# <span id="page-0-0"></span>UNMASKING TREES FOR TABULAR DATA

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### ABSTRACT

Despite much work on advanced deep learning and generative modeling techniques for tabular data generation and imputation, traditional methods have continued to win on imputation benchmarks. We herein present UnmaskingTrees, a simple method for tabular imputation (and generation) employing gradient-boosted decision trees which are used to incrementally unmask individual features. This approach offers state-of-the-art performance on imputation, and on generation given training data with missingness; and it has competitive performance on vanilla generation. To solve the conditional generation subproblem, we propose a tabular probabilistic prediction method, BaltoBot, which fits a *bal*anced *t*ree *o*f *bo*osted *t*ree classifiers. Unlike older methods, it requires no parametric assumption on the conditional distribution, accommodating features with multimodal distributions; unlike newer diffusion methods, it offers fast sampling, closed-form density estimation, and flexible handling of discrete variables. We finally consider our two approaches as meta-algorithms, demonstrating in-context learning-based generative modeling with TabPFN.

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#### 1 INTRODUCTION

**027 028 029 030 031 032 033** Given a tabular dataset, it is frequently desirable to impute missing values within that dataset, and to generate new synthetic examples. On data generation, recent work [\(Jolicoeur-Martineau et al.,](#page-11-0) [2024b\)](#page-11-0) (ForestDiffusion) has shown state-of-the-art results on data generation using gradient-boosted trees [\(Chen & Guestrin, 2016\)](#page-10-0) trained on diffusion or flow-matching objectives, outperforming deep learning-based approaches. However, this approach tended to struggle on tabular imputation tasks, outperformed by MissForest [\(Stekhoven & Bühlmann, 2012\)](#page-12-0), an older multiple imputation approach based on random forests [\(Breiman, 2001\)](#page-10-1).

**034 035 036 037 038 039 040 041 042** We address this shortfall by training gradient-boosted trees to autoregressively unmask features in random order, via permutation language modeling  $(Yang, 2019)$ . This autoregressive approach, which we dub UnmaskingTrees, naturally performs conditional generation (i.e. imputation): we simply fill in and condition on observed values, autoregressively generating the remaining missing values. This contrasts with tabular diffusion modeling, for which the RePaint inpainting algorithm [\(Lugmayr et al.,](#page-11-1) [2022\)](#page-11-1) is employed to mediocre effect [\(Jolicoeur-Martineau et al., 2024b\)](#page-11-0). Because the predictor for a given feature must condition on varying subsets of the other features, the ability of gradient-boosted trees to handle missing features makes them a natural choice for autoregressive modeling. Hence, we maintain the tree-based approach of **Jolicoeur-Martineau et al.** [\(2024b\)](#page-11-0), while replacing their tree-based regressors with our novel tree-based probabilistic predictors, which we turn to next.

**043 044 045 046 047 048 049 050 051 052 053** While mean-estimating regression models are satisfactory for diffusion, for autoregression we must inject noise, and hence must estimate the entire conditional distribution of each feature. We therefore revisit the long-studied problem of (tabular) probabilistic prediction [\(Le et al., 2005;](#page-11-2) Meinshausen  $\&$ [Ridgeway, 2006\)](#page-12-2). Because the conditional distribution is possibly multi-modal, parametric approaches such as XGBoostLSS [\(März, 2019\)](#page-11-3), NGBoost [\(Duan et al., 2020\)](#page-10-2), and PGBM [\(Sprangers et al.,](#page-12-3) [2021\)](#page-12-3) are poor choices for our setting. Meanwhile, quantization of a continuous variable can model its multi-modality, but at the cost of destroying either low-resolution or high-resolution information. A diffusion-based method, Treeffuser [Beltran-Velez et al.](#page-10-3) [\(2024\)](#page-10-3), was recently proposed to address these problems. However, as a diffusion method, it suffers from slow sampling and is unable to provide closed-form density estimates; furthermore, Treeffuser does not naturally model discrete outcomes. To address these problems, we propose BaltoBot, a *bal*anced *t*ree *o*f *bo*osted *t*rees. For each individual variable, we recursively divide its output space with the kernel density integral (KDI) **054 055 056 057 058** quantizer [\(McCarter, 2023\)](#page-12-4) into a "meta-tree" of binary classifiers, which for us are gradient-boosted trees. This allows us to efficiently generate samples and estimate densities, because each sample follows only one path from root to leaf of the meta-tree. Performing regression with hierarchical classification proved successful in computer vision object bounding box prediction [\(Li et al., 2020\)](#page-11-4), but has been surprisingly underexplored in tabular ML and in generative modeling.

**059 060 061 062 063 064 065 066 067 068** Our two methods are in fact meta-algorithms that, in combination, can create a generative model out of *any* probabilistic binary classifier. To demonstrate this flexibility, we swap out XGBoost [\(Chen &](#page-10-0) [Guestrin, 2016\)](#page-10-0) for TabPFN [\(Hollmann et al., 2022\)](#page-10-4). TabPFN is a deep learning model pretrained to perform in-context learning for tabular classification. While it has state-of-the-art classification benchmark performance [\(McElfresh et al., 2024\)](#page-12-5), it currently does not perform regression tasks, nor does it inherently perform generative modeling [\(Ma et al., 2024\)](#page-11-5). Constructing a generative model out of TabPFN [\(Hollmann et al., 2022\)](#page-10-4) was first proposed in TabPFGen [\(Ma et al., 2024\)](#page-11-5), which approximates the posterior from TabPFN-provided likelihoods by iteratively applying stochastic gradient Langevin dynamics (Welling & Teh,  $[2011]$ ). But unlike the previous work, ours requires only a few TabPFN forward-passes for each sample rather than many iterative data updates.

**069 070 071 072 073 074** We showcase UnmaskingTrees on two tabular case studies, and on the benchmark of 27 tabular datasets presented by [Jolicoeur-Martineau et al.](#page-11-0) [\(2024b\)](#page-11-0). Most notably on this benchmark, our approach offers state-of-the-art performance on imputation and on generation given training data with missingness; and it has competitive performance on vanilla generation. We also demonstrate that BaltoBot is on its own a promising method for probabilistic prediction, showing its advantages on synthetic case studies and on a heavy-tailed sales forecasting benchmark.

**075 076 077 078 079 080 081** Finally, we provide code with an easy-to-use sklearn-style API at [https://github.com/](https://github.com/another-anonymous-account/unmasking-trees) [another-anonymous-account/unmasking-trees](https://github.com/another-anonymous-account/unmasking-trees). In addition to being useful for practitioners, we hope our work sparks study within the tabular ML community about whether diffusion or autoregression is better for tabular data. Previous autoregressive tabular modeling methods, TabMT [\(Gulati & Roysdon, 2024\)](#page-10-5) and DP-TBART [\(Castellon et al., 2023\)](#page-10-6), use Transformer [\(Vaswani, 2017\)](#page-12-7) models, making them less applicable for the GPU-poor. Our simple, efficient implementations of UnmaskingTrees and BaltoBot contribute to investigating this question.

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### 2 METHOD

#### 2.1 UNMASKINGTREES FOR TABULAR JOINT DISTRIBUTION MODELING

UnmaskingTrees combines the gradient-boosted trees of ForestDiffusion [\(Jolicoeur-Martineau et al.,](#page-11-0) [2024b\)](#page-11-0) with the training objective of generalized autoregressive language modeling [\(Yang, 2019\)](#page-12-1), inheriting the benefits of both. Consider a dataset with  $N$  examples and  $D$  features. We learn the joint distribution over *D*-dimensional example x by maximizing the expected log-likelihood with respect to all possible permutations of the factorization order,

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\log p(\mathbf{x}) = \log \mathbb{E}_{\sigma \in \mathcal{U}(G_D)} \Big[ \prod_{t=1}^{D} p(x_{\sigma(t)} | \mathbf{x}_{\sigma(
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**096 097 098 099 100 101** where  $\sigma$  is a permutation drawn uniformly from  $\mathcal{U}(G_D)$ , the permutation group on *D* features;  $\mathbf{x}_{\sigma(\langle t \rangle)}$ denotes all features that precede the *t*-th feature in the permuted sequence of features. If we were to have marginalized over permutations, we would have obtained a masked language modeling procedure with a randomly-sampled masking rate  $r \sim \mathcal{U}(0, 1)$  [\(Kitouni et al., 2023;](#page-11-6) [2024\)](#page-11-7); such a procedure was previously shown to have benefits in combination with tabular Transformer models [\(Gulati & Roysdon, 2024\)](#page-10-5) (TabMT).

**102 103 104 105 106 107** For each example, we generate new training samples by randomly sampling an order over the features, then incrementally masking the features in that random order. Given duplication factor *K*, we repeat this process *K* times with *K* different random permutations, leading to a training dataset with *KND* samples. Given this, we train XGBoost (Chen & Guestrin,  $2016$ ) models to predict each unmasked sample given the more-masked example derived from it, one per feature. We model categorical features via softmax-based classification with cross-entropy loss; our approach for continuous features is described in Section [2.2.](#page-2-0)

**108 109 110 111** For both generation and imputation, we generate features of each sample in random order. For imputation rather than generation tasks, we begin by filling in each sample with the observed values, and run inference on the remaining unobserved features. Implementing this is very simple: it requires about 70 lines of Python code for training, and about 20 lines for inference.

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#### <span id="page-2-0"></span>2.2 BALTOBOT FOR TABULAR PROBABILISTIC PREDICTION

**115 116 117 118 119 120 121 122 123** A key problem when autoregressively generating continuous data is that a regression model will attempt to predict the mean of a conditional distribution, whereas we would like it to sample from the possibly-multimodal conditional distribution. The simplest solution is to quantize continuous features into bins, because classification over histograms is inherently multimodal; TabMT [\(Gulati](#page-10-5) [& Roysdon, 2024\)](#page-10-5) did this with 1d k-Means clustering [\(Lloyd, 1982\)](#page-11-8). Yet this not only destroys information within bins due to rounding, it also destroys information about the proximity among the ordered bins. Thus, it forces us to choose between a small number of quantization bins, yielding low resolution; or to choose a large number of bins, risking catastrophic errors due to overfitting and/or clumping of generated samples due to poor calibration. This not only limits performance, but also necessitates hyperparameter tuning [\(Gulati & Roysdon, 2024\)](#page-10-5).

**124 125 126 127 128 129 130 131 132 133 134 135** Inspired by this, we propose a general-purpose solution to the tabular probabilistic prediction problem. For each individual regression output variable, we build a height-*H* balanced tree of binary classifiers. Consider a node with height *h* on this "meta-tree", which is fit with  $(\mathbf{X}_{\text{train}} \in \mathbb{R}^{n \times d}, \mathbf{y}_{\text{train}} \in \mathbb{R}^n)$ . Using kernel density integral quantization (KDI)  $\sqrt{\text{McCarter}}$ ,  $\sqrt{2023}$ ), which adaptively interpolates between uniform quantization and quantile quantization, we obtain binarized  $\tilde{\mathbf{y}}_{\text{train}} \in [0, 1]^n$ . Thus, the input space to every node is partitioned into two with the splitting point determined by KDI. We train an XGBoost classifier on  $(\mathbf{X}_{train}, \tilde{\mathbf{y}}_{train})$ . If  $h > 0$ , we then recursively pass  $\{(\mathbf{X}^{(i)}, y^{(i)}) \in$  $(\mathbf{X}_{train}, \mathbf{y}_{train})|\tilde{y}^{(i)} = 0$  to its left child, and analogously for  $\tilde{y}^{(i)} = 1$  to its right child. At a leaf node,  $h = 0$ , if given a single unique training set output value in a bin, we record this value. At inference time, given a query input  $X$ , we descend the tree by obtaining predicted probabilities from each node's XGBoost classifier, then sampling from these. Once we reach a leaf node, we either sample uniformly from its appropriate bin, or we return the lone output value if a singleton bin.

**136 137 138 139 140 141 142 143** At training and inference time, each XGBoost model within the meta-tree only sees examples that fall into its corresponding region of the output space. Thus, for a meta-tree with height *H* (and thus 2*<sup>H</sup>* models), each example is only passed as input to *H* different models. While lower-level classifiers receive less data and are poorer quality, the magnitude of such errors are smaller due to our hierarchical partitioning approach. Furthermore, our singleton-bin technique allows us to adaptively generate discrete and even mixed-type variables, if these discrete outcomes are high-frequency relative to the total size of the data and to the height of the meta-tree. (Up to 2*<sup>H</sup>* discrete outcomes can be produced by BaltoBot.) Finally, eschewing diffusion modeling enables us to perform closed-form conditional density estimation.

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#### Algorithms for UnmaskingTrees and BaltoBot are given in Appendix Section [A.](#page-0-0)

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#### 2.3 COMPUTATIONAL COMPLEXITY

**149 150 151 152 153 154 155 156** ForestDiffusion, with *T* diffusion steps and duplication factor *K*, constructs a training dataset of size  $TKN \times D$ . Given the same duplication factor *K*, UnmaskingTrees will construct a training dataset of size  $KND \times D$ . Meanwhile, ForestDiffusion must train  $DT$  different XGBoost regression models. We, on the other hand, train *D* different BaltoBot models, one per feature; with BaltoBot meta-tree height of *H*, we then train a total of *D*2*<sup>H</sup>* XGBoost binary classifiers. However, classifiers lower in the BaltoBot meta-tree become progressively faster to train. Indeed, each constructed training sample will be seen by *DT* different XGBoost regressors with ForestDiffusion, but only *DH* classifiers with our approach. Given that  $T \sim 50$  and  $H \sim 4$ , this yields a large speedup for our approach.

**157 158 159** The KDI quantizer [\(McCarter, 2023\)](#page-12-4) has negligible contribution to runtime, because it uses the polynomial-exponential kernel density estimator (KDE) ( $Hofmeyr$ , 2019), which has linear complexity in sample size for 1d data, unlike the quadratic complexity of the Gaussian KDE.

**160 161** At inference time, each ForestDiffusion generated sample passes through *T* steps of the diffusion reverse-process, for a total of *DT* XGBoost predictions. For UnmaskingTrees with BaltoBot, each generated sample instead requires only *DH* XGBoost predictions, because each sample follows only  one path from root to leaf of the meta-tree. The resulting speedup is especially impactful for the multiple imputation scenario, where inference time dominates.

#### 2.4 IN-CONTEXT LEARNING-BASED GENERATION WITH BALTOBOTABPFN AND UNMASKINGTABPFN

Within our flexible frameworks for joint and conditional modeling, TabPFN [\(Hollmann et al., 2022\)](#page-10-4) can be used as a base learner for probabilistic prediction and generative modeling. For UnmaskingTabPFN joint modeling, a difficulty arises from TabPFN's inability to handle inputs  $\mathbf{X}_{\text{train}}$  with missing values (NaNs). To address this, we developed NanTabPFN, a wrapper for TabPFN that supports missingness in both training and test features. Based on each test query  $x_{test}$ , we select row indices  $R$  and column indices  $C$  so that  $[\mathbf{X}_{train}]\}_{R,C}$  has no NaNs, using the following key idea. Consider a particular train example  $\mathbf{x}_{train}$  and test query  $\mathbf{x}_{test}$ , with visible (non-missing) features denoted by sets  $V(\mathbf{x}_{train})$  and  $V(\mathbf{x}_{test})$ . We can maximize the number of utilized features, while also ensuring that TabPFN receives no NaNs, by restricting the set of columns to those observed for the test query,  $C := \mathcal{V}(\mathbf{x}_{\text{test}})$ , then choosing training examples  $\mathcal{R} := \{i | C \subseteq \mathcal{V}(\mathbf{x}_{\text{train}}^{(i)})\}$ . In practice, our procedure is more complicated, because the above choices may result in either empty *C* or empty *R*. If  $R$  is empty, we incrementally set random features of  $\mathbf{x}_{test}$  to missing until we are able to obtain a non-empty training set. If *C* is empty, we introduce a new all-1s feature to both  $X_{train}$  and  $X_{test}$ .

#### 3 RESULTS

 



<span id="page-3-0"></span>Figure 1: Results on Two Moons case study. Original data is shown in green; generated data is shown in red; imputed data is shown in blue.

 We evaluate UnmaskingTrees on two case studies (Section  $[3.1]$ ) and on a tabular benchmark of 27 datasets (Section  $\overline{3.2}$ ). We then evaluate BaltoBot and BaltoBoTabPFN on tabular probabilistic prediction case studies (Section  $\overline{3.3}$ ) and on a sales forecasting dataset (Section  $\overline{3.4}$ ). Results were obtained always using the default hyperparameters: output tree height of 4, and duplication factor  $K = 50$ . These hyperparameter values were tuned on the Two Moons and Iris case studies, then applied without further tuning to the remaining experiments, because hyperparameter tuning is no fun at all. XGBoost hyperparameters were set to their defaults. Experiments were performed on a iMac (21.5-inch, Late 2015) with 2.8GHz Intel Core i5 processor and 16GB memory.

 Overall, UnmaskingTrees (using BaltoBot) has state-of-the-art performance on imputation and on generation after training on incomplete data; and it has competitive performance on vanilla tabular generation scenarios. We further demonstrate the benefits of BaltoBot and BaltoBoTabPFN when evaluated in their own right for probabilistic prediction.



<span id="page-4-1"></span>Figure 2: Results on Iris dataset, with species, petal width, and petal length depicted. Original data and synthetically-generated datasets are shown on the left columns. The imputed dataset is shown on the right columns, with  $\times$  symbols highlighting the samples with any missingness that required imputation.

 

#### <span id="page-4-0"></span>3.1 CASE STUDIES ON TWO MOONS AND IRIS DATASETS

 Two Moons dataset We first compare our approach to previous leading methods on the synthetic Two Moons dataset with 200 training samples and noise level  $\mathcal{N}(0, 0.1)$ . We compare Unmask-ingTrees to MissForest [\(Stekhoven & Bühlmann, 2012\)](#page-12-0), MICE-Forest [\(Van Buuren et al., 1999;](#page-12-8) Wilson et al., ) (another popular traditional multiple imputation method), and ForestDiffusion, with default hyperparameters for all methods. For ForestDiffusion, we evaluate both the variancepreserving SDE diffusion (Forest-VP) and flow-matching (Forest-Flow) versions on generation; on imputation, we evaluate Forest-VP with and without RePaint, again using default RePaint hyperparameters; Forest-Flow does not support imputation.

 We show results in Figure  $\overline{1}$ . On generation, Forest-VP appears to do best according to visual inspection, while UnmaskingTrees and Forest-Flow perform similarly decently. UnmaskingTabPFN performs poorly, but does capture the overall shape of the distribution. Next, we turn to imputation, wherein we request a single imputation for a copy of the original training data with the second dimension (*y*-axis) values masked out. ForestDiffusion struggles with and without RePaint, with substantial out-of-distribution imputations, and MissForest and MICE-Forest share this problem to lesser degrees. Meanwhile, UnmaskingTrees generates impeccable imputations.

 **Iris dataset** In Figure  $\hat{Z}$ , we show results for the Iris dataset [\(Fisher, 1936\)](#page-10-8), plotting petal length, petal width, and species. We compare both methods on generation, and to compare on imputation, we create another version of the Iris dataset, with missingness completely at random: we randomly select samples with 50% chance to have any missingness, and on these samples, we mask the nonspecies feature values with 50% chance. Visually, ForestDiffusion and UnmaskingTrees perform about equally well on generation. Meanwhile, on imputation, UnmaskingTrees does a better job

**270 271 272** conditioning on species information than ForestDiffusion. UnmaskingTrees also produces more diverse imputations than MissForest.

<span id="page-5-0"></span>3.2 BENCHMARKING UNMASKINGTREES ON 27 TABULAR DATASETS

**275 276 277 278 279 280 281 282 283 284 285** Imputation Here, we add UnmaskingTrees to the benchmark of 8 imputation methods on 27 public datasets, evaluated according to 9 metrics, developed by [Jolicoeur-Martineau et al.](#page-11-0) [\(2024b\)](#page-11-0) for evaluating tabular imputation and generation methods. This benchmark primarily contains smallersized (with  $103 \le N \le 20,640$  and  $4 \le D \le 90$ ) datasets, which our approach is especially geared towards. Namely, we compare our approach against Forest-VP [Jolicoeur-Martineau et al.](#page-11-0) [\(2024b\)](#page-11-0), as well as k-NN imputation [\(Troyanskaya et al., 2001\)](#page-12-10), ICE [\(Buck, 1960\)](#page-10-9), MICE-Forest [\(Van Buuren](#page-12-8) [et al., 1999;](#page-12-8) [Wilson et al., 2022\)](#page-12-9), MissForest [\(Stekhoven & Bühlmann, 2012\)](#page-12-0), Softimpute [\(Hastie](#page-10-10) et al.,  $[2015]$ , minibatch Sinkhorn optimal transport (Muzellec et al.,  $[2020]$ ), and generative adversarial nets (GAIN) [\(Yoon et al., 2018\)](#page-12-12). <sup>[1](#page-5-1)</sup> We follow [Jolicoeur-Martineau et al.](#page-11-0) [\(2024b\)](#page-11-0) in computing the per-dataset rank of each method relative to other methods, then reporting the average over 27 datasets. For all methods other than our own, we compute ranks by reusing the raw scores provided in [Jolicoeur-Martineau et al.](#page-11-0) [\(2024b\)](#page-11-0)'s code repository.

**286 287 288 289 290 291** Results for imputation are shown in Table  $\Pi$ . Unmasking Trees wins first place on 3/9 metrics, including both metrics based on downstream prediction tasks; and it generally outperforms ForestDiffusion, winning on 8/9 metrics. While MissForest wins first place on 4/9 metrics, UnmaskingTrees wins 5-4 head-to-head vs MissForest; UnmaskingTrees has average *averaged rank* of 3.2 compared to 3.5 for MissForest. UnmaskingTrees is also the only method with better than 5th place rank on all metrics.

**292 293 294 295** We report further ablation experiments in Table  $2$ , wherein we run UnmaskingTrees without BaltoBot, and instead with vanilla quantization using k-Means clustering  $(Lloyd, 1982)$  and KDI quantization  $\langle \text{McCarter}, 2023 \rangle$ . Results showing progressive improvements for the UnmaskingTrees framework, for KDI quantization versus k-Means, and for the BaltoBot method used in our full proposed solution.

**297 298 299 300 301 302 303** Table 1: Tabular data imputation (27 datasets, 3 experiments per dataset, 10 imputations per experiment) with 20% missing. Shown are *averaged rank* over all datasets and experiments (standard-error). Overall best is **highlighted**; better of Forest-VP versus ours is **boldface blue**. Metrics are Minimum and Average mean-absolute error (MinMAE and AvgMAE) to ground-truth, Wasserstein distance to train and test dataset distributions (*Wtrain* and *Wtest*), Mean Absolute Deviation (MAD) around the median/mode (for diversity), *R*<sup>2</sup> and *F*<sup>1</sup> for downstream regression / classification problems, and percent bias *Pbias* and confidence interval coverage rate *Covrate* for statistical inferences.



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> Generation with and without missingness We next repeat the experimental setup of [Jolicoeur-](#page-11-0)[Martineau et al.](#page-11-0) [\(2024b\)](#page-11-0) for evaluating tabular generation methods. For tabular generation, using the same 27 datasets, [Jolicoeur-Martineau et al.](#page-11-0) [\(2024b\)](#page-11-0) benchmark their methods (Forest-VP and Forest-Flow) against 6 other methods, namely, Gaussian Copula [\(Joe, 2014\)](#page-11-9), tabular variational autoencoding (TVAE)  $(Xu et al., 2019)$ , two conditional generative adversarial net methods (CTGAN [\(Xu et al., 2019\)](#page-12-13) and CTAB-GAN+ (Zhao et al.,  $[2021]$ ), and two other tabular diffusion methods (STaSy (Kim et al.,  $2022$ ) and TabDDPM (Kotelnikov et al.,  $2023$ )). These are evaluated with 9 metrics, in the vanilla fully-observed setting and in the synthetically-induced 20% missing completely at random (MCAR) setting.

**320 321 322** Results for partially-missing data are shown in Table  $\overline{3}$ . UnmaskingTrees is first place on 5/9 metrics; head-to-head, UnmaskingTrees beats TabDDPM 5-4, and beats Forest-Flow 6-3. Results for fully-

<span id="page-5-1"></span><sup>&</sup>lt;sup>1</sup>We do not add TabMT [\(Gulati & Roysdon, 2024\)](#page-10-5) and TabPFGen (Ma et al.,  $2024$ ) to the benchmark because no code was provided. We do not add UnmaskingTabPFN because of out-of-memory errors on our machine.

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**325 326 327 328** Table 2: Averaged ranks from ablation study of tabular data imputation (27 datasets, 3 experiments per dataset, 10 imputations per experiment) with 20% missing. Shown are *averaged rank* over all datasets and experiments (standard-error). Overall best is **highlighted**; better of Forest-VP versus ours is **boldface blue**. See Table  $\frac{1}{1}$  for column meanings.

	MinMAE $\downarrow$	AvgMAE $\downarrow$	$W_{train}$	$W_{test} \downarrow$	$MAD \downarrow$	$R^2 \downarrow$	$F_1 \downarrow$	$P_{bias}$	$Cov_{rate} \downarrow$
<b>KNN</b>	6.8(0.6)	7.8(0.6)	6.0(0.4)	6.1(0.5)	10.4(0)	8.2(1.3)	7.0(1.5)	7.5(1.5)	6.5(0.8)
ICE	8.3(0.5)	5.8(0.5)	8.5(0.6)	8.8(0.5)	1.9(0.4)	8.0(1.1)	9.0(0.6)	7.2(1.1)	6.4(0.8)
<b>MICE-Forest</b>	4.8(0.6)	3.3(0.6)	3.5(0.3)	3.4(0.3)	4.6(0.4)	4.3(1.8)	4.3(1.3)	6.8(1.6)	4.8(0.7)
MissForest	3.3(0.7)	5.0(0.6)	2.2(0.4)	2.3(0.4)	7.2(0.3)	4.7(1.8)	3.3(0.9)	6.8(1.9)	3.8(0.6)
Softimpute	8.3(0.5)	9.3(0.5)	8.8(0.6)	8.9(0.6)	10.4(0)	7.5(1.2)	9.8(0.4)	8.3(0.9)	7.9(0.6)
<b>OT</b>	7.2(0.5)	7.6(0.4)	7.4(0.6)	7.4(0.6)	4.8(0.4)	8.2(0.5)	8.8(0.6)	7.3(0.7)	5.8(0.7)
GAIN	5.8(0.5)	8.3(0.4)	7.2(0.5)	7.5(0.4)	8.9(0.1)	7.5(0.8)	7.4(0.8)	6.7(1)	6.1(0.8)
Forest-VP	6.4(0.5)	4.8(0.6)	7.0(0.4)	6.1(0.5)	3.8(0.5)	6.5(0.9)	6.6(0.8)	4.5(0.8)	6.5(0.8)
UTrees-kMeans	6.0(0.6)	5.8(0.5)	6.3(0.6)	6.1(0.6)	4.1(0.3)	4.0(0.7)	2.9(0.6)	3.8(1)	6.0(0.7)
UTrees-KDI	5.1(0.5)	5.1(0.5)	5.4(0.6)	5.6(0.5)	4.8(0.3)	4.5(0.9)	4.0(0.5)	3.5(1.2)	6.4(0.7)
<b>UTrees</b>	3.8(0.5)	3.2(0.5)	3.8(0.4)	3.8(0.5)	5.0(0.3)	2.7(0.6)	2.9(0.8)	3.5(0.8)	5.8(0.7)

observed data are shown in Table  $\frac{1}{4}$ . UnmaskingTrees loses head-to-head to Forest-Flow, Forest-VP, and TabDDPM, but wins against the other methods.

<span id="page-6-2"></span>Table 3: Tabular data generation with incomplete data (27 datasets, 3 experiments per dataset, 20% missing values), MissForest is used to impute missing data except in Forest-VP, Forest-Flow, and UnmaskingTrees; *averaged rank* over all datasets and experiments (standard-error). Overall best is highlighted; better of Forest-VP versus Forest-Flow versus ours is **boldface blue**.

	$W_{train}$	$W_{test} \downarrow$	$cov_{train}$	$cov_{test}$		$R_{fake}^2 \downarrow F1_{fake} \downarrow$	$F1_{disc} \downarrow$	$P_{bias}$	$cov_{rate} \downarrow$
GaussianCopula	7.0(0.3)	7.1(0.2)	7.2(0.3)	7.1(0.3)	6.3(0.4)	6.6(0.3)	6.7(0.4)	5.5(1.0)	7.7(0.6)
<b>TVAE</b>	5.2(0.3)	4.9(0.3)	5.7(0.3)	5.8(0.2)	6.0(1.0)	5.8(0.5)	5.8(0.4)	8.0(0.4)	6.2(1.0)
<b>CTGAN</b>	8.3(0.2)	8.4(0.2)	8.4(0.2)	8.3(0.2)	8.3(0.3)	8.4(0.2)	6.5(0.2)	4.8(1.2)	7.1(0.7)
<b>CTABGAN</b>	6.7(0.4)	6.5(0.4)	7.1(0.3)	6.8(0.3)	7.3(0.6)	7.1(0.4)	6.6(0.3)	7.5(1.0)	6.1(0.6)
<b>Stasy</b>	5.9(0.2)	6.1(0.3)	5.3(0.2)	5.1(0.3)	5.8(0.9)	4.4(0.4)	5.3(0.4)	3.7(0.4)	4.6(1.1)
TabDDPM	3.0(0.7)	3.4(0.7)	2.3(0.5)	2.9(0.6)	1.7(0.3)	3.3(0.6)	3.9(0.6)	3.8(1.2)	2.0(0.5)
Forest-VP	3.7(0.2)	3.2(0.3)	3.9(0.2)	3.8(0.3)	3.2(0.3)	2.3(0.3)	4.2(0.4)	4.2(0.8)	4.5(1.1)
Forest-Flow	3.0(0.3)	2.6(0.3)	2.6(0.3)	2.7(0.2)	3.0(0.7)	3.7(0.3)	5.0(0.5)	3.8(0.9)	3.2(0.8)
<b>UTrees</b>	2.1(0.2)	2.8(0.3)	2.5(0.2)	2.5(0.2)	3.3(0.8)	3.5(0.5)	1.0(0.0)	3.7(0.9)	3.7(1.0)

<span id="page-6-3"></span>Table 4: Tabular data generation with complete data (27 datasets, 3 experiments per dataset); *averaged rank* over all datasets and experiments (standard-error). Overall best is **highlighted**; better of Forest-VP versus Forest-Flow versus ours is **boldface blue**.



Raw scores, per-dataset results, and runtimes are provided in the Appendix.

<span id="page-6-0"></span>3.3 EVALUATING BALTOBOT ON SYNTHETIC PROBABILISTIC PREDICTION CASE STUDIES

**369 370 371 372 373 374 375 376 377 Wave dataset** We compare our approach with Treeffuser (Beltran-Velez et al.,  $2024$ ) on the "wave" synthetic dataset from Treeffuser (Beltran-Velez et al.,  $2024$ ), which as shown in Figure  $\overline{3}$  is nonlinear, multimodal, and heteroskedastic. On the raw probabilistic predictions in Figure  $\overline{\beta}(A)$ , we see that BaltoBot and BaltoBoTabPFN are (by visual inspection) able to model the conditional distribution as well as Treeffuser. Yet this case study illustrates the two advantages of BaltoBot. First, in Figure [3\(](#page-7-1)B) we show the runtime of the different methods: training, sampling, and total. To train on 5000 samples, Treeffuser took 1.1s and BaltoBot took 2.6s. But to generate 5000 samples, Treeffuser took 5.0s while BaltoBot took 0.72s, for  $\sim$  7 $\times$  speedup. Second, BaltoBot offers the ability to estimate a closed-form probability density function (pdf) of the predictive distribution as shown in Figure  $\overline{3}(C)$ ; in contrast, Treeffuser can only sample from the predictive distribution.



<span id="page-7-1"></span>Figure 3: Comparison of Treeffuser and our approach on wave synthetic data with 5000 samples. (A) Probabilistic predictions for Treeffuser (top), BaltoBot (center), and BaltoBoTabPFN (bottom). (B) Runtime comparison for the different methods. (C) Estimated pdf from our methods at  $X = 2$ , depicted as the vertical dotted line in (A).

**Poisson-distributed count data** We generate 500 samples of  $X_i \sim \text{Unif}[0, 3], Y_i \sim \text{Poisson}(\lambda = \sqrt{X_i})$ , and show probabilistic predictions for Y in Figure  $|\mathbf{A}|$ . Whereas Treeffuser generates a spurious negative-valued outlier and many non-integer *Y* samples, our approach automatically models the count-type distribution of the data.



<span id="page-7-2"></span>Figure 4: Comparison of Treeffuser, BaltoBot, and BaltoBoTabPFN on Poisson-distributed data. The input variable is on the x-axis, while probabilistic predictions are shown on the y-axis.

#### <span id="page-7-0"></span>3.4 SALES FORECASTING WITH UNCERTAINTY

 We employ the M5 sales forecasting Kaggle dataset  $(Makridakis & Howard, 2020)$  to compare BaltoBot with other probabilistic prediction methods. The dataset has five years of sales data from ten Walmart stores, and the task requires predicting the (heavy-tailed) number of units sold given a product's attributes and previous sales. We use the exact same data preparation used for Treeffuser **[\(Beltran-Velez et al., 2024\)](#page-10-3)** experiments, which yields 1k products, 120k training samples, and 10k test samples. As in the Treeffuser evaluation [\(Beltran-Velez et al., 2024\)](#page-10-3), we evaluate probabilistic predictions with the continuous ranked probability score (CRPS), and evaluate the conditional mean predictions with the mean absolute error (MAE) and root mean-squared error (RMSE).



**433 434 435** Table 5: Sales forecasting evaluation on M5 dataset. We highlight the best 2 methods for each metric. The best of Treeffuser versus ours (with tuning) is **boldface blue**; the best of Treeffuser versus ours (without tuning) is boldface brown.

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**449 450 451 452 453 454 455** For full comparability, we follow the Treeffuser evaluation setup [\(Beltran-Velez et al., 2024\)](#page-10-3) and evaluate CRPS by generating 100 samples from our estimators' *p*(*y|*X) for each X in the testset; and for MAE and RMSE, we estimate the conditional means  $\mathbb{E}[y|\mathbf{X}]$  using 50 samples. For comparability, for this (and only this) dataset, we also evaluate BaltoBot with hyperparameter tuning, using the same setup used for all other methods (10 folds, each with 80%-20% train-validation split, and 25 Bayesian optimization iterations).  $\frac{2}{3}$  $\frac{2}{3}$  $\frac{2}{3}$  We also compare Treeffuser, BaltoBot, and BaltoBoTabPFN when run without hyperparameter tuning.

**456 457 458 459 460 461 462 463** We report results in Table  $\overline{5}$ . In addition to ours' and Treeffuser, we report results for Deep Ensembles [\(Lakshminarayanan et al., 2017\)](#page-11-13), IBUG [\(Brophy & Lowd, 2022\)](#page-10-11), NGBoost Poisson [\(Duan et al.,](#page-10-2) [2020\)](#page-10-2), and Quantile Regression Forests [\(Meinshausen & Ridgeway, 2006\)](#page-12-2). For methods other than our own, we report the metrics provided in Table 2 of  $\left(\text{Beltran-Velez et al.}\right)$  [2024]. Overall, our proposed methods outperform previous methods at combining excellent performance on both conditional distribution prediction and conditional mean prediction. Treeffuser and BaltoBot (both with tuning) tie for first-place according to CRPS, yet BaltoBot outperforms Treeffuser on RMSE and MAE. The winners on conditional mean metrics (RMSE and MAE) are Deep Ensembles and BaltoBoTabPFN, yet BaltoBoTabPFN (no tuning) strongly outperforms Deep Ensembles on CRPS.

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## 4 LIMITATIONS

While UnmaskingTrees is *overall* state-of-the-art on the tabular imputation benchmark, MissForest still outperformed on the metrics based on Wasserstein distance to train and test dataset distributions. And Forest-Flow still won on vanilla generation benchmark (without any missingness). It remains to be seen whether a single method can be developed which wins on all scenarios and metrics. While BaltoBoTabPFN performed well on probabilistic prediction tasks, when used as a subroutine in UnmaskingTabPFN, it is very slow and experienced out-of-memory errors on the [\(Jolicoeur-](#page-11-0)[Martineau et al., 2024b\)](#page-11-0) benchmark on our machine. Further improvements either to it, or to how it is employed, are needed to make it practical for all but the smallest datasets.

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## 5 DISCUSSION AND RELATED WORK

Diffusion modeling has recently gained popularity in tabular ML [\(Zheng & Charoenphakdee, 2022;](#page-12-15) [Jolicoeur-Martineau et al., 2024b;](#page-11-0) [Beltran-Velez et al., 2024;](#page-10-3) [Kotelnikov et al., 2023\)](#page-11-11). Our proposed approach is an instance of the autoregressive discrete diffusion framework (Hoogeboom et al.,  $[2021]$ ), instances of which have shown success in a variety of tasks  $\langle \text{Yang}, 2019 \rangle$  Austin et al.,  $\langle 2021 \rangle$  [Kitouni](#page-11-7) [et al., 2024;](#page-11-7) [Jolicoeur-Martineau et al., 2024a\)](#page-11-14). Yet our results call into question whether diffusion is beneficial for tabular conditional generation, or whether autoregression is sufficient for our setting.

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<span id="page-8-0"></span><sup>&</sup>lt;sup>2</sup>We optimize over the following XGBoost hyperparameter spaces: learning\_rate  $\in$  log-uniform $(0.05, 0.5)$ , max\_leaves  $\in$   $\{0, 25, 50\}$ , and subsample  $\in$  log-uniform $(0.3, 1)$ .

**486 487 488 489** It has been observed that diffusion is autoregression in frequency space, progressing from low frequencies to high frequencies, which makes it a good match for image data with its power law spectra (Rissanen et al.,  $2022$ ; Dieleman,  $2024$ ; Stewart,  $2024$ ). In tabular datasets without this phenomena, we would expect diffusion modeling to be less advantageous.

**490 491 492 493 494 495 496 497 498 499 500** Why is ForestDiffusion better at vanilla generative modeling, while UnmaskingTrees is better on missing data problems? We offer two speculative explanations. First, imputation is a conditional modeling scenario, except that you do not know the partition of the features into input features and output features *a priori*. One could address imputation by learning all possible  $2^D$  conditional distributions, but this is impractical for large *D*, so one would prefer to learn a single joint distribution. Both autoregression and diffusion are ways of learning a joint distribution; because autoregression does so by learning conditional distributions, it is more suited to the conditional modeling imputation setting. Second, for missing data, diffusion has a train-inference gap: during training, observed features begin the reverse process from  $\mathcal{N}(0, 1)$ ; during inference for imputation, observed features begin the reverse process at their actual values. On the other hand, the advantages of diffusion modeling give it superiority when these problems can be avoided.

**501 502 503 504 505 506 507** Despite their strong outperformance on other modalities, deep learning approaches have laboured against gradient-boosted decision trees on tabular data [\(Shwartz-Ziv & Armon, 2022;](#page-12-18) [Jolicoeur-](#page-11-0)[Martineau et al., 2024b\)](#page-11-0). Previous work [\(Breejen et al., 2024\)](#page-10-15) suggests that tabular data requires an inductive prior that favors sharpness rather than smoothness, showing that TabPFN [\(Hollmann](#page-10-4) et al.,  $2022$ ) (the leading deep learning tabular classification method) can be further improved with synthetic data generated from random forests. We anticipate that our XGBoost classifiers may be swapped out for a future variant of TabPFN that learns sharper boundaries and handles missingness.

**508 509 510 511 512 513 514 515** We also note that MissForest (Stekhoven & Bühlmann,  $[2012]$ , hailing from statistical literature on multiple imputation, has yet to be completely dethroned. Future progress in tabular conditional generation may require going back to the well of this traditional literature. As one example, we observe that MissForest exploits feature missingness fraction information, but we are not aware of any "machine learning" approaches which do so. The statistical literature has also previously explored the value of conditional modeling for joint modeling (Gelman & Raghunathan,  $[2001]$ , Liu et al.,  $[2014]$ ; [Kropko et al., 2014\)](#page-11-16). Indeed, our UnmaskingTrees approach, and all autoregressive modeling, is presaged by the full-mechanism bootstrap [\(Efron, 1994\)](#page-10-17).

**516 517 518 519 520 521 522 523 524** Finally, we observe where randomness enters into our generation process compared to previous work. Flow-matching [\(Liu et al., 2022;](#page-11-17) [Albergo & Vanden-Eijnden, 2022;](#page-10-18) [Lipman et al., 2022\)](#page-11-18) (used in Forest-Flow) injects randomness solely at the beginning of the reverse process via Gaussian sampling, whereas diffusion modeling (Sohl-Dickstein et al.,  $2015$ ; Song & Ermon,  $2019$ ) (used in Forest-VP) injects randomness both at the beginning and during the reverse process. In contrast, because our method starts with a fully-masked sample, it injects randomness gradually during the generation process. First, we randomly generate the order over features for unmasking. Second, we do not "greedily decode" to the most likely leaf in the meta-tree, but instead sample according to predicted probabilities. Third, for continuous features, having sampled a particular meta-tree leaf bin, we sample from within the bin, treating it as a uniform distribution.

6 CONCLUSIONS

We proposed tree-based autoregressive modeling of tabular data, especially for data with missingness. For the subproblem of conditional probabilistic prediction of individual variables, we presented a hierarchical partitioning method with benefits over vanilla quantization and diffusion-based probabilistic prediction. We then considered each of these as meta-algorithms that enable pure in-context learning-based modeling using TabPFN as base classifier. We showed SotA results for imputation and for generation given data with missingness, and on probabilistic prediction for sales forecasting.

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### 7 REPRODUCIBILITY STATEMENT

All our code is in an anonymized public Github repo. We evaluate on public real datasets, using experimental setups released by previous works; or on synthetic data, using scripts in our repo.

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