 744 the original images. The SR model adopted in SuperMark may face challenges with these intricate 745 contents and have more generative freedom, leading to lower fidelity. However, we believe that 746 future advancements in more powerful SR models will further enhance the fidelity for such images. 747

We also select some watermarked images generated by StegaStamp, RoSteALS and SuperMark
which can be found in Figure 9 and Figure 10. From the residual images, we can see that the
watermarks embedded by our method are more concentrated at the edges of objects, that is, at
places with strong semantic correlation, thus ensuring both fidelity and strong robustness. However,
StegaStamp embeds more watermarks in both objects and backgrounds, which improves robustness
but sacrifices more fidelity.

754 ⁴https://github.com/InterDigitalInc/CompressAI/tree/master

^{755 &}lt;sup>5</sup>https://huggingface.co/stable-diffusion-v1-5/stable-diffusion-v1-5

⁶https://huggingface.co/timbrooks/instruct-pix2pix



Figure 6: Some visual results from the default COCO dataset. The last row marks the distortion or attack type of each column and the corresponding watermark extraction accuracy.



Figure 7: Fidelity distribution of watermarked images generated by StgeaStamp, RoSteALS and SuperMark on the default COCO dataset.

Watermarked images generated by SuperMark on different datasets. See Figure 11, Figure 12, Figure 13 and Figure 14. It can be observed that for different types of images from various datasets, SuperMark is able to achieve high-fidelity watermarked image generation, with the watermark embedded at the edges of semantically relevant objects.

Watermarked images generated by SuperMark using LDM-SR as the SR model and Tree Ring as the watermark injection method. See Figure 15 and Figure 16. It can be observed that,
 despite using different SR models and watermark injection methods, SuperMark consistently shows
 similar embedding patterns on the same original image, leading to comparable fidelity. This further
 reinforces the strong transferability of our method.



Figure 8: Some watermarked images with relatively low fidelity generated by SuperMark. From the first row to the fourth row are: original image, residual image, watermarked image and PSNR/SSIM. Same for the following Figures.



Figure 9: Comparison of watermarked images generated by StegaStamp, RoSteALS and Super-Mark.



Figure 10: Comparison of watermarked images generated by StegaStamp, RoSteALS and Super-Mark.



Figure 11: Some watermarked images generated by SuperMark with the original images sampled from the DiffusionDB dataset.



1025 Figure 12: Some watermarked images generated by SuperMark with the original images sampled from the WikiArt dataset.



Figure 13: Some watermarked images generated by SuperMark with the original images sampled from the CLIC dataset.



1079 Figure 14: Some watermarked images generated by SuperMark with the original images sampled from the MetFACE dataset.



Figure 15: Comparison of watermarked images generated by SuperMark with default setting, LDM-SR as the SR model and Tree-Ring as the watermark injection method. The first column is the default setting, the second column is using LDM-SR, and the third column is using Tree-Ring. Same as Figure 16.



Figure 16: Comparison of watermarked images generated by SuperMark with default setting, LDM-SR as the SR model and Tree-Ring as the watermark injection method.